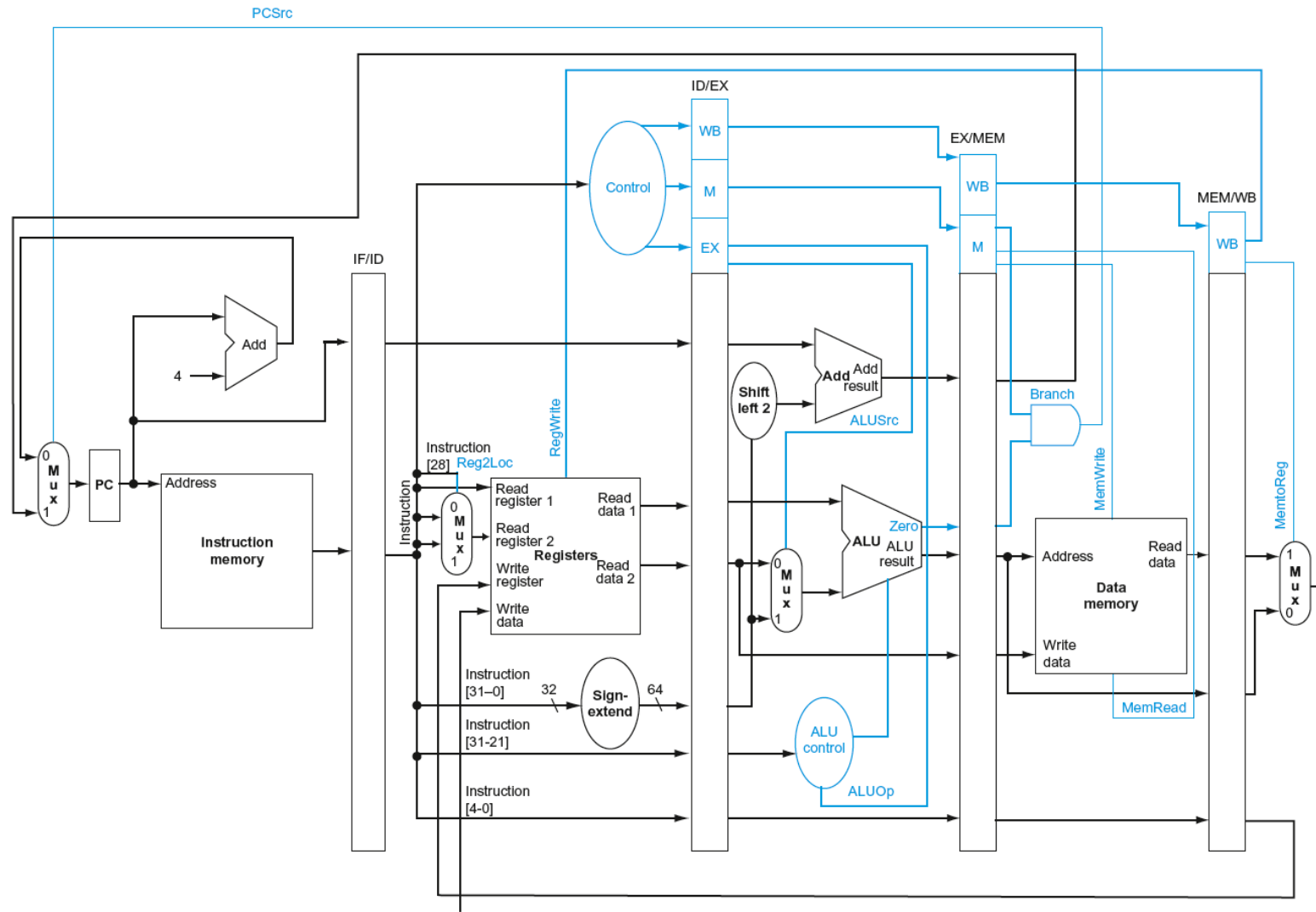


Chapter 5

Large and Fast: Exploiting Memory Hierarchy

Pipelined Control



Principle of Locality

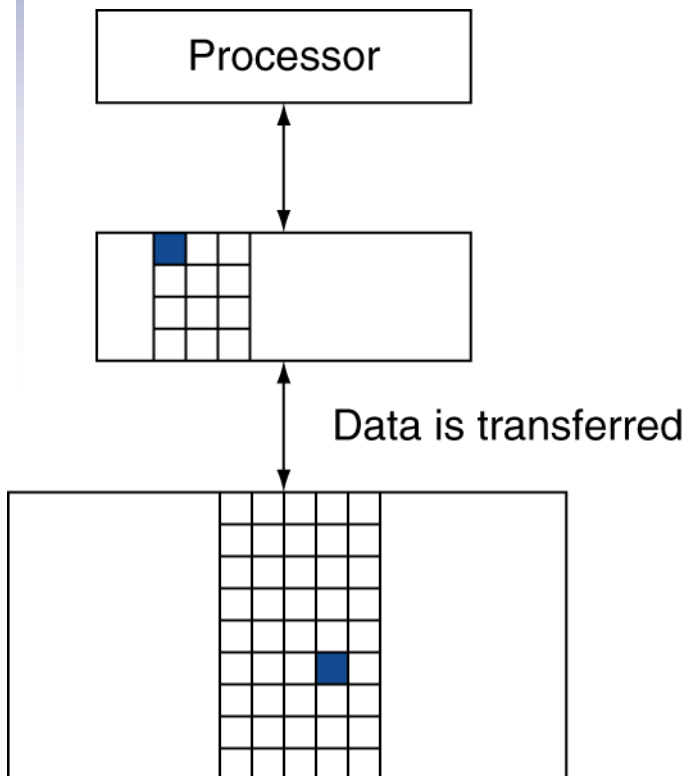
- Programs access a small proportion of their address space at any time
- Temporal locality
 - Items accessed recently are likely to be accessed again soon
 - e.g., instructions in a loop, induction variables
- Spatial locality
 - Items near those accessed recently are likely to be accessed soon
 - E.g., sequential instruction access, array data

Taking Advantage of Locality

- Memory hierarchy
- Store everything on disk
- Copy recently accessed (and nearby) items from disk to smaller DRAM memory
 - Main memory
- Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
 - Cache memory attached to CPU

Memory Hierarchy Levels

- Block (aka line): unit of copying
 - May be multiple words
- If accessed data is present in upper level
 - Hit: access satisfied by upper level
 - Hit ratio: hits/accesses
- If accessed data is absent
 - Miss: block copied from lower level
 - Time taken: miss penalty
 - Miss ratio: misses/accesses
 $= 1 - \text{hit ratio}$
 - Then accessed data supplied from upper level

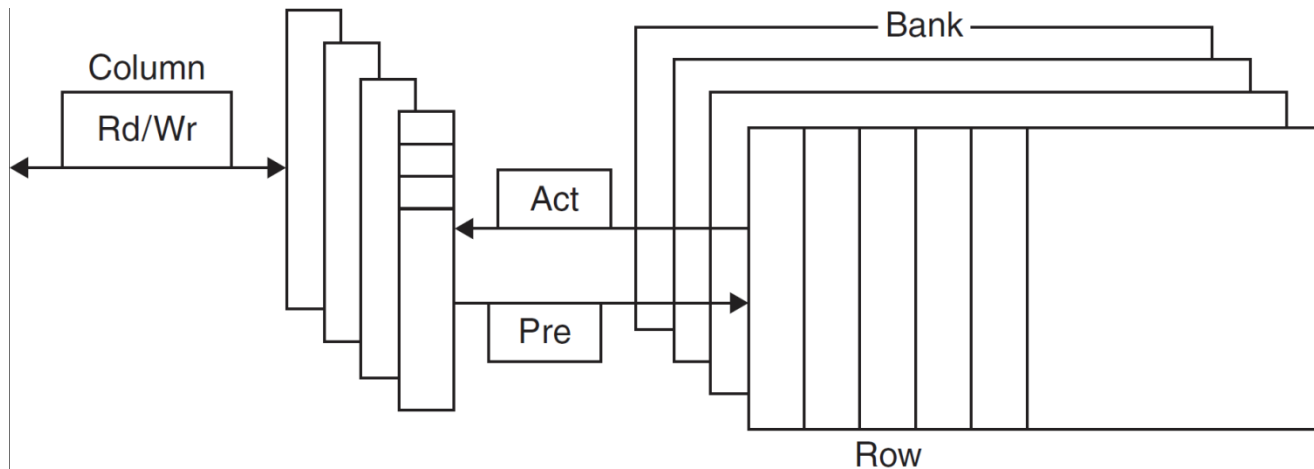


Memory Technology

- Static RAM (SRAM)
 - 0.5ns – 2.5ns, \$2000 – \$5000 per GB
- Dynamic RAM (DRAM)
 - 50ns – 70ns, \$20 – \$75 per GB
- Magnetic disk
 - 5ms – 20ms, \$0.20 – \$2 per GB
- Ideal memory
 - Access time of SRAM
 - Capacity and cost/GB of disk

DRAM Technology

- Data stored as a charge in a capacitor
 - Single transistor used to access the charge
 - Must periodically be refreshed
 - Read contents and write back
 - Performed on a DRAM “row”

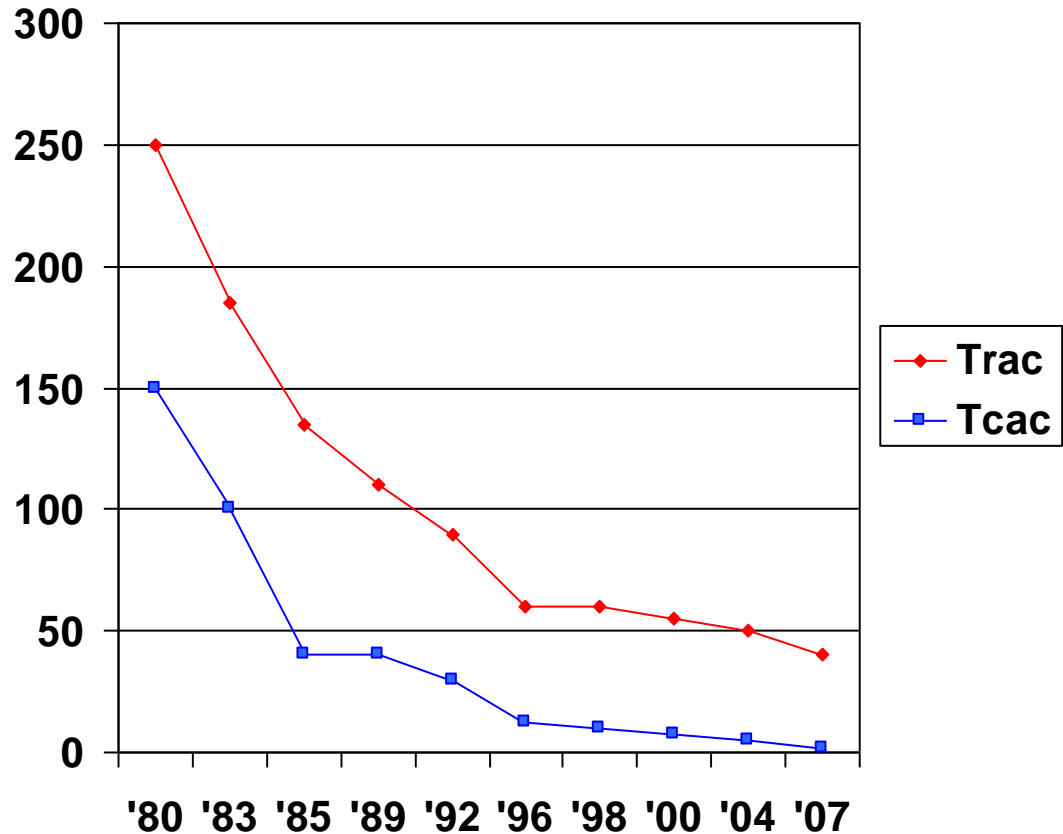


Advanced DRAM Organization

- Bits in a DRAM are organized as a rectangular array
 - DRAM accesses an entire row
 - Burst mode: supply successive words from a row with reduced latency
- Double data rate (DDR) DRAM
 - Transfer on rising and falling clock edges
- Quad data rate (QDR) DRAM
 - Separate DDR inputs and outputs

DRAM Generations

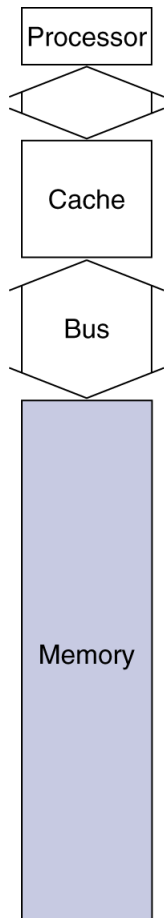
| Year | Capacity | \$/GB |
|------|----------|-----------|
| 1980 | 64Kbit | \$1500000 |
| 1983 | 256Kbit | \$500000 |
| 1985 | 1Mbit | \$200000 |
| 1989 | 4Mbit | \$50000 |
| 1992 | 16Mbit | \$15000 |
| 1996 | 64Mbit | \$10000 |
| 1998 | 128Mbit | \$4000 |
| 2000 | 256Mbit | \$1000 |
| 2004 | 512Mbit | \$250 |
| 2007 | 1Gbit | \$50 |



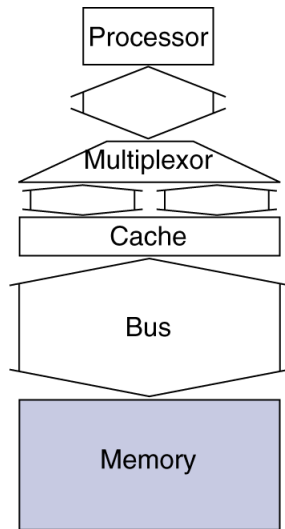
DRAM Performance Factors

- Row buffer
 - Allows several words to be read and refreshed in parallel
- Synchronous DRAM
 - Allows for consecutive accesses in bursts without needing to send each address
 - Improves bandwidth
- DRAM banking
 - Allows simultaneous access to multiple DRAMs
 - Improves bandwidth

