

Modeling Variability

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Maître de Conférences

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Material

<http://mathieuacher.com/teaching/MDE/MRI1516/>

Plan

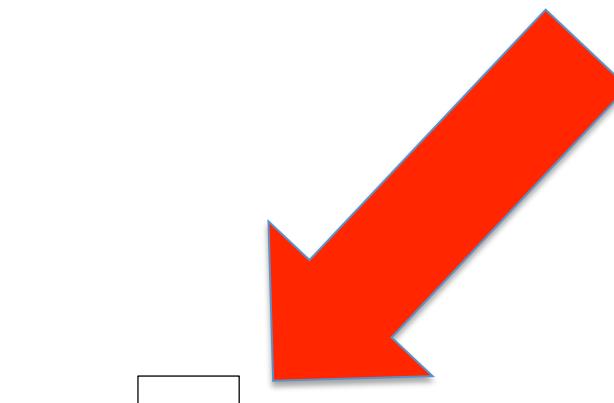
- Challenges and Overview
 - Developping billions of software product is hard but now a common practice
- Implementing Variability
 - Revisit of existing techniques and curriculum
- Specificity of Product Line Engineering
 - Process, methods
- Feature Models
 - **Defacto standard for modeling product lines and variability**
 - **Syntax, semantics, automated reasoning, synthesis**

Contract

- The idea of software product lines and variability
 - You will be able to recognize this class of systems
 - Aware of the complexity, the specific development process, and existing techniques
- **Feature modeling**
 - A widely used formalism for modeling product lines and configurable systems in a broad sense
- **Composing/Decomposing feature models with a domain-specific language**
- **Reverse engineering variability models**

Modeling Variability

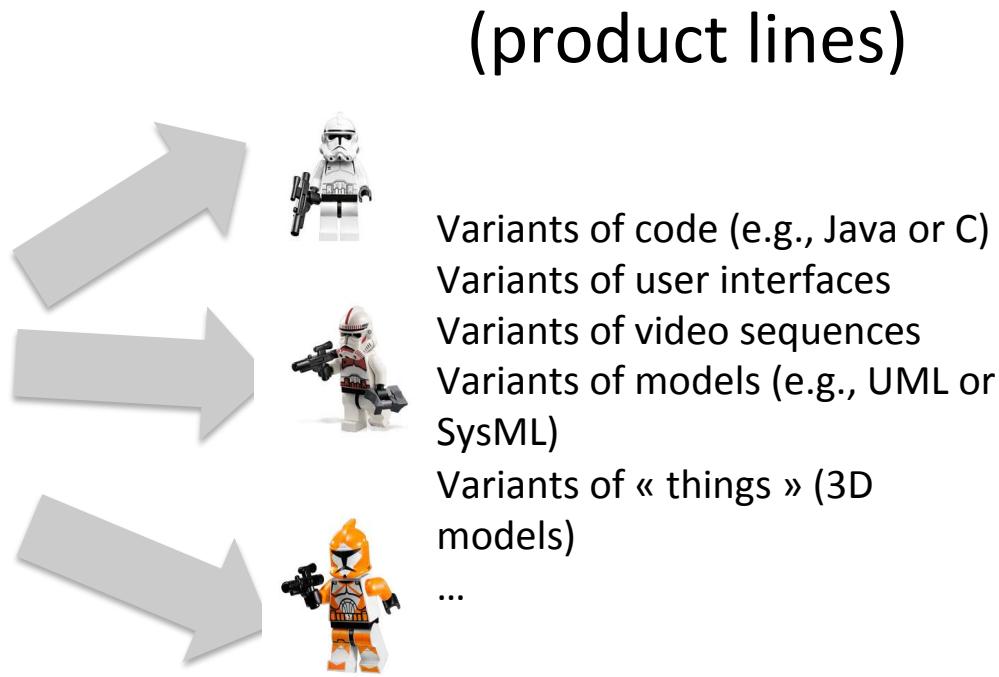
Modeling and Reverse Engineering Variability



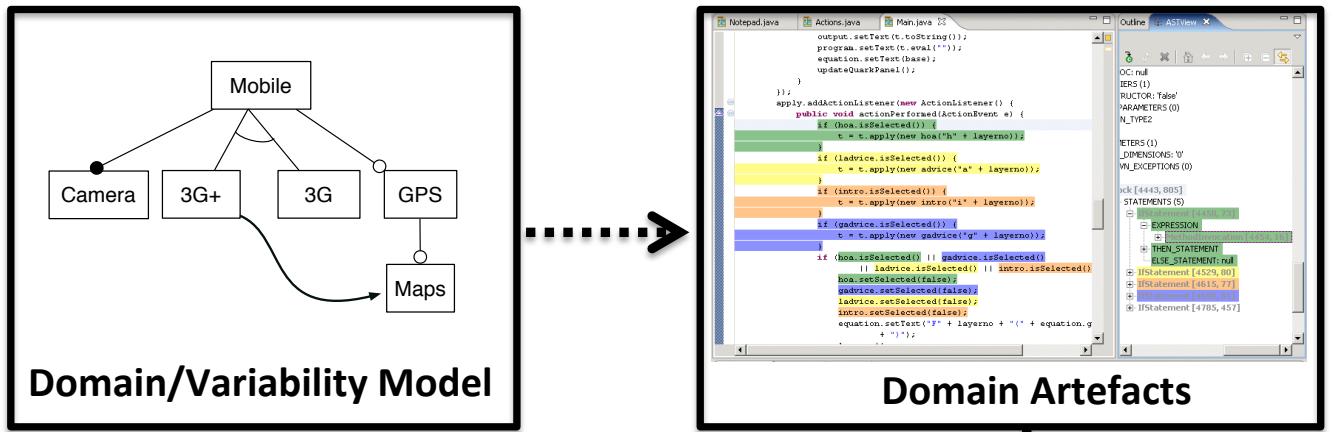
not, and, or, implies

Product	License	Price	Language Support	Language	WYSIWIG
W1	Commercial	10	Yes	Java	Yes
W2	NoLimit	20	No		Yes
W3	NoLimit	10	No		Yes
W4	GPL	0	Yes	Python	Yes
W5	GPL	0	Yes	Perl	Yes
W6	GPL	10	Yes	Perl	Yes
W7	GPL	0	Yes	PHP	No
W8	GPL	10	Yes	PHP	Yes

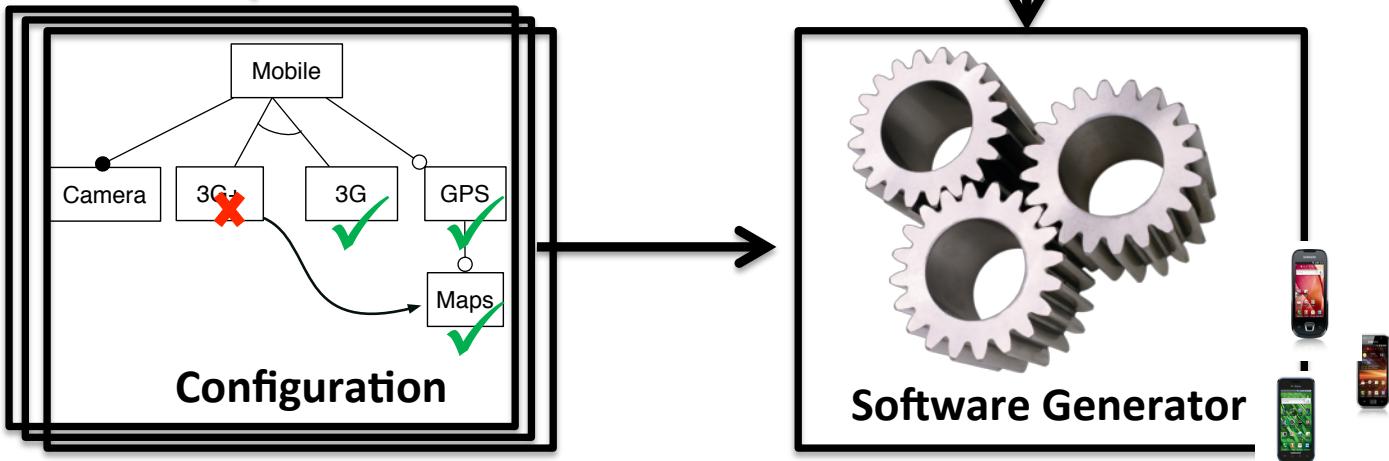
Feature models
or Product Matrices



Domain Engineering

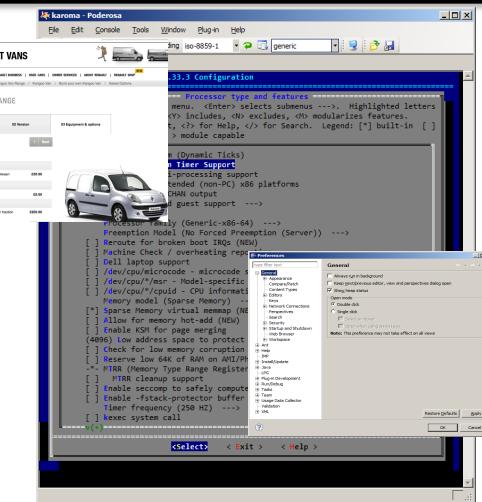


Application Engineering

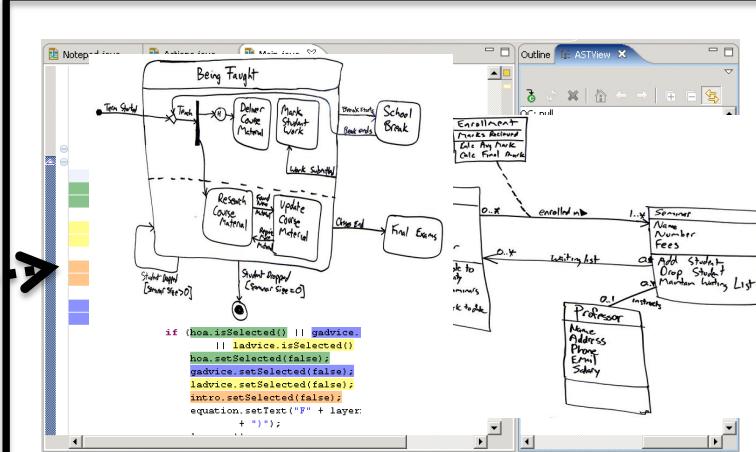


« the investments required to develop the reusable artifacts during **domain engineering**, are outweighed by the benefits of deriving the individual products during **application engineering** »

Jan Bosch et al. (2004)



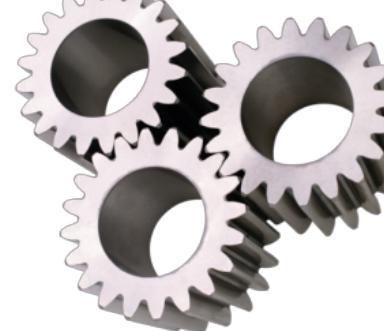
Variability Model



Base Artefacts (e.g., models)



Configuration



Software Generator (derivation engine)



Quizz: what are the constraints over WORLD and BYE?

```
#include <stdio.h>

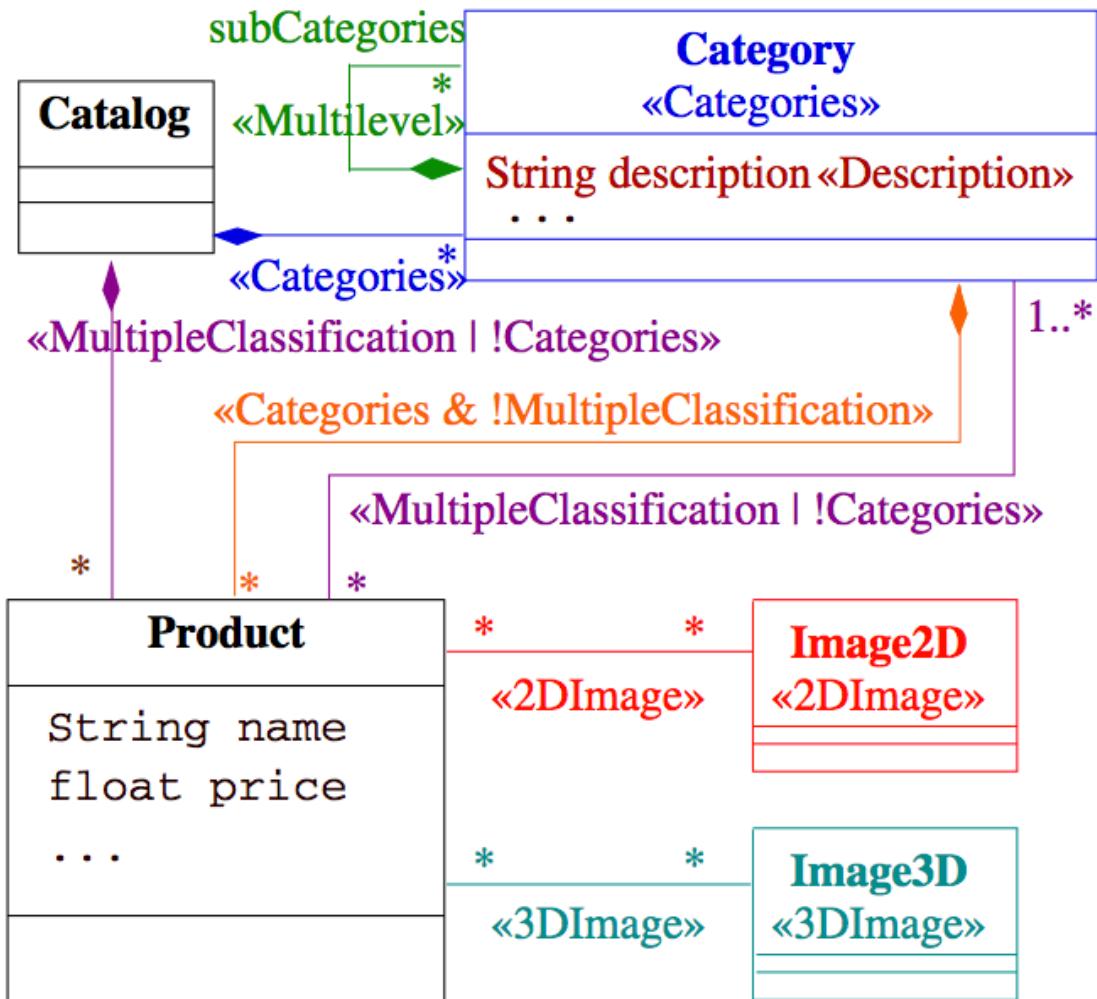
#ifndef WORLD
char * msg = "Hello_World\n";
#endif

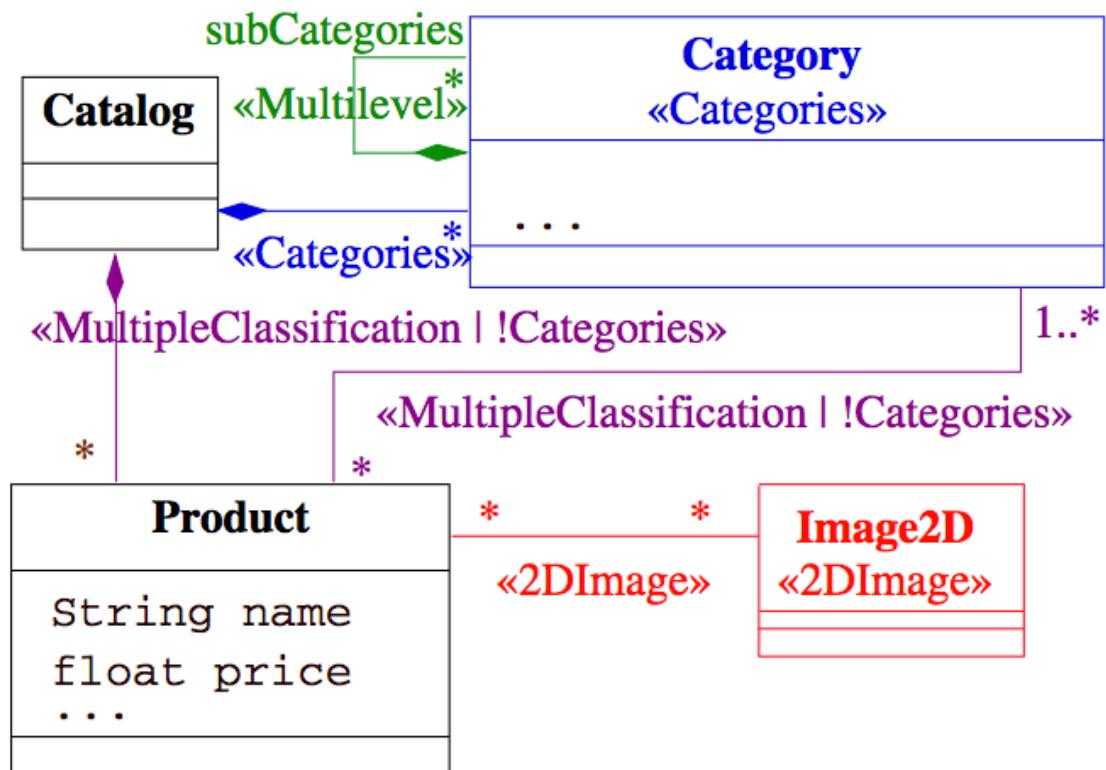
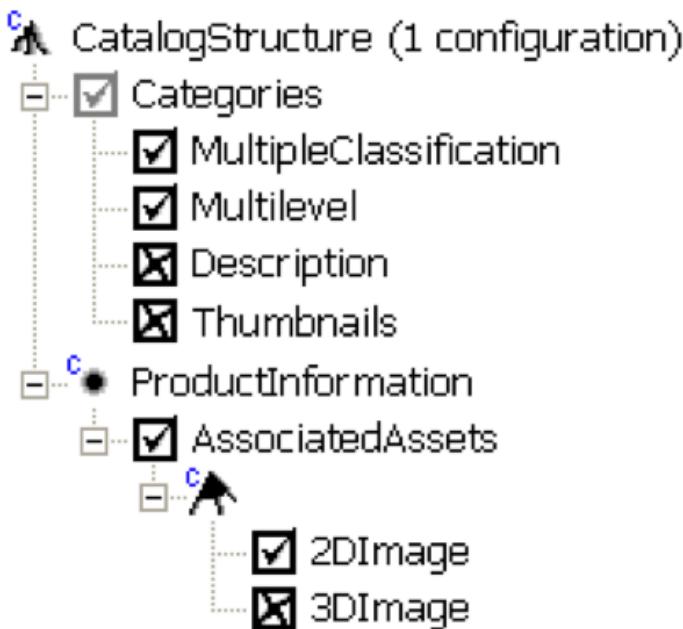
#ifndef BYE
char * msg = "Bye_bye!\n";
#endif

main() {
    printf(msg);
}
```

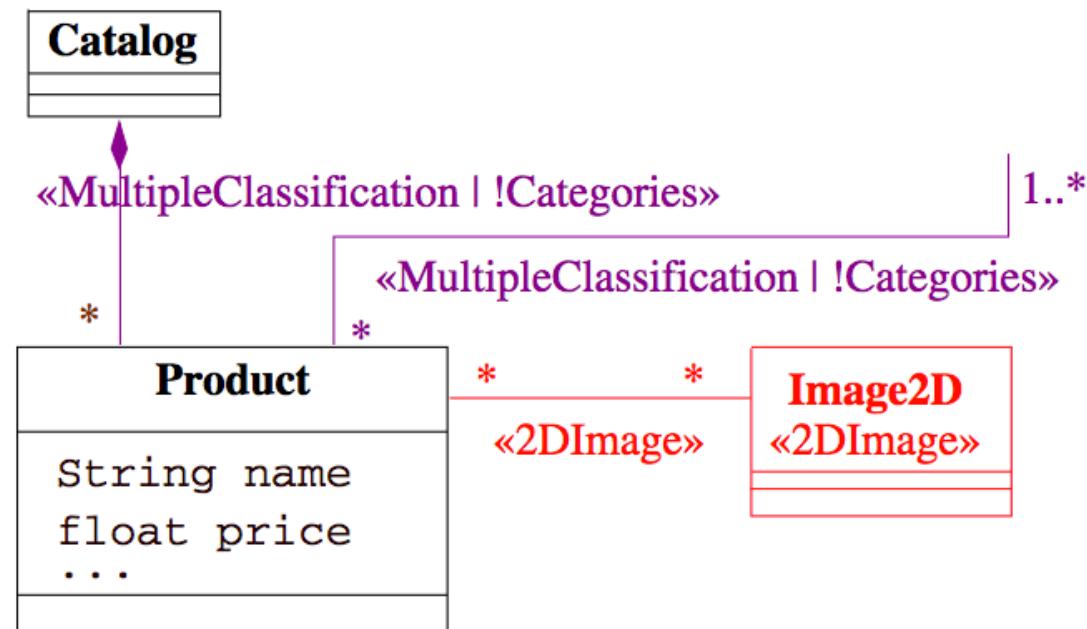
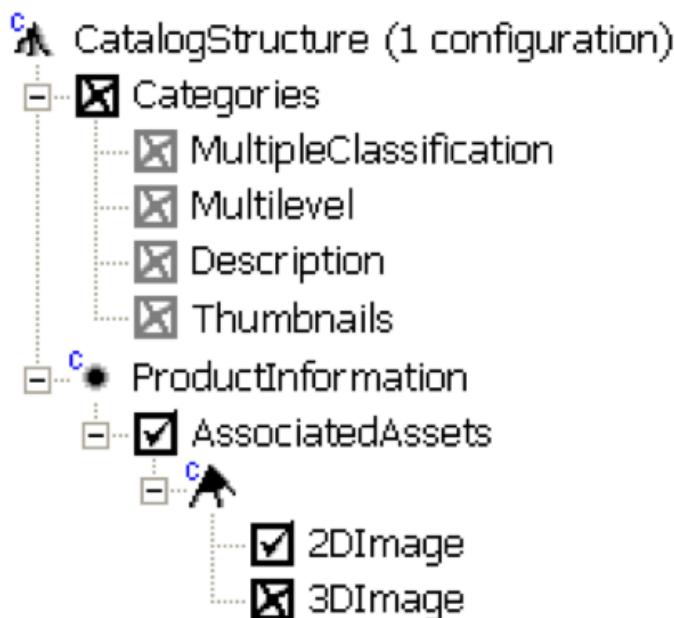
▲ CatalogStructure (52 configurations)

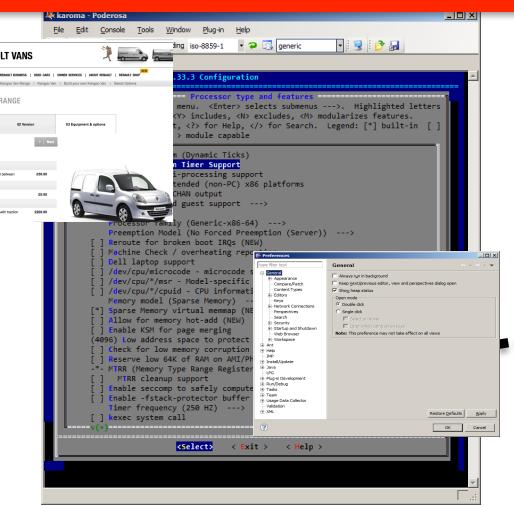
- Categories
 - MultipleClassification
 - Multilevel
 - Description
 - Thumbnails
- ProductInformation
 - AssociatedAssets
 - 2DImage
 - 3DImage





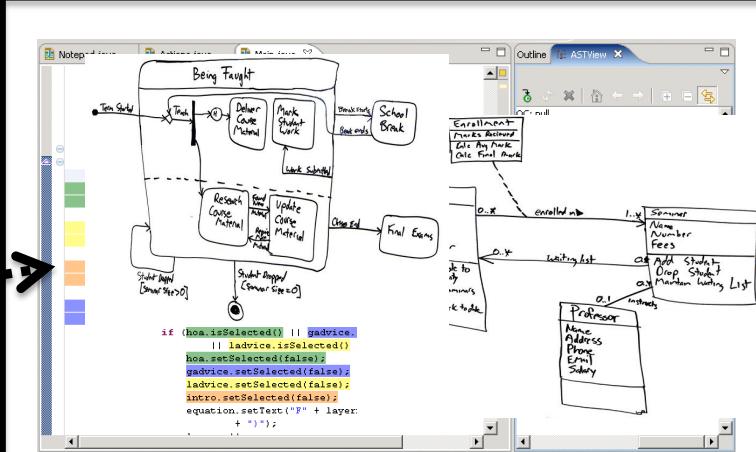
Ooops





Variability Model

mapping



Base Artefacts (e.g.,
models)



Configuration



Software Generator
(derivation engine)



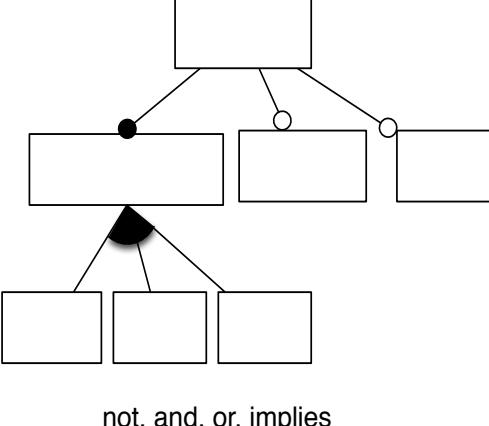
A photograph of an old, green-painted pickup truck that has been left to decay in a field. The truck is heavily rusted, particularly on the body and the front fenders. The driver's side door is open, revealing the interior frame and some remaining mechanical components. The truck is positioned in front of a dense thicket of green bushes and tall grass. In the bottom left corner, there are some wooden planks and metal debris, suggesting a construction or demolition site nearby.

