

1)
a) α ?

$$5\alpha \sum_{x=1}^3 x + \alpha \sum_{x=4}^7 x^3 = 1$$

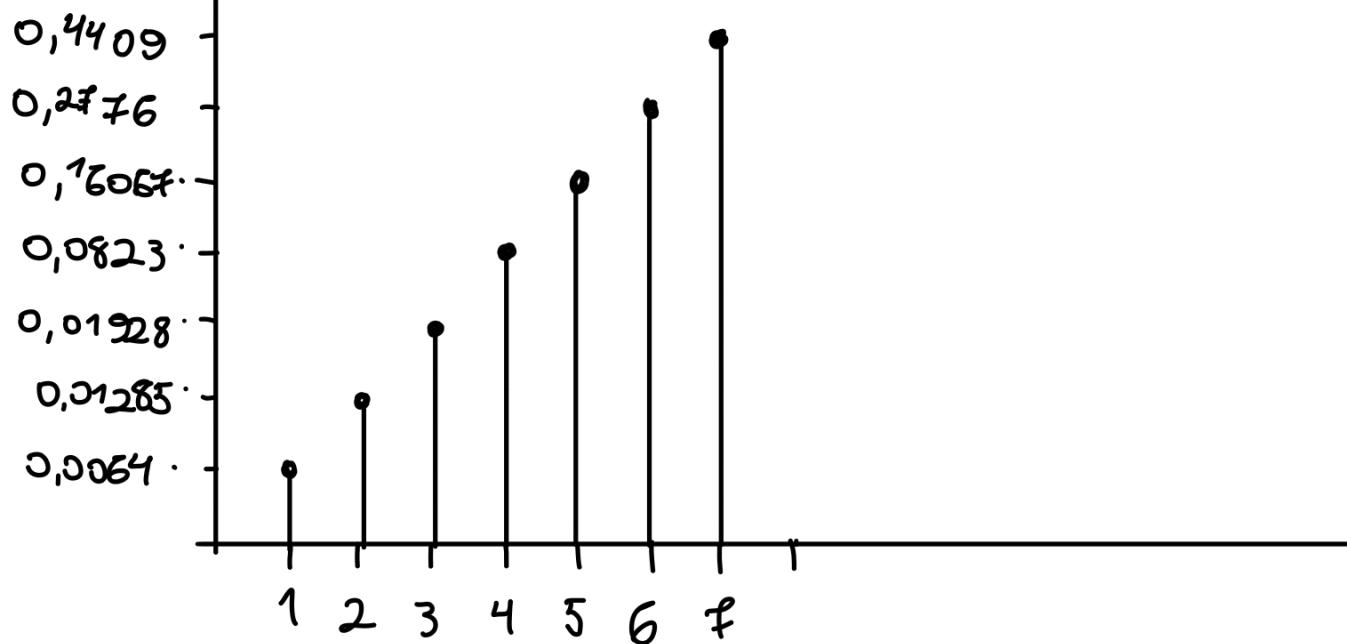
$$5\alpha(6) + \alpha(748) = 1$$
$$\alpha = \frac{1}{748}$$

b) $P(3 \leq x \leq 5)$

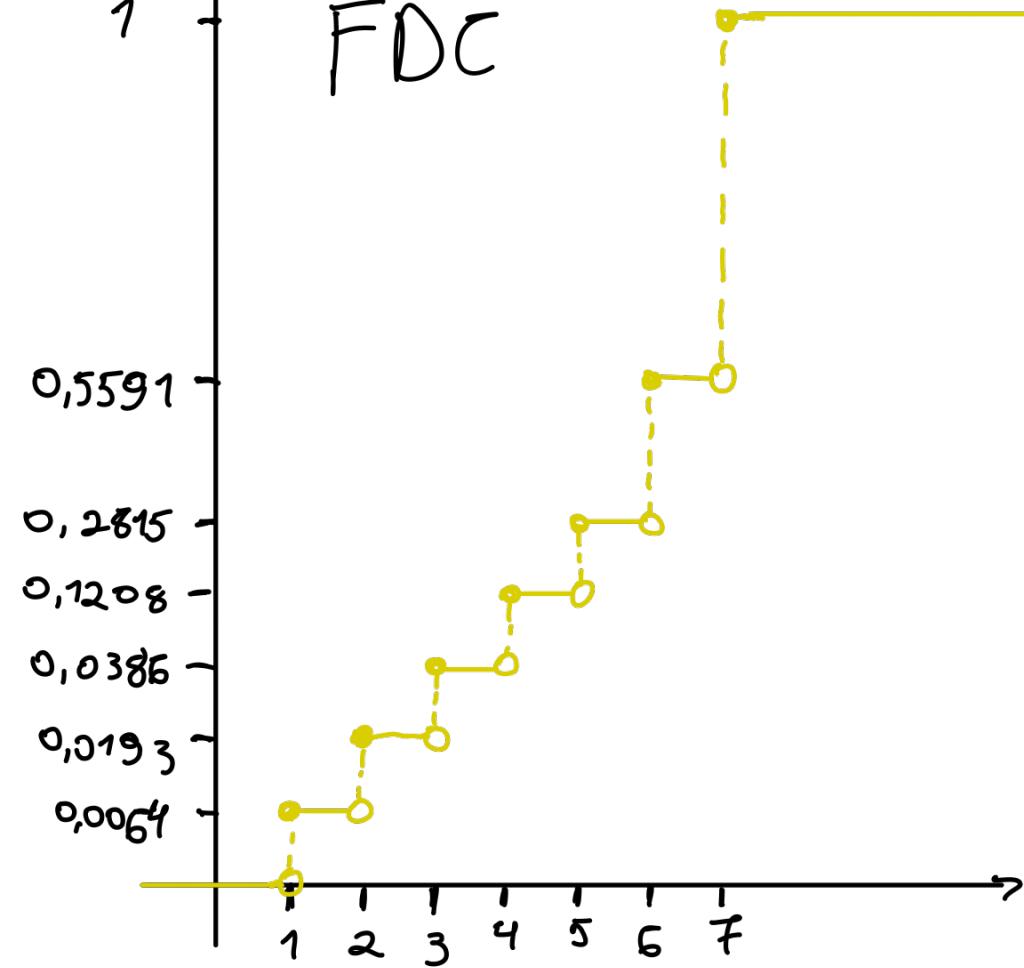
$$\frac{5}{748} \cdot 3 + \frac{1}{748} \cdot (4^3 + 5^3) = \frac{102}{389}$$

c)

FDP



FDC



2)

$$a) P(X \leq 1) = F_x(1) = 0,72$$

$$b) P(X \geq 2) = 1 - P(X < 2) = 1 - F_x(1) = 0,28$$

$$c) P(X = 1) = F_x(1) - F_x(0) = 0,31$$

3)

$$a) C \int_0^{10} x(10-x) dx = 1 \rightarrow C \cdot \frac{500}{3} = 1 \therefore C = \frac{3}{500}$$

$$b) P(X = 8) = \text{zero}$$

$$c) P(5 \leq X \leq 8)$$

$$\frac{3}{500} \int_5^8 x(10-x) dx = \frac{99}{250}$$

d) $f_x(x) \xrightarrow{\int dx} F_x(x)$

$$\frac{3}{500} \int_0^x x(10-x) dx = \frac{3}{500} \left[5x^2 - \frac{x^3}{3} \right]_{x=0}^x$$

$$F_x(x) = \begin{cases} 0, & x < 0 \\ \frac{3}{500} \cdot x^2 \left(5 - \frac{x}{3} \right), & 0 \leq x \leq 10 \\ 1, & x > 10 \end{cases}$$