Lecture 22: Quantitative Analysis

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Based on slides by Edward Lee

Embedded Real-Time Systems

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Review

- (Embedded) Real-time OSs
 - Characteristics
 - Microkernels
 - Tasks and scheduling
 - Queues and intercommunication
 - Semaphores and synchronization
 - Other facilities
- RTOS standards

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Outline

- Worst-case execution time problem
- · Programs as Graphs
- Challenges of Execution Time Analysis
- Current Approaches
- Limitations and Future Directions

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Quantitative Analysis / Verification



Does the brake-by-wire software always actuate the brakes within 1^{ms}?

Safety-critical embedded systems

Can this new app drain my iPhone battery in an hour?

Consumer devices





How much energy must the sensor node harvest for RSA encryption?

Energy-limited sensor nets, bio-medical

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Time is Central to Cyber-Physical Systems

Several timing analysis problems

- Worst-case execution time (WCET) estimation
- Estimating the distribution of execution times
- Threshold property: can you produce a test case that causes a program to violate its deadline?
- Software-in-the-loop simulation: predict execution time of particular program path
- > Various forms of the same basic problem.

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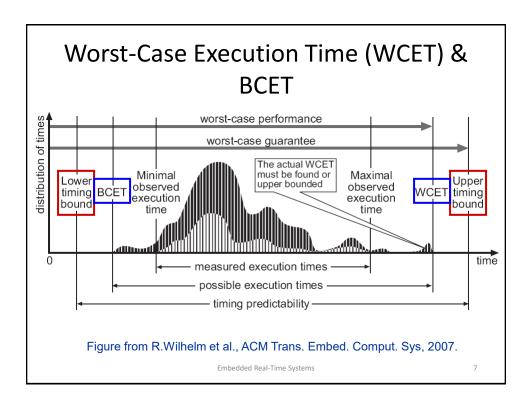
Worst-Case Execution Time (WCET)

- The longest time taken by a software task to execute
 - Function of input data and environment conditions
- BCET = Best-Case Execution Time
 - shortest time taken by the task to execute

Consider this code: *x = 10; on ARM Cortex-A9 MPCore dual core processor.

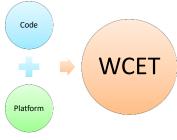
What's the WCET? BCET?

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The WCET Problem

- Given
 - the code for a software task
 - the platform (OS + hardware) that it will run on
- Determine the WCET of the task.



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The WCET Problem

Why is this important? Where is the WCET used?

The WCET is central to the design of Embedded Systems: Needed for <u>Correctness</u> (does the task finish in time?) and <u>Performance</u> (find optimal schedule for tasks)

Can the WCET always be found?

In general, no, because the problem is undecidable.

• Is knowing WCET enough?

In general, no, because anomalies can occur when tasks end earlier than expected.

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Typical WCET Problem

Task executes within an infinite loop

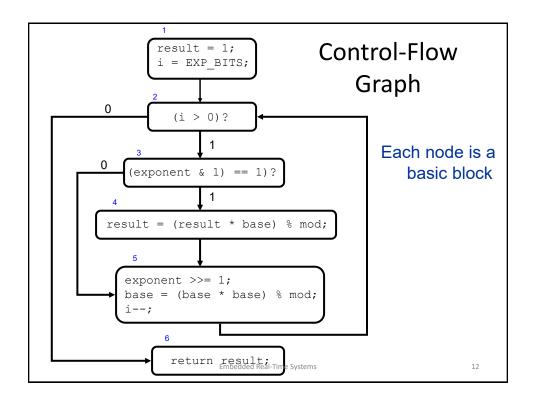
```
while(1) {
    read_sensors();
    compute();
    write_to_actuators();
}

This code typically has
    loops with finite bounds
    no recursion
Additional assumptions
    runs uninterrupted
    single-threaded
```

