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1 Basic

1.1 .vimrc

```

1 filetype indent on
2 syntax enable
3 set nu
4 set cursorline
5 set ts=2 sts=2 sw=2 et ai
6 set mouse=a
7 set wrap
8 set showcmd
9 set backspace=indent,eol,start
10
11 inoremap ( (<ESC>i
12 inoremap [ [<ESC>i
13 inoremap {<CR> {<CR><ESC>ko

```

2 Dynamic Programming

2.1 0/1 Knapsack_problems

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 int f[1000]={0};
4 int n=0, m=0;
5 int main(){
6     cin >> n >> m;

```

```

7     for (int i = 1; i <= n; i++){
8         int price = 0, value = 0;
9         cin >> price >> value;
10        for (int j = m; j >= price; j--){
11            if (f[j-price]+value>f[j]){
12                f[j]=f[j-price]+value;
13            }
14        }
15    }
16    cout << f[m] << endl;
17    return 0;
18 }

```

2.2 Complete_Knapsack_problems

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 int f[1000]={0};
4 int n=0, m=0;
5 int main(){
6     cin >> n >> m;
7     for (int i=1; i<=n; i++){
8         int price=0, value=0;
9         cin >> price >> value;
10        for (int j=price; j<=m; j++){
11            if (f[j-price]+value>f[j]){
12                f[j]=f[j-price]+value;
13            }
14        }
15    }
16    cout << f[m] << endl;
17    return 0;
18 }

```

2.3 Longest Common Subsequence(LCS)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3
4 int dp[1001][1001];
5 int lcs(const string &s, const string &t){
6     int m = s.size(), n = t.size();
7     if (m == 0 || n == 0){
8         return 0;
9     }
10    for(int i = 0; i <= m; ++i){
11        dp[i][0] = 0;
12    }
13    for(int j = 1; j <= n; ++j){
14        dp[0][j] = 0;
15    }
16    for(int i = 0; i < m; ++i){
17        for (int j = 0; j < n; ++j){
18            if(s[i] == t[j]){
19                dp[i+1][j+1] = dp[i][j]+1;
20            }else{
21                dp[i+1][j+1] = max(dp[i+1][j],
22                                   dp[i][j+1]);
23            }
24        }
25    }
26    return dp[m][n];
27 }

```

2.4 Longest increasing common sequence(LICS)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 int a[100] = {0};
4 int b[100] = {0};

```

```

5 int f[100] = {0};
6 int n = 0, m = 0;
7 int main(){
8     cin >> n;
9     for(int i = 1; i <= n; i++){
10         cin >> a[i];
11     }
12     cin >> m;
13     for(int i = 1; i <= m; i++){
14         cin >> b[i];
15     }
16     for(int i = 1; i <= n; i++){
17         int k = 0;
18         for (int j = 1; j <= m; j++){
19             if(a[i] > b[j] && f[j] > k){
20                 k = f[j];
21             }else if(a[i] == b[j] && k + 1 > f[j]){
22                 f[j] = k + 1;
23             }
24         }
25     }
26     int ans = 0;
27     for(int i = 1; i <= m; i++){
28         if(f[i] > ans){
29             ans = f[i];
30         }
31     }
32     cout << ans << endl;
33     return 0;
34 }

```

2.5 Longest Increasing Subsequence(LIS)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 int n=0;
4 int a[100]={0}, f[100]={0}, x[100]={0};
5 int main(){
6     cin >> n;
7     for(int i = 1; i <= n; i++){
8         cin >> a[i];
9         x[i] = INT_MAX;
10    }
11    f[0]=0;
12    int ans=0;
13    for(int i = 1; i <= n; i++){
14        int l = 0, r = i;
15        while (l+1<r){
16            int m=(l+r)/2;
17            if (x[m]<a[i]){
18                l=m;
19            }else{
20                r=m;
21            }
22            // change to x[m]<=a[i] for
            // non-decreasing case
23        }
24        f[i]=l+1;
25        x[l+1]=a[i];
26        if(f[i]>ans){
27            ans=f[i];
28        }
29    }
30    cout << ans << endl;
31    return 0;
32 }

```

2.6 Longest Palindromic Subsequence(LPS)

