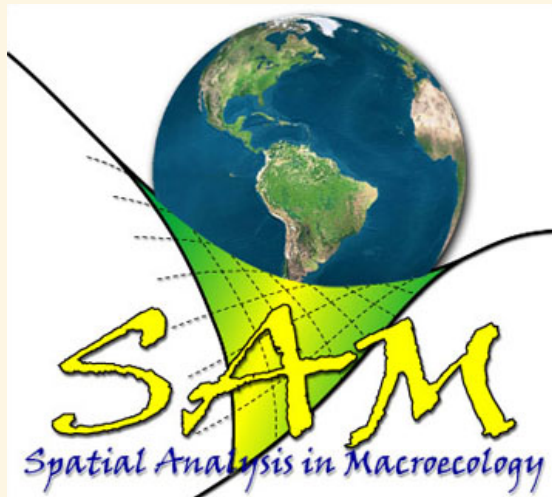


SPATIAL MODELLING

DAVID ORME

SPATIAL MODELLING TOOLS

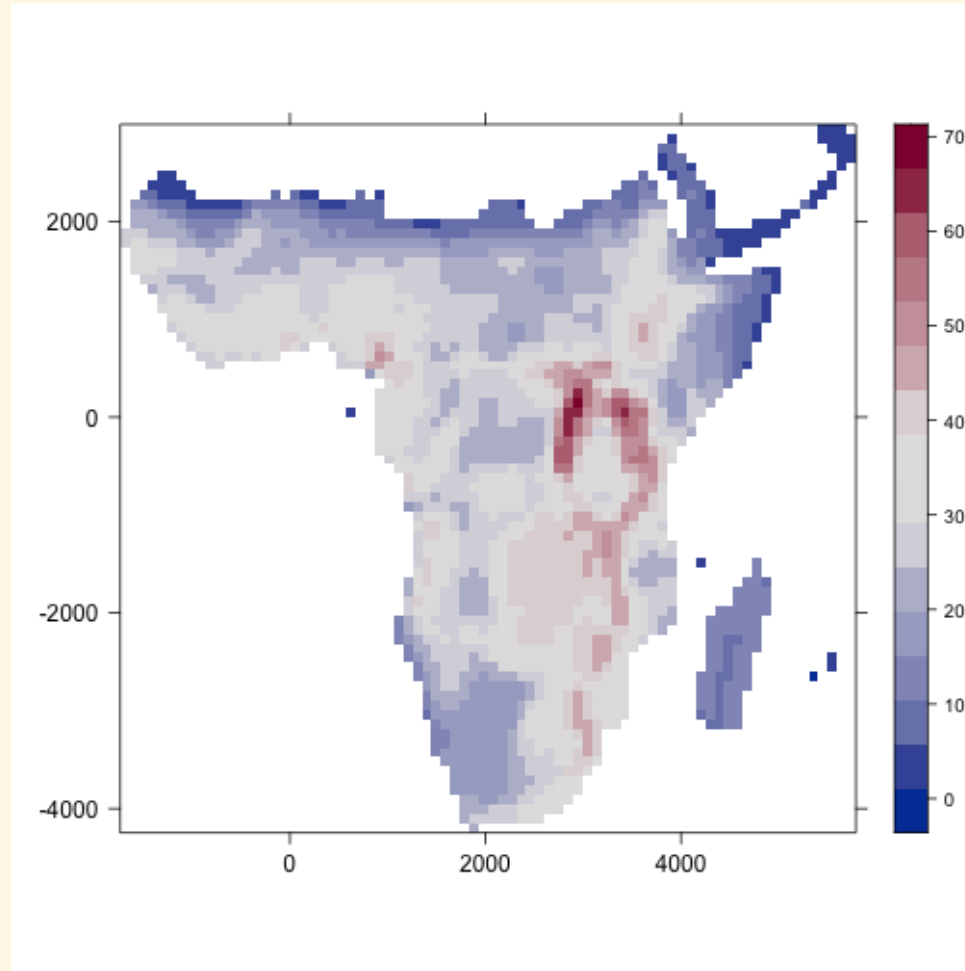
- The examples presented here use R
- Another excellent program with a nice GUI interface:
 - Spatial Analysis in Macroecology
 - <http://www.ecoevol.ufg.br/sam/>



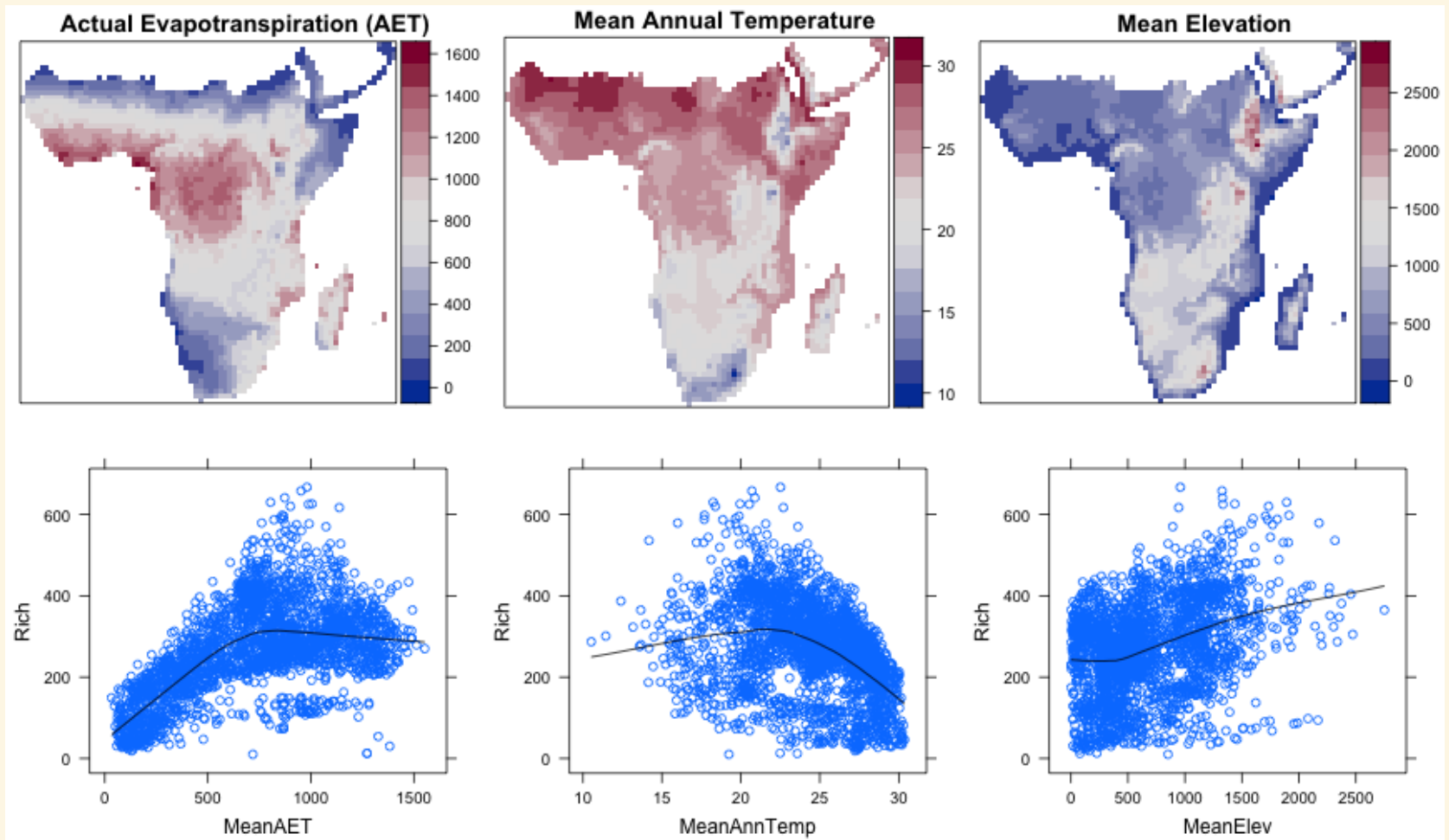
OVERVIEW

- Example data: Afrotropical bird diversity
- Naive models
- Describing spatial autocorrelation
- Accounting for spatial autocorrelation