Unused flexibility

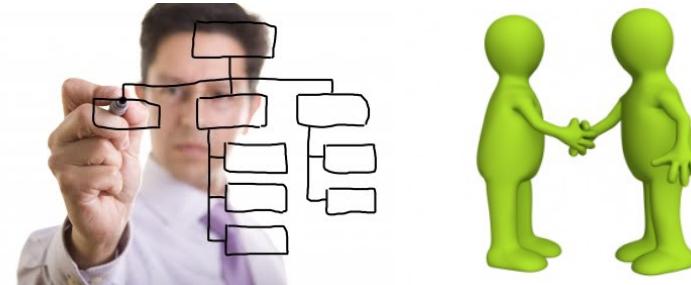


Illegal variant

Feature Model



Communicative



Analytic

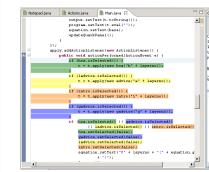
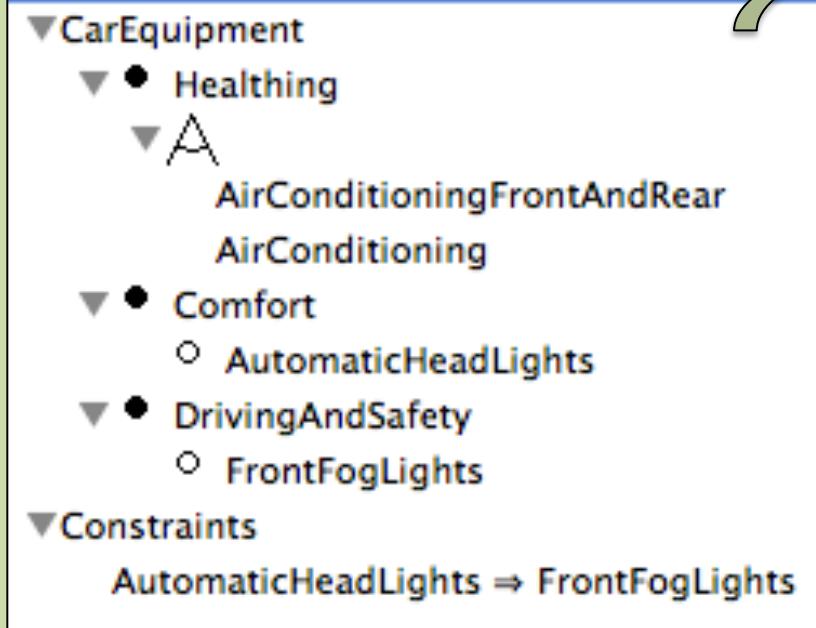


Generative



Feature Models

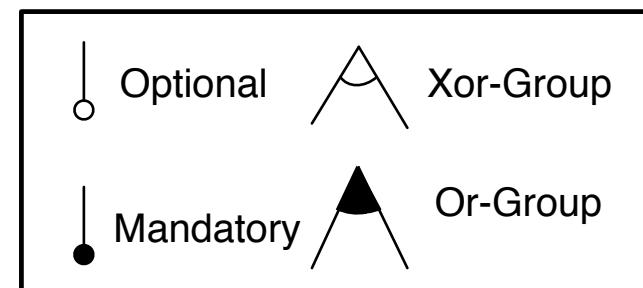
(defacto standard for modeling variability)

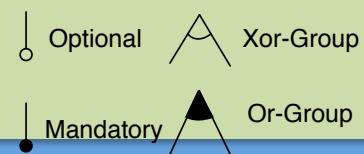
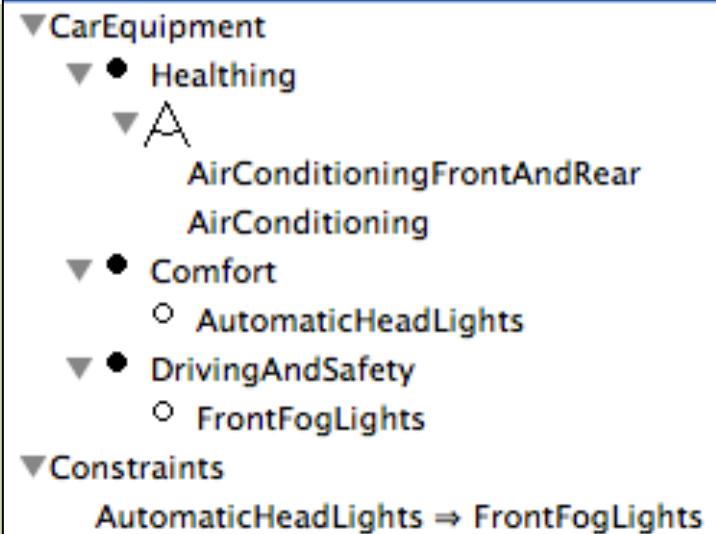
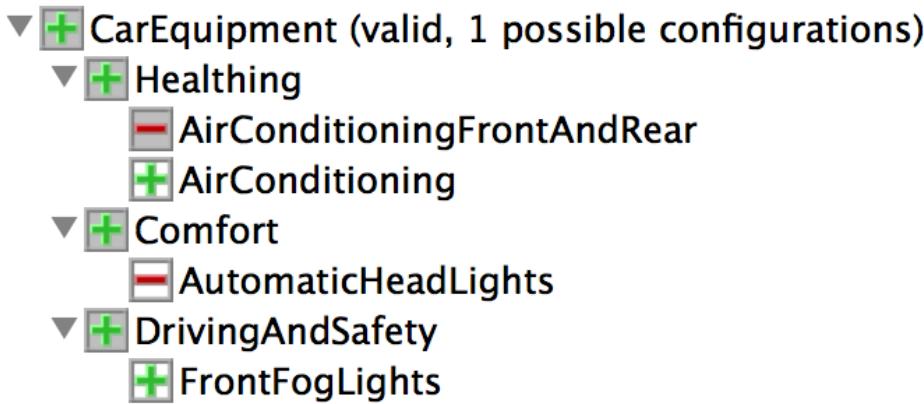


Hierarchy: rooted tree

Variability:

- mandatory,
- optional,
- Groups: exclusive or inclusive features
- Cross-tree constraints





Hierarchy + Variability

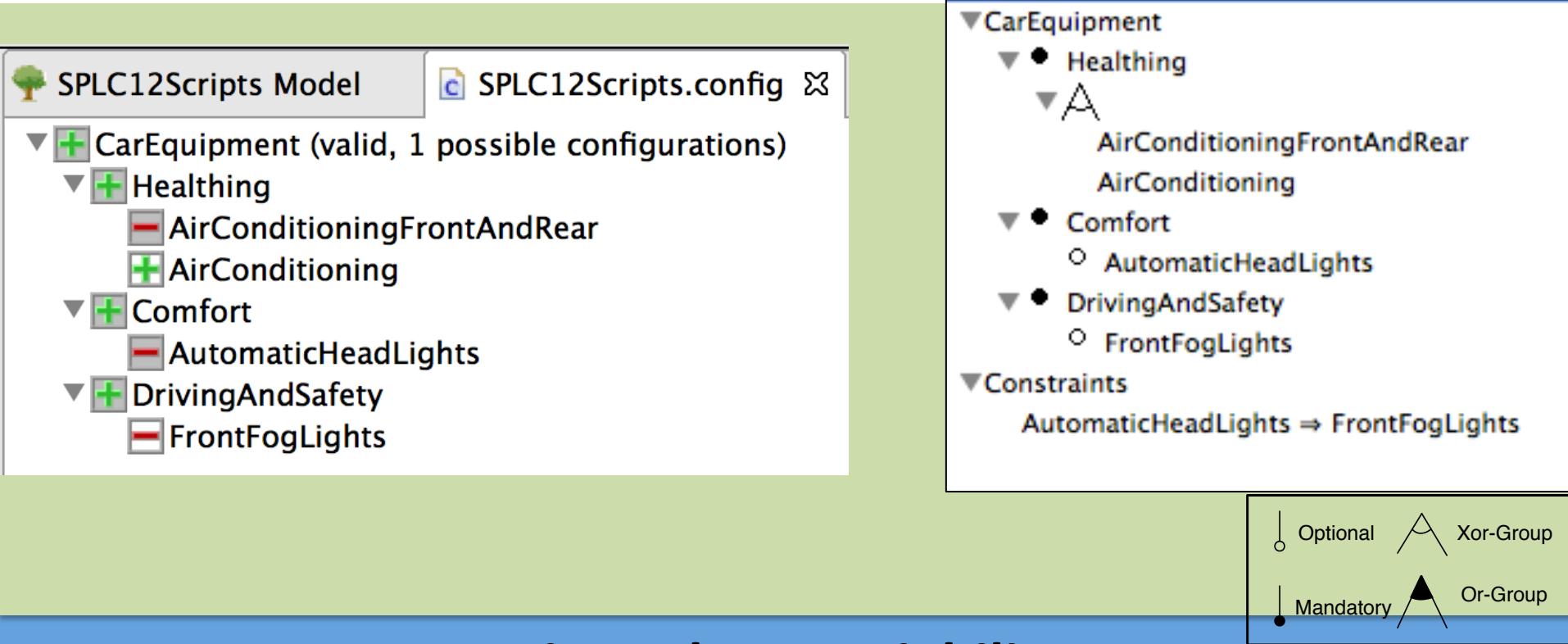
=

set of valid configurations

configuration = set of features selected

{CarEquipment, Comfort, DrivingAndSafety, Healthing, AirConditioning, FrontFogLights}





Hierarchy + Variability

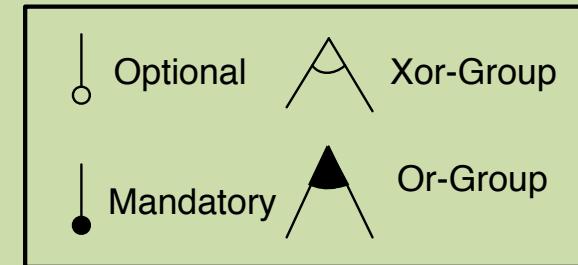
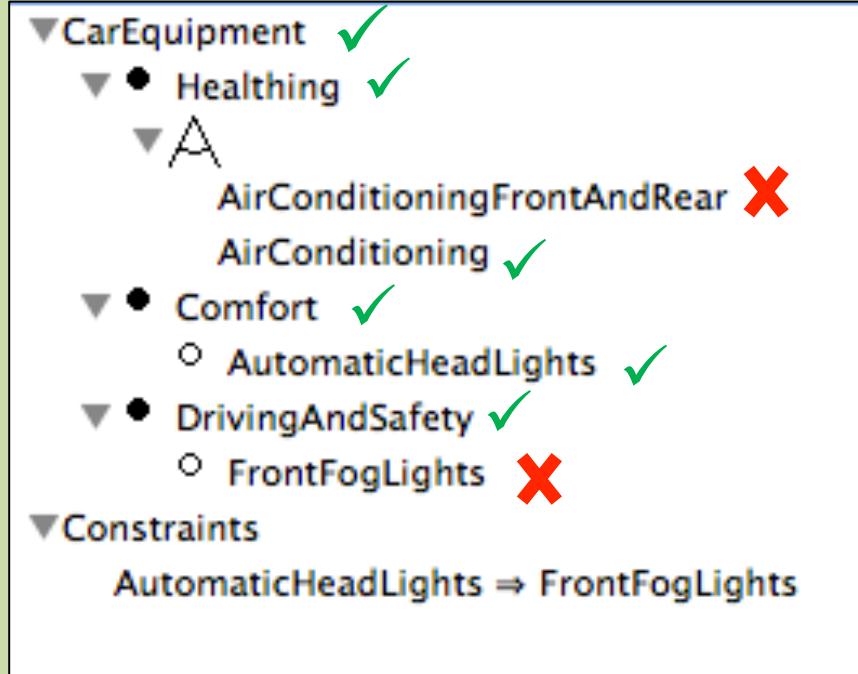
=

set of valid configurations

configuration = set of features selected

{CarEquipment, Comfort, DrivingAndSafety, Healthing, AirConditioning}





Hierarchy + Variability

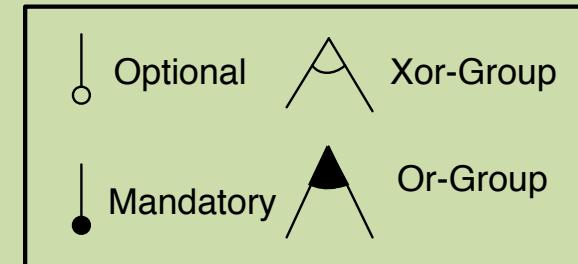
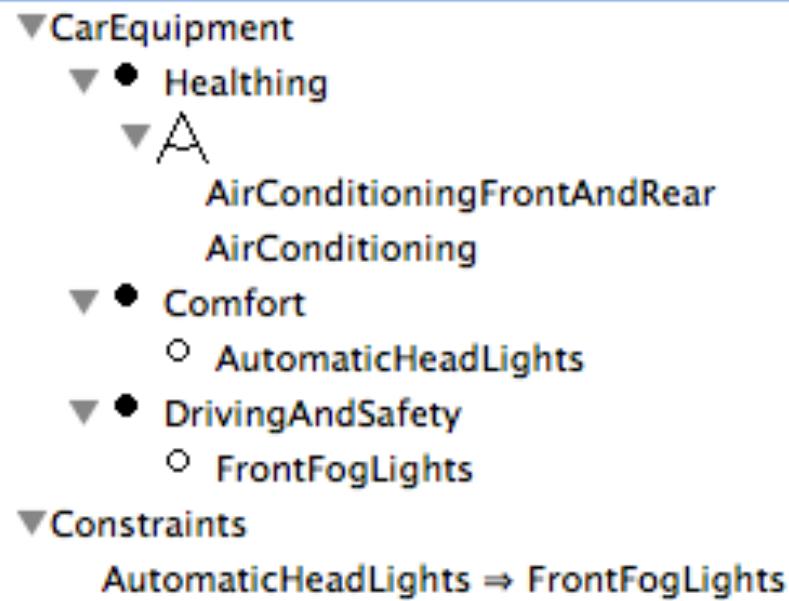
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set of valid configurations

configuration = set of features selected

{CarEquipment, Comfort, DrivingAndSafety, Healthing, AirConditioning, AutomaticHeadLights}





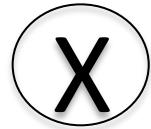
Hierarchy + Variability

=

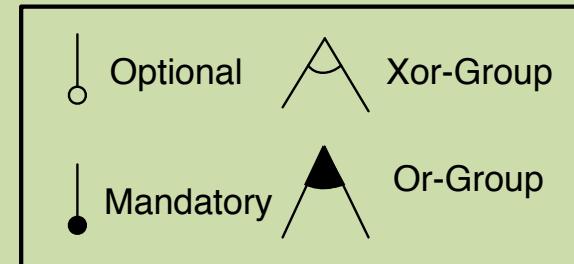
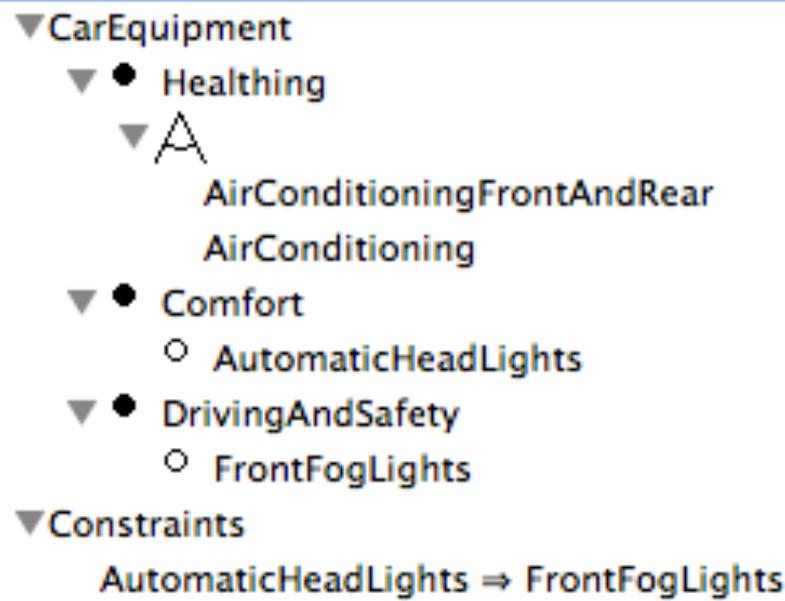
set of valid configurations



{CarEquipment, Comfort,
DrivingAndSafety,
Healthing}



- {AirConditioning, FrontFogLights}
- {AutomaticHeadLights, AirConditioning, FrontFogLights}
- {AutomaticHeadLights, FrontFogLights, AirConditioningFrontAndRear}
- {AirConditioningFrontAndRear}
- {AirConditioning}
- {AirConditioningFrontAndRear, FrontFogLights}



Hierarchy + Variability

=

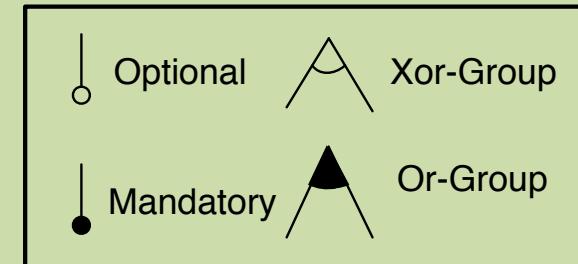
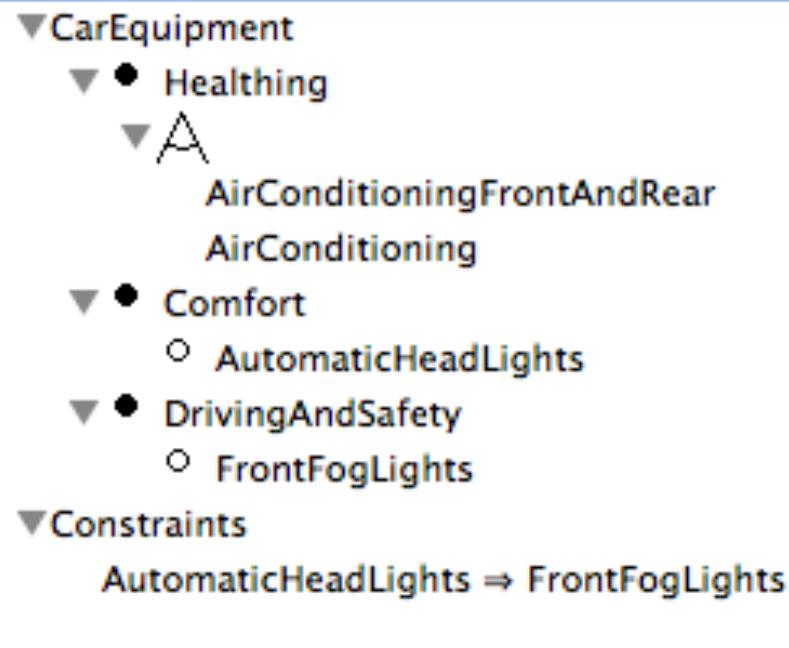
set of valid configurations

Configuration set (from a basic feature model of car)

	CarEquipment	Comfort	DrivingAndSafety	Healting	AirConditioning	FrontFogLights	AutomaticHeadLights	AirConditioningFrontAndRear
Car2	yes	yes	yes	yes	yes	yes	yes	no
Car6	yes	yes	yes	yes	no	yes	no	yes
Car1	yes	yes	yes	yes	yes	yes	no	no
Car4	yes	yes	yes	yes	no	no	no	yes
Car5	yes	yes	yes	yes	yes	no	no	no
Car3	yes	yes	yes	yes	no	yes	yes	yes



ar}



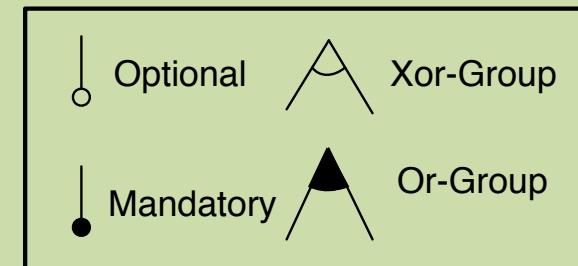
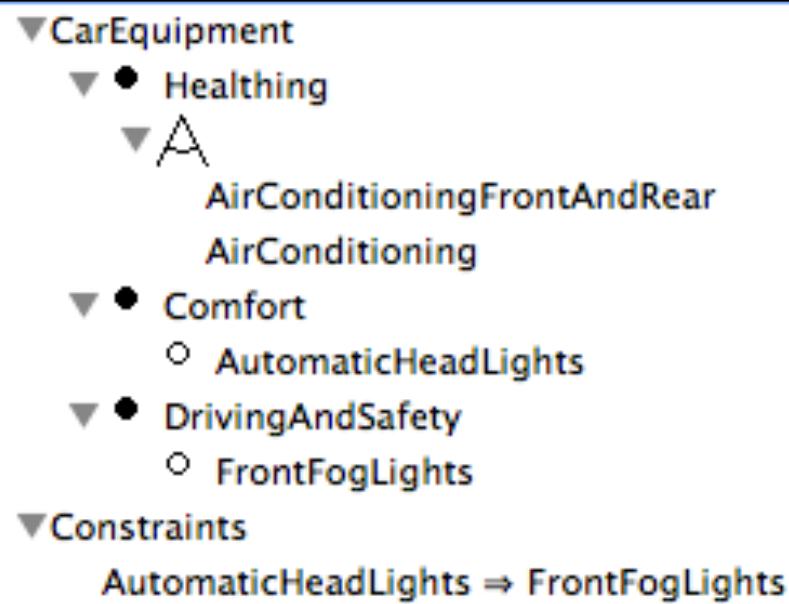
Hierarchy + Variability

=

set of valid configurations



Product ▾ ▾	CarEquipment ▾	Comfort ▾	DrivingAndSafety ▾	Healting ▾	AirConditioning ▾	FrontFogLights ▾	AutomaticHeadLights ▾	AirConditioningFrontAndRear ▾
	Find	Yes <input type="checkbox"/> No <input type="checkbox"/>						
Car1	yes	yes	yes	yes	yes	yes	no	no
Car2	yes	yes	yes	yes	yes	yes	yes	no
Car3	yes	yes	yes	yes	no	yes	yes	yes
Car4	yes	yes	yes	yes	no	no	no	yes
Car5	yes	yes	yes	yes	yes	no	no	no
Car6	yes	yes	yes	yes	no	yes	no	yes



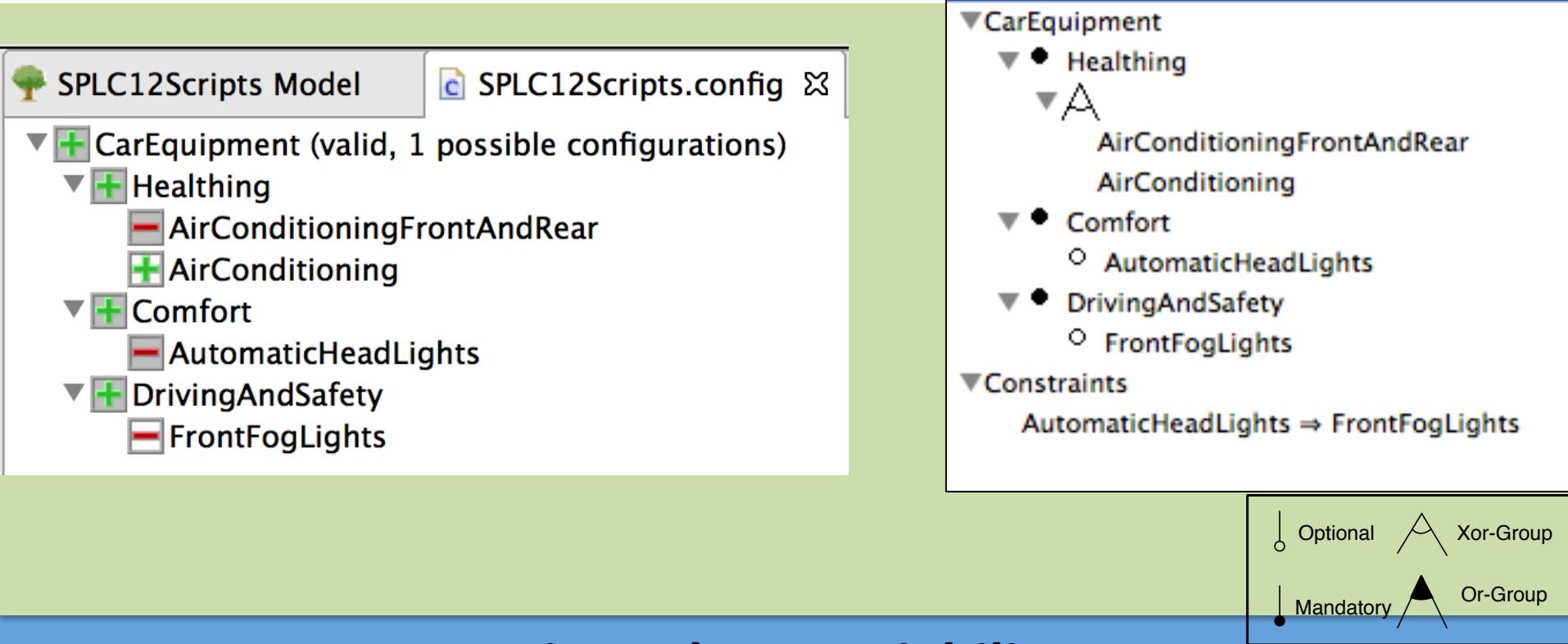
Hierarchy + Variability

=

set of valid configurations



Product ▾ ▾	▼	▼	▼	▼	▼	AirConditioning ▾	FrontFogLights ▾	AutomaticHeadLights ▾	AirConditioningFrontAndRear ▾
Find						Yes <input type="checkbox"/> No <input type="checkbox"/>			
Car1						yes	yes	no	no
Car2						yes	yes	yes	no
Car3						no	yes	yes	yes
Car4						no	no	no	yes
Car5						yes	no	no	no
Car6						no	yes	no	yes



Hierarchy + Variability

=

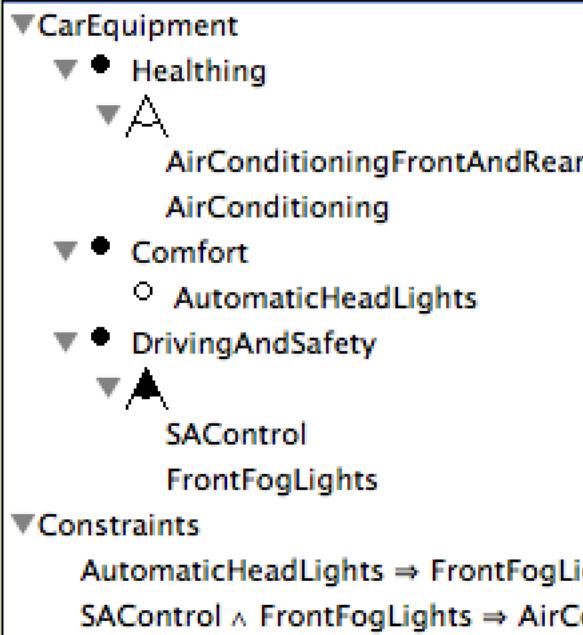
set of valid configurations

configuration = set of features selected

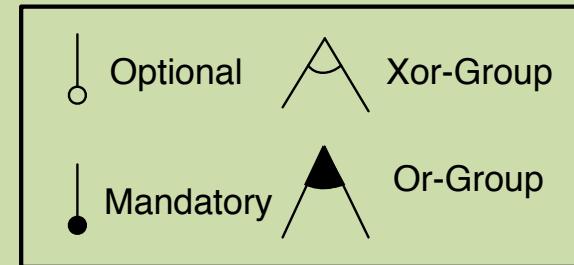
{CarEquipment, Comfort, DrivingAndSafety, Healthing, AirConditioning}

Product ▾	▼	▼	▼	▼	▼	AirConditioning	▼	FrontFogLights	▼	AutomaticHeadLights	▼	AirConditioningFrontAndRear	▼
Find						Yes <input checked="" type="checkbox"/> No <input type="checkbox"/>		Yes <input type="checkbox"/> No <input checked="" type="checkbox"/>		Yes <input type="checkbox"/> No <input checked="" type="checkbox"/>		Yes <input type="checkbox"/> No <input checked="" type="checkbox"/>	
Car5						yes		no		no		no	





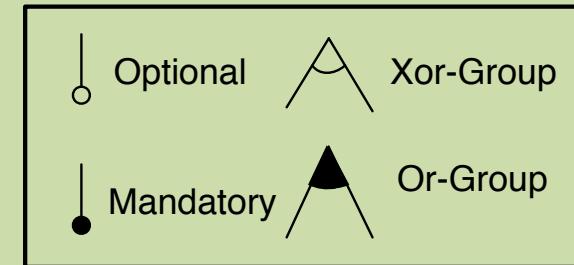
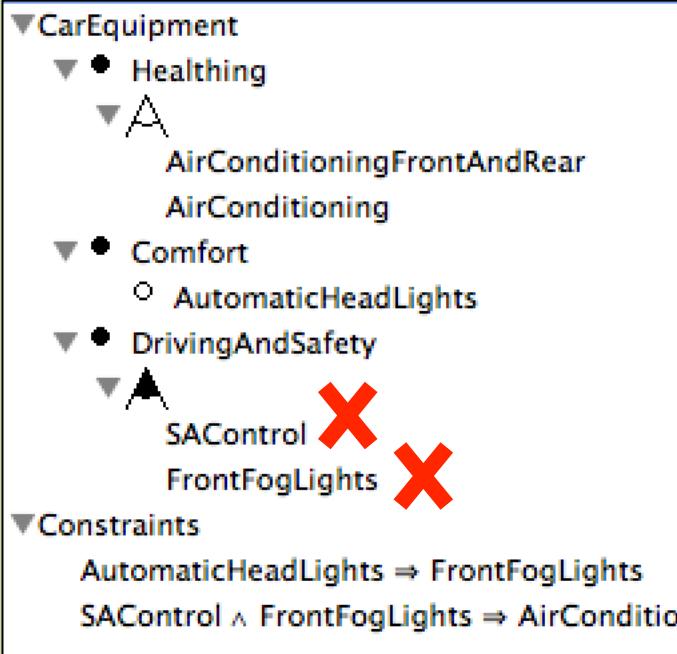
Boolean logic: \wedge , \vee , not, implies



Hierarchy + Variability
=

set of valid configurations





Hierarchy + Variability

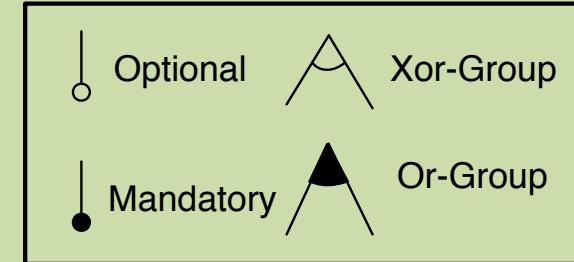
=

set of valid configurations



Or-group: at least one!