```

1 int LPS(vector<vector<int>>& dp, string& s, int l,
2         int r){
3     if(~dp[l][r]) return dp[l][r];
4     if(l == r) return dp[l][r] = 1;

```

```

4     if(l > r) return dp[l][r] = 0;
5     if(s[l] == s[r]) return dp[l][r] = LPS(dp, s,
6         l+1, r-1) + 2;
7     return dp[l][r] = max(LPS(dp, s, l + 1, r),
8         LPS(dp, s, l, r - 1));
9 }

```

3 Graph Theory

3.1 Lowest Common Ancestor(LCA)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 const int LOG = 20;
4 int par[N][LOG];
5 int tin[N], tout[N];
6 int timer = 0;
7 void dfs(int v, int p){
8     tin[v] = ++timer;
9     par[v][0] = p;
10    for (int it : G[v]){
11        if (it != p){
12            dfs(it, v);
13        }
14    }
15    tout[v] = ++timer;
16 }
17 void Doubling(){
18     for (int i = 1; i < N; ++i){
19         for (int j = 1; j < LOG; ++j){
20             par[i][j] = par[par[i][j-1]][j-1];
21         }
22     }
23 }
24 bool anc(int v, int u){
25     return tin[v] <= tin[u] && tout[u] <= tout[v];
26 }
27 int LCA(int v, int u){
28     if (anc(v, u)){
29         return v;
30     }
31     for (int j = LOG - 1; j >= 0; --j){
32         if (!anc(par[v][j], u)){
33             v = par[v][j];
34         }
35     }
36     return par[v][0];
37 }

```

3.2 bellman-ford

```

1 void bellman(vector<edge>& edges, vector<int>& dist,
2             int n){
3     // n - 1 relax
4     for(int i = 1; i < n; i++){
5         for(edge e : edges){
6             int u = e.start, v = e.end, d = e.dist;
7             if(dist[u] == INF) continue;
8             dist[v] = min(dist[v], d + dist[u]);
9         }
10    }
11    // 偵測負權迴路
12    for(edge e : edges){
13        int u = e.start, v = e.end, d = e.dist;
14        if(dist[u] == INF) continue;
15        if(dist[v] > dist[v] + d){
16            printf("It is contained negative
17                cycle.\n");
18            break;
19        }
20    }

```

3.3 dijkstra

```

1 void dijkstra(ll st){
2     vector<ll> dis(n, INF);
3     //pll (vetrex, distance)
4     priority_queue<pll, vector<pll>, greater<pll>> pq;
5     pq.push({st, 0});
6     dis[st] = 0;
7     while(!pq.empty()){
8         pll now = pq.top();
9         pq.pop();
10        if(now.ss != dis[now.ff]) continue;
11        for(pll i : graph[t.ff]){
12            if(dis[now.ff] + i.ss < dis[i.ff]){
13                dis[i.ff] = now.ss + i.ss;
14                pq.push({i.ff, dis[i.ff]});
15            }
16        }
17    }
18 }

```

```

11 int ans = 0;
12 for (int i = 0; i < m; i ++ ){
13     int a = edge[i].a, b = edge[i].b, c =
        edge[i].c;
14
15     int pa = find(a), pb = find(b); // 找節點 A
        與節點 B 所屬的集合
16
17     if (pa != pb){ // 若為不同集合，就合併
18         p[pb] = pa;
19         cnt ++;
20         ans += c;
21     }
22 }
23
24 if (cnt == n - 1) cout << ans << endl; //
        邊的數量不為 n - 1，則沒有 MST
25 else puts("impossible");
26 }

