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System Initial Values:

- Sprung mass ($m_s = 300 \text{ kg}$) \rightarrow the vehicle body
- Unsprung mass ($m_u = 40 \text{ kg}$) \rightarrow wheel + axle
- Suspension spring ($k_s = 15,000 \text{ N/m}$)
- Suspension damper ($c_s = 1,000 \text{ Ns/m}$)
- Tire spring ($k_t = 200,000 \text{ N/m}$)
- Tire damping ($c_t = 50 \text{ Ns/m}$)
- Road input (a bump applied as a step of 1 cm)

The simulation runs for 5 seconds using an ODE45 solver.

Mathematical Model:

Body (sprung mass):

$$m_s \ddot{z}_s = -k_s(z_s - z_u) - c_s(\dot{z}_s - \dot{z}_u) + u$$

Wheel (unsprung mass):

$$m_u \ddot{z}_u = k_s(z_s - z_u) + c_s(\dot{z}_s - \dot{z}_u) - k_t(z_u - z_r) - c_t(\dot{z}_u - \dot{z}_r) - u$$

u is the Skyhook control force.

For passive suspension, $u = 0$.

Natural Frequencies (How the car vibrates):

| Mode | Frequency | Damping Ratio |
|------|-----------|---------------|
|------|-----------|---------------|

| | | |
|-----------------------|-----------------|--------------|
| Body mode | 1.09 Hz | 0.212 |
| Wheel-hop mode | 11.59 Hz | 0.183 |

These values are typical for cars:

- 1–2 Hz → felt by passengers (comfort zone)
- 10–12 Hz → wheel vibration (tire dynamic)

Skyhook Control

Skyhook control acts like a virtual damper connected to the sky:

$$u = -c_{sky}(z_s)'$$

It only damps the body motion, not the wheel.

This improves comfort without making the suspension too stiff.

Value used in my project is:

$c_{sky} = 2000$

Skyhook adds additional damping **only to the body**, improving comfort without increasing stiffness.

Comparison of results:

a) Comfort (Body Acceleration):

| Metric | Passive | Skyhook | Improvement |
|---------------------|----------------|----------------|--------------------|
| RMS (acc_s) | 0.289 | 0.262 | 9.2% better |
| Peak (acc_s) | 2.061 | 1.882 | improved |

b) Suspension Travel:

| Passive | Skyhook |
|----------------|----------------|
| 0.0134 m | 0.0135 m |

c) Settling Time:

| Passive | Skyhook |
|---------|---------|
| 1.021 s | 1.011 s |

Frequency-Domain Comparison:

Passive Suspension

- $GM = 7.85$
- $PM = 60.40^\circ$

Skyhook Suspension

- Gain Margin = 8.079 (18.15 dB)
- Phase Margin = 149.41°

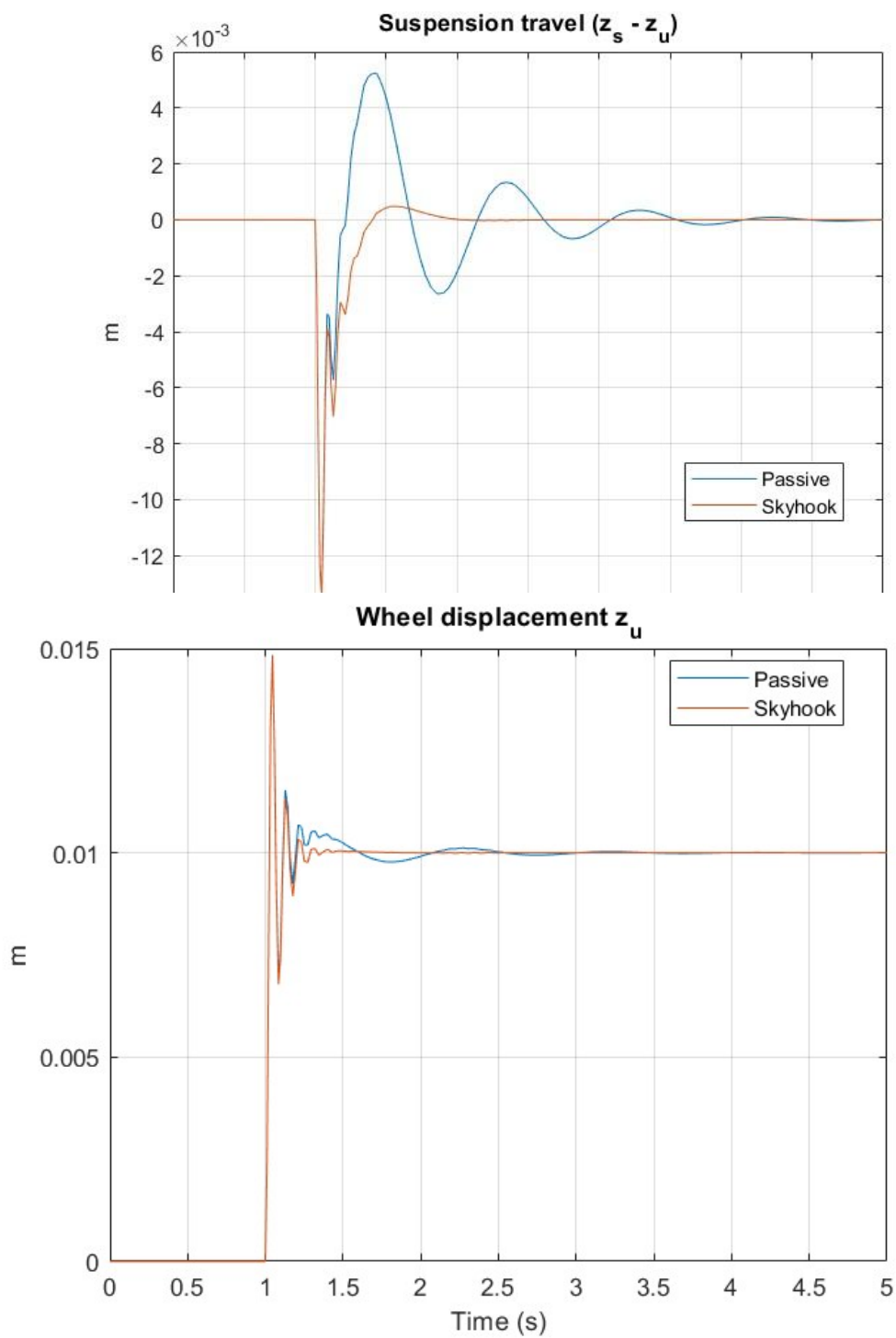
This huge increase in phase margin shows:

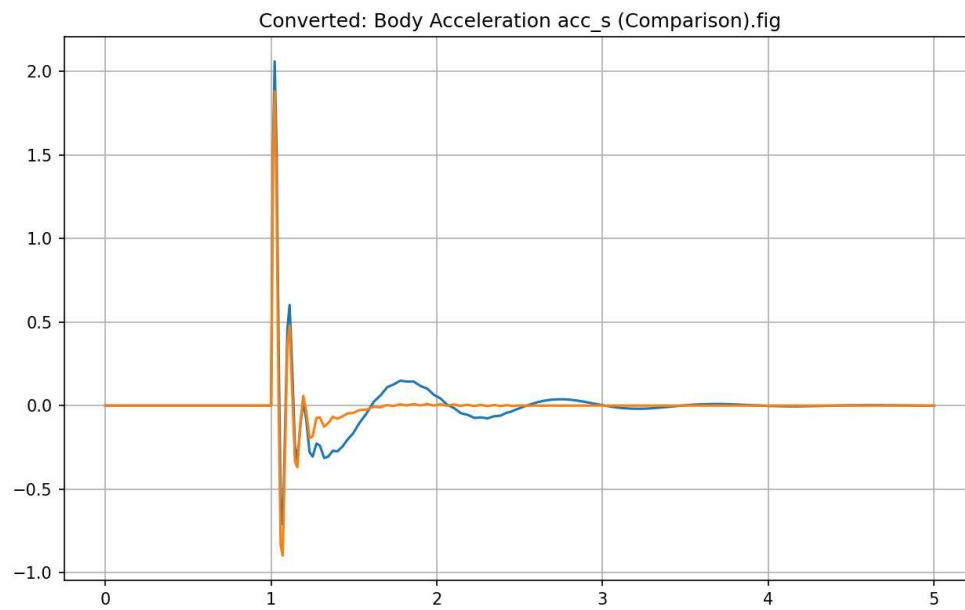
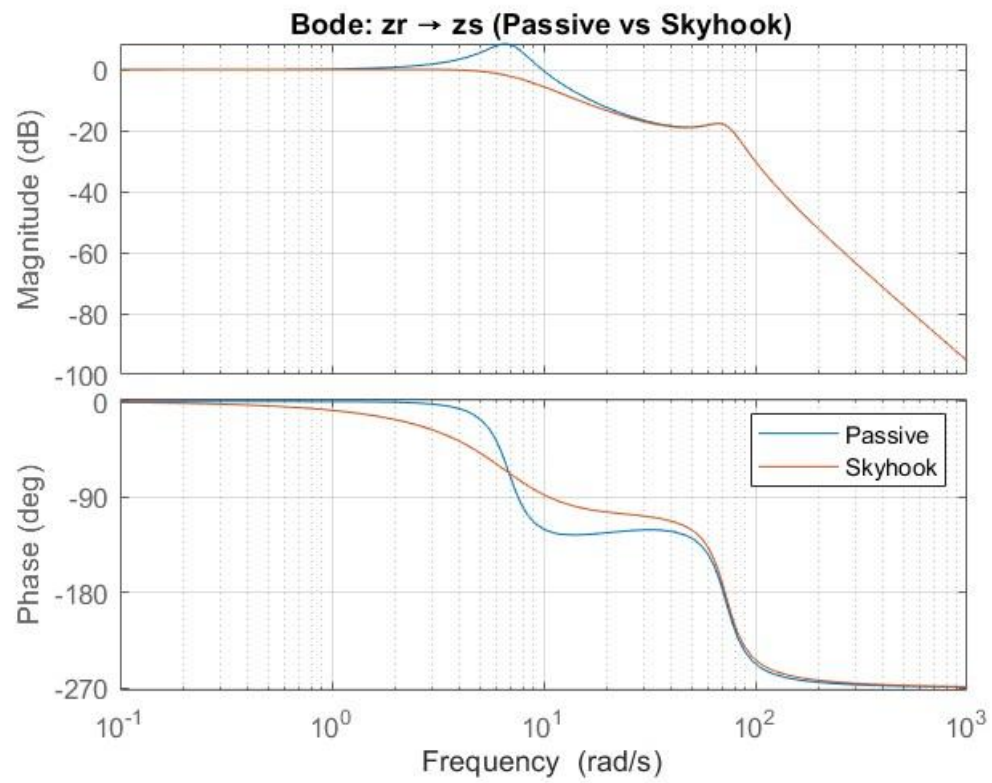
- Much higher stability
- More damping
- Increased robustness

