



University of
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Using Constraint Programming to Enumerate Permutations avoiding Mesh Patterns

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Permutation Patterns 2022, Valparaiso

Why?

- At Permutation Patterns 2021 I heard that the enumeration research has stalled a wee bit.
- Constraint programming is great (and modular)!
- Sergey has had a few successes with CP and enumerating word problems.
- (Really I just want to return to the Permutation Pattern Community)
- (There are grants being submitted/reviewed that mention Permutation Patterns and CP)

Constraint Satisfaction Problem (CSP)

Constraint Satisfaction Problem is a neat way of representing a problem and the solving of it is a very fast combinatorial search. It takes

- some variables,
- some values that the variables can have,
- some rules about these variables and values,

and then mix and matches the values to the variables and checks if any of the rules are being broken.

More formally

A CSP consists of the *given*

- V – set of *decision variables*.
- For each $v \in V$ there is a *domain* D_v , which consists of potential values of v .
- C – set of *constraints* on the decision variables.

and we want to *find* an assignment of values to variables such that all constraints are satisfied The instance consists of some specific assignments which apply to a particular case of the problem.

Decision Variables

A decision variable corresponds to a choice that must be made in solving a problem.

Domains

- Values in the domain of a decision variable correspond to the options for a particular choice.
- A decision variable is assigned a single value from its domain.

Constraints

- *scope*: subset of the decision variables a constraint involves.
- Of the possible combinations of assignments to the variables in its scope, a constraint specifies:
 - Which are allowed. (Assignments that satisfy the constraint.)
 - Which are disallowed. (Assignments that violate the constraint.)

Solving Problems with Constraints

Consists of 2 phases

- 1 Describe the problem to be solved as a constraint model. (In a format suitable for input to a constraint solver)
- 2 Search (automatically) for solutions to the model with a constraint solver.

Why should you care?

- There are a few tools out there already (Permuta, PermLab, PatternClass,...)
- This might not be faster than those (we haven't tested it yet)
- Is it giving us new insights for $Av(1324)$ or any other classes? (Not yet)

So really why?

- It's modular, and we are making it more friendly for mathematicians.
- It's *just* expressing our/your definitions in a nice way as constraints.

Demo

Let's have a look at CP in action.

If the demo went well

This is early work, but here are our plans.

- We are looking for more properties, more problems, more anything to model.
- We are going to compare it to the existing tools out there.
- We are working on making it nicer for mathematicians to work in.
- We are working on making it faster through symmetries, 'homomorphisms', etc.

If the demo did not go well

This is very early work, the demo was run in a student created online collaborative worksheet and we are working on making it more stable. But you can create models and run things locally, which works! Here are our plans.

- We are looking for more properties, more problems, more anything to model.
- We are working on making it nicer for mathematicians to work in.
- We are working on making it faster through symmetries, 'homomorphisms', etc.




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Thank you!

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