```

3.4 Topological

```

1 //此處為建立 Adjacency List 和每個節點的入度點數量
2 vector<vector<int>> make(vector<Edge>& nodes, int n){
3     vector<vector<int>> graph(n + 1);
4     vector<int> indegree(n, 0);
5     for(auto node : nodes){
6         graph[node.src].pb(node.des);
7         indegree[node.des] ++; //計算入度點
8     }
9     graph[n] = indegree;
10    return graph;
11 }
12
13 // 拓樸排序
14 vector<int> TopologicalOrder(vector<vector<int>>
    graph){
15     int n = graph.size();
16     queue<int> q;
17     vector<int> result;
18     for(int i=0; i<graph[n - 1].size(); i++){
19         if(!graph[n - 1][i]) q.push(i);
20     }
21     while(!q.empty()){
22         int cnt = q.front();
23         result.pb(cnt);
24         q.pop();
25         for(int i=0; i<graph[cnt].size(); i++){
26             graph[n - 1][graph[cnt][i]]--;
27             if(!graph[n - 1][graph[cnt][i]])
28                 q.push(graph[cnt][i]);
29         }
30     }
31     //偵測循環
32     for(auto i : graph[n-1]) if(i) return {};
33
34     return result;
35 }

```

3.5 kruskal

```

1 struct Edge{
2     int a, b, c;
3 }edge[M];
4
5 int find(int x) {
6     return x == p[x] ? x : p[x] = find(p[x]);
7 }
8
9 // 要先按照邊權重升序
10 void kruskal(){

```

3.6 prime

```

1 // 0(N^2) 類似 dijkstra
2 void prim(){
3     memset(dis, 0x3f, sizeof dis);
4     dis[1] = 0; st[1] = 1; // 抓個初始點
5     int ans = 0; // 記錄邊上權重
6
7     for (int i = 0; i < n; i ++ ){
8         int t = -1;
9         for (int j = 1; j <= n; j ++ ){
10            if (!st[j] && (t == -1 || dis[j] <
                dis[t])) t = j; // 尋找距離最近的節點
11        }
12
13        if (dis[t] == INF) { // 最短距離為
            INF，則不存在 MST
14            puts("impossible");
15            return;
16        }
17
18        ans += dis[t];
19        st[t] = 1; // 將節點加入 MST
20
21        for (int j = 1; j <= n; j ++ ){
22            if (!st[j]){
23                dis[j] = min(dis[j], dis[t] +
                    g[t][j]); // 更新其他節點到 MST
                    的距離
24            }
25        }
26    }
27
28    return ans;
29 }

```

4 Algorithm

4.1 Ternary Search

```

1 int l = -10000;
2 int r = 10000;
3 int iterations = 100;
4 for (int i = 0; i < iterations; i++){
5     double mr = (l + r) / 2.0;
6     double ml = (l + mr) / 2.0;
7     // f( ): 目標函數
8     if (f(ml) < f(mr)) r = mr;
9     else l = ml;
10 }

```

5 Number Theory

5.1 質數篩法 Sieve of Eratosthenes

```

1 bool a[46342];
2 vector<int> v;
3 for (int j = 2; j < 46342; j++){
4     if (!a[j]){
5         v.push_back(j);
6         for (int i = j * j; i < 46342; i += j){
7             a[i] = true;
8         }
9     }
10 }

```

5.2 擴展歐幾里得

```

1 pair<int,int> extgcd(int a, int b){
2     if (b==0) return {1,0};
3     int k = a/b;
4     pair<int,int> p = extgcd(b,a-k*b);
5     return { p.second, p.first - k*p.second };
6 }

```

5.3 快速幂

```

1 constexpr int mod = 1e9 + 7;
2 ll fpow(ll i, int j) {
3     ll ret = 1, tmp = i;
4     for (; j; j >= 1, tmp = tmp * tmp % mod)
5         if (j & 1) ret = ret * tmp % mod;
6     return ret;
7 }

```

5.4 大質數

```

1 97, 101, 131, 487, 593, 877, 1087, 1187, 1487, 1787,
   3187, 12721,
2 13331, 14341, 75577, 123457, 222557, 556679, 999983,
3 1097774749, 1076767633, 100102021, 999997771,
4 1001010013, 1000512343, 987654361, 999991231,
5 999888733, 98789101, 987777733, 999991921, 1000000007,
6 1000000087, 1000000123, 1010101333, 1010102101,
7 100000000039, 100000000000037, 2305843009213693951,
8 4611686018427387847, 9223372036854775783,
9 18446744073709551557