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Example Program: Modular Exponentiation #define EXP_BITS 32

```
\int (b^2)^{e/2} = (b^{e/2})^2,
                                                                           e is even,
                                           (b^2)^{(e-1)/2} \cdot b = (b^{(e-1)/2})^2 \cdot b, e is odd.
   typedef unsigned int UI;
   UI modexp(UI base, UI exponent, UI mod) {
      int i;
      UI result = 1;
      i = EXP_BITS;
9
10
      while (i > 0) {
        if ((exponent & 1) == 1) {
11
           result = (result * base) % mod;
13
        exponent >>= 1;
14
        base = (base * base) % mod;
16
17
18
      return result;
19
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```



Components of Execution Time Analysis (traditional approaches)

- Program path (Control flow) analysis
 - Want to find longest path through the program
 - Find loop bounds
 - Identify feasible paths through the program
 - Identify dependencies amongst different code fragments
- Processor behavior analysis
 - For small code fragments (basic blocks), generate bounds on run-times on the platform
 - Model details of architecture, including cache behavior, pipeline stalls, branch prediction, etc.
- Outputs of both analyses feed into each other

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Program Path Analysis: Path Explosion

```
/* MAXSIZE = 100 */
for (Outer = 0; Outer < MAXSIZE; Outer++) {</pre>
   for (Inner = 0; Inner < MAXSIZE; Inner++) {</pre>
      if (Array[Outer][Inner] >= 0) {
         Ptotal += Array[Outer][Inner];
         Pcnt++;
      } else {
         Ntotal += Array[Outer][Inner];
         Ncnt++;
      }
   Postotal = Ptotal;
                                  How many paths?
   Poscnt = Pcnt;
   Negtotal = Ntotal;
   Negcnt = Ncnt;
}
```

Example cnt.c from WCET benchmarks, Mälardalen Univ.

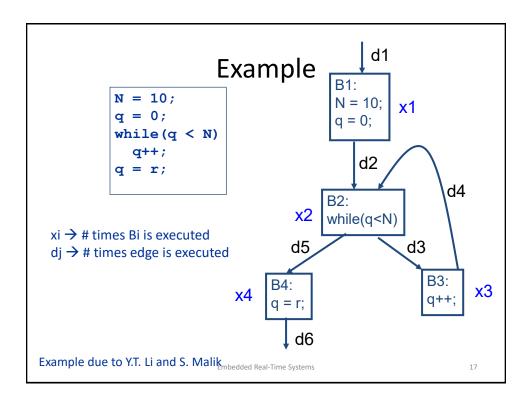
Program Path Analysis: Determining Loop Bounds

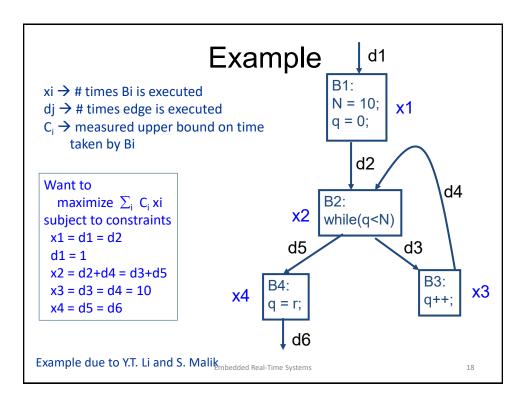
```
#define EXP BITS 32
  typedef unsigned int UI;
  UI modexp(UI base, UI exponent, UI mod) {
     int i;
     UI result = 1;
                                   How many times around the while
     i = EXP_BITS;
     while (i > 0) {
       if ((exponent & 1) == 1) {
12
         result = (result * base) % mod;
13
14
      exponent >>= 1;
15
      base = (base * base) % mod;
       i--;
17
     return result;
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```

Common Current Approach (high-level)

- 1. Manually construct processor behavior model
- Use model to find "worst-case" starting processor states for each basic block → measure execution times of the blocks from these states
- 3. Use these times as upper bounds on the time of each basic block
- Formulate an integer linear program to find the maximum sum of these bounds along any program path

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Integer Linear Programming

xi → # times Bi is executed

dj → # times edge is executed

C_i → measured upper bound on time taken by Bi

```
Want to

maximize \sum_i C_i xi

subject to constraints

x1 = d1 = d2

d1 = 1

x2 = d2+d4 = d3+d5

x3 = d3 = d4 = 10

x4 = d5 = d6
```

The problem to solve is:

Find integer values xi that maximize the sum (total execution time) subject to the (linear) constraint equations.