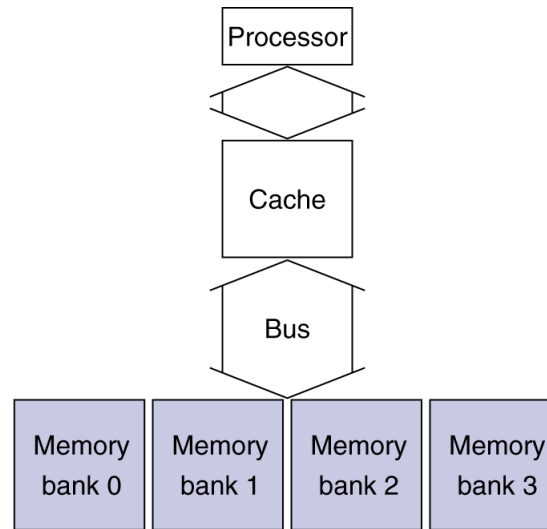
Increasing Memory Bandwidth



a. One-word-wide memory organization



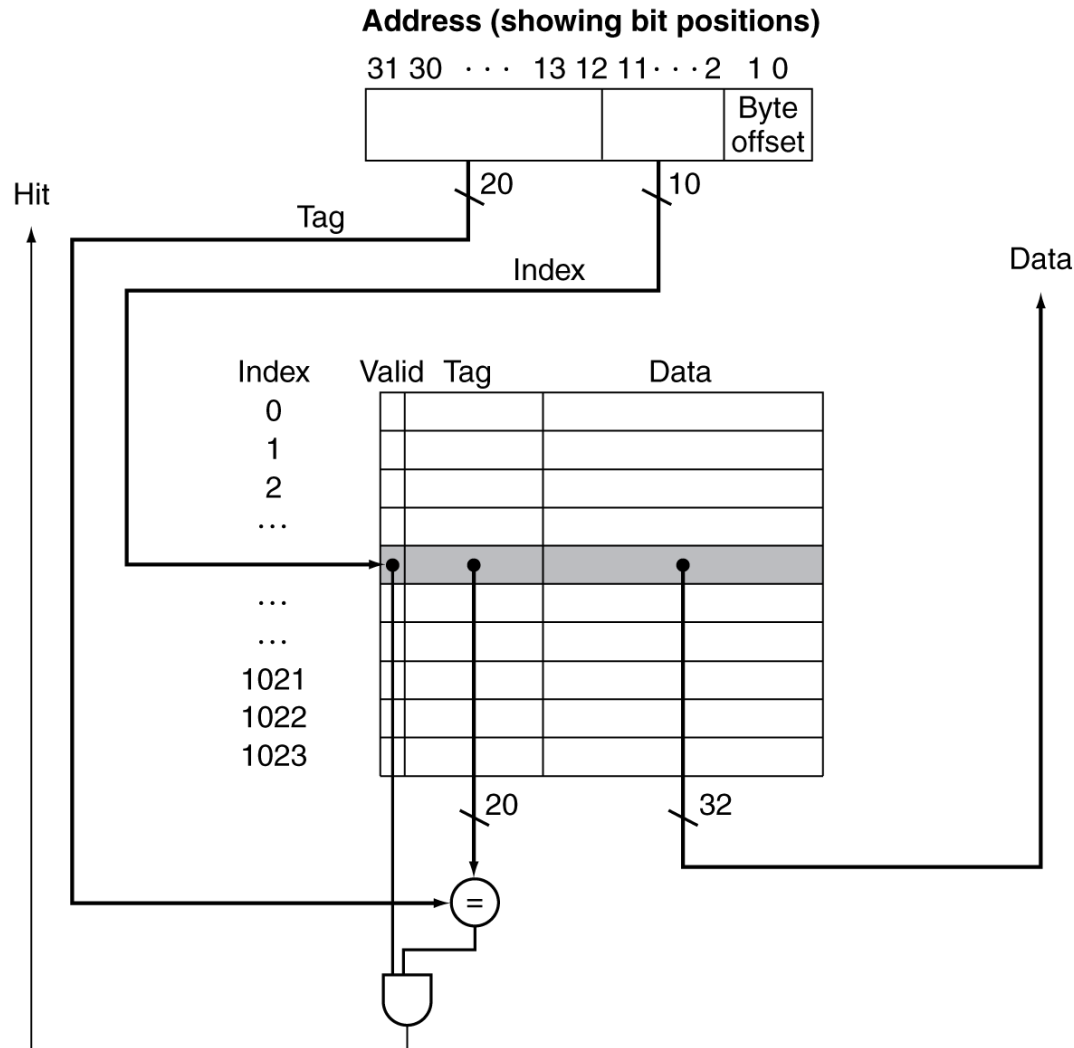
b. Wider memory organization



c. Interleaved memory organization

- 4-word wide memory
 - Miss penalty = $1 + 15 + 1 = 17$ bus cycles
 - Bandwidth = $16 \text{ bytes} / 17 \text{ cycles} = 0.94 \text{ B/cycle}$
- 4-bank interleaved memory
 - Miss penalty = $1 + 15 + 4 \times 1 = 20$ bus cycles
 - Bandwidth = $16 \text{ bytes} / 20 \text{ cycles} = 0.8 \text{ B/cycle}$

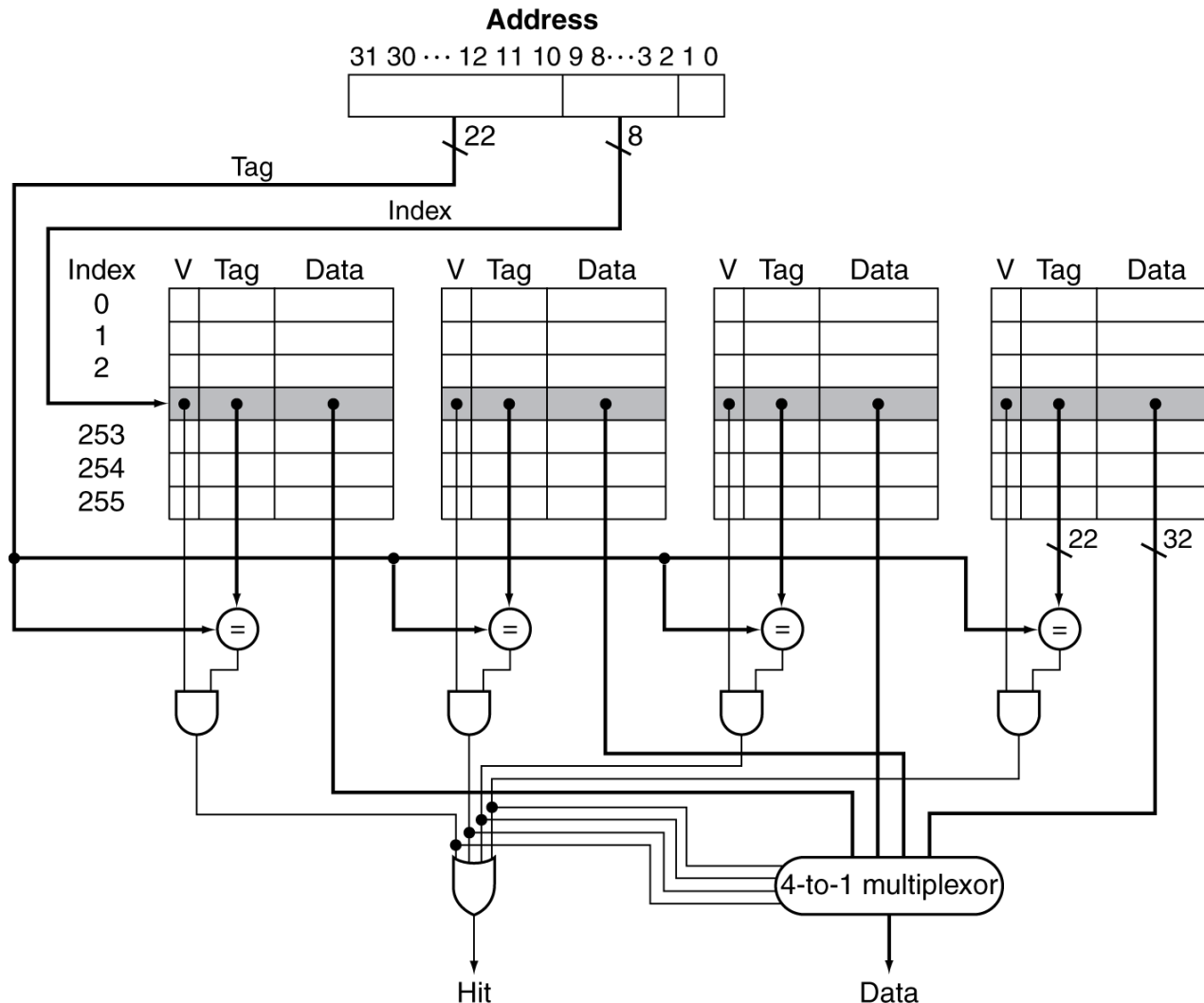
Address Subdivision



Address Subdivision

Address Subdivision

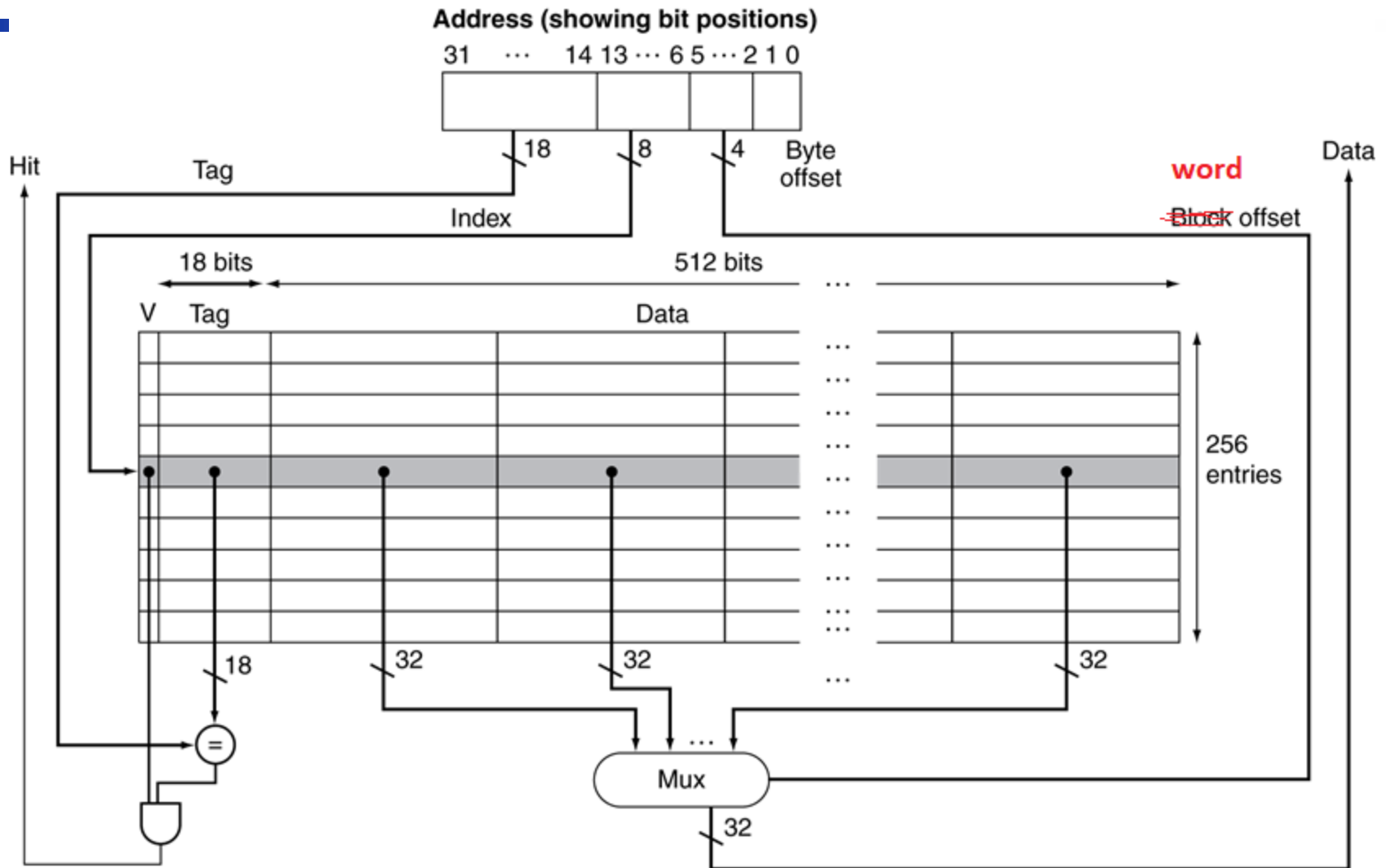
Set Associative Cache Organization



Set Associative Cache Organization

Set Associative Cache Organization

¿lo siguiente: 1 Vía o 4 Vías?



¿lo siguiente: 1 Vía o 4 Vías?

Spectrum of Associativity

- For a cache with 8 entries

**One-way set associative
(direct mapped)**

| Block | Tag | Data |
|-------|-----|------|
| 0 | | |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |
| 6 | | |
| 7 | | |

Two-way set associative

| Set | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|
| 0 | | | | |
| 1 | | | | |
| 2 | | | | |
| 3 | | | | |

Four-way set associative

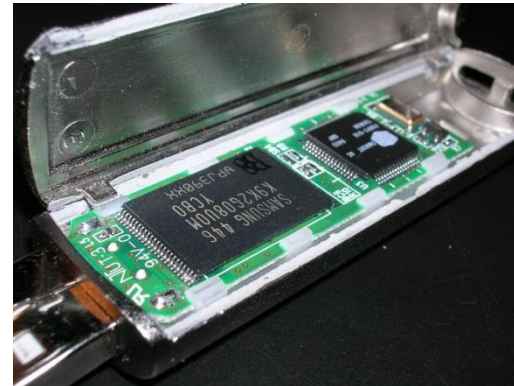
| Set | Tag | Data | Tag | Data | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|-----|------|-----|------|
| 0 | | | | | | | | |
| 1 | | | | | | | | |

Eight-way set associative (fully associative)

| Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data |
|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|
| | | | | | | | | | | | | | | | |

Flash Storage

- Nonvolatile semiconductor storage
 - 100× – 1000× faster than disk
 - Smaller, lower power, more robust
 - But more \$/GB (between disk and DRAM)

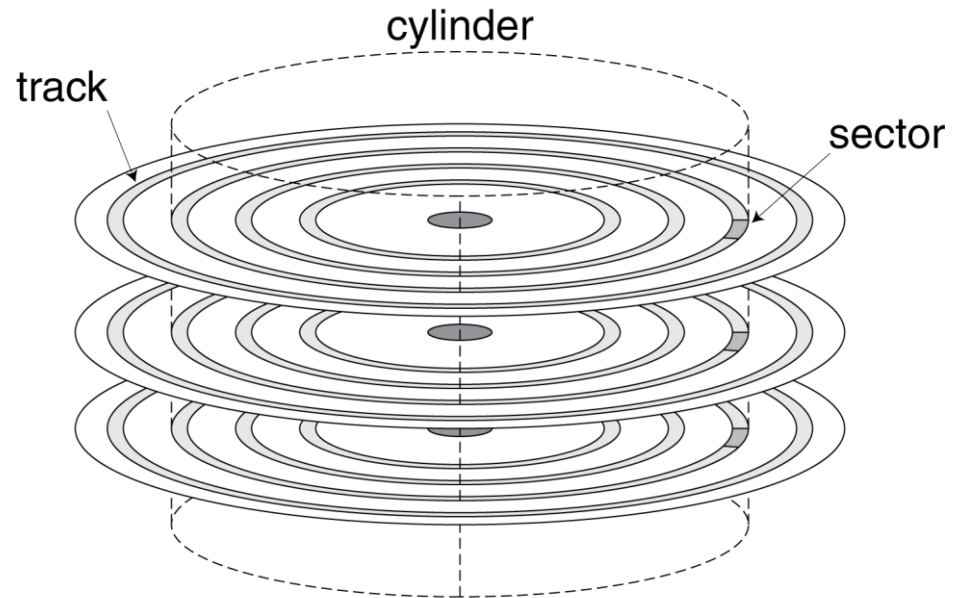


Flash Types

- NOR flash: bit cell like a NOR gate
 - Random read/write access
 - Used for instruction memory in embedded systems
- NAND flash: bit cell like a NAND gate
 - Denser (bits/area), but block-at-a-time access
 - Cheaper per GB
 - Used for USB keys, media storage, ...
- Flash bits wears out after 1000's of accesses
 - Not suitable for direct RAM or disk replacement
 - Wear leveling: remap data to less used blocks