```

6 Data Structure

6.1 Disjoint Set Union-Find

```

1 #include<bits/stdc++.h>
2 using namespace std;
3
4 vector<int> dsu, rk;
5
6 void initDSU(int n){
7     dsu.resize(n);
8     rk.resize(n);
9     for(int i = 0; i < n; i++) dsu[i] = i, rk[i] = 1;
10 }
11
12 int findDSU(int x){
13     if(dsu[x] == x) return x;
14     dsu[x] = findDSU(dsu[x]);
15     return dsu[x];

```

```

16 }
17
18 void unionDSU(int a, int b){
19     int pa = findDSU(a), pb = findDSU(b);
20     if(rk[pa] > rk[pb]) swap(pa, pb);
21     if(rk[pa] == rk[pb]) rk[pb]++;
22     dsu[pa] = pb;
23 }

```

6.2 Segment Tree

```

1 #include <bits/stdc++.h>
2 #define ll long long
3 using namespace std;
4
5 struct segtree {
6
7     vector<ll> sums;
8     ll size;
9
10    // 線段樹初始化
11    void init(ll n){
12        size = 1;
13        while(size < n) size<<1;
14        sums.assign(size<<1, 0LL);
15    }
16
17    // 更新數值
18    void update(ll i, ll v, ll x, ll Lptr, ll Rptr){
19        if(Rptr - Lptr == 1){
20            sums[x] = v;
21            return;
22        }
23        ll m = ( Lptr + Rptr )/2;
24        if(i<m) update(i, v, 2*x+1, Lptr, m);
25        else update(i, v, 2*x+2, m, Rptr);
26        sums[x] = sums[2*x+1] + sums[2*x+2];
27    }
28
29    void update(ll a, ll b){
30        update(a, b, 0, 0, size);
31    }
32
33    // 查詢資訊
34    ll query(ll l, ll r, ll x, ll Lptr, ll Rptr){
35        if( Lptr >= r || Rptr <= l ) return 0;
36        if( Lptr >= l && Rptr <= r ) return sums[x];
37        ll m = (Lptr + Rptr) / 2;
38        ll s1 = query(l, r, 2*x+1, Lptr, m);
39        ll s2 = query(l, r, 2*x+2, m, Rptr);
40        return s1 + s2;
41    }
42
43    ll query(ll a, ll b){
44        return query(a, b, 0, 0, size);
45    }
46 };

```

6.3 Segment Tree Lazy

```

1 #include <bits/stdc++.h>
2 using namespace std;
3 #define int long long
4 #define MAXN (int)(5e5 + 10)
5
6 vector<int> lazy(4 * MAXN, 0);
7 void build_tree(vector<int>& arr, vector<int>& tree,
8     int node, int start, int end) {
9     if ( start == end ) {
10         tree[node] = arr[start];
11         return;
12     }
13     int mid = ( start + end ) >> 1;

