

Linear Regression

Presented by
FCAI-CU-AI-Community

One a day as a ML
Engineer your Manager
Asked you to work on a
problem

Our Problem

Given some attributes, we will discuss them in next slide

We want to predict **Flight Ticket Price**.



ID	airline	flight	source_city	destination_city	arrival_time	departure_time	stops	class	duration	days_left	price
0	SpiceJet	SG-8709	Delhi	Mumbai	Night	Evening	zero	Economy	2.17	1	5953
1	SpiceJet	SG-8157	Delhi	Mumbai	Morning	Early_Morning	zero	Economy	2.33	1	5953
2	AirAsia	I5-764	Delhi	Mumbai	Early_Morning	Early_Morning	zero	Economy	2.17	1	5956

**So, What Do you Think?
Is it suitable to solve it
with traditional
approach or use ML
approach**

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As you can see, when **arrival_time** and **duration** changed that didn't affect the **price** so using rules will not benefit us.

arrival_time	departure_time	stops	class	duration	days_left	price
Night	Evening	zero	Economy	2.17	1	5953
Morning	Early_Morning	zero	Economy	2.33	1	5953

ML Approach

Questions that need to be answered to select the appropriate algorithm:

1. Is problem **Supervised** or **Unsupervised**?
2. Is it **classification** or **Regression**?



It is a Supervised Problem

because our target exists in data which is **price**



**But What is the
Difference between
Classification and
Regression?**

	Classification	Regression
Target	Discrete values	Continuous Values
Example	Cat or Dog, Spam or Ham	House Prices, Score in Exam

It is a Regression Problem

Because price has continuous values



So, prepare for meeting
our first regression
model which is

Linear Regression

Remember straight line equation:

$$Y = W * X + b$$

Where:

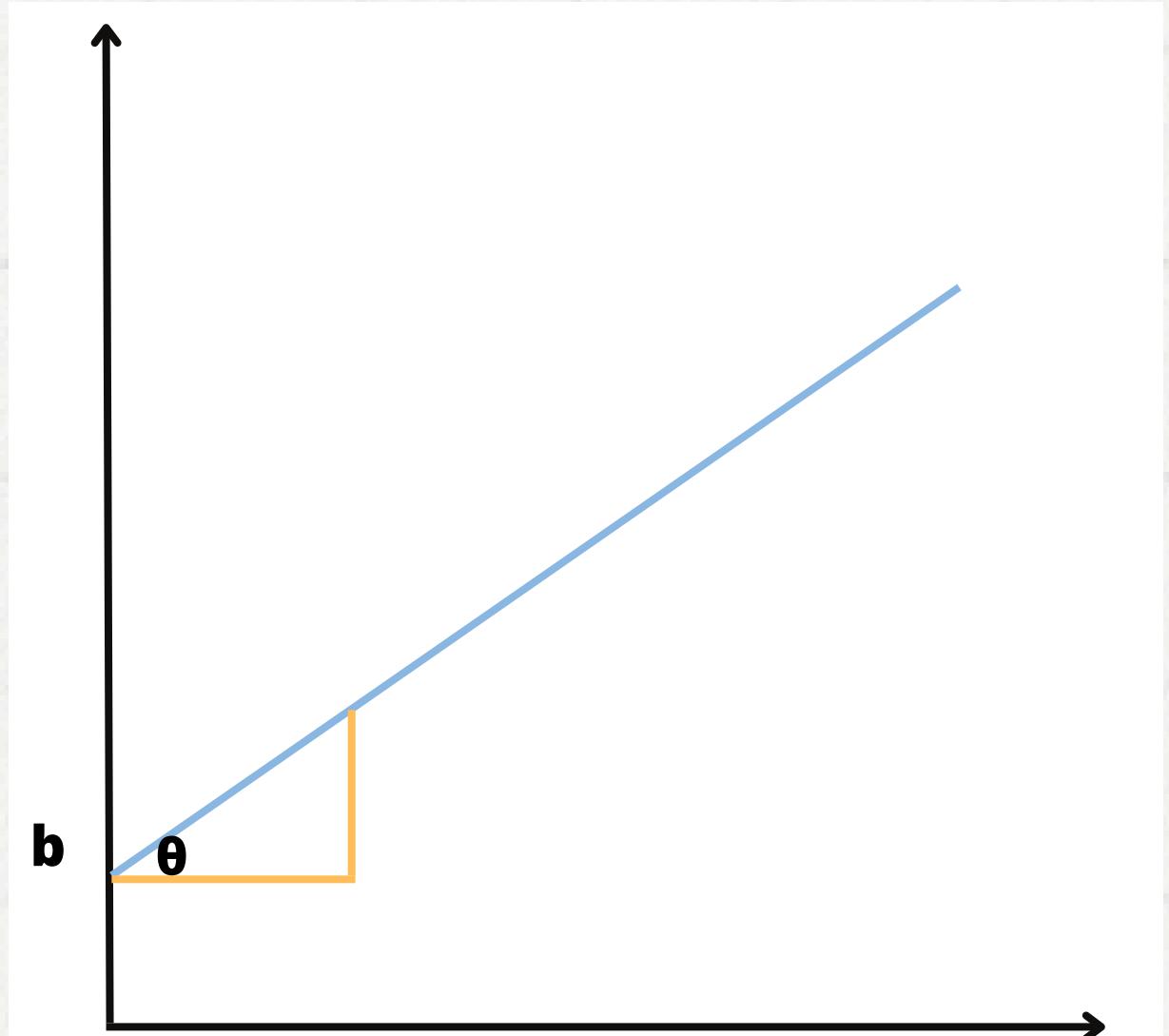
$$W = \tan(\theta) = \frac{y}{x}$$

b: is intercepted part from y-axis

Inputs: X

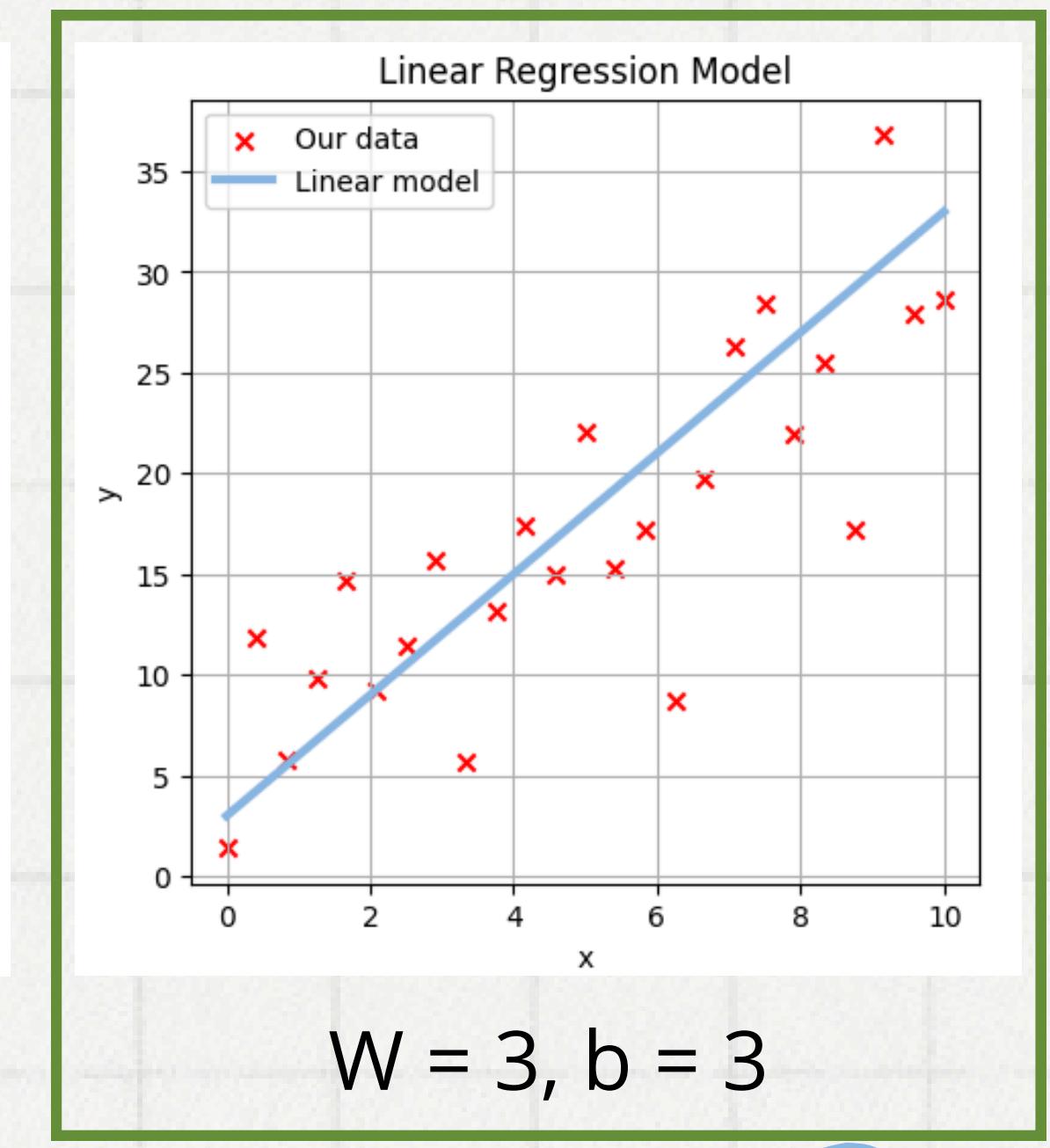
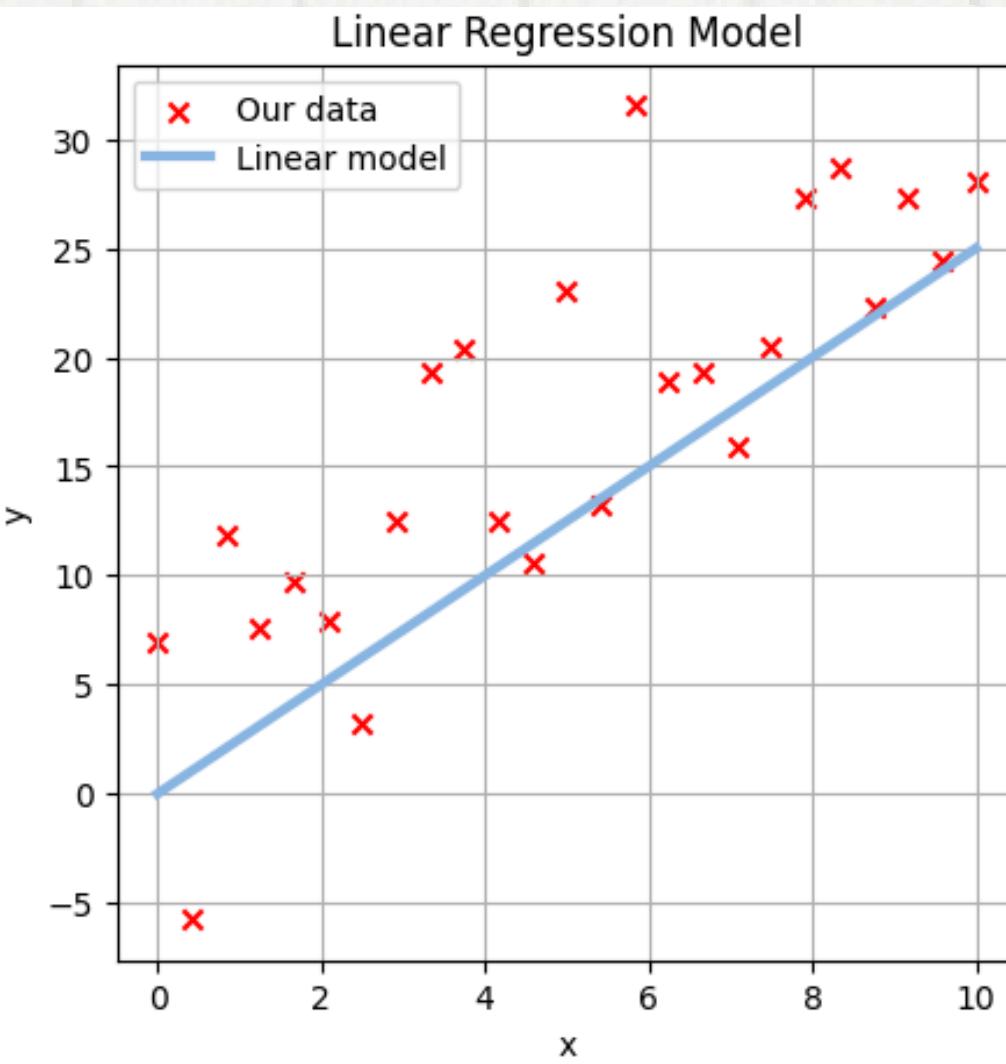
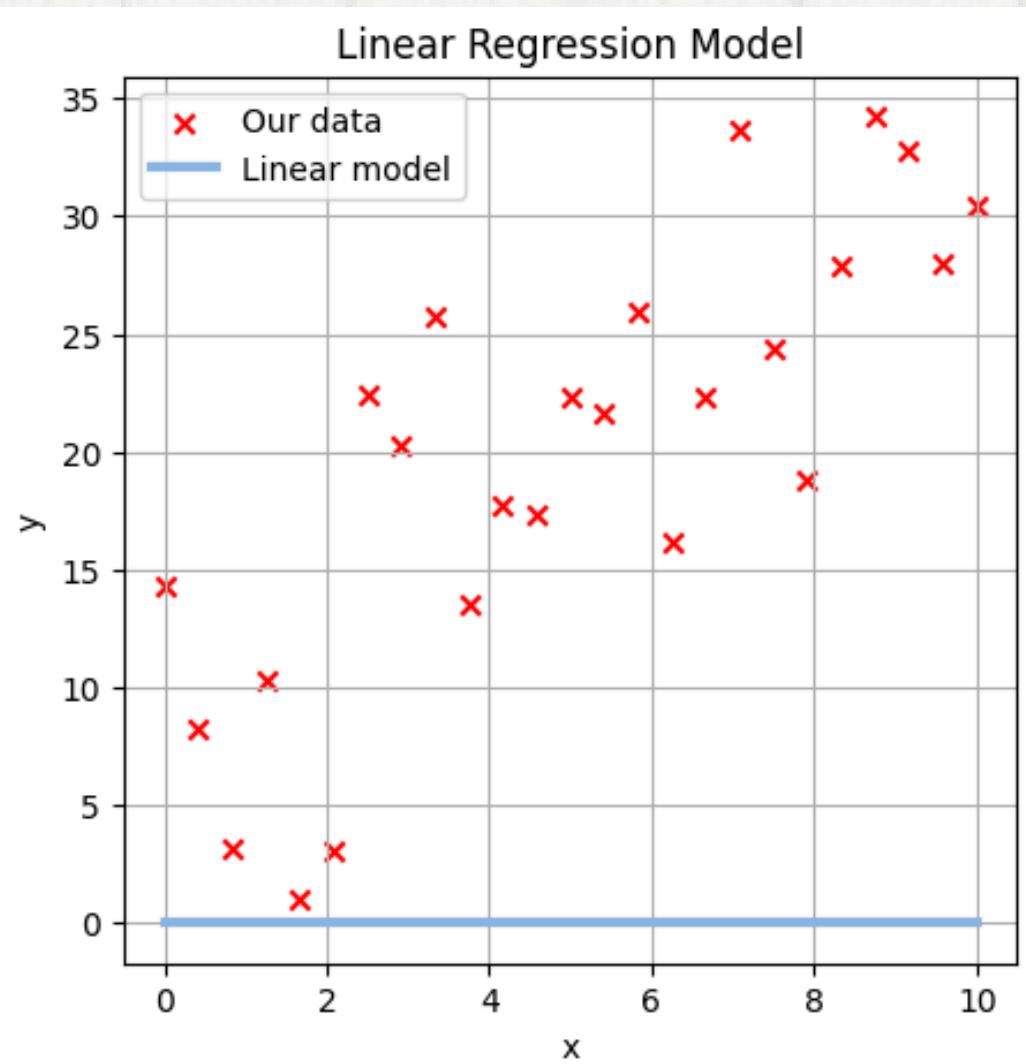
outputs: Y

variables: W, b



**Linear Regression
simply is just finding
best line to fit our data**

Which line is the best?

