

2004 N1

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Let  $\tau(n)$  denote the number of positive divisors of the positive integer  $n$ . Prove that there exist infinitely many positive integers  $a$  such that the equation  $\tau(an) = n$  does not have a positive integer solution  $n$ .