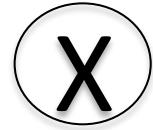
Hierarchy + Variability

=

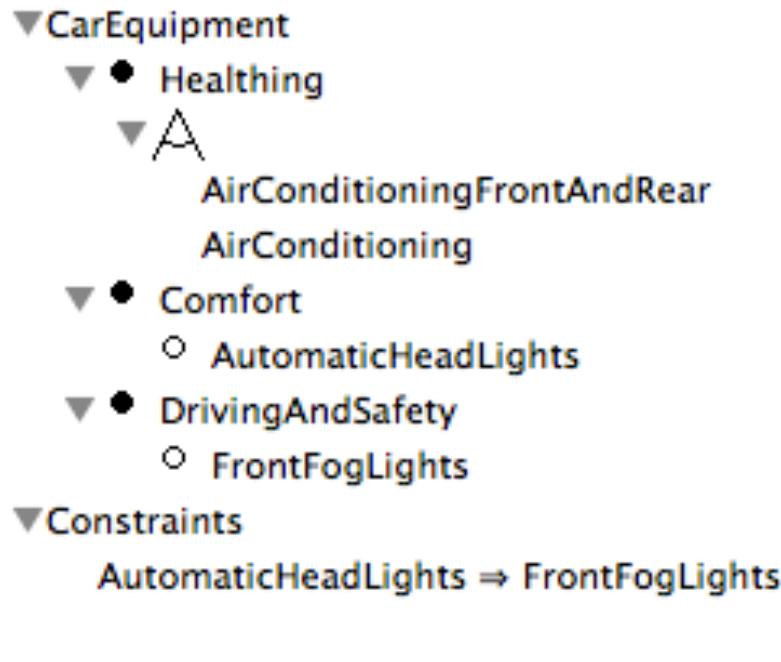
set of valid configurations



{CarEquipment, Comfort,
DrivingAndSafety,
Healthing}



- {AirConditioningFrontAndRear, FrontFogLights, SAControl}
- {AirConditioningFrontAndRear, SAControl}
- {AutomaticHeadLights, AirConditioning, FrontFogLights}
- {AirConditioningFrontAndRear, SAControl, AutomaticHeadLights, FrontFogLights}
- {FrontFogLights, AirConditioning}
- {AutomaticHeadLights, AirConditioningFrontAndRear, FrontFogLights}
- {FrontFogLights, AirConditioningFrontAndRear}
- {SAControl, AirConditioning}



(Boolean)
Feature Models



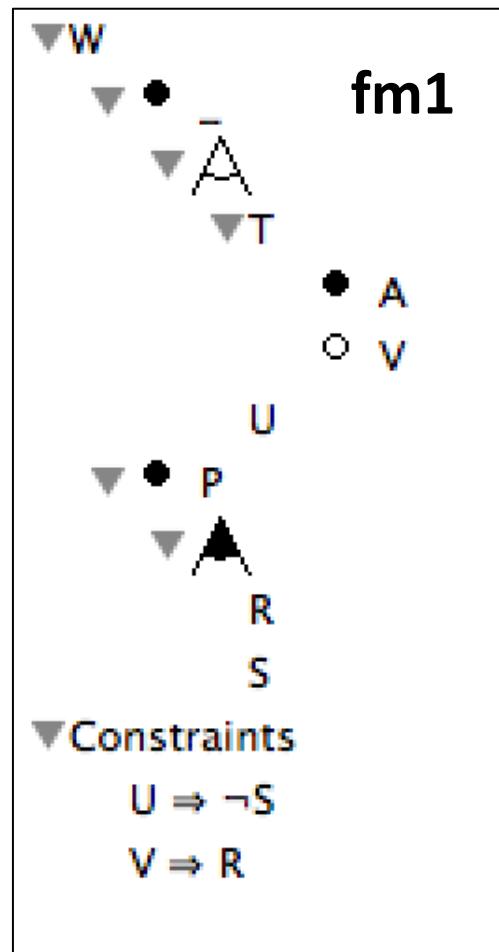
(Boolean)
Formula φ

Product ▾	CarEquipment	Comfort	DrivingAndSafety	Healthing	AirConditioning	FrontFogLights	AutomaticHeadLights	AirConditioningFrontAndRear
Find	Yes <input type="checkbox"/> No <input type="checkbox"/>							
Car1	yes	yes	yes	yes	yes	yes	no	no
Car2	yes	no						
Car3	yes	yes	yes	yes	no	yes	yes	yes
Car4	yes	yes	yes	yes	no	no	no	yes
Car5	yes	yes	yes	yes	yes	no	no	no
Car6	yes	yes	yes	yes	no	yes	no	yes

(Boolean)
Product Comparison Matrix

(Boolean) Feature Models

Hierarchy + Variability = set of valid configurations



$\llbracket fm1 \rrbracket = \{$

$\{W, P, R, S, T, A, V\},$

$\{W, P, S, T, A\},$

$\{W, P, R, T, A\},$

$\{W, P, R, U\},$

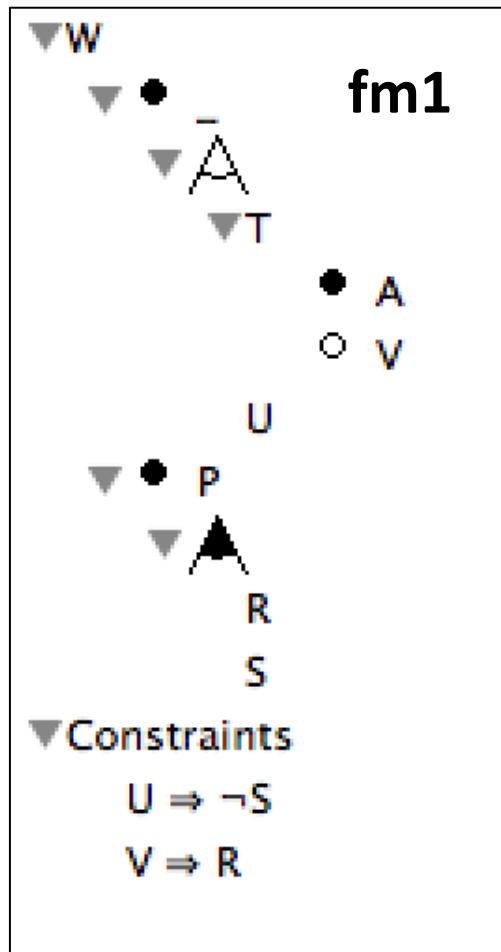
$\{W, P, R, T, V, A\},$

$\{W, P, R, S, T, A\},$

$\}$

(Boolean) Feature Models

~ Boolean formula

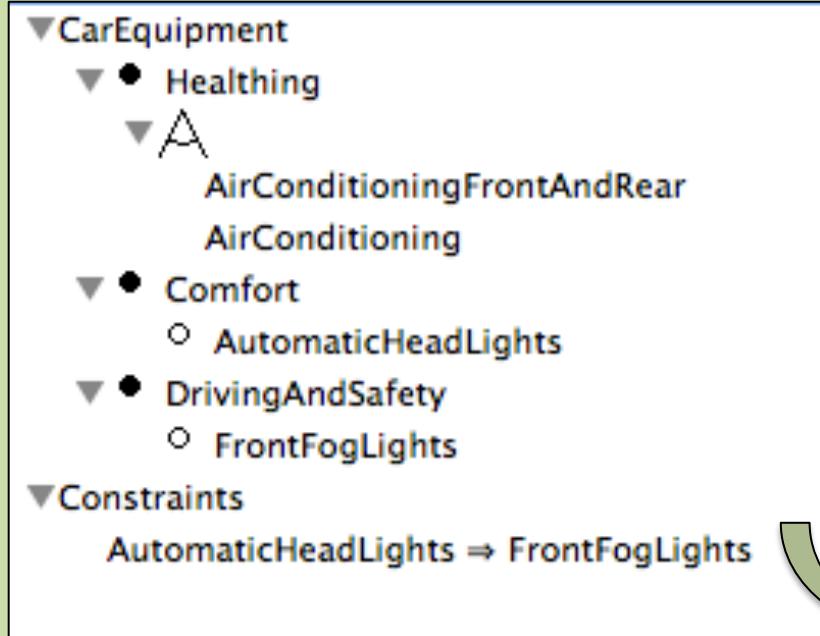
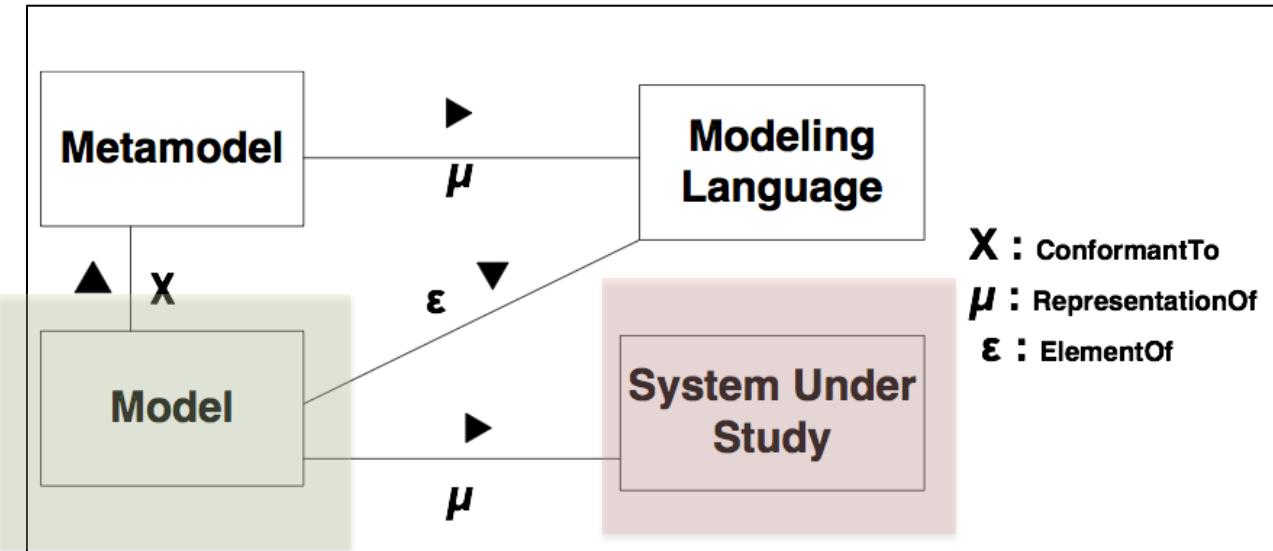


$\phi_{fm_1} = W // \text{root}$
 $\wedge W \Leftrightarrow P // \text{mandatory}$
 $// \text{Or-group}$
 $\wedge P \Rightarrow R \vee S$
 $\wedge R \Rightarrow P \wedge S \Rightarrow P$
 $\wedge V \Rightarrow T // \text{optional}$
 $\wedge A \Leftrightarrow T // \text{mandatory}$
 $// \text{Xor-group}$
 $\wedge T \Rightarrow W$
 $\wedge U \Rightarrow W$
 $\wedge \neg T \vee \neg U$
 $// \text{constraints}$
 $\wedge V \Rightarrow R // \text{implies}$
 $\wedge \neg U \Rightarrow \neg S // \text{excludes}$

Languages:

How to specify feature models?

Feature Models



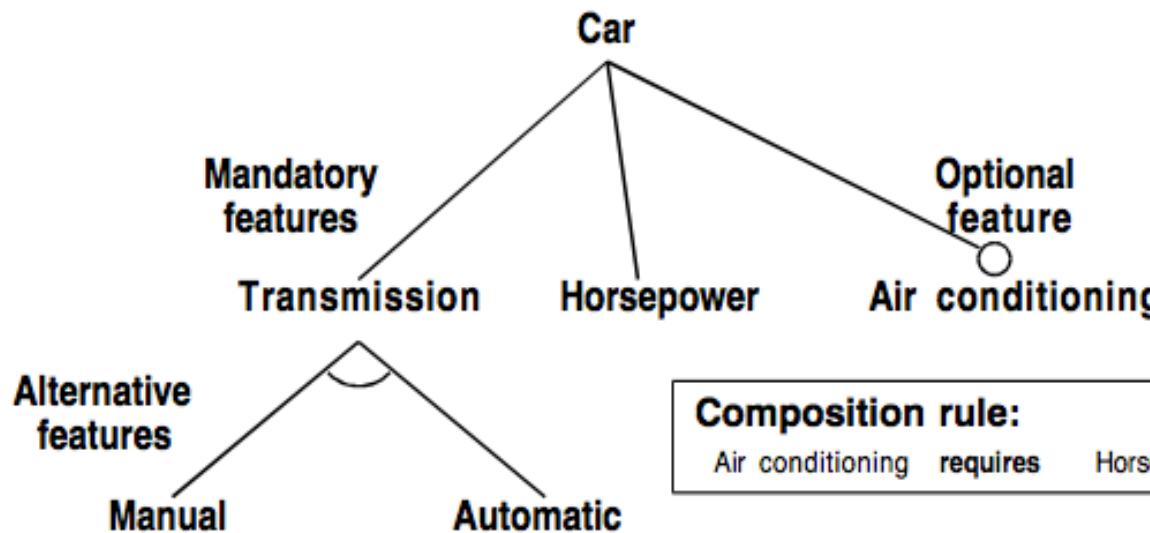
History of Feature Models

~ often called **Feature Diagrams**
(suggest a visual representation)

graphical languages

Feature Models

Kang et al. (1990)

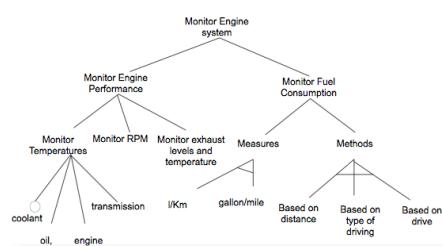


Composition rule:

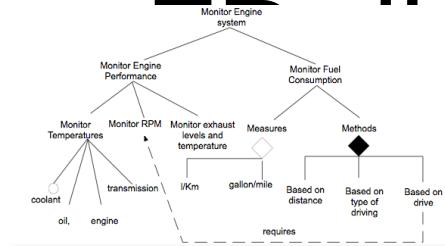
Air conditioning requires Horsepower > 100

Rationale:

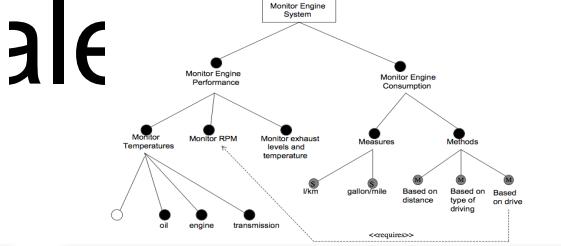
Manual more fuel efficient



FODA (OFT)
[Kang et al., 1990]



FeatuRSEB (RFD)
[Griss et al., 1998]



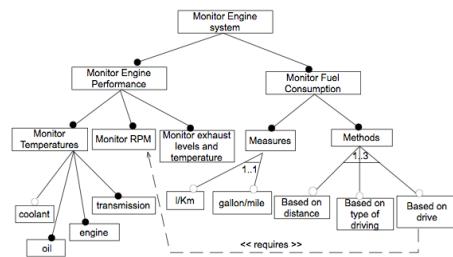
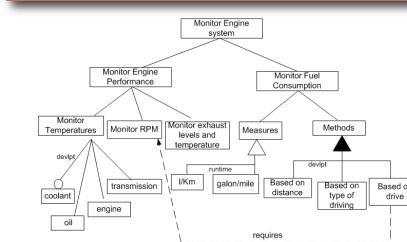
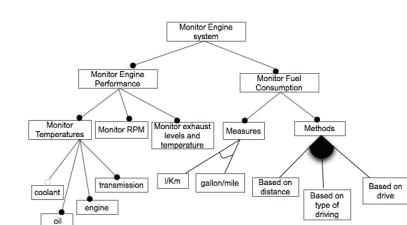
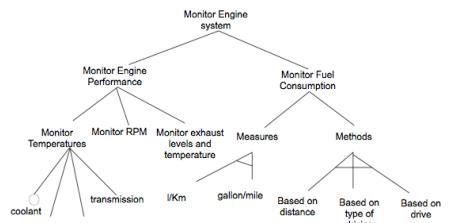
PLUSS (PFT)
[Eriksson et al., 2005]

FORM (OFD)
[Kang et al., 1998]

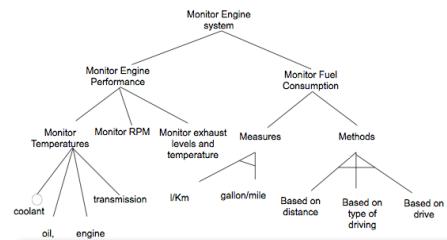
Gen. Prog. (GPFT)
[Czarnecki et al., 2000]

VBFD
[van Gurp et al., 2001]

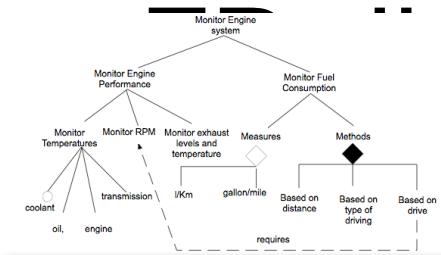
EFD
[Riebisch et al., 2002]



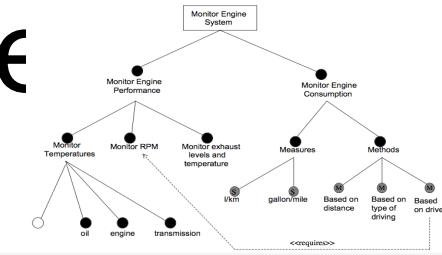
ale



FODA (OFT)
[Kang et al., 1990]



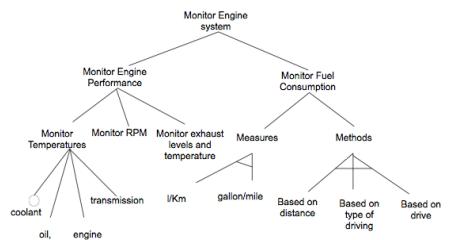
FeatuRSEB (RFD)
[Griss et al., 1998]



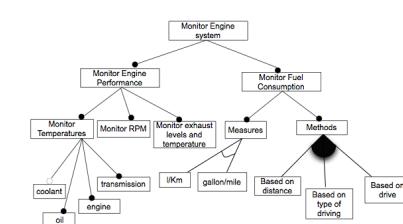
PLUSS (PFT)
[Eriksson et al., 2005]

Aesthetic differences

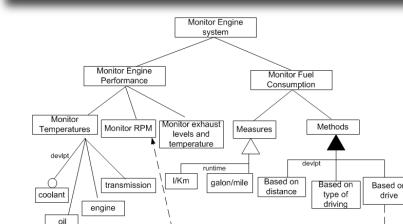
FORM (OFD)
[Kang et al., 1998]



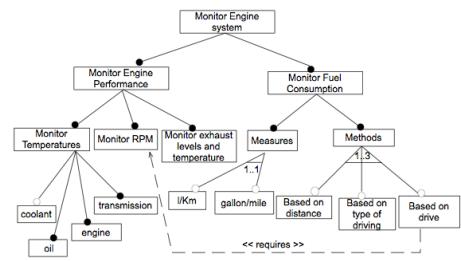
Gen. Prog. (GPFT)
[Czarnecki et al., 2000]



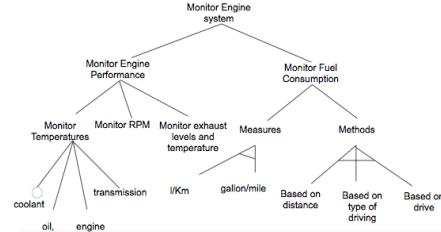
VBFD
[van Gurp et al., 2001]



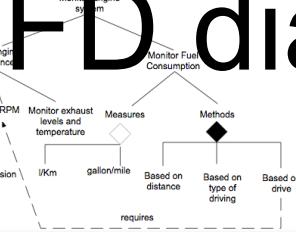
EFD
[Riebisch et al., 2002]



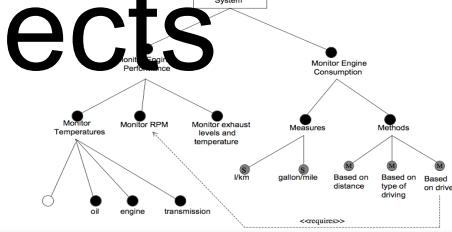
FD dialects



FODA (OFT)
[Kang et al., 1990]



FeatuRSEB (RFD)
[Griss et al., 1998]

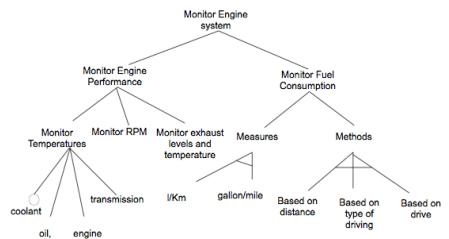


PLUSS (PFT)
[Eriksson et al., 2005]

Aesthetic differences
Stronger claims

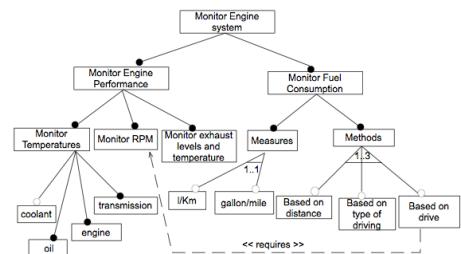
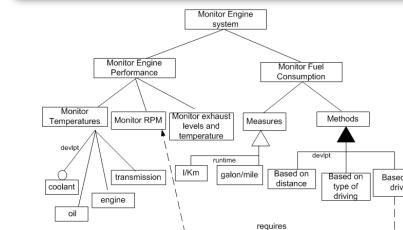
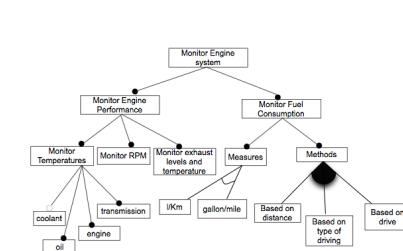
FORM (OFD)
[Kang et al., 1998]

Gen. Prog. (GPFT)
[Czarnecki et al., 2000]

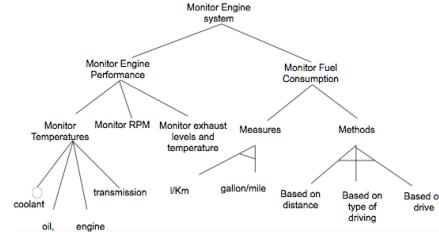


VBFD
[van Gurp et al., 2001]

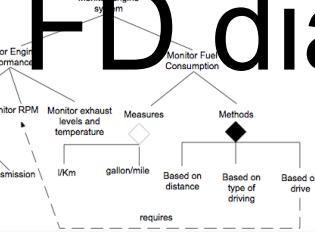
EFD
[Riebisch et al., 2002]



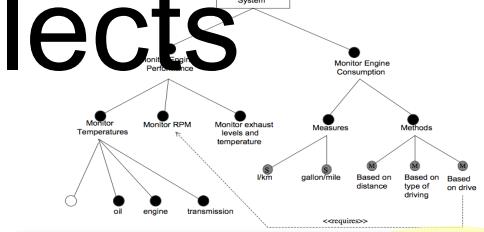
FD dialects



FODA (OFT)
[Kang et al., 1990]



FeatuRSEB (RFD)
[Griss et al., 1998]



PLUSS (PFT)
[Eriksson et al., 2001]

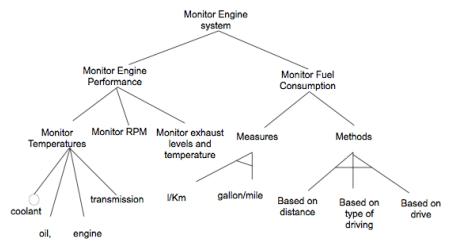
Aesthetic differences

Stronger claims

Vague use of terms
syntax, semantics,
expressiveness, ambiguity ...

