



ISOPOD

Isolating Poled On-chip Device

PHYS 559 Final Project

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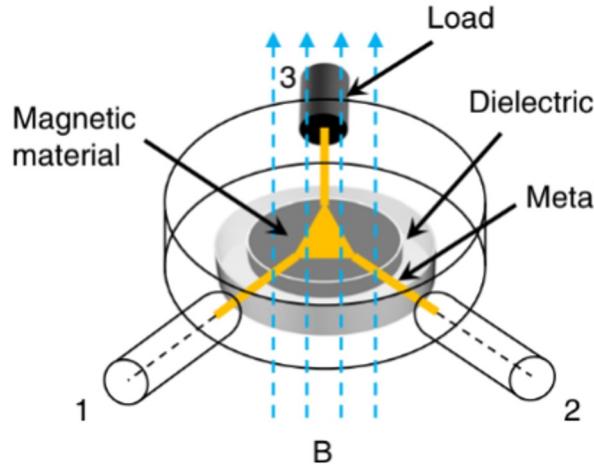
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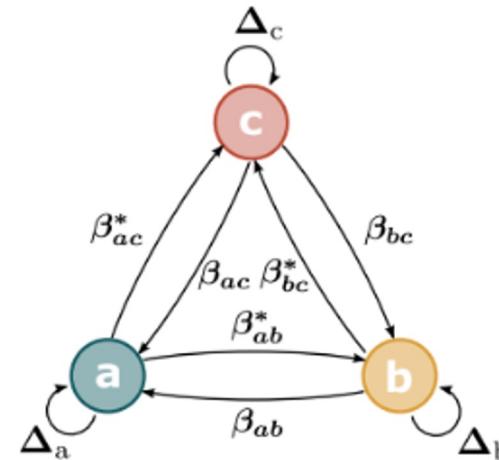
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Motivation

- Isolation of microwaves is essential for the qubit readout and amplification chain
 - Protect qubit from backpropagating noise
 - We **need** nonreciprocity
- Current isolators are: bulky, highly magnetic, and lossy

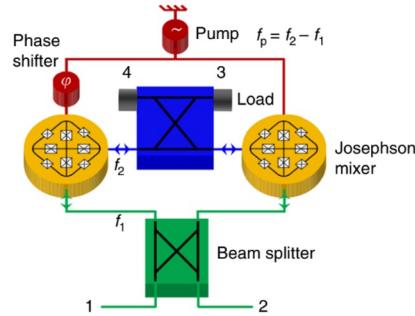


Bulk ferrite isolators
Abdo et al, *Nature Comm* (2019)

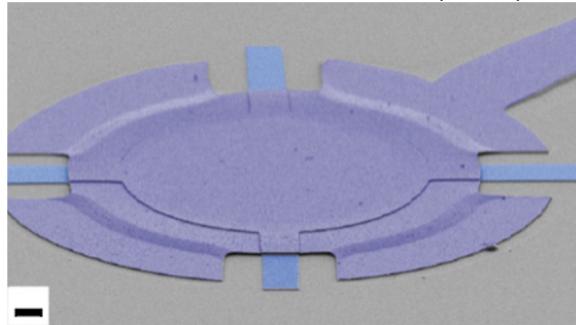


Nonreciprocal phase relations
Lecoq et al, *Phys Rev Appl* (2017)

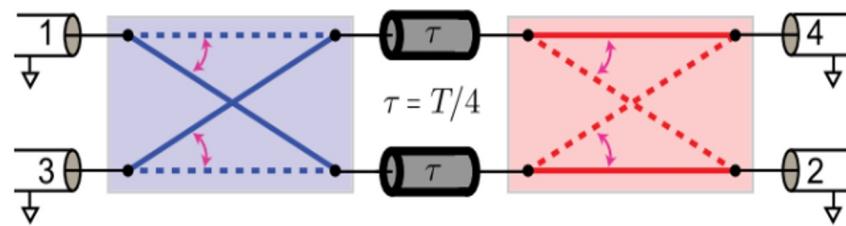
Literature Background: State of the Art Approaches



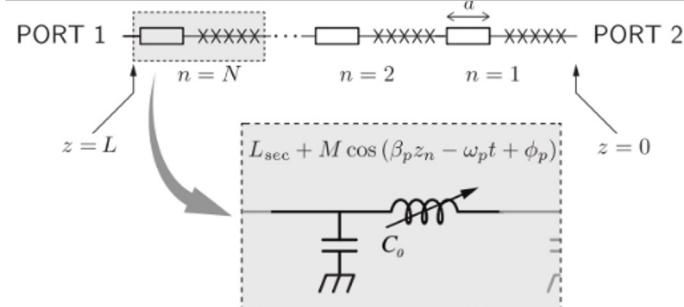
Interferometric Isolator
Abdo et al, *Nature Comm* (2019)



Optomechanical Isolator
Bernier et al, *Nature Comm* (2017)



Active Modulation-based Isolator
Chapman et al, *Phys Rev Appl* (2019)



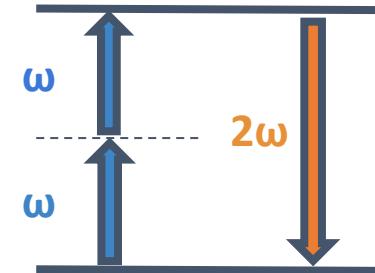
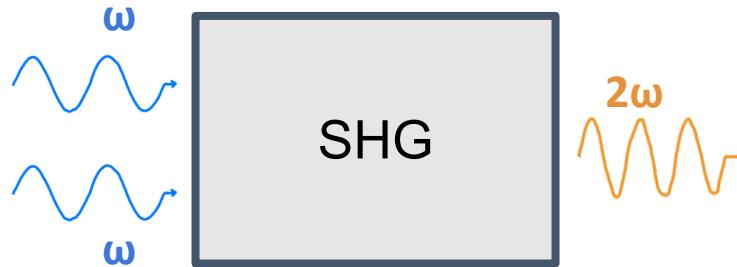
Unidirectional Frequency Conversion
Ranzani et al, *Phys Rev Appl* (2017)

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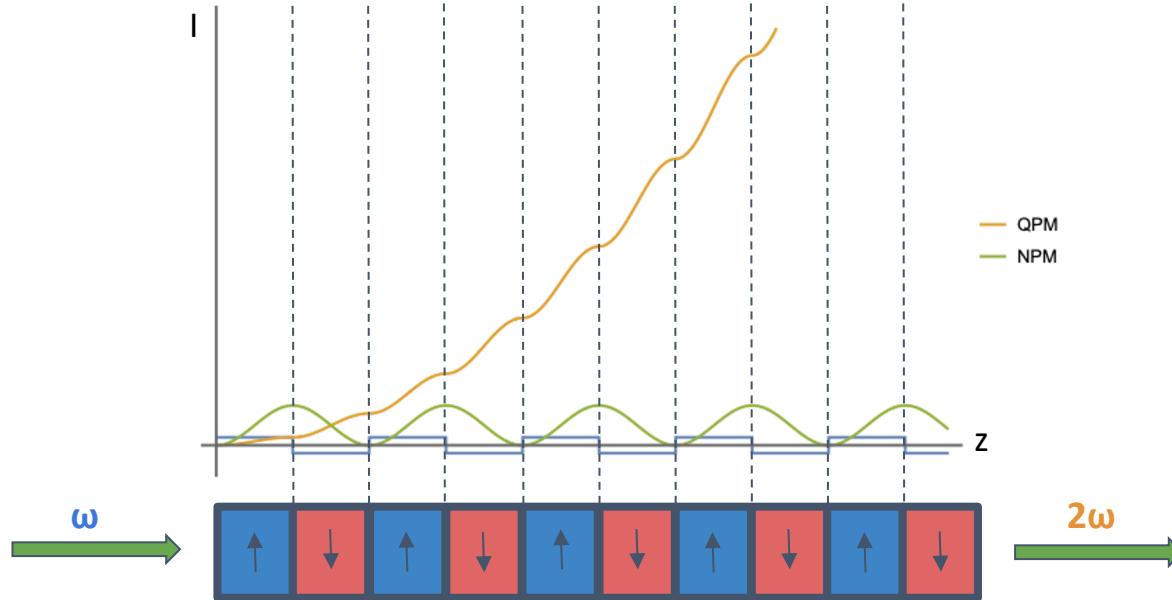
Physics Background: Parametric Interactions

