# 1 Abstract Syntax

This section explains abstract syntax of  $IR_{ES}$ .

```
n \in FloatingPoint
                                       \in Integer
                                   d
                                       \in String
                                       \in Boolean
                                       \in Reference
                                       \in Identifier
                                       \in Type
  Program p ::= i; \dots; i
Instruction i ::= e
                                                      (expression)
                         \mathtt{let}\ x = e
                                                      (let)
                                                      (assign)
                         r := e
                         \mathtt{delete}\ r
                                                      (delete)
                         \mathtt{append}\ e\ \to\ e
                                                      (append)
                         \mathtt{prepend}\; e \; \to \; e
                                                      (prepend)
                                                      (return)
                         \mathtt{return}\ e
                         \mathtt{if}\ e\ i\ i
                                                      (if-then-else)
                         while e\ i
                                                      (while)
                         \{i^*\}
                                                      (sequence)
                                                      (assert)
                         \mathtt{assert}\ e
                         \mathtt{print}\; e
                                                      (print)
                         \mathsf{app}\ x = (e\ e^*)
                                                      (function application)
                         access x = (e e)
                                                      (access)
                         withcont x(x^*) = i
                                                     (continuation)
 Reference r ::= x
                                                      (identifier)
                                                      (reference to value of field in heap)
                      |r[e]
```

```
Expression e ::= n
                                                                   (number)
                                                                   (integer)
                          d
                          s
                                                                   (string)
                                                                   (boolean)
                          b
                                                                   (reference)
                          undefined
                                                                   (undefined)
                          null
                                                                   (null)
                          absent
                                                                   (absent)
                          \mathtt{new}\;e
                                                                   (symbol)
                          \mathtt{new}\ [e^*]
                                                                   (list)
                          \texttt{new}\ t\ (e\ \mapsto\ e,\ \cdots,\ e\ \mapsto\ e)
                                                                   (map)
                                                                   (pop)
                          pop e e
                          {\tt typeof}\ e
                                                                   (typeof)
                          \verb|is-instance-of| e s
                                                                   (is-instance-of)
                          {\tt get-elems}\;e\;s
                                                                   (get-elements)
                                                                   (get-syntax)
                          \verb"get-syntax" e
                          parse-syntax e \ e \ e^*
                                                                   (parse-syntax)
                          \mathtt{convert}\; e \; \triangleright \; e^*
                                                                   (convert)
                          \verb|contains|| e e
                                                                   (contains)
                          \operatorname{copy-obj} e
                                                                   (copy-object)
                          \verb|map-keys|| e
                                                                   (map-keys)
                          ! ! ! s
                                                                   (not supported)
                                                                   (unary operation)
                          \odot e
                                                                   (binary operation)
                          e \oplus e
                          (x^*) \ [\Rightarrow] \ i
                                                                   (continuation)
```

```
UnaryOperator \odot ::= -
                                        (negation)
                                        (boolean not)
                                        (bitwise not)
 {\bf Binary Operator} \ \oplus \ ::=
                                        (addition)
                                        (subtraction)
                                        (multiplication)
                                        (power)
                                        (division)
                                        (modulo)
                             %
                                        (modulo)
                                        (equals)
                                        (boolean and)
                             &&
                             \prod
                                        (boolean or)
                                        (boolean xor)
                                        (bitwise and)
                             &
                             (bitwise or)
                                        (bitwise xor)
                             <<
                                        (shift left)
                             <
                                        (less-then)
                                        (unsigned shift right)
                             >>>
                             >>
                                        (shift right)
ConvertOperator \triangleright ::=
                                        (string to number)
                             str2num
                             num2str
                                        (number to string)
                             num2int (number to integer)
```

# 2 Operational Semantic

This section explains operational semantic of IR<sub>ES</sub>.