Disk Storage

- Nonvolatile, rotating magnetic storage



Disk Sectors and Access

- Each sector records
 - Sector ID
 - Data (512 bytes, 4096 bytes proposed)
 - Error correcting code (ECC)
 - Used to hide defects and recording errors
 - Synchronization fields and gaps
- Access to a sector involves
 - Queuing delay if other accesses are pending
 - Seek: move the heads
 - Rotational latency
 - Data transfer
 - Controller overhead

Disk Access Example

- Given
 - 512B sector, 15,000rpm, 4ms average seek time, 100MB/s transfer rate, 0.2ms controller overhead, idle disk
- Average read time
 - 4ms seek time
+ $\frac{1}{2} / (15,000/60) = 2\text{ms}$ rotational latency
+ $512 / 100\text{MB/s} = 0.005\text{ms}$ transfer time
+ 0.2ms controller delay
= 6.2ms
- If actual average seek time is 1ms
 - Average read time = 3.2ms

Disk Performance Issues

- Manufacturers quote average seek time
 - Based on all possible seeks
 - Locality and OS scheduling lead to smaller actual average seek times
- Smart disk controller allocate physical sectors on disk
 - Present logical sector interface to host
 - SCSI, ATA, SATA
- Disk drives include caches
 - Prefetch sectors in anticipation of access
 - Avoid seek and rotational delay

Cache Memory

- Cache memory
 - The level of the memory hierarchy closest to the CPU
- Given accesses X_1, \dots, X_{n-1}, X_n

| |
|-----------|
| X_4 |
| X_1 |
| X_{n-2} |
| |
| X_{n-1} |
| X_2 |
| |
| X_3 |

a. Before the reference to X_n

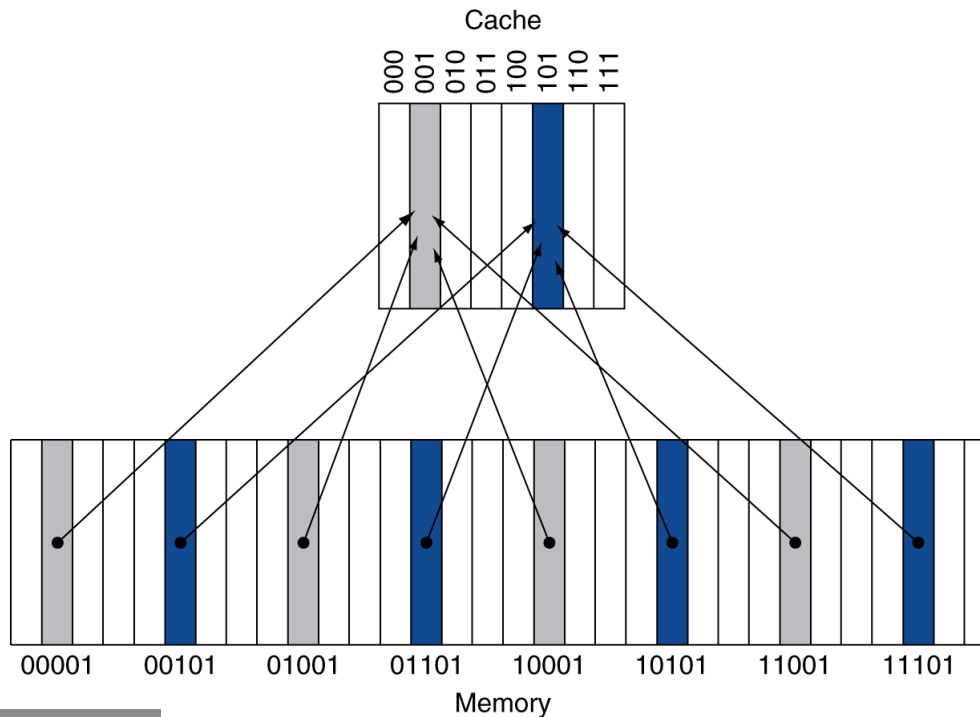
| |
|-----------|
| X_4 |
| X_1 |
| X_{n-2} |
| |
| X_{n-1} |
| X_2 |
| X_n |
| X_3 |

b. After the reference to X_n

- How do we know if the data is present?
- Where do we look?

Direct Mapped Cache

- Location determined by address
- Direct mapped: only one choice
 - (Block address) modulo (#Blocks in cache)



- #Blocks is a power of 2
- Use low-order address bits

Tags and Valid Bits

- How do we know which particular block is stored in a cache location?
 - Store block address as well as the data
 - Actually, only need the high-order bits
 - Called the tag
- What if there is no data in a location?
 - Valid bit: 1 = present, 0 = not present
 - Initially 0

Cache Example

- 8-blocks, 1 word/block, direct mapped
- Initial state

| Index | V | Tag | Data |
|-------|---|-----|------|
| 000 | N | | |
| 001 | N | | |
| 010 | N | | |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | N | | |
| 111 | N | | |

Cache Example

| Word addr | Binary addr | Hit/miss | Cache block |
|-----------|-------------|----------|-------------|
| 22 | 10 110 | Miss | 110 |

| Index | V | Tag | Data |
|-------|---|-----|------------|
| 000 | N | | |
| 001 | N | | |
| 010 | N | | |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 | Mem[10110] |
| 111 | N | | |

Cache Example

| Word addr | Binary addr | Hit/miss | Cache block |
|-----------|-------------|----------|-------------|
| 26 | 11 010 | Miss | 010 |

| Index | V | Tag | Data |
|-------|---|-----|------------|
| 000 | N | | |
| 001 | N | | |
| 010 | Y | 11 | Mem[11010] |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 | Mem[10110] |
| 111 | N | | |

Cache Example

| Word addr | Binary addr | Hit/miss | Cache block |
|-----------|-------------|----------|-------------|
| 22 | 10 110 | Hit | 110 |
| 26 | 11 010 | Hit | 010 |

| Index | V | Tag | Data |
|-------|---|-----|------------|
| 000 | N | | |
| 001 | N | | |
| 010 | Y | 11 | Mem[11010] |
| 011 | N | | |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 | Mem[10110] |
| 111 | N | | |

Cache Example

| Word addr | Binary addr | Hit/miss | Cache block |
|-----------|-------------|----------|-------------|
| 16 | 10 000 | Miss | 000 |
| 3 | 00 011 | Miss | 011 |
| 16 | 10 000 | Hit | 000 |

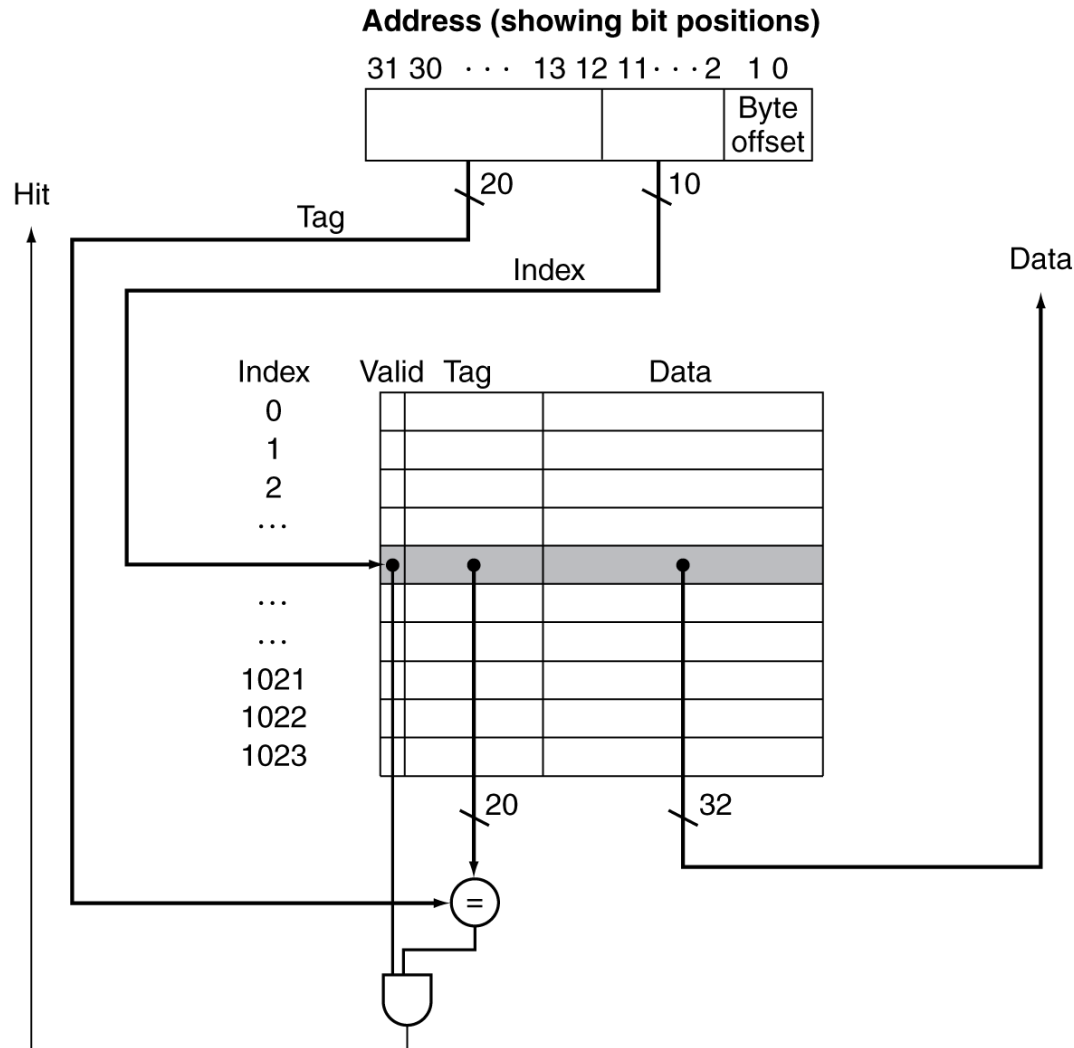
| Index | V | Tag | Data |
|-------|---|-----|------------|
| 000 | Y | 10 | Mem[10000] |
| 001 | N | | |
| 010 | Y | 11 | Mem[11010] |
| 011 | Y | 00 | Mem[00011] |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 | Mem[10110] |
| 111 | N | | |

Cache Example

| Word addr | Binary addr | Hit/miss | Cache block |
|-----------|-------------|----------|-------------|
| 18 | 10 010 | Miss | 010 |

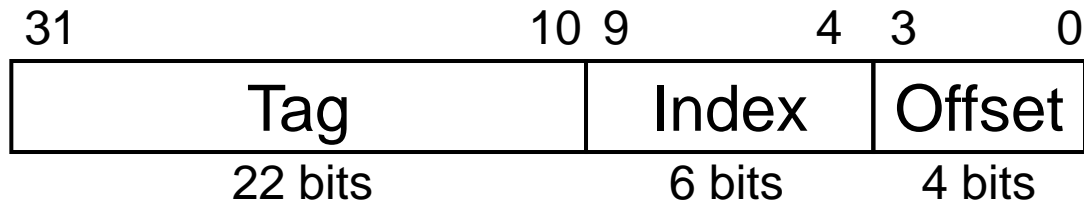
| Index | V | Tag | Data |
|------------|----------|-----------|-------------------|
| 000 | Y | 10 | Mem[10000] |
| 001 | N | | |
| 010 | Y | 10 | Mem[10010] |
| 011 | Y | 00 | Mem[00011] |
| 100 | N | | |
| 101 | N | | |
| 110 | Y | 10 | Mem[10110] |
| 111 | N | | |

Address Subdivision



Example: Larger Block Size

- 64 blocks, 16 bytes/block
 - To what block number does address 1200 map?
- Block address = $\lfloor 1200/16 \rfloor = 75$
- Block number = $75 \text{ modulo } 64 = 11$



Block Size Considerations

- Larger blocks should reduce miss rate
 - Due to spatial locality
- But in a fixed-sized cache
 - Larger blocks \Rightarrow fewer of them
 - More competition \Rightarrow increased miss rate
 - Larger blocks \Rightarrow pollution
- Larger miss penalty
 - Can override benefit of reduced miss rate
 - Early restart and critical-word-first can help

Cache Misses

- On cache hit, CPU proceeds normally
- On cache miss
 - Stall the CPU pipeline
 - Fetch block from next level of hierarchy
 - Instruction cache miss
 - Restart instruction fetch
 - Data cache miss
 - Complete data access

Write-Through

- On data-write hit, could just update the block in cache
 - But then cache and memory would be inconsistent
- Write through: also update memory
- But makes writes take longer
 - e.g., if base CPI = 1, 10% of instructions are stores, write to memory takes 100 cycles
 - Effective CPI = $1 + 0.1 \times 100 = 11$
- Solution: write buffer
 - Holds data waiting to be written to memory
 - CPU continues immediately
 - Only stalls on write if write buffer is already full

Write-Back

- Alternative: On data-write hit, just update the block in cache
 - Keep track of whether each block is dirty
- When a dirty block is replaced
 - Write it back to memory
 - Can use a write buffer to allow replacing block to be read first

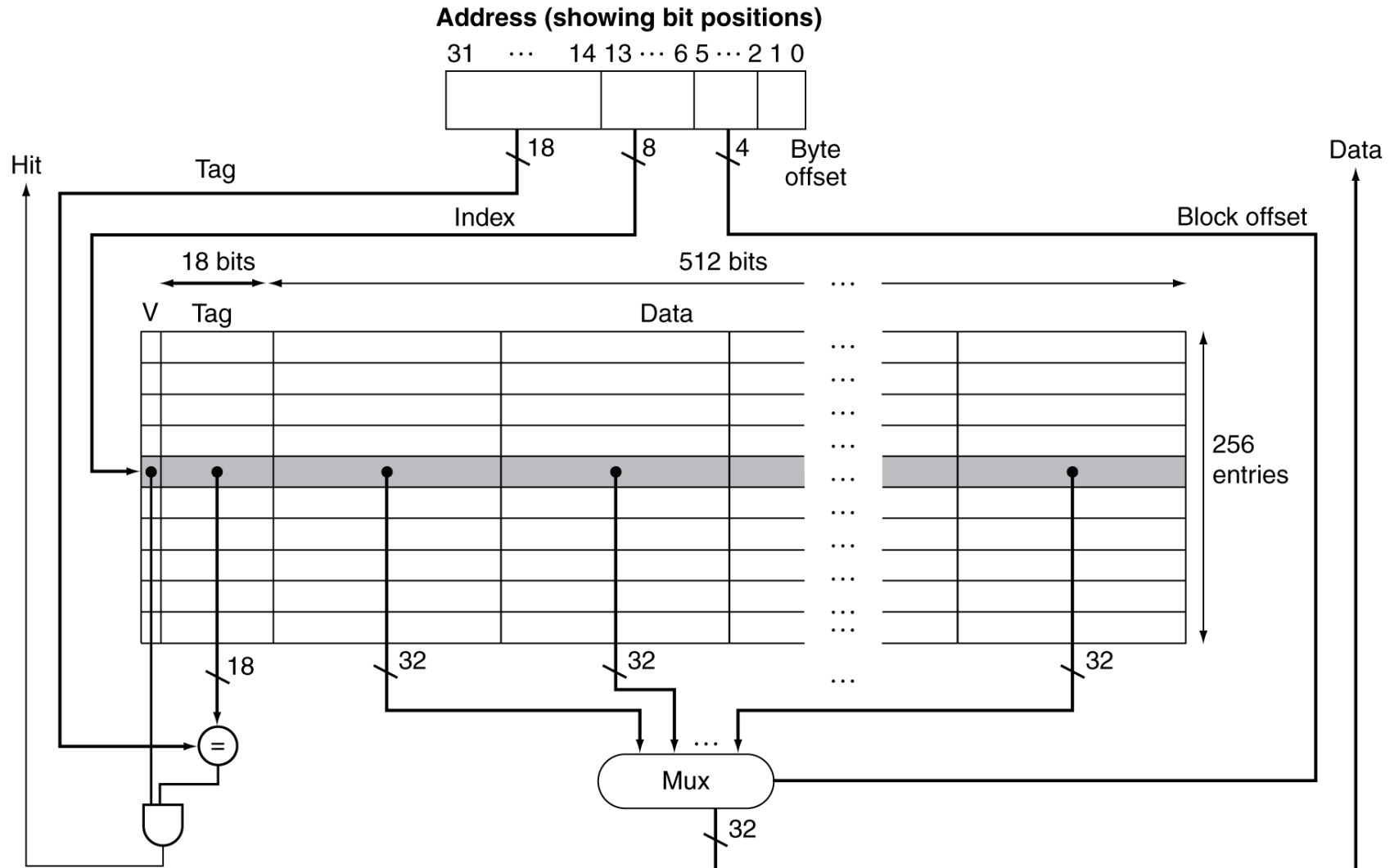
Write Allocation

- What should happen on a write miss?
- Alternatives for write-through
 - Allocate on miss: fetch the block
 - Write around: don't fetch the block
 - Since programs often write a whole block before reading it (e.g., initialization)
- For write-back
 - Usually fetch the block