- Nonlinearity can provide frequency mixing
 - A Josephson junction is a nonlinear inductor
 - We need to control **phase matching** and **dispersion**
- Second harmonic generation can allow us to create 2ω light from ω



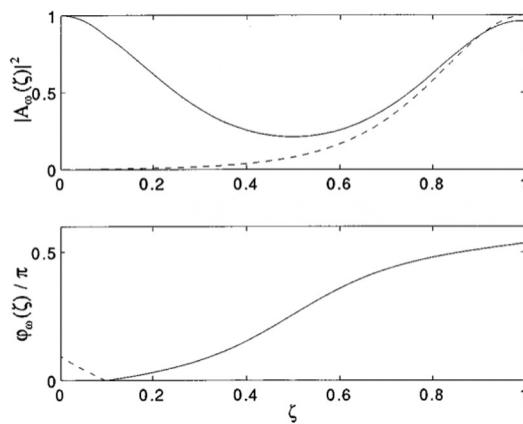
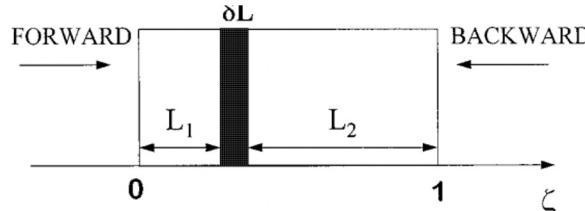
Physics Background: Poling

- Kerr reversal can *invert* the sign of our nonlinearity
 - Typically used to quasi-phase match in photonic systems
- Poling period(Λ_{coh}) can control phase mismatch $\Delta k = k_2 - 2k_1 - 2\pi/\Lambda_{coh}$

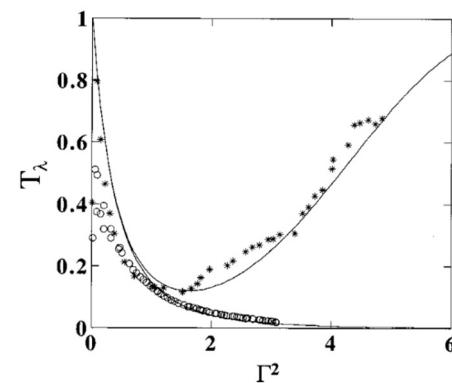
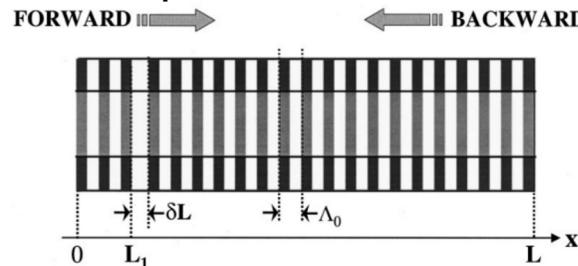


Inspiration: Optical

- Poling defects can create **isolation** in optics



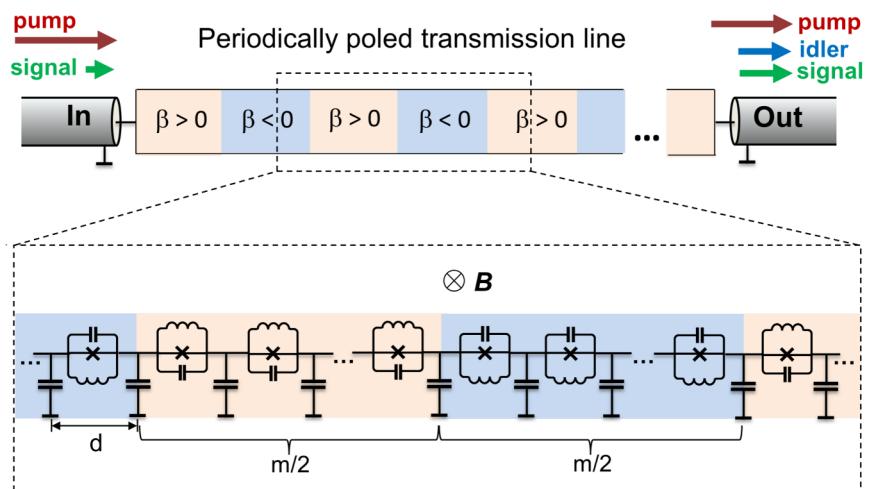
Theoretical poling-inspired defect
Gallo et al., *Optica* (1998)



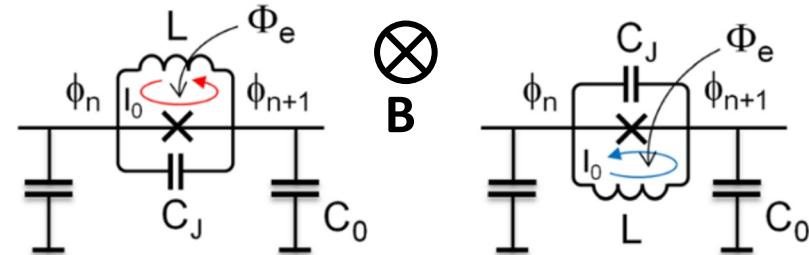
Experimental quasi phase matched isolator
Gallo et al., *Appl. Phys. Lett.* (2001)

Inspiration: Superconducting Circuits

- Transmission lines and optical waveguides are both wave-propagation media
 - They can also be nonlinear (JJs here, ferroelectric crystals in optics)
- Just like optics, we can “pole” our transmission lines with flux-biased SQUIDs



Periodic poling in superconducting transmission line
A.B. Zorin, *Appl Phys Lett* (2021)



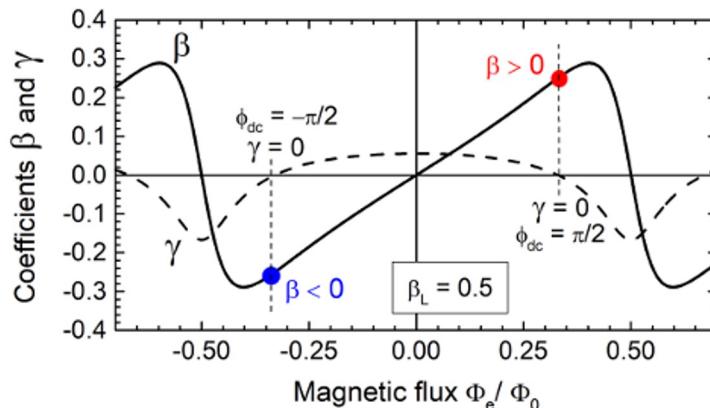
Kerr reversal with RF SQUIDS
A.B. Zorin, *Appl Phys Lett* (2021)

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Inspiration: Important Parameters

- Our 2nd order nonlinearity is related to the SQUID screening parameter (β_L) and DC flux bias (φ_{DC})
 - We can bias into the three-wave mixing (3WM)/second harmonic generation (SHG) regime via $\varphi_{DC}=\pi/2$



Plot of β and γ against flux
A.B. Zorin, *Appl. Phys. Lett.* (2021)

$$I(\varphi) = \frac{I_c \varphi}{\beta_L} + I_c (\sin(\varphi_{dc} + \varphi) - \sin(\varphi))$$

$$\frac{I}{I_c} = (\beta_L^{-1} + \cos \varphi_{dc}) \varphi - \tilde{\beta} \varphi^2 - \tilde{\gamma} \varphi^3 \dots$$