#### 2.1 Domain

Semantic domain of IR<sub>ES</sub>.

```
State
                                    \in Context \times ContextStack \times Global \times Heap
                   Context
                               \Delta \in Identifier \times String \times Instruction^* \times Environment
             ContextStack \sqcup \in Context^*
                     Global \mathbb{G} \in Identifier \rightarrow Value
             Environment
                               \sigma \in Identifier \rightarrow Value
                       Heap
                               \Sigma \in Address \rightarrow Object
                      Value
                               v \in Value
                                a \in Address
                    Address
                     Object
                                o \in Object
              c ::= n \mid d \mid s \mid b \mid \mathtt{undefined} \mid \mathtt{null} \mid \mathtt{absent}
Constant
 Address
                                                                            (named address)
              a ::= s
                   \mid d
                                                                            (dynamic address)
  Object
              o ::= \operatorname{symbol} v
                                                                            (symbol)
                     | \quad \texttt{map} \ t \ (v \ \mapsto \ v, \ \cdots, \ v \ \mapsto \ v)
                                                                            (map)
                                                                            (list)
                                                                            (not supported)
    Value v ::= a
                                                                            (address)
                                                                            (constant)
                     | s(x^*, [x]) \Rightarrow i
                                                                            (function)
                     | \quad \Delta, \ \sqcup, \ x^* \ [ \ \Rightarrow \ ] \ i
                                                                            (continuation)
                     ASTVal?
                                                                            (AST value)
                        ASTMethod?
                                                                            (AST method)
RefValue rv ::= x
                                                                            (identifier)
                                                                            (reference to value of map in heap)
                     |a[v]
                                                                            (reference to ???)
                     | s.v
```

# 2.1.1 Global, Environment, Heap Description

```
[[description of initial configuration of IR<sub>ES</sub>]] Heap = (Base + Built-in) \rightarrow named addr + Dynamic \rightarrow dynamic addr [[description of operators used in state, context, heap]]
```

# 2.2 Semantic of $IR_{ES}$

• program : [[description of program execution]]

• instruction :  $\delta \vdash i \Rightarrow \delta$ 

• expression :  $\delta \vdash e \Rightarrow v, \ \delta$ 

• expression - escape completion :  $\delta \vdash_{escape} e \Rightarrow v, \ \delta$ 

• reference :  $\delta \vdash r \Rightarrow rv$ ,  $\delta$ 

• reference value :  $\delta \vdash rv \Rightarrow v$ ,  $\delta$ 

• unary operator :  $\odot v \Rightarrow v$ 

• binary operator :  $v \oplus v \Rightarrow v$ 

[[description of semantic relation]]

[[description of escape completion]]: result of abstract algorithm in ECMAScript is represented by completion record. "Escape completion" means "use value of completion record( $IR_{ES}$  object), instead of record itself".

# 2.2.1 State Helper Function

[[description of state function]]

## 2.2.2 Instruction

$$\frac{\delta \vdash e \Rightarrow v, \ \delta_0}{\delta \vdash e \Rightarrow \delta_0} \qquad \frac{\delta \vdash e \Rightarrow v, \ \delta_0}{\delta \vdash \text{let } x = e \Rightarrow \delta_1}$$
 
$$\frac{\delta \vdash r \Rightarrow x, \ \delta_0 \quad \delta_0 \vdash e \Rightarrow v, \ \delta_1 \quad \text{updated}(\delta_1, \ x, \ v) = \delta_2}{\delta \vdash r := e \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash r \Rightarrow a[v], \ \delta_0 \quad \delta_0 \vdash_{escape} e \Rightarrow v_0, \ \delta_1 \quad \text{updated}(\delta_1, \ a[v], \ v_0) = \delta_2}{\delta \vdash r := e \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash r \Rightarrow a[v], \ \delta_0 \quad \delta_0 \vdash_{escape} e \Rightarrow v_0, \ \delta_1 \quad \text{updated}(\delta_1, \ a[v], \ v_0) = \delta_2}{\delta \vdash r := e \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash r \Rightarrow s.v, \ \delta_0 \quad \delta_0 \vdash_{escape} e \Rightarrow v_0, \ \delta_1 \quad \text{updated}(\delta_1, \ s.v, \ v_0) = \delta_2}{\delta \vdash r := e \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash r \Rightarrow r.v, \ \delta_0 \quad \text{deleted}(\delta_0, \ rv) = \delta_1}{\delta \vdash \text{delete} \ r \Rightarrow \delta_1}$$
 