AFROTROPICAL BIRD SPECIES RICHNESS



EXPLANATORY VARIABLES



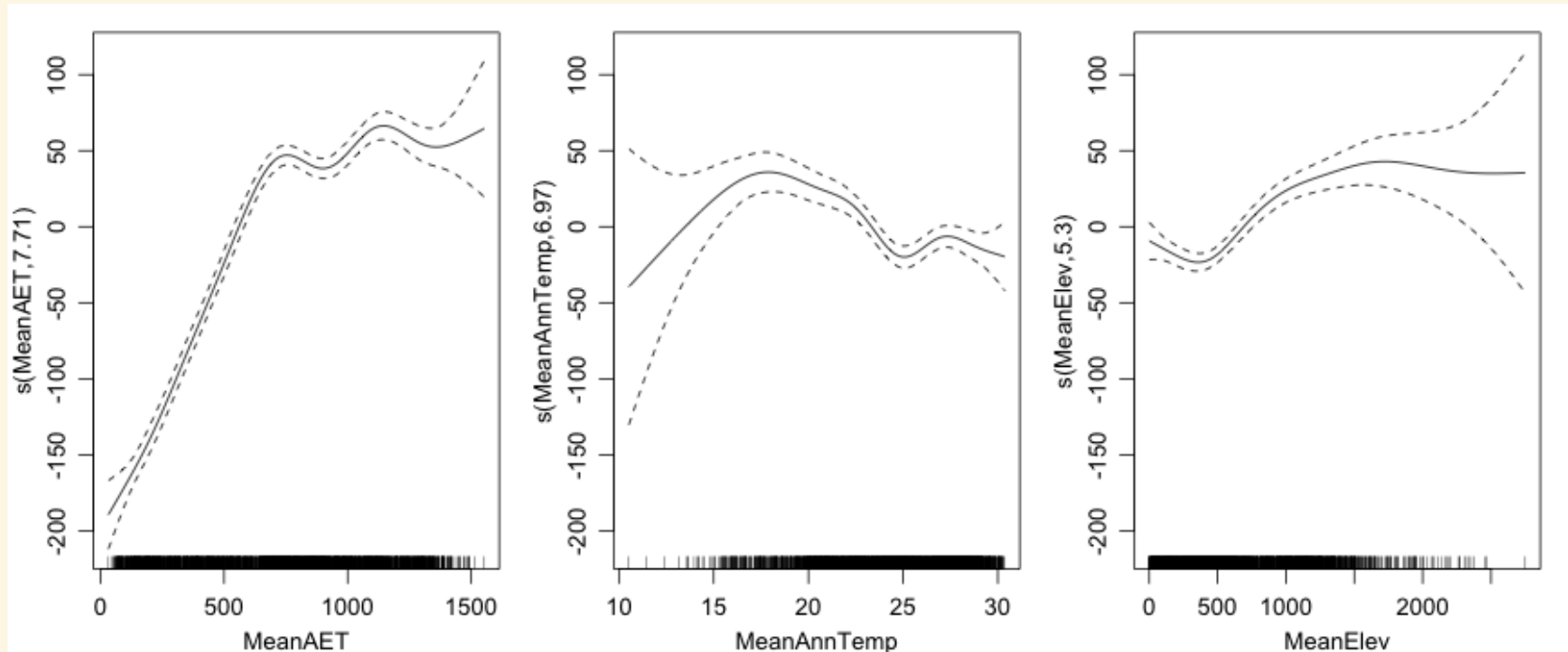
A SIMPLE LINEAR MODEL

Richness ~ AET + Temperature + Elevation

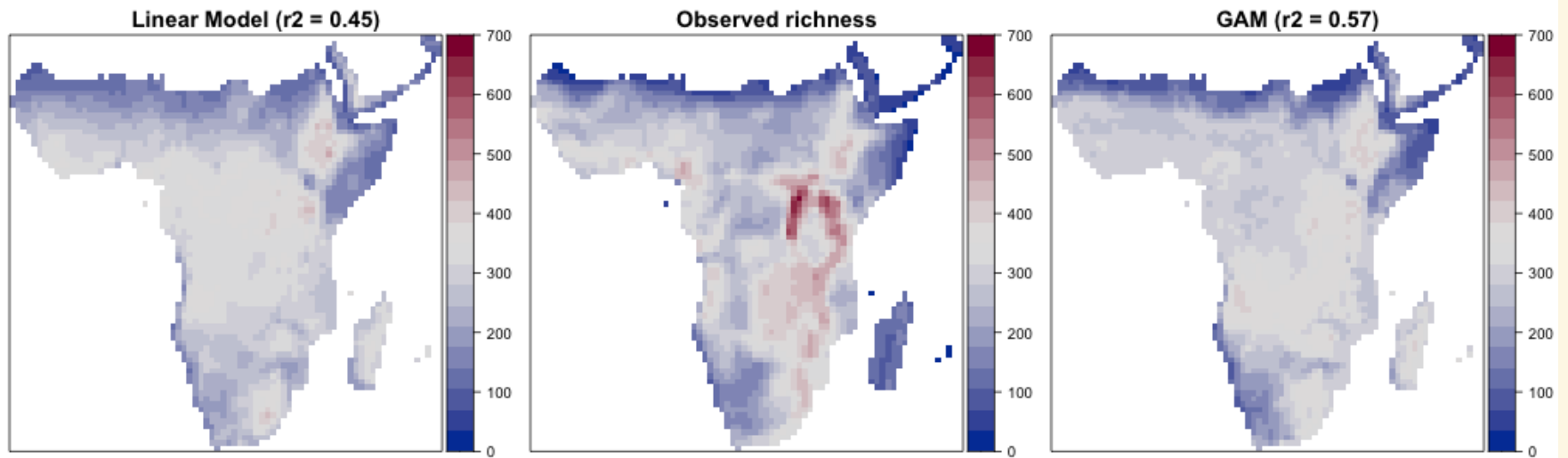
	Est	SE	t	p
(Intercept)	189.45	21.33	8.88	< 0.001
MeanAET	0.18	0.00	37.34	< 0.001
MeanAnnTemp	-4.18	0.72	-5.79	< 0.001
MeanElev	0.08	0.01	13.85	< 0.001

A SIMPLE GAM

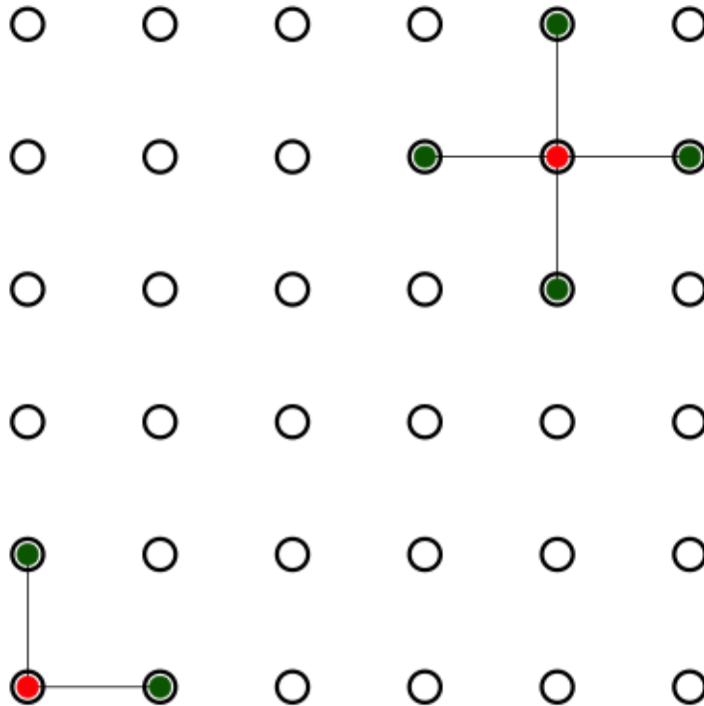
Richness $\sim s(\text{AET}) + s(\text{Temperature}) + s(\text{Elevation})$



MODEL PREDICTIONS



NEIGHBOURHOODS

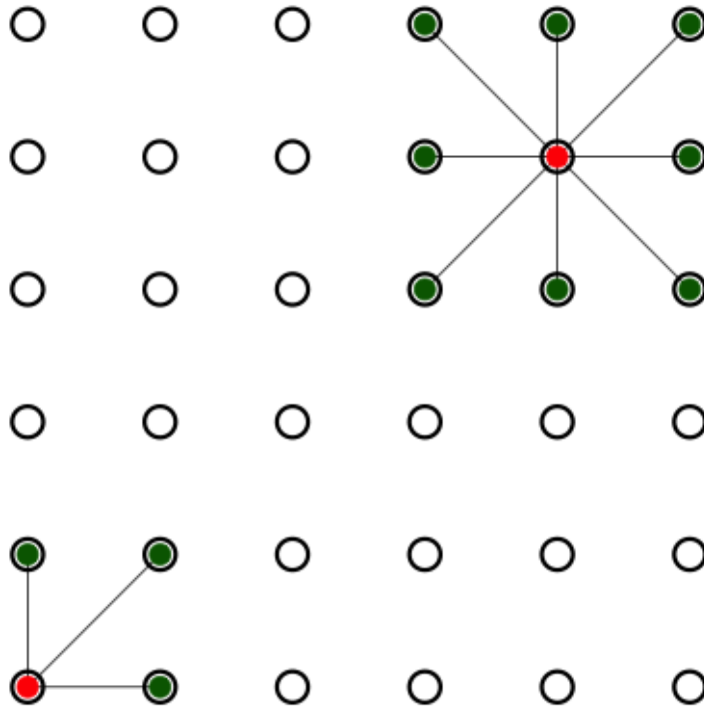


Rooks move

All cells within
one step:

