



Graphic Era
Deemed to be University

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Submitted to:

Mr. Piyush Aggarwal

Assistant Professor
GEU D.Dun

Submitted by:

SHOURYA KAPOOR

Roll.No.:1918914

Class Roll.No./Section: 84/IT

DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

GRAPHIC ERA UNIVERSITY, DEHRADUN
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SHOURYA

Uni. Roll No.- 1918914

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GEU Dehradun



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Program 1

Objective: Program to Implement Bisection Method

Algorithm:

1. Start
2. Read x_1 , x_2 , e
*Here x_1 and x_2 are initial guesses
 e is the absolute error i.e. the desired degree of accuracy*
3. Compute: $f_1 = f(x_1)$ and $f_2 = f(x_2)$
4. If $(f_1 * f_2) > 0$, then display initial guesses are wrong and goto (11).
Otherwise continue.
5. $x = (x_1 + x_2)/2$
6. If $([(x_1 - x_2)/x] < e)$, then display x and goto (11).
* Here $[]$ refers to the modulus sign. *
7. Else, $f = f(x)$
8. If $((f * f_1) > 0)$, then $x_1 = x$ and $f_1 = f$.
9. Else, $x_2 = x$ and $f_2 = f$.
10. Goto (5).
Now the loop continues with new values.
11. Stop

Source Code

```
#include<stdio.h>
#include<math.h>
float fun (float x)
{
    return (x*x*x - 4*x - 9);
    cos(x) - x * exp(x)
    x=cos(x)
}
void bisection (float *x, float a, float b, int *itr)
/* this function performs and prints the result of one iteration */
{
    *x=(a+b)/2;
    ++(*itr);
    printf("Iteration no. %3d X = %7.5f\n", *itr, *x);
}
void main ()
{
    int itr = 0, maxmitr;
    float x, a, b, allerr, x1;
    printf("\nEnter the values of a, b, allowed error and maximum
iterations:\n");
    scanf("%f %f %f %d", &a, &b, &allerr, &maxmitr);
    bisection (&x, a, b, &itr);
    do
    {
        if (fun(a)*fun(x) < 0)
            b=x;
        else
            a=x;
        bisection (&x1, a, b, &itr);
        if (fabs(x1-x) < allerr)
```

```
{  
    printf("After %d iterations, root = %6.4f\n", itr, x1);  
    return 0;  
}  
x=x1;  
}  
while (itr < maxmitr);  
printf("The solution does not converge or iterations are not  
sufficient");  
return 1;  
}
```

Output

"C:\Users\LENEVO\Desktop\CBNST\Bisection algebric.exe"

Enter the values of a, b, allowed error and maximum iterations:

0

1

0.001

14

Iteration no. 1 X = 0.50000

Iteration no. 2 X = 0.75000

Iteration no. 3 X = 0.87500

Iteration no. 4 X = 0.93750

Iteration no. 5 X = 0.96875

Iteration no. 6 X = 0.98438

Iteration no. 7 X = 0.99219

Iteration no. 8 X = 0.99609

Iteration no. 9 X = 0.99805

Iteration no. 10 X = 0.99902

After 10 iterations, root = 0.9990

Process returned 35 (0x23) execution time : 12.174 s

"C:\Users\LENEVO\Desktop\CBNST\Bisection algebric.exe"

Enter the values of a, b, allowed error and maximum iterations:

1

2

0.01

10

Iteration no. 1 X = 1.50000

Iteration no. 2 X = 1.75000

Iteration no. 3 X = 1.62500

Iteration no. 4 X = 1.56250

Iteration no. 5 X = 1.59375

Iteration no. 6 X = 1.57813

Iteration no. 7 X = 1.57031

After 7 iterations, root = 1.5703

"C:\Users\LENEVO\Desktop\CBNST\Bisection algebric.exe"

Enter the values of a, b, allowed error and maximum iterations:

0

1

0.001

10

Iteration no. 1 X = 0.50000

Iteration no. 2 X = 0.75000

Iteration no. 3 X = 0.62500

Iteration no. 4 X = 0.56250

Iteration no. 5 X = 0.53125

Iteration no. 6 X = 0.51563

Iteration no. 7 X = 0.52344

Iteration no. 8 X = 0.51953

Iteration no. 9 X = 0.51758

Iteration no. 10 X = 0.51855

After 10 iterations, root = 0.5186

Process returned 35 (0x23) execution time : 11.336 s

Program 2

Objective: Program to Implement Regular Falsi Method

Algorithm:

1. Start
2. Read values of x_0 , x_1 and e
*Here x_0 and x_1 are the two initial guesses
 e is the degree of accuracy or the absolute error i.e. the stopping criteria*
3. Compute function values $f(x_0)$ and $f(x_1)$
4. Check whether the product of $f(x_0)$ and $f(x_1)$ is negative or not.
If it is positive take another initial guesses.
If it is negative then goto step 5.
5. Determine:
$$x = \frac{x_0 \cdot f(x_1) - x_1 \cdot f(x_0)}{f(x_1) - f(x_0)}$$
6. Check whether the product of $f(x_1)$ and $f(x)$ is negative or not.
If it is negative, then assign $x_0 = x$;
If it is positive, assign $x_1 = x$;
7. Check whether the value of $f(x)$ is greater than 0.00001 or not.
If yes, goto step 5.
If no, goto step 8.
Here the value 0.00001 is the desired degree of accuracy, and hence the stopping criteria.
8. Display the root as x .
9. Stop

Source Code


```
#include<stdio.h>
#include<math.h>
float f(float x)
{
    return cos(x) - x*exp(x);
        (x*x*x - 4*x - 9)
        x=cos(x)
}

void regula (float *x, float x0, float x1, float fx0, float fx1, int *itr)
{
    *x = x0 - ((x1 - x0) / (fx1 - fx0))*fx0;
    ++(*itr);
    printf("Iteration no. %3d X = %7.5f \n", *itr, *x);
}

void main ()
{
    int itr = 0, maxmitr;
    float x0,x1,x2,x3,allerr;
    printf("\nEnter the values of x0, x1, allowed error and maximum iterations:
\n");
    scanf("%f %f %f %d", &x0, &x1, &allerr, &maxmitr);
    regula (&x2, x0, x1, f(x0), f(x1), &itr);
    do
    {
        if (f(x0)*f(x2) < 0)
            x1=x2;
        else
            x0=x2;
        regula (&x3, x0, x1, f(x0), f(x1), &itr);
        if (fabs(x3-x2) < allerr)
        {
            printf("After %d iterations, root = %6.4f\n", itr, x3);
            return 0;
        }
        x2=x3;
    }
    while (itr<maxmitr);
    printf("Solution does not converge or iterations not sufficient:\n");
    return 1;
```