```

```

13 int left_node = 2 * node + 1;
14 int right_node = 2 * node + 2;
15 build_tree(arr, tree, left_node, start, mid);
16 build_tree(arr, tree, right_node, mid + 1, end);
17 tree[node] = tree[left_node] + tree[right_node];
18 return;
19 }
20
21 void lazy_node(vector<int>& tree, int node, int
    start, int end) {
22     if ( lazy[node] == 0 ) return;
23
24     tree[node] += lazy[node] * ( end - start + 1 );
25     int left_node = 2 * node + 1;
26     int right_node = 2 * node + 2;
27     if ( start != end ) {
28         lazy[left_node] += lazy[node];
29         lazy[right_node] += lazy[node];
30     }
31     lazy[node] = 0;
32     return;
33 }
34
35 void update(vector<int>& arr, vector<int>& tree, int
    node, int start, int end, int l, int r, int k) {
36     lazy_node(tree, node, start, end);
37     if ( start > r || end < l ) return;
38     int mid = ( start + end ) >> 1;
39     int left_node = 2 * node + 1;
40     int right_node = 2 * node + 2;
41     if ( start >= l && end <= r ) {
42         tree[node] += k * (end - start + 1);
43         if ( start != end ) {
44             lazy[left_node] += k;
45             lazy[right_node] += k;
46         }
47         return;
48     }
49     update(arr, tree, left_node, start, mid, l, r, k);
50     update(arr, tree, right_node, mid + 1, end, l, r,
        k);
51     tree[node] = tree[left_node] + tree[right_node];
52     return;
53 }
54 int query_tree(vector<int>& arr, vector<int>& tree,
    int node, int start, int end, int l, int r) {
55     if ( start > r || end < l ) return 0;
56
57     lazy_node(tree, node, start, end);
58
59     int mid = ( start + end ) >> 1;
60     int left_node = 2 * node + 1;
61     int right_node = 2 * node + 2;
62
63     if ( start >= l && end <= r ) {
64         return tree[node];
65     }
66
67     return query_tree(arr, tree, left_node, start, mid,
        l, r) + query_tree(arr, tree, right_node, mid +
        1, end, l, r);
68 }
69
70 void solve(){
71     int n;
72     cin >> n;
73     vector<int> arr(MAXN), tree(4 * MAXN);
74     for(int i = 0; i < n; i++) cin >> arr[i];
75     build_tree(arr, tree, 0, 0, n - 1);
76     int q, v, l, r, k;
77     cin >> q;
78     while(q--) {
79         cin >> v >> l >> r;
80         if ( v == 1 ) {
81             cin >> k;
82             update(arr, tree, 0, 0, n - 1, l - 1, r - 1, k);
83         } else if ( v == 2 ) {

```

```

84         cout << query_tree(arr, tree, 0, 0, n - 1, l -
            1, r - 1) << "\n";
85     }
86 }
87 return;
88 }
89 signed main(){
90     solve();
91     return 0;
92 }

```

6.4 PBDS

```

1 #include <bits/stdc++.h>
2 #include <ext/pb_ds/assoc_container.hpp>
3 #include <ext/pb_ds/tree_policy.hpp>
4 using namespace std;
5 using namespace __gnu_pbds;
6 template <typename T>
7 using ordered_set = tree<T, null_type, less<T>,
    rb_tree_tag, tree_order_statistics_node_update>;
8
9 #define int long long
10
11 signed main () {
12     ordered_set<int> os;
13
14     int k = 1, x = 5;
15
16     os.insert(x); // O(log n)
17     os.erase(x); // O(log n)
18     // os.count(x); order_set 沒有 count 方法
19     os.find(x); // O(log n)
20
21     // ordered_set 獨有的操作
22     // 1. 查找第k小
23     int val = *os.find_by_order(k); // O(log n)
24     // 2. 求排名
25     int order = os.order_of_key(x); // O(log n)
26
27     // set 需要遍歷才能實現上述功能
28     set<int> s;
29     auto it = next(s.begin(), k); // O(n)
30     distance(s.begin(), s.lower_bound(x)); // O(n)
31 }

```

7 String

7.1 Suffix Array

```

1 #include<bits/stdc++.h>
2 #define int long long
3
4 using namespace std;
5
6 void count_sort(auto &p, auto &c){
7     int n = p.size();
8     vector<int> cnt(n);
9     for(auto el : c) cnt[el] ++;
10    vector<int> p_new(n), pos(n);
11    pos[0] = 0;
12    for(int i=1;i<n;i++) pos[i] = pos[i-1] + cnt[i-1];
13    for(auto el : p){
14        int i = c[el];
15        p_new[pos[i]] = el;
16        pos[i] ++;
17    }
18    p = p_new;
19 }
20
21 signed main(){
22     string s;