In general, this is an **Integer Linear Programming** (ILP) problem, which is known to be NP-hard, but for which there is good software.

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Program Path Analysis: Dependencies

```
void altitude_pid_run(void) {
  float err = estimator_z - desired_altitude;
  desired_climb = pre_climb + altitude_pgain * err;
  if (desired_climb < -CLIMB_MAX)
      desired_climb = -CLIMB_MAX;
  if (desired_climb > CLIMB_MAX)
      desired_climb = CLIMB_MAX;
}

Only one of these statements is executed
  (CLIMB_MAX = 1.0)
```

How many *feasible* paths?

Example from "PapaBench" UAV autopilot code, IRIT, France

Program Path Analysis: Dependencies

```
void altitude_pid_run(void) {
  float err = estimator_z - desired_altitude;
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}

Only one of these statements is executed
  (CLIMB_MAX = 1.0)
```

This adds an additional constraint of the form: $xi + xj \le 1$

Example from "PapaBench" UAV autopilot code, IRIT, France

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But the problem gets even harder... Timing Analysis and Compositionality

Consider a task T with two parts A and B composed in sequence: T = A; B

```
Is WCET(T) = WCET(A) + WCET(B) ?

NOT ALWAYS!

WCETs cannot simply be composed ☺

→ Due to dependencies "through environment"
```

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Processor Behavior Analysis: Cache Effects

```
float dot_product(float *x, float *y, int n) {
float result = 0.0;
int i;
for(i=0; i < n; i++) {
    result += x[i] * y[i];
}
return result;
}</pre>
```

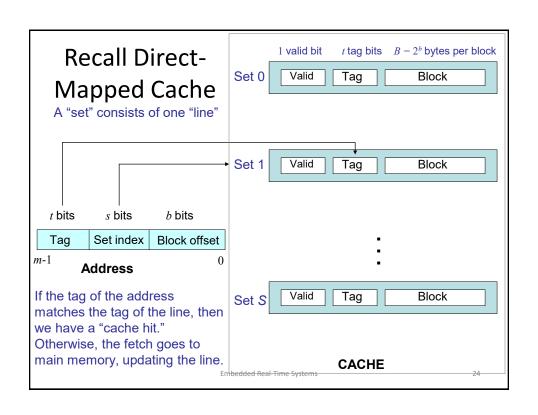
Suppose:

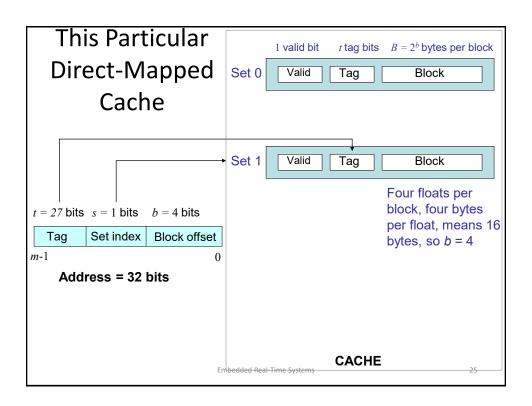
32-bit processor

What happens when **n=2**?

- 2. Direct-mapped cache holds two sets
 - 4 floats per set
 - x and y stored contiguously starting at address 0x0

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Processor Behavior Analysis: Cache Effects

```
float dot_product(float *x, float *y, int n) {
  float result = 0.0;
  int i;
  for(i=0; i < n; i++) {
    result += x[i] * y[i];
  }
  return result;
  }
}</pre>
```

What happens when **n=2**?

Suppose:

- 1. 32-bit processor
- 2. Direct-mapped cache holds two sets
 - O 4 floats per set
 - x and y stored contiguously starting at address 0x0

x[0] will miss, pulling x[0], x[1], y[0] and y[0] into the set 0. All but one access will be a cache hit.