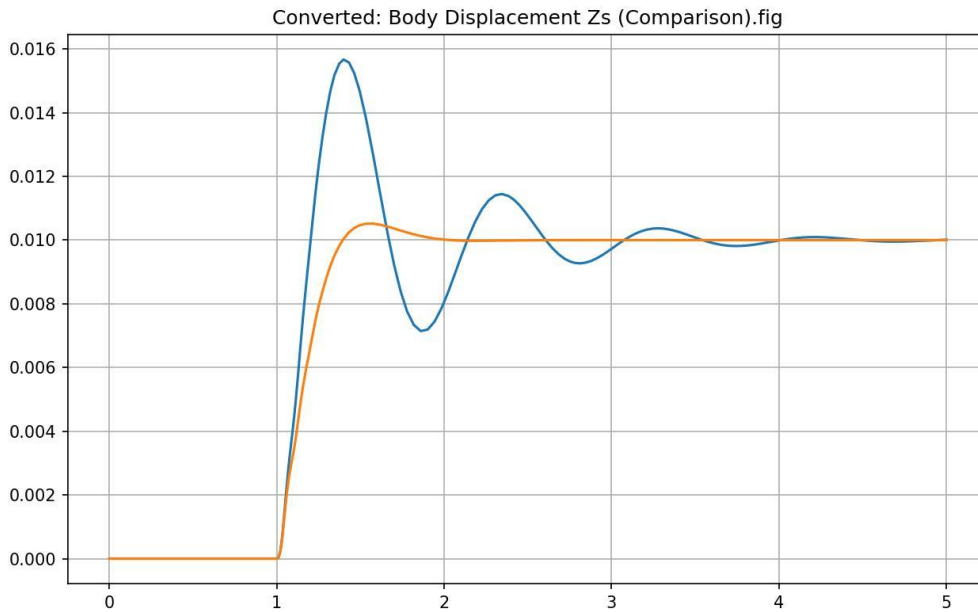
Modal Damping with Skyhook:

| Mode | Damping Ratio |
|----------------|------------------------------------|
| Body mode | 0.7048 (vs. 0.2124 passive) |
| Wheel-hop mode | unchanged |

Comparison Graphs:







Conclusion:

With a 1 cm road bump, the quarter-car suspension system behaves realistically.

Skyhook control clearly improves comfort by:

- Reducing RMS acceleration by 9.2%
- Lowering peak acceleration
- Increasing body-mode damping by more than 3×
- Increasing phase margin to 149°, showing excellent robustness
- Maintaining safe suspension travel

This confirms that Skyhook damping is an effective approach for enhancing ride comfort without compromising the vehicle's mechanical limits.