Example: Intrinsity FastMATH

- Embedded MIPS processor
 - 12-stage pipeline
 - Instruction and data access on each cycle
- Split cache: separate I-cache and D-cache
 - Each 16KB: $256 \text{ blocks} \times 16 \text{ words/block}$
 - D-cache: write-through or write-back
- SPEC2000 miss rates
 - I-cache: 0.4%
 - D-cache: 11.4%
 - Weighted average: 3.2%

Example: Intrinsic FastMATH



Main Memory Supporting Caches

- Use DRAMs for main memory
 - Fixed width (e.g., 1 word)
 - Connected by fixed-width clocked bus
 - Bus clock is typically slower than CPU clock
- Example cache block read
 - 1 bus cycle for address transfer
 - 15 bus cycles per DRAM access
 - 1 bus cycle per data transfer
- For 4-word block, 1-word-wide DRAM
 - Miss penalty = $1 + 4 \times 15 + 4 \times 1 = 65$ bus cycles
 - Bandwidth = $16 \text{ bytes} / 65 \text{ cycles} = 0.25 \text{ B/cycle}$

Measuring Cache Performance

- Components of CPU time
 - Program execution cycles
 - Includes cache hit time
 - Memory stall cycles
 - Mainly from cache misses
- With simplifying assumptions:

Memory stall cycles

$$= \frac{\text{Memory accesses}}{\text{Program}} \times \text{Miss rate} \times \text{Miss penalty}$$

$$= \frac{\text{Instructions}}{\text{Program}} \times \frac{\text{Misses}}{\text{Instruction}} \times \text{Miss penalty}$$

Cache Performance Example

- Given
 - I-cache miss rate = 2%
 - D-cache miss rate = 4%
 - Miss penalty = 100 cycles
 - Base CPI (ideal cache) = 2
 - Load & stores are 36% of instructions
- Miss cycles per instruction
 - I-cache: $0.02 \times 100 = 2$
 - D-cache: $0.36 \times 0.04 \times 100 = 1.44$
- Actual CPI = $2 + 2 + 1.44 = 5.44$
 - Ideal CPU is $5.44/2 = 2.72$ times faster

Average Access Time

- Hit time is also important for performance
- Average memory access time (AMAT)
 - $AMAT = \text{Hit time} + \text{Miss rate} \times \text{Miss penalty}$
- Example
 - CPU with 1ns clock, hit time = 1 cycle, miss penalty = 20 cycles, l-cache miss rate = 5%
 - $AMAT = 1 + 0.05 \times 20 = 2\text{ns}$
 - 2 cycles per instruction

Performance Summary

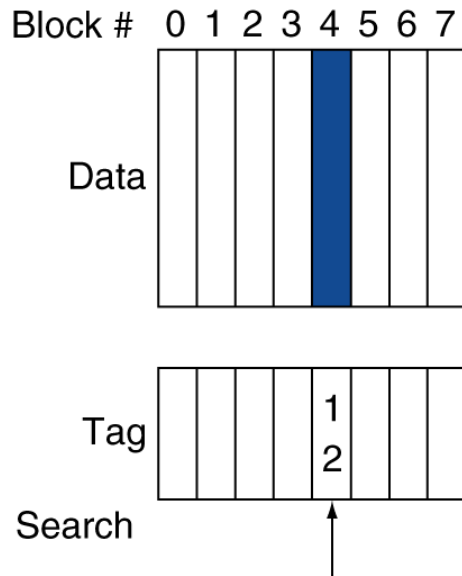
- When CPU performance increased
 - Miss penalty becomes more significant
- Decreasing base CPI
 - Greater proportion of time spent on memory stalls
- Increasing clock rate
 - Memory stalls account for more CPU cycles
- Can't neglect cache behavior when evaluating system performance

Associative Caches

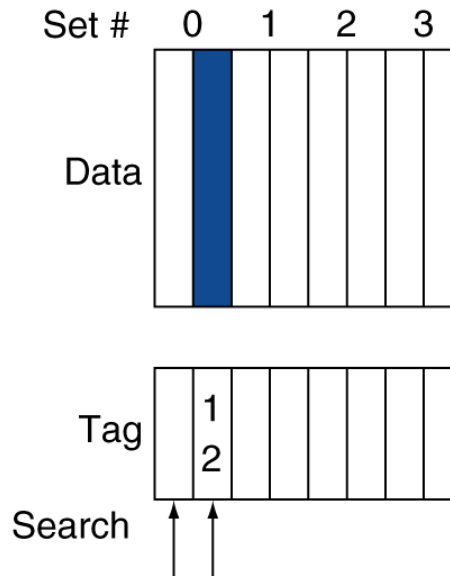
- Fully associative
 - Allow a given block to go in any cache entry
 - Requires all entries to be searched at once
 - Comparator per entry (expensive)
- *n*-way set associative
 - Each set contains *n* entries
 - Block number determines which set
 - (Block number) modulo (#Sets in cache)
 - Search all entries in a given set at once
 - *n* comparators (less expensive)

Associative Cache Example

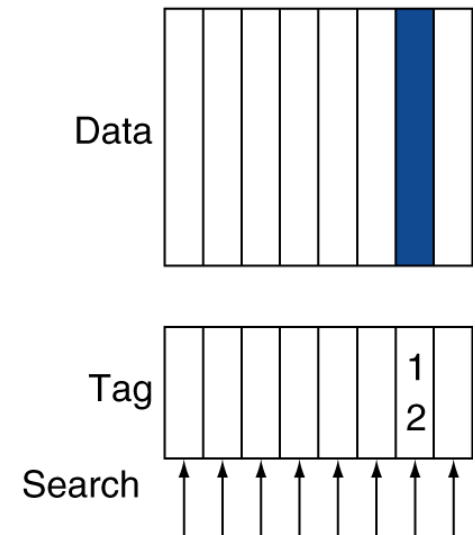
Direct mapped



Set associative



Fully associative



Spectrum of Associativity

- For a cache with 8 entries

**One-way set associative
(direct mapped)**

| Block | Tag | Data |
|-------|-----|------|
| 0 | | |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |
| 6 | | |
| 7 | | |

Two-way set associative

| Set | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|
| 0 | | | | |
| 1 | | | | |
| 2 | | | | |
| 3 | | | | |

Four-way set associative

| Set | Tag | Data | Tag | Data | Tag | Data | Tag | Data |
|-----|-----|------|-----|------|-----|------|-----|------|
| 0 | | | | | | | | |
| 1 | | | | | | | | |

Eight-way set associative (fully associative)

| Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data | Tag | Data |
|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|-----|------|
| | | | | | | | | | | | | | | | |

Associativity Example

- Compare 4-block caches
 - Direct mapped, 2-way set associative, fully associative
 - Block access sequence: 0, 8, 0, 6, 8
- Direct mapped

| Block address | Cache index | Hit/miss | Cache content after access | | | |
|---------------|-------------|----------|----------------------------|---|--------|---|
| | | | 0 | 1 | 2 | 3 |
| 0 | 0 | miss | Mem[0] | | | |
| 8 | 0 | miss | Mem[8] | | | |
| 0 | 0 | miss | Mem[0] | | | |
| 6 | 2 | miss | Mem[0] | | Mem[6] | |
| 8 | 0 | miss | Mem[8] | | Mem[6] | |

Associativity Example

■ 2-way set associative

| Block address | Cache index | Hit/miss | Cache content after access | | | |
|---------------|-------------|----------|----------------------------|--------|-------|--|
| | | | Set 0 | | Set 1 | |
| 0 | 0 | miss | Mem[0] | | | |
| 8 | 0 | miss | Mem[0] | Mem[8] | | |
| 0 | 0 | hit | Mem[0] | Mem[8] | | |
| 6 | 0 | miss | Mem[0] | Mem[6] | | |
| 8 | 0 | miss | Mem[8] | Mem[6] | | |

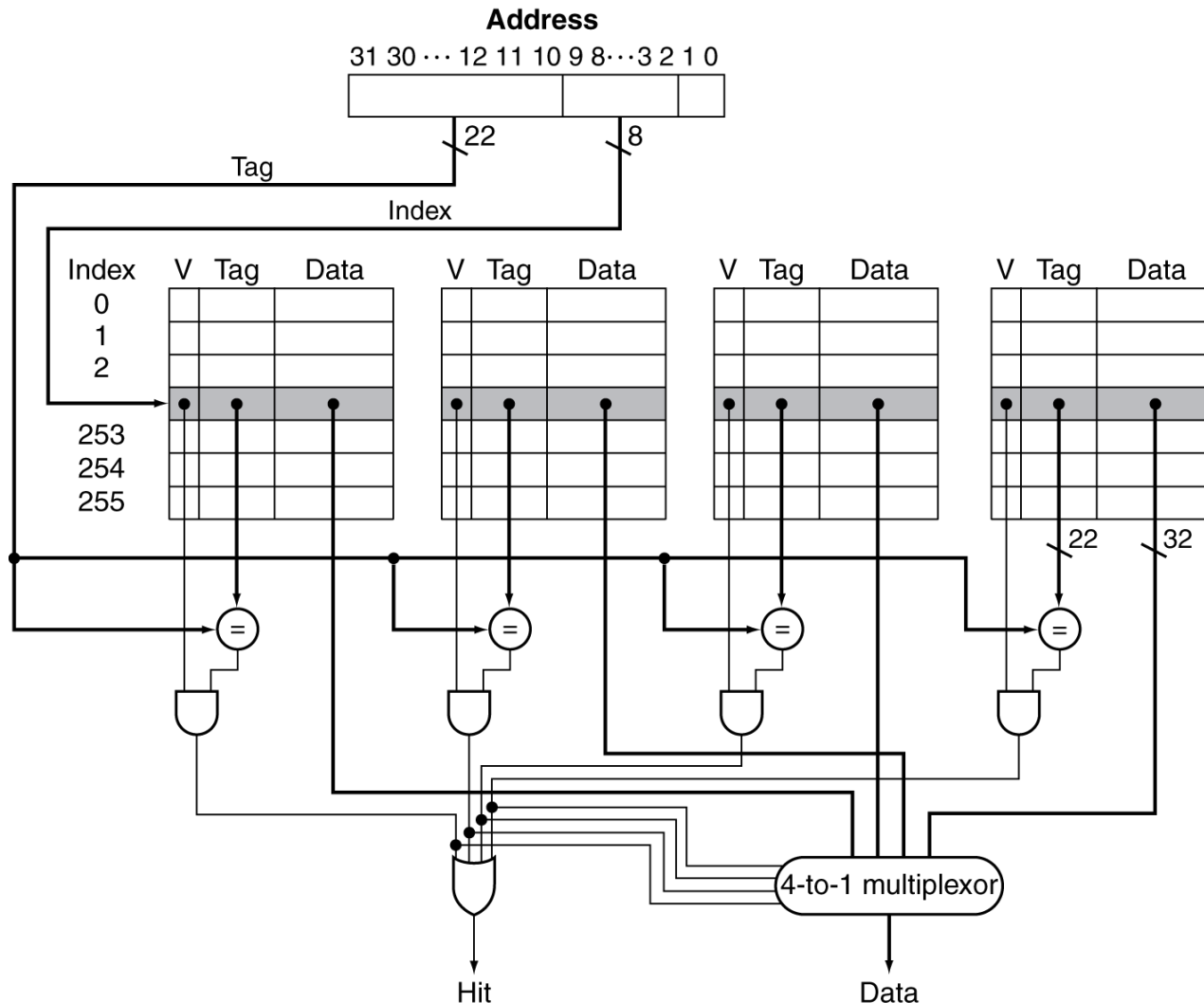
■ Fully associative

| Block address | | Hit/miss | Cache content after access | | | |
|---------------|--|----------|----------------------------|--------|--------|--|
| 0 | | miss | Mem[0] | | | |
| 8 | | miss | Mem[0] | Mem[8] | | |
| 0 | | hit | Mem[0] | Mem[8] | | |
| 6 | | miss | Mem[0] | Mem[8] | Mem[6] | |
| 8 | | hit | Mem[0] | Mem[8] | Mem[6] | |

How Much Associativity

- Increased associativity decreases miss rate
 - But with diminishing returns
- Simulation of a system with 64KB D-cache, 16-word blocks, SPEC2000
 - 1-way: 10.3%
 - 2-way: 8.6%
 - 4-way: 8.3%
 - 8-way: 8.1%

Set Associative Cache Organization



Replacement Policy

- Direct mapped: no choice
- Set associative
 - Prefer non-valid entry, if there is one
 - Otherwise, choose among entries in the set
- Least-recently used (LRU)
 - Choose the one unused for the longest time
 - Simple for 2-way, manageable for 4-way, too hard beyond that
- Random
 - Gives approximately the same performance as LRU for high associativity

Multilevel Caches

- Primary cache attached to CPU
 - Small, but fast
- Level-2 cache services misses from primary cache
 - Larger, slower, but still faster than main memory
- Main memory services L-2 cache misses
- Some high-end systems include L-3 cache

Multilevel Cache Example

- Given
 - CPU base CPI = 1, clock rate = 4GHz
 - Miss rate/instruction = 2%
 - Main memory access time = 100ns
- With just primary cache
 - Miss penalty = $100\text{ns} / 0.25\text{ns} = 400$ cycles
 - Effective CPI = $1 + 0.02 \times 400 = 9$

Example (cont.)