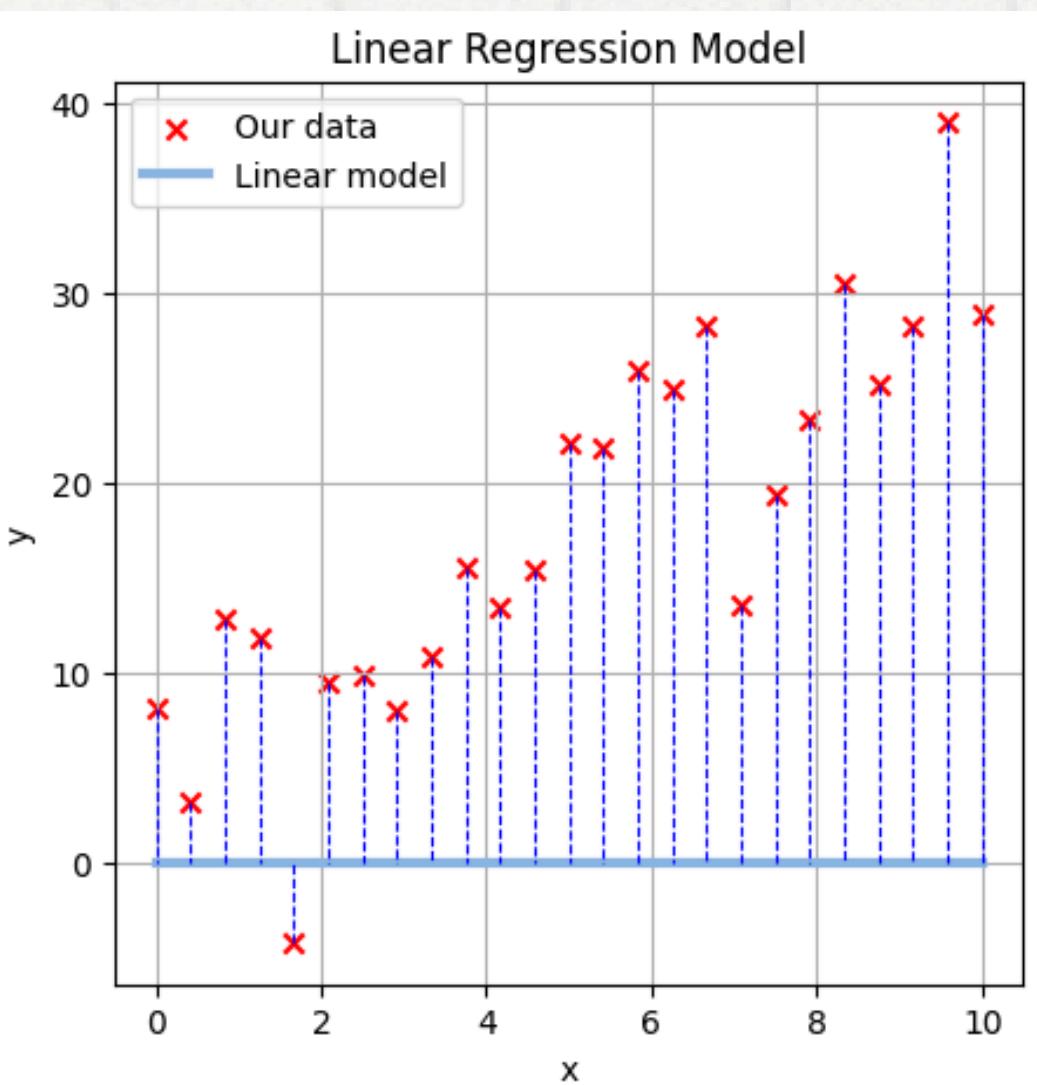


$W = 0, b = 0$

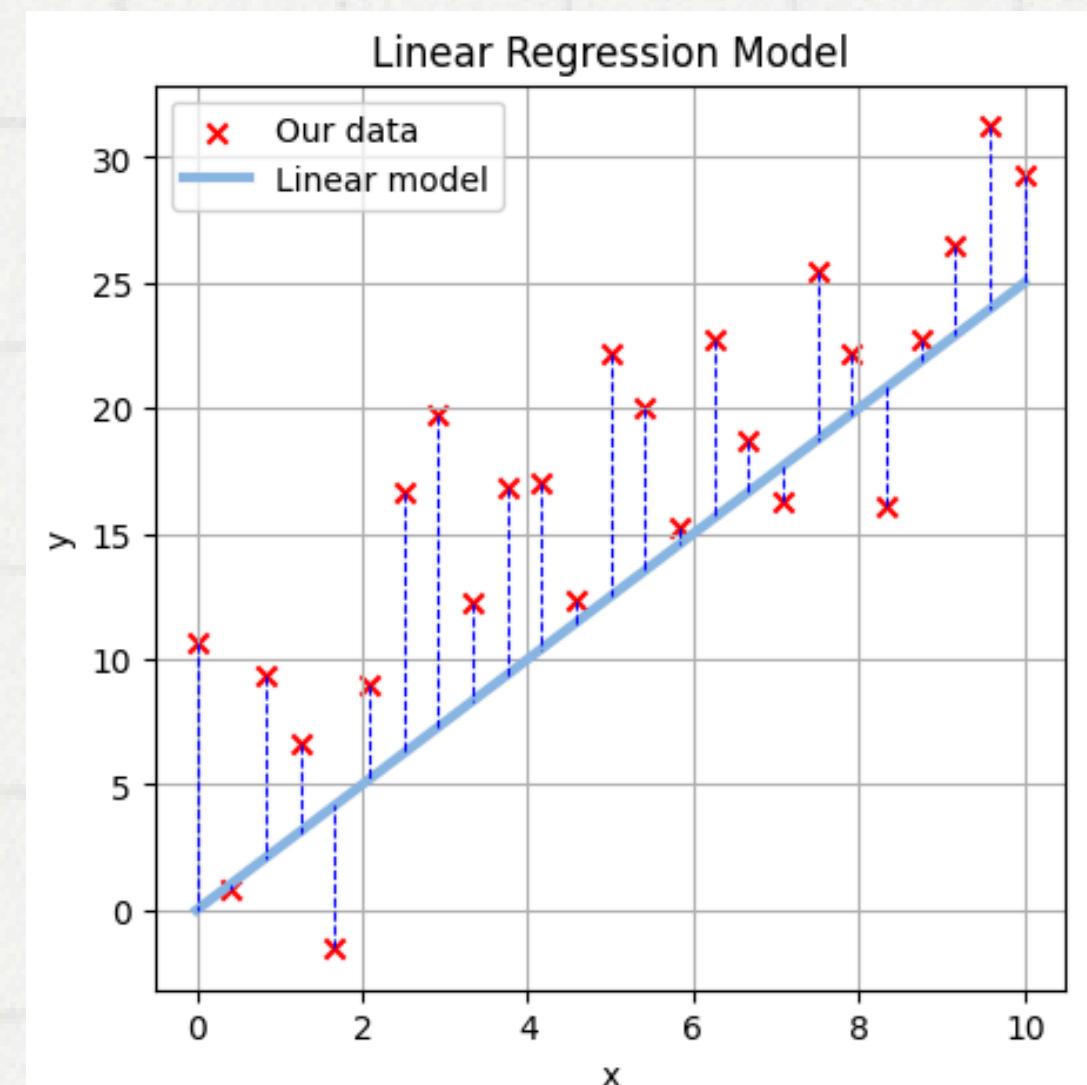
$W = 2.5, b = 0$

**As humans, we can
choose the best line,
but how can a machine
do that?**

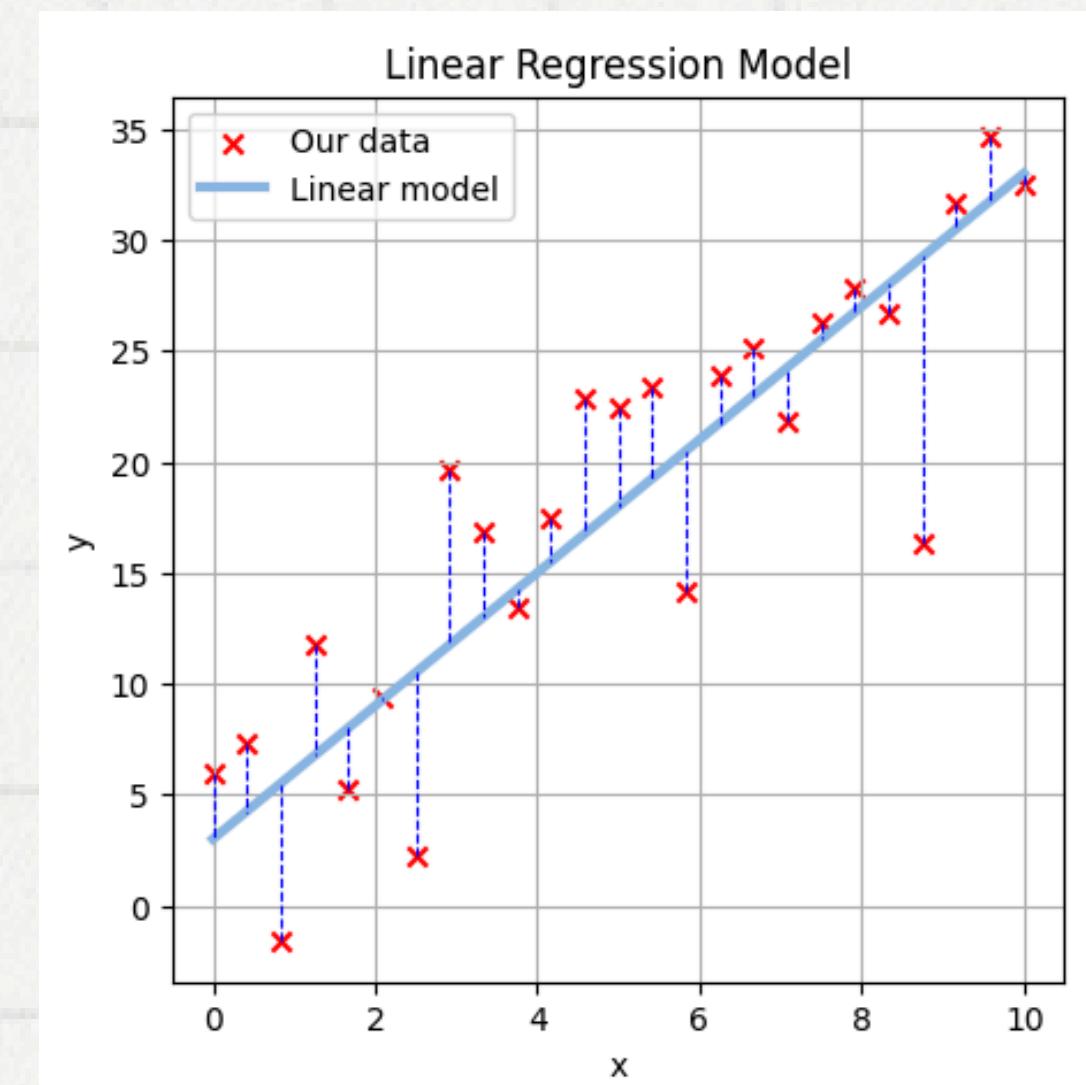
Is measuring distance between actual and predict can help us?