}

Output

 C:\Users\LENEVO\Desktop\CBNST\regular.exe

Enter the values of x0, x1, allowed error and maximum iterations:

0

1

0.001

9

Iteration no. 1 X = 0.31467

Iteration no. 2 X = 0.44673

Iteration no. 3 X = 0.49402

Iteration no. 4 X = 0.50995


Iteration no. 5 X = 0.51520

Iteration no. 6 X = 0.51692

Iteration no. 7 X = 0.51748

After 7 iterations, root = 0.5175

Process returned 34 (0x22) execution time : 9.333 s

 C:\Users\LENEVO\Desktop\CBNST\regular.exe

Enter the values of x0, x1, allowed error and maximum iterations:

1

2

0.01

15

Iteration no. 1 X = 5.00000

Iteration no. 2 X = 1.44444

Iteration no. 3 X = 1.83259

Iteration no. 4 X = 2.13615

Iteration no. 5 X = 2.35128

Iteration no. 6 X = 2.49248

Iteration no. 7 X = 2.58033

Iteration no. 8 X = 2.63312

Iteration no. 9 X = 2.66417

Iteration no. 10 X = 2.68221

Iteration no. 11 X = 2.69260

Iteration no. 12 X = 2.69856

After 12 iterations, root = 2.6986

Process returned 35 (0x23) execution time : 4.822 s

Press any key to continue.

```
C:\Users\LENEVO\Desktop\CBNST\regular.exe

Enter the values of x0, x1, allowed error and maximum iterations:
1
2
0.001
15
Iteration no.   1 X = 1.56490
Iteration no.   2 X = 1.57098
Iteration no.   3 X = 1.57080
After 3 iterations, root = 1.5708
```

Program 3

Objective: Program to Implement Secant Method

Algorithm:

1. Start
2. Get values of x_0 , x_1 and e
*Here x_0 and x_1 are the two initial guesses
 e is the stopping criteria, absolute error or the desired degree of accuracy*
3. Compute $f(x_0)$ and $f(x_1)$
4. Compute $x_2 = [x_0 * f(x_1) - x_1 * f(x_0)] / [f(x_1) - f(x_0)]$
5. Test for accuracy of x_2
If $[(x_2 - x_1)/x_2] > e$, *Here $[\]$ is used as modulus sign*
then assign $x_0 = x_1$ and $x_1 = x_2$
goto step 4
Else,
goto step 6
6. Display the required root as x_2 .
7. Stop

Source Code


```
#include<stdio.h>
float f(float x)
{
    return cos(x) - x*exp(x);
        (x*x*x - 4*x - 9)
        x=cos(x)
}
float main()
{
    float a,b,c,d,e;
    int count=1,n;
    printf("\n\nEnter the values of a and b:\n"); //(a,b) must contain the solution.
    scanf("%f%f",&a,&b);
    printf("Enter the values of allowed error and maximun number of iterations:
\n");
    scanf("%f %d",&e,&n);
    do
    {
        if(f(a)==f(b))
        {
            printf("\nSolution cannot be found as the values of a and b are same.
\n");
            return;
        }
        c=(a*f(b)-b*f(a))/(f(b)-f(a));
        a=b;
        b=c;
        printf("Iteration No-%d    x=%f\n",count,c);
        count++;
        if(count==n)
        {
```

```

        break;
    }
} while(fabs(f(c))>e);
printf("\n The required solution is %f\n",c);
}

```

Output

 C:\Users\LENEVO\Desktop\CBNST\secant.exe


```

Enter the values of a and b:
1
2
Enter the values of allowed error and maximun number of iterations:
0.01
10
Iteration No-1      x=0.832673
Iteration No-2      x=0.728779
Iteration No-3      x=0.562401
Iteration No-4      x=0.524782
Iteration No-5      x=0.518014

The required solution is 0.518014

Process returned 36 (0x24)   execution time : 10.369 s

```

 C:\Users\LENEVO\Desktop\CBNST\secant.exe

```

Enter the values of a and b:
1
2
Enter the values of allowed error and maximun number of iterations:
0.001
5
Iteration No-1      x=5.000000
Iteration No-2      x=2.257143
Iteration No-3      x=2.431810
Iteration No-4      x=2.779584

The required solution is 2.779584

Process returned 36 (0x24)   execution time : 7.428 s

```

C:\Users\LENEVO\Desktop\CBNST\secant.exe

```
Enter the values of a and b:  
0  
1  
Enter the values of allowed error and maximun number of iterations:  
0.0001  
4  
Iteration No-1      x=2.175343  
Iteration No-2      x=1.572784  
Iteration No-3      x=1.570669  
  
The required solution is 1.570669  
  
Process returned 36 (0x24)   execution time : 11.116 s
```

Program 4

Objective: Program to Implement Iteration Method

Algorithm:

1. Start
2. Read values of x_0 and e .
*Here x_0 is the initial approximation
 e is the absolute error or the desired degree of accuracy, also the stopping criteria*
3. Calculate $x_1 = g(x_0)$
4. If $[x_1 - x_0] \leq e$, goto step 6.
Here $[]$ refers to the modulus sign
5. Else, assign $x_0 = x_1$ and goto step 3.
6. Display x_1 as the root.
7. Stop

Source Code

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
#define f(x) cos(x)-3*x+1
#define g(x) (1+cos(x))/3
           x*x*x - x -1

int main()
{
    int step=1, N;
    float x0, x1, e;
    printf("Enter initial guess: ");
    scanf("%f", &x0);
    printf("Enter tolerable error: ");
    scanf("%f", &e);
    printf("Enter maximum iteration: ");
    scanf("%d", &N);
    printf("\nStep\tx0\t\tf(x0)\t\tx1\t\tf(x1)\n");
    do
    {
        x1 = g(x0);
        printf("%d\t%f\t%f\t%f\t%f\n",step, x0, f(x0), x1, f(x1));

        step = step + 1;

        if(step>N)
        {
            printf("Not Convergent.");
            exit(0);
        }

        x0 = x1;
    }while( fabs(f(x1)) > e);

    printf("\nRoot is %f", x1);
```

```

    getch();
    return(0);
}

```

Output

```

C:\Users\LENEVO\Desktop\CBNST\Iteration.exe
Enter initial guess: 1
Enter tolerable error: 0.01
Enter maximum iteration: 5