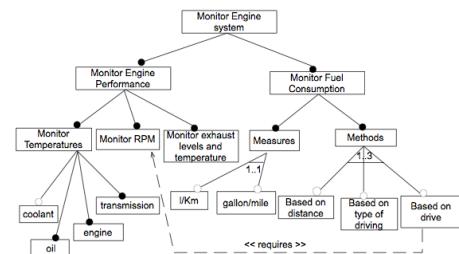
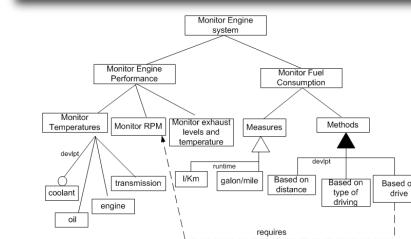
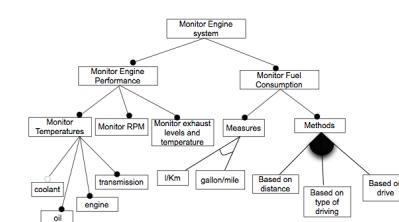
FORM (OFD)
[Kang et al., 1998]

Gen. Prog. (GPFT)
[Czarnecki et al., 2000]



VBFD
[van Gurp et al., 2001]

EFD
[Riebisch et al., 2002]



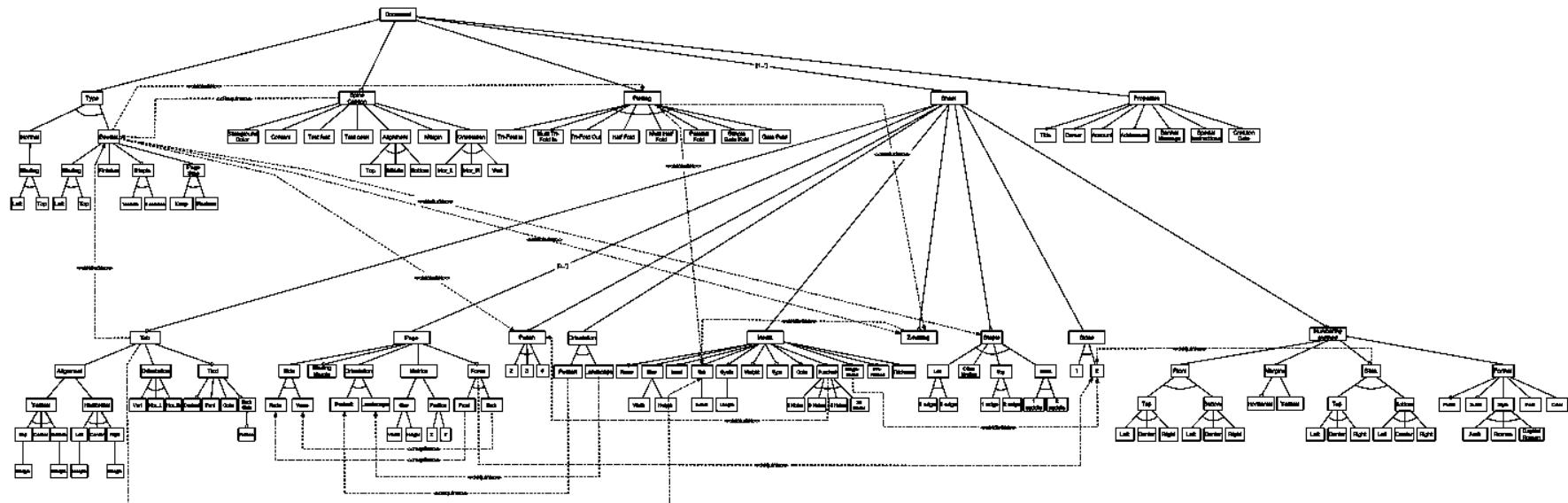
Concrete (graphical)
syntax matters...

But semantics even more!

Feature Models

~ Feature Diagrams
(suggest a visual representation)

but that's not mandatory
that does not necessary scale
or respond to users' concerns



Textual variability languages

- Andreas Classen, Quentin Boucher, Patrick Heymans: A text-based approach to feature modelling: Syntax and semantics of TVL. *Sci. Comput. Program.* 76(12): 1130-1143 (2011)
- Czarnecki et al. “Clafer: Unifying Class and Feature Modeling” SoSyM’15
- Mathieu Acher, Philippe Collet, Philippe Lahire, Robert B. France « A Domain-Specific Language for Large-Scale Management of Feature Models » *Science of Computer Programming* (SCP), 2013
- Mauricio Alférez, José A. Galindo, Mathieu Acher, and Benoit Baudry. Modeling Variability in the Video Domain: Language and Experience Report (2014). Research Report RR-8576

FAMILIAR

(FeAture Model script Language for manipulation and Automatic Reasoning)

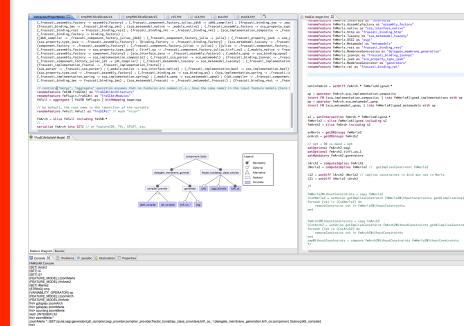
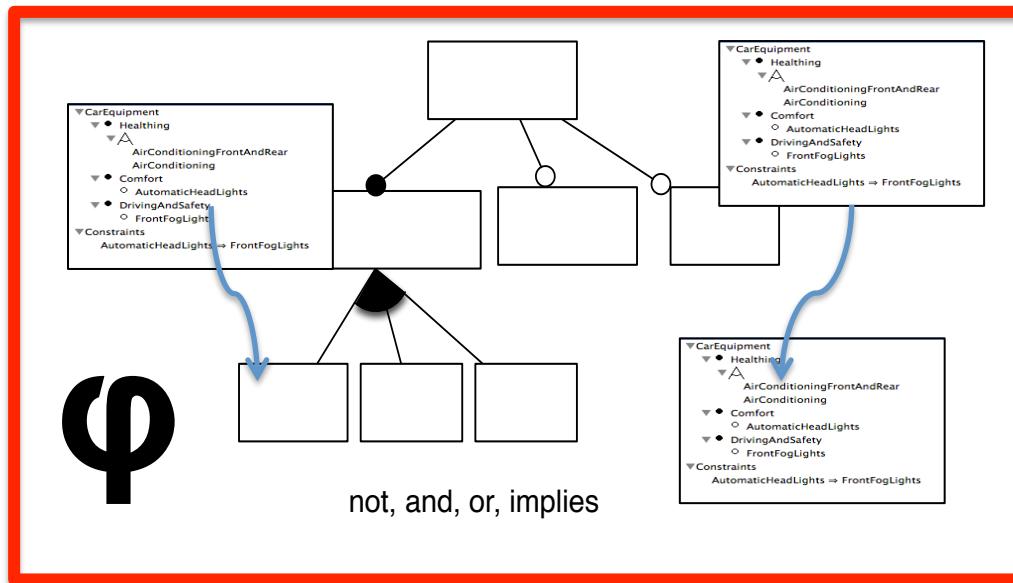
<http://familiar-project.github.com/>

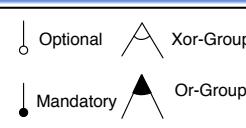
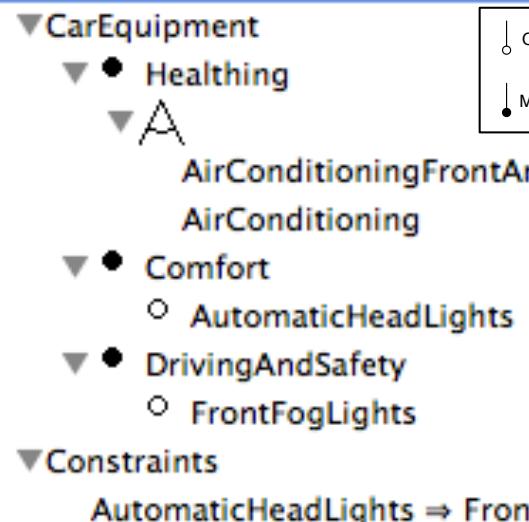


S.P.L.O.T.
Software Product Lines Online Tools

IDE
Feature

TVL
DIMACS





```
fml> convert fmCarEquipment into SPLIT
res1: (STRING) <feature_model name="fmCarEquipment">
<meta>
<data name="description"/>
<data name="creator"/>
<data name="address"/>
<data name="email"/>
<data name="phone"/>
<data name="website"/>
<data name="organization"/>
<data name="department"/>
<data name="date"/>
<data name="reference"/>
</meta>
<feature_tree>
: r CarEquipment(_r0)
  : m Healthing(_r1)
    : g [1,1]
      : AirConditioningFrontAndRear(_r2)
      : AirConditioning(_r3)
    : m DrivingAndSafety(_r4)
      : o FrontFogLights(_r5)
    : m Comfort(_r6)
      : o AutomaticHeadLights(_r7)
</feature_tree>
<constraints>
C0: ~_r7 or _r5
</constraints>
</feature_model>
```



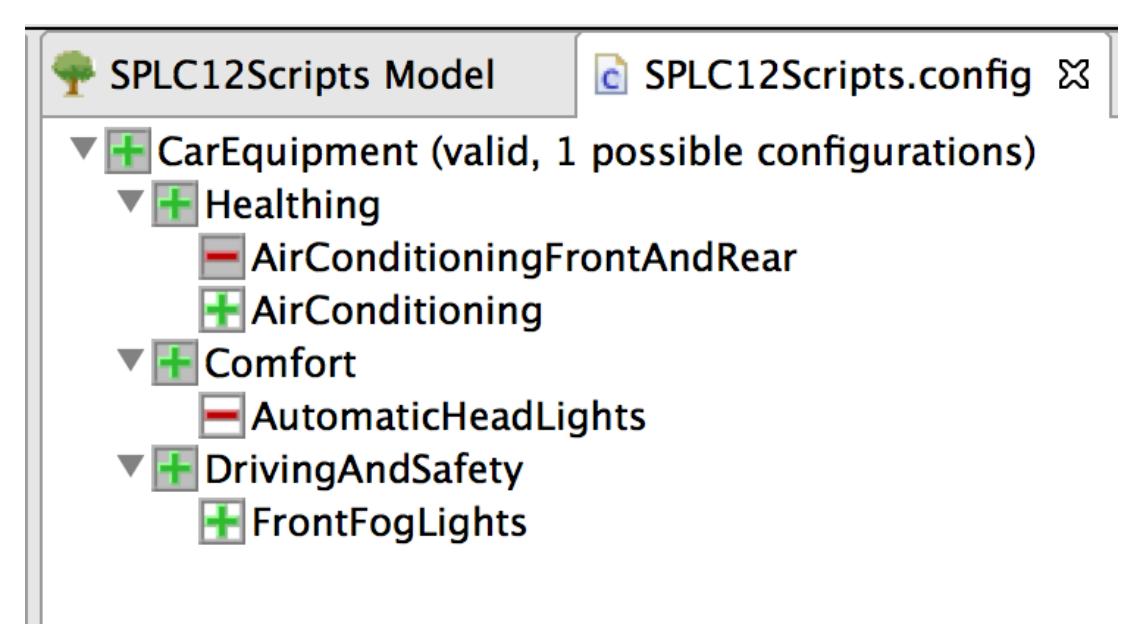
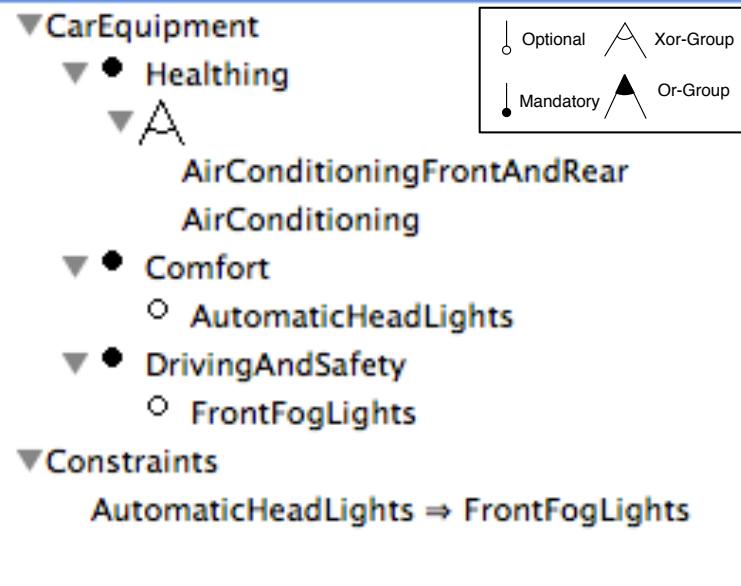
CarEquipment ;

ty ;



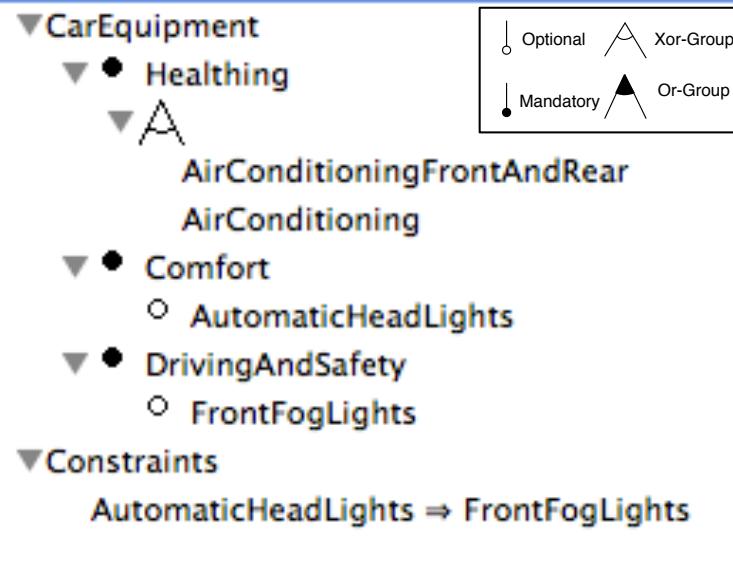
```
fmCarEquipment = FM (CarEquipment : Healthing DrivingAndSafety Comfort ; // 3 mandatory features
                      Healthing : (AirConditioning|AirConditioningFrontAndRear) ; // xor
                      DrivingAndSafety : [FrontFogLights] ; // optional
                      Comfort : [AutomaticHeadLights] ; // optional
                      // cross-tree constraints
                      AutomaticHeadLights -> FrontFogLights ; )
```

```
MacBook-Pro-de-Mathieu-3:Documents macher1$ java -Xmx1024M -jar FML-basic-1.1.jar FMLTestRepository/carEquipTuto.fml
FAMILIAR (for FeAture Model scrIpt Language for manIpulation and Automatic Reasoning) version 1.1 (beta)
http://familiar-project.github.com/
fml> ls
(FEATURE_MODEL) fmCarEquipment
fml> 
```

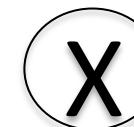


```
fmlCarEquipment = FM (CarEquipment : Healthing DrivingAndSafety Comfort ; // 3 mandatory features
                      Healthing : (AirConditioning|AirConditioningFrontAndRear) ; // Xor
                      DrivingAndSafety : [FrontFogLights] ; // optional
                      Comfort : [AutomaticHeadLights] ; // optional
                      // cross-tree constraints
                      AutomaticHeadLights -> FrontFogLights ; )
```

```
fml> c1 = configuration fmlCarEquipment
c1: (CONFIGURATION) selected: [Healthing, CarEquipment, DrivingAndSafety, Comfort]           deselected: []
fml> select AirConditioning FrontFogLights in c1
res2: (BOOLEAN) true
fml> deselect AutomaticHeadLights in c1
res3: (BOOLEAN) true
fml> selectedF c1
res4: (SET) {Comfort;CarEquipment;Healthing;AirConditioning;DrivingAndSafety;FrontFogLights}
```



{CarEquipment, Comfort,
DrivingAndSafety,
Healthing}



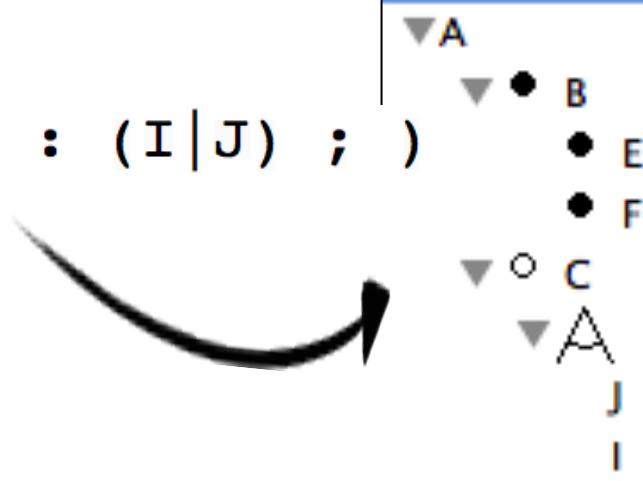
{AirConditioning, FrontFogLights}
 {AutomaticHeadLights, AirConditioning,
FrontFogLights}
 {AutomaticHeadLights, FrontFogLights,
AirConditioningFrontAndRear}
 {AirConditioningFrontAndRear}
 {AirConditioning}
 {AirConditioningFrontAndRear, FrontFogLights}

```
fmlCarEquipment = FM (CarEquipment : Healthing DrivingAndSafety Comfort ; // 3 mandatory features
                      Healthing : (AirConditioning|AirConditioningFrontAndRear) ; // Xor
                      DrivingAndSafety : [FrontFogLights] ; // optional
                      Comfort : [AutomaticHeadLights] ; // optional
                      // cross-tree constraints
                      AutomaticHeadLights -> FrontFogLights ; )
```

```
fml> s1 = configs fmlCarEquipment
s1: (SET) {{Comfort;CarEquipment;FrontFogLights;DrivingAndSafety;AirConditioning;Healthing};{AirConditioningFrontAndRear;CarEquipment;Comfort;DrivingAndSafety;Healthing};{FrontFogLights;DrivingAndSafety;AutomaticHeadLights;CarEquipment;Healthing;AirConditioningFrontAndRear;Comfort};{Healthing;CarEquipment;AirConditioning;DrivingAndSafety;Comfort};{Healthing;CarEquipment;Comfort;FrontFogLights;DrivingAndSafety;AirConditioningFrontAndRear};{AutomaticHeadLights;DrivingAndSafety;CarEquipment;AirConditioning;Healthing;Comfort;FrontFogLights}}
fml> size s1
res0: (INTEGER) 6
fml> counting fmlCarEquipment
res1: (DOUBLE) 6.0
```

```
fml> co = cores fmlCarEquipment
co: (SET) {CarEquipment;Healthing;DrivingAndSafety;Comfort}
fml> fmlCarEquipment.*
res6: (SET) {DrivingAndSafety;AirConditioningFrontAndRear;Comfort;Healthing;FrontFogLights;AirConditioning;AutomaticHeadLights;CarEquipment}
fml> setDiff fmlCarEquipment.* co
res7: (SET) {AutomaticHeadLights;FrontFogLights;AirConditioning;AirConditioningFrontAndRear}
fml>
```

```
fml = FM (A : B [C] ; B : E F ; C : (I|J) ; )
```



```
r1 = root fml
```

```
s = children r1
```

```
s1 = children fml.A
```

```
assert (s eq s1) // equality of the two sets
```

```
ft1 = parent fml.F
```

```
str1 = name ft1
```

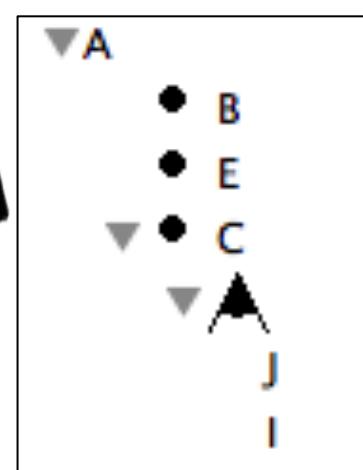
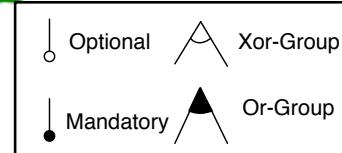
```
ft2 = parent F // parent fml.F
```

```
// another FM
```

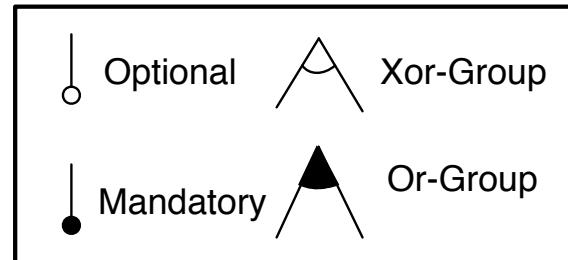
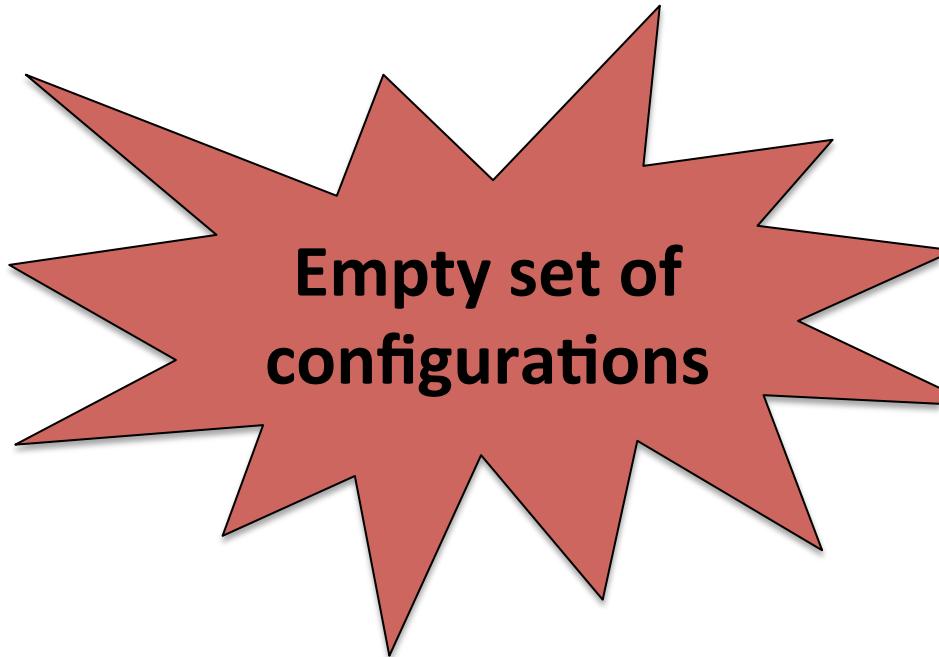
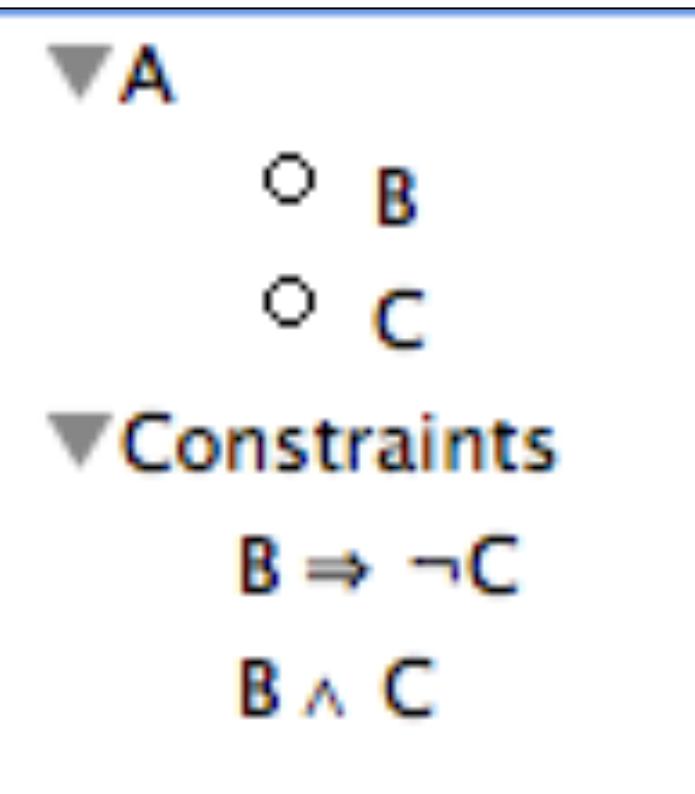
```
fm2 = FM (A : B C E ; C : (I|J)+ ; )
```