- Now add L-2 cache
 - Access time = 5ns
 - Global miss rate to main memory = 0.5%
- Primary miss with L-2 hit
 - Penalty = $5\text{ns}/0.25\text{ns} = 20$ cycles
- Primary miss with L-2 miss
 - Extra penalty = 500 cycles
- $\text{CPI} = 1 + 0.02 \times 20 + 0.005 \times 400 = 3.4$
- Performance ratio = $9/3.4 = 2.6$

Multilevel Cache Considerations

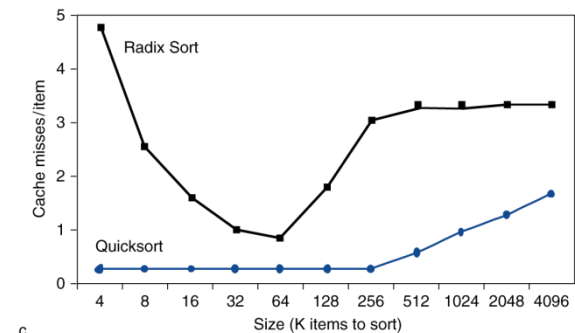
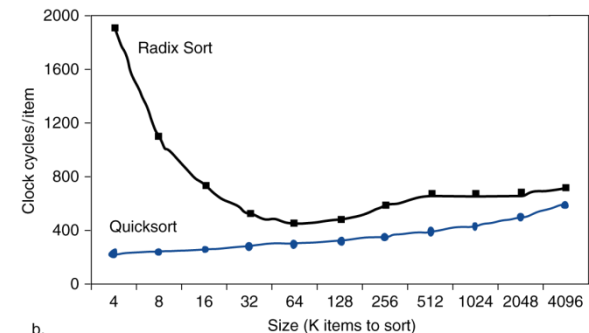
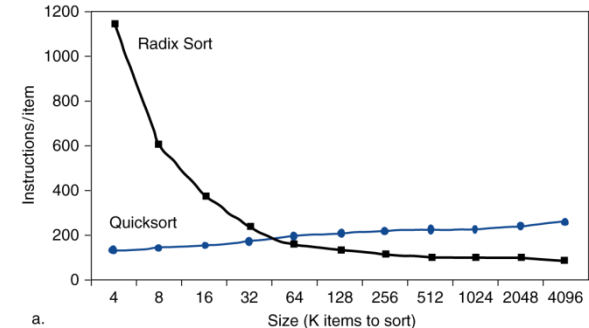
- Primary cache
 - Focus on minimal hit time
- L-2 cache
 - Focus on low miss rate to avoid main memory access
 - Hit time has less overall impact
- Results
 - L-1 cache usually smaller than a single cache
 - L-1 block size smaller than L-2 block size

Interactions with Advanced CPUs

- Out-of-order CPUs can execute instructions during cache miss
 - Pending store stays in load/store unit
 - Dependent instructions wait in reservation stations
 - Independent instructions continue
- Effect of miss depends on program data flow
 - Much harder to analyse
 - Use system simulation

Interactions with Software

- Misses depend on memory access patterns
 - Algorithm behavior
 - Compiler optimization for memory access



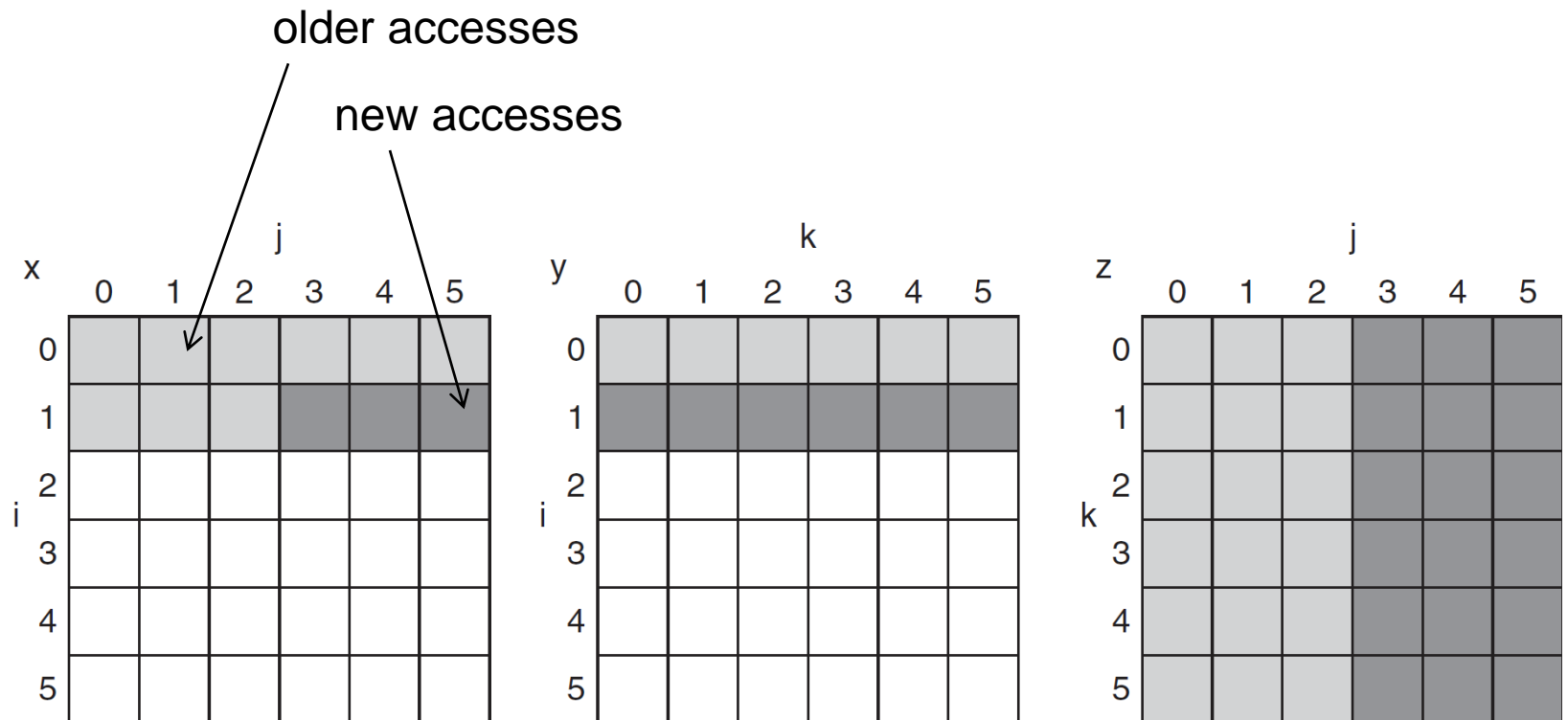
Software Optimization via Blocking

- Goal: maximize accesses to data before it is replaced
- Consider inner loops of DGEMM:

```
for (int j = 0; j < n; ++j)
{
    double cij = C[i+j*n];
    for( int k = 0; k < n; k++ )
        cij += A[i+k*n] * B[k+j*n];
    C[i+j*n] = cij;
}
```


DGEMM Access Pattern

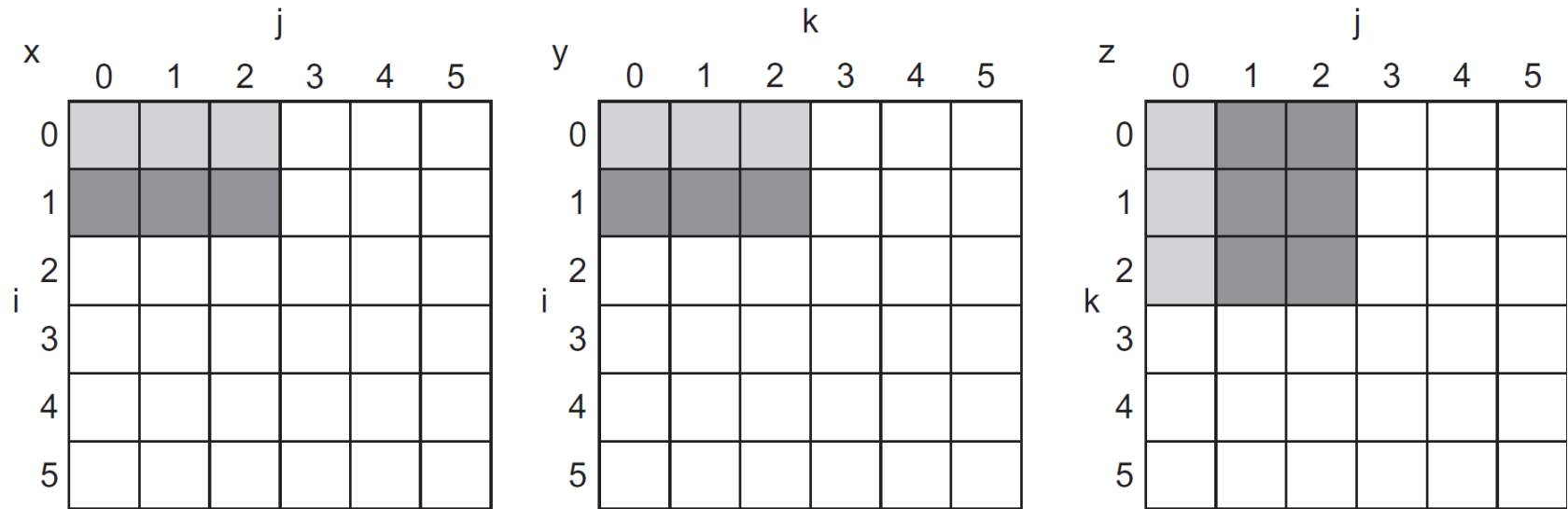
- C, A, and B arrays



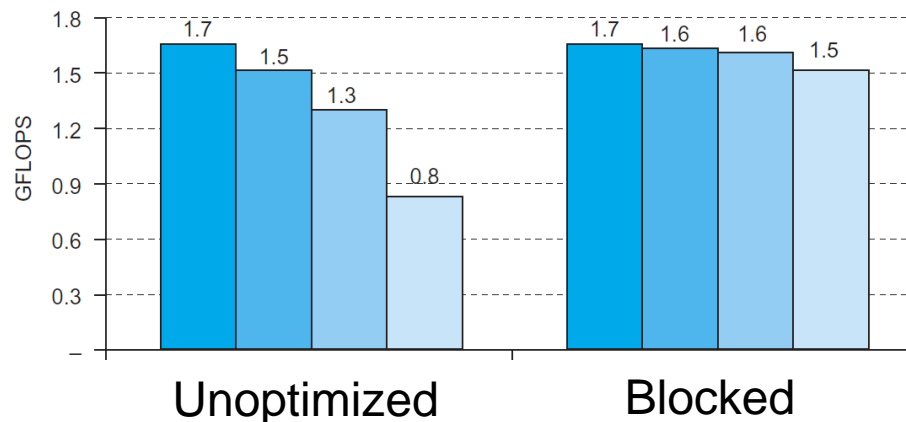
Cache Blocked DGEMM

```
1 #define BLOCKSIZE 32
2 void do_block (int n, int si, int sj, int sk, double *A, double
3 *B, double *C)
4 {
5   for (int i = si; i < si+BLOCKSIZE; ++i)
6     for (int j = sj; j < sj+BLOCKSIZE; ++j)
7       {
8         double cij = C[i+j*n];/* cij = C[i][j] */
9         for( int k = sk; k < sk+BLOCKSIZE; k++ )
10          cij += A[i+k*n] * B[k+j*n];/* cij+=A[i][k]*B[k][j] */
11        C[i+j*n] = cij;/* C[i][j] = cij */
12      }
13 }
14 void dgemm (int n, double* A, double* B, double* C)
15 {
16   for ( int sj = 0; sj < n; sj += BLOCKSIZE )
17     for ( int si = 0; si < n; si += BLOCKSIZE )
18       for ( int sk = 0; sk < n; sk += BLOCKSIZE )
19         do_block(n, si, sj, sk, A, B, C);
20 }
```

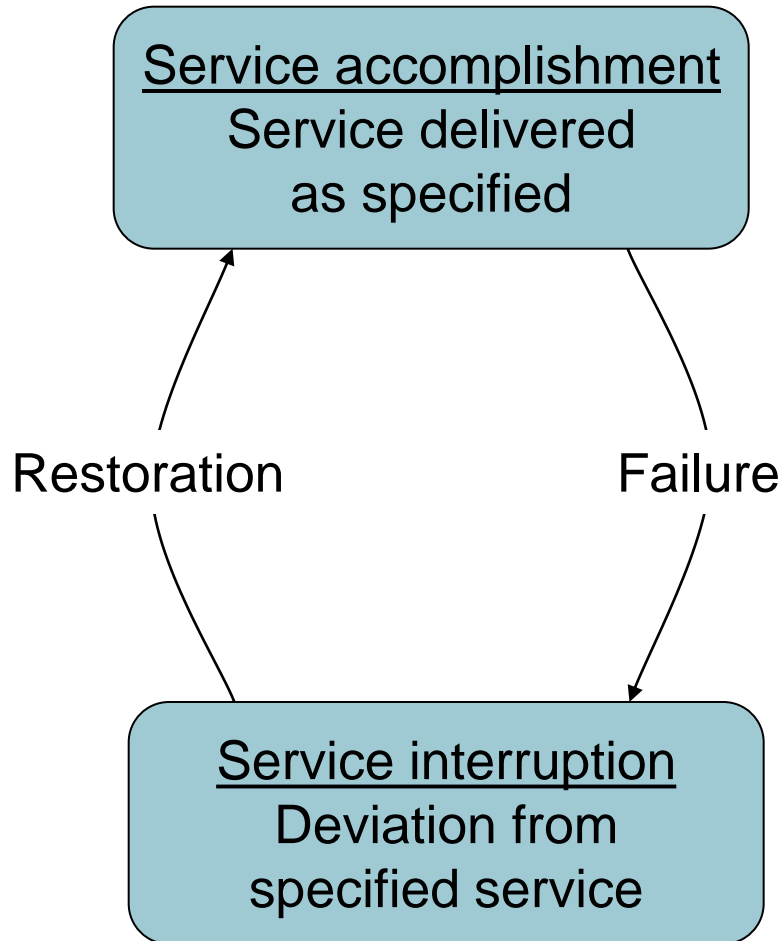
Blocked DGEMM Access Pattern



■ 32x32 ■ 160x160 ■ 480x480 ■ 960x960



Dependability



- Fault: failure of a component
 - May or may not lead to system failure

Dependability Measures

- Reliability: mean time to failure (MTTF)
- Service interruption: mean time to repair (MTTR)
- Mean time between failures
 - $MTBF = MTTF + MTTR$
- $Availability = MTTF / (MTTF + MTTR)$
- Improving Availability
 - Increase MTTF: fault avoidance, fault tolerance, fault forecasting
 - Reduce MTTR: improved tools and processes for diagnosis and repair

The Hamming SEC Code

- Hamming distance
 - Number of bits that are different between two bit patterns
- Minimum distance = 2 provides single bit error detection
 - E.g. parity code
- Minimum distance = 3 provides single error correction, 2 bit error detection

Encoding SEC

- To calculate Hamming code:
 - Number bits from 1 on the left
 - All bit positions that are a power 2 are parity bits
 - Each parity bit checks certain data bits:

| Bit position | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|---------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|
| Encoded data bits | | p1 | p2 | d1 | p4 | d2 | d3 | d4 | p8 | d5 | d6 | d7 | d8 |
| Parity bit coverage | p1 | X | | X | | X | | X | | X | | X | |
| | p2 | | X | X | | | X | X | | | X | X | |
| | p4 | | | | X | X | X | X | | | | | X |
| | p8 | | | | | | | | X | X | X | X | X |