Step    x0          f(x0)         x1           f(x1)
1       1.000000   -1.459698     0.513434     0.330761
2       0.513434   0.330761     0.623688    -0.059333
3       0.623688   -0.059333    0.603910     0.011391
4       0.603910   0.011391     0.607707    -0.002162

Root is 0.607707_

```

```

C:\Users\LENEVO\Desktop\CBNST\Iteration.exe
Enter initial guess: 1
Enter tolerable error: 0.01
Enter maximum iteration: 6

Step    x0          f(x0)         x1           f(x1)
1       1.000000   -1.000000     1.000000    -1.000000
2       1.000000   -1.000000     1.000000    -1.000000
3       1.000000   -1.000000     1.000000    -1.000000
4       1.000000   -1.000000     1.000000    -1.000000
5       1.000000   -1.000000     1.000000    -1.000000
6       1.000000   -1.000000     1.000000    -1.000000

Not Convergent.
Process returned 0 (0x0)   execution time : 9.320 s

```


Program 5

Objective: Program to finding errors.


Algorithm:

1. Start
2. Take input say True value and Approximate value
3. Calculate absolute error using formula-
 - a. $\text{Absolute error} = \text{True value} - \text{Approximate value}$
4. Calculate relative error using formula-
 - a. $\text{relative error} = \text{Approximate value} / \text{True value}$
5. Calculate percentage error using formula
 - a. $\text{Percentage error} = \text{relative error} * 100$
6. Stop

Source Code

```
#include<stdio.h>
#include<math.h>
void main()
{
    float abserror, relerror, percerror, trueval, approxval;
    printf("Enter True value");
    scanf("%f",&trueval);
    printf("Enter approx value");
    scanf("%f",&approxval);
    abserror=fabs(trueval-approxval);
    relerror=abserror/trueval;
    percerror=relerror*100;
    printf("\nabsolute error = %f\n",abserror);
    printf("\nrelative error = %f\n",relerror);
    printf("\npercentage error = %f\n",percerror);
}
```

Output



A screenshot of a Windows command prompt window. The title bar shows the file path "C:\Users\LENEVO\Desktop\CBNST\error.exe". The command prompt displays the following text: "Enter True value", "3.14159", "Enter approx value", "3.14", "absolute error = 0.001590", "relative error = 0.000506", "percentage error = 0.050612", "Process returned 29 (0x1D) execution time : 11.307 s", and "Press any key to continue.".

```
C:\Users\LENEVO\Desktop\CBNST\error.exe
Enter True value
3.14159
Enter approx value
3.14

absolute error = 0.001590

relative error = 0.000506

percentage error = 0.050612

Process returned 29 (0x1D)   execution time : 11.307 s
Press any key to continue.
```

Program 6

Objective: Program to implement Newton Raphson Method.

Algorithm:


1. Start
2. Read x , e , n , d
 x is the initial guess
 e is the absolute error i.e the desired degree of accuracy
 n is for operating loop
 d is for checking slope*
3. Do for $i = 1$ to n in step of 2
4. $f = f(x)$
5. $f1 = f'(x)$
6. If ($[f1] < d$), then display too small slope and goto 11.
 $[]$ is used as modulus sign*
7. $x1 = x - f/f1$
8. If ($[(x1 - x)/x1] < e$), the display the root as $x1$ and goto 11.
 $[]$ is used as modulus sign*
9. $x = x1$ and end loop
10. Display method does not converge due to oscillation.
11. Stop

Source Code

```
#include<stdio.h>
#include<math.h>
float f(float x)
{
    return x*log10(x) - 1.2;
        x * x * x - x * x + 2;
        3*x - cos(x) -1 ;
}
float df (float x)
{
    return log10(x) + 0.43429;
        3 * x * x - 2 * x;
        3 + sin(x);
}
void main()
{
    int itr, maxmitr;
    float h, x0, x1, allerr;
    printf("\nEnter x0, allowed error and maximum iterations\n");
    scanf("%f %f %d", &x0, &allerr, &maxmitr);
    for (itr=1; itr<=maxmitr; itr++)
    {
        h=f(x0)/df(x0);
        x1=x0-h;
        printf(" At Iteration no. %3d, x = %9.6f\n", itr, x1);
        if (fabs(h) < allerr)
        {
```

```
        printf("After %3d iterations, root = %8.6f\n", itr, x1);
        return 0;
    }
    x0=x1;
}
    printf(" The required solution does not converge or iterations
are insufficient\n");
    return 1;
}
```

Output

 "C:\Users\LENEVO\Desktop\CBNST\newton raphson.exe"

```
Enter x0, allowed error and maximum iterations
2
0.001
5
At Iteration no. 1, x = 2.813170
At Iteration no. 2, x = 2.741109
At Iteration no. 3, x = 2.740646
After 3 iterations, root = 2.740646

Process returned 38 (0x26)   execution time : 8.218 s
```

 "C:\Users\LENEVO\Desktop\CBNST\newton raphson.exe"

```
Enter x0, allowed error and maximum iterations
1
0.01
6
At Iteration no. 1, x = -1.000000
At Iteration no. 2, x = -1.000000
After 2 iterations, root = -1.000000

Process returned 39 (0x27)   execution time : 10.037 s
```

 "C:\Users\LENEVO\Desktop\CBNST\newton raphson.exe"

```
Enter x0, allowed error and maximum iterations
1
0.0001
5
At Iteration no. 1, x = 0.620016
At Iteration no. 2, x = 0.607121
At Iteration no. 3, x = 0.607102
After 3 iterations, root = 0.607102