$$W = 0, b = 0$$



$$W = 2.5, b = 0$$



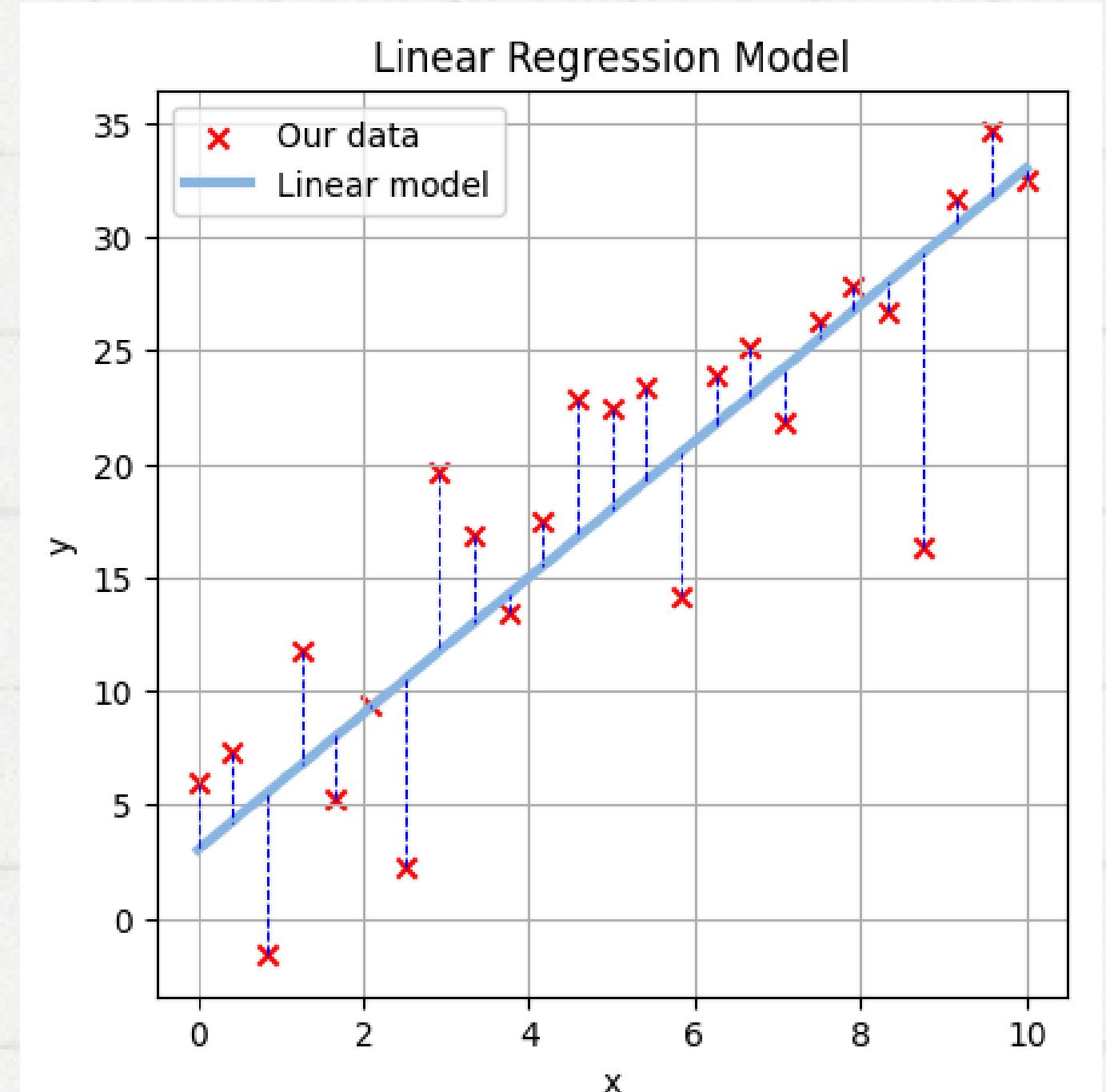
$$W = 3, b = 3$$

Lets define some symbols:

y : *Actual data value*

\hat{y} : *Predicted data value*

$$\hat{y} = W * X + b$$



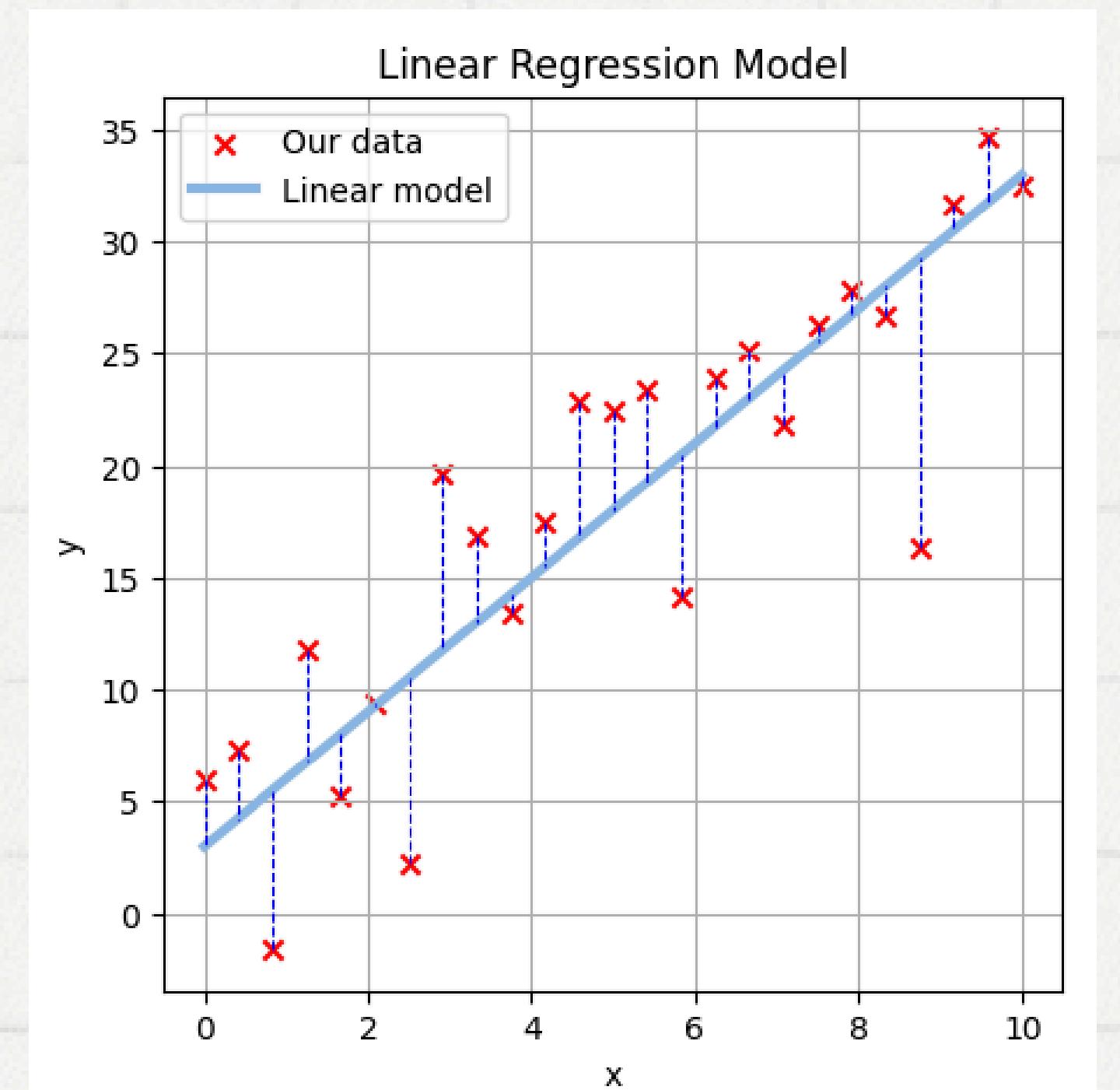
$$\hat{y} = W * X + b \quad y$$

$$distance = \hat{y} - y$$

$$distance = (\hat{y} - y)^2$$

$$Total\ distance = \sum_{i=0}^m (\hat{y}_i - y_i)^2$$

$$MSE = \frac{1}{2m} \sum_{i=0}^m (\hat{y}_i - y_i)^2$$



**Now that we have
calculated MSE what
will we do with it?**

**Of course we need to minimize it
but how?**

$$\hat{y} = W * X + b \quad y$$

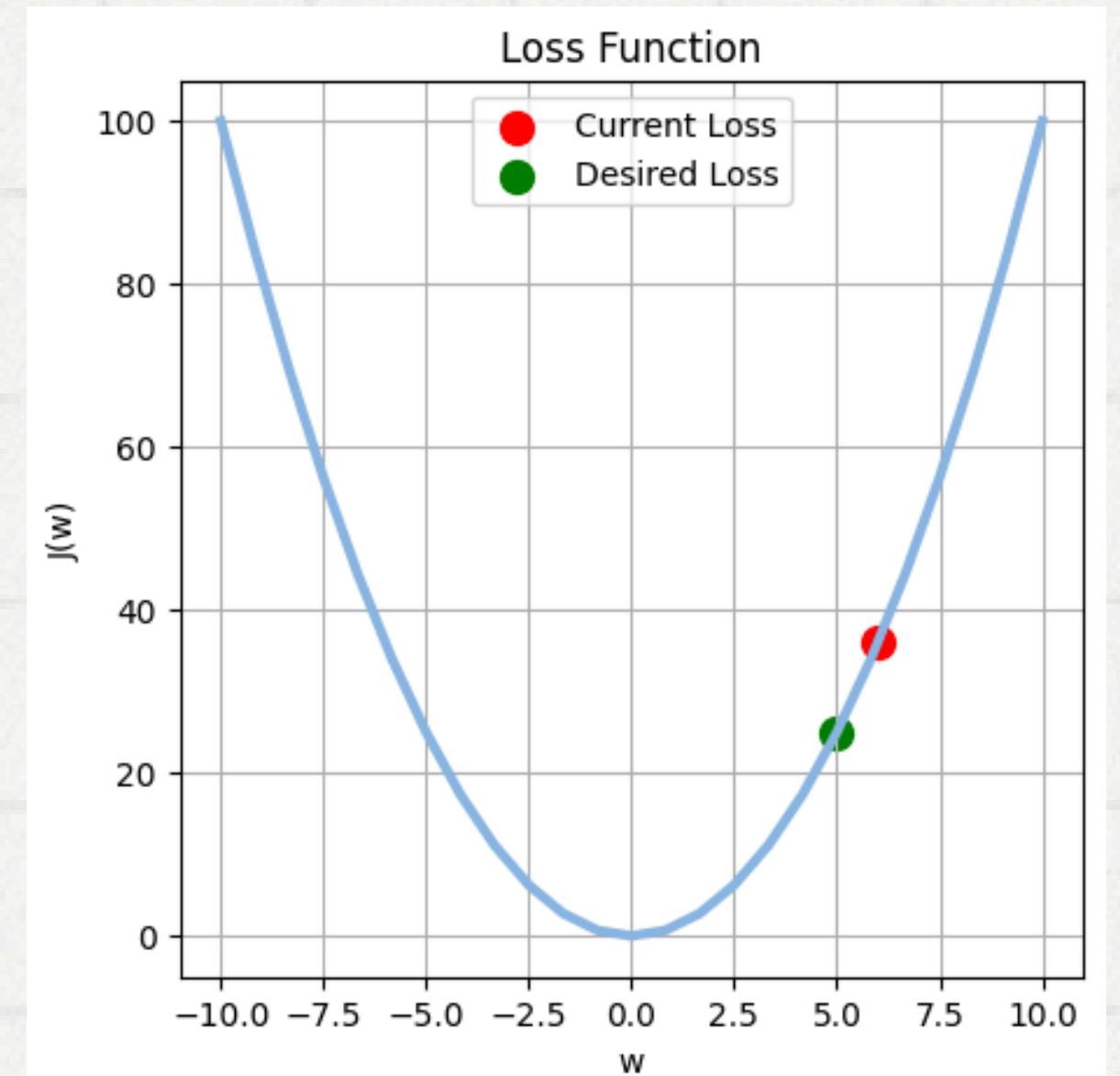
$$J(w, b) = \frac{1}{2m} \sum_{i=0}^m (\hat{y}_i - y_i)^2$$

$$J(w, b) = \frac{1}{2m} \sum_{i=0}^m ((w * x_i + b) - y_i)^2$$

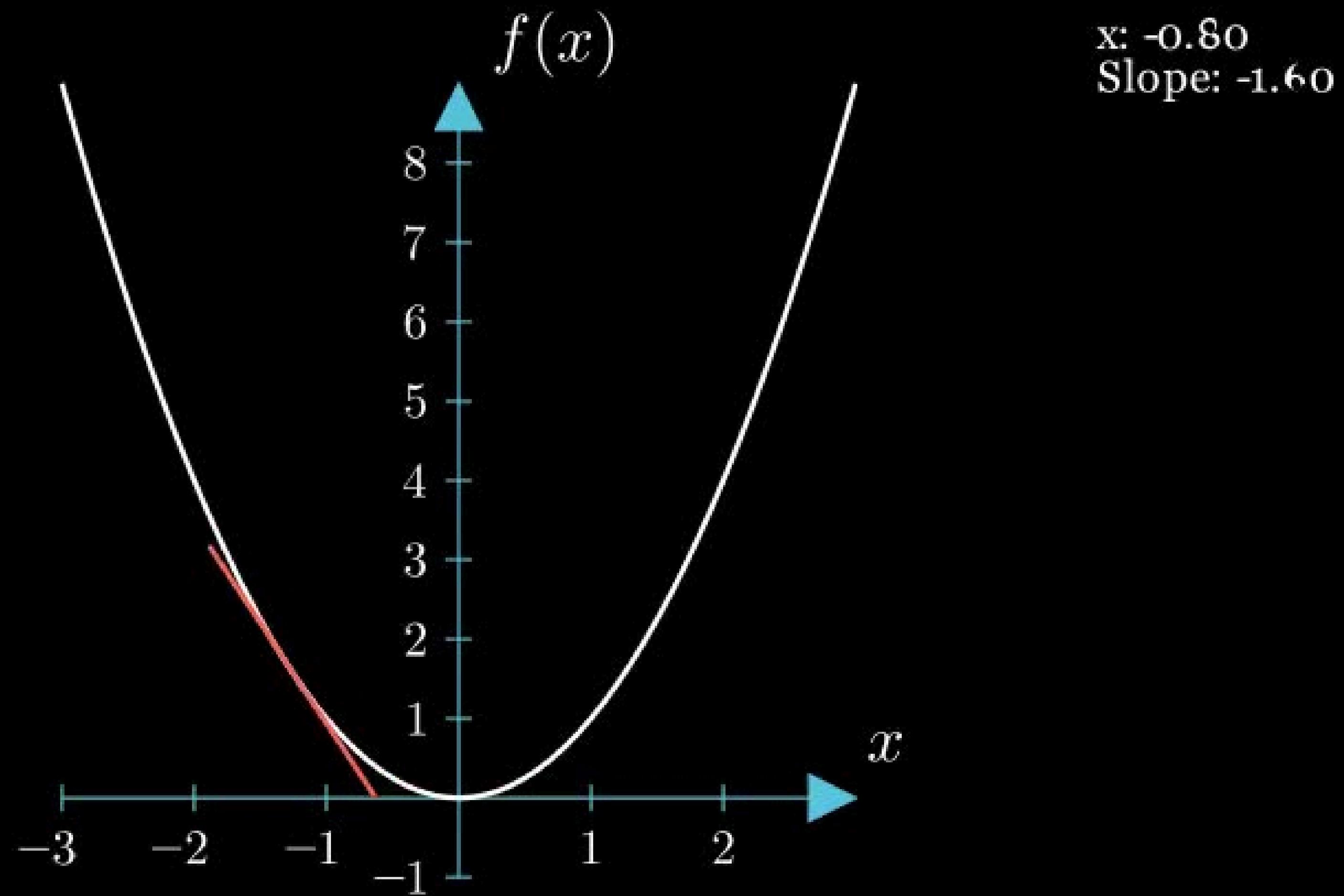
So as we can see in $J(w, b)$ if we want to minimize its value we need to change either W , b , or both

**Lets assume our Loss function: $J(W, b)$
Has only one input which is W and $b = 0$**

$$J(w, b) = \frac{1}{2m} \sum_{i=0}^m ((w * x_i) - y_i)^2$$



How we can move from the **red** dot to the **green** dot?

