Lists

- A list is a finite sequence of elements
- Examples of lists in Prolog:

```
[mia, vincent, jules, yolanda]
[mia, robber(honeybunny), X, 2, mia]
[]
[mia, [vincent, jules], [butch, friend(butch)]]
[[], dead(z), [2, [b,c]], [], Z, [2, [b,c]]]
```

Important things about lists

- List elements are enclosed in square brackets
- The length of a list is the number of elements it has
- All sorts of Prolog terms can be elements of a list
- There is a special list: the empty list []

Head and Tail

- A non-empty list can be thought of as consisting of two parts
 - The head
 - The tail
- The head is the first item in the list
- The tail is everything else
 - The tail is the list that remains when we take the first element away
 - The tail of a list is always a list

[mia, vincent, jules, yolanda]

Head:

Tail:

[mia, vincent, jules, yolanda]

Head: mia

Tail:

[mia, vincent, jules, yolanda]

Head: mia

Tail: [vincent, jules, yolanda]

[[], dead(z), [2, [b,c]], [], Z, [2, [b,c]]]

Head:

Tail:

• [[], dead(z), [2, [b,c]], [], Z, [2, [b,c]]]

Head: []

Tail:

[[], dead(z), [2, [b,c]], [], Z, [2, [b,c]]]

Head: []

Tail: [dead(z), [2, [b,c]], [], Z, [2, [b,c]]]

[dead(z)]

Head:

Tail:

[dead(z)]

Head: dead(z)

Tail:

[dead(z)]

Head: dead(z)

Tail: []

Head and tail of empty list

- The empty list has neither a head nor a tail
- For Prolog, [] is a special simple list without any internal structure

 The empty list plays an important role in recursive predicates for list processing in Prolog

- Prolog has a special built-in operator | which can be used to decompose a list into its head and tail
- The | operator is a key tool for writing Prolog list manipulation predicates

```
?- [Head|Tail] = [mia, vincent, jules, yolanda].

Head = mia

Tail = [vincent, jules, yolanda]

yes

?-
```

```
?- [X|Y] = [mia, vincent, jules, yolanda].
X = mia
Y = [vincent, jules, yolanda]
yes
?-
```

?- [X|Y] = [].

no

?-

```
?- [X,Y|Tail] = [[ ], dead(z), [2, [b,c]], [], Z, [2, [b,c]]] .

X = [ ]
Y = dead(z)
Z = _4543
Tail = [[2, [b,c]], [ ], Z, [2, [b,c]]]
yes
?-
```

Anonymous variable

 Suppose we are interested in the second and fourth element of a list

```
?- [X1,X2,X3,X4|Tail] = [mia, vincent, marsellus, jody, yolanda].
X1 = mia
X2 = vincent
X3 = marsellus
X4 = jody
Tail = [yolanda]
yes
?-
```

Anonymous variables

 There is a simpler way of obtaining only the information we want:

```
?- [_,X2,_,X4|_] = [mia, vincent, marsellus, jody, yolanda].

X2 = vincent

X4 = jody

yes

?-
```

The underscore is an anonymous variable

The anonymous variable

- Is used when you need to use a variable, but you are not interested in what Prolog instantiates it to
- Each occurrence of the anonymous variable is independent, i.e. can be bound to something different

Member

- One of the most basic things we would like to know is whether something is an element of a list or not
- So let's write a predicate that when given a term X and a list L, tells us whether or not X belongs to L
- This predicate is usually called member/2

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

?-

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

?- member(yolanda,[yolanda,trudy,vincent,jules]).

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

```
?- member(yolanda,[yolanda,trudy,vincent,jules]).
yes
?-
```

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

?- member(vincent,[yolanda,trudy,vincent,jules]).

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

```
?- member(vincent,[yolanda,trudy,vincent,jules]).
yes
?-
```

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

?- member(zed,[yolanda,trudy,vincent,jules]).

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

```
?- member(zed,[yolanda,trudy,vincent,jules]).
no
?-
```

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

?- member(X,[yolanda,trudy,vincent,jules]).

```
member(X,[X|T]).
member(X,[H|T]):- member(X,T).
```

```
?- member(X,[yolanda,trudy,vincent,jules]).
X = yolanda;
X = trudy;
X = vincent;
X = jules;
no
```

Rewriting member/2

```
member(X,[X|\_]). member(X,[\_|T]):-member(X,T).
```

Recursing down lists

- The member/2 predicate works by recursively working its way down a list
 - doing something to the head, and then
 - recursively doing the same thing to the tail
- This technique is very common in Prolog and therefore very important that you master it
- So let's look at another example!