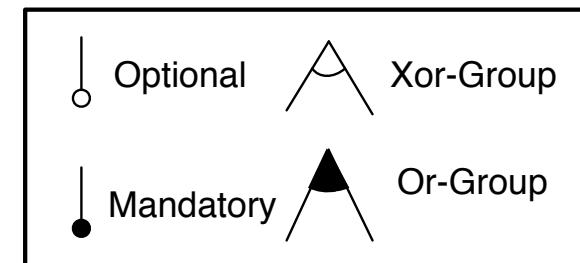
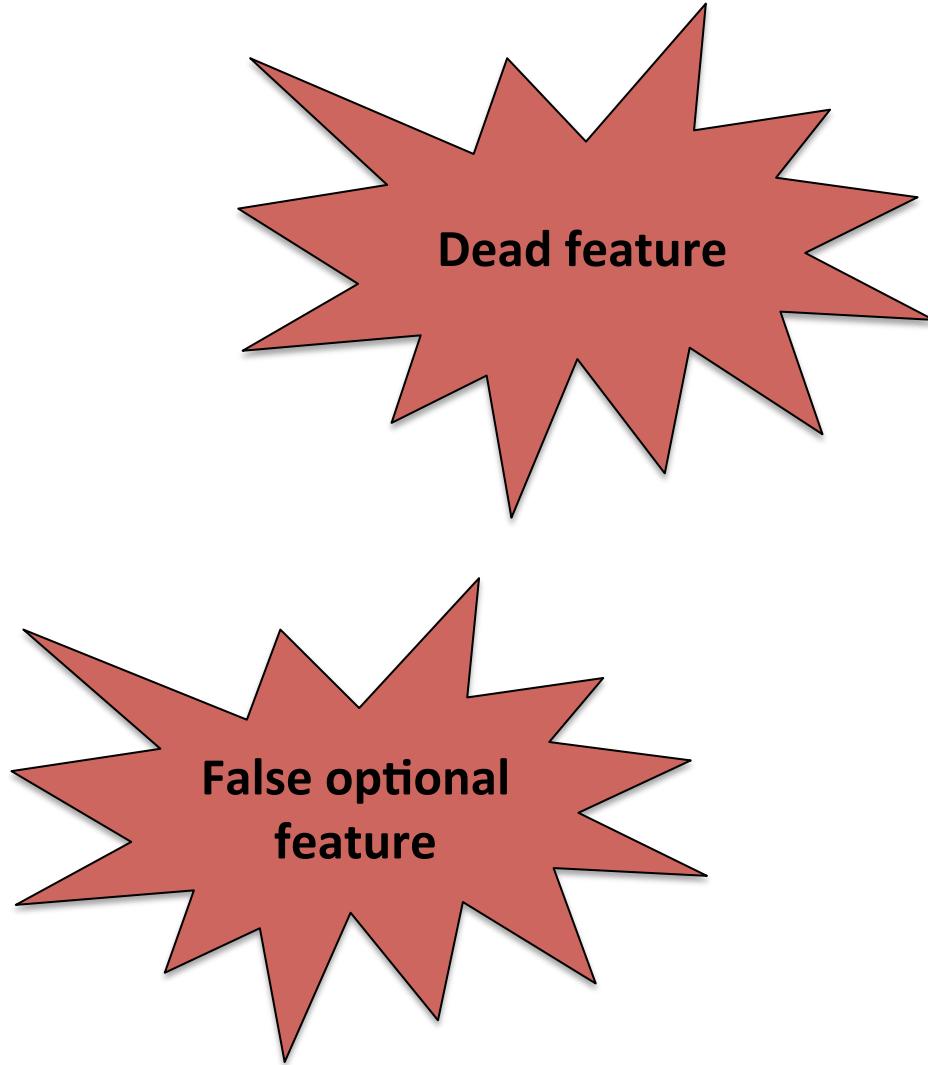
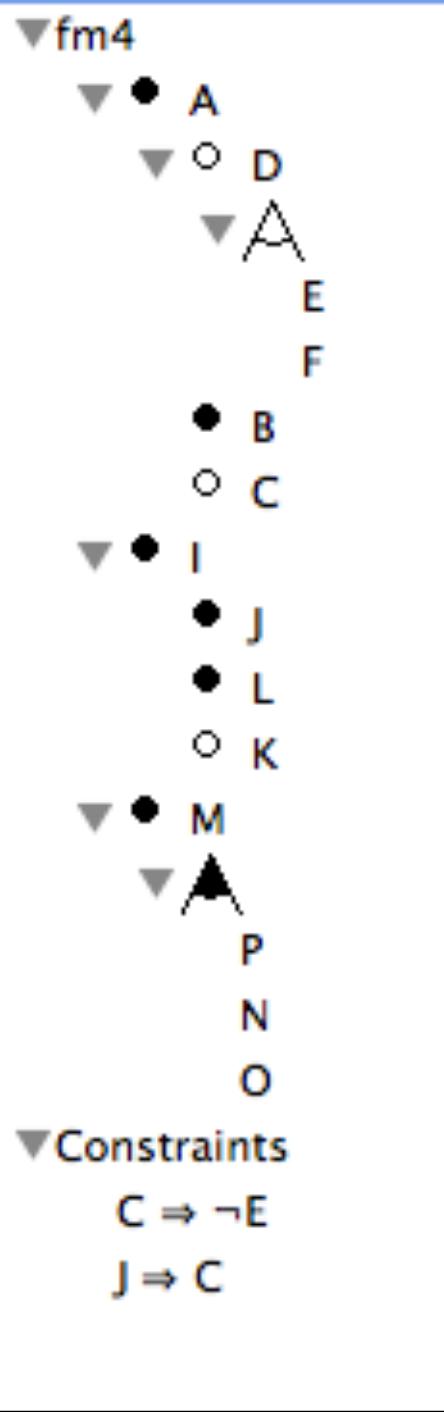
```
ft3 = fm2.B
```

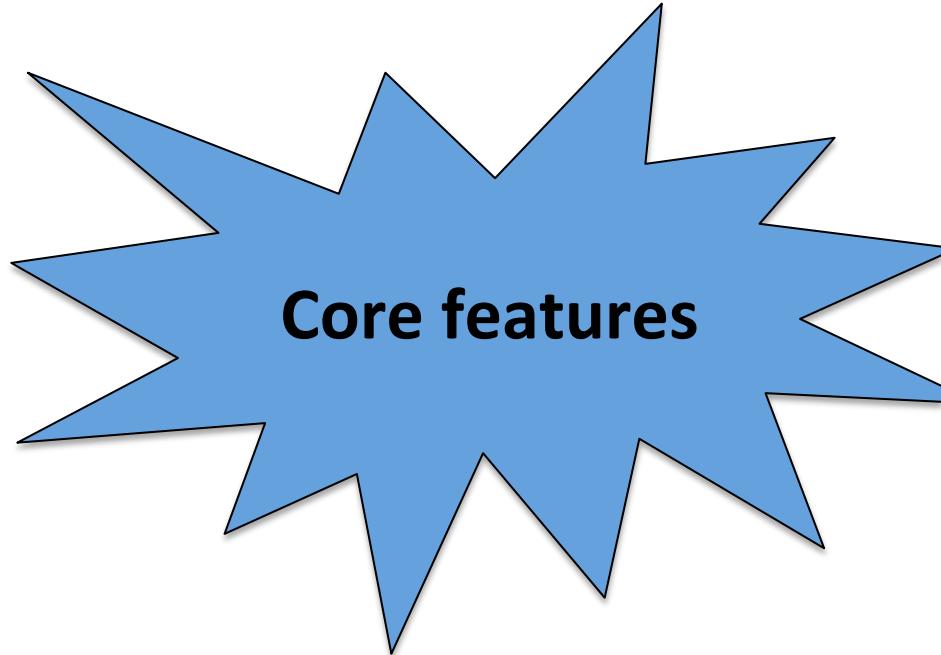
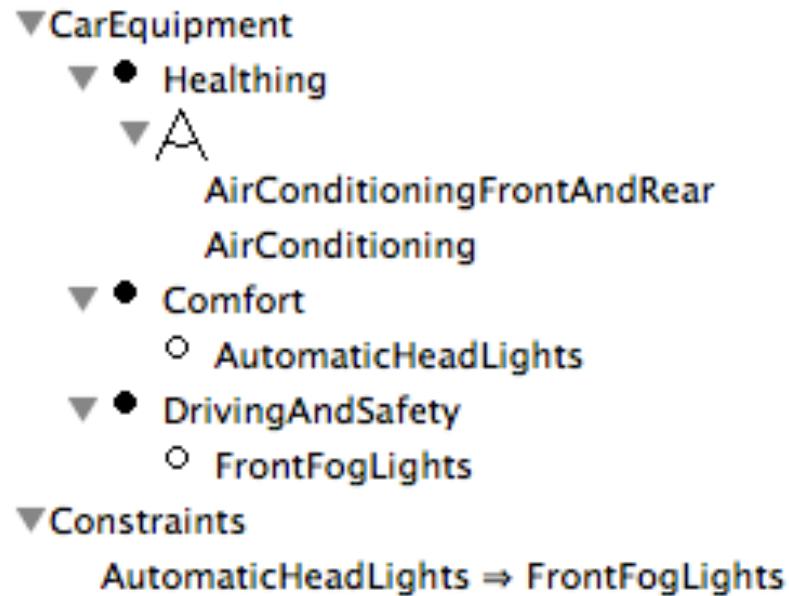
```
ft4 = name B // ambiguity
```



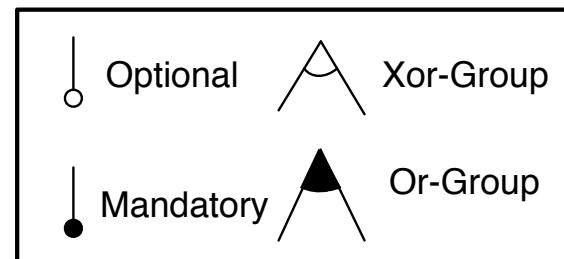
I want to analyze and
play with my specification!

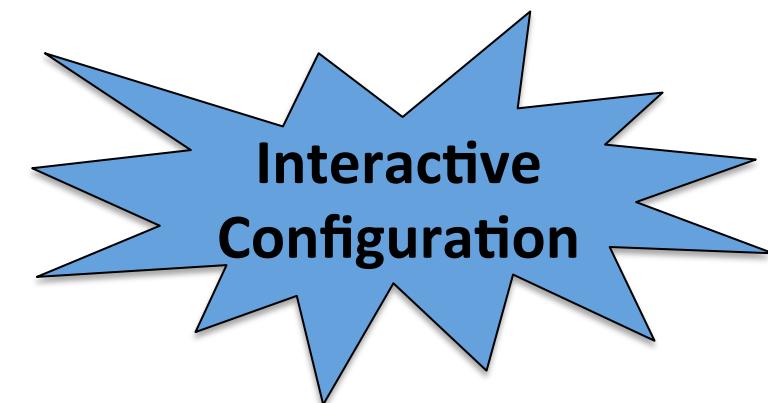
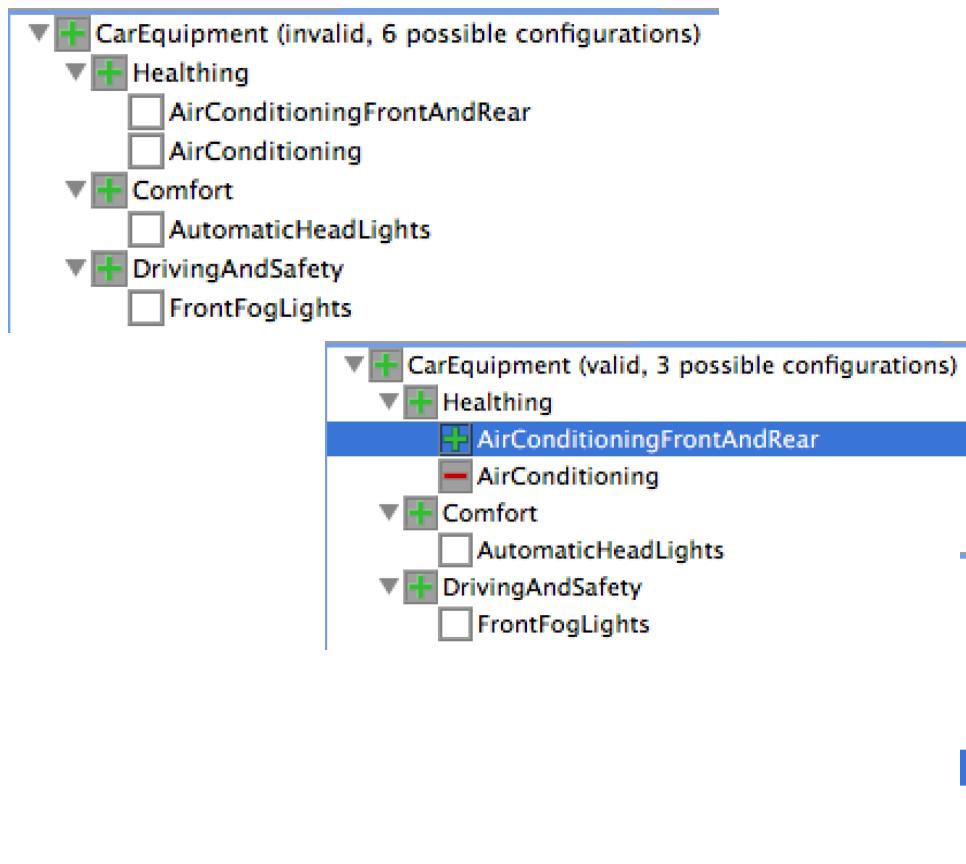
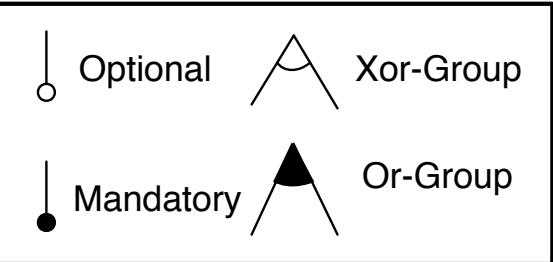
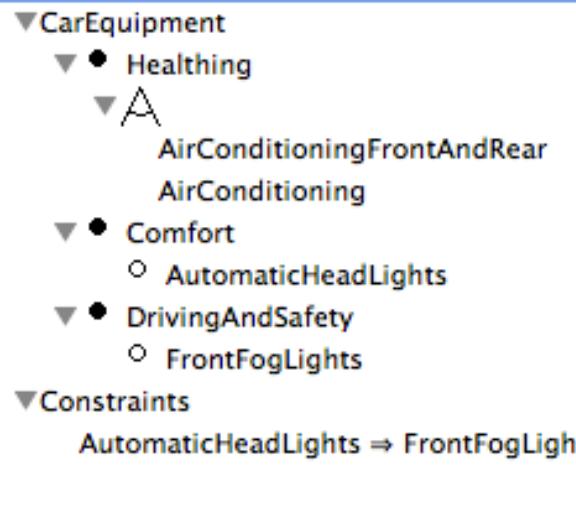






{CarEquipment, Comfort,
DrivingAndSafety, Healthing}





Feature Models and Automated Reasoning

Benavides et al. survey, 2010

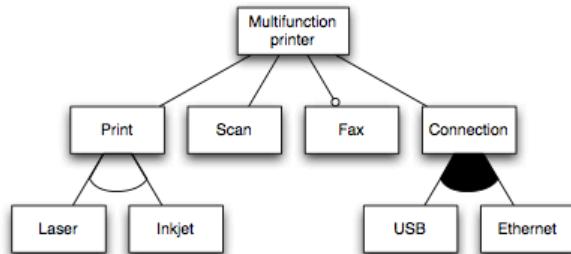
Decision problems and complexity

- Validity of a feature model
- Validity of a configuration
- Computation of dead and core features
- Counting of the number of valid configurations
- Equivalence between two feature models
- Satisfiability (SAT) problem
 - NP-complete

How to automate analysis of your feature models?

Binary Decision Diagram (BDD)
SAT solver

Typical implementations



Fontsource (Attributed - Free Processing 2012) (Attributed - Creative Commons)



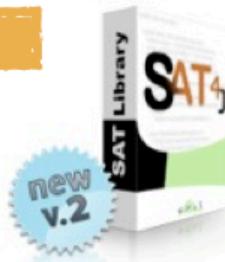
result



logics



solvers

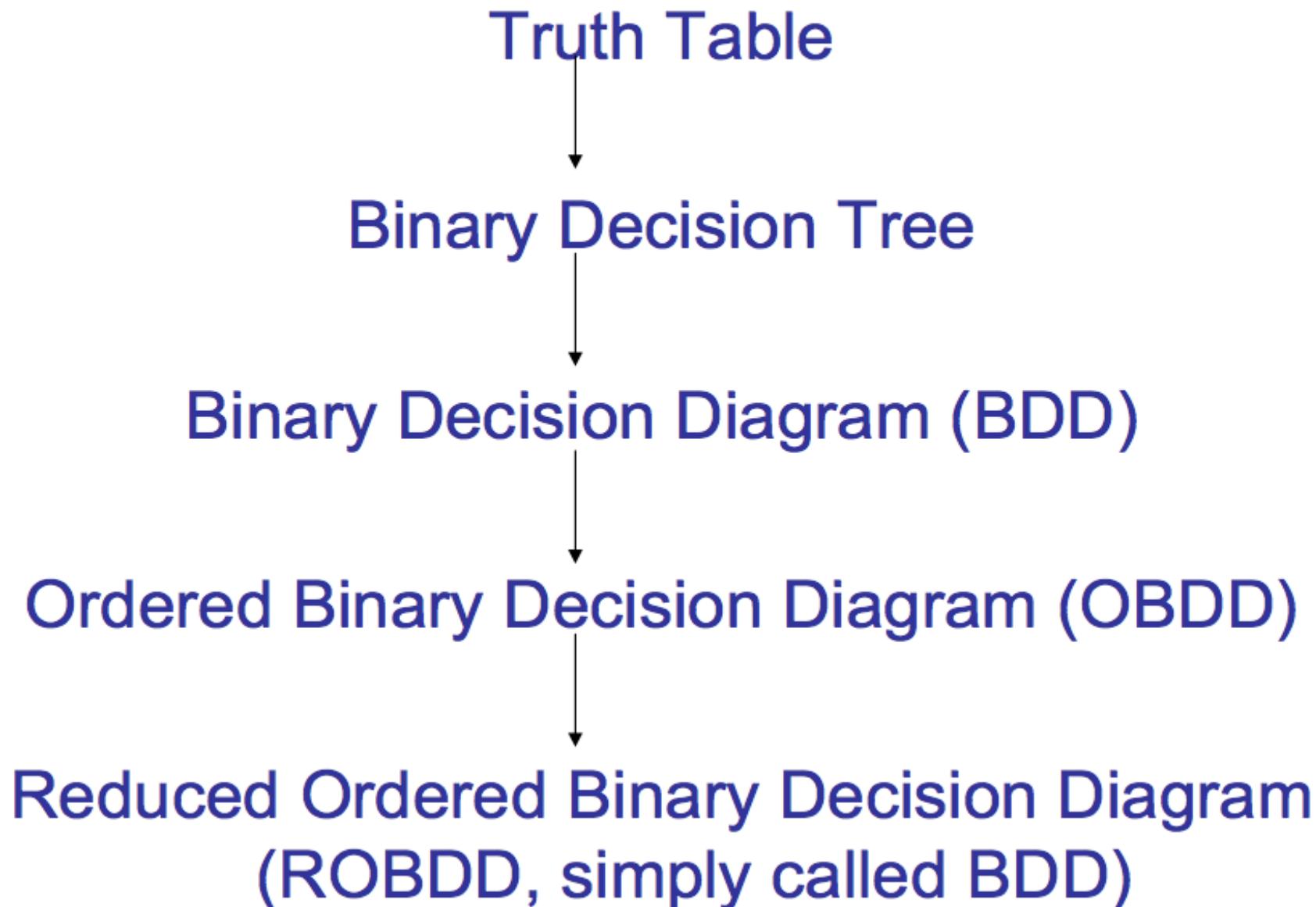


Z3

Truth table, boolean function

from		to		
x_1	x_2	x_3	x_4	f
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

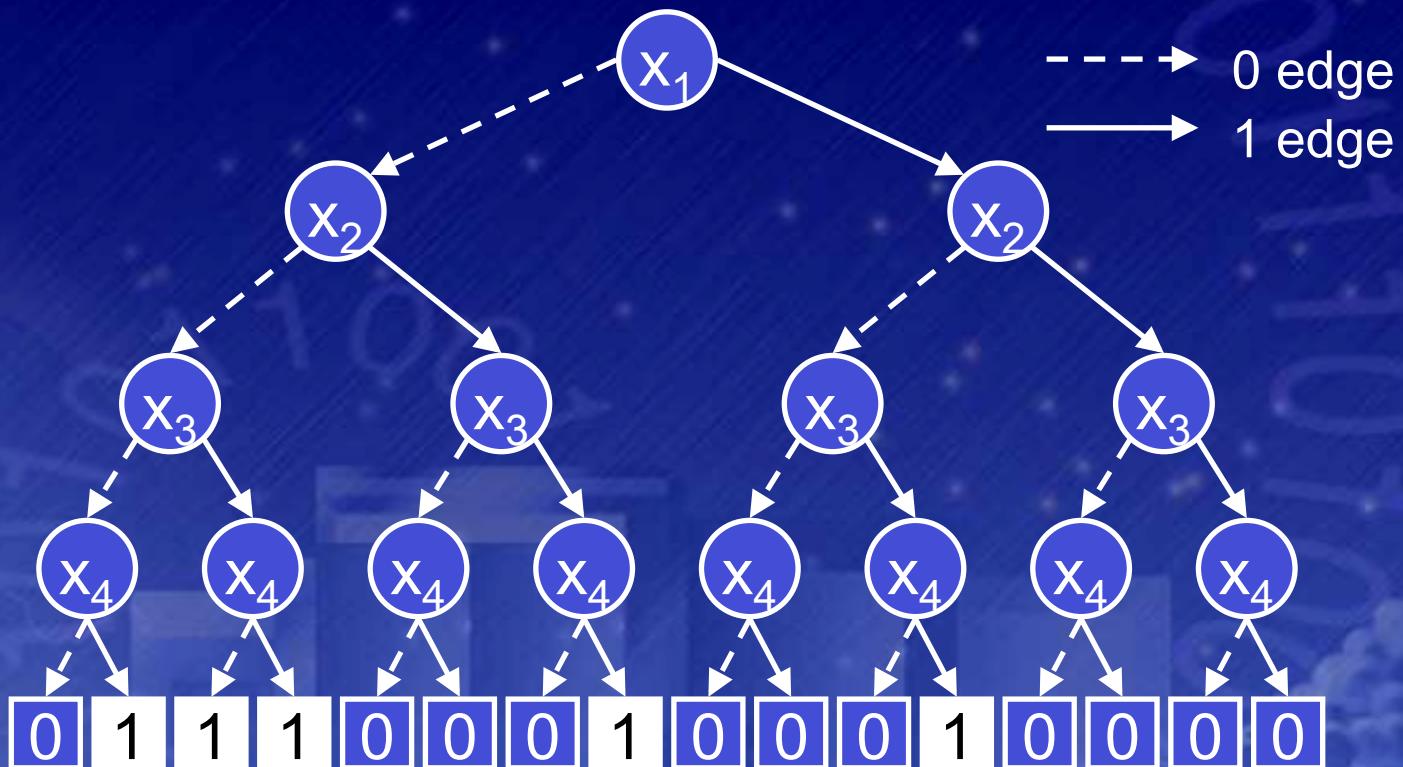
BDDs from Truth Tables



Binary Decision Diagrams

(Bryant 1986)
encoding of a truth table.

from		to		
x_1	x_2	x_3	x_4	f
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0



Reduction

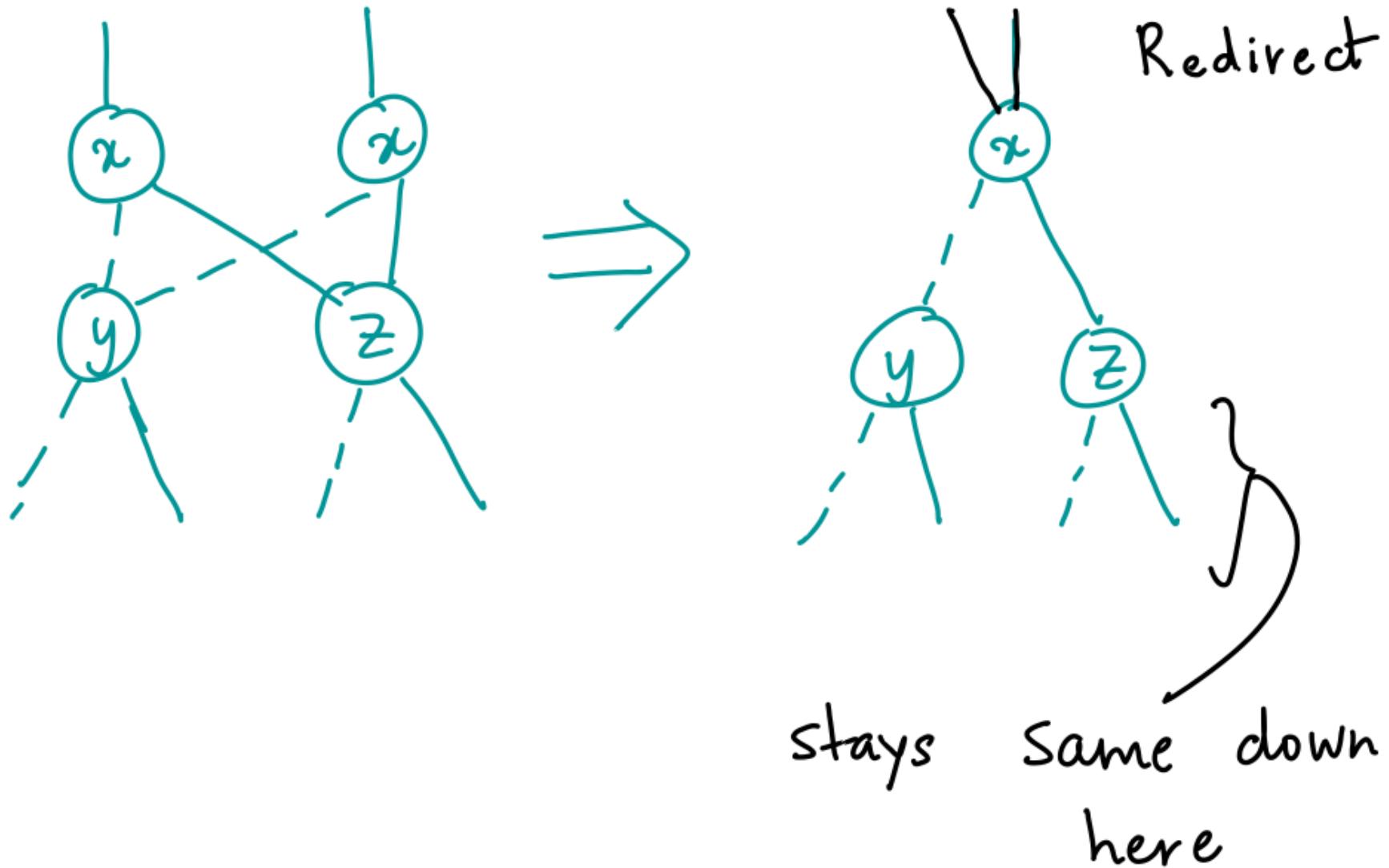
- Identify Redundancies
- 3 Rules
 - Merge equivalent leaves
 - Merge isomorphic nodes
 - Eliminate redundant tests