Decoding SEC

- Value of parity bits indicates which bits are in error
 - Use numbering from encoding procedure
 - E.g.
 - Parity bits = 0000 indicates no error
 - Parity bits = 1010 indicates bit 10 was flipped

SEC/DEC Code

- Add an additional parity bit for the whole word (p_n)
- Make Hamming distance = 4
- Decoding:
 - Let H = SEC parity bits
 - H even, p_n even, no error
 - H odd, p_n odd, correctable single bit error
 - H even, p_n odd, error in p_n bit
 - H odd, p_n even, double error occurred
- Note: ECC DRAM uses SEC/DEC with 8 bits protecting each 64 bits

Virtual Machines

- Host computer emulates guest operating system and machine resources
 - Improved isolation of multiple guests
 - Avoids security and reliability problems
 - Aids sharing of resources
- Virtualization has some performance impact
 - Feasible with modern high-performance computers
- Examples
 - IBM VM/370 (1970s technology!)
 - VMWare
 - Microsoft Virtual PC

Virtual Machine Monitor

- Maps virtual resources to physical resources
 - Memory, I/O devices, CPUs
- Guest code runs on native machine in user mode
 - Traps to VMM on privileged instructions and access to protected resources
- Guest OS may be different from host OS
- VMM handles real I/O devices
 - Emulates generic virtual I/O devices for guest

Example: Timer Virtualization

- In native machine, on timer interrupt
 - OS suspends current process, handles interrupt, selects and resumes next process
- With Virtual Machine Monitor
 - VMM suspends current VM, handles interrupt, selects and resumes next VM
- If a VM requires timer interrupts
 - VMM emulates a virtual timer
 - Emulates interrupt for VM when physical timer interrupt occurs

Instruction Set Support

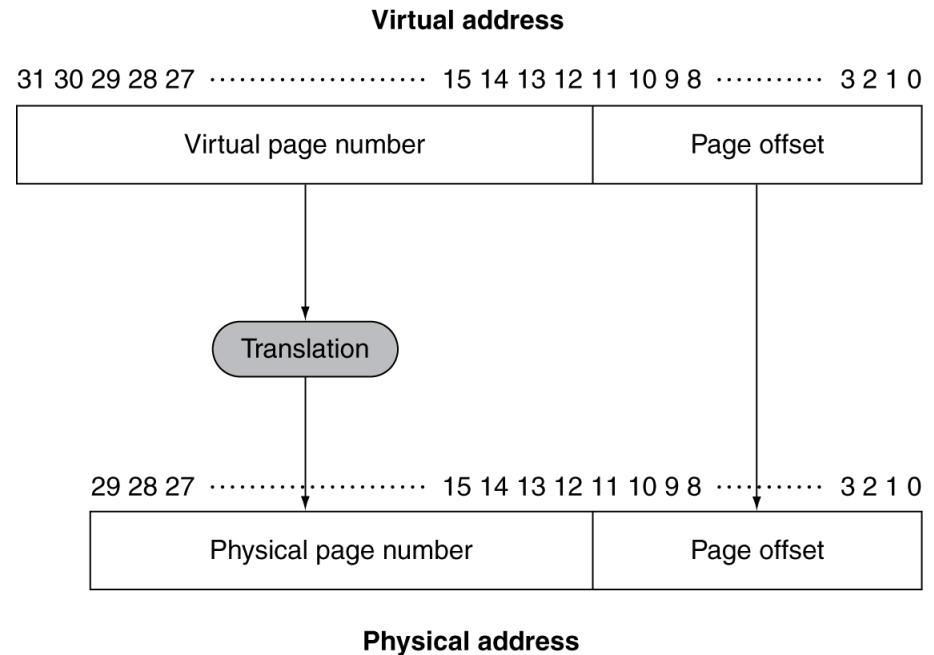
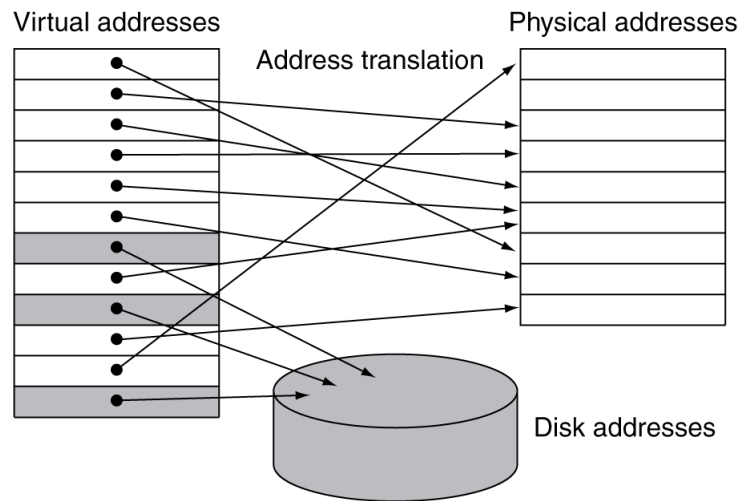
- User and System modes
- Privileged instructions only available in system mode
 - Trap to system if executed in user mode
- All physical resources only accessible using privileged instructions
 - Including page tables, interrupt controls, I/O registers
- Renaissance of virtualization support
 - Current ISAs (e.g., x86) adapting

Virtual Memory

- Use main memory as a “cache” for secondary (disk) storage
 - Managed jointly by CPU hardware and the operating system (OS)
- Programs share main memory
 - Each gets a private virtual address space holding its frequently used code and data
 - Protected from other programs
- CPU and OS translate virtual addresses to physical addresses
 - VM “block” is called a page
 - VM translation “miss” is called a page fault

Address Translation

- Fixed-size pages (e.g., 4K)



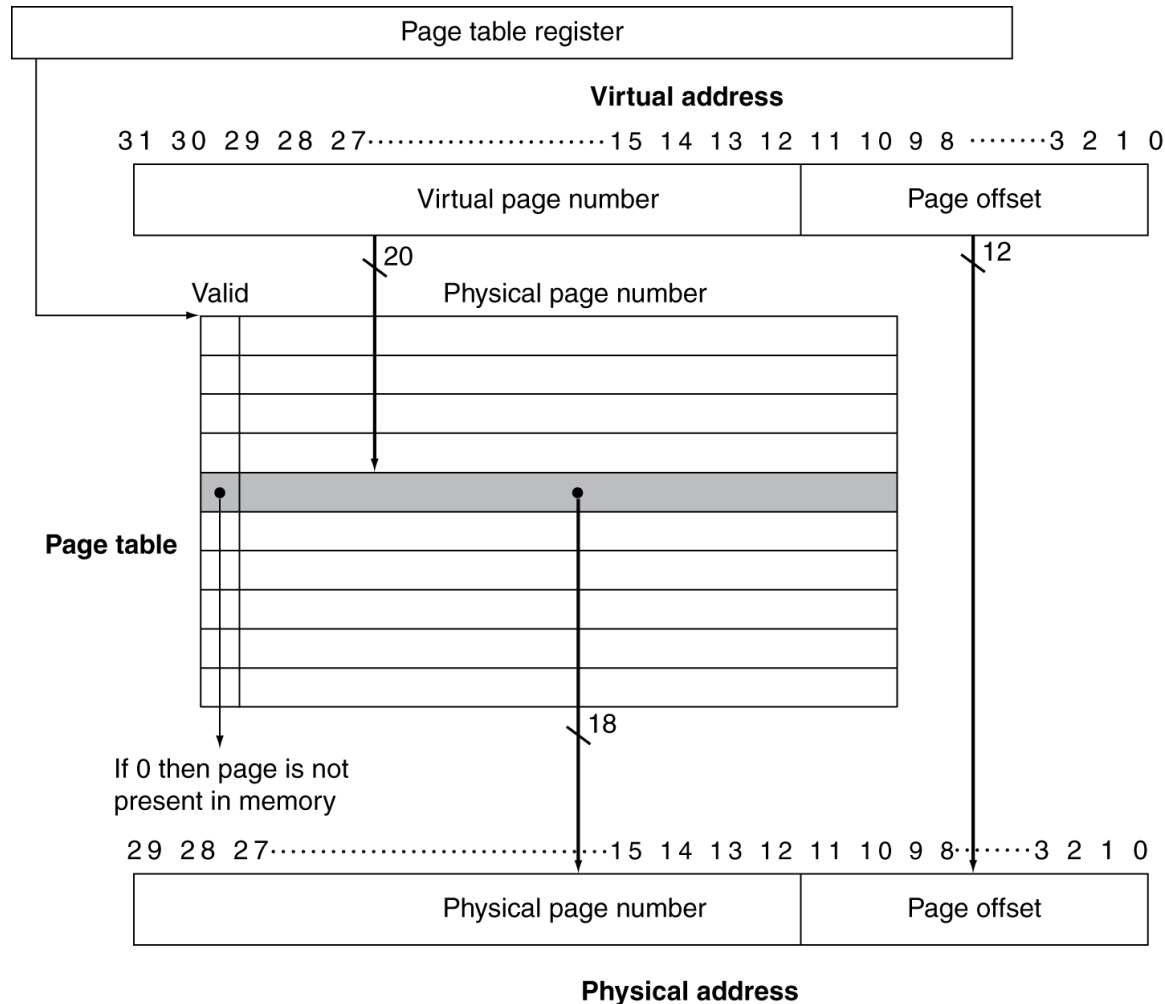
Page Fault Penalty

- On page fault, the page must be fetched from disk
 - Takes millions of clock cycles
 - Handled by OS code
- Try to minimize page fault rate
 - Fully associative placement
 - Smart replacement algorithms

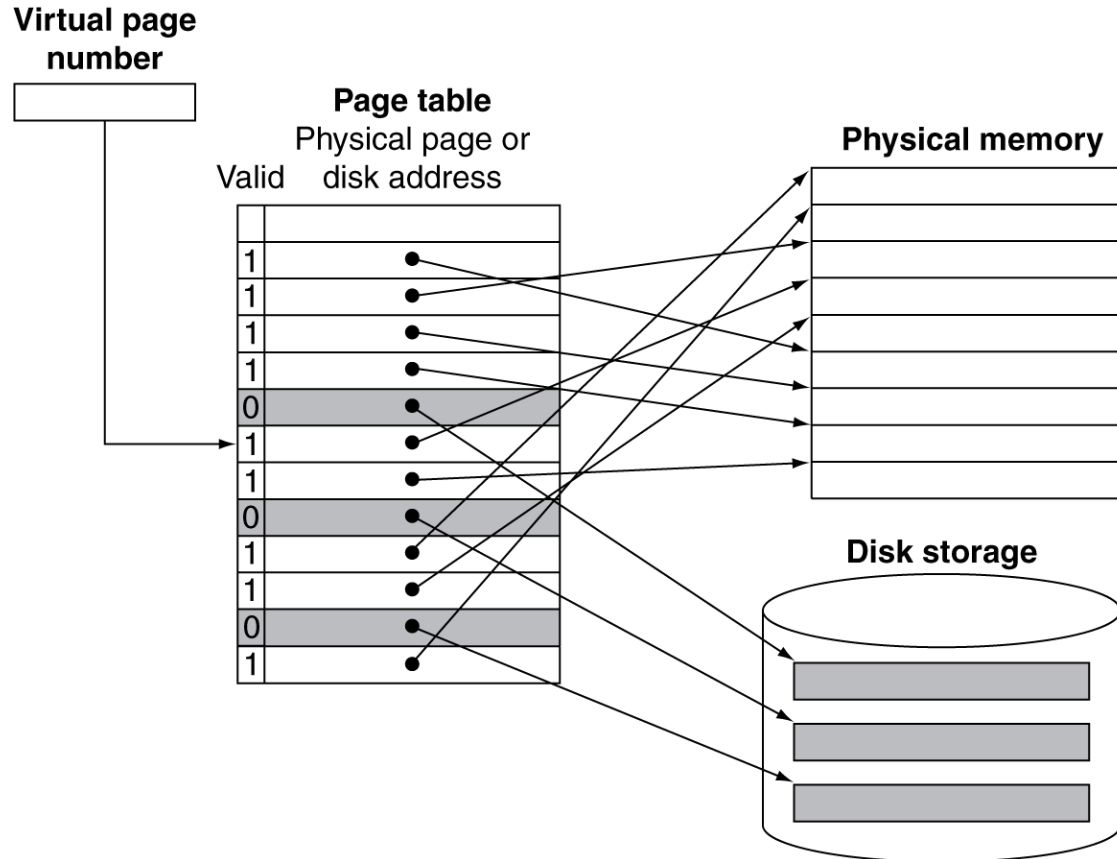
Page Tables

- Stores placement information
 - Array of page table entries, indexed by virtual page number
 - Page table register in CPU points to page table in physical memory
- If page is present in memory
 - PTE stores the physical page number
 - Plus other status bits (referenced, dirty, ...)
- If page is not present
 - PTE can refer to location in swap space on disk

Translation Using a Page Table



Mapping Pages to Storage



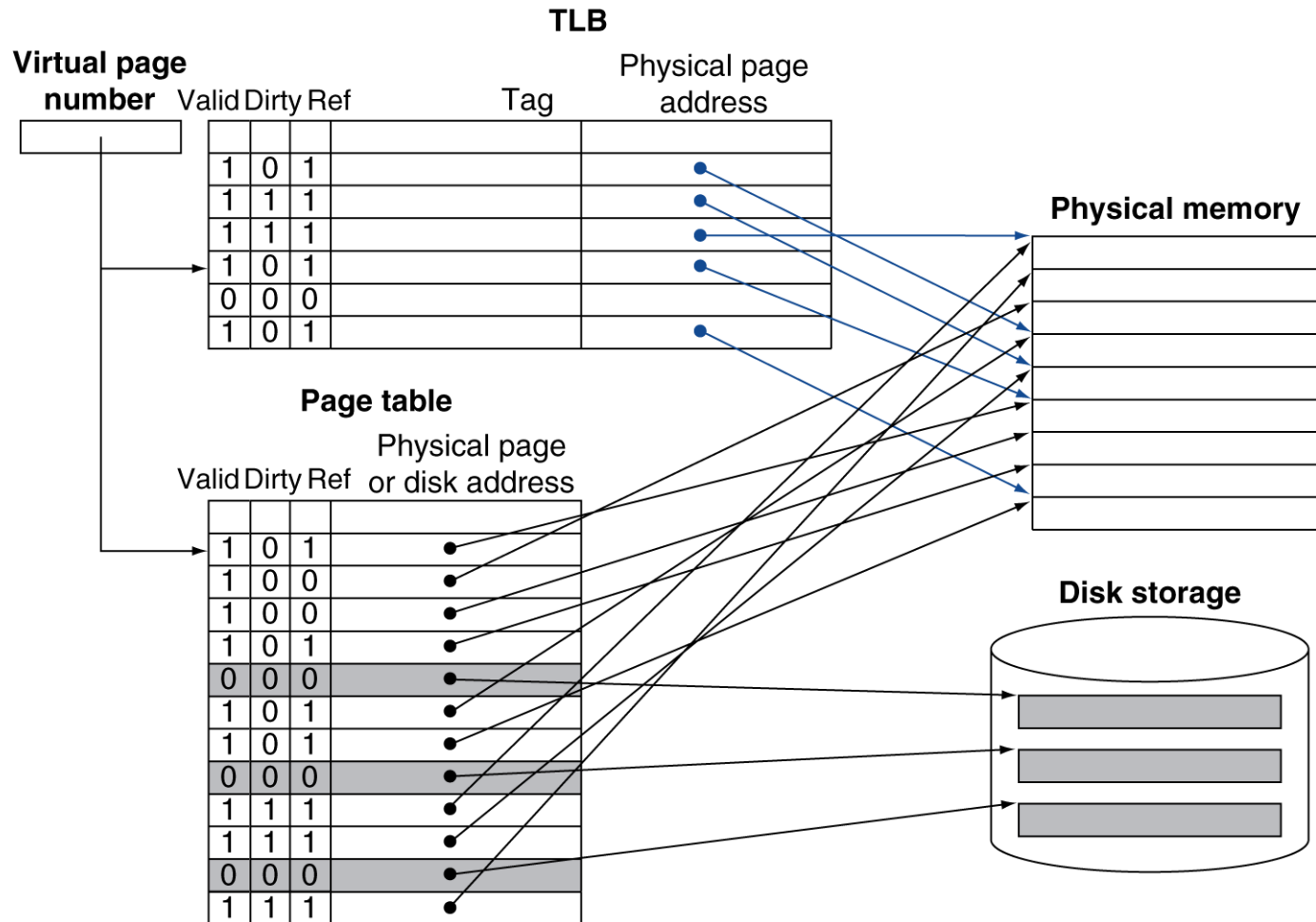
Replacement and Writes

- To reduce page fault rate, prefer least-recently used (LRU) replacement
 - Reference bit (aka use bit) in PTE set to 1 on access to page
 - Periodically cleared to 0 by OS
 - A page with reference bit = 0 has not been used recently
- Disk writes take millions of cycles
 - Block at once, not individual locations
 - Write through is impractical
 - Use write-back
 - Dirty bit in PTE set when page is written