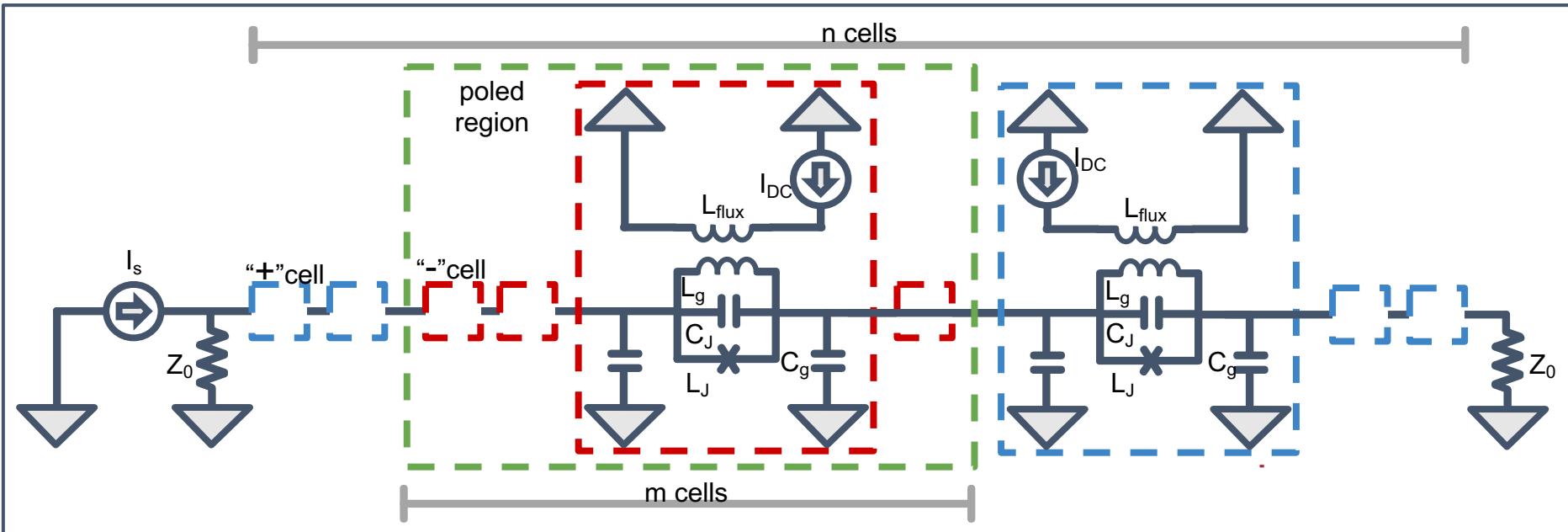
$$\beta = \frac{\beta_L}{2} \sin(\varphi_{dc}) \quad \gamma = \frac{\beta_L}{6} \cos(\varphi_{dc})$$

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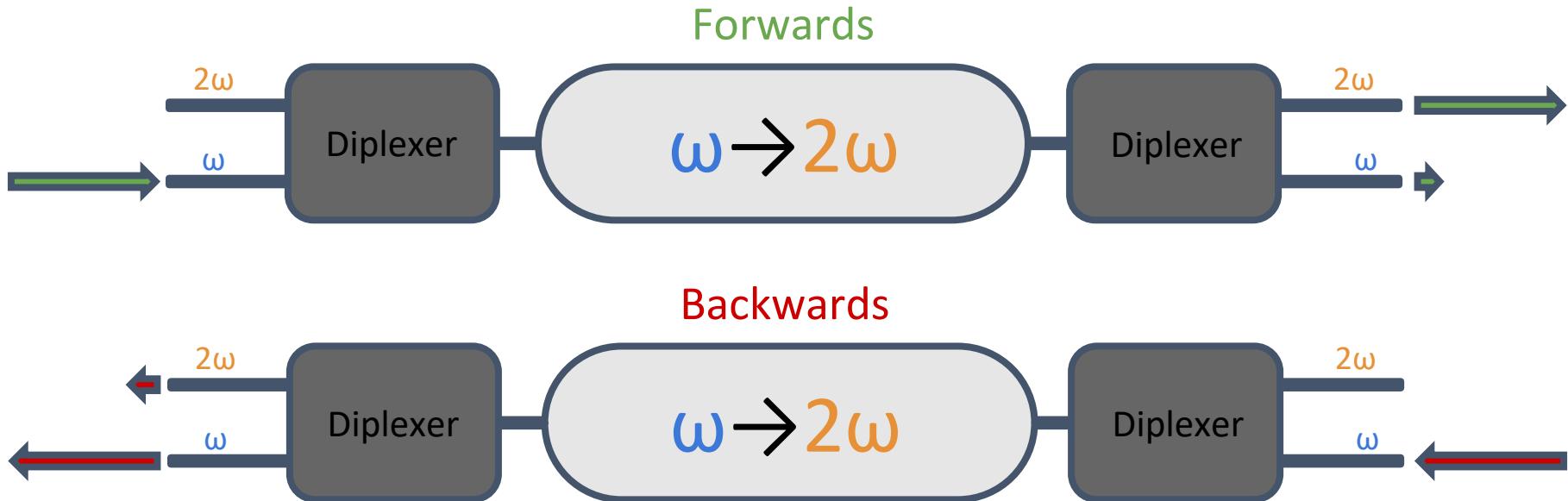
Our Device

- We propose an on-chip microwave isolator on a superconducting platform
 - Our device realizes **unidirectional frequency conversion**
 - Combine that with filtering/diplexing to achieve **isolation**
 - **On-chip** and **scalable**
 - **Integratable** with traveling wave parametric amplifiers (TWPAAs)



Extension to Isolation

- With filters and/or frequency diplexers, we can harness our nonreciprocal frequency conversion for isolation



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Simulation: Coupled-Mode Equations

- Coupled mode equations describe frequency conversion and power transfer
 - To accurately simulate, we need very high harmonics = Many equations...

How many equations, you ask?

$$\begin{aligned} \frac{dA_i}{dx} = & \frac{\beta}{2} \left(k_s k_p A_p A_s^* e^{i(k_p - k_s)x} + k_{p+i} k_p A_{p+i} A_s^* e^{i(k_{p+i} - k_p)x} \right. \\ & + k_{2p} k_{p+s} A_{2p} A_s^* e^{i(k_{2p} - k_{p+s})x} + k_{2p+i} k_{2p} A_{2p+i} A_s^* e^{i(k_{2p+i} - k_{2p})x} \\ & + k_{3p} k_{2p+s} A_{3p} A_{2p+s}^* e^{i(k_{3p} - k_{2p+s})x} + k_{3p+s} k_{3p} A_{3p+s} A_{3p}^* e^{i(k_{3p+s} - k_{3p})x} \\ & + k_{4p} k_{3p+s} A_{4p} A_{3p+s}^* e^{i(k_{4p} - k_{3p+s})x} + k_{4p+i} k_{4p} A_{4p+i} A_{4p}^* e^{i(k_{4p+i} - k_{4p})x} \\ & \left. + k_{5p} k_{4p+s} A_{5p} A_{4p+s}^* e^{i(k_{5p} - k_{4p+s})x} \right) e^{-ik_s x}, \end{aligned} \quad (B.2)$$