Example: a2b/2

- The predicate a2b/2 takes two lists as arguments and succeeds
 - if the first argument is a list of as, and
 - the second argument is a list of bs of exactly the same length

```
?- a2b([a,a,a,a],[b,b,b]).

yes
?- a2b([a,a,a,a],[b,b,b]).

no
?- a2b([a,c,a,a],[b,b,b,t]).

no
```

Defining a2b/2: step 1

a2b([],[]).

- Often the best away to solve such problems is to think about the simplest possible case
- Here it means: the empty list

Defining a2b/2: step 2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

- Now think recursively!
- When should a2b/2 decide that two non-empty lists are a list of as and a list of bs of exactly the same length?

Testing a2b/2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

```
?- a2b([a,a,a],[b,b,b]).

yes
?-
```

Testing a2b/2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

```
?- a2b([a,a,a,a],[b,b,b]).
no
?-
```

Testing a2b/2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

```
?- a2b([a,t,a,a],[b,b,b,c]).
no
?-
```

Further investigating a2b/2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

```
?- a2b([a,a,a,a,a], X).
X = [b,b,b,b,b]
yes
?-
```

Further investigating a2b/2

```
a2b([],[]).
a2b([a|L1],[b|L2]):- a2b(L1,L2).
```

```
?- a2b(X,[b,b,b,b,b,b]).
X = [a,a,a,a,a,a]
yes
?-
```

List summary

- We introduced list and recursive predicates that work on lists
- The kind of programming that these predicates illustrated is fundamental to Prolog
- You will see that most Predicates you will write in your Prolog career will be variants of these predicates

Append

- We will define an important predicate append/3 whose arguments are all lists
- Declaratively, append(L1,L2,L3) is true if list L3 is the result of concatenating the lists L1 and L2 together

```
?- append([a,b,c,d],[3,4,5],[a,b,c,d,3,4,5]).
yes
?- append([a,b,c],[3,4,5],[a,b,c,d,3,4,5]).
no
```

Append viewed procedurally

- From a procedural perspective, the most obvious use of append/3 is to concatenate two lists together
- We can do this simply by using a variable as third argument

```
?- append([a,b,c,d],[1,2,3,4,5], X).
X=[a,b,c,d,1,2,3,4,5]
yes
```

?_

Definition of append/3

append([], L, L).

append([H|L1], L2, [H|L3]):
append(L1, L2, L3).

Recursive definition

- Base clause: appending the empty list to any list produces that same list
- The recursive step says that when concatenating a non-empty list [H|T] with a list L, the result is a list with head H and the result of concatenating T and L

How append/3 works

- Two ways to find out:
 - Use trace/0 on some examples
 - Draw a search tree!
 Let us consider a simple example

?- append([a,b,c],[1,2,3], R).

?- append([a,b,c],[1,2,3], R).

append([], L, L). append([H|L1], L2, [H|L3]):append(L1, L2, L3).

```
?- append([a,b,c],[1,2,3], R). /
```

```
append([], L, L).
append([H|L1], L2, [H|L3]):-
append(L1, L2, L3).
```

```
append([], L, L).
append([H|L1], L2, [H|L3]):-
append(L1, L2, L3).
```

```
append([], L, L).
append([H|L1], L2, [H|L3]):-
append(L1, L2, L3).
```

```
append([], L, L).
?- append([a,b,c],[1,2,3], R).
                                          append([H|L1], L2, [H|L3]):-
                                              append(L1, L2, L3).
             R = [a|L0]
            ?- append([b,c],[1,2,3],L0)
                            L0=[b|L1]
                            ?- append([c],[1,2,3],L1)
                                        L1=[c|L2]
                                       ?- append([],[1,2,3],L2)
```

```
append([], L, L).
?- append([a,b,c],[1,2,3], R).
                                          append([H|L1], L2, [H|L3]):-
                                              append(L1, L2, L3).
             R = [a|L0]
            ?- append([b,c],[1,2,3],L0)
                            L0=[b|L1]
                            ?- append([c],[1,2,3],L1)
                                        L1=[c|L2]
                                       ?- append([],[1,2,3],L2)
```

```
append([], L, L).
?- append([a,b,c],[1,2,3], R).
                                          append([H|L1], L2, [H|L3]):-
                                              append(L1, L2, L3).
             R = [a|L0]
            ?- append([b,c],[1,2,3],L0)
                            L0=[b|L1]
                            ?- append([c],[1,2,3],L1)
                                        L1=[c|L2]
                                       ?- append([],[1,2,3],L2)
                                     L2=[1,2,3]
```

```
append([], L, L).
?- append([a,b,c],[1,2,3], R).
                                          append([H|L1], L2, [H|L3]):-
                                              append(L1, L2, L3).
             R = [a|L0]
            ?- append([b,c],[1,2,3],L0)
                             L0=[b|L1]
                            ?- append([c],[1,2,3],L1)
L2=[1,2,3]
                                        L1=[c|L2]
L1=[c|L2]=[c,1,2,3]
                                       ?- append([],[1,2,3],L2)
L0=[b|L1]=[b,c,1,2,3]
R=[a|L0]=[a,b,c,1,2,3]
                                     L2=[1,2,3]
```