Process returned 38 (0x26)   execution time : 9.051 s
```

Program 7

Objective: Program to implement Gauss Elimination Method.

Algorithm:

1. Start
2. Declare the variables and read the order of the matrix n.
3. Take the coefficients of the linear equation as:
 Do for k=1 to n
 Do for j=1 to n+1
 Read a[k][j]
 End for j
 End for k
4. Do for k=1 to n-1
 Do for i=k+1 to n
 Do for j=k+1 to n+1
 $a[i][j] = a[i][j] - a[i][k] / a[k][k] * a[k][j]$
 End for j
 End for i
 End for k
5. Compute $x[n] = a[n][n+1] / a[n][n]$
6. Do for k=n-1 to 1
 sum = 0
 Do for j=k+1 to n
 sum = sum + a[k][j] * x[j]
 End for j
 $x[k] = 1 / a[k][k] * (a[k][n+1] - \text{sum})$
 End for k
7. Display the result x[k]
8. Stop

Source Code

```
#include<stdio.h>

int main()
{
    int i,j,k,n;
    float A[20][20],c,x[10],sum=0.0;
    printf("\nEnter the order of matrix: ");
    scanf("%d",&n);
    printf("\nEnter the elements of augmented matrix row-wise:
\n\n");
    for(i=1; i<=n; i++)
    {
        for(j=1; j<=(n+1); j++)
        {
            printf("A[%d][%d] : ", i,j);
            scanf("%f",&A[i][j]);
        }
    }
    for(j=1; j<=n; j++) /* loop for the generation of upper triangular
matrix*/
    {
        for(i=1; i<=n; i++)
        {
            if(i>j)
            {
                c=A[i][j]/A[j][j];
                for(k=1; k<=n+1; k++)
                {
                    A[i][k]=A[i][k]-c*A[j][k];
                }
            }
        }
    }
}
```

```

    }
}
}
x[n]=A[n][n+1]/A[n][n];
for(i=n-1; i>=1; i--)
{
    sum=0;
    for(j=i+1; j<=n; j++)
    {
        sum=sum+A[i][j]*x[j];
    }
    x[i]=(A[i][n+1]-sum)/A[i][i];
}
printf("\nThe solution is: \n");
for(i=1; i<=n; i++)
{
    printf("\nx%d=%f\t",i,x[i]);
}
return(0);
}

```

Output

"C:\Users\LENEVO\Desktop\CBNST\Gauss elimination.exe"

```
Enter the order of matrix: 3
Enter the elements of augmented matrix row-wise:
A[1][1] : 5
A[1][2] : 4
A[1][3] : 1
A[1][4] : 2
A[2][1] : 3
A[2][2] : -5
A[2][3] : -8
A[2][4] : -4
A[3][1] : 6
A[3][2] : -8
A[3][3] : -9
A[3][4] : 3

The solution is:
x1=1.335260
x2=-1.682080
x3=2.052022
Process returned 0 (0x0)   execution time : 36.080 s
Press any key to continue.
```

Program 8

Objective: Program to implement Gauss Jordan Method.

Algorithm:

1. Start
2. Read the order of the matrix 'n' and read the coefficients of the linear equations.
3. Do for k=1 to n
 Do for l=k+1 to n+1
 $a[k][l] = a[k][l] / a[k][k]$
 End for l
 Set $a[k][k] = 1$
 Do for i=1 to n
 if (i not equal to k) then,
 Do for j=k+1 to n+1
 $a[i][j] = a[i][j] - (a[k][j] * a[i][k])$
 End for j
 End for i
 End for k
4. Do for m=1 to n
 $x[m] = a[m][n+1]$
 Display $x[m]$
 End for m
5. Stop

Source Code

```
#include<stdio.h>
int main()
{
```

```

int i,j,k,n;
float A[20][20],c,x[10];
printf("\nEnter the size of matrix: ");
scanf("%d",&n);
printf("\nEnter the elements of augmented matrix row-wise:\n");
for(i=1; i<=n; i++)
{
    for(j=1; j<=(n+1); j++)
    {
        printf(" A[%d][%d]:", i,j);
        scanf("%f",&A[i][j]);
    }
}
for(j=1; j<=n; j++)
{
    for(i=1; i<=n; i++)
    {
        if(i!=j)
        {
            c=A[i][j]/A[j][j];
            for(k=1; k<=n+1; k++)
            {
                A[i][k]=A[i][k]-c*A[j][k];
            }
        }
    }
}
printf("\nThe solution is:\n");
for(i=1; i<=n; i++)
{
    x[i]=A[i][n+1]/A[i][i];
    printf("\n x%d=%f\n",i,x[i]);
}
return(0);
}

```

Output

```
C:\Users\LENEVO\Desktop\CBNST\Jordan.exe

Enter the size of matrix: 3

Enter the elements of augmented matrix row-wise:
A[1][1]:-10
A[1][2]:7
A[1][3]:9
A[1][4]:5
A[2][1]:-5
A[2][2]:-3
A[2][3]:-1
A[2][4]:5
A[3][1]:-4
A[3][2]:2
A[3][3]:3
A[3][4]:-7

The solution is:

x1=-37.999985
x2=101.999962
x3=-120.999977

Process returned 0 (0x0)   execution time : 38.528 s
Press any key to continue.
_
```

Program 9

Objective: Program to implement Gauss Jacobi Method.

Algorithm:

1. Start

2. Arrange the given system of linear equation in diagonally dominant form
3. Read tolerance error
4. Convert the first equation in terms of first variable, and second equation in term of second variable and so on
5. Set initial guess for x_0, y_0, z_0
6. Substitute value of x_0, y_0, z_0 , -----from step 5 in equation obtained on step 4 to calculate new values
7. X_1, y_1, z_1 -----
8. If $|x_0 - x_1| > e$ and $|y_0 - y_1| > e$ and so on, then goto step 9
9. Set $x_0 = x_1, y_0 = y_1, z_0 = z_1$, and so on goto step 6
10. Print value of x_1, y_1, z_1 and so on
11. stop

Source Code