$$\begin{aligned} \frac{dA_s}{dx} = & \frac{\beta}{2} \left(k_i k_p A_p A_s^* e^{i(k_p - k_i)x} + k_{p+s} k_p A_{p+s} A_s^* e^{i(k_{p+s} - k_p)x} \right. \\ & + k_{2p} k_{p+s} A_{2p} A_s^* e^{i(k_{2p} - k_{p+s})x} + k_{2p+s} k_{2p} A_{2p+s} A_{2p}^* e^{i(k_{2p+s} - k_{2p})x} \\ & + k_{3p} k_{2p+s} A_{3p} A_{2p+s}^* e^{i(k_{3p} - k_{2p+s})x} + k_{3p+s} k_{3p} A_{3p+s} A_{3p}^* e^{i(k_{3p+s} - k_{3p})x} \\ & + k_{4p} k_{3p+s} A_{4p} A_{3p+s}^* e^{i(k_{4p} - k_{3p+s})x} + k_{4p+s} k_{4p} A_{4p+s} A_{4p}^* e^{i(k_{4p+s} - k_{4p})x} \\ & \left. + k_{5p} k_{4p+s} A_{5p} A_{4p+s}^* e^{i(k_{5p} - k_{4p+s})x} \right) e^{-ik_s x}, \end{aligned} \quad (B.3)$$

$$\begin{aligned} \frac{dA_p}{dx} = & \frac{\beta}{2} \left(-k_i k_s A_s A_s^* e^{i(k_i + k_s)x} + k_{p+i} k_i A_{p+i} A_s^* e^{i(k_{p+i} - k_i)x} \right. \\ & + k_{p+s} k_s A_{p+s} A_s^* e^{i(k_{p+s} - k_s)x} + k_{2p} k_p A_{2p} A_s^* e^{i(k_{2p} - k_p)x} \\ & + k_{2p+i} k_{p+i} A_{2p+i} A_s^* e^{i(k_{2p+i} - k_{p+i})x} + k_{2p+s} k_{p+s} A_{2p+s} A_{2p}^* e^{i(k_{2p+s} - k_{p+s})x} \\ & + k_{3p} k_{2p} A_{3p} A_{2p}^* e^{i(k_{3p} - k_{2p})x} + k_{3p+s} k_{2p+i} A_{3p+i} A_{2p}^* e^{i(k_{3p+s} - k_{2p+i})x} \\ & + k_{3p+s} k_{2p+s} A_{3p+s} A_{2p+s}^* e^{i(k_{3p+s} - k_{2p+s})x} + k_{4p} k_{3p} A_{4p} A_{3p}^* e^{i(k_{4p} - k_{3p})x} \\ & + k_{4p+i} k_{3p+i} A_{4p+i} A_{3p+i}^* e^{i(k_{4p+i} - k_{3p+i})x} + k_{4p+s} k_{3p+s} A_{4p+s} A_{3p+s}^* e^{i(k_{4p+s} - k_{3p+s})x} \\ & \left. + k_{5p} k_{4p} A_{5p} A_{4p}^* e^{i(k_{5p} - k_{4p})x} \right) e^{-ik_p x} \end{aligned} \quad (B.4)$$

$$\begin{aligned} \frac{dA_{p+i}}{dx} = & \frac{\beta}{2} \left(-k_i k_p A_p A_s^* e^{i(k_i + k_p)x} + k_{2p} k_s A_{2p} A_s^* e^{i(k_{2p} - k_s)x} \right. \\ & + k_{2p+i} k_p A_{2p+i} A_s^* e^{i(k_{2p+i} - k_p)x} + k_{3p} k_{p+s} A_{3p} A_{p+s}^* e^{i(k_{3p} - k_{p+s})x} \\ & + k_{3p+i} k_{2p} A_{3p+i} A_{2p}^* e^{i(k_{3p+i} - k_{2p})x} + k_{4p} k_{2p+s} A_{4p} A_{2p+s}^* e^{i(k_{4p} - k_{2p+s})x} \\ & + k_{4p+i} k_{3p+s} A_{4p+i} A_{3p+s}^* e^{i(k_{4p+i} - k_{3p+s})x} + k_{5p} k_{3p+s} A_{5p} A_{3p+s}^* e^{i(k_{5p} - k_{3p+s})x} \\ & \left. + k_{5p} k_{4p+s} A_{4p+s} A_{4p}^* e^{i(k_{5p} - k_{4p+s})x} \right) e^{-ik_{p+i} x}, \end{aligned} \quad (B.5)$$

$$\begin{aligned} \frac{dA_{p+s}}{dx} = & \frac{\beta}{2} \left(-k_i k_p A_s A_p^* e^{i(k_i + k_p)x} + k_{2p} k_i A_{2p} A_s^* e^{i(k_{2p} - k_i)x} \right. \\ & + k_{2p+s} k_p A_{2p+s} A_s^* e^{i(k_{2p+s} - k_p)x} + k_{3p} k_{p+s} A_{3p} A_{p+s}^* e^{i(k_{3p} - k_{p+s})x} \\ & + k_{3p+s} k_{2p} A_{3p+s} A_{2p}^* e^{i(k_{3p+s} - k_{2p})x} + k_{4p} k_{2p+s} A_{4p} A_{2p+s}^* e^{i(k_{4p} - k_{2p+s})x} \\ & + k_{4p+s} k_{3p+s} A_{4p+s} A_{4p}^* e^{i(k_{4p+s} - k_{3p+s})x} + k_{5p} k_{3p+s} A_{5p} A_{3p+s}^* e^{i(k_{5p} - k_{3p+s})x} \\ & \left. + k_{5p} k_{4p+s} A_{4p+s} A_{4p}^* e^{i(k_{5p} - k_{4p+s})x} \right) e^{-ik_{p+s} x}, \end{aligned} \quad (B.6)$$

$$\begin{aligned} \frac{dA_{2p}}{dx} = & \frac{\beta}{2} \left(-k_i k_{2p+s} A_i A_{2p+s} e^{i(k_i + k_{2p+s})x} - k_s k_{p+i} A_s A_{p+i} e^{i(k_s + k_{p+i})x} \right. \\ & - \frac{k_p^2}{A_p^2} 2 e^{i(k_p + k_p)x} + k_{2p+i} k_i A_{2p+i} A_i^* e^{i(k_{2p+i} - k_i)x} \\ & + k_{2p+2} k_s A_{2p+s} A_s^* e^{i(k_{2p+s} - k_{2p+2})x} + k_{3p} k_p A_{3p} A_p^* e^{i(k_{3p} - k_p)x} \\ & + k_{3p+s} k_{p+i} A_{3p+i} A_i^* e^{i(k_{3p+i} - k_{p+i})x} + k_{3p+s} k_{p+s} A_{3p+s} A_{p+s}^* e^{i(k_{3p+s} - k_{p+s})x} \\ & + k_{4p} k_{2p} A_{4p} A_{2p}^* e^{i(k_{4p} - k_{2p})x} + k_{4p+i} k_{2p+i} A_{4p+i} A_{2p+i}^* e^{i(k_{4p+i} - k_{2p+i})x} \\ & \left. + k_{4p+s} k_{2p+s} A_{4p+s} A_{2p+s}^* e^{i(k_{4p+s} - k_{2p+s})x} + k_{5p} k_{3p} A_{5p} A_{3p}^* e^{i(k_{5p} - k_{3p})x} \right) e^{-ik_{2p} x} \end{aligned} \quad (B.7)$$

$$\begin{aligned} \frac{dA_{2p+i}}{dx} = & \frac{\beta}{2} \left(-k_i k_{2p} A_i A_{2p} e^{i(k_i + k_{2p})x} - k_p k_{p+i} A_p A_{p+i} e^{i(k_p + k_{p+i})x} \right. \\ & + k_{3p} k_s A_{3p} A_s^* e^{i(k_{3p} - k_s)x} + k_{3p+i} k_p A_{3p+i} A_i^* e^{i(k_{3p+i} - k_p)x} \\ & + k_{4p} k_{p+s} A_{4p} A_{p+s}^* e^{i(k_{4p} - k_{p+s})x} + k_{4p+i} k_{2p} A_{4p+i} A_{2p}^* e^{i(k_{4p+i} - k_{2p})x} \\ & + k_{5p} k_{2p+s} A_{5p} A_{2p+s}^* e^{i(k_{5p} - k_{2p+s})x} \left. \right) e^{-ik_{2p+i} x}, \end{aligned} \quad (B.8)$$