Using append/3

- Now that we understand how append/3 works, let's look at some applications
- Splitting up a list:

```
?- append(X,Y, [a,b,c,d]).

X=[ ] Y=[a,b,c,d];

X=[a] Y=[b,c,d];

X=[a,b] Y=[c,d];

X=[a,b,c] Y=[d];

X=[a,b,c,d] Y=[ ];

no
```

Prefix and suffix

- We can also use append/3 to define other useful predicates
- A nice example is finding prefixes and suffixes of a list

Definition of prefix/2

```
prefix(P,L):-
append(P,_,L).
```

- A list P is a prefix of some list L when there is some list such that L is the result of concatenating P with that list.
- We use the anonymous variable because we don't care what that list is.

Use of prefix/2

```
prefix(P,L):-
append(P,_,L).
```

```
?- prefix(X, [a,b,c,d]).

X=[ ];

X=[a];

X=[a,b];

X=[a,b,c];

X=[a,b,c,d];

no
```

Definition of suffix/2

```
suffix(S,L):-
append(_,S,L).
```

- A list S is a suffix of some list L when there is some list such that L is the result of concatenating that list with S.
- Once again, we use the anonymous variable because we don't care what that list is.

Use of suffix/2

```
suffix(S,L):-
append(_,S,L).
```

```
?- suffix(X, [a,b,c,d]).
X=[a,b,c,d];
X=[b,c,d];
X=[c,d];
X=[d];
X=[j;
no
```

Definition of sublist/2

- Now it is very easy to write a predicate that finds sub-lists of lists
- The sub-lists of a list L are simply the prefixes of suffixes of L

```
sublist(Sub,List):-
suffix(Suffix,List),
prefix(Sub,Suffix).
```

append/3 and efficiency

- The append/3 predicate is useful, and it is important to know how to to use it
- It is of equal importance to know that append/3 can be source of inefficiency
- Why?
 - Concatenating a list is not done in a simple action
 - But by traversing down one of the lists

Reversing a List

- We will illustrate the problem with append/3 by using it to reverse the elements of a list
- That is we will define a predicate that changes a list [a,b,c,d,e] into a list [e,d,c,b,a]
- This would be a useful tool to have, as Prolog only allows easy access to the front of the list

Naïve reverse

- Recursive definition
 - 1. If we reverse the empty list, we obtain the empty list
 - 2. If we reverse the list [H|T], we end up with the list obtained by reversing T and concatenating it with [H]
- To see that this definition is correct, consider the list [a,b,c,d].
 - If we reverse the tail of this list we get [d,c,b].
 - Concatenating this with [a] yields [d,c,b,a]

Naïve reverse in Prolog

```
naiveReverse([],[]).
naiveReverse([H|T],R):-
naiveReverse(T,RT),
append(RT,[H],R).
```

- This definition is correct, but it does an awful lot of work
- It spends a lot of time carrying out appends
- But there is a better way...

Reverse using an accumulator

- The better way is using an accumulator
- The accumulator will be a list, and when we start reversing it will be empty
- We simply take the head of the list that we want to reverse and add it to the the head of the accumulator list
- We continue this until we hit the empty list
- At this point the accumulator will contain the reversed list!

Reverse using an accumulator

accReverse([],L,L).
accReverse([H|T],Acc,Rev):accReverse(T,[H|Acc],Rev).

Adding a wrapper predicate

```
accReverse([],L,L).
accReverse([H|T],Acc,Rev):-
accReverse(T,[H|Acc],Rev).
```

```
reverse(L1,L2):-
accReverse(L1,[],L2).
```

Illustration of the accumulator

List: [a,b,c,d] Accumulator: []

Illustration of the accumulator

List: [a,b,c,d] Accumulator: []

• List: [b,c,d] Accumulator: [a]

Illustration of the accumulator

List: [a,b,c,d] Accumulator: []

• List: [c,d] Accumulator: [b,a]

Illustration of the accumulator

- List: [a,b,c,d] Accumulator: []
- List: [c,d] Accumulator: [b,a]
- List: [d] Accumulator: [c,b,a]

Illustration of the accumulator

- List: [a,b,c,d] Accumulator: []
- List: [b,c,d] Accumulator: [a]
- List: [c,d] Accumulator: [b,a]
- List: [d] Accumulator: [c,b,a]
- List: [] Accumulator: [d,c,b,a]

A few other things ...