```
#include<stdio.h>
#include<conio.h>
#include<math.h>

float fx(float y,float z)
{
    float x1; x1=4-2*y-3*z;
    return x1;
}

float fy(float x,float z)
{
    float y1;
    y1=(8-5*x-7*z)/6;
    return y1;
}

float fz(float x,float y)
{
    float z1;
    z1=(3-9*x-y)/2;
    return z1;
}

void main()
```



```

{
    int i,j,n;
    float a1,b1,c1;
    float a,b,c;
    float ar[3][4],x[3];
    printf("Enter the no. of Iteration : ");
    scanf("%d",&n);
    printf("Enter The initial value : ");
    scanf("%f %f %f",&a,&b,&c);
    for(i=0;i<n;i++)
    {
        for(j=0;j<n;j++)
        {
            a1=fx(b,c);
            b1=fy(a,c);
            c1=fz(a,b);
            a=a1;
            b=b1;
            c=c1;
        }
    }
    printf("a1 = %f\n a2 = %f\n a3 = %f",a1,b1,c1);

    getch();
}

```

Output

C:\Users\LENEVO\Desktop\CBNST\Jacobi.exe

Enter the no. of Iteration : 3

Enter The initial value : 1

2

3

a1 = -852427.875000

a2 = -405496.750000

a3 = -818762.500000

Program 10

Objective: Program to implement Gauss Seidel Method.

Algorithm:

1. Start
2. Declare the variables and read the order of the matrix n
3. Read the stopping criteria er
4. Read the coefficients aim as
 Do for i=1 to n
 Do for j=1 to n
 Read a[i][j]
 Repeat for j
 Repeat for i
5. Read the coefficients b[i] for i=1 to n
6. Initialize $x_0[i] = 0$ for i=1 to n
7. Set key=0
8. For i=1 to n
 Set sum = b[i]
 For j=1 to n
 If (j not equal to i)
 Set sum = sum - a[i][j] * $x_0[j]$
 Repeat j
 $x[i] = \text{sum} / a[i][i]$
 If absolute value of $((x[i] - x_0[i]) / x[i]) > er$, then
 Set key = 1
 Set $x_0[i] = x[i]$
 Repeat i

9. If key = 1, then
 Goto step 6
 Otherwise print results

Source Code

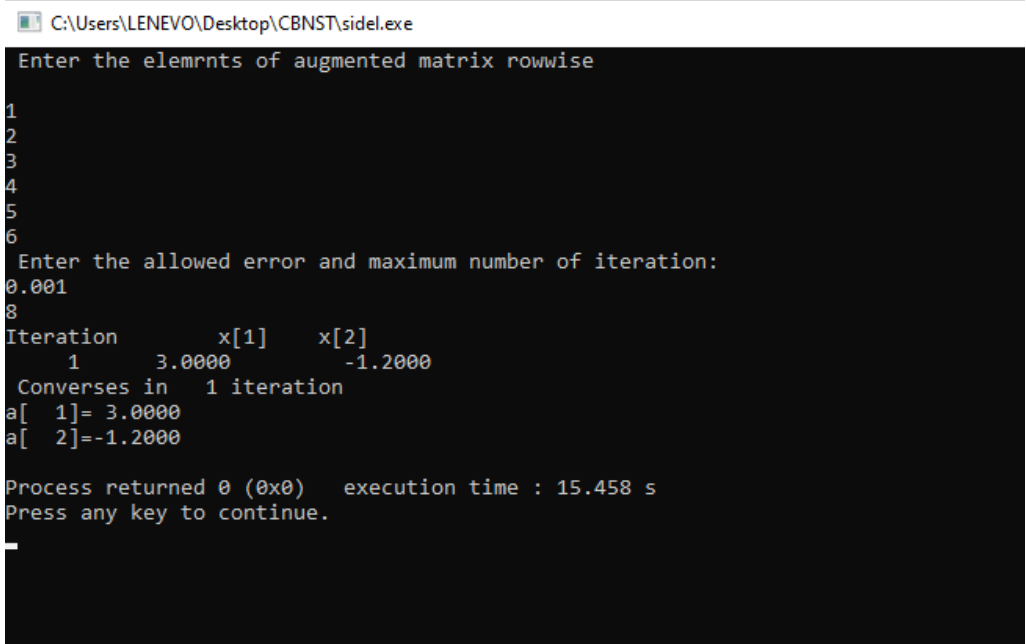
```
#include<stdio.h>
#include<math.h>
#define X 2
main()
{
    float x[X][X+1],a[X], ae, max,t,s,e;
    int i,j,r,mxit;
    for(i=0;i<X;i++) a[i]=0;
    puts(" Enter the elemrnts of augmented matrix rowwise\n");
    for(i=0;i<X;i++)
    {
        for(j=0;j<X+1;j++)
        {
            scanf("%f",&x[i][j]);
        }
    }
    printf(" Enter the allowed error and maximum number of iteration: ");
    scanf("%f%d",&ae,&mxit);
    printf("Iteration\tx[1]\tx[2]\n");
    for(r=1;r<=mxit;r++)
    {
        max=0;
        for(i=0;i<X;i++)
        {
            s=0;
            for(j=0;j<X;j++)
            if(j!=i) s+=x[i][j]*a[j];
            t=(x[i][X]-s)/x[i][i];
            e=fabs(a[i]-t);
            a[i]=t;
        }
        printf(" %5d\t",r);
        for(i=0;i<X;i++)
        printf(" %9.4f\t",a[i]);
        printf("\n");
        if(max<ae)
```

```

    {
        printf(" Converges in %3d iteration\n", r);
        for(i=0;i<X;i++)
            printf("a[%3d]=%7.4f\n", i+1,a[i]);
        return 0;
    }
}

```

Output



```

C:\Users\LENEVO\Desktop\CBNST\sidel.exe
Enter the elemrnts of augmented matrix rowwise
1
2
3
4
5
6
Enter the allowed error and maximum number of iteration:
0.001
8
Iteration      x[1]      x[2]
      1      3.0000      -1.2000
Converges in 1 iteration
a[ 1]= 3.0000
a[ 2]=-1.2000