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Processor Behavior Analysis: Cache Effects

```
float dot_product(float *x, float *y, int n) {
  float result = 0.0;
  int i;
  for(i=0; i < n; i++) {
    result += x[i] * y[i];
  }
  return result;
  }
}</pre>
```

Suppose:

- 1. 32-bit processor
- 2. Direct-mapped cache holds two sets
 - O 4 floats per set
 - x and y stored contiguously starting at address 0x0

What happens when **n=8**?

x[0] will miss, pulling x[0-3] into the set 0. Then y[0] will miss, pulling y[0-3] into the same set, evicting x[0-3]. Every access will be a miss!

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Timing Anomalies

I-Cache Hit

A pre-fetch B (I\$ miss due to pre-fetch)

I-Cache Miss

A (miss in I\$)

B

Branch evaluated

B (I\$ miss due to pre-fetch)



<u>Scenario 1:</u> Block A hits in I-cache, triggers branch speculation, and prefetch of instructions, then predicted branch is wrong, so Block B must execute, but it's been evicted from I-cache, execution of B delayed.

<u>Scenario 2:</u> Block A misses in I-cache, no branch prediction, then B hits in I-cache, B completes.

[from R.Wilhelm et al., ACM Trans. Embed. Comput. Sys, 2007.]

How to Measure Run-Time

Several techniques, with varying accuracy

- Instrument code to sample CPU cycle counter
 - relatively easy to do, read processor documentation for assembly instruction
- Use cycle-accurate simulator for processor
 - useful when hardware is not available/ready
- Use Logic Analyzer
 - non-intrusive measurement, more accurate
- ...

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Measurement Pitfalls

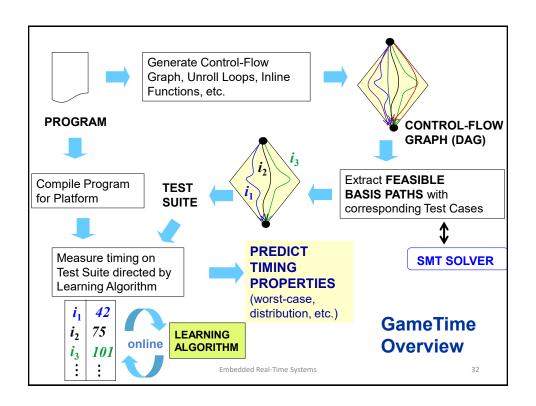
- Instrumentation incurs small overhead
 - measure long enough code sequence to compensate
- Multi-tasking effects: counter keeps going even when the task of interest is inactive
 - take multiple measurements and pick "k best" (cluster)
- Multicores/hyperthreading
 - Need to ensure that task is 'locked' to a single core
- Power management effects
 - CPU speed might change, timer could get reset during hibernation

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Some WCET Estimation Tools

- Commercial Tools: aiT, RapiTime, ...
- University/Research Tools: GameTime, Chronos, ...
 - GameTime: combines machine learning with automated theorem proving technology
 - Uses Programs as Graphs and integer linear programming ideas, but almost everything else different from other tools!

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Open Problems

- Architectures are getting much more complex.
 - Can we create processor models without the agonizing pain?
 [Yes, employ machine learning from systematic measurements
 → GameTime project]
 - Can we change the architecture to make timing analysis easier?
 [Yes, see PRET machine project]
- Analysis methods are "Brittle" small changes to code and/or architecture can require completely re-doing the WCET computation
 - GameTime project addresses this:
 - Use robust techniques that learn about processor/platform behavior
 - · Need to deal with concurrency, e.g., interrupts
- Need more reliable ways to measure execution time

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PRET Machines – Giving Software the Capabilities their Hardware Already Has.