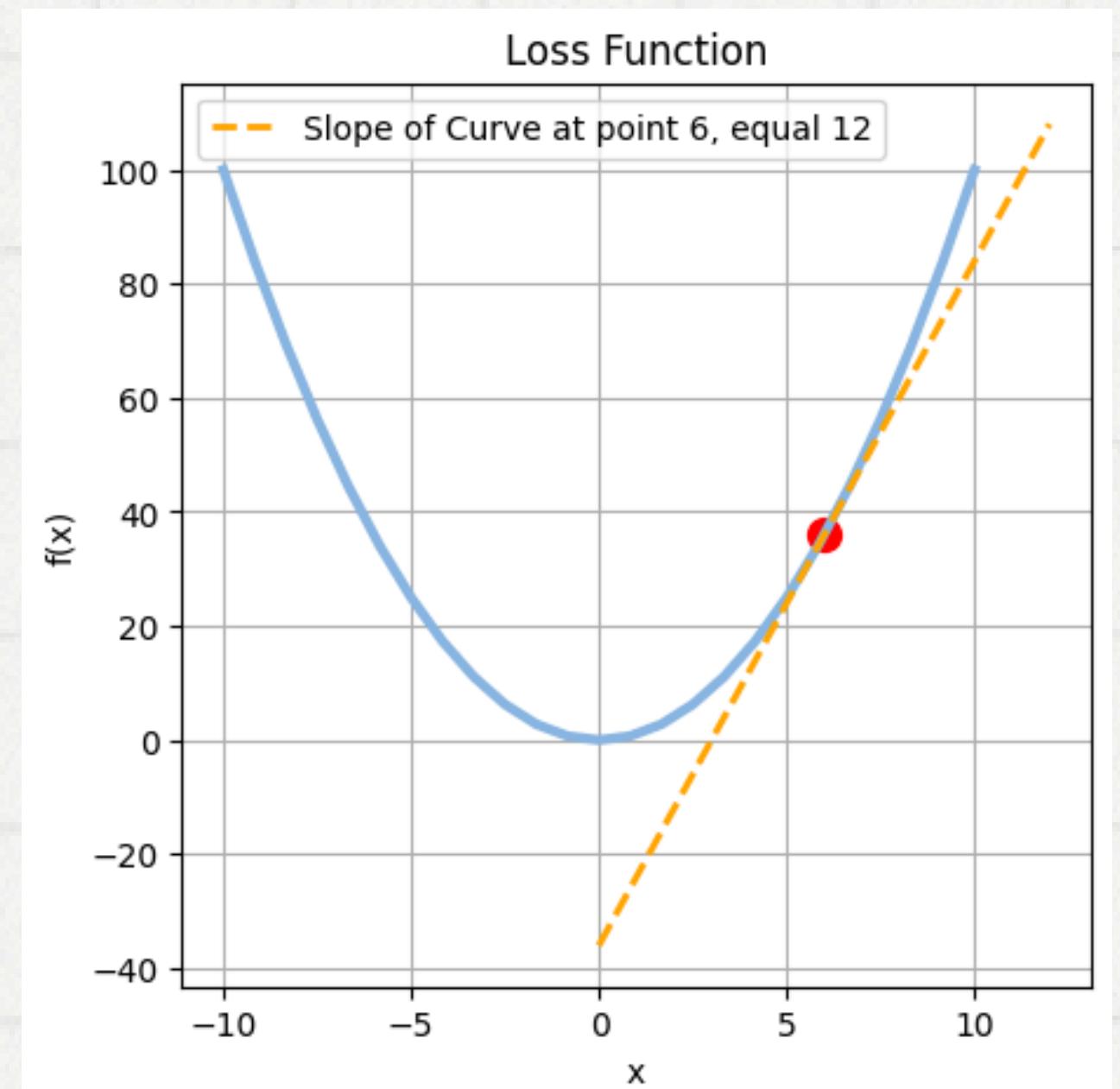


We can use the **slope** of the loss
function to update the **weights**

But actually, what is slope:

- Slope have different interpretations but one of its interpretations is that it is the derivative of function.
- Another interpretation is that it is $\tan(\theta)$, θ is angle made with x-axis