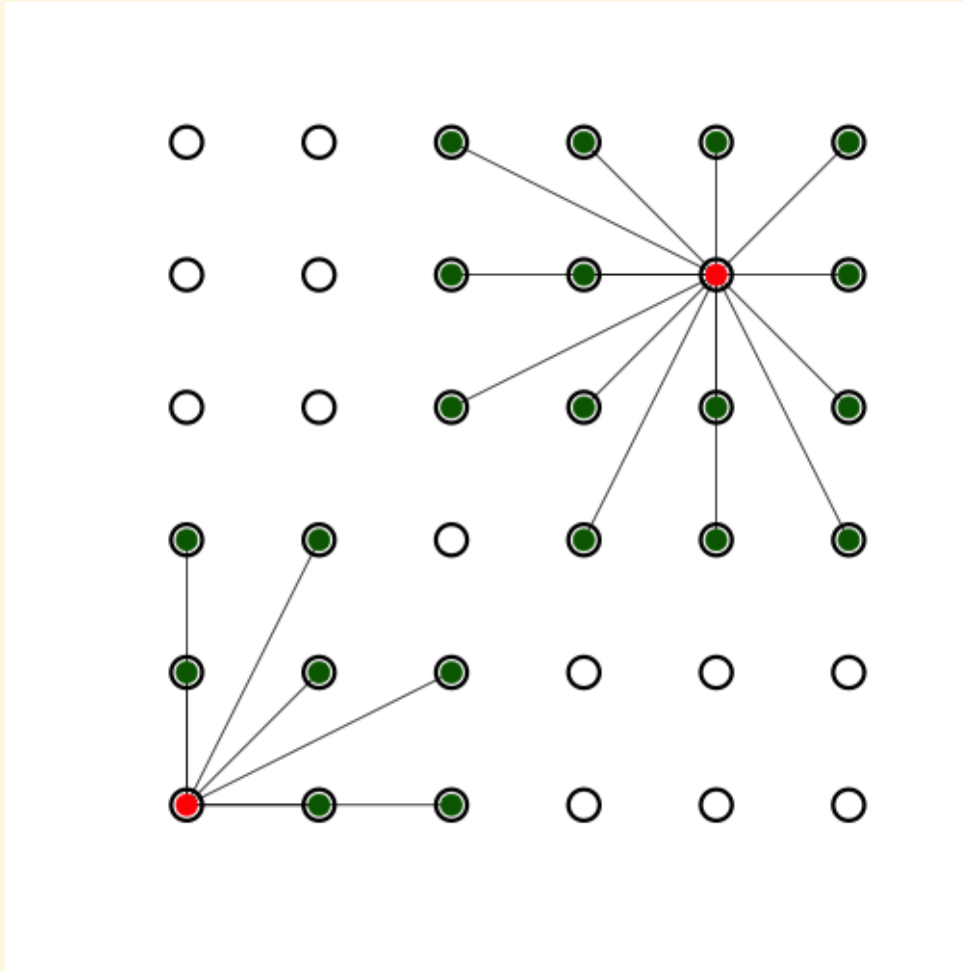
- vertically or
- horizontally

NEIGHBOURHOODS



- Queens move
- All cells within one step:
- vertically,
 - horizontally
 - or
 - diagonally

NEIGHBOURHOODS

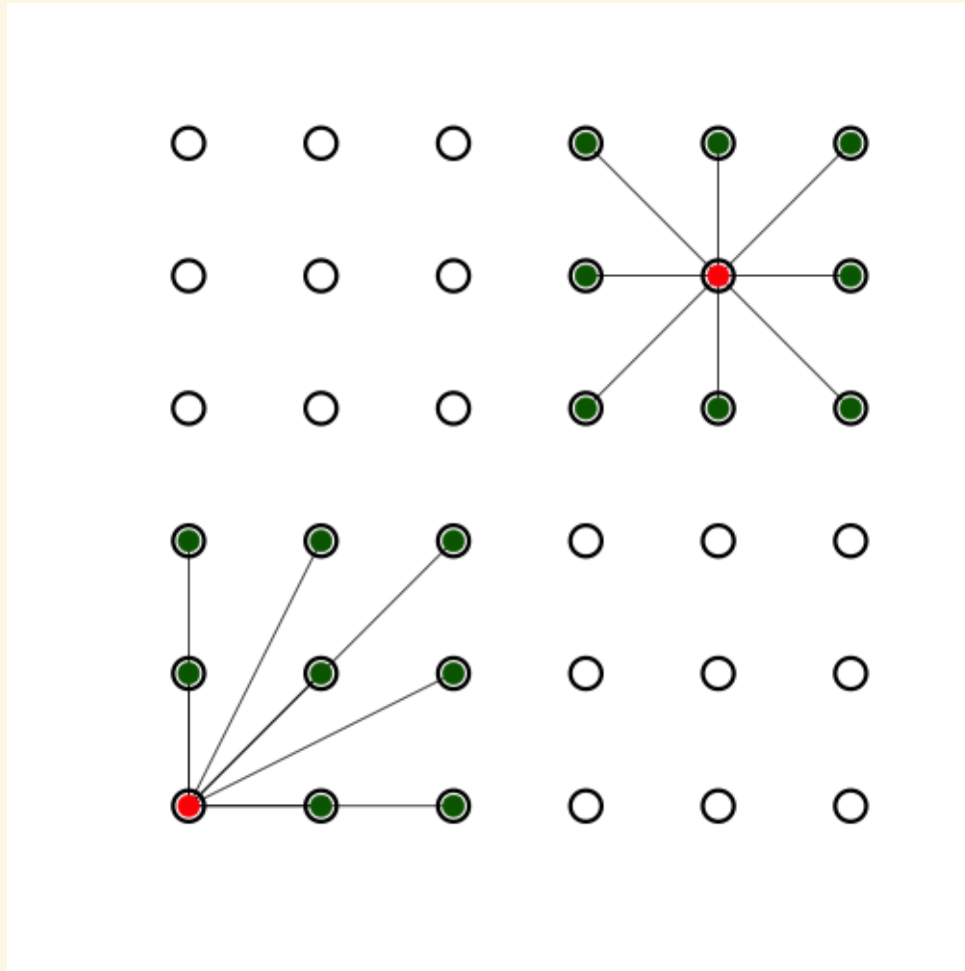


Distance based

All cells within:

- 2.4 units

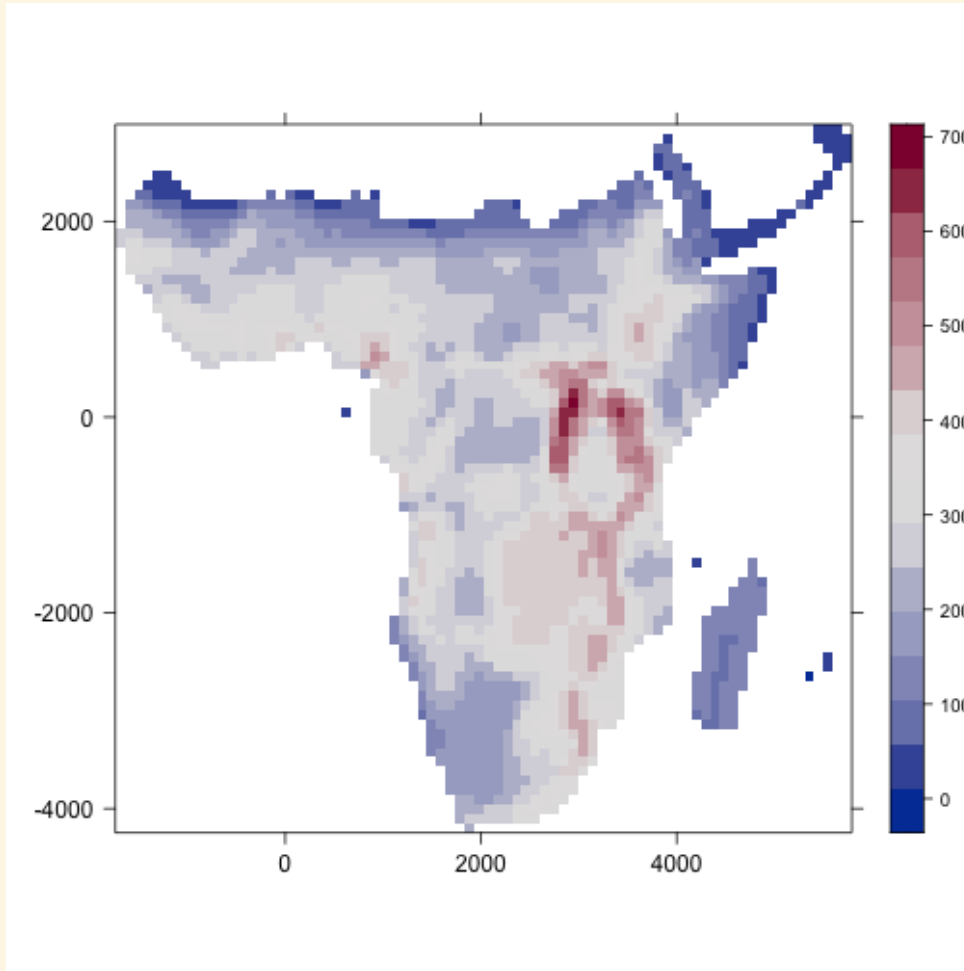
NEIGHBOURHOODS



k nearest

The closest k cells

SPATIAL AUTOCORRELATION



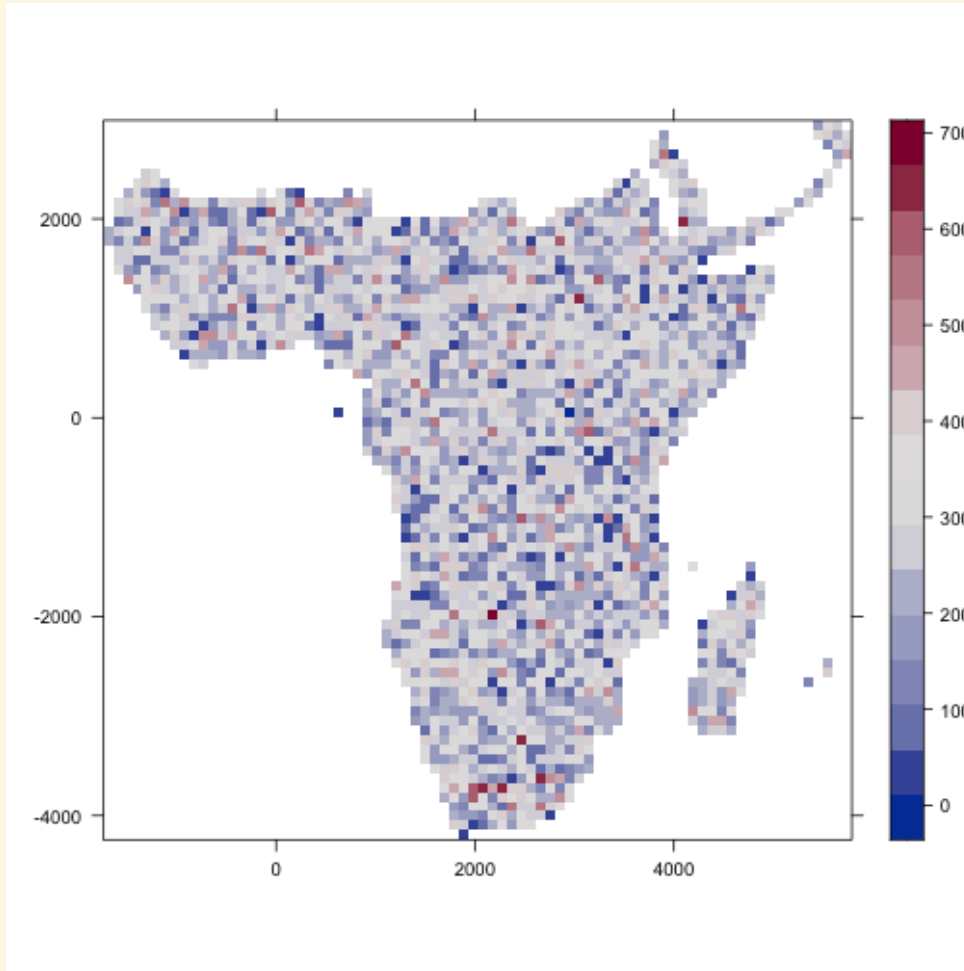
Global Moran's I

- $I = 0.922$
- $p < < 0.001$

Global Geary's C

- $C = 0.070$
- $p < < 0.001$

SPATIAL AUTOCORRELATION



Global Moran's I

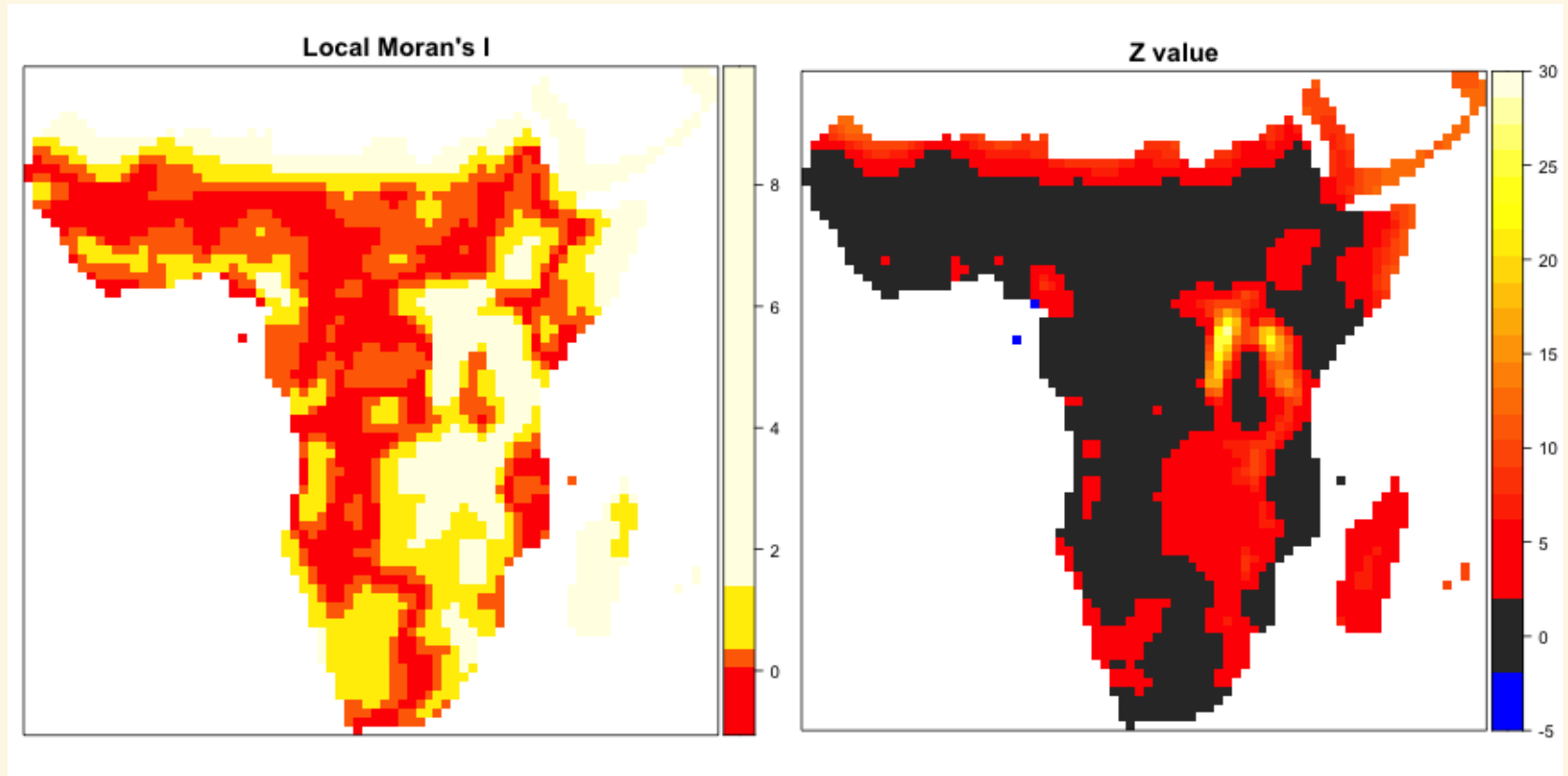
- $I = 0.008$
- $p = 0.211$

Global Geary's C

- $C = 0.994$
- $p = 0.262$

LOCAL AUTOCORRELATION

Local indicators of spatial autocorrelation (LISA)