- PREcision-Timed processors = PRET
- Predictable, REpeatable Timing = PRET

• Performance with REpeatable Timing = PRET http://chess.eecs.berkeley.edu/pret

```
// Perform the convolution.
for (int i=0; i<10; i++) {
   x[i] = a[i]*b[j-i];
   // Notify listeners.
   notify(x[i]);
}</pre>
```

Computing

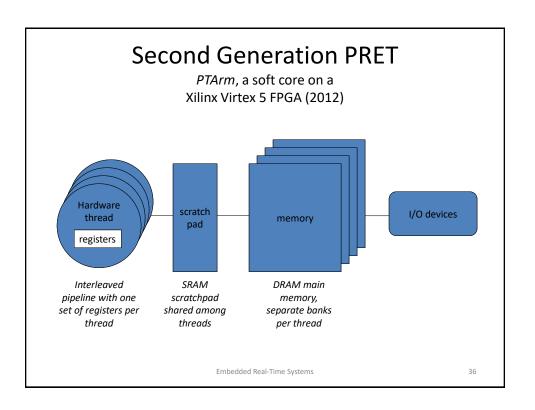
= PRET

With time
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Major Challenges and existence proofs that they can be met

- Pipelines
 - fine-grain multithreading
- Memory hierarchy
 - memory controllers with controllable latency
- I/O
 - threaded interrupts, with bounded effects on timing

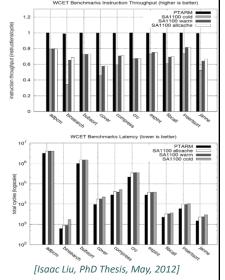
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Performance Cost?

No!

- The PRET project has shown that you do not need to sacrifice performance to get control over timing.
- But in PtARM, you need enough concurrency to not lose performance.

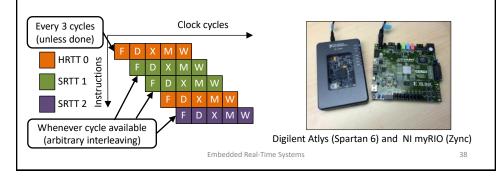


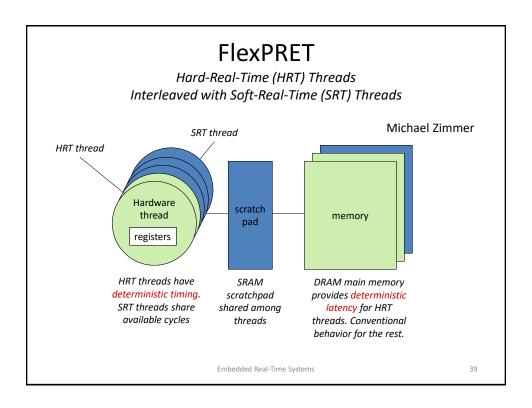
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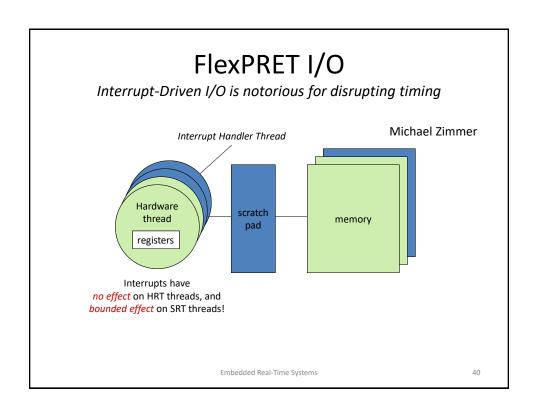
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Third-Generation PRET: Open-Source FlexPRET (Zimmer 2014/15)

- 32-bit, 5-stage thread interleaved pipeline, RISC-V ISA
 - Hard real-time HW threads: scheduled at constant rate for isolation and repeatability.
 - Soft real-time HW threads: share all available cycles for efficiency.
- Deployed on Xilinx FPGA (area comparable to Microblaze)







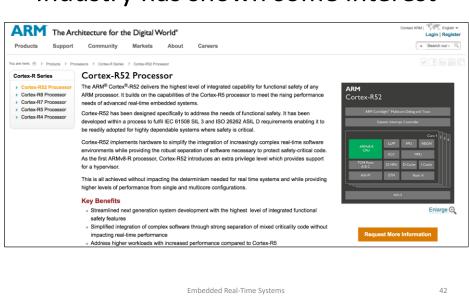
FlexPRET Shows

- Not only is there no performance cost for appropriate workloads, but there is also no performance cost for inappropriate workloads!
- Pipelining, memory hierarchy, and interruptdriven I/O can all be done without losing timing determinacy!

