

# Introduction to Computers Lab

## First Year (2017 – 2018)



Lab 6

# Complement Number system

- ✧ The word complement in the number system means the difference of the number from the highest number of that digit.
- ✧ This definition can be applied to various number systems and they are named differently as well. But in general, if a number has base of  $N$  then that is known as  $(N-1)$ 's complement. However, if we add one with that value that will give us  $N$ 's complement.

# Numeric complements (Decimal)

∞ Complements is the another part of number that complete it to  $10^n$  OR  $10^n - 1$

∞ 9's complements

○ if we want to find out the 9's complement of a number x, we can do it by following the following formula,

○ , where n = number of digits in  $9's \text{ complement of a value } x = (10^n - 1) - x$

○ **Ex :**

•  $25 \rightarrow 10^2 - 1 - 25 = 100 - 1 - 25 = 74$

# Numeric complements (Decimal)

∞ Complements is the another part of number that complete it to  $10^n$  OR  $10^n - 1$

∞ 10's complements

- it is easy to find out the 10's complement after finding out the 9's complement of that number.
- We have to add 1 with the 9's complement of any number to obtain the desired 10's complement of that number.
- Or if we want to find out the 10's complement directly, we can do it by following the following formula,

$$\text{10's complement of a value } x = 10^n - x$$

- where  $n$  = number of digits in the number.
- **Ex :**
  - $25 \rightarrow 10^2 - 25 = 100 - 25 = 75$

# Numeric complements (Binary)

∞ Complements is the another part of number that complete it to  $2^n$  OR  $2^n - 1$

∞ 1's complements

- if we want to find out the 1's complement ,we can do it by following the following formula,

$$\text{1's complement of a value } x = (2^n - 1) - x$$

- ,where  $n$  = number of bits in the number.

○ **Ex :**

- $1001 \rightarrow 2^4 - 1 - 1001 = 10000 - 1 - 1001 = 0110$



# Numeric complements (Binary)

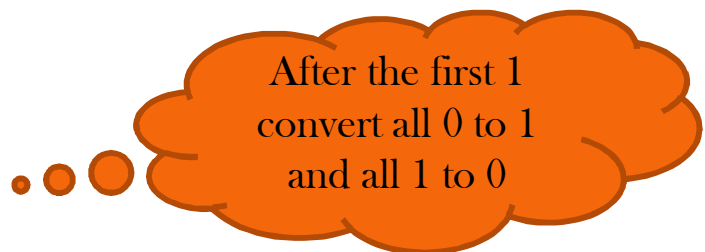
∞ Complements is the another part of number that complete it to  $2^n$  OR  $2^n - 1$

∞ 2's complements

- it is easy to find out the 2's complement after finding out the 1's complement of that number.
- We have to add 1 to the 1's complement of any number to obtain the desired 2's complement of that number.
- Or if we want to find out the 2's complement directly, we can do it by following the following formula,

$$2's \text{ complement of a value } x = (2^n) - x$$

- where  $n$  = number of bits in the number.
- **Ex :**
  - $1001 \rightarrow 2^4 - 1001 = 10000 - 1001 = 0111$



After the first 1  
convert all 0 to 1  
and all 1 to 0

# Arithmetic Operations in binary system

- Arithmetic operations can be performed in all numbering systems
- Arithmetic operations include:
  - ❖ Addition
  - ❖ Subtraction

# Addition in binary

∞ Rule:

$$0 + 0 = 0$$

$$0 + 1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 0 \text{ (carry 1)}$$

$$1 + 1 + 1 = 1 \text{ (carry 1)}$$

∞ EX:

○  $101 + 101 = ?$

∞  $1 + 11 = ???$

∞  $1010 + 11 = ???$



$$\begin{array}{r} \text{1} \quad \text{carry} \\ 101 \\ + \\ 101 \\ \hline 1010 \end{array}$$



# Subtraction (use 2's complement)

∞ Rule:

1. The size of two number must be the same.
2. The first number don't change.
3. Get the 2's complement of the second number.
4. Add the new 2 numbers.
5. If the number of digits for result > the number of digits for 2 numbers (carry)
  - Neglect the carry and the result is +ve.
6. If the number of digits for result = the number of digits for 2 numbers (no carry)
  - Get the 2's complement for the result and the result is -ve.

∞ EX1: 101 - 1001

$$\begin{array}{r} 0101 \\ - 1001 \\ \hline \end{array} \quad \begin{array}{c} \text{↘} \\ \text{↙} \end{array} \quad \begin{array}{r} 0101 \\ + 0111 \\ \hline \end{array} = 1100 \quad \begin{array}{l} \text{No carry ; So result is} \\ - 0100 \end{array}$$

∞ EX2: 1001 - 101

$$\begin{array}{r} 1001 \\ - 0101 \\ \hline \end{array} \quad \begin{array}{c} \text{↘} \\ \text{↙} \end{array} \quad \begin{array}{r} 1001 \\ + 1011 \\ \hline \end{array} = 10100 \quad \begin{array}{l} \text{carry ; So result is} \\ + 0100 \end{array}$$

# Solve

- Addition

$$101 + 1110 = ?$$

$$10110 + 100 = ?$$

$$101 + 101 = ?$$

- Subtraction

$$101 - 1100 = ?$$

$$1011 - 100 = ?$$

$$101 - 101 = ?$$

# Hexadecimal Addition

1. Add one column at a time.
2. Convert to decimal and add the numbers.
3. If the result of step two is 16 or larger subtract the result from 16 and carry 1 to the next column.
4. If the result of step two is less than 16, convert the number to hexadecimal.

# Hexadecimal Addition(cont.)

∞ Example:

$$\begin{array}{rcccc} & & & & \text{Carry} \\ & & & & \longleftarrow \\ 1 & 0 & 0 & 1 & \\ & 8 & A & 5 & C \\ & F & 3 & 9 & A \\ \hline 1 & 7 & D & F & 6 \end{array}$$

# Solve

## ∞ Exercises:

1.  $82CD + 1982$
2.  $E2C + A31$



# Thank You