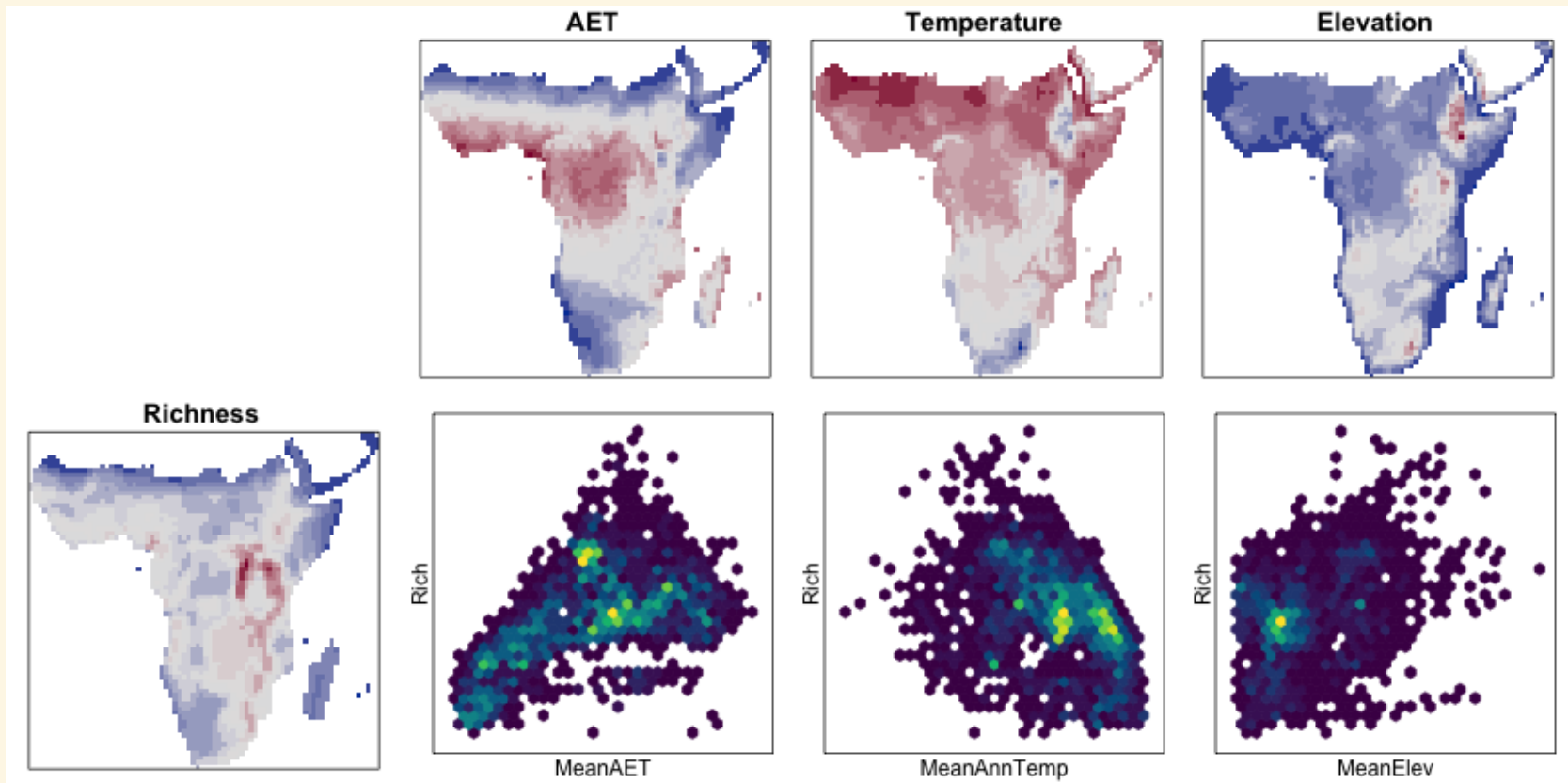
EFFECTS OF SPATIAL AUTOCORRELATION

- Data points not independent
- Degrees of freedom reduced:
 - standard errors and significance testing affected
- Not equally weighted :
 - parameter estimation affected

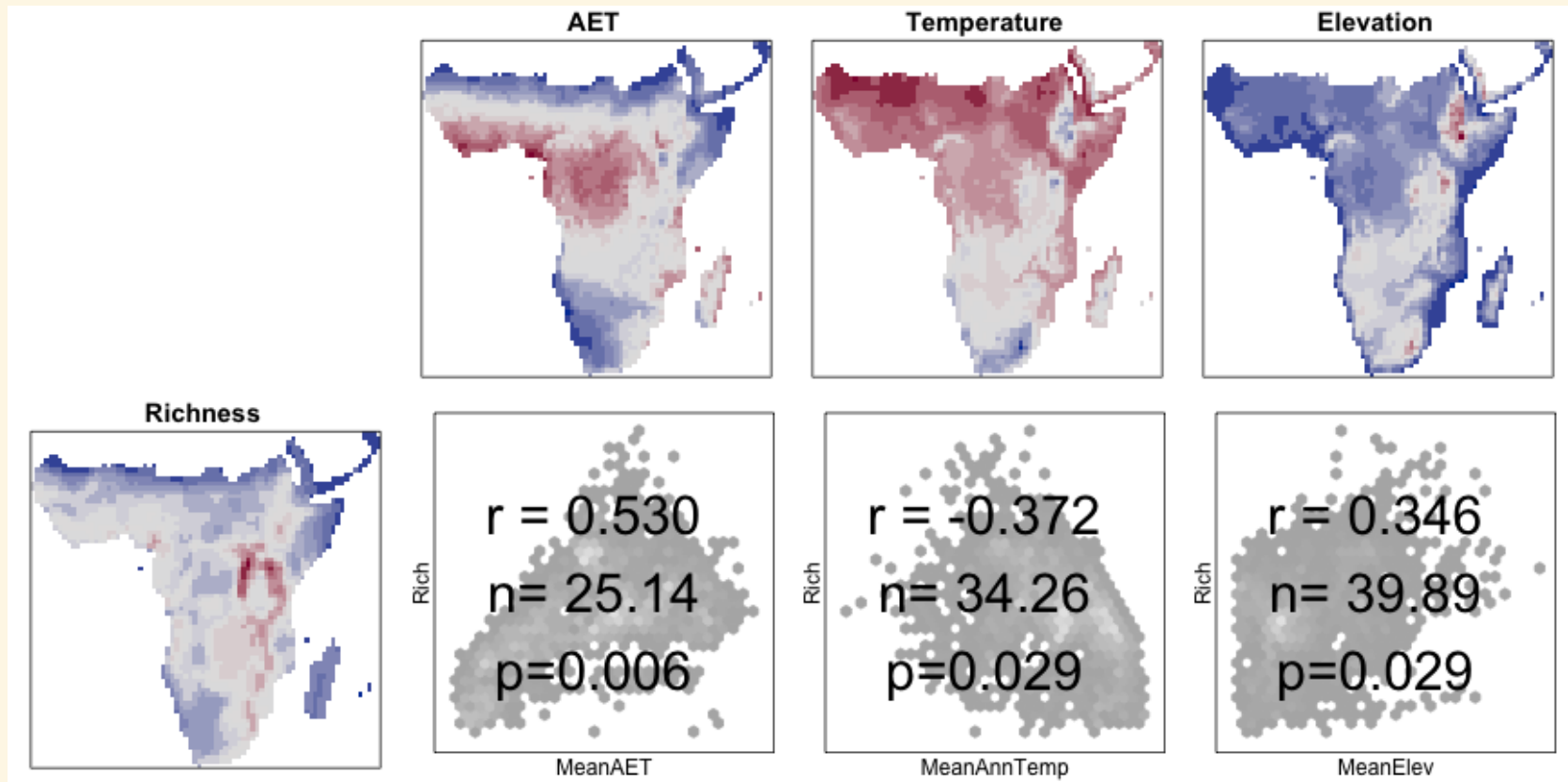
DEALING WITH SPATIAL AUTOCORRELATION

- Modify the degrees of freedom in significance testing
- Account for autocorrelation in models:
 - Simultaneous autoregressive models
 - Generalised least squares
 - Eigenvector filtering
 - Geographically weighted regression