Fast Translation Using a TLB

- Address translation would appear to require extra memory references
 - One to access the PTE
 - Then the actual memory access
- But access to page tables has good locality
 - So use a fast cache of PTEs within the CPU
 - Called a Translation Look-aside Buffer (TLB)
 - Typical: 16–512 PTEs, 0.5–1 cycle for hit, 10–100 cycles for miss, 0.01%–1% miss rate
 - Misses could be handled by hardware or software

Fast Translation Using a TLB



TLB Misses

- If page is in memory
 - Load the PTE from memory and retry
 - Could be handled in hardware
 - Can get complex for more complicated page table structures
 - Or in software
 - Raise a special exception, with optimized handler
- If page is not in memory (page fault)
 - OS handles fetching the page and updating the page table
 - Then restart the faulting instruction

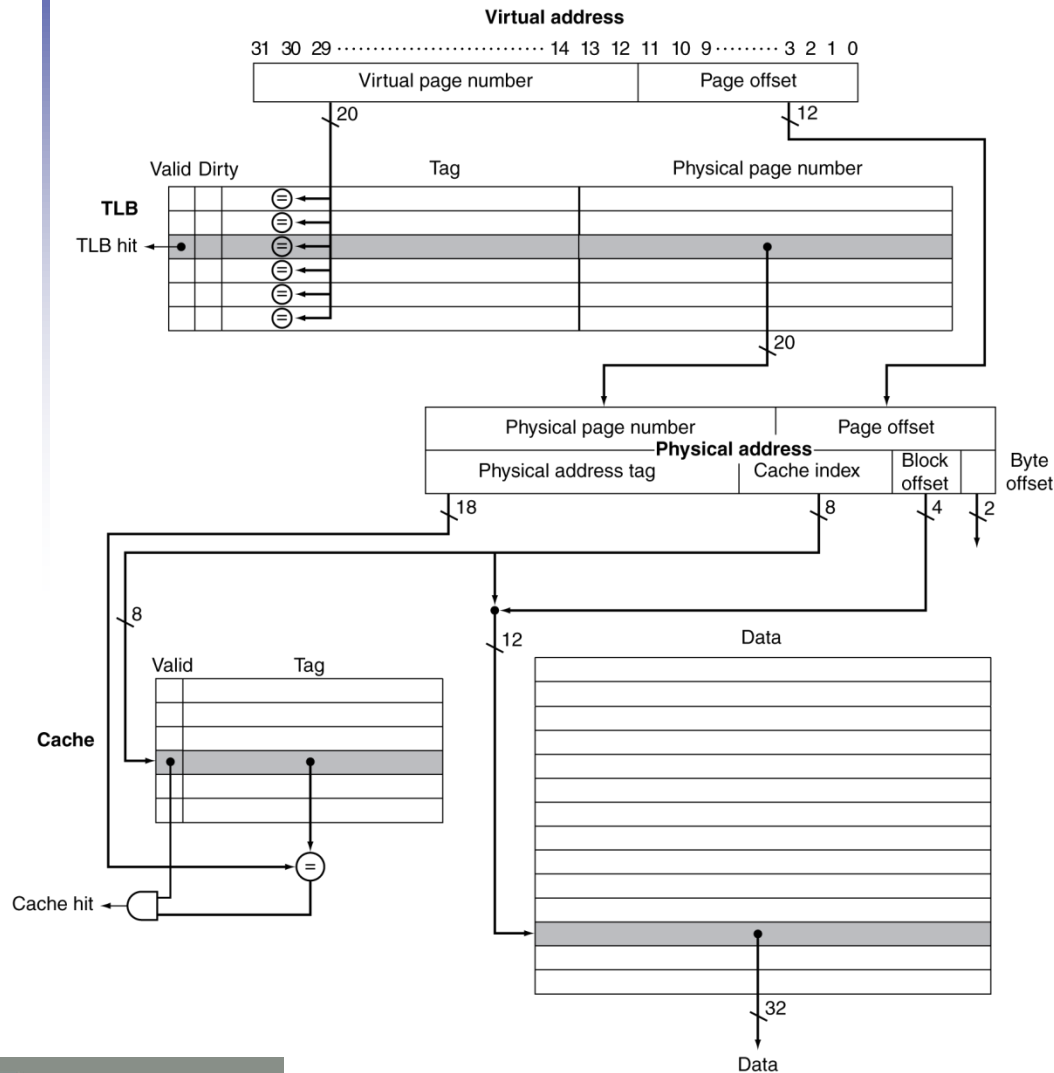
TLB Miss Handler

- TLB miss indicates
 - Page present, but PTE not in TLB
 - Page not present
- Must recognize TLB miss before destination register overwritten
 - Raise exception
- Handler copies PTE from memory to TLB
 - Then restarts instruction
 - If page not present, page fault will occur

Page Fault Handler

- Use faulting virtual address to find PTE
- Locate page on disk
- Choose page to replace
 - If dirty, write to disk first
- Read page into memory and update page table
- Make process runnable again
 - Restart from faulting instruction

TLB and Cache Interaction



- If cache tag uses physical address
 - Need to translate before cache lookup
- Alternative: use virtual address tag
 - Complications due to aliasing
 - Different virtual addresses for shared physical address

Memory Protection

- Different tasks can share parts of their virtual address spaces
 - But need to protect against errant access
 - Requires OS assistance
- Hardware support for OS protection
 - Privileged supervisor mode (aka kernel mode)
 - Privileged instructions
 - Page tables and other state information only accessible in supervisor mode
 - System call exception (e.g., syscall in MIPS)

The Memory Hierarchy

The BIG Picture

- Common principles apply at all levels of the memory hierarchy
 - Based on notions of caching
- At each level in the hierarchy
 - Block placement
 - Finding a block
 - Replacement on a miss
 - Write policy

Block Placement

- Determined by associativity
 - Direct mapped (1-way associative)
 - One choice for placement
 - n-way set associative
 - n choices within a set
 - Fully associative
 - Any location
- Higher associativity reduces miss rate
 - Increases complexity, cost, and access time

Finding a Block

| Associativity | Location method | Tag comparisons |
|-----------------------|---|-----------------|
| Direct mapped | Index | 1 |
| n-way set associative | Set index, then search entries within the set | n |
| Fully associative | Search all entries | #entries |
| | Full lookup table | 0 |

- Hardware caches
 - Reduce comparisons to reduce cost
- Virtual memory
 - Full table lookup makes full associativity feasible
 - Benefit in reduced miss rate

Replacement

- Choice of entry to replace on a miss
 - Least recently used (LRU)
 - Complex and costly hardware for high associativity
 - Random
 - Close to LRU, easier to implement
- Virtual memory
 - LRU approximation with hardware support

Write Policy

- Write-through
 - Update both upper and lower levels
 - Simplifies replacement, but may require write buffer
- Write-back
 - Update upper level only
 - Update lower level when block is replaced
 - Need to keep more state
- Virtual memory
 - Only write-back is feasible, given disk write latency

Sources of Misses

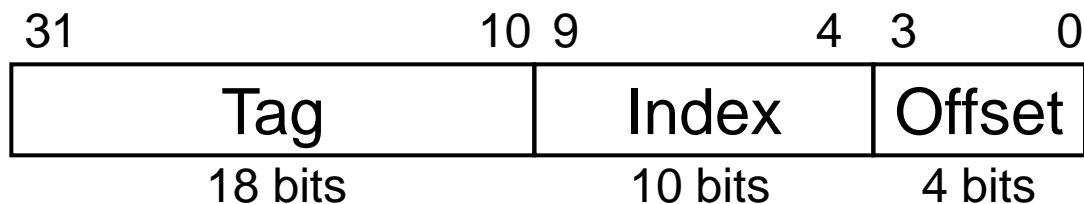
- Compulsory misses (aka cold start misses)
 - First access to a block
- Capacity misses
 - Due to finite cache size
 - A replaced block is later accessed again
- Conflict misses (aka collision misses)
 - In a non-fully associative cache
 - Due to competition for entries in a set
 - Would not occur in a fully associative cache of the same total size

Cache Design Trade-offs

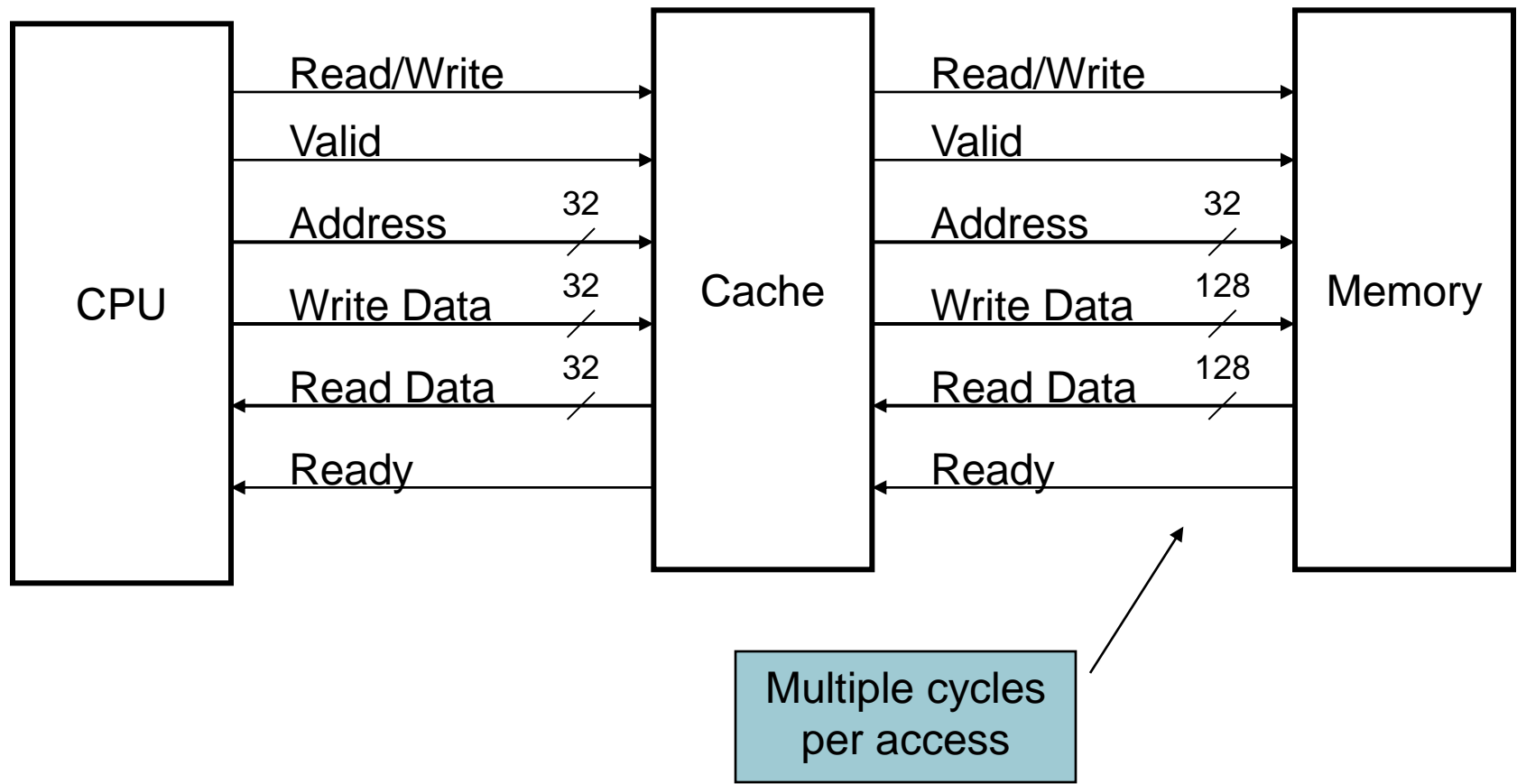
| Design change | Effect on miss rate | Negative performance effect |
|------------------------|----------------------------|---|
| Increase cache size | Decrease capacity misses | May increase access time |
| Increase associativity | Decrease conflict misses | May increase access time |
| Increase block size | Decrease compulsory misses | Increases miss penalty. For very large block size, may increase miss rate due to pollution. |

Cache Control

- Example cache characteristics
 - Direct-mapped, write-back, write allocate
 - Block size: 4 words (16 bytes)
 - Cache size: 16 KB (1024 blocks)
 - 32-bit byte addresses
 - Valid bit and dirty bit per block
 - Blocking cache
 - CPU waits until access is complete