Merge equivalent leaves

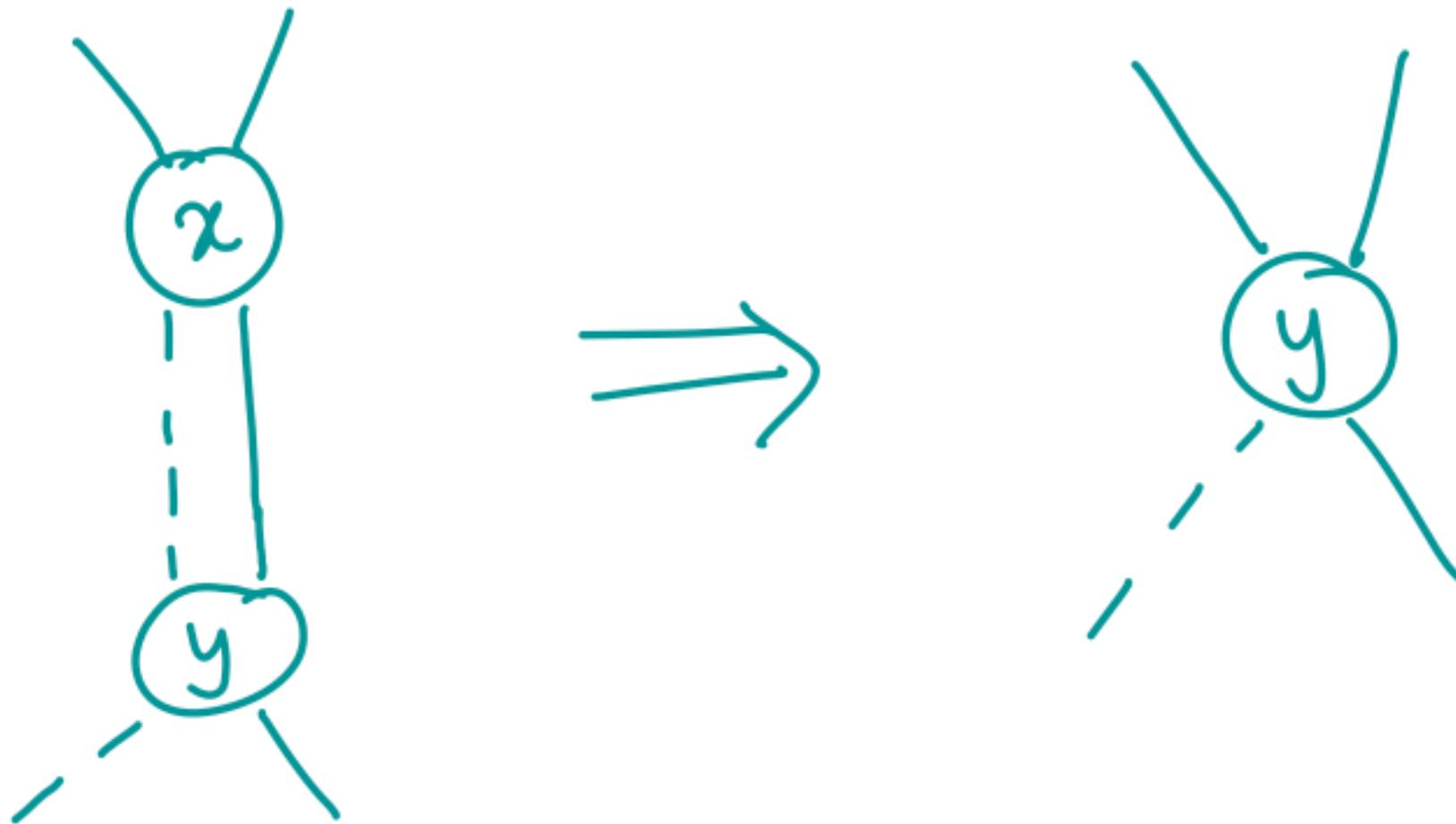


"a" is either 0 or 1

Merge isomorphic nodes

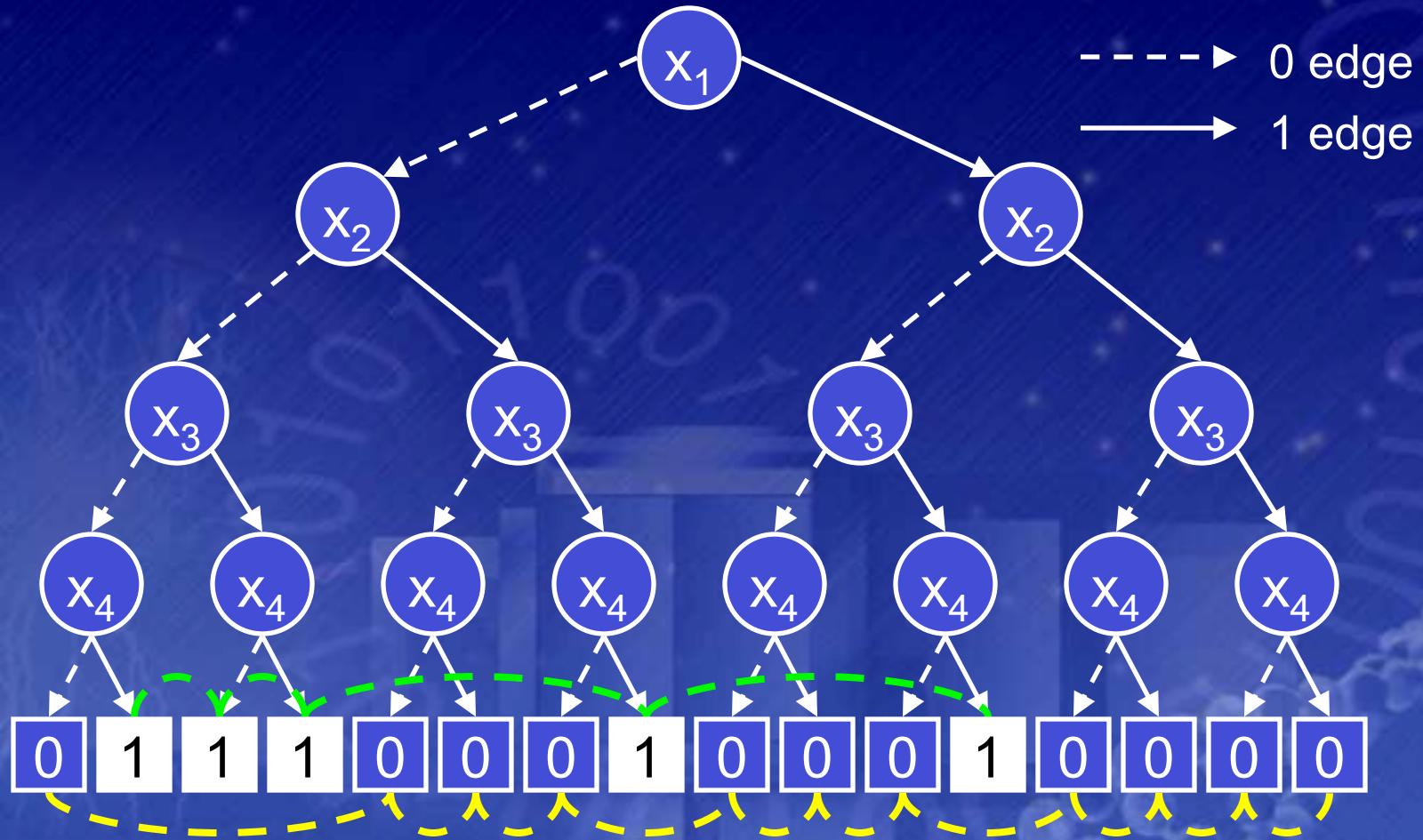


Eliminate redundant tests



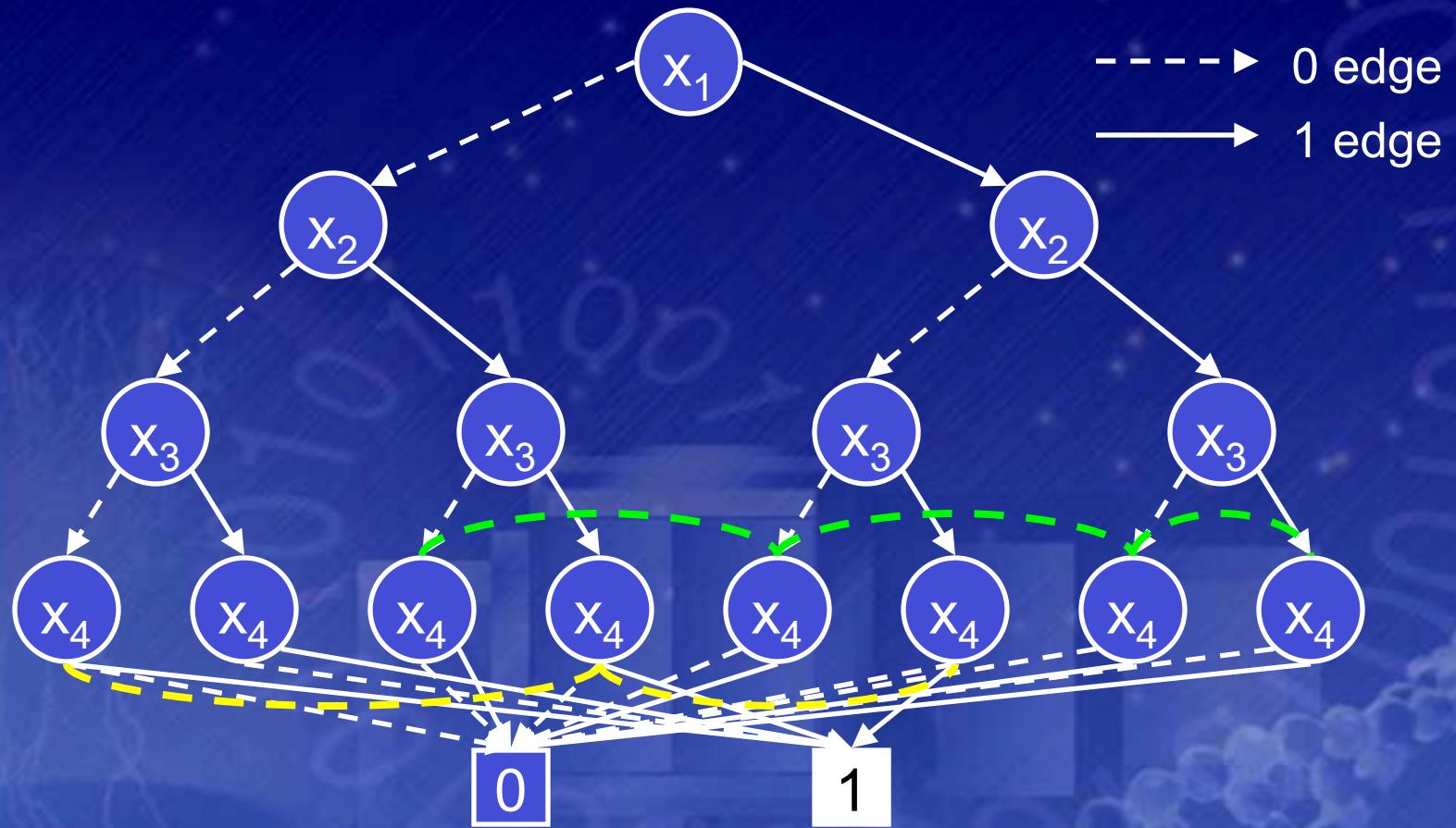
Binary Decision Diagrams

- Collapse redundant nodes.



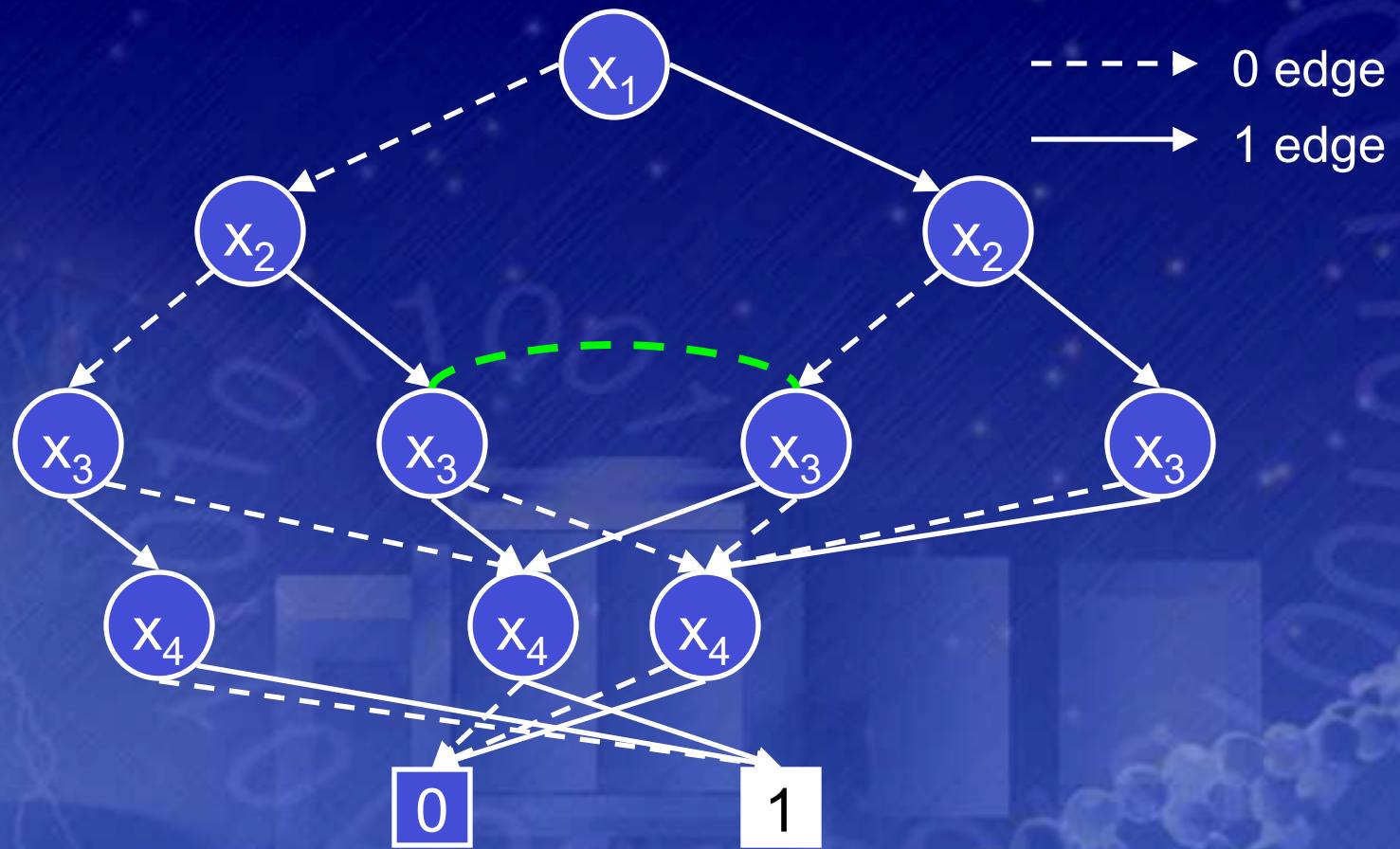
Binary Decision Diagrams

- Collapse redundant nodes.



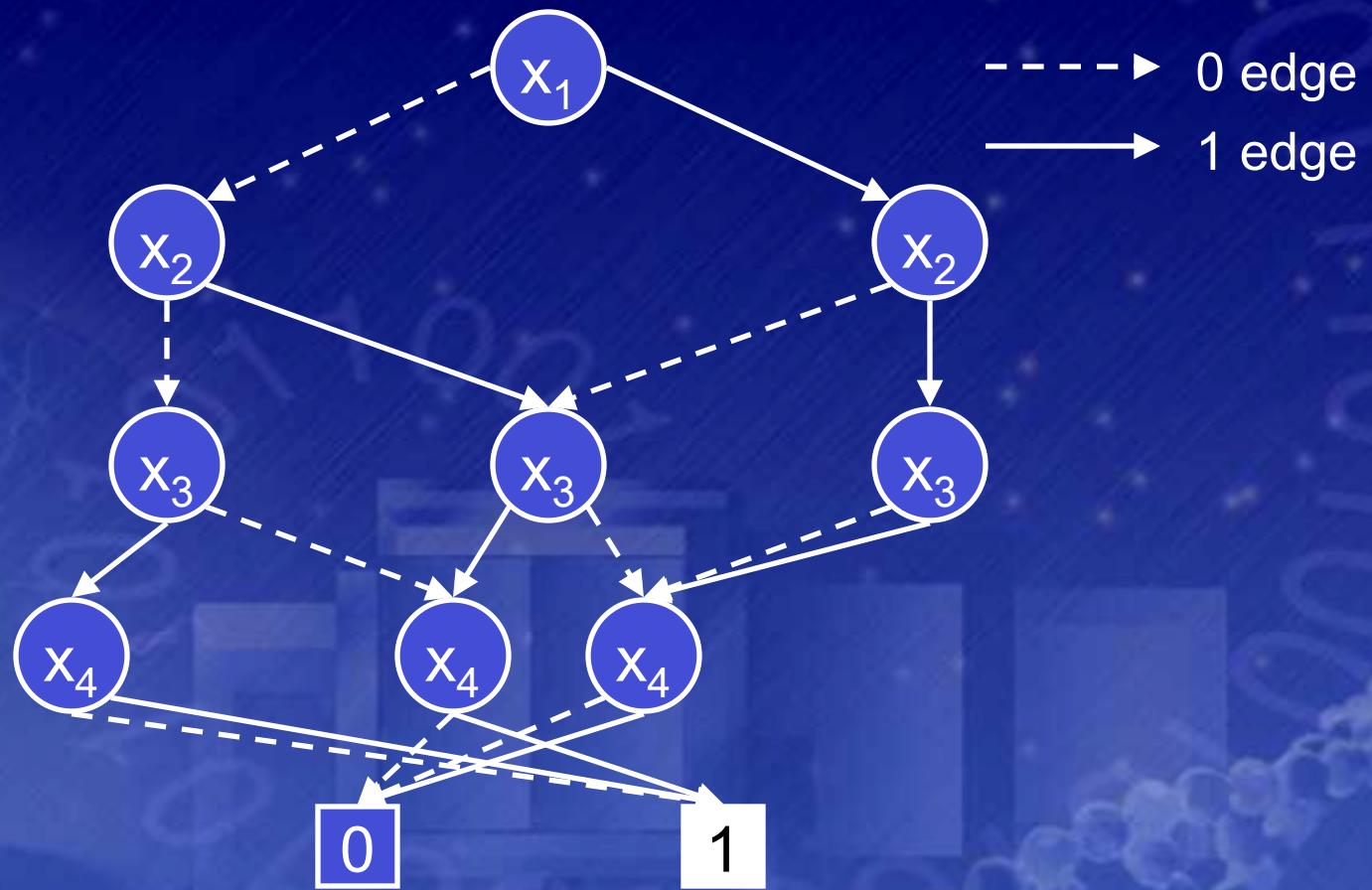
Binary Decision Diagrams

- Collapse redundant nodes.



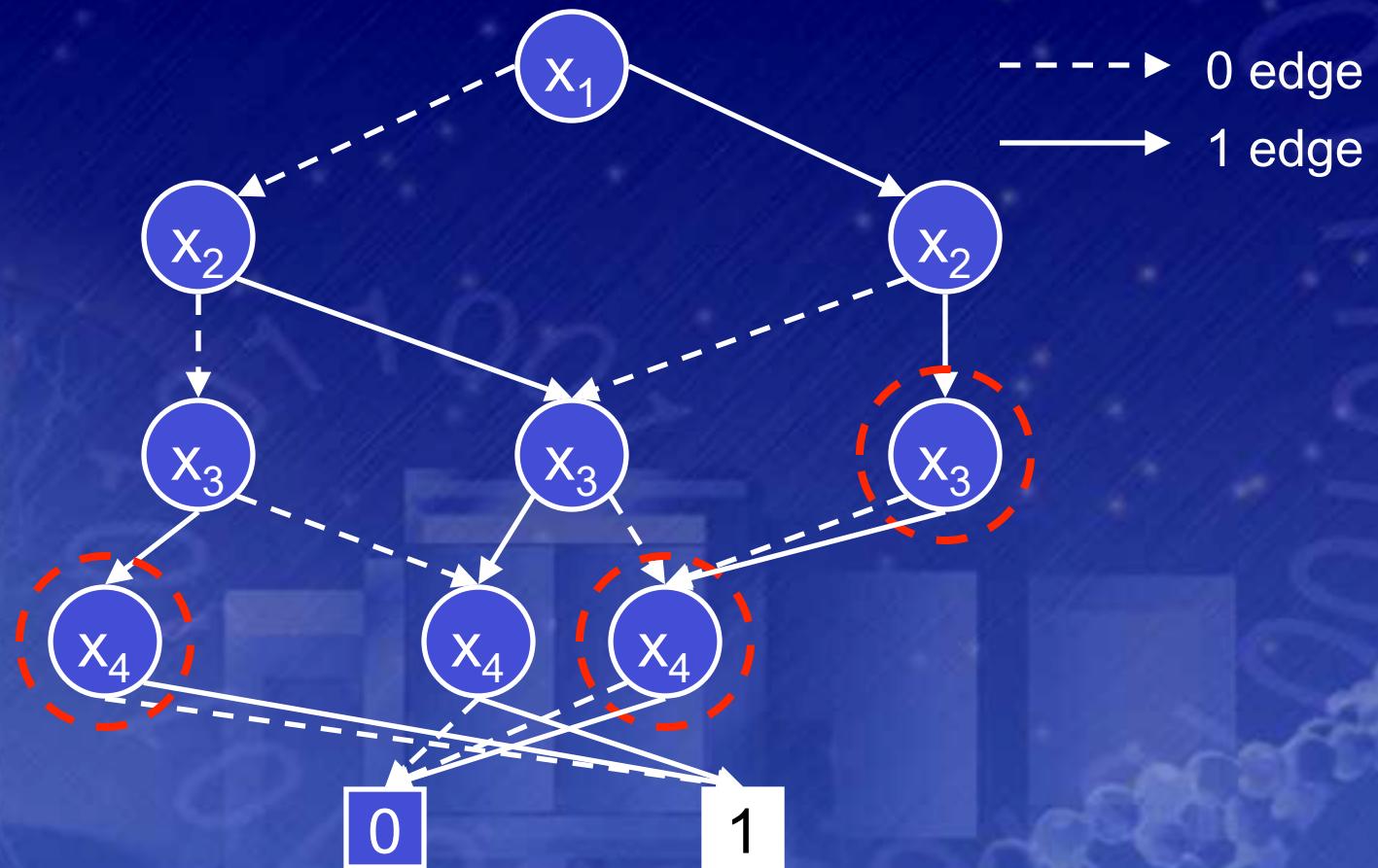
Binary Decision Diagrams

- Collapse redundant nodes.



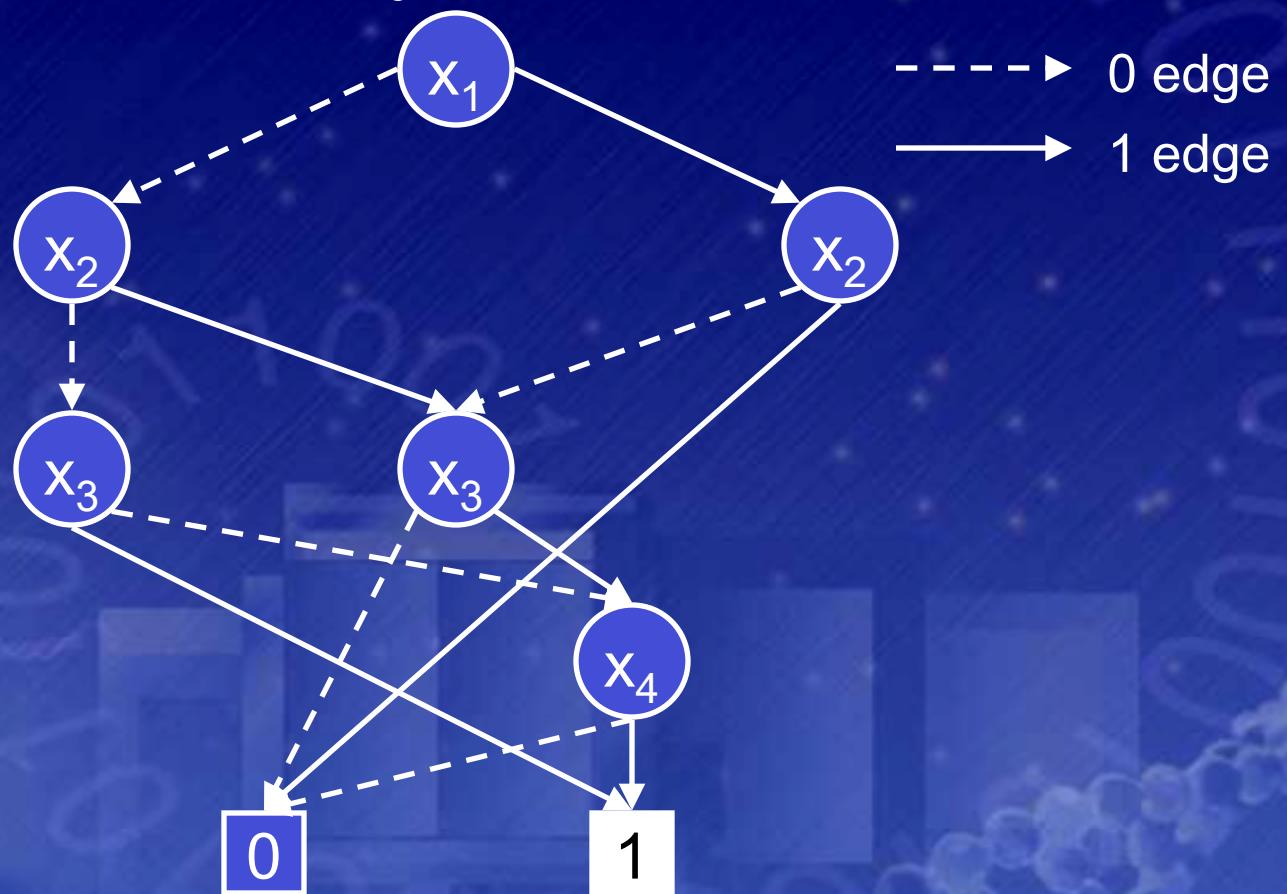
Binary Decision Diagrams

- Eliminate unnecessary nodes.



Binary Decision Diagrams

- Eliminate unnecessary nodes.