DEGREES OF FREEDOM CORRECTION



DEGREES OF FREEDOM CORRECTION



SPATIAL AUTOREGRESSION

Solve for b :



$$bx_1 + \frac{1}{2}bx_2$$



$$\frac{1}{2}bx_1 + bx_2 + \frac{1}{2}bx_3$$



$$\frac{1}{2}bx_2 + bx_3 + \frac{1}{2}bx_4$$



$$\frac{1}{2}bx_3 + \frac{1}{2}bx_4$$

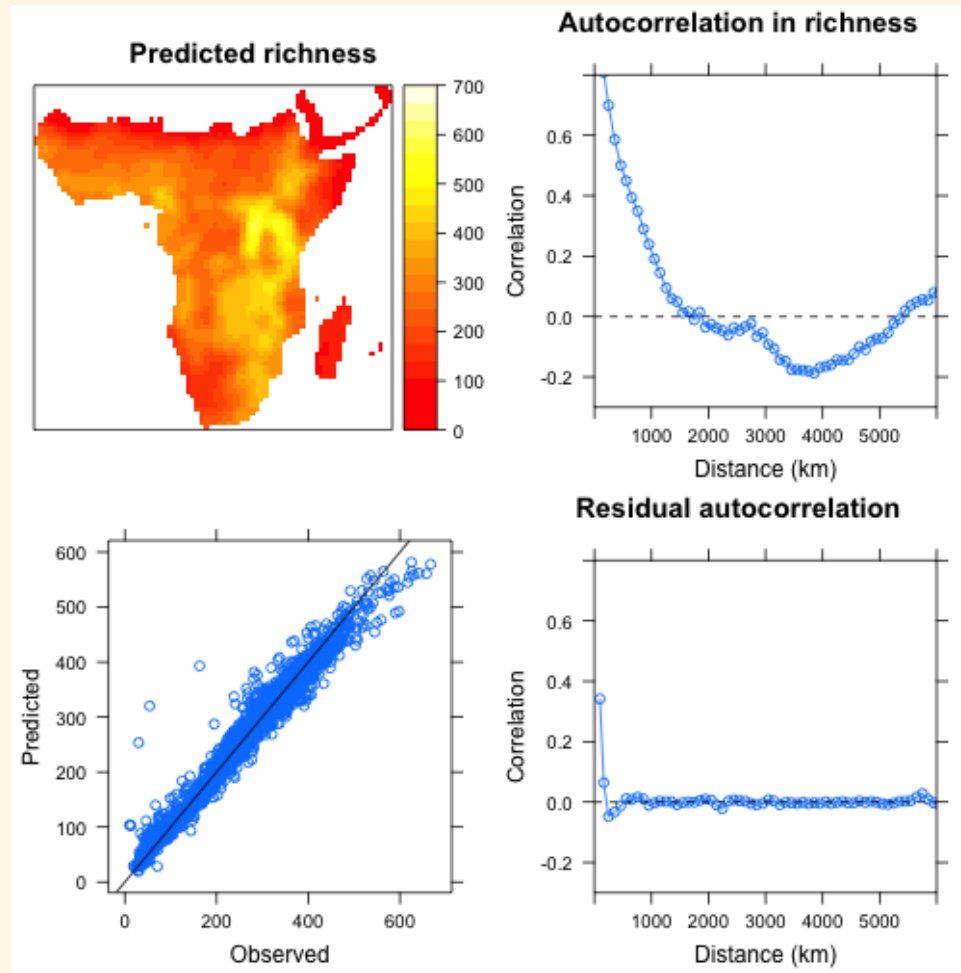
x_1

x_1

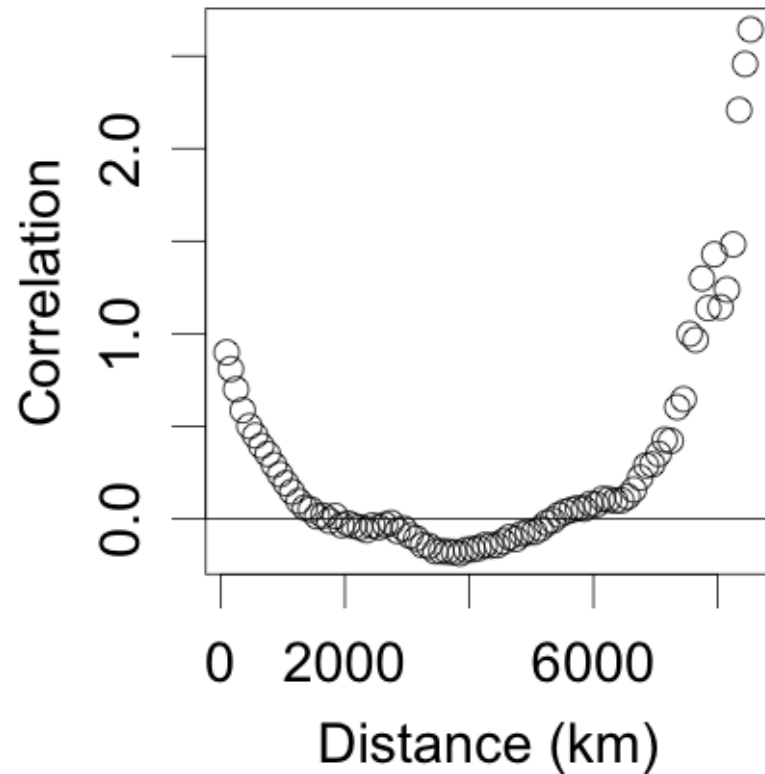
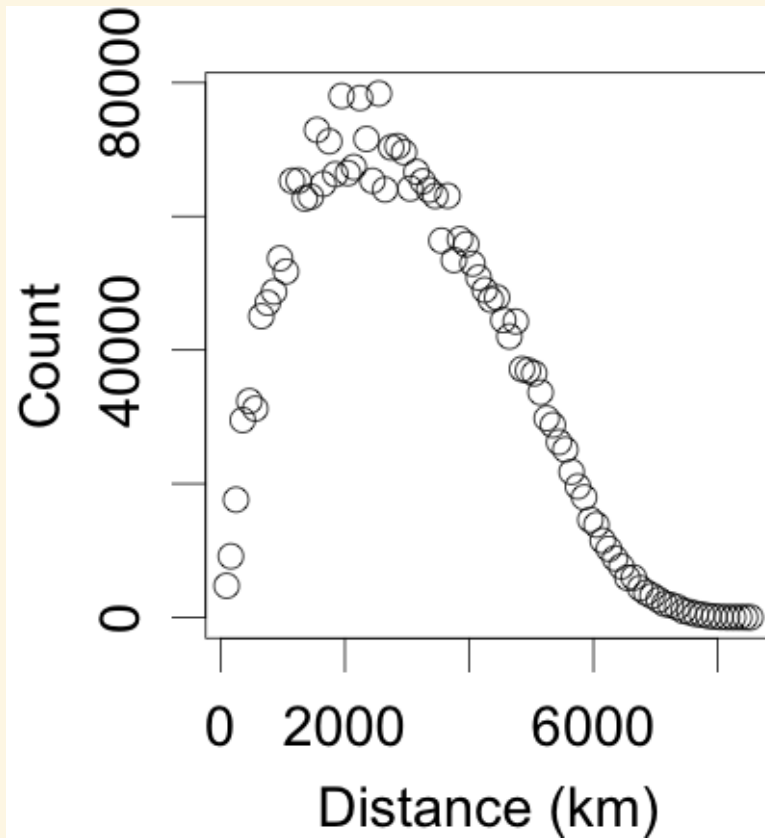
x_3