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Industry has shown some interest



Optional Reading Material

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Cycle Counters

- Most modern systems have built in registers that are incremented every clock cycle
- Special assembly code instruction to access
- On Intel 32-bit x86 machines since Pentium:
 - 64 bit counter
 - RDTSC instruction (ReaD Time Stamp Counter) sets %edx register to high order 32-bits, %eax register to low order 32-bits
- Wrap-around time for 2 GHz machine
 - Low order 32-bits every 2.1 seconds
 - High order 64 bits every 293 years

[slide due to R. E. Bryant and D. R. O Hallaron] -Time Systems

Measuring with Cycle Counter

- Idea
 - Get current value of cycle counter
 - store as pair of unsigned's cyc_hi and cyc_lo
 - Compute something
 - Get new value of cycle counter
 - Perform double precision subtraction to get elapsed cycles

```
/* Keep track of most recent reading of cycle counter */
static unsigned cyc_hi = 0;
static unsigned cyc_lo = 0;

void start_counter()
{
   /* Get current value of cycle counter */
   access_counter(&cyc_hi, &cyc_lo);
}
```

[slide due to R. E. Bryant and D. R. O Hallaron]

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Accessing the Cycle Counter

- GCC allows inline assembly code with mechanism for matching registers with program variables
- Code only works on x86 machine compiling with GCC

Emit assembly with rdtsc and two movl instructions

[slide due to R. E. Bryant and D. R. O'Hailaron] I-Time Systems

Completing Measurement

- Get new value of cycle counter
- Perform double precision subtraction to get elapsed cycles
- Express as double to avoid overflow problems

```
double get_counter()
{
  unsigned ncyc_hi, ncyc_lo
  unsigned hi, lo, borrow;
  /* Get cycle counter */
  access_counter(&ncyc_hi, &ncyc_lo);
  /* Do double precision subtraction */
  lo = ncyc_lo - cyc_lo;
  borrow = lo > ncyc_lo;
  hi = ncyc_hi - cyc_hi - borrow;
  return (double) hi * (1 << 30) * 4 + lo;
}</pre>
```

[slide due to R. E. Bryant and D. R. O'Hallaron]

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Timing With Cycle Counter

- Time Function P
 - First attempt: Simply count cycles for one execution of P

```
double tcycles;
start_counter();
P();
tcycles = get_counter();
```

– What can go wrong here?

[slide due to R. E. Bryant and D. R. O'Hallaron]

Dealing with Overhead & Cache Effects

- Always execute function once to "warm up" cache
- Keep doubling number of times execute P() until reach some threshold
 Used CMIN = 50000

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Timing With Cycle Counter

- Determine Clock Rate of Processor
 - Count number of cycles required for some fixed number of seconds

```
double MHZ;
int sleep_time = 10;
start_counter();
sleep(sleep_time);
MHZ = get_counter()/(sleep_time * 1e6);
```

- Time Function P
 - First attempt: Simply count cycles for one execution of P

```
double tsecs;
start_counter();
P();
tsecs = get_counter() / (MHZ * 1e6);
```

[slide due to R. E. Bryant and D. R. O'Hallaron] I-Time Systems

Measurement Pitfalls

- Instrumentation incurs small overhead
 - measure long enough code sequence to compensate
- Cache effects can skew measurements
 - "warm up" the cache before making measurement
- Multi-tasking effects: counter keeps going even when the task of interest is inactive
 - take multiple measurements and pick "k best" (cluster)
- Multicores/hyperthreading
 - Need to ensure that task is 'locked' to a single core
- Power management effects
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