COMP3314_2C Machine Learning

Homework:

Release date: March 12, 2024

Due date: 11:59pm, March 22, 2024

- Consider a Perceptron with 2 inputs and 1 output. Let the weights of the Perceptron be w1=1 and w2=1 and let the bias be w0=-1.5. Calculate the output of the following inputs:(0, 0), (1, 0), (0, 1), (1, 1). (12 points)
- 2. Suppose that the following are a set of point in two classes:
 - Class1: (1,1), (1,2), (2,1)
 - Class2: (0,0), (1,0), (0,1)
 - (1) Plot them and find the optimal separating line. (10 points)
 - (2) What are the support vectors, and what is the meaning? (14 points)
- 3. Suppose that the probability of five events are P(first) = 0.5, P(second) = P(third) = P(fourth) = P(fifth) = 0.125. Calculate the entropy and write down in words what this means. (14 points)
- 4. Suppose we collect data for a group of students in a postgraduate machine learning class with features x1 = hours studies, x2 = undergraduate GPA and label y = receive an A. We fit a logistic regression and produce estimated weights as follows: w0=-6, w1=0.05, w2=1.
 - (1) Estimate the probability that a student who studies for 40h and has an undergraduate GPA of 3.5 gets an A in the class. (10 points)
 - (2) How many hours would the student in part 1. need to study to have a 50% chance of getting an A in the class? (10 points)

5. Given the following dataset:

V	W	X	Y
0	0	0	0
0	1	0	1
1	0	0	1
1	1	0	0
1	1	1	0

Your task is to build a decision tree for classifying variable Y. (You can think of the dataset as replicated many times, i.e. overfitting is not an issue here).

(1) Compute the information gains IG(Y|V), IG(Y|W) and IG(Y|X). Remember, information gain is defined as

$$IG(D_p) = I_G(D_p) - \sum_{i=1}^m \frac{N_j}{N_p} I_G(D_j)$$

where

$$I_G(t) = 1 - \sum_{i=1}^{c} p(i|t)^2$$

c is the class number, D_p and D_j are the dataset of the parent and j-th child node. I_G is gini impurity. N_p is the total number of samples at the parent node and N_j is the number of samples in the j-th child node. (10 points)

(2) Write down the entire decision tree with gini impurity. (20 points)