$$\begin{aligned} \frac{dA_{2p+s}}{dx} = & \frac{\beta}{2} \left(-k_s k_{2p} A_s A_{2p} e^{i(k_s + k_{2p})x} - k_p k_{p+s} A_p A_{p+s} e^{i(k_p + k_{p+s})x} \right. \\ & + k_{3p} k_i A_{3p} A_i^* e^{i(k_{3p} - k_i)x} + k_{3p+s} k_p A_{3p+s} A_{p+s}^* e^{i(k_{3p+s} - k_p)x} \\ & + k_{4p} k_{p+i} A_{4p} A_{p+i}^* e^{i(k_{4p} - k_{p+i})x} + k_{4p+s} k_{2p} A_{4p+s} A_{2p}^* e^{i(k_{4p+s} - k_{2p})x} \\ & + k_{5p} k_{2p+i} A_{5p} A_{2p+i}^* e^{i(k_{5p} - k_{2p+i})x} \left. \right) e^{-ik_{2p+s} x}, \end{aligned} \quad (B.9)$$

$$\begin{aligned} \frac{dA_{3p}}{dx} = & \frac{\beta}{2} \left(-k_i k_{2p+s} A_i A_{2p+s} e^{i(k_i + k_{2p+s})x} - k_s k_{2p+i} A_s A_{2p+i} e^{i(k_s + k_{2p+i})x} \right. \\ & - k_p k_{2p} A_{2p} A_{2p}^* e^{i(k_{2p} + k_{2p})x} - k_{p+i} k_{p+s} A_{p+i} A_{p+s}^* e^{i(k_{p+i} + k_{p+s})x} \\ & + k_{3p+i} k_i A_{3p+i} A_i^* e^{i(k_{3p+i} - k_i)x} + k_{3p+s} k_s A_{3p+s} A_s^* e^{i(k_{3p+s} - k_s)x} \\ & + k_{4p} k_{p+s} A_{4p} A_{p+s}^* e^{i(k_{4p} - k_{p+s})x} + k_{4p+i} k_{p+i} A_{4p+i} A_{p+i}^* e^{i(k_{4p+i} - k_{p+i})x} \\ & + k_{4p+s} k_{p+s} A_{4p+s} A_{p+s}^* e^{i(k_{4p+s} - k_{p+s})x} + k_{5p} k_{2p} A_{5p} A_{2p}^* e^{i(k_{5p} - k_{2p})x} \left. \right) e^{-ik_{3p} x}, \end{aligned} \quad (B.10)$$

$$\begin{aligned} \frac{dA_{3p+i}}{dx} = & \frac{\beta}{2} \left(-k_i k_{3p} A_i A_{3p} e^{i(k_i + k_{3p})x} - k_p k_{2p+i} A_p A_{2p+i} e^{i(k_p + k_{2p+i})x} \right. \\ & - k_{p+i} k_{2p} A_{p+i} A_{2p}^* e^{i(k_{p+i} + k_{2p})x} + k_{4p} k_{3p} A_{4p} A_{3p}^* e^{i(k_{4p} - k_{3p})x} \\ & + k_{4p+s} k_{3p+s} A_{4p+s} A_{3p+s}^* e^{i(k_{4p+s} - k_{3p+s})x} + k_{5p} k_{3p+i} A_{5p} A_{3p+i}^* e^{i(k_{5p} - k_{3p+i})x} \left. \right) e^{-ik_{3p+i} x} \end{aligned} \quad (B.11)$$

$$\begin{aligned} \frac{dA_{3p+s}}{dx} = & \frac{\beta}{2} \left(-k_s k_{3p} A_s A_{3p} e^{i(k_s + k_{3p})x} - k_p k_{2p+s} A_p A_{2p+s} e^{i(k_p + k_{2p+s})x} \right. \\ & - k_{p+i} k_{2p} A_{p+i} A_{2p}^* e^{i(k_{p+i} + k_{2p})x} + k_{4p} k_{3p} A_{4p} A_{3p}^* e^{i(k_{4p} - k_{3p})x} \\ & + k_{4p+s} k_p A_{4p+s} A_{3p+s}^* e^{i(k_{4p+s} - k_p)x} + k_{5p} k_{3p+s} A_{5p} A_{3p+s}^* e^{i(k_{5p} - k_{3p+s})x} \left. \right) e^{-ik_{3p+s} x}, \end{aligned} \quad (B.12)$$

$$\begin{aligned} \frac{dA_{4p}}{dx} = & \frac{\beta}{2} \left(-k_i k_{3p+s} A_i A_{3p+s} e^{i(k_i + k_{3p+s})x} - k_s k_{3p+i} A_s A_{3p+i} e^{i(k_s + k_{3p+i})x} \right. \\ & - k_p k_{3p} A_{3p} A_{3p}^* e^{i(k_{3p} + k_{3p})x} - k_{p+i} k_{2p+s} A_{p+i} A_{2p+s} e^{i(k_{p+i} + k_{2p+s})x} \\ & - k_{p+s} k_{2p+s} A_{p+s} A_{2p+s} e^{i(k_{p+s} + k_{2p+s})x} - \frac{k_{2p}^2}{A_{2p}^2} 2 e^{i(k_{2p} + k_{2p})x} \\ & + k_{4p+s} k_i A_{4p+s} A_i^* e^{i(k_{4p+s} - k_i)x} + k_{4p+s} k_{3p} A_{4p+s} A_{3p}^* e^{i(k_{4p+s} - k_{3p})x} \\ & + k_{5p} k_{3p} A_{5p} A_{3p}^* e^{i(k_{5p} - k_{3p})x} \left. \right) e^{-ik_{4p} x}, \end{aligned} \quad (B.13)$$

$$\begin{aligned} \frac{dA_{4p+i}}{dx} = & \frac{\beta}{2} \left(-k_i k_{4p} A_i A_{4p} e^{i(k_i + k_{4p})x} - k_p k_{3p+i} A_p A_{3p+i} e^{i(k_p + k_{3p+i})x} \right. \\ & - k_{p+i} k_{3p} A_{p+i} A_{3p}^* e^{i(k_{p+i} + k_{3p})x} - k_{2p} k_{2p+s} A_{2p} A_{2p+s} e^{i(k_{2p} + k_{2p+s})x} \\ & + k_{5p} k_s A_{5p} A_s^* e^{i(k_{5p} - k_s)x} \left. \right) e^{-ik_{4p+i} x}, \end{aligned} \quad (B.14)$$

$$\begin{aligned} \frac{dA_{4p+s}}{dx} = & \frac{\beta}{2} \left(-k_s k_{4p} A_s A_{4p} e^{i(k_s + k_{4p})x} - k_p k_{3p+s} A_p A_{3p+s} e^{i(k_p + k_{3p+s})x} \right. \\ & - k_{p+s} k_{3p} A_{p+s} A_{3p}^* e^{i(k_{p+s} + k_{3p})x} - k_{2p} k_{2p+s} A_{2p} A_{2p+s} e^{i(k_{2p} + k_{2p+s})x} \\ & + k_{5p} k_s A_{5p} A_s^* e^{i(k_{5p} - k_s)x} \left. \right) e^{-ik_{4p+s} x}, \end{aligned} \quad (B.15)$$

$$\begin{aligned} \frac{dA_{5p}}{dx} = & \frac{\beta}{2} \left(-k_i k_{4p+s} A_i A_{4p+s} e^{i(k_i + k_{4p+s})x} - k_s k_{4p+i} A_s A_{4p+i} e^{i(k_s + k_{4p+i})x} \right. \\ & - k_p k_{4p} A_{4p} A_{4p}^* e^{i(k_{4p} + k_{4p})x} - k_{p+i} k_{3p+s} A_{p+i} A_{3p+s} e^{i(k_{p+i} + k_{3p+s})x} \\ & - k_{p+s} k_{3p} A_{p+s} A_{3p}^* e^{i(k_{p+s} + k_{3p})x} - k_{2p} k_{2p+s} A_{2p} A_{2p+s} e^{i(k_{2p} + k_{2p+s})x} \\ & - k_{5p} k_{3p} A_{5p} A_{3p}^* e^{i(k_{5p} - k_{3p})x} \left. \right) e^{-ik_{5p} x}, \end{aligned} \quad (B.16)$$

Still just a bad approximation with error.