```

```

23 cin>>s;
24 s += "$";
25 int n = s.size();
26 vector<pair<char, int>> v(n);
27 vector<int> p(n), c(n);
28 for(int i=0;i<n;i++) v[i] = {s[i], i};
29 sort(v.begin(), v.end());
30
31 for(int i=0;i<v.size();i++) p[i] = v[i].second;
32 c[p[0]] = 0;
33 for(int i=1;i<v.size();i++){
34     if(v[i].first == v[i-1].first) c[p[i]] =
35         c[p[i-1]];
36     else c[p[i]] = c[p[i-1]] + 1;
37 }
38
39 int k = 0;
40 while((1 << k) < n){
41     for(int i=0;i<n;i++) p[i] = (p[i] - (1 << k) + n)
42         % n;
43     count_sort(p, c);
44
45     vector<int> c_new(n);
46     c_new[p[0]] = 0;
47     for(int i=1;i<v.size();i++){
48         pair<int, int> prev = {c[p[i-1]], c[(p[i-1] +
49             (1 << k)) % n]};
50         pair<int, int> now = {c[p[i]], c[(p[i] + (1 <<
51             k)) % n]};
52         if(prev == now) c_new[p[i]] = c_new[p[i-1]];
53         else c_new[p[i]] = c_new[p[i-1]] + 1;
54     }
55     c = c_new;
56     k++;
57 }
58 for(int i=0;i<n;i++) cout<<p[i]<<"\n";
59 }

```

7.2 Suffix Array LCP

```

1 #include <bits/stdc++.h>
2 #define int long long
3 using namespace std;
4
5 vector<int> lcp(n);
6 int k = 0;
7 for(int i=0;i<n-1;i++){
8     int pi = c[i];
9     int j = p[pi - 1];
10    while(s[i+k] == s[j+k]) k++;
11    lcp[pi] = k;
12    k = k-1 > 0 ? k-1 : 0;
13 }

```

7.3 KMP algorithm

```

1 vector<int> NEXT;
2 void getNext(string p){
3     int i = 1, j = i - 1;
4     while(i < p.size()){
5         if(p[i] == p[j]){
6             NEXT[i++] = ++j;
7         }
8         else if(j <= 0){
9             NEXT[i++] = 0;
10        }
11        else{
12            j = NEXT[j - 1];
13        }
14    }
15 }
16
17 int KMP(string s, string p){

```

```

18     int i = 0, j = 0;
19     while(i < s.size() && j < p.size()){
20         if(s[i] == p[j]){
21             ++i;
22             ++j;
23         }else if(j <= 0){
24             ++i;
25         }else{
26             j = NEXT[j - 1];
27         }
28     }
29
30     if(j >= p.size()) return i - p.size();
31     else return -1;
32 }

```

7.4 Manacher's algorithm

```

1 int P[SIZE * 2];
2
3 string convertToNewString(const string &s) {
4     string newString = "@";
5
6     for (int i = 0; i < s.size(); i++) {
7         newString += "#" + s.substr(i, 1);
8     }
9
10    newString += "$";
11    return newString;
12 }
13
14 string longestPalindromeSubstring(const string &s) {
15     string Q = convertToNewString(s);
16     int c = 0, r = 0; // current
17                        // center, right limit
18
19     for (int i = 1; i < Q.size() - 1; i++) {
20         // find the corresponding letter in the
21         // palidrome subString
22         int iMirror = c - (i - c);
23
24         if(r > i) {
25             P[i] = min(r - i, P[iMirror]);
26         }
27
28         // expanding around center i
29         while (Q[i + 1 + P[i]] == Q[i - 1 - P[i]]){
30             P[i]++;
31         }
32
33         // Update c,r in case if the palindrome
34         // centered at i expands past r,
35         if (i + P[i] > r) {
36             c = i; // next center = i
37             r = i + P[i];
38         }
39     }
40
41     // Find the longest palindrome length in p.
42
43     int maxPalindrome = 0;
44     int centerIndex = 0;
45
46     for (int i = 1; i < Q.size() - 1; i++) {
47         if (P[i] > maxPalindrome) {
48             maxPalindrome = P[i];
49             centerIndex = i;
50         }
51     }
52
53     cout << maxPalindrome << "\n";
54     return s.substr( (centerIndex - 1 -
55         maxPalindrome) / 2, maxPalindrome);
56 }