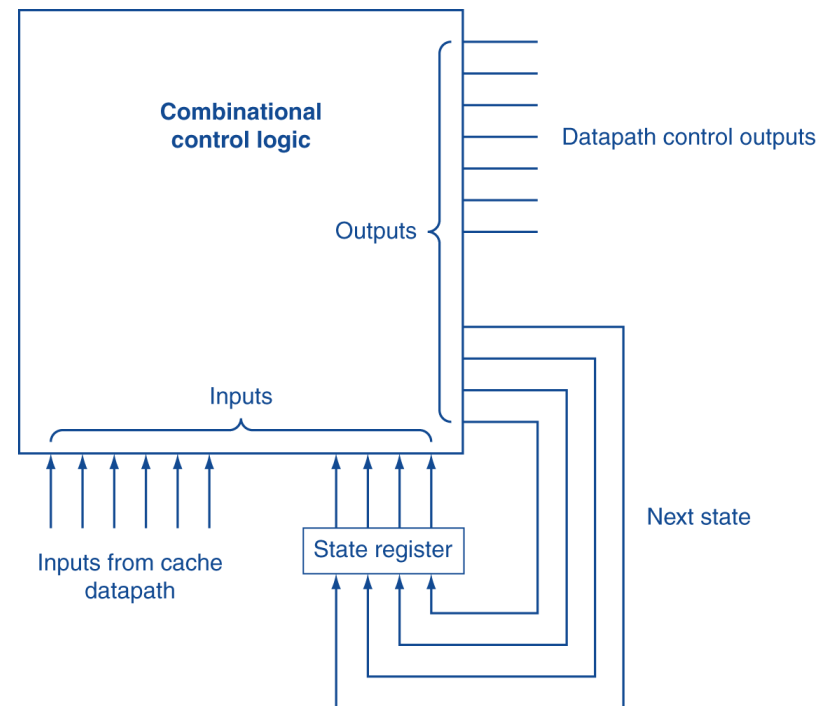


Interface Signals

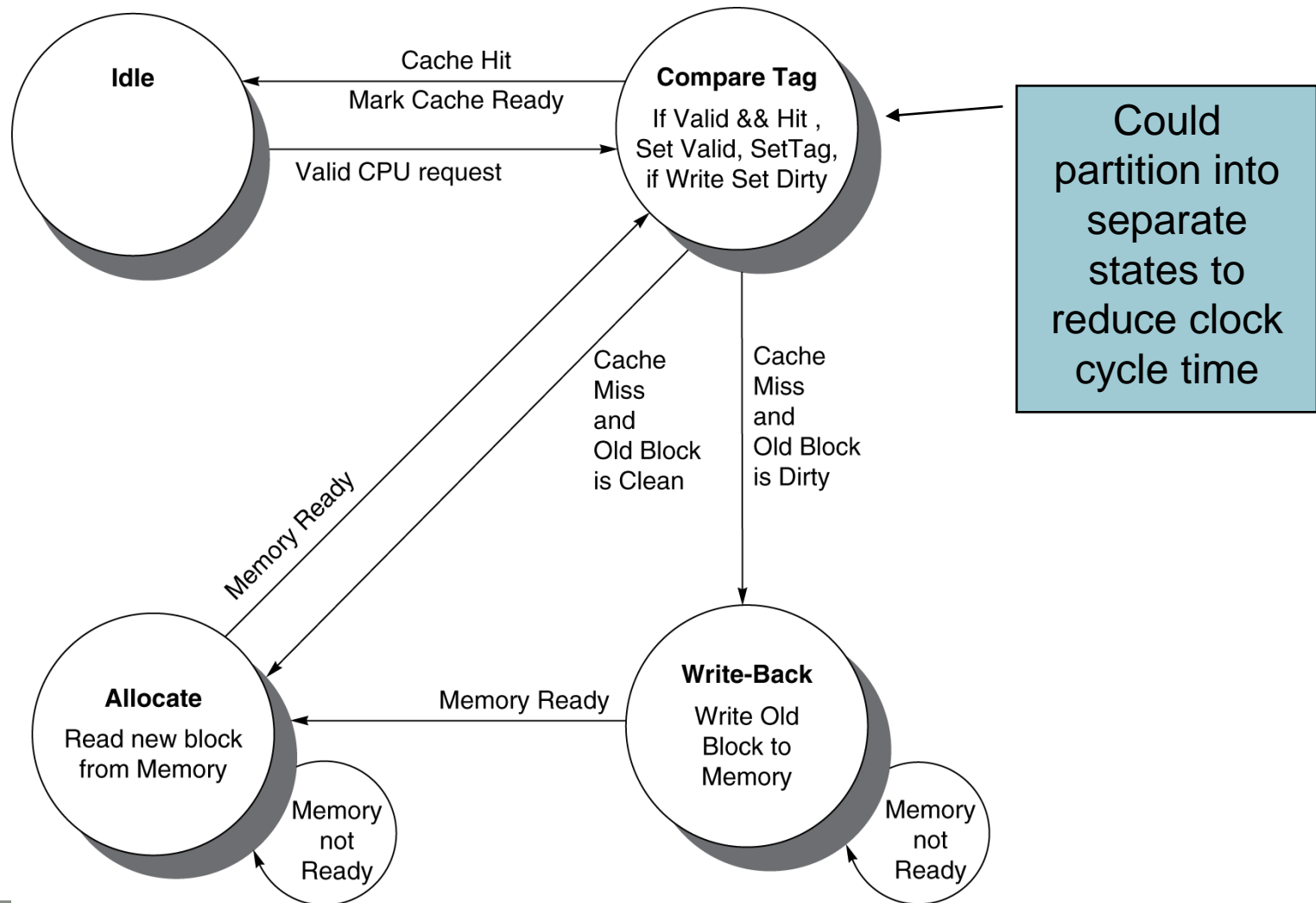


Finite State Machines

- Use an FSM to sequence control steps
- Set of states, transition on each clock edge
 - State values are binary encoded
 - Current state stored in a register
 - Next state = f_n (current state, current inputs)
- Control output signals = f_o (current state)



Cache Controller FSM



Cache Coherence Problem

- Suppose two CPU cores share a physical address space
 - Write-through caches

| Time step | Event | CPU A's cache | CPU B's cache | Memory |
|-----------|---------------------|---------------|---------------|--------|
| 0 | | | | 0 |
| 1 | CPU A reads X | 0 | | 0 |
| 2 | CPU B reads X | 0 | 0 | 0 |
| 3 | CPU A writes 1 to X | 1 | 0 | 1 |

Coherence Defined

- Informally: Reads return most recently written value
- Formally:
 - P writes X ; P reads X (no intervening writes)
 \Rightarrow read returns written value
 - P_1 writes X ; P_2 reads X (sufficiently later)
 \Rightarrow read returns written value
 - c.f. CPU B reading X after step 3 in example
 - P_1 writes X , P_2 writes X
 \Rightarrow all processors see writes in the same order
 - End up with the same final value for X

Cache Coherence Protocols

- Operations performed by caches in multiprocessors to ensure coherence
 - Migration of data to local caches
 - Reduces bandwidth for shared memory
 - Replication of read-shared data
 - Reduces contention for access
- Snooping protocols
 - Each cache monitors bus reads/writes
- Directory-based protocols
 - Caches and memory record sharing status of blocks in a directory

Invalidating Snooping Protocols

- Cache gets exclusive access to a block when it is to be written
 - Broadcasts an invalidate message on the bus
 - Subsequent read in another cache misses
 - Owning cache supplies updated value

| CPU activity | Bus activity | CPU A's cache | CPU B's cache | Memory |
|---------------------|------------------|---------------|---------------|--------|
| | | | | 0 |
| CPU A reads X | Cache miss for X | 0 | | 0 |
| CPU B reads X | Cache miss for X | 0 | 0 | 0 |
| CPU A writes 1 to X | Invalidate for X | 1 | | 0 |
| CPU B read X | Cache miss for X | 1 | 1 | 1 |

Memory Consistency

- When are writes seen by other processors
 - “Seen” means a read returns the written value
 - Can’t be instantaneously
- Assumptions
 - A write completes only when all processors have seen it
 - A processor does not reorder writes with other accesses
- Consequence
 - P writes X then writes Y
⇒ all processors that see new Y also see new X
 - Processors can reorder reads, but not writes

Multilevel On-Chip Caches

| Characteristic | ARM Cortex-A8 | Intel Nehalem |
|------------------------|--------------------------------------|--|
| L1 cache organization | Split instruction and data caches | Split instruction and data caches |
| L1 cache size | 32 KiB each for instructions/data | 32 KiB each for instructions/data per core |
| L1 cache associativity | 4-way (I), 4-way (D) set associative | 4-way (I), 8-way (D) set associative |
| L1 replacement | Random | Approximated LRU |
| L1 block size | 64 bytes | 64 bytes |
| L1 write policy | Write-back, Write-allocate(?) | Write-back, No-write-allocate |
| L1 hit time (load-use) | 1 clock cycle | 4 clock cycles, pipelined |
| L2 cache organization | Unified (instruction and data) | Unified (instruction and data) per core |
| L2 cache size | 128 KiB to 1 MiB | 256 KiB (0.25 MiB) |
| L2 cache associativity | 8-way set associative | 8-way set associative |
| L2 replacement | Random(?) | Approximated LRU |
| L2 block size | 64 bytes | 64 bytes |
| L2 write policy | Write-back, Write-allocate (?) | Write-back, Write-allocate |
| L2 hit time | 11 clock cycles | 10 clock cycles |
| L3 cache organization | - | Unified (instruction and data) |
| L3 cache size | - | 8 MiB, shared |
| L3 cache associativity | - | 16-way set associative |
| L3 replacement | - | Approximated LRU |
| L3 block size | - | 64 bytes |
| L3 write policy | - | Write-back, Write-allocate |
| L3 hit time | - | 35 clock cycles |

2-Level TLB Organization

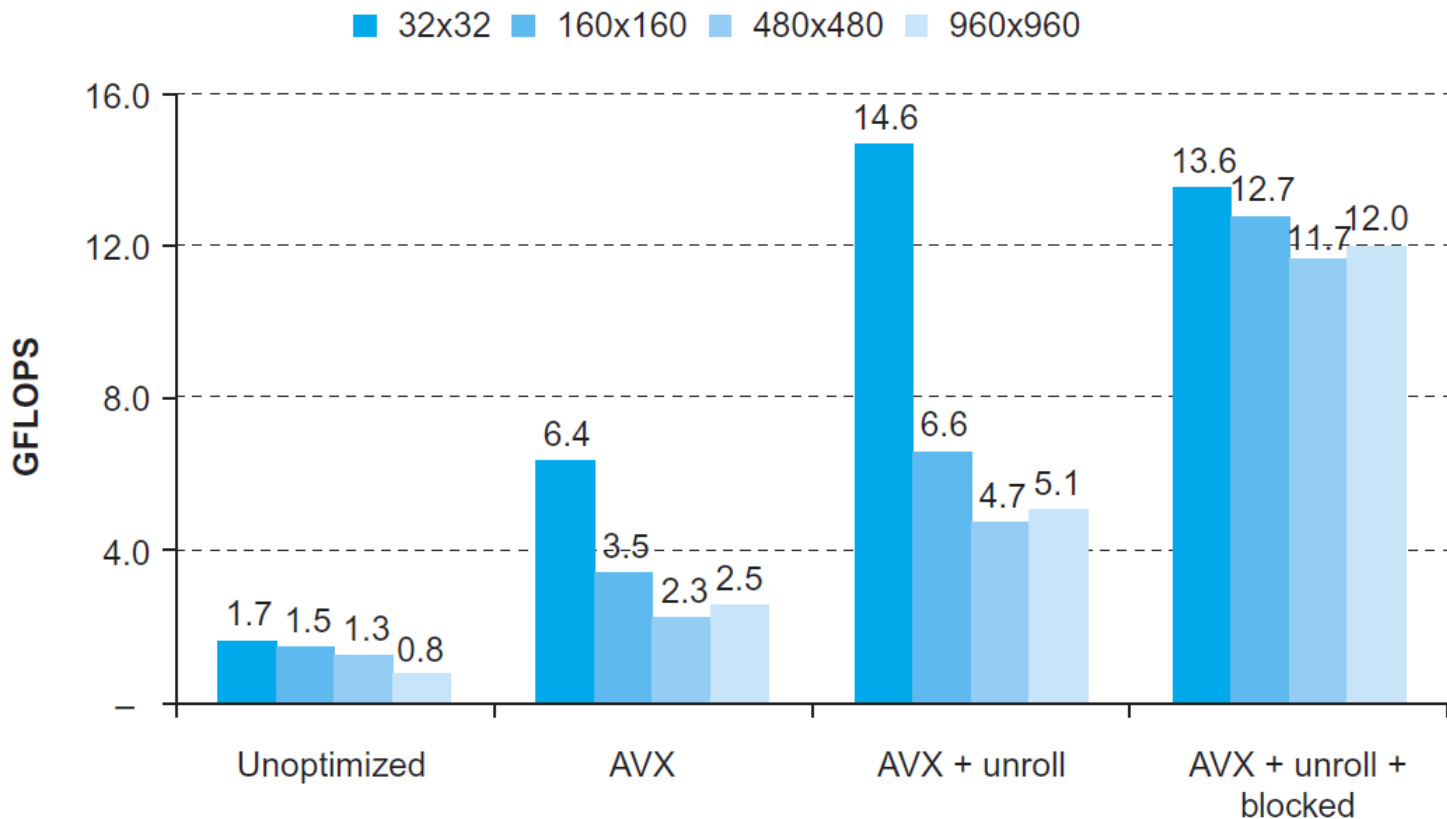
| Characteristic | ARM Cortex-A8 | Intel Core i7 |
|------------------|---|---|
| Virtual address | 32 bits | 48 bits |
| Physical address | 32 bits | 44 bits |
| Page size | Variable: 4, 16, 64 KiB, 1, 16 MiB | Variable: 4 KiB, 2/4 MiB |
| TLB organization | <p>1 TLB for instructions and 1 TLB for data</p> <p>Both TLBs are fully associative, with 32 entries, round robin replacement</p> <p>TLB misses handled in hardware</p> | <p>1 TLB for instructions and 1 TLB for data per core</p> <p>Both L1 TLBs are four-way set associative, LRU replacement</p> <p>L1 I-TLB has 128 entries for small pages, 7 per thread for large pages</p> <p>L1 D-TLB has 64 entries for small pages, 32 for large pages</p> <p>The L2 TLB is four-way set associative, LRU replacement</p> <p>The L2 TLB has 512 entries</p> <p>TLB misses handled in hardware</p> |

Supporting Multiple Issue

- Both have multi-banked caches that allow multiple accesses per cycle assuming no bank conflicts
- Core i7 cache optimizations
 - Return requested word first
 - Non-blocking cache
 - Hit under miss
 - Miss under miss
 - Data prefetching

DGEMM

- Combine cache blocking and subword parallelism



Pitfalls

- Byte vs. word addressing
 - Example: 32-byte direct-mapped cache, 4-byte blocks
 - Byte 36 maps to block 1
 - Word 36 maps to block 4
- Ignoring memory system effects when writing or generating code
 - Example: iterating over rows vs. columns of arrays
 - Large strides result in poor locality

Pitfalls

- In multiprocessor with shared L2 or L3 cache
 - Less associativity than cores results in conflict misses
 - More cores \Rightarrow need to increase associativity
- Using AMAT to evaluate performance of out-of-order processors
 - Ignores effect of non-blocked accesses
 - Instead, evaluate performance by simulation

Pitfalls

- Extending address range using segments
 - E.g., Intel 80286
 - But a segment is not always big enough
 - Makes address arithmetic complicated
- Implementing a VMM on an ISA not designed for virtualization
 - E.g., non-privileged instructions accessing hardware resources
 - Either extend ISA, or require guest OS not to use problematic instructions

Concluding Remarks

- Fast memories are small, large memories are slow
 - We really want fast, large memories ☹️
 - Caching gives this illusion 😊
- Principle of locality
 - Programs use a small part of their memory space frequently
- Memory hierarchy
 - L1 cache ↔ L2 cache ↔ ... ↔ DRAM memory ↔ disk
- Memory system design is critical for multiprocessors