Parallel Programming Assignment 2

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Prime Number Code Generation

This report compares different methods for optimizing prime number generation in the fastest way possible by converting the code into a parallel cyclic approach.

- P_0 starts from 3 and checks for prime numbers, then increases the step size by the number of total processes.
- P_1 starts from the next odd number after 3, which is 5, and continues in a similar manner.
- Each process follows this cyclic pattern for generating prime numbers efficiently.

Also compares how fast parallel processing distributes numbers in a cyclic manner, either by dividing them among processes.

Q1: Why the algorithms checks only up to sqrt(n) not up to N?

n is the input number. The algorithm checks if n is prime by starting from 2 up to \sqrt{n} . This is because if there is a factor divisible by n, it must be less than or equal to \sqrt{n} . This method reduces the number of iterations for the loop, making the algorithm more efficient.

Q3: pseudocode for the mpiprime.cpp code

Terminal 1: pseudocode function main() if process_id == 0 then begin = 3stop = input_from_user() // Get the stop value from user input int block_test=stop/number_of_processes; for i: integer = 1 to number_of_processes - 1 send (i*block_test) to process i send (i*block test+block test) to process i end for else receive begin from process 0 receive stop from process 0 for num: integer = begin to stop // test for prime number and print begin=begin+1 end for end if end function

This method divides all numbers from 'begin' to 'stop' among all processes Let the number of processes be 4 and the stop value be 12. When we divide 12 by 4, each process will test 3 numbers after removing the even numbers:

- Process 0 will test 3, 4, and 5.
- Process 1 will test 6, 7, and 8.
- Process 2 will test 9, 10, and 11.
- Process 3 will test 12.

Q4: pseudocode for the mpiprimecyclic.cpp code

Terminal 2: pseudocode function main() if process_id == 0 then begin = 3stop = input_from_user() // Get the stop value from user input rank = # process for i: integer = 1 to number_of_processes - 1 if rank is even then begin = begin + 2else begin = begin + 3send begin to process i send stop to process i end for end if else receive begin from process 0 receive stop from process 0 for num: integer = begin to stop // test for prime number and print //step size is number_of_processes*2 to move in cyclic way begin=begin+number of processes*2 end for end function

- 1. Obtain the input value from the user using command-line arguments.
- 2. Check if the process ID is odd.
- 3. If the process ID is odd, add 3 to begin, else add 2. This will be the starting point for the process.
- 4. Send begin and stop for each process
- 5. Each process moves in steps of size equal to the number of processes multiplied by 2. Multiplying by 2 eliminates even numbers from consideration.

Result

Definition 1: Time effect

If a process takes more time than other processes, it will slow down the entire program. Therefore, it is important for most processes to have similar execution times.

n	Process 0	Process 1	Process 2	Process 3
4	2.0188e-05	9.514e-06	1.4312e-05	1.447e-05
27	1.9036e-05	1.4312e-05	1.4072e-05	1.5406e-05
256	2.0566e-05	1.7013e-05	1.3513e-05	1.3792e-05
3125	4.6505e-05	4.4858e-05	5.5102e-05	5.9473e-05
46656	0.000902282	0.00131633	0.00128097	0.00165753
823543	0.033588	0.0612693	0.0649758	0.0749103
16777216	2.19437	3.51942	4.38887	4.93196

Table 1: Test with Block mpiprime.cpp

n	Process 0	Process 1	Process 2	Process 3
4	2.1778e-05	1.674e-05	1.5346e-05	1.5547e-05
27	1.9529e-05	1.2089e-05	1.5456e-05	1.0563e-05
256	2.3556e-05	2.0128e-05	1.853e-05	1.6039e-05
3125	5.7887e-05	3.9829e-05	3.7447e-05	5.1583e-05
46656	0.0012891	0.000718887	0.00125227	0.000739666
823543	0.0564921	0.056242	0.0532188	0.0530984
16777216	4.01768	4.03032	3.96029	4.02423

Table 2: Test with cyclic mpiprimecycilc.cpp

Note 1: 16777216

Note that when n is 16777216, the execution time of the mpiprime code differed, while in the mpiprimecycilc code, we saved 1 second

cyclic was faster, and all the processes worked equally. On the other hand, without cyclic by block, the time between processes was different. Considering my high-speed CPU and the heavy programs I work with, these factors might have affected the results. However, it is clear that cyclic was more stable.

Note 2: Windows Subsystem for Linux

I work on WSL (Windows Subsystem for Linux) on my PC; perhaps this could affect the results.

How to Run the Code

Terminal 3: Bash: mpiprimecyclic.cpp

```
$ mpic++ ./mpiprimecyclic.cpp
# Comilpe the code
$ mpirun -np 8 --allow-run-as-root a.out 256
# mpirun -np 8 --allow-run-as-root a.out [Argument ]
process 3: 41 73 89 137 233    time = 2.9024e-05
process 4: 11 43 59 107 139 251    time = 2.0499e-05
process 6: 31 47 79 127 191 223 239    time = 1.7274e-05
process 0: 3 19 67 83 131 163 179 211 227    time = 1.5743e-05
process 1: 5 37 53 101 149 181 197 229    time = 1.6261e-05
process 2: 7 23 71 103 151 167 199    time = 1.5841e-05
process 7: 17 97 113 193 241    time = 1.6951e-05
process 5: 13 29 61 109 157 173    time = 1.4858e-05
```

Terminal 4: Bash: mpiprime.cpp

```
$ mpic++ ./mpiprime.cpp
# Comilpe the code
$ mpirun -np 8 --allow-run-as-root a.out 256
# mpirun -np 8 --allow-run-as-root a.out [Argument ]
process 4: 131 137 139 149 151 157 time = 2.4752e-05
process 5: 163 167 173 179 181 191 time = 1.575e-05
process 6: 193 197 199 211 223 time = 1.7078e-05
process 7: 227 229 233 239 241 251 time = 1.591e-05
process 0: 3 5 7 11 13 17 19 23 29 31 time = 1.4383e-05
process 1: 37 41 43 47 53 59 61 time = 1.8054e-05
process 2: 67 71 73 79 83 89 time = 2.7491e-05
process 3: 97 101 103 107 109 113 127 time = 2.7615e-05
```