

## An Implementation of a Distributed Queue

We are going to implement a distributed queue based on the Multi-Paxos algorithm by modifying the files from the previous lab. In particular, this requires updating the following classes:

**Message** : use the message types and payloads relevant for Multi-Paxos

**Replica** : the `execute` method has to be modified to handle messages according to a node in Multi-Paxos.

For storage, you can still use a `HashMap` where keys are `Integer` (and denote indices in the log) and values represent enqueue/dequeue invocations, with inputs for enqueues (you may define another class to represent such invocations).

The communication between the DDS and the clients also needs to be updated:

**Inputs:** In the previous lab, each invocation (except for Stop) is sent to a single replica. Now, every invocation is broadcasted to all replicas. A replica stores the invocations it receives (e.g., in a map from client ids to invocations). *We will assume that every client submits a single invocation.*

**Outputs:** An output (of a dequeue) is sent by a replica only when all the previous indices in the log are filled. This output is computed by simulating the sequence of methods on a “real” queue, e.g., `java.util.Queue`.

The channels between the DDS and clients should be of type FIFO. The channels between replicas should be of type Bag.

The leader of a round  $r$  is chosen as explained in the lecture, i.e. the replica with  $\text{id} = r \bmod N$  where  $N$  is the total number of replicas. After a decision, the leader should continue with proposals until a random integer in the interval  $[0,1]$  becomes 0. Use the function `nextInt(1)` of the class `Random` to sample a random integer in the interval  $[0,1]$  (see the class `ChannelBag` for an example).

Test your implementations with multiple combinations of clients (as suggested in the Testing file). Be careful to correctness when messages are received in arbitrary orders.

**Optional.** Modify your implementation so that every client can submit multiple invocations. An invocation should be associated to an identifier that is a pair (`clientId`, `inv_number`) where `inv_number` is an integer that fixes an order between invocations of the same client (it is assumed that clients submit invocations with consecutive numbers). Be careful so that the invocations “proposed” in multi-Paxos respect the order between invocations of the same client (each proposer must check what invocations of a client were already decided before choosing a next one).