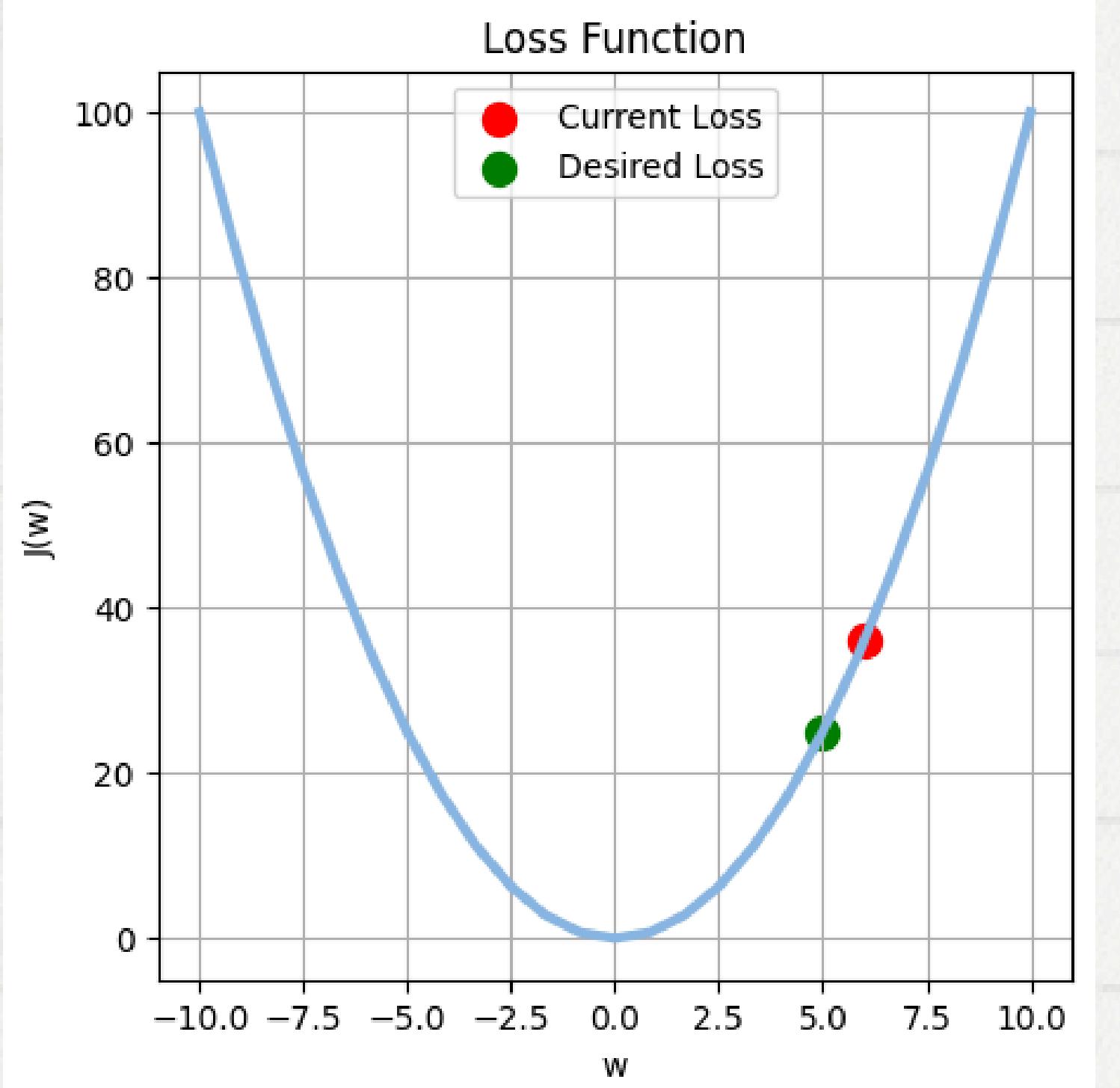
$$f(x) = x^2, \frac{df}{dx} = 2x$$



$$J(w, b) = \frac{1}{2m} \sum_{i=0}^m ((w * x_i) - y_i)^2$$

$$\frac{dJ}{dw} = \frac{2}{2m} \sum_{i=0}^m ((w * x_i) - y_i) * x_i$$

$$\frac{dJ}{dw} = \frac{1}{m} \sum_{i=0}^m ((w * x_i) - y_i) * x_i$$

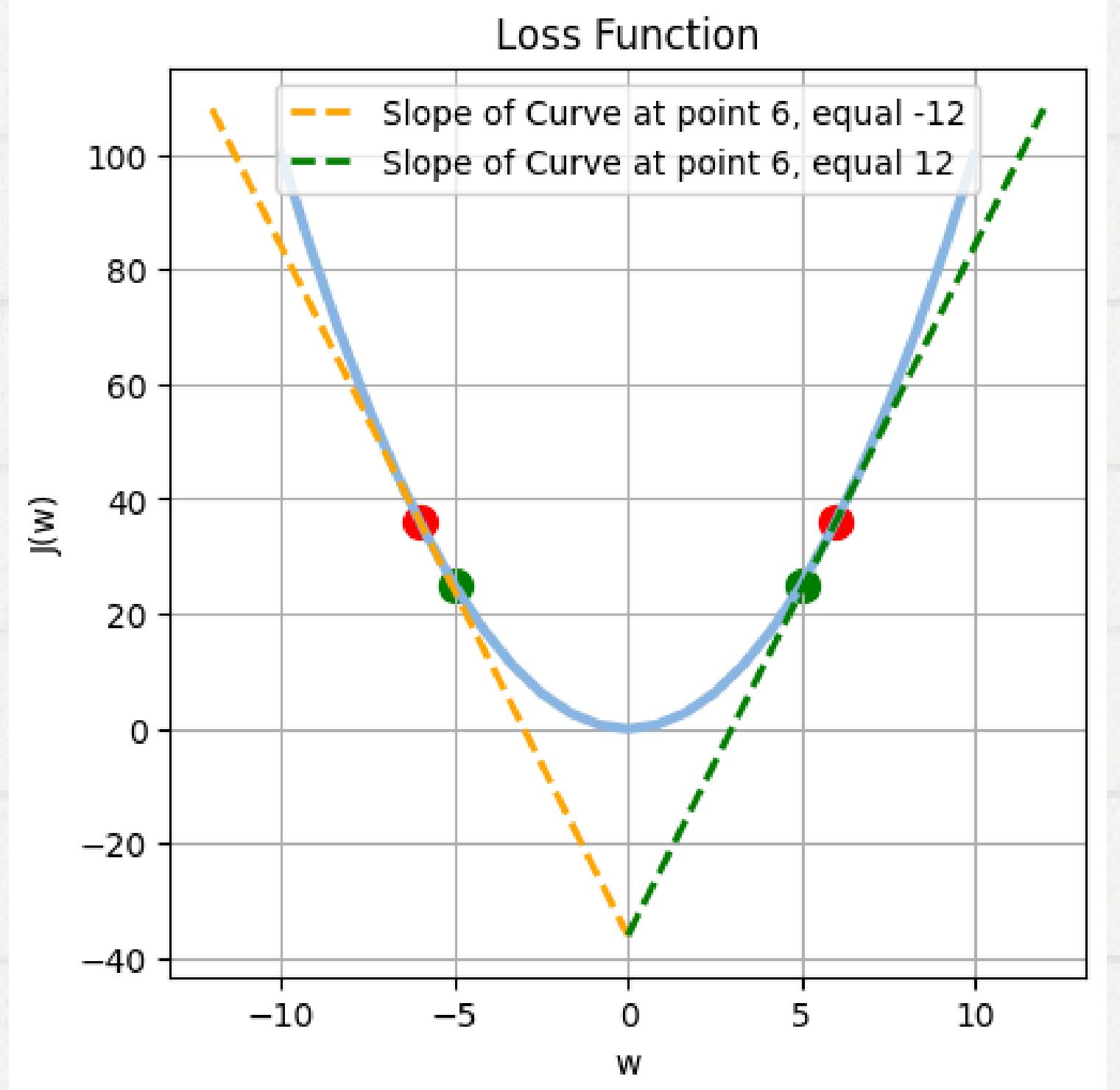


How can we use
this $\frac{dJ}{dw} = \frac{1}{m} \sum_{i=0}^m ((w * x_i) - y_i) * x_i$
To Update W



$$\frac{dJ}{dw} = \frac{1}{m} \sum_{i=0}^m ((w * x_i) - y_i) * x_i$$

$$w_{new} = w_{old} - \alpha * \frac{dJ}{dw}$$



$$J(w, b) = \frac{1}{2m} \sum_{i=0}^m ((w * x_i) - y_i)^2$$

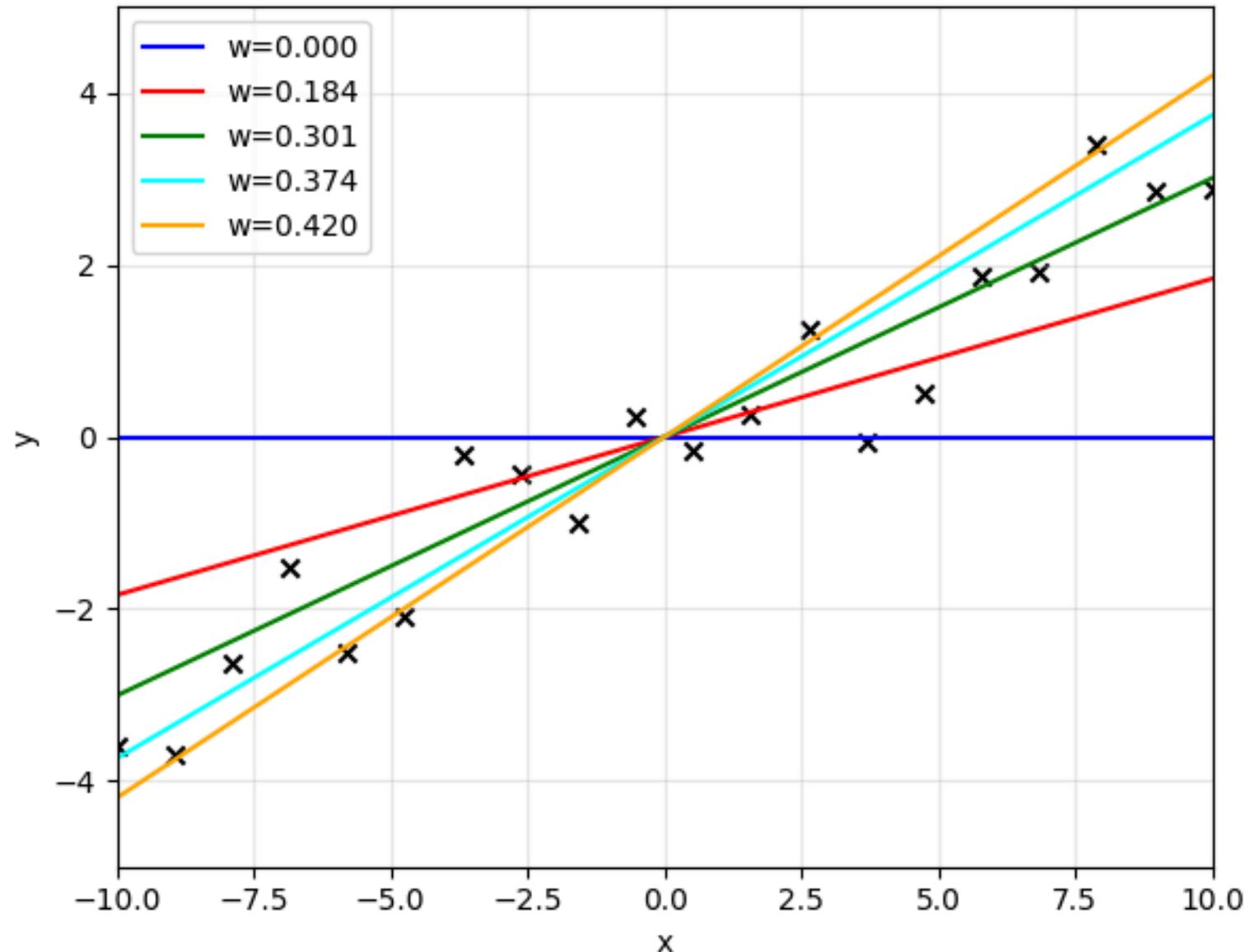
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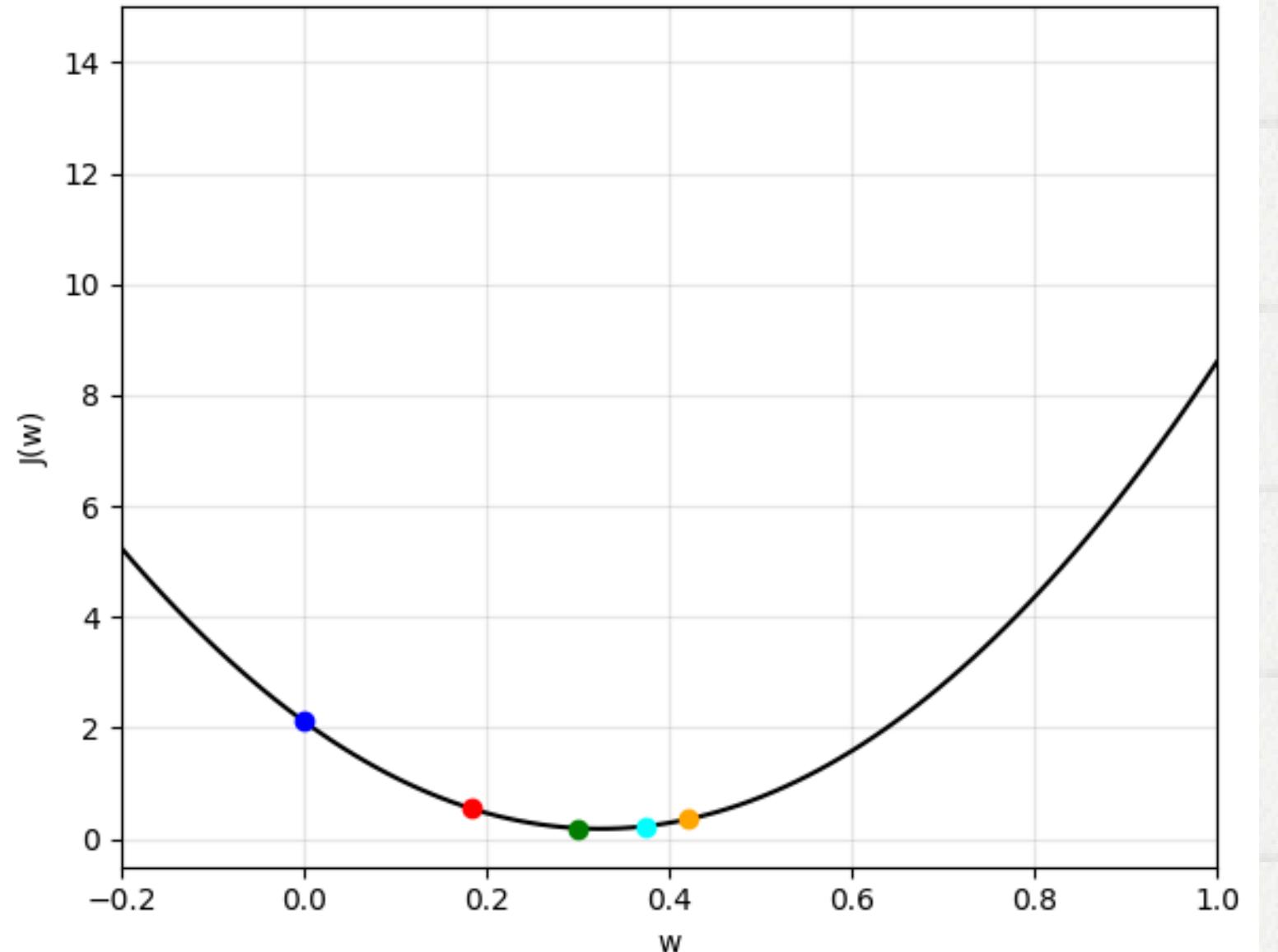
Repeat those three steps until convergence or reaching max iterations