USC Viterbi

School of Engineering

Simulation: Coupled-Mode Equations

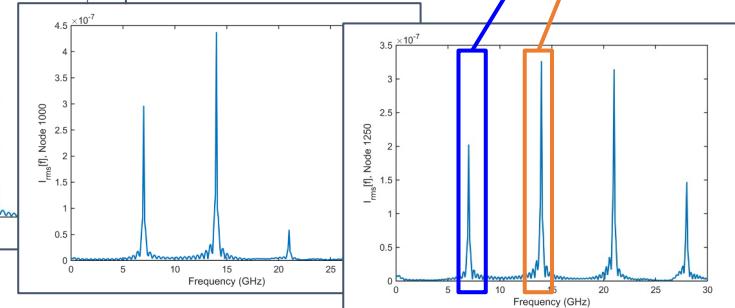
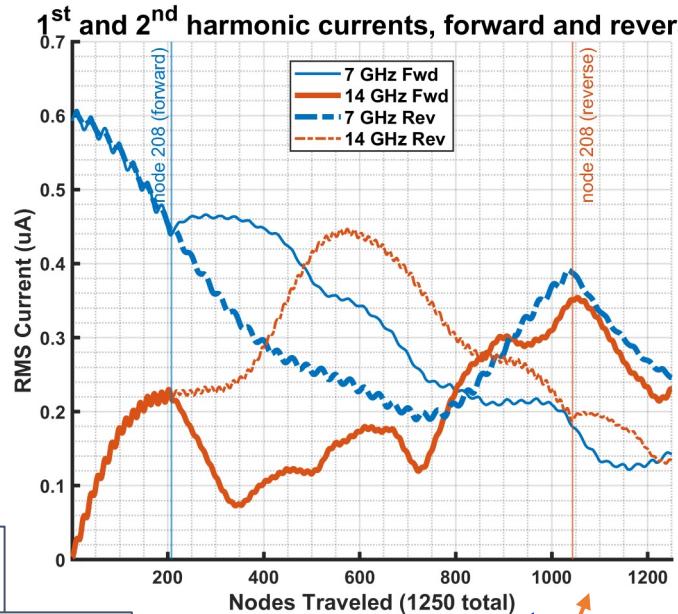
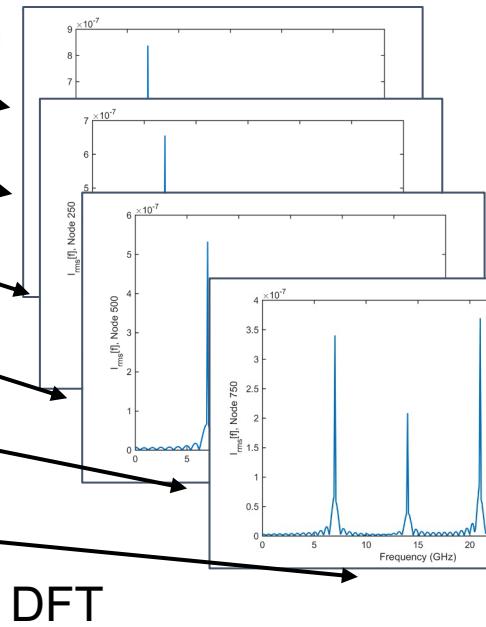
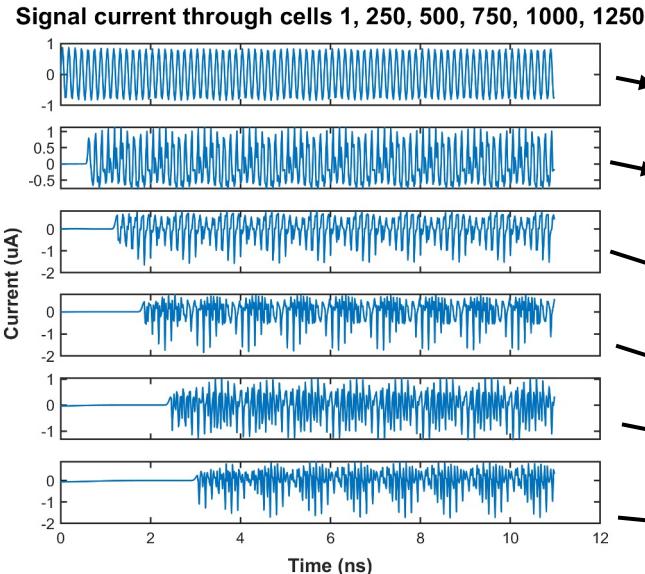
- Coupled mode equations describe frequency conversion and power transfer
 - To accurately simulate, we need very high harmonics = Many equations...
- These coupled equations below describe second harmonic generation
- If β depends on the position, you get nonreciprocity

$$\frac{dA_\omega}{dx} = -\beta A_{2\omega} A_\omega^* k_{2\omega} k_\omega e^{i(k_{2\omega}-2k_\omega)x}$$

$$\frac{dA_{2\omega}}{dx} = \beta A_\omega^2 k_\omega^2 e^{-i(k_{2\omega}-2k_\omega)x}$$

Simulation: Circuit Level

- We use *WRspice* to simulate our device
- Lumped elements, passive and nonlinear
- Post-process to obtain frequency-domain data



Simulation: Circuit Level Parameters

- These are the parameters we used:
- The length of our device is 1250 nodes with $1\mu\text{m}/\text{node}$

n	1250
a	1
b	208 / 500
m	208 /500

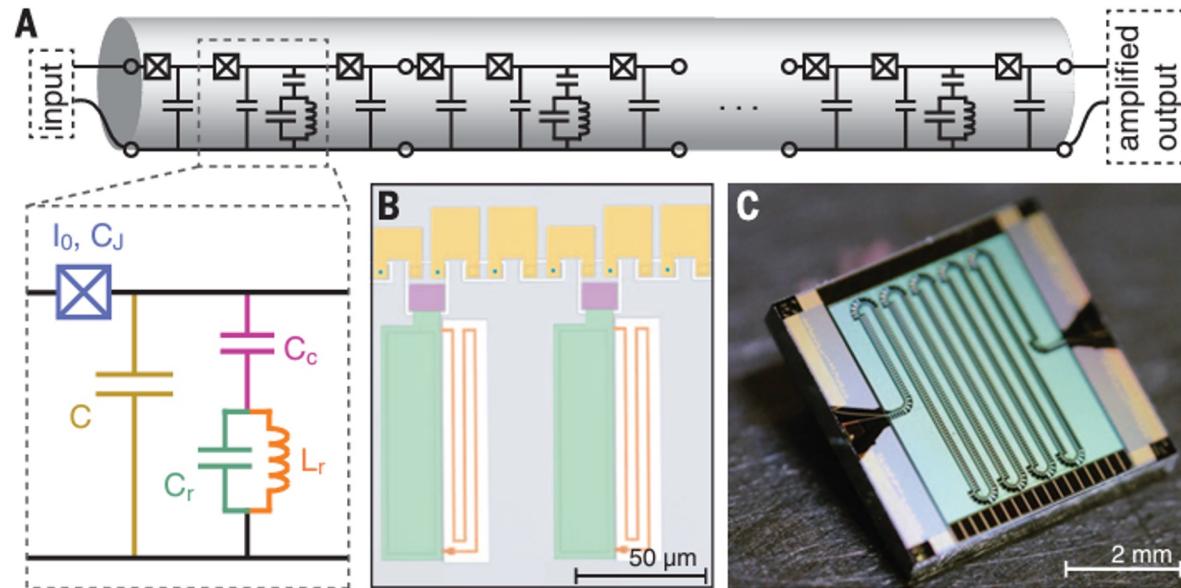
L_g	57 pH
L_J	
C_g	50 fF
C_J	60 fF

I_p	0 A
I_s	0.6 μA
I_{dc}	14.068 μA
I_{crit}	5 μA

f_p	14 GHz
f_s	7 GHz
R_{term}	23.8747 Ω

Fabrication and Design

- Our device is essentially a modified Josephson traveling wave parametric amplifier (JTWPA) and the parameters we use reflect this