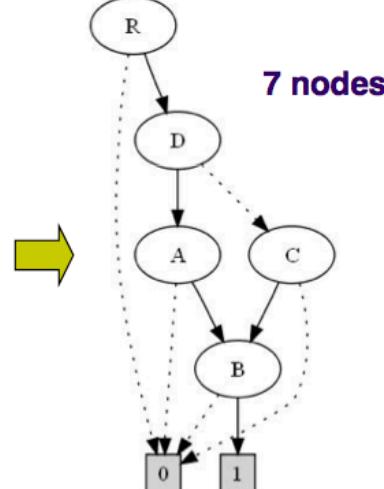
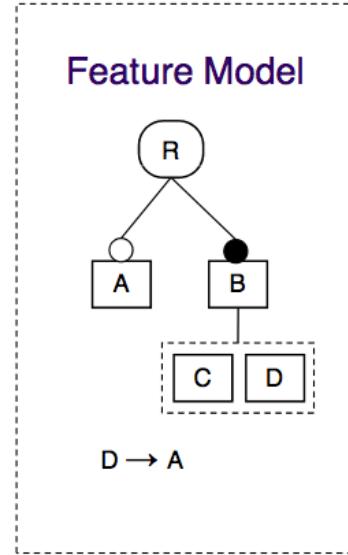
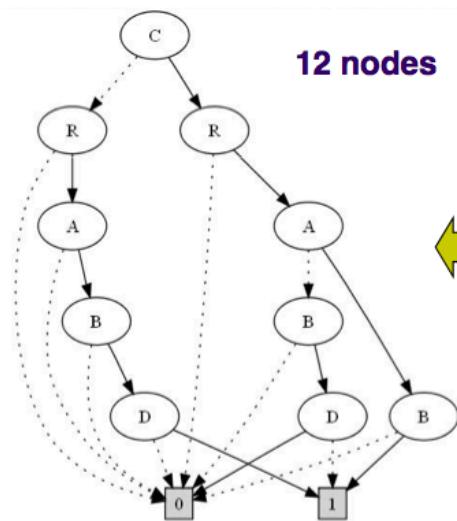


Binary Decision Diagrams (BDDs)

- Very efficient structure for most of the satisfiability operations
- Polynomial in time for checking satisfiability and determining equivalence between two BDDs
- Graph traversal
- So great?

Binary Decision Diagrams (BDDs): Theoretical Problem

- The size of the BDD is very sensitive to the order of the BDD variables
 - e.g. two equivalent BDDs for the same feature

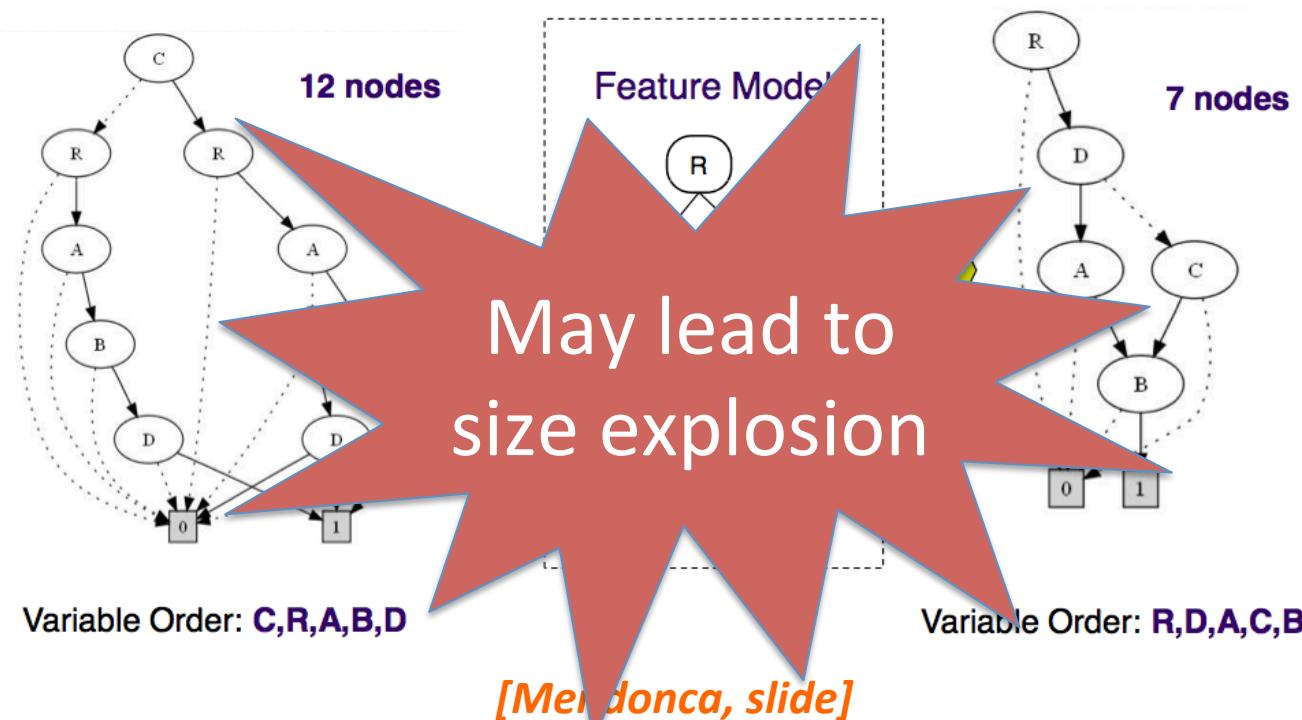


Variable Order: **C,R,A,B,D**

Variable Order: **R,D,A,C,B**

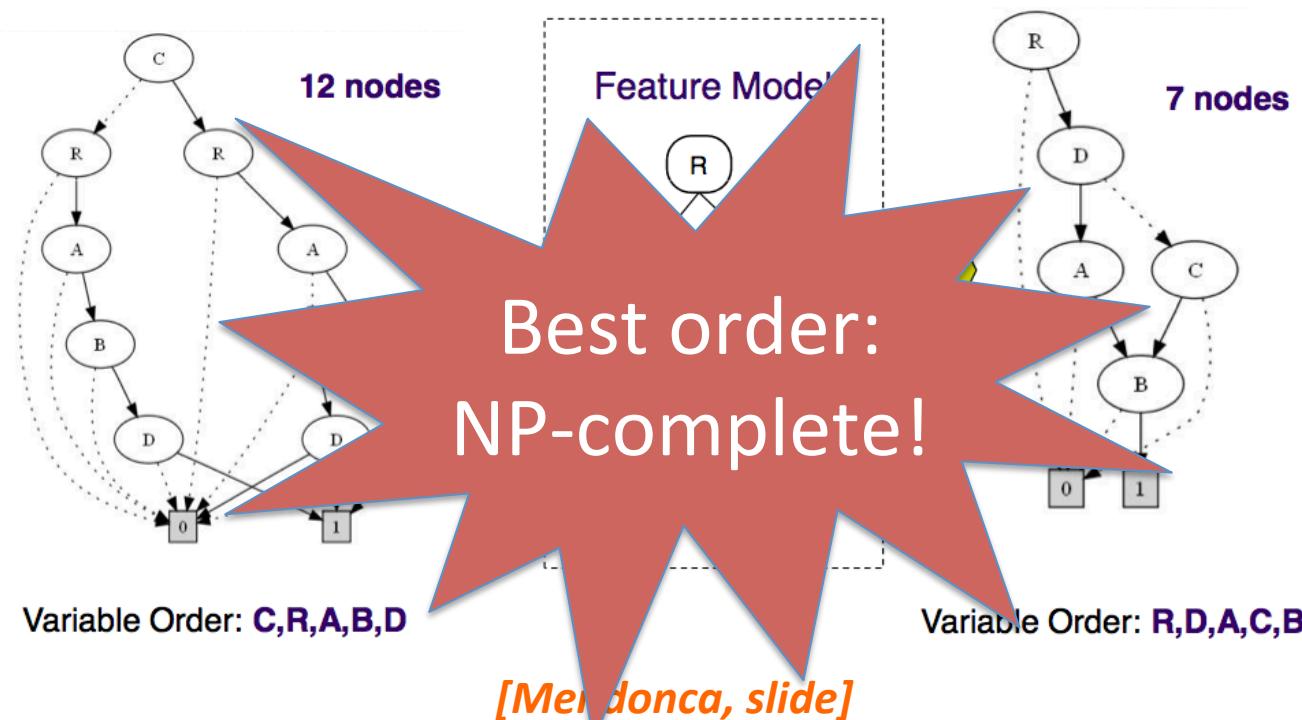
Binary Decision Diagrams (BDDs): Theoretical Problem

- The size of the BDD is very sensitive to the order of the BDD variables
 - e.g. two equivalent BDDs for the same feature



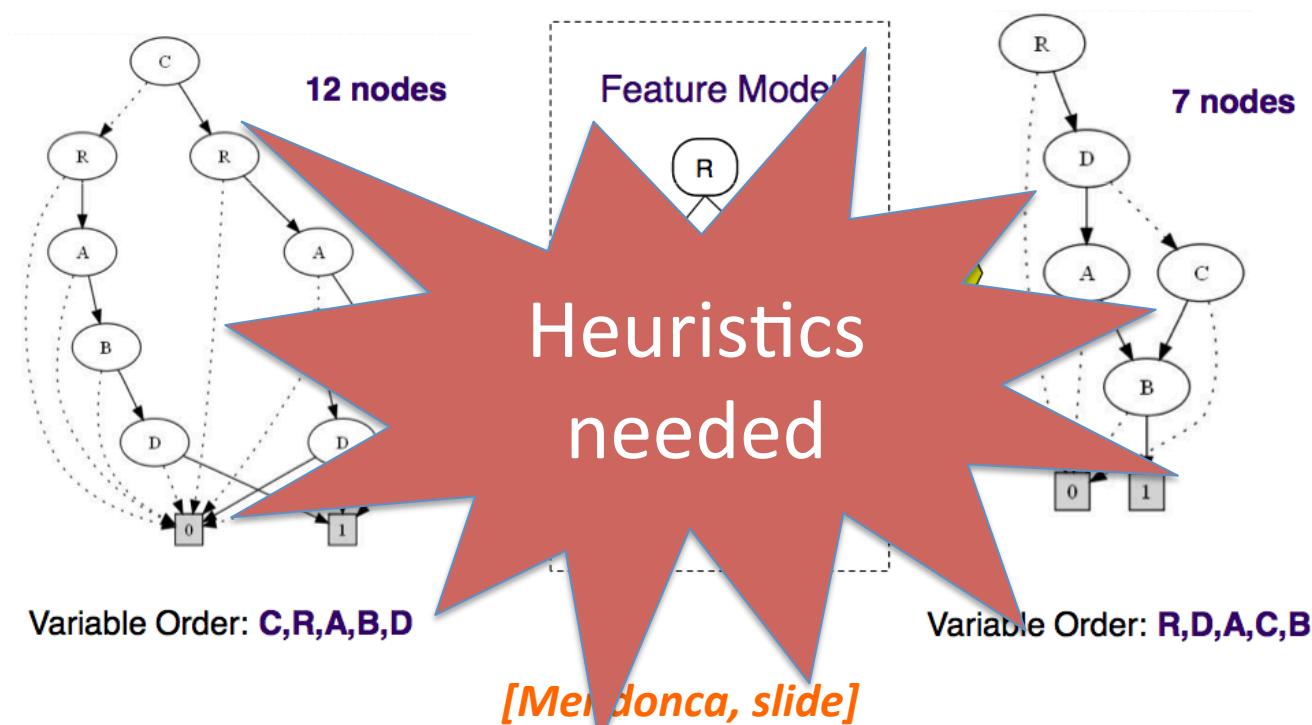
Binary Decision Diagrams (BDDs): Theoretical Problem

- The size of the BDD is very sensitive to the order of the BDD variables
 - e.g. two equivalent BDDs for the same feature



Binary Decision Diagrams (BDDs): Practical Problem

- The size of the BDD is very sensitive to the order of the BDD variables. In practice: **BDDs cannot be build for feature models with 2000+ features**

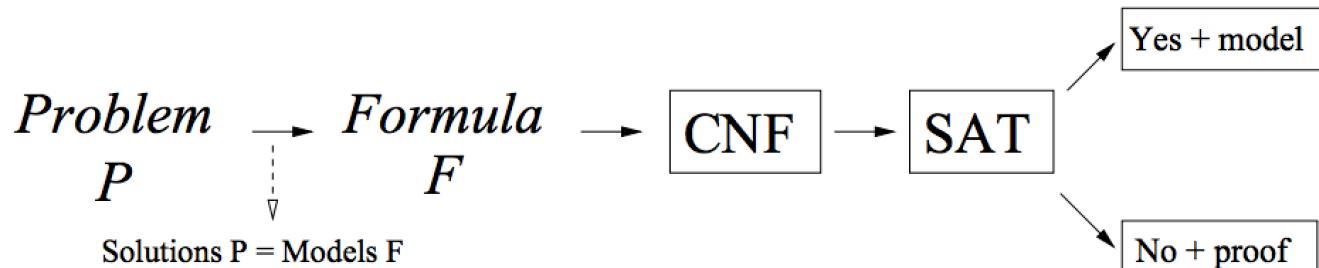


How to automate analysis of your feature models?

Let us try with SAT solvers

Satisfiability (SAT) solver

- A “SAT solver” is a program that automatically decides whether a propositional logic formula is satisfiable.
 - If it is satisfiable, a SAT solver will produce an example of a truth assignment that satisfies the formula.



- Basic idea: since all NP-complete problems are mutually reducible:
 - Write one really good solver for NP-complete problems (in fact, get lots of people to do it. Hold competitions.)
 - Translate your NP-complete problems to that problem.

SAT solver and CNF

- All current fast SAT solvers work on CNF
- Terminology:
 - A literal is a propositional variable or its negation (e.g., p or $\neg q$).
 - A clause is a disjunction of literals (e.g., $(p \vee \neg q \vee r)$). Since \vee is associative, we can represent clauses as lists of literals.
- A formula is in conjunctive normal form (CNF) if it is a conjunction of clauses
 - e.g., $(p \vee q \vee \neg r) \wedge (\neg p \vee s \vee t \vee \neg u)$

SAT solver and Unit Propagation

- Whenever all the literals in a clause are false except one, the remaining literal must be true in any satisfying assignment (such a clause is called a **unit clause**).
 - Therefore, the algorithm can assign it to true immediately. After choosing a variable there are often many unit clauses.
 - Setting a literal in a unit clause often creates other unit clauses, leading to a cascade.

$$\{\neg p \vee q, \neg p \vee \neg q \vee r, p, \neg r\}.$$

$$\begin{array}{c|c} \begin{array}{l} \neg p \vee q \\ \neg p \vee \neg q \vee r \\ p \\ \neg r \end{array} & \begin{array}{l} q \\ \neg q \vee r \\ \neg r \end{array} \end{array}$$

- A good SAT solver often spends 80-90% of its time in unit propagation.

$$\begin{aligned}
\mathcal{F}_{\text{unit}} := & (\neg x_1 \vee \neg x_3 \vee x_4) \wedge (\neg x_1 \vee \neg x_2 \vee x_3) \\
& (\neg x_1 \vee x_2) \wedge (x_1 \vee x_3 \vee x_6) \wedge (\neg x_1 \vee x_4 \vee \neg x_5) \\
& (x_1 \vee \neg x_6) \wedge (x_4 \vee x_5 \vee x_6) \wedge (x_5 \vee \neg x_6)
\end{aligned}$$

$$\begin{aligned}\mathcal{F}_{\text{unit}} := & (\neg x_1 \vee \neg x_3 \vee x_4) \wedge (\neg x_1 \vee \neg x_2 \vee x_3) \\ & (\neg x_1 \vee x_2) \wedge (\textcolor{red}{x}_1 \vee x_3 \vee x_6) \wedge (\neg x_1 \vee x_4 \vee \neg x_5) \\ & (\textcolor{red}{x}_1 \vee \neg x_6) \wedge (x_4 \vee x_5 \vee x_6) \wedge (x_5 \vee \neg x_6)\end{aligned}$$

$$\varphi = \{x_1=1\}$$

$$\begin{aligned}
\mathcal{F}_{\text{unit}} := & (\neg x_1 \vee \neg x_3 \vee x_4) \wedge (\neg x_1 \vee \neg x_2 \vee x_3) \\
& (\neg x_1 \vee x_2) \wedge (\textcolor{green}{x_1} \vee x_3 \vee x_6) \wedge (\neg x_1 \vee x_4 \vee \neg x_5) \\
& (\textcolor{green}{x_1} \vee \neg x_6) \wedge (x_4 \vee x_5 \vee x_6) \wedge (x_5 \vee \neg x_6)
\end{aligned}$$

$$\varphi = \{x_1=1, \textcolor{teal}{x_2=1}\}$$

$$\begin{aligned}
\mathcal{F}_{\text{unit}} := & (\neg x_1 \vee \neg x_3 \vee x_4) \wedge (\neg x_1 \vee \neg x_2 \vee x_3) \\
& (\neg x_1 \vee x_2) \wedge (x_1 \vee x_3 \vee x_6) \wedge (\neg x_1 \vee x_4 \vee \neg x_5) \\
& (x_1 \vee \neg x_6) \wedge (x_4 \vee x_5 \vee x_6) \wedge (x_5 \vee \neg x_6)
\end{aligned}$$

$$\varphi = \{x_1=1, x_2=1, x_3=1\}$$

$$\begin{aligned}
\mathcal{F}_{\text{unit}} := & (\neg x_1 \vee \neg x_3 \vee x_4) \wedge (\neg x_1 \vee \neg x_2 \vee x_3) \\
& (\neg x_1 \vee x_2) \wedge (x_1 \vee x_3 \vee x_6) \wedge (\neg x_1 \vee x_4 \vee \neg x_5) \\
& (x_1 \vee \neg x_6) \wedge (x_4 \vee x_5 \vee x_6) \wedge (x_5 \vee \neg x_6)
\end{aligned}$$

$$\varphi = \{x_1=1, x_2=1, x_3=1, x_4=1\}$$

SAT solver and Unit Propagation

BCP():

Repeatedly search for unit clauses, and
set unassigned literal to required value.

If a literal is assigned conflicting values, return F
else return T;

satisfy(ϕ) {

if every clause of ϕ has a true literal, return T;

if BCP() == F, return F;

assign appropriate values to all pure literals;

choose an $x \in V$ that is unassigned in A ,

and choose $v \in \{T, F\}$.

$A(x) = v$;

if satisfy(ϕ) return T;

$A(x) = \neg v$;

if satisfy(ϕ) return T;

unassign $A(x)$; // undo assignment for backtracking.

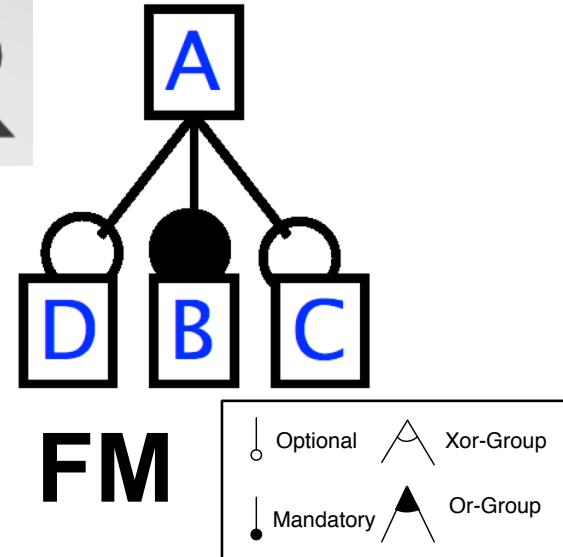
return F; }

How to automate analysis of your feature models?

Let us use BDDs and SAT solvers

$A \wedge$
 $A \Leftrightarrow B \wedge$
 $C \Rightarrow A \wedge$
 $D \Rightarrow A$

FAMILiAR



φ

```

fm1bis = FM ("foo3.dimacs")
fm1bisbis = FM ("foo3.constraints")

```

```

fml> c1 = cores fm1
fml> s1c1: (SET) {B;A}
s1: (SET) {A;B}
fml> c1bis = cores fm1bis
fml> compare fm1 fm1bis
s1bis: (SET) {A;B;D}
res7: (STRING) REFACTORING
fml> compare fm1bis fm1bisbis
s1bis: (SET) {A;B;D}
res8: (STRING) REFACTORING
fml> c1 eq c1bisbis
res3: (BOOLEAN) true
fml> s1res6: (BOOLEAN) true
res4: (BOOLEAN) true

```

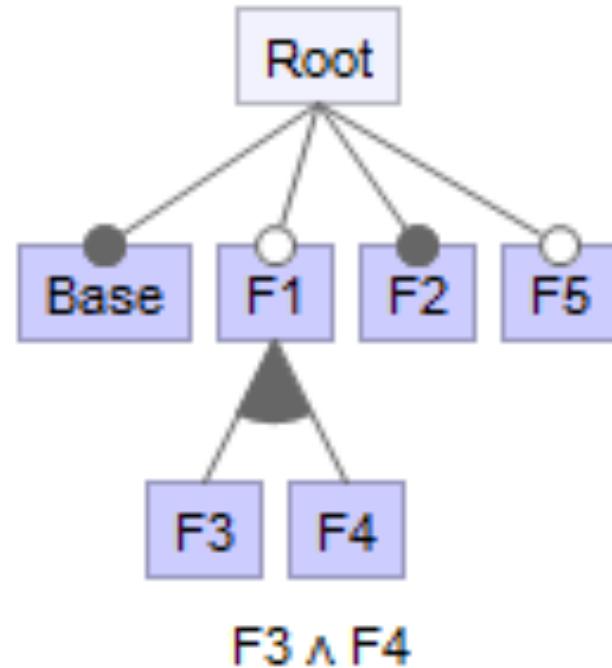
```

fml> fm1 = FM ("output/fm1.tvl")
root A {
    group [ 3..3 ] {
        opt D {
            },
            B {
            },
        opt C {
            }
    }
}
fm1: (FEATURE_MODEL) A: [D] B [C] ;

```

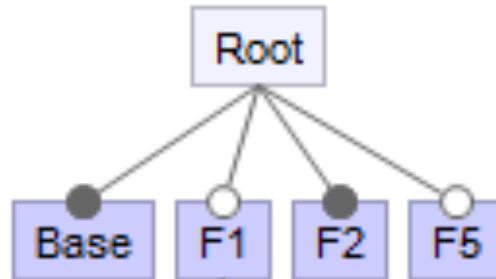
Consistency

- SAT-Solver
 - SAT(FM)



Core and dead features

- Dead : $\text{SAT}(\text{FM} \wedge F)$
- Core: $\text{SAT}(\text{FM} \wedge \text{not}(F))$



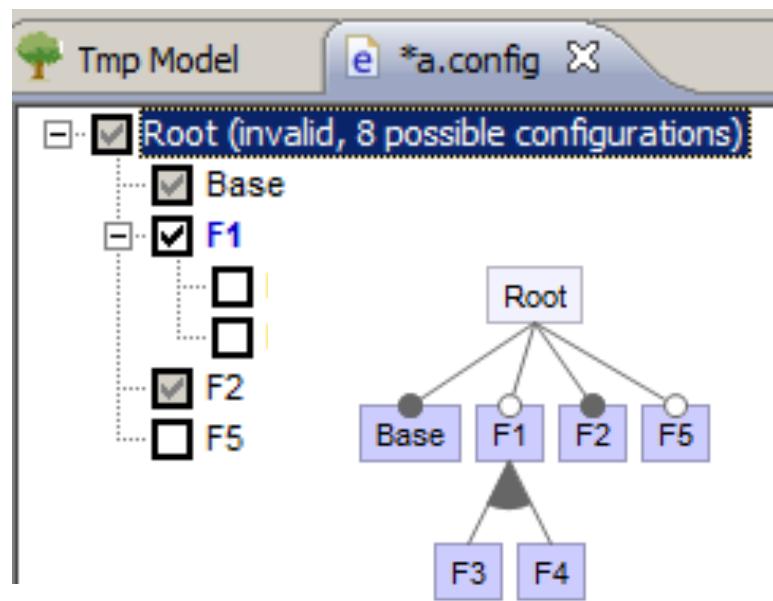
$$F5 \Rightarrow F4 \vee \text{Base}$$

$$F3 \Rightarrow F2 \wedge F5$$

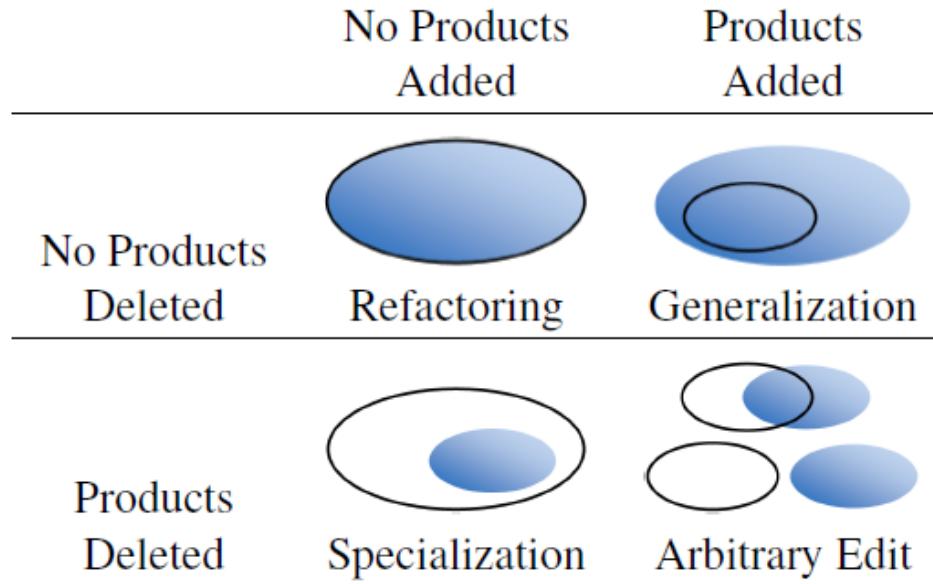
$$\neg(F4 \wedge F2)$$

Partial configuration

- $SAT(FM \wedge PK \wedge F)$
- $SAT(FM \wedge PK \wedge \neg(F))$



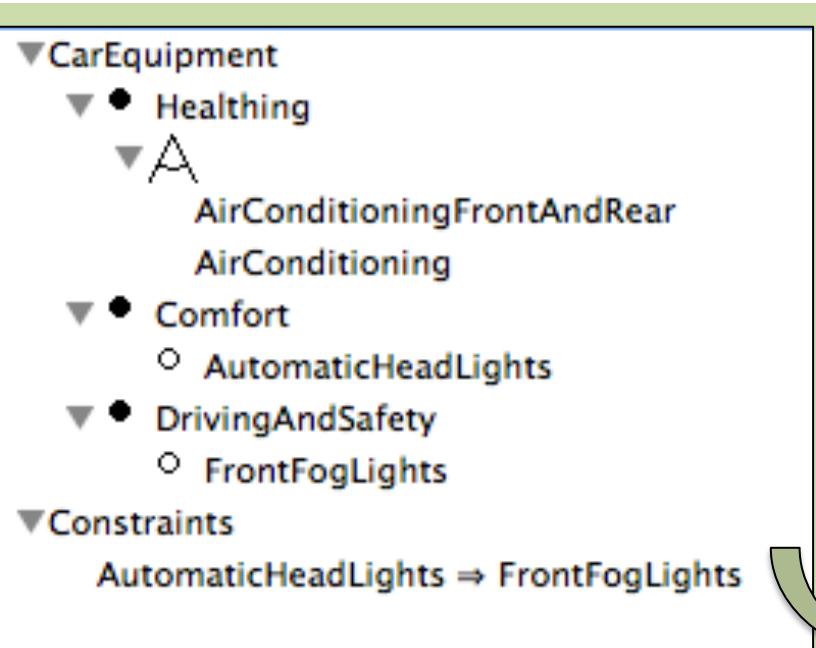
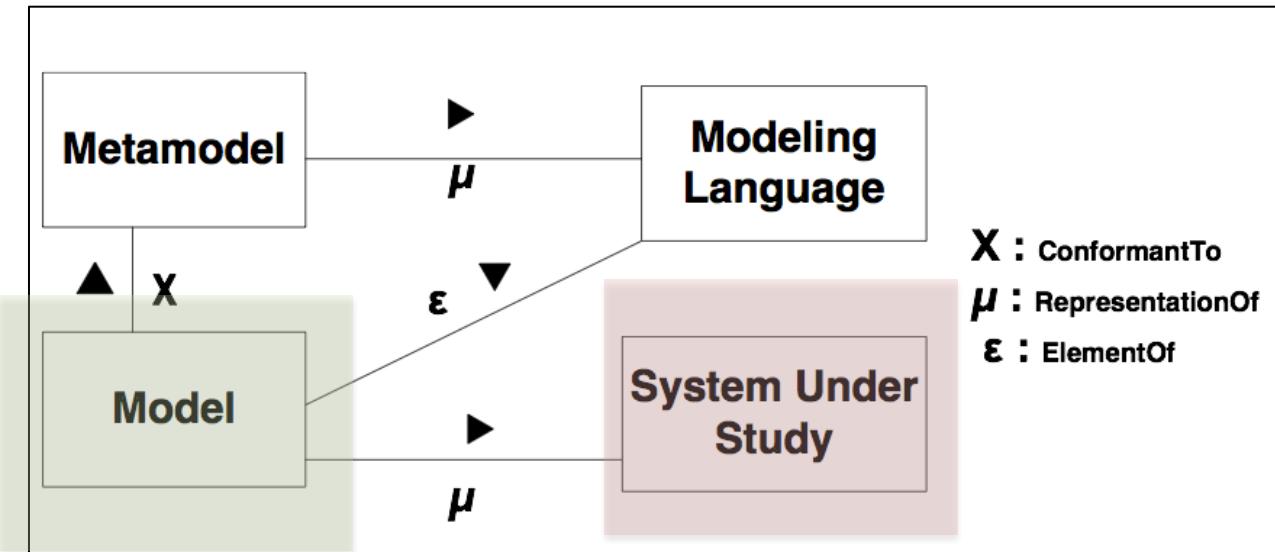
Relationship between feature models