Comparing Integers

Arithmetic

x > y

x < y $x \le y$ x = y $x \ne y$ $x \ge y$

Prolog

Comparison Operators

- Have the obvious meaning
- Force both left and right hand argument to be evaluated

```
?- 2 < 4+1.
yes
?- 4+3 > 5+5.
no
```

Comparison Operators

- Have the obvious meaning
- Force both left and right hand argument to be evaluated

```
?- 4 = 4.
yes
?- 2+2 = 4.
no
?- 2+2 =:= 4.
yes
```

Similar looking symbols

= The unification predicate.

Succeeds if it can unify its arguments, fails otherwise.

\= The negation of the unification predicate. Succeeds if = fails, and vice-versa.

== The identity predicate.

Succeeds if its arguments are identical, fails

Negation as Failure

- The cut operator (!) suppresses backtracking.
 - The fail predicate always fails.
- They can be combined to get <u>negation</u>
 <u>as failure</u> as follows:

neg(Goal):- Goal, !, fail. neg(Goal).

Vincent and burgers

```
enjoys(vincent,X):- burger(X),
neg(bigKahunaBurger(X)).
```

burger(X):- bigMac(X).
burger(X):- bigKahunaBurger(X).
burger(X):- whopper(X).

bigMac(a).
bigKahunaBurger(b).
bigMac(c).
whopper(d).

Vincent and burgers

```
enjoys(vincent,X):- burger(X),
neg(bigKahunaBurger(X)).
```

burger(X):- bigMac(X).
burger(X):- bigKahunaBurger(X).
burger(X):- whopper(X).

bigMac(a).
bigKahunaBurger(b).
bigMac(c).
whopper(d).

?- enjoys(vincent,X).
X=a
X=c

X=d

Another built-in predicate: \+

- Because negation as failure is so often used, there is no need to define it.
- In standard Prolog the prefix operator \+ means negation as failure
- We can define Vincent's preferences as follows:

enjoys(vincent,X):- burger(X), \+ bigKahunaBurger(X). ?- enjoys(vincent,X).

X=a

X=c

X=d

Negation as failure and logic

- Negation as failure is not logical negation
- Changing the order of the goals in the vincent and burgers program gives a different behaviour:

enjoys(vincent,X):- \+ bigKahunaBurger(X), burger(X).

?- enjoys(vincent,X).

Complete negation example

```
enjoys(vincent,X):- burger(X),
              \+ bigKahunaBurger(X).
    burger(X):- bigMac(X).
burger(X):- bigKahunaBurger(X).
    burger(X):- whopper(X).
           bigMac(a).
      bigKahunaBurger(b).
           bigMac(c).
          whopper(d).
```

```
?- enjoys(vincent,X).

X=a;

X=c;

X=d;

no
```

Miscellaneous Examples and Applications

Quick sort in Prolog

```
partition([], Pivot, [], []).
partition([H|T], Pivot, [H|Left], Right) :- H =< Pivot,
                        partition(T, Pivot, Left, Right).
partition([H|T], Pivot, Left, [H|Right]) :- H > Pivot,
                        partition(T, Pivot, Left, Right).
quicksort([], []).
quicksort([P|T], Sorted) :- partition(T, P, Left, Right),
                  quicksort(Left, SortedLeft),
                  quicksort(Right, SortedRight),
                  append(SortedLeft, [P|SortedRight], Sorted).
```

Complex queries and Expert systems

```
person(ann).
person(bob).
personSkill(ann, software).
personSkill(bob, software).
personSkill(bob, floating).
job(lifeguard).
job(developer).
jobSkill(lifeguard, firstaid).
jobSkill(lifeguard, swimming).
hasSkills(P, Skills):- person(P), findall(S, personSkill(P,S), Skills).
needsSkills(J, Skills):- job(J), findall(S, jobSkill(J,S), Skills).
fit for job(P, J):- hasSkills(P, SkillsHas),
            needsSkills(J, SkillsNeeded),
            forall(member(S, SkillsNeeded), member(S, SkillsHas)).
```

Natural language processing

- See:
 - Parsing and difference lists
 - Eliza chatbot
- IBM Watson:
 - Unstructured Information Management Architecture framework running on Hadoop

"We required a language in which we could conveniently express pattern matching rules over the parse trees and other annotations (such as named entity recognition results), and a technology that could execute these rules very efficiently. We found that Prolog was the ideal choice for the language due to its simplicity and expressiveness." -- Watson development team