```

7.5 Z-algorithm

```

1 void z_build(const char *S, int *Z) {
2     Z[0] = 0;
3     int bst = 0;
4     for(int i = 1; S[i]; i++) {
5         if(Z[bst] + bst < i) Z[i] = 0;
6         else Z[i] = min(Z[bst]+bst-i, Z[i-bst]);
7         while(S[Z[i]] == S[i+Z[i]]) Z[i]++;
8         if(Z[i] + i > Z[bst] + bst) bst = i;
9     }
10 }

```

8 Flow

8.1 dinic

```

1 struct edge{
2     int u, v, c, f;
3     edge(int u, int v, int c, int f):u(u), v(v),
4         c(c), f(f){}
5 };
6 vector<edge> e;
7 vector<int> G[maxn];
8 int level[maxn]; // 紀錄每個點的層數
9 int iter[maxn]; // 目前弧優化
10 int m;
11 void init(int n){
12     for(int i = 0; i <= n; i++)G[i].clear();
13     e.clear();
14 }
15 void addedge(int u, int v, int c){
16     e.push_back(edge(u, v, c, 0));
17     e.push_back(edge(v, u, 0, 0));
18     m = e.size();
19     G[u].push_back(m - 2);
20     G[v].push_back(m - 1);
21 }
22 void BFS(int s){
23     memset(level, -1, sizeof(level));
24     queue<int> q;
25     level[s] = 0;
26     q.push(s);
27     while(!q.empty()){
28         int u = q.front();
29         q.pop();
30         for(int v = 0; v < G[u].size(); v++){
31             edge& now = e[G[u][v]];
32             if(now.c > now.f && level[now.v] < 0){
33                 level[now.v] = level[u] + 1;
34                 q.push(now.v);
35             }
36         }
37     }
38 }
39 // 尋找增廣路徑
40 int dfs(int u, int t, int f){
41     if(u == t) return f;
42     // 用 iter 表示每個節點目前的弧，防止多次遍歷
43     for(int &v = iter[u]; v < G[u].size(); v++){
44         edge &now = e[G[u][v]];
45         // now.c - now.f > 0 表示此路未清空
46         // level[u] < level[now.v] 表示這條路是最短路
47         if(now.c - now.f > 0 && level[u] <
48             level[now.v]){
49             int d = dfs(now.v, t, min(f, now.c -
50                 now.f));
51             if(d > 0) {
52                 now.f += d; // 正向邊流量 +d
53             }
54         }
55     }
56 }

```

```

54         e[G[u][v] ^ 1].f -= d; // 反向邊 -d
55         return d;
56     }
57 }
58 }
59 return 0;
60 }
61 int Maxflow(int s, int t){
62     int flow = 0;
63     for(;;) {
64         BFS(s);
65         // 殘餘的路線達不到 t，增廣路徑不存在
66         if(level[t] < 0) return flow;
67         memset(iter, 0, sizeof(iter));
68         int f;
69         while((f = dfs(s, t, INF)) > 0) flow += f;
70     }
71     return flow;
72 }
73 }

```

9 離散化 Discretization

9.1 Vector ($O(N \log N)$)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3
4 int main()
5 {
6     vector<int> a = {1561, 777, 89898, 5}; // --> {3,
7         2, 4, 1}
8     vector<int> b = a;
9     sort(b.begin(), b.end());
10    b.resize(unique(b.begin(), b.end()) - b.begin());
11
12    for(int i:a)
13    {
14        cout << lower_bound(b.begin(), b.end(), i) -
15            b.begin() + 1 << "\n";
16    }
17    return 0;
18 }

```

9.2 Map + Set ($O(N \log N)$)

```

1 #include<bits/stdc++.h>
2 using namespace std;
3
4 int main(){
5     vector<int> a = {1561, 777, 89898, 5}; // -> {3,
6         2, 4, 1}
7
8     int now = 1;
9     map<int, int> mp;
10    set<int> ms;
11
12    for(int i:a){
13        ms.insert(i);
14    }
15
16    for(int i:ms){
17        mp[i] = now++;
18    }
19
20    for(int i:a){
21        cout << mp[i] << "\n";
22    }
23
24    return 0;
25 }

```