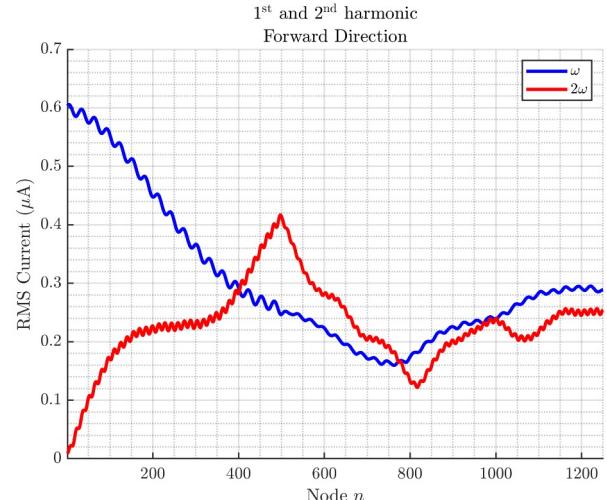
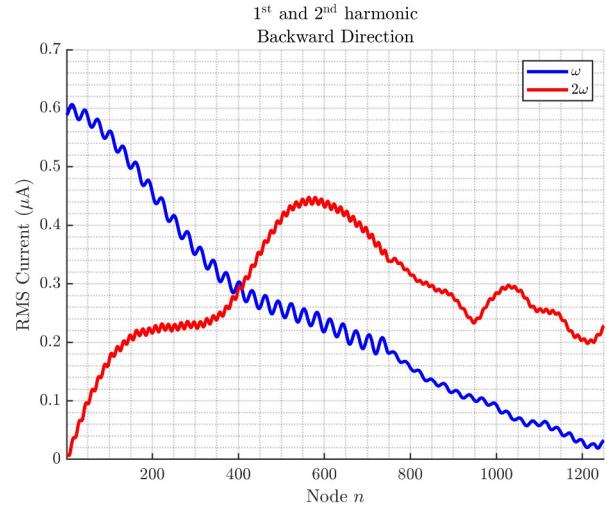
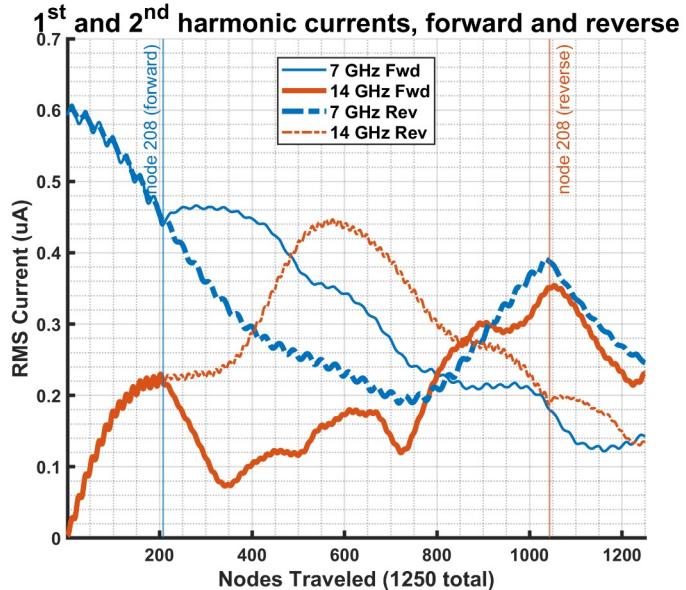
Schematic of a JTWPA in which we obtain our circuit parameters
Macklin et al., *Science* (2015)

Refresher on our device



Results: Plots of Two Device Iterations

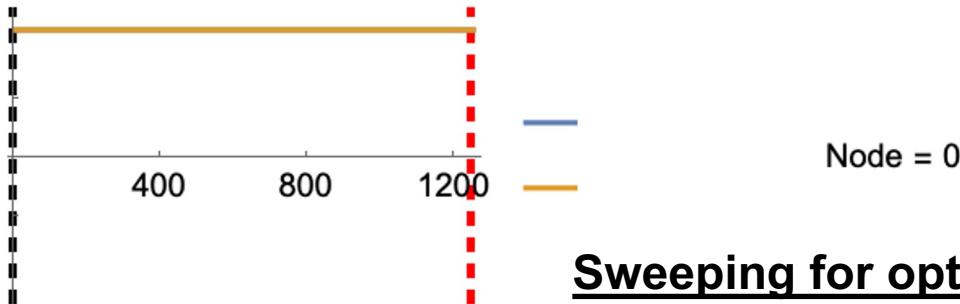
- Bottom: Poled region from cells 0 to 208
- Right: Poled region from cells 0 to 500
(Total of 1250 cells)
- We *thought* these would be optimal, based on the differential equations...



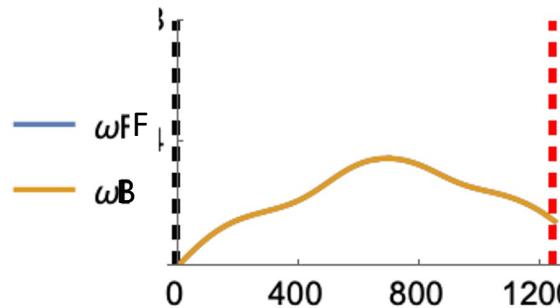
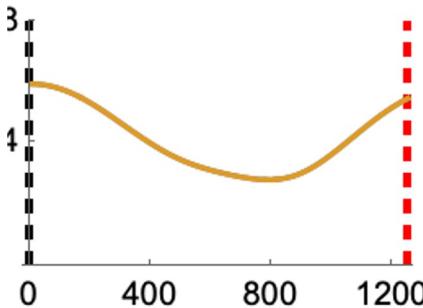
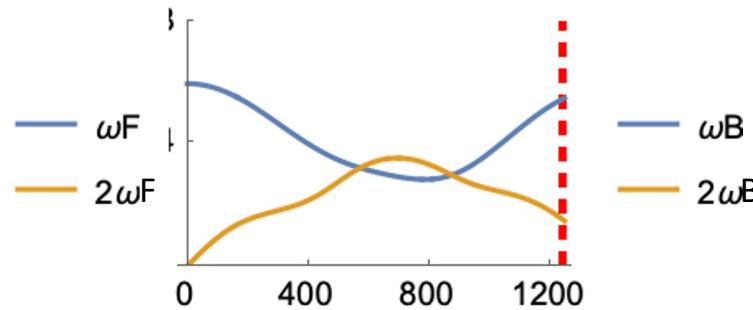
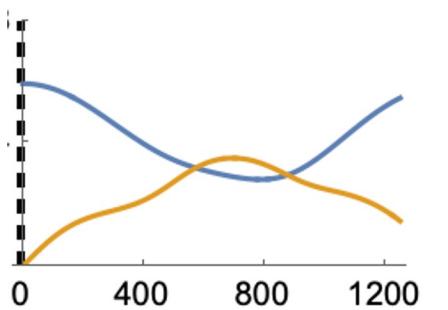
Results