$$\frac{\delta \vdash_{escape} e_0 \Rightarrow v_0, \ \delta_0 \quad \delta_0 \vdash_{escape} e_1 \Rightarrow v_1, \ \delta_1 \quad \text{append}(\delta_0??, \ v_1, \ v_0) = \delta_2}{\delta \vdash \text{prepend} \ e_0 \Rightarrow e_1 \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash_{escape} e_0 \Rightarrow v_0, \ \delta_0 \quad \delta_0 \vdash_{escape} e_1 \Rightarrow v_1, \ \delta_1 \quad \text{prepend}(\delta_0??, \ v_1, \ v_0) = \delta_2}{\delta \vdash \text{prepend} \ e_0 \Rightarrow e_1 \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash_{escape} e_0 \Rightarrow v_0, \ \delta_0 \quad \delta_0 \vdash_{escape} e_1 \Rightarrow v_1, \ \delta_1 \quad \text{prepend}(\delta_0??, \ v_1, \ v_0) = \delta_2}{\delta \vdash \text{prepend} \ e_0 \Rightarrow e_1 \Rightarrow \delta_2}$$
 
$$\frac{\delta \vdash_{escape} e_0 \Rightarrow v_0, \ \delta_0 \quad \text{updateCtxStack}(\delta_0, \ v) = \delta_1}{\delta \vdash \text{return} \ e \Rightarrow \delta_1}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{true}, \ \delta_0 \quad \text{updateCtx}(\delta_0, \ i_0) = \delta_1}{\delta \vdash \text{if} \ e \ i_0 \ i_1 \Rightarrow \delta_1}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{false}, \ \delta_0 \quad \text{updateCtx}(\delta_0, \ i_1) = \delta_1}{\delta \vdash \text{while} \ e \ i \Rightarrow \delta_0}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{false}, \ \delta_0}{\delta \vdash \text{while} \ e \ i \Rightarrow \delta_0}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{false}, \ \delta_0}{\delta \vdash \text{while} \ e \ i \Rightarrow \delta_0}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{false}, \ \delta_0}{\delta \vdash \text{while} \ e \ i \Rightarrow \delta_0}$$
 
$$\frac{\delta \vdash_{escape} e \Rightarrow \text{false}, \ \delta_0}{\delta \vdash \text{while} \ e \ i \Rightarrow \delta_0}$$

$$\frac{\Delta = \mathtt{getCtx}(\delta) \quad \sqcup = \mathtt{getCtxStack}(\delta) \quad v_c = \Delta, \ \sqcup, \ x^* \ [ \Rightarrow ] \ i \quad \mathtt{define}(\delta, \ x_{id}, \ v_c) = \delta_0}{\delta \vdash \mathtt{withcont} \ x_{id} \ (x^*) = i \Rightarrow \delta_0}$$

$$\frac{\delta \vdash e_f \Rightarrow v, \ \delta_0}{\delta \vdash \mathsf{app} \ x = (e_f \ e^*) \Rightarrow \delta_0}$$

$$\frac{\delta \vdash e_f \Rightarrow v_f, \ \delta_f \qquad v_f = \Delta, \ \sqcup, \ x^* \ [\Rightarrow] \ i}{\delta_f \vdash e_0 \Rightarrow v_0, \ \delta_0 \qquad \cdots \qquad \delta_{n-1} \vdash e_n \Rightarrow v_n, \ \delta_n} \\ \underline{\text{setCtxInst}(\Delta, \ i) = \Delta_0 \qquad \text{updateCtxEnv}(\Delta_0, \ x^*, \ v^*) = \Delta_1 \qquad \text{updateState}(\delta_n, \ \Delta_1, \ \sqcup) = \delta_{next}}} \\ \delta \vdash \text{app } x = (e_f \ e^*) \Rightarrow \delta_{next}$$

## TODO

function application - method access

#### 2.2.3 Expression

$$\boxed{\delta \vdash e \Rightarrow v, \ \delta} \qquad \delta \vdash n \Rightarrow n, \ \delta \qquad \delta \vdash d \Rightarrow d, \ \delta \qquad \delta \vdash s \Rightarrow s, \ \delta \qquad \delta \vdash b \Rightarrow b, \ \delta \rightarrow b \Rightarrow$$