Process returned 0 (0x0)   execution time : 15.458 s
Press any key to continue.

```

Program 11

Objective: Program to implement Newton Forward Interpolation Method.

Algorithm:

1. Start of the program
2. Input number of terms n
3. Input the array ax
4. Input the array ay
5. $h = ax[1] - ax[0]$
6. for $i=0; i < n-1; i++$
7. $diff[i][1] = ay[i+1] - ay[i]$
8. End Loop i
9. for $j=2; j \leq 4; j++$
10. for $i = 0; i < n - j; i++$
11. $diff[i][j] = diff[i+1][j-1] - diff[i][j-1]$
12. End Loop i
13. End Loop j
14. $i=0$
15. Repeat Step 16 until $ax[i] < x$
16. $i = i + 1$
17. $i = i - 1;$

$$18. p = (x - ax[i])/h$$

$$19. y1 = p * \text{diff}[i - 1][1]$$

$$20. y2 = p * (p + 1) * \text{diff}[i - 1][2] / 2$$

$$21. y3 = (p + 1) * p * (p - 1) * \text{diff}[i - 2][3] / 6$$

$$22. y4 = (p + 2) * (p + 1) * p * (p - 1) * \text{diff}[i - 3][4] / 24$$

$$23. y = ay[i] + y1 + y2 + y3 + y4$$

24. Print output x, y

25. End of program.

Source Code

```
# include <stdio.h>
# include <conio.h>
# include <math.h>
# include <process.h>
# include <string.h>
void main()
{
    int n;
    int i,j;
    float ax[10];
    float ay[10];
    float x;
    float y = 0;
    float h;
    float p;
    float diff[20][20];
    float y1,y2,y3,y4;
    clrscr();
    printf("\n Enter the number of terms - ");
    scanf("%d",&n);
    printf("Enter the value in the form of x - ");
    for (i=0;i<n;i++)
    {
        printf("Enter the value of x%d - ",i+1);
        scanf("%f",&ax[i]);
    }
    printf("\n Enter the value in the form of y - ");
    for (i=0;i<n;i++)
    {
        printf ("Enter the value of y%d - ", i+1);
        scanf ("%f",&ay [i]);
    }
    printf("\nEnter the value of x for");
    printf("\nwhich you want the value of y - ");
    scanf("%f",&x);
    h=ax[1]-ax[0];
    for(i=0;i<n-1;i++)
    {
        diff[i][1]=ay[i+1]-ay[i];
    }
}
```



```

for(j=2;j<=4;j++)
{
for(i=0;i<n-j;i++)
{
diff[i][j]=diff[i+1][j-1]-diff[i][j-1];
}
}
i=0;
do
{
i++;
}
while(ax[i]<x);
i--;
p=(x-ax[i])/h;
y1=p*diff[i-1][1];
y2=p*(p+1)*diff[i-1][2]/2;
y3=(p+1)*p*(p-1)*diff[i-2][3]/6;
y4=(p+2)*(p+1)*p*(p-1)*diff[i-3][4]/24;
y=ay[i]+y1+y2+y3+y4;

printf("\nwhen x=%6.4f, y=%6.8f ",x,y);
getch();
}

```

Output

"C:\Users\LENEVO\Desktop\CBNST\Newtons forward interpolation.exe"

```
Enter the number of terms - 5
Enter the value in the form of x - Enter the value of x1 - 2
Enter the value of x2 - 4
Enter the value of x3 - 6
Enter the value of x4 - 8
Enter the value of x5 - 10

Enter the value in the form of y - Enter the value of y1 - 12.3
Enter the value of y2 - 15.8
Enter the value of y3 - 19.7
Enter the value of y4 - 23.8
Enter the value of y5 - 27.9

Enter the value of x for
which you want the value of y - 5

when x=5.0000, y=17.70000076
```

Program 12

Objective: Program to implement Newton Backward Interpolation Method.

Algorithm:

1. Start of the program.
2. Input number of terms n
3. Input the array ax
4. Input the array ay
5. $h = ax[1] - ax[0]$
6. for $i = 0; i < n - 1; i++$
7. $diff[i][1] = ay[i+1] - ay[i]$
8. End Loop i
9. for $j = 2; j \leq 4; j++$
10. for $i = 0; i < n - j; i++$
11. $diff[i][j] = diff[i+1][j-1] - diff[i][j-1]$
12. End Loop i
13. End Loop j
14. $i = 0$
15. Repeat Step 16 until $(!ax[i] < x)$
16. $x0 = mx[i]$
17. $sum = 0$
18. $y0 = my[i]$

19.fun=1

20.p=(x-x0)/h

21.sum=y0

22.k=1; k<=4; k++

23.fun=(fun*(p-(k-1)))/k

24.sum=sum+fun*diff[i][k]

25.End loop k

26.Print Output x,sum

27.End of Program

Source Code

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
#include<process.h>
#include<string.h>
void main()
{
int n,i,j,k;
float mx[10],my[10],x,x0=0,y0,sum,h,fun,p,diff[20][20],y1,y2,y3,y4;
clrscr();
printf("\n enter the no. of terms - ");
scanf("%d",&n);
printf("\n enter the value in the form of x - ");
for(i=0;i<n;i++)
{
printf("\n enter the value of x%d- ",i+1);
scanf("%f",&mx[i]);
}
printf("\n enter the value in the form of y - ");
for(i=0;i<n;i++)
{
printf("\n\n enter the value of y%d- ",i+1);
scanf("%f",&my[i]);
}
printf("\n enter the value of x for");
printf("\nwhich you want the value of of y -");

scanf("%f",&x);h=mx[1]-mx[0];
for(i=0;i<n-1;i++)
{
diff[i][1]=my[i+1]-my[i];
}
for(j=2;j<=4;j++)
{
for(i=0;i<n-j;i++)
{
diff[i][j]=diff[i+1][j-1]-diff[i][j-1];
}
}
i=0;
while(!mx[i]>x)
{
i++;
```

```
}
x0=mx[i];
sum=0;
y0=my[i];
fun=1;
p=(x-x0)/h;
sum=y0;
for(k=1;k<=4;k++)
{
fun=(fun*(p-(k-1)))/k;
sum=sum+fun*diff[i][k];}
printf("\n when x=%6.4f,y=%6.8f",x,sum);
printf("\n press enter to exit");
getch();
}
```

Output

```
enter the no. of terms -    5
enter the value in the form of x -
enter the value of x1-    1
enter the value of x2-    3
enter the value of x3-    5
enter the value of x4-    7
enter the value of x5-    9
enter the value in the form of y -
enter the value of y1-    5.6
enter the value of y2-    7.9
enter the value of y3-    13.8
enter the value of y4-    15
enter the value of y5-    19
enter the value of x for
which you want the value of of y -8
when x=8.0000,y=15.56406212
press enter to exit_
```

Program 13

Objective: Program to implement Lagrange's Interpolation Method.