How slope of Line change by changing w

Data and fit



Cost function

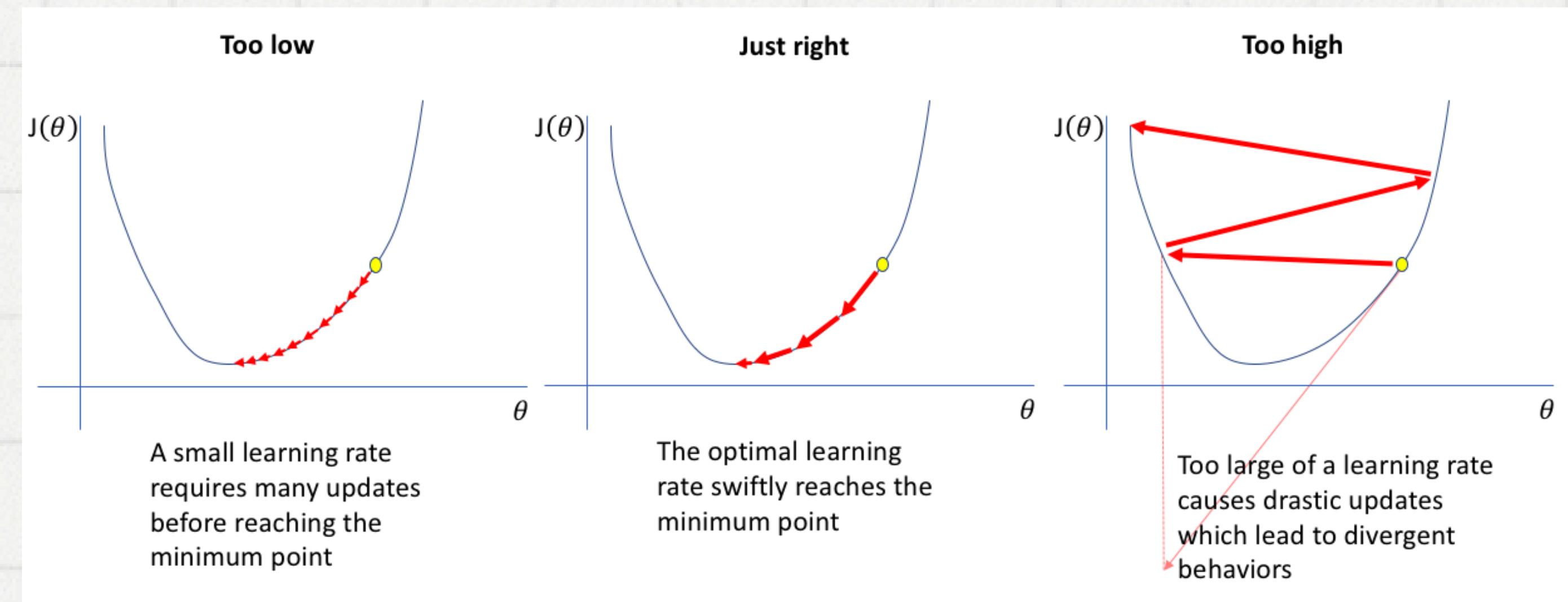


**So, we made what we wanted
but, what is α ?**

α is Called learning rate

- It is first hyperparameter you meet.
- It is used to control step of gradient towards global minima.
- usually ranges between 0.1 to 0.0001

Learning rate values effect:



Lets sum up the whole idea

Gradient descent steps:

1- Start with random w and b

2- compute cost $J(w, b) = \frac{1}{2m} \sum_{i=0}^m ((w * x_i + b) - y_i)^2$

3- compute derivative of cost with respect to w and b

$$3.1- \frac{dJ}{dw} = \frac{1}{m} \sum_{i=0}^m ((w * x_i + b) - y_i) * x_i$$

$$3.2- \frac{dJ}{db} = \frac{1}{m} \sum_{i=0}^m ((w * x_i + b) - y_i)$$

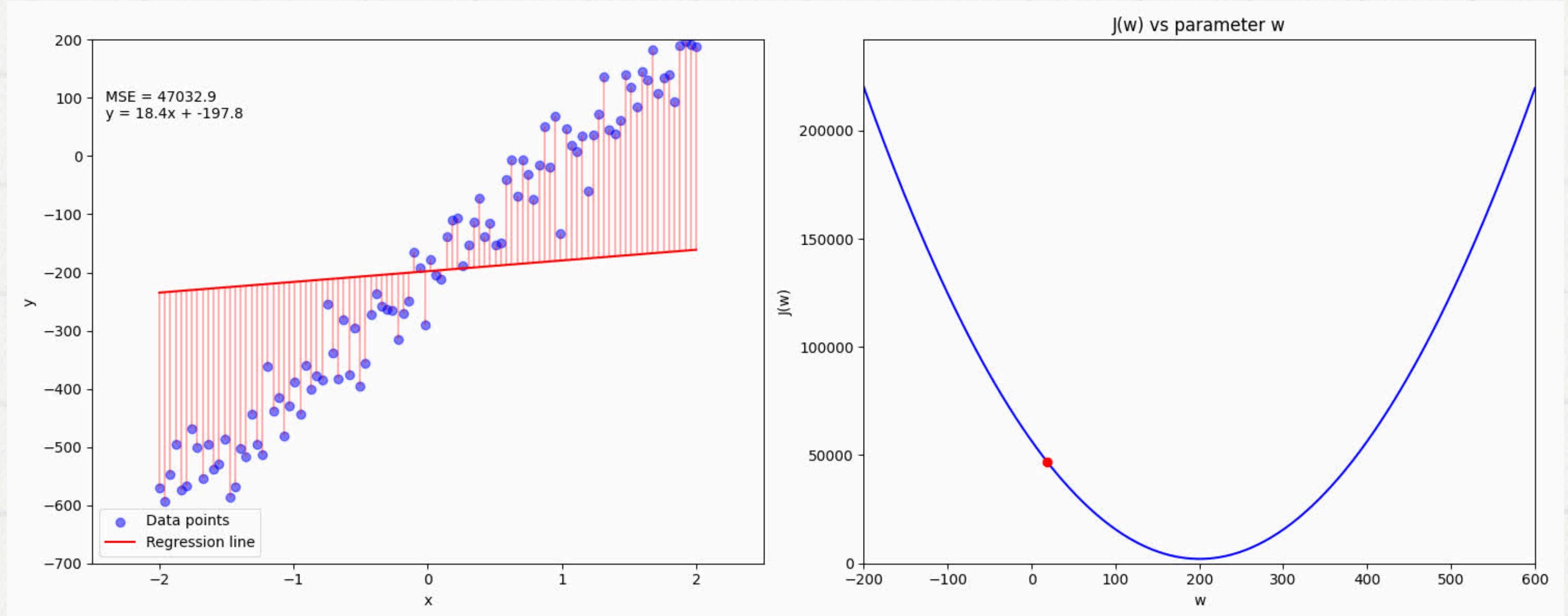
4- use this derivative to update weight and bias

$$4.1- w_{new} = w_{old} - \alpha \frac{dJ}{dw}$$

$$4.2- b_{new} = b_{old} - \alpha \frac{dJ}{db}$$

5- repeat 2,3,4 until converge or for some number of iterations

Gradient descent in action



**Thank you
very much!**