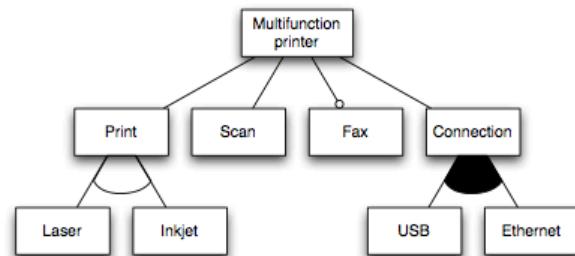
- Refactoring
 - Tautology: $(FM1 \Leftrightarrow FM2)$
 $= \text{not SAT}(\text{not } (FM1 \Leftrightarrow FM2))$

Recap

Feature Models



Typical implementations



result



logics



solvers



Z3

FAMILIAR

(FeAture Model script Language for manipulation and Automatic Reasoning)

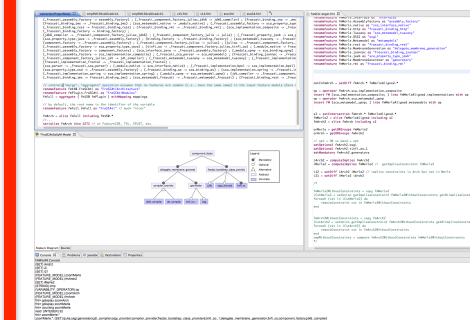
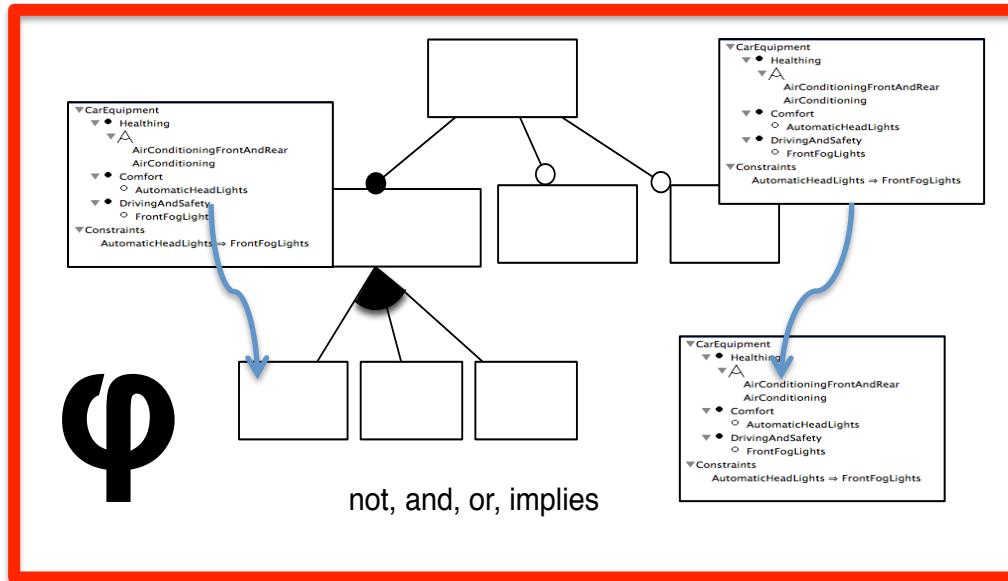
<http://familiar-project.github.com/>



S.P.L.O.T.
Software Product Lines Online Tools



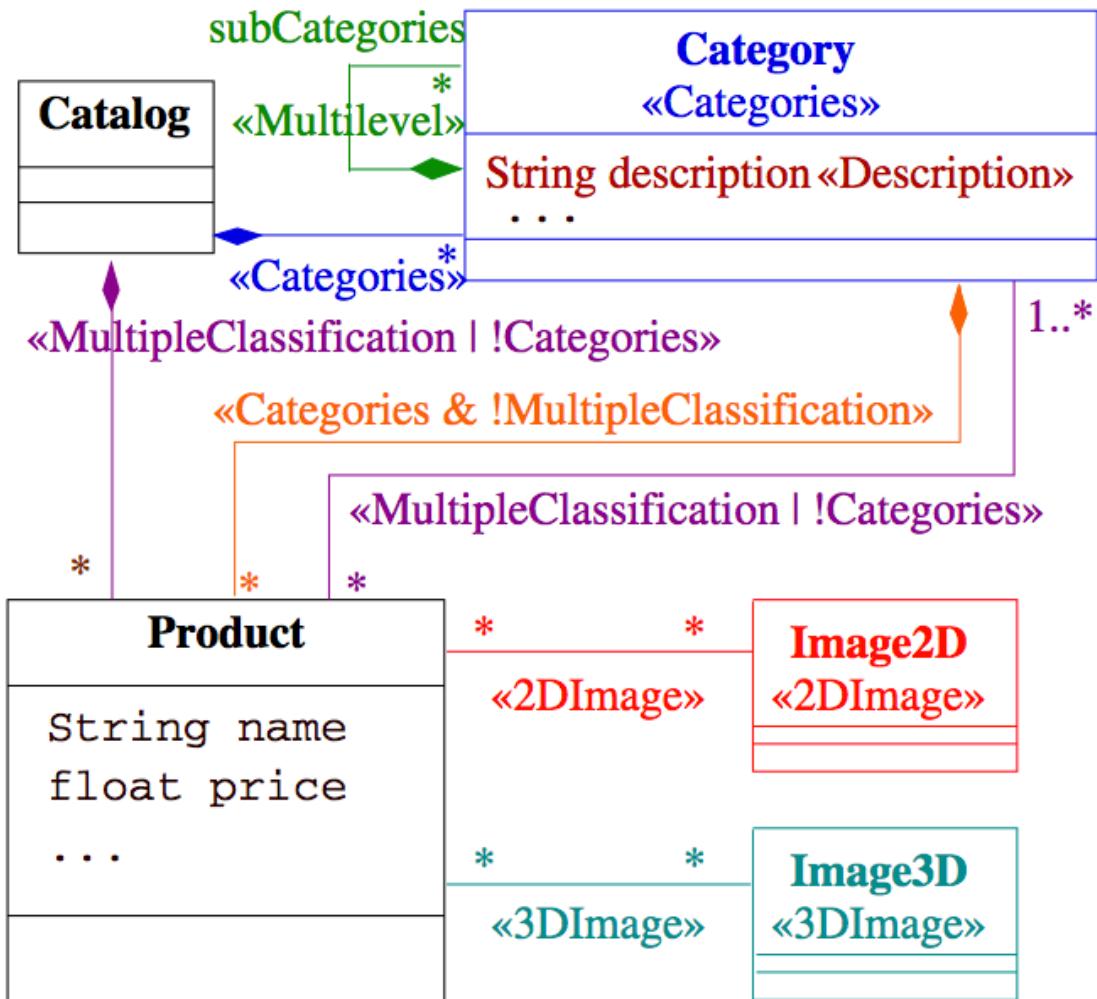
TVL
DIMACS

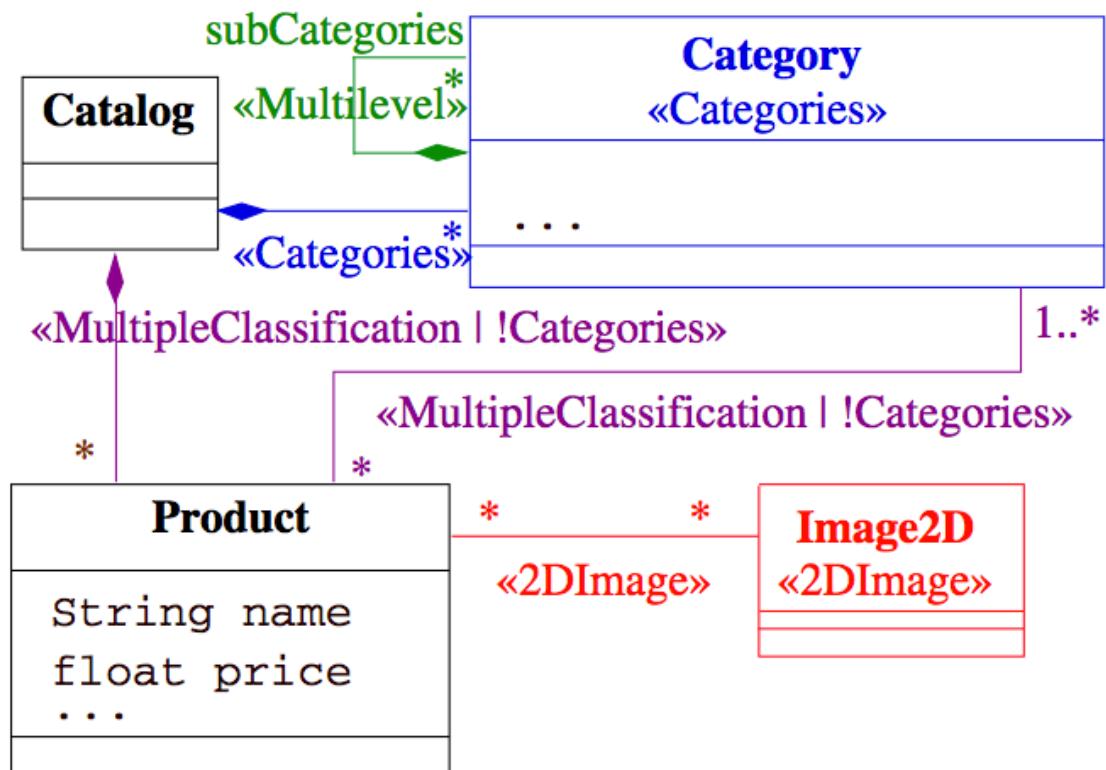
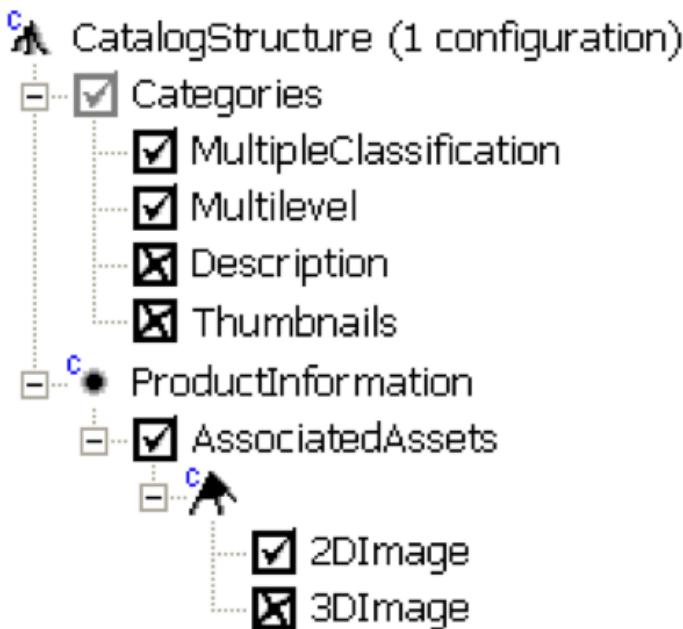


importing, exporting, composing, decomposing, editing, configuring,
reverse engineering, computing "diffs", refactoring, testing,
and reasoning about (multiple) variability models

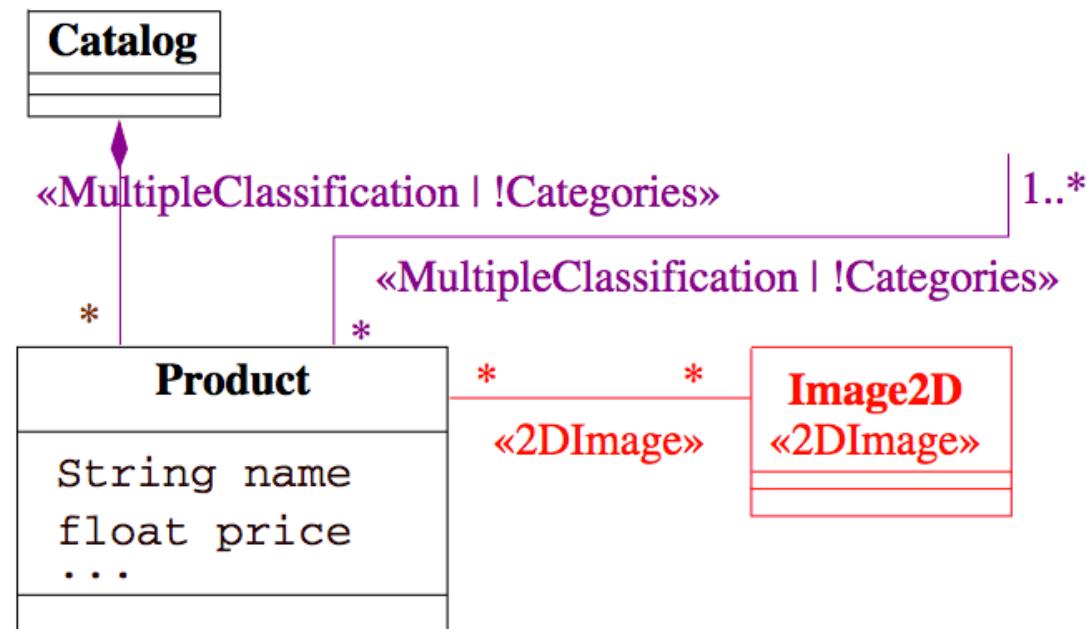
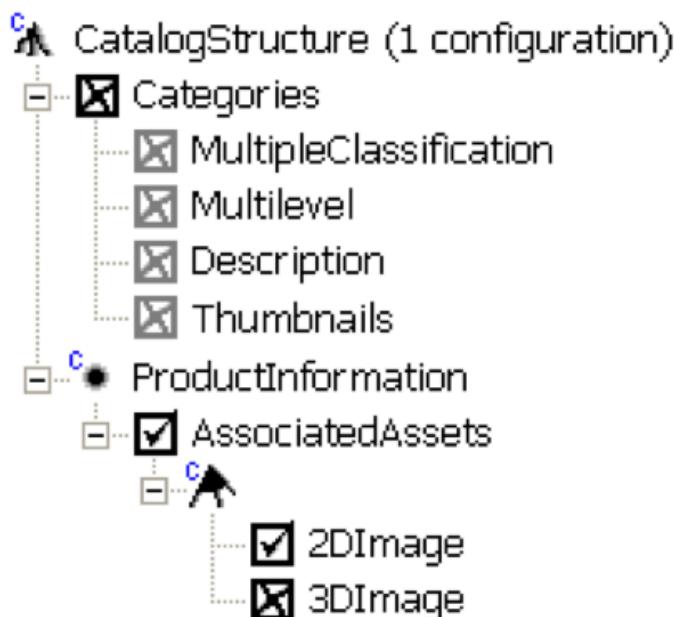
▲ CatalogStructure (52 configurations)

- Categories
 - MultipleClassification
 - Multilevel
 - Description
 - Thumbnails
- ProductInformation
 - AssociatedAssets
 - 2DImage
 - 3DImage





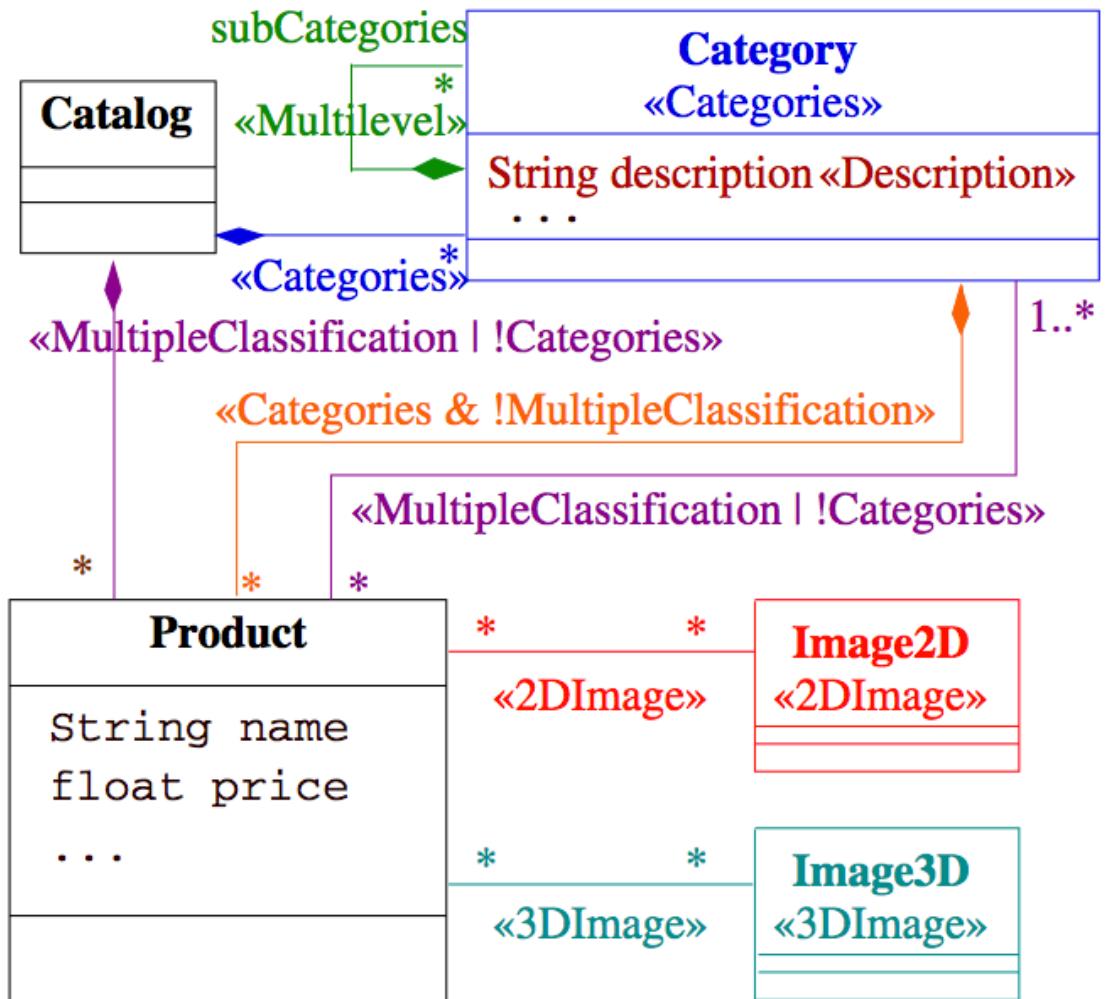
Ooops



Safe composition? No!

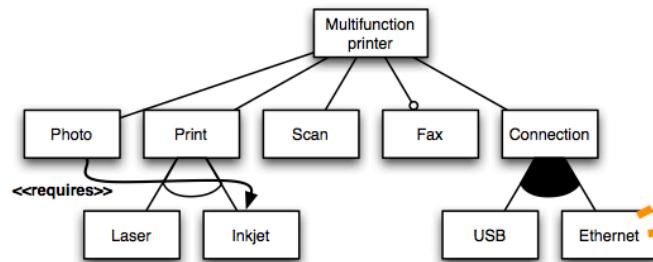
CatalogStructure (52 configurations)

- Categories
 - MultipleClassification
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Product Derivation

feature model

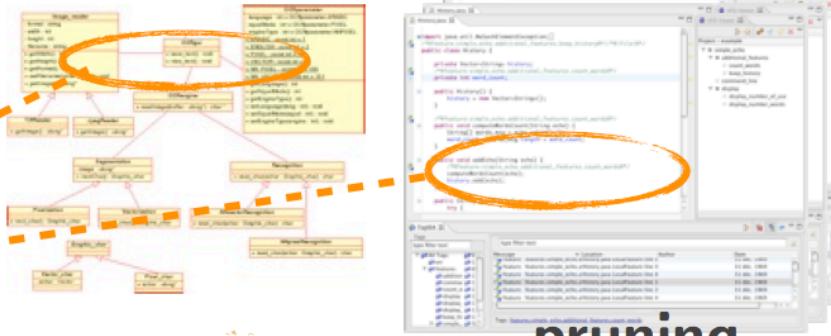


configuration

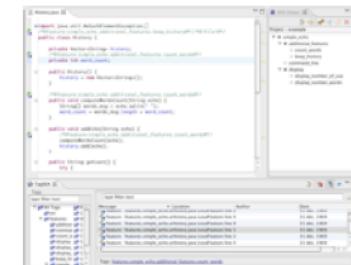
{ MP, Photo, Print, Inkjet, Scan,
Fax, Connection, USB, Ethernet }

product spec

variable model and
code assets

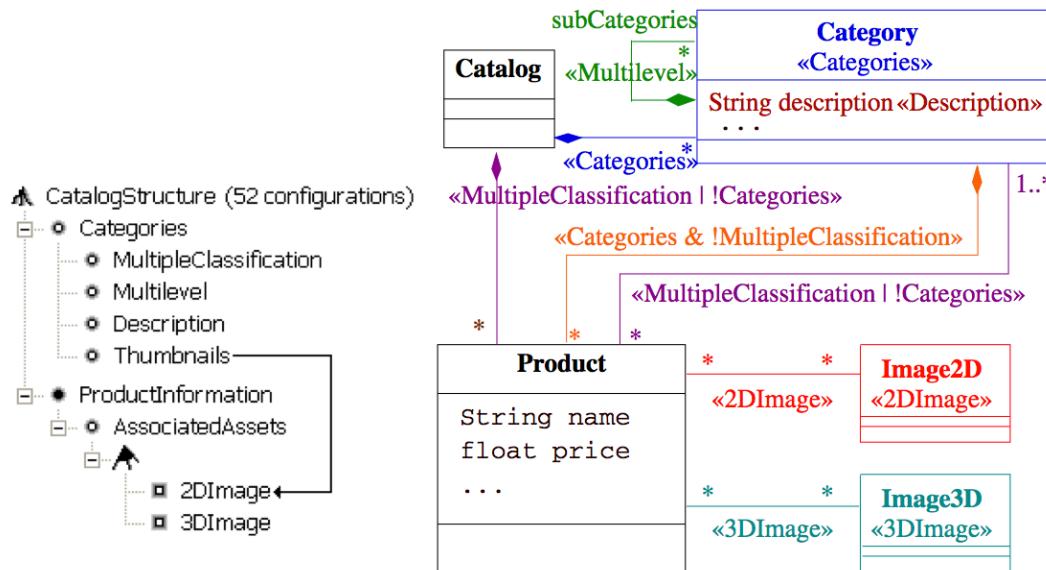


pruning,
composition,
weaving,
transformation



product

Safe composition: how does it work?



```

qFM          =
root:        cs ∧
child-parent: (ct ⇒ cs) ∧ (mc ⇒ ct) ∧ (ml ⇒ ct) ∧
              (ds ⇒ ct) ∧ (tn ⇒ ct) ∧ (pi ⇒ cs) ∧
              (aa ⇒ pi) ∧ (i2 ⇒ aa) ∧ (i3 ⇒ aa) ∧
              (aa ⇒ choice1,2(i2, i3)) ∧
              (cs ⇒ pi) ∧
              (tn ⇒ i2)
group:
mandatory:
additional:
  
```



**Another
propositional
formula**