x_4

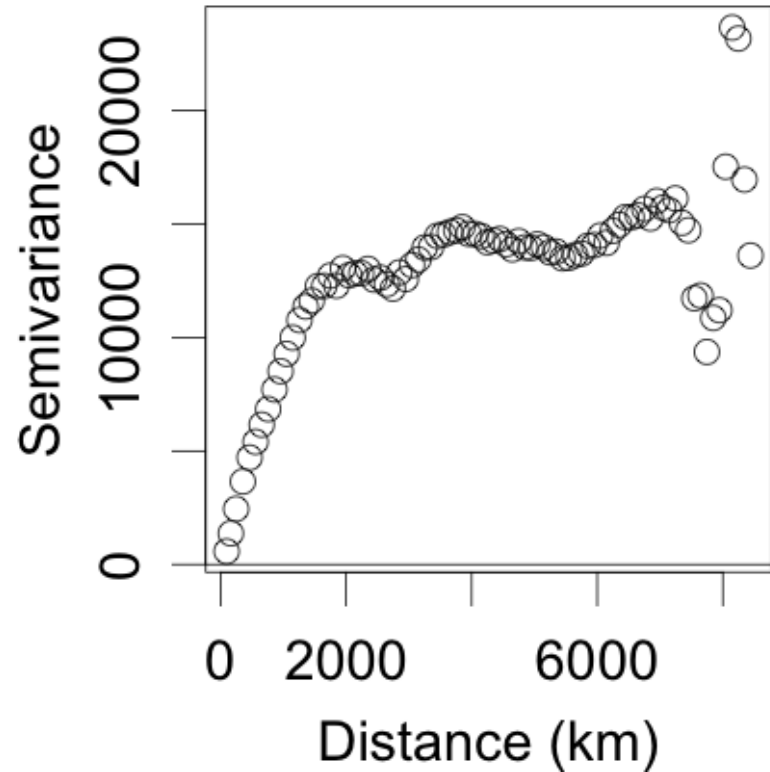
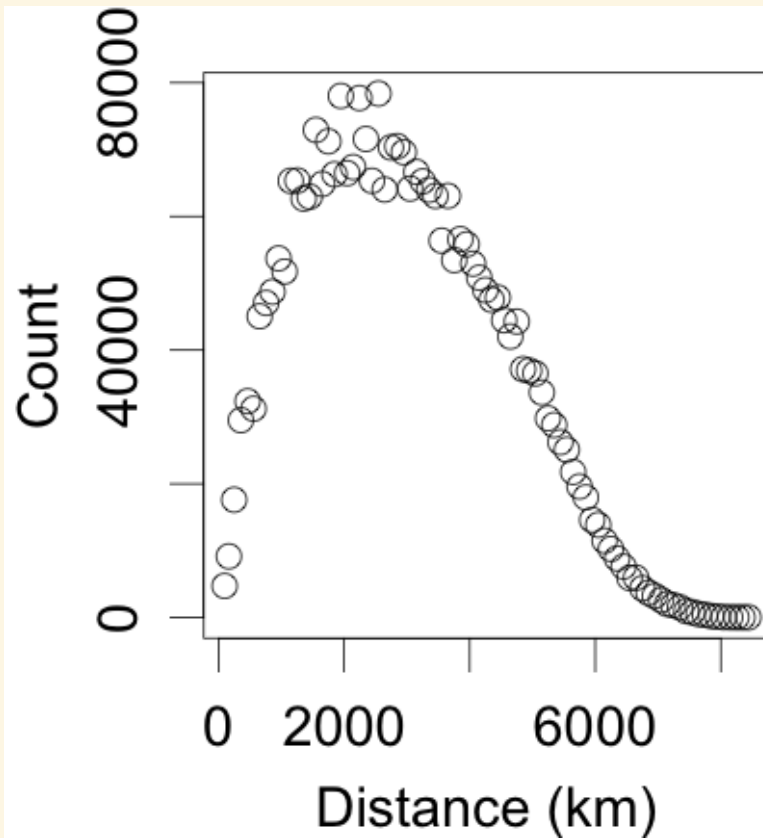
SPATIAL AUTOREGRESSION



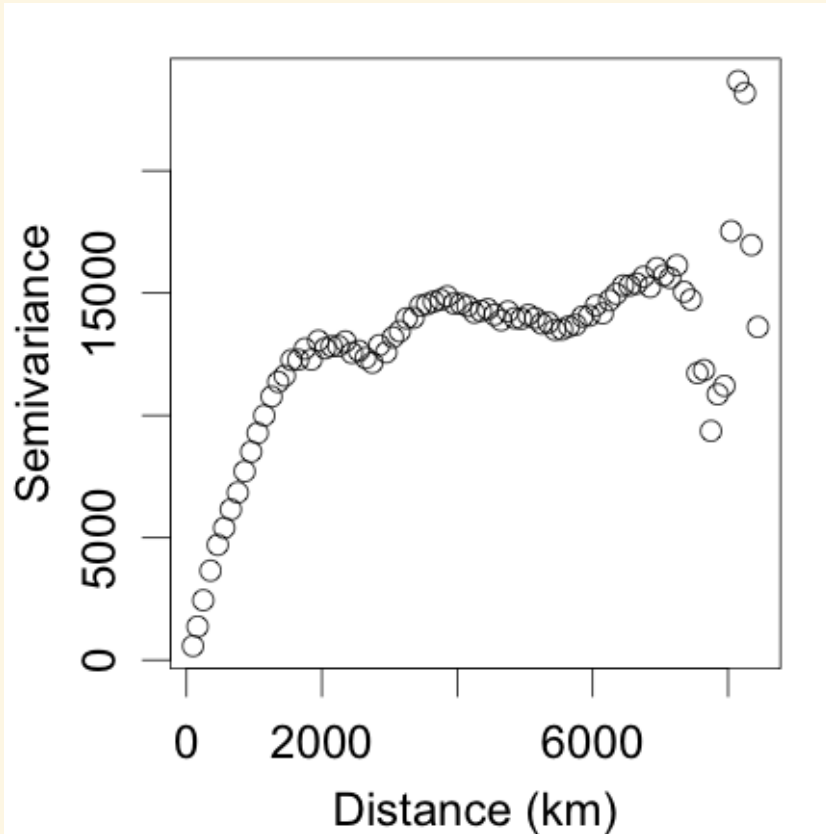
CORRELOGRAM



VARIOGRAM

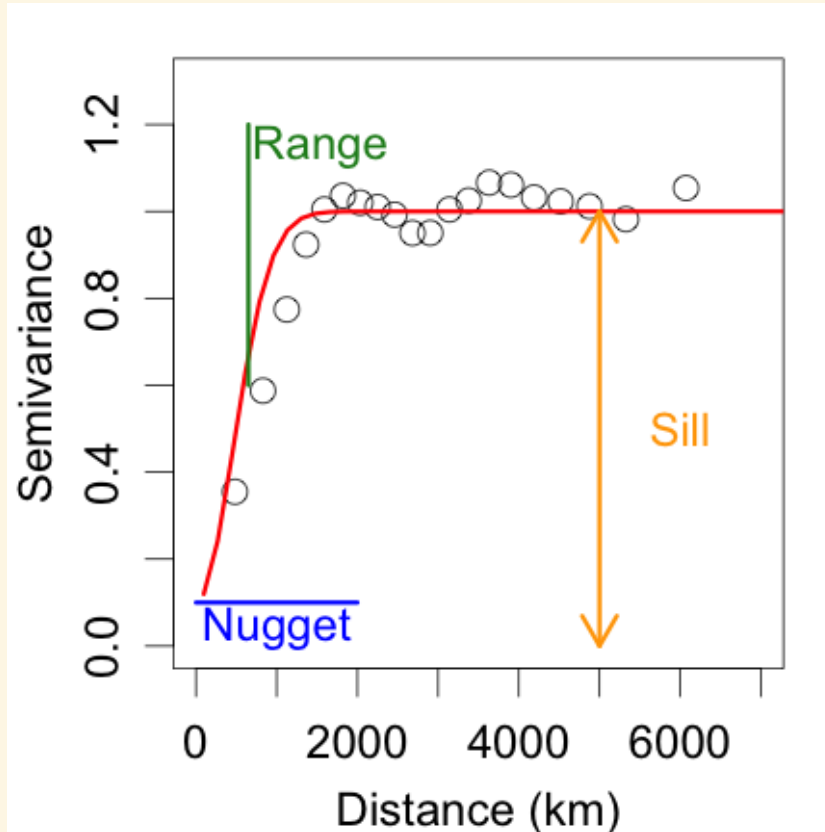


GENERALISED LEAST SQUARES



- Model correlation as a function of **distance**
- Generate a correlation **matrix**

GENERALISED LEAST SQUARES



- Different shapes:
 - Exponential
 - Spherical
 - Linear
- Parameters

GENERALISED LEAST SQUARES

```
Generalized least squares fit by REML
Model: Rich ~ MeanAETScaled + MeanAnnTempScaled + MeanElevScaled
Data: figDat
      AIC      BIC    logLik
24676.89 24705.97 -12333.44

Correlation Structure: Gaussian spatial correlation
Formula: ~e_centre_behr + n_centre_behr
Parameter estimate(s):
range nugget
650.0    0.1

Coefficients:
              Value Std.Error   t-value p-value
(Intercept)  199.67323 16.755430 11.916927  0.0000
MeanAETScaled  17.65050  3.038337  5.809265  0.0000
MeanAnnTempScaled -27.53775  5.663121 -4.862645  0.0000
MeanElevScaled   3.59893  4.321932  0.832712  0.4051

Correlation:
              (Intr) MnAETS MnAnTS
MeanAETScaled  0.048
MeanAnnTempScaled 0.141  0.047
MeanElevScaled  0.156  0.079  0.936

Standardized residuals:
      Min      Q1      Med      Q3      Max
-2.35080108  0.09376345  0.73813223  1.30659392  4.48588628

Residual standard error: 97.85917
Degrees of freedom: 2484 total; 2480 residual
```

STATIONARITY AND ISOTROPY

Is the same process happening in:

- different locations (stationarity)?
- different directions (isotropy)?