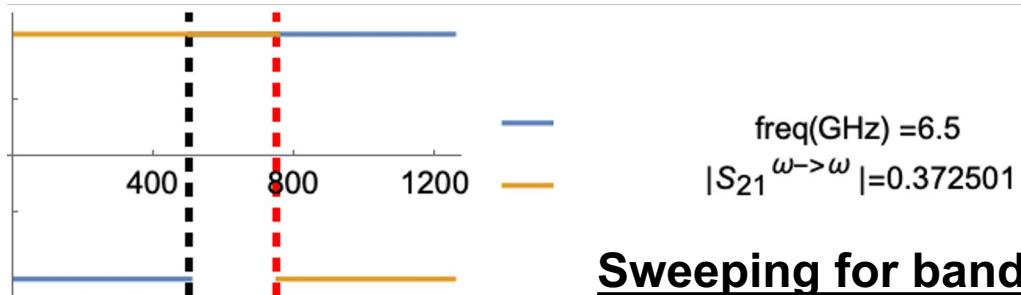
- We care about **isolation**, **insertion loss**, and **bandwidth**
 - 3dB bandwidth is 200MHz
 - Insertion loss is 7.7dB
 - Isolation is 4.75dB

	$ S_{21} ^2(\text{dB})$	$ S_{12} ^2(\text{dB})$
$\omega \rightarrow \omega$	-12.33	-7.70
$\omega \rightarrow 2\omega$	-8.18	-12.93
$2\omega \rightarrow \omega$	33.27	39.74
$2\omega \rightarrow 2\omega$	37.42	34.51

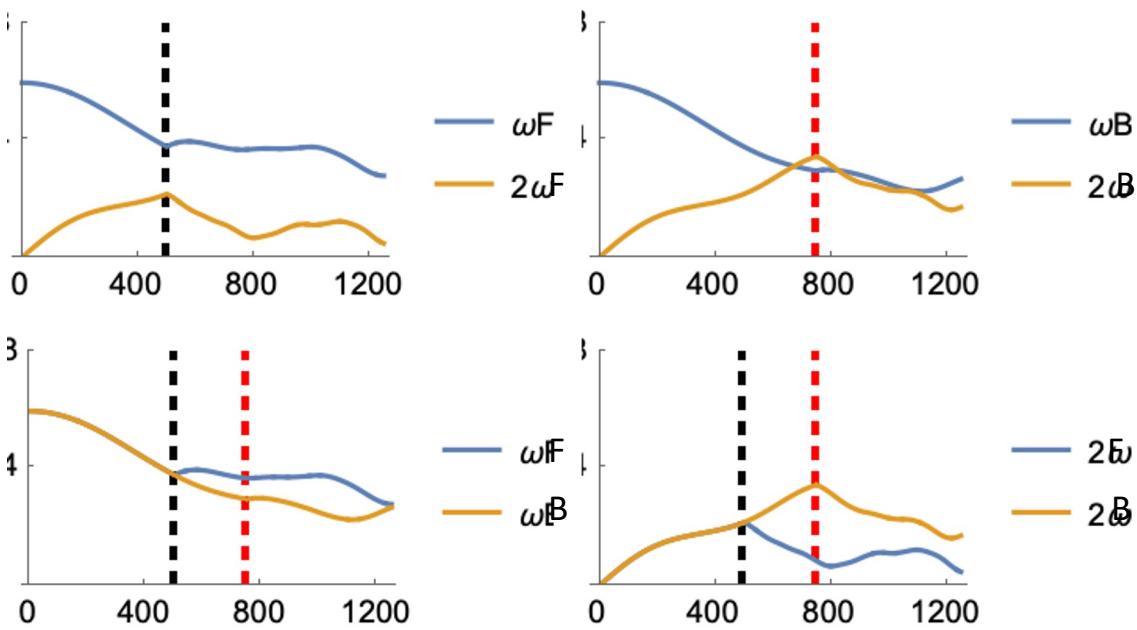


Sweeping for optimal poled region



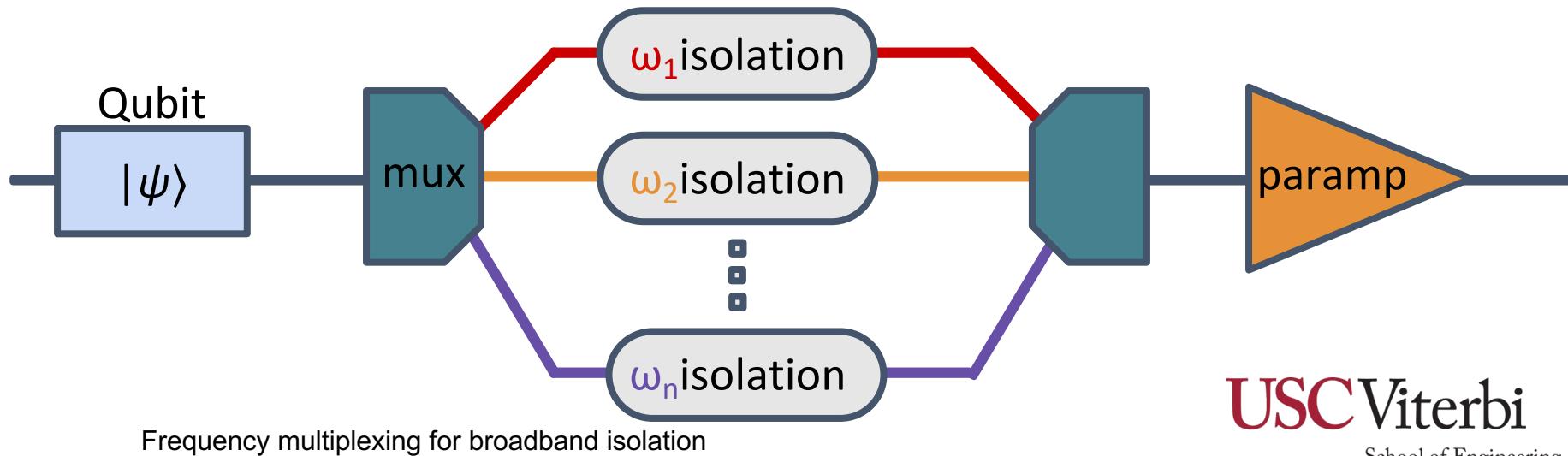


Sweeping for bandwidth



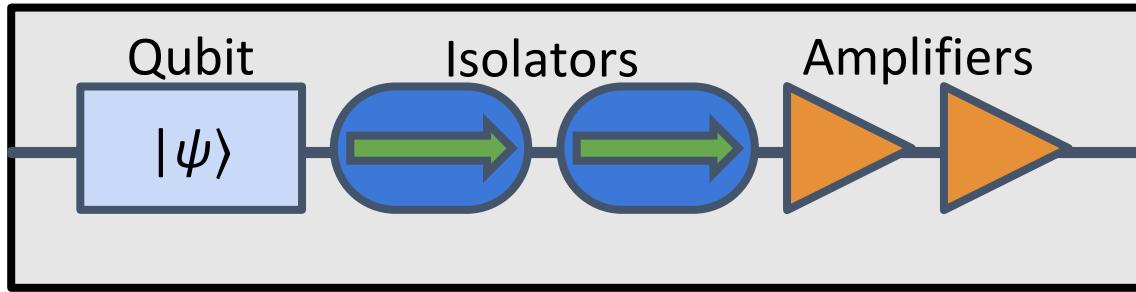
Drawbacks on our Design

- Our device combines this optical isolator on a superconducting platform
 - Not **impedance matched**
 - Even **harder to fabricate** compared to a JTWPA
 - Narrow **bandwidth** due to sensitivity to initial signal frequency
 - May be resolvable with an array of isolators with frequency multiplexing



Future Directions

- We need to sweep all our design parameters: circuit elements, defect location, SQUID screening parameter value, etc. at once to optimize
- A full 4x4 S-parameter matrix
 - Requires sweeping group delay to obtain phase information
 - Requires reflectometry to obtain S_{11} and S_{22}
- We can attach this to a TWPA to create a **directional parametric amplifier**
 - Towards fully on-chip qubit readout



Thank you!