Algorithm:

1. Start
2. Read number of data (n)
3. Read data X_i and Y_i for $i=1$ to n
4. Read value of independent variables say x_p
whose corresponding value of dependent say y_p is to be determined.
5. Initialize: $y_p = 0$
6. For $i = 1$ to n
 Set $p = 1$
 For $j = 1$ to n
 If $i \neq j$ then
 Calculate $p = p * (x_p - X_j) / (X_i - X_j)$
 End If
 Next j
 Calculate $y_p = y_p + p * Y_i$
Next i
7. Display value of y_p as interpolated value.
8. Stop

Source Code

```
#include<stdio.h>
```



```
#include<conio.h>
```

```
void main()
```

```
{
```

```
    float x[100], y[100], xp, yp=0, p;
```

```
    int i,j,n;
```

```
    clrscr();
```

```
    /* Input Section */
```

```
    printf("Enter number of data: ");
```

```
    scanf("%d", &n);
```

```
    printf("Enter data:\n");
```

```
    for(i=1;i<=n;i++)
```

```
    {
```

```
        printf("x[%d] = ", i);
```

```
        scanf("%f", &x[i]);
```

```
        printf("y[%d] = ", i);
```

```
        scanf("%f", &y[i]);
```

```
    }
```

```
    printf("Enter interpolation point: ");
```

```
    scanf("%f", &xp);
```

```
    /* Implementing Lagrange Interpolation */
```

```
    for(i=1;i<=n;i++)
```

```
    {
```

```
        p=1;
```

```
        for(j=1;j<=n;j++)
```

```
        {
```

```
            if(i!=j)
```

```
            {
```

```
                 $p = p * (xp - x[j]) / (x[i] - x[j]);$ 
```

```
            }
```

```
        }
```

```
        yp = yp + p * y[i];
```

```
}  
printf("Interpolated value at %.3f is %.3f.", xp, yp);  
getch();  
}
```

Output

```
Enter number of data: 5
Enter data:
x[1] = 1
y[1] = 2
x[2] = 3
y[2] = 4
x[3] = 5
y[3] = 6
x[4] = 7
y[4] = 8
x[5] = 9
y[5] = 1
Enter interpolation point: 5.5
Interpolated value at 5.500 is 6.698.█
```

Program 14

Objective: Program to implement Trapezoidal rule.

Algorithm:

- Start
- Define and Declare function
- Input initial boundary value, final boundary value and length of interval
- Calculate number of strips, $n = (\text{final boundary value} - \text{initial boundary value}) / \text{length of interval}$
- Perform following operation in loop

$x[i] = x_0 + i * h$

$y[i] = f(x[i])$

print $y[i]$

- Initialize $se=0$, $s0=0$
- Do the following using loop

If $i \% 2 = 0$

$So = s0 + y[i]$

Otherwise

$Se = se + y[i]$

- $ans = h/3 * (y[0] + y[n] + 4 * so + 2 * se)$
- print the ans
- Stop

Source Code

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
float f(float x)
```

```

{
    return(1/(1+pow(x,2)));
}
void main(){
    int i,n;
    float x0,xn,h,y[20],so,se,ans,x[20];
    printf("\n Enter values of x0,xn,h:\n");
    scanf("%f%f%f",&x0,&xn,&h);
    n=(xn-x0)/h;
    if(n%2==1)
    {
        n=n+1;
    }
    h=(xn-x0)/n;
    printf("\nrefined value of n and h are:%d  %f\n",n,h);
    printf("\n Y values \n");
    for(i=0; i<=n; i++)
    {
        x[i]=x0+i*h;
        y[i]=f(x[i]);
        printf("\n%f\n",y[i]);
    }
    so=0;
    se=0;
    for(i=1; i<n; i++)
    {
        if(i%2==1)
        {
            so=so+y[i];
        }
        else
        {
            se=se+y[i];
        }
    }
    ans=h/3*(y[0]+y[n]+4*so+2*se);
    printf("\nfinal integration is %f",ans);
    getch();
}

```

Output

```
Enter values of x0,xn,h:
0
3
0.5
refined value of n and h are:6  0.500000
Y values
1.000000
0.800000
0.500000
0.307692
0.200000
0.137931
0.100000
final integration is 1.247082_
```

Program 15

Objective: Program to implement Simpson 1/3 rule.

Algorithm:

Step 1. Start;

Step 2. Input function $f(x)$;

Step 3. Read a, b, n ; // the lower and upper limits and number of sub-intervals

Step 4. Compute $h = (b - a) / n$;

Step 5. $\text{Sum} = [f(a) - f(a + nh)]$;

Step 6. for $i = 1$ to $n - 1$ step 2 do

 Compute $\text{sum} = \text{sum} + 4 * f(a + ih) + 2 * f(a + (i + 1)h)$;

endfor;

Step 7. Compute $\text{result} = \text{sum} * h / 3$;

Step 8. Print result;

Step 9. Stop;

Source Code

```
#include<stdio.h>
#include<conio.h>
float f(float x) {
```

```

    return(1/(1+x));
}
void main() {
    int i,n;
    float x0,xn,h,y[20],so,se,ans,x[20];
    printf("\n Enter values of x0,xn,h: ");
    scanf("%f%f%f",&x0,&xn,&h);
    n=(xn-x0)/h;
    if(n%2==1)
    {
        n=n+1;
    }
    h=(xn-x0)/n;
    printf("\n Refined value of n and h are:%d %f\n",n,h);
    printf("\n Y values: \n");
    for(i=0; i<=n; i++)
    {
        x[i]=x0+i*h;
        y[i]=f(x[i]);
        printf("\n %f\n",y[i]);
    }
    so=0;
    se=0;
    for(i=1; i<n; i++)
    {
        if(i%2==1)
        {
            so=so+y[i];
        }
        else
        {
            se=se+y[i];
        }
    }
    ans=h/3*(y[0]+y[n]+4*so+2*se);
    printf("\n Final integration is %f",ans);

    getch();
}

```

Output


```
Enter values of x0,xn,h:
2
4
0.5

Refined value of n and h are:4 0.500000

Y values:

0.333333
0.285714
0.250000
0.222222
0.200000

Final integration is 0.510847_
```

Program 16

Objective: Program to implement Simpson 3/8 rule.

Algorithm:

1. Given a function $f(x)$:
2. (Get user inputs) Input a, b =endpoints of interval n =number of intervals
3. Set $h = (b-a)/n$.
4. Set $sum = 0$.
5. Begin For $i = 1$ to $n - 1$ Set $x = a + h*i$. If $i \% 3 = 0$ Then Set $sum = sum + 2*f(x)$
Else Set $sum = sum + 3*f(x)$ End For
6. Set $sum = sum + f(a) + f(b)$
7. Set $ans = sum * (3h/8)$
8. End

Source Code

```
#include<stdio.h>
#include<conio.h>
#include<math.h>
#define f(x) 1/(1+x*x)
int main() {
    float lower, upper, integration=0.0, stepSize, k;
    int i, subInterval;
```

```

printf("Enter lower limit of integration: ");
scanf("%f", &lower);
printf("Enter upper limit of integration: ");
scanf("%f", &upper);
printf("Enter number of sub intervals: ");
scanf("%d", &subInterval);
stepSize = (upper - lower)/subInterval;
integration = f(lower) + f(upper);
for(i=1; i<= subInterval-1; i++)
{
    k = lower + i*stepSize;
    if(i%3 == 0)
    {
        integration = integration + 2 * f(k);
    }
    else
    {
        integration = integration + 3 * f(k);
    }
}
integration = integration * stepSize*3/8;
printf("\nRequired value of integration is: %.3f", integration);
getch();
return 0;
}

```

Output

```
Enter lower limit of integration: 0
Enter upper limit of integration: 1
Enter number of sub intervals: 12

Required value of integration is: 0.785_
```

Program 17

Objective: Program to Fit a line.

Algorithm:

1. Take two floating types of array. $x[10]$ and $y[10]$.

2. Now take n as input from the user.
3. Take x,y as input from the user with the help of for loop.
($0 \leq i < n$)
4. Now find the values of Σx , Σy , Σxy , Σx^2 using for loop.
5. Using the formula to solve the simultaneous equation solve for a and b. For formula have a look at Fig 2.
6. Put the values of a and b in the equation of the straight line by checking the condition if $b > 0$ or $b = 0$.
7. Print the result.

Source Code

```
#include<stdio.h>
int main() {
    int i,j,n;
    float x[10],y[10],sum1=0,sum2=0,sum3=0,sum4=0;
```

```

float a,b,d;
printf("\nInput the Value of n\n");
scanf("%d",&n);
printf("\nInput the values of x and y\n");
for(i=0;i<n;i++) {
    scanf("%f%f",&x[i],&y[i]);
}
for(i=0;i<n;i++)
{
    sum1=sum1+x[i];
    sum2=sum2+x[i]*x[i];
    sum3=sum3+y[i];
    sum4=sum4+x[i]*y[i];
}
d=n*sum2-sum1*sum1;
a=(sum2*sum3-sum1*sum4)/d;
b=(n*sum4-sum1*sum3)/d;
printf("\nThe values of a and b are : %f\t%f\n",a,b);
printf("\nThe Linear Relation is : \n");
if(b>0) {
    printf("\ny=%f+%fx\n",a,b);
}
else
{
    printf("y=%f%fx",a,b);
}
}

```

Output

```
Input the Value of n
2

Input the values of x and y
1
2
3
4

The values of a and b are : 1.000000    1.000000

The Linear Relation is :

y=1.000000+1.000000x

Process returned 0 (0x0)    execution time : 17.792 s
Press any key to continue.
_
```

Program 18

Objective: Program to Fit a Parabola.

Algorithm:

1. Read no. of data points n and order of polynomial Mp .
2. Read data values .
3. If $n < M_p$ [Regression is not possible] stop else continue ;

4. Set $M = M_p + 1$;
5. Compute co-efficient of C-matrix .
6. Compute co-efficient of B-matrix .
7. Solve for the co-efficients a_1, a_2, \dots, a_n .
8. Write the co-efficient .
9. Estimate the function value at the given of independent variables .

Source Code

```
#include<stdio.h>
#include<math.h>
int main(){
    float xy[20][20], matrix[3][4], ratio, a;
    float sum_x = 0, sum_y = 0, sum_x2 = 0, sum_x3 = 0, sum_x4
=0, sum_xy = 0, sum_x2y = 0;
    int i, j , k, n;
    printf("Enter no of data: ");
    scanf("%d", &n);
    printf("Enter the data: \n");
```



```

for(i = 0; i < 2; i++){
    for(j = 0; j < n; j++){
        scanf("%f", &xy[i][j]);
    }
}

for(i = 0; i < n; i++){
    sum_x += xy[0][i];
    sum_y += xy[1][i];
    sum_x2 += pow(xy[0][i], 2);
    sum_x3 += pow(xy[0][i], 3);
    sum_x4 += pow(xy[0][i], 4);
    sum_xy += xy[0][i]*xy[1][i];
    sum_x2y += pow(xy[0][i], 2) * xy[1][i];
}

matrix[0][0] = n;
matrix[0][1] = sum_x;
matrix[0][2] = sum_x2;
matrix[0][3] = sum_y;
matrix[1][0] = sum_x;
matrix[1][1] = sum_x2;
matrix[1][2] = sum_x3;
matrix[1][3] = sum_xy;
matrix[2][0] = sum_x2;
matrix[2][1] = sum_x3;
matrix[2][2] = sum_x4;
matrix[2][3] = sum_x2y;
for(i = 0; i < 3; i++){
    for(j = 0; j < 3; j++){
        if(i!=j){
            ratio = matrix[j][i]/matrix[i][i];
            for(k = 0; k < 4; k++){
                matrix[j][k] -= ratio * matrix[i][k];
            }
        }
    }
}

```

```
        }
    }
}
}
for(i = 0; i < 3; i++){
    a = matrix[i][i];
    for(j = 0; j < 4; j++){
        matrix[i][j] /= a;
    }
}
for(i = 0; i < 3; i++){
    printf("\n%c => %.2f", 97+i, matrix[i][3]);
}
}
```

Output

```
Enter no of data: 6
Enter the data:
1
2
3
5
5
4
6
7
8
9
4
5

a => 5.50
b => 0.97
c => -0.17
Process returned 0 (0x0)   execution time : 19.232 s
Press any key to continue.
```