 $\delta \vdash \text{undefined} \Rightarrow \text{undefined}, \ \delta \qquad \delta \vdash \text{null} \Rightarrow \text{null}, \ \delta \qquad \delta \vdash \text{absent} \Rightarrow \text{absent}, \ \delta$ 

$$\frac{\delta \vdash_{escape} e \Rightarrow v, \ \delta_0 \quad \odot v \Rightarrow v_0}{\delta \vdash \odot e \Rightarrow v_0, \ \delta_0} \qquad \frac{\delta \vdash_{escape} e_0 \Rightarrow v_0, \ \delta_0 \quad \delta_0 \vdash_{escape} e_1 \Rightarrow v_1, \ \delta_1 \quad v_0 \oplus v_1 \Rightarrow v_2}{\delta \vdash e_0 \oplus e_1 \Rightarrow v_2, \ \delta_1}$$

$$\frac{\Delta = \mathtt{getCtx}(\delta) \quad \sqcup = \mathtt{getCtxStack}(\delta) \quad v_c = \Delta, \ \sqcup, \ x^* \ [\Rightarrow] \ i}{\delta \vdash (x^*) \ [\Rightarrow] \ i \Rightarrow v_c, \ \delta} \qquad \frac{\delta \vdash e \Rightarrow v, \ \delta_0 \quad \mathtt{getType}(v) = s_{type}}{\delta \vdash \mathtt{typeof} \ e \Rightarrow s_{type}, \ \delta_0}$$

$$\frac{\delta \vdash_{escape} e \Rightarrow s, \ \delta_0 \quad \text{allocSymbol}(\delta_0, \ s) = (a, \ \delta_1)}{\delta \vdash \text{new } e \Rightarrow a, \ \delta_1}$$

$$\frac{\delta \vdash_{escape} e \Rightarrow \mathtt{undefined}, \ \delta_0 \quad \mathtt{allocSymbol}(\delta_0, \ \mathtt{undefined}) = (a, \ \delta_1)}{\delta \vdash \mathtt{new} \ e \Rightarrow a, \ \delta_1}$$

$$\frac{\delta \vdash e_0 \Rightarrow v_0, \ \delta_0 \quad \cdots \quad \delta_{n-1} \vdash e_n \Rightarrow v_n, \ \delta_n}{\delta \vdash \texttt{new } [e^*] \Rightarrow a, \ \delta_{next}}$$

$$\text{allocMap}(\delta,\ t) = (a,\ \delta_t)$$
 
$$\delta_t \vdash_{escape} e_{k_0} \Rightarrow v_{k_0},\ \delta_{0_k} \quad \delta_{0_k} \vdash e_{v_0} \Rightarrow v_{v_0},\ \delta_{0_v} \quad \text{updated}(\delta_{0_v},\ v_{k_0},\ v_{v_0}) = \delta_0$$

$$\delta_{n-1} \vdash_{escape} e_{k_n} \Rightarrow v_{k_n}, \ \delta_{n_k} \quad \delta_{n_k} \vdash e_{v_n} \Rightarrow v_{v_n}, \ \delta_{n_v} \quad \text{updated}(\delta_{n_v}, \ v_{k_n}, \ v_{v_n}) = \delta_n$$
 
$$\delta \vdash \text{new } t \ (e_{k_0} \ \mapsto \ e_{v_0}, \ \cdots, \ e_{k_n} \ \mapsto \ e_{v_n}) \Rightarrow a, \ \delta_n$$

$$\frac{\delta \vdash_{escape} e_0 \Rightarrow a, \ \delta_0 \quad \ \delta_0 \vdash_{escape} e_1 \Rightarrow v_k, \ \delta_1 \quad \ \mathsf{pop}(\delta_1, \ a, \ v_k) = (v, \ \delta_2)}{\delta \vdash \mathsf{pop} \ e_0 \ e_1 \Rightarrow v, \ \delta_2}$$

$$\frac{\delta \vdash_{escape} e \Rightarrow a_0, \ \delta_0 \quad \mathsf{copyObj}(\delta_0, \ a_0) = (a_1, \ \delta_1)}{\delta \vdash_{escape} e \Rightarrow a_0, \ \delta_0 \quad \mathsf{keys}(\delta_0, \ a_0) = (a_1, \ \delta_1)}{\delta \vdash_{escape} e \Rightarrow a_0, \ \delta_0 \quad \mathsf{keys}(\delta_0, \ a_0) = (a_1, \ \delta_1)}$$

$$\frac{\delta \vdash_{escape} e_0 \Rightarrow a_l, \ \delta_0 \quad \delta_0 \vdash_{escape} e_1 \Rightarrow v, \ \delta_1 \quad \mathtt{contains}(\delta_1, \ a_l, \ v) = b}{\delta \vdash \mathtt{contains} \ e_0 \ e_1 \Rightarrow b, \ \delta_1}$$

## TODO

reference is-instance-of get-elements

get-syntax

parse-syntax

convert

not supported

handle escapeCompletion