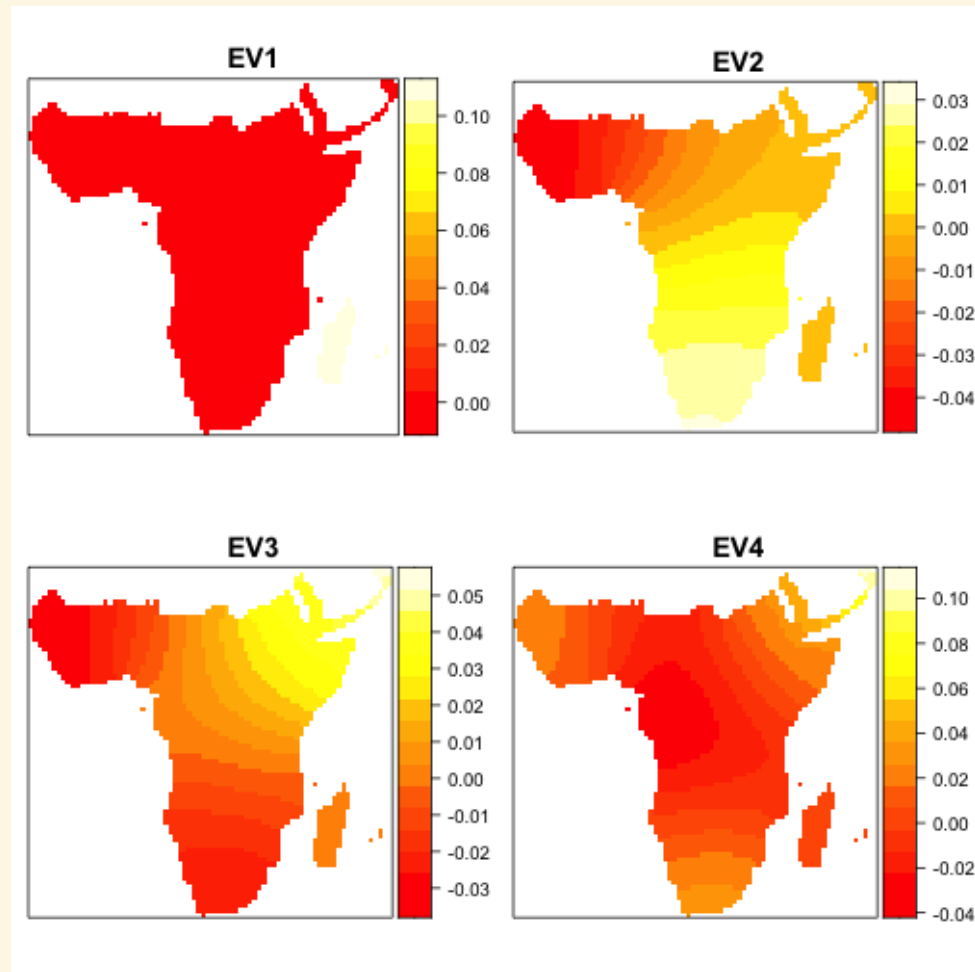
Is the problem in:

- the spatial structure of autocorrelation?
- differences in the actual relationship?

EIGENVECTOR FILTERING

- Take the **eigendecomposition** of a spatial weights model
- Use the **eigenvectors** as variables in the model
- Use a selection process to identify and include only important eigenvectors

EIGENVECTOR FILTERING



EIGENVECTOR FILTERING

lm(Rich ~ MeanAET + MeanAnnTemp + MeanElev

	Est	SE	t	p
(Intercept)	189.45	21.33	8.88	< 0.001
MeanAET	0.18	0.00	37.34	< 0.001
MeanAnnTemp	-4.18	0.72	-5.79	< 0.001
MeanElev	0.08	0.01	13.85	< 0.001

EIGENVECTOR FILTERING

lm(Rich ~ MeanAET + MeanAnnTemp +
MeanElev + Re(spEV1) + Re(spEV2) + Re(spEV3)
+ Re(spEV4))

	Est	SE	t	p
(Intercept)	80.23	33.00	2.43	1.5e-02
MeanAET	0.18	0.01	31.43	< 0.001
MeanAnnTemp	0.10	1.14	0.09	9.3e-01
MeanElev	0.08	0.01	12.70	< 0.001
Re(spEV1)	-1617.63	77.64	-20.83	< 0.001
Re(spEV2)	963.97	129.21	7.46	< 0.001
Re(spEV3)	-813.56	95.87	-8.49	< 0.001
Re(spEV4)	-150.38	100.28	-1.50	1.3e-01

EIGENVECTOR FILTERING

lm(Rich ~ MeanAET + MeanAnnTemp +
MeanElev + Re(spEV1) + Re(spEV2) + Re(spEV3))

	Est	SE	t	p
(Intercept)	58.39	29.62	1.97	4.9e-02
MeanAET	0.19	0.00	43.68	< 0.001
MeanAnnTemp	0.75	1.06	0.71	4.8e-01
MeanElev	0.08	0.01	13.78	< 0.001
Re(spEV1)	-1610.75	77.53	-20.78	< 0.001
Re(spEV2)	1031.60	121.11	8.52	< 0.001
Re(spEV3)	-848.19	93.07	-9.11	< 0.001

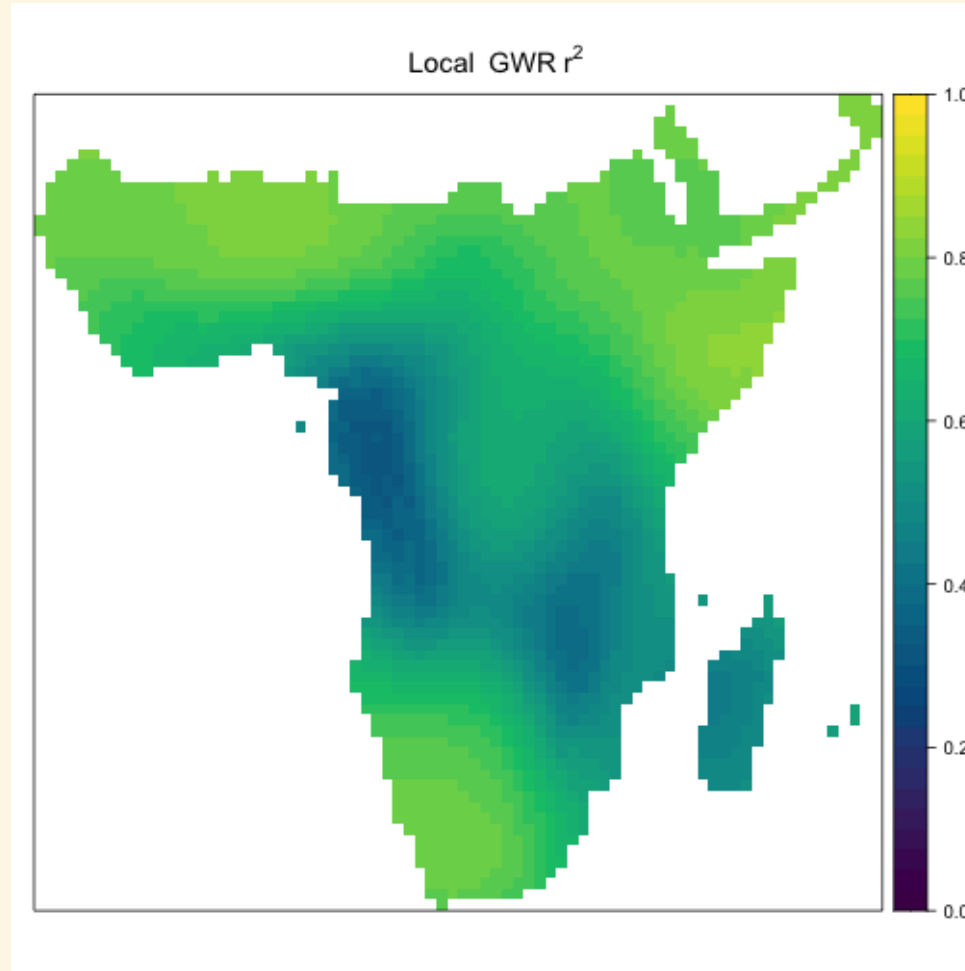
GEOGRAPHICALLY WEIGHTED REGRESSION

Fit a model for **every cell**:

- Define a local **region size** and a **weighting function**
- Fit a weighted regression for each cell using the weights
- Look at how coefficients **vary in space**
- Possibly serious statistical issues!

GEOGRAPHICALLY WEIGHTED REGRESSION

GEOGRAPHICALLY WEIGHTED REGRESSION



PROBLEMS

- Profusion of packages: sf, sp, spdep, mgcv, ncf, gstat, nlme, spgwr
- Different data structures
- Sometimes poor documentation
- Speed of calculation (= size of dataset)
- Memory hungry
- Too many options