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# Week 3

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## Week 3 作业

- 教材P105 : 3.7.3(4) , 教材P109 : 3.8.1
- 教材P118 : 3.9.3 (用算法3.36构造) , 3.9.4

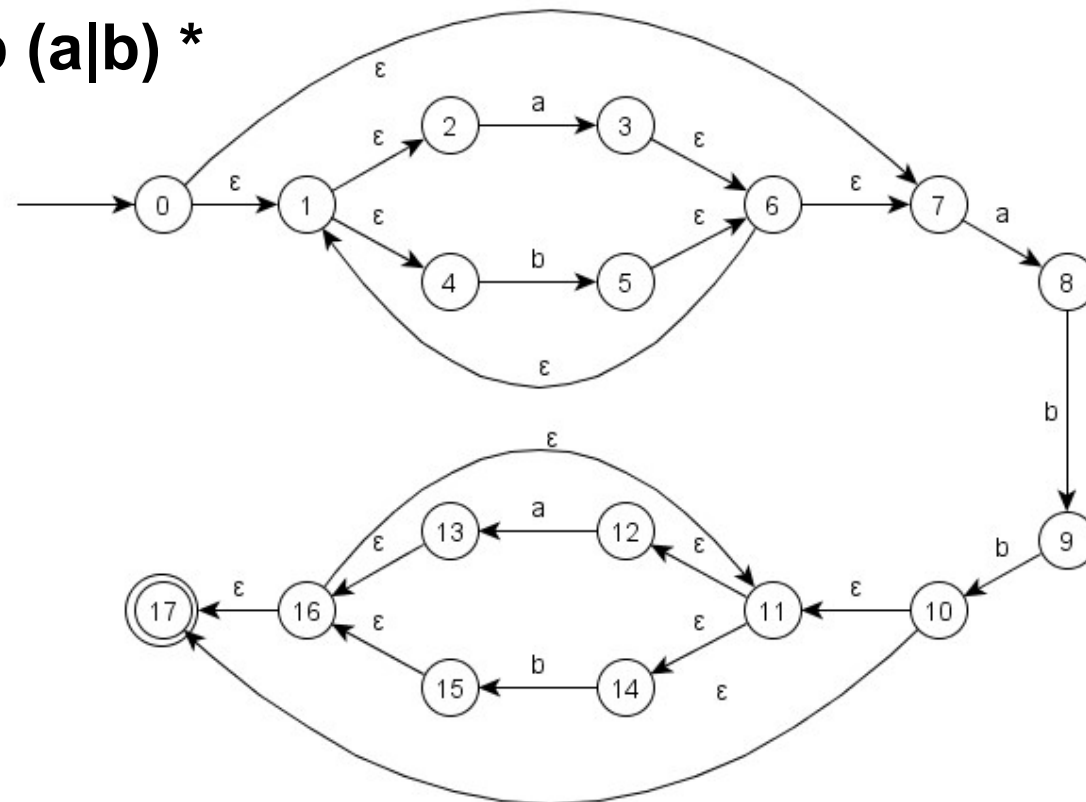
## Week 3 作业

- **教材P105 3.7.3(4) : Convert the following regular expressions to deterministic finite automata, using algorithms 3.23 and 3.20**
  - 4)  $(a|b)^*abb(a|b)^*$

## Week 3 作业

■  $(a|b)^* abb (a|b)^*$

■ NFA



## Week 3 作业

### ■ $(a|b)^* abb (a|b)^*$

#### ■ Transition table

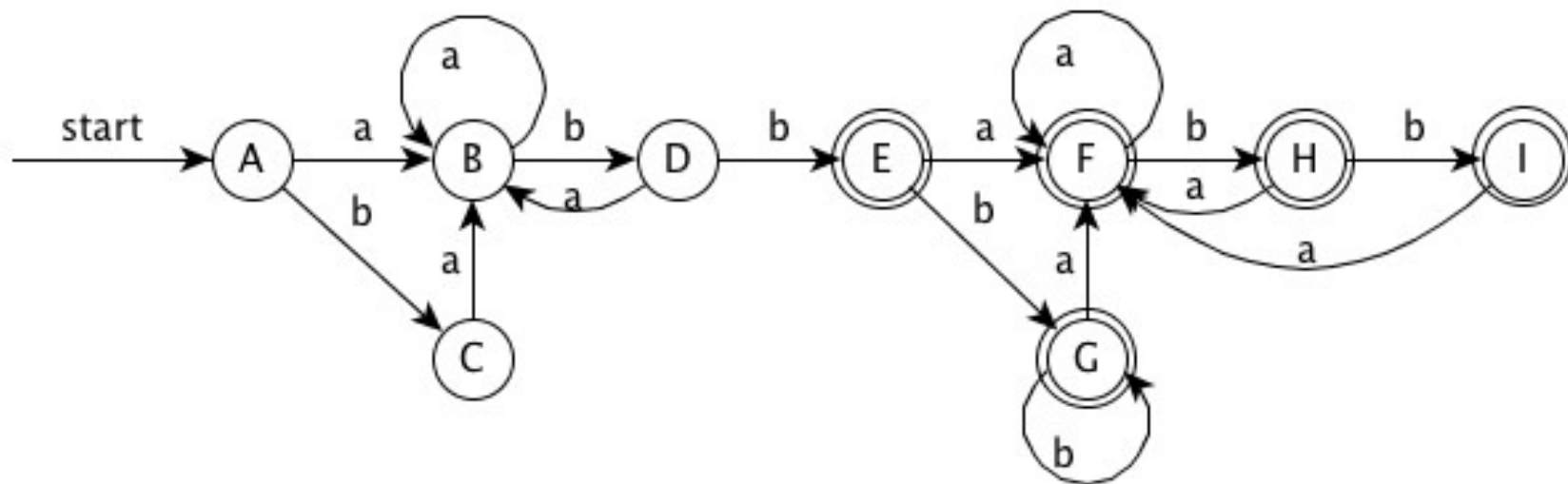
NFA State	DFA State	a	b
{0,1,2,4,7}	A	B	C
{1,2,3,4,6,7,8}	B	B	D
{1,2,4,5,6,7}	C	B	C
{1,2,4,5,6,7,9}	D	B	E
{1,2,4,5,6,7,10,11,12,14,17}	E	F	G
{1,2,3,4,6,7,8,11,12,13,14,16,17}	F	F	H
{1,2,4,5,6,7,11,12,13,15,16,17}	G	F	G
{1,2,4,5,6,7,9,11,12,14,15,16,17}	H	F	I
{1,2,4,5,6,7,10,11,12,14,15,16,17}	I	F	G



## Week 3 作业

■  $(a|b)^* abb (a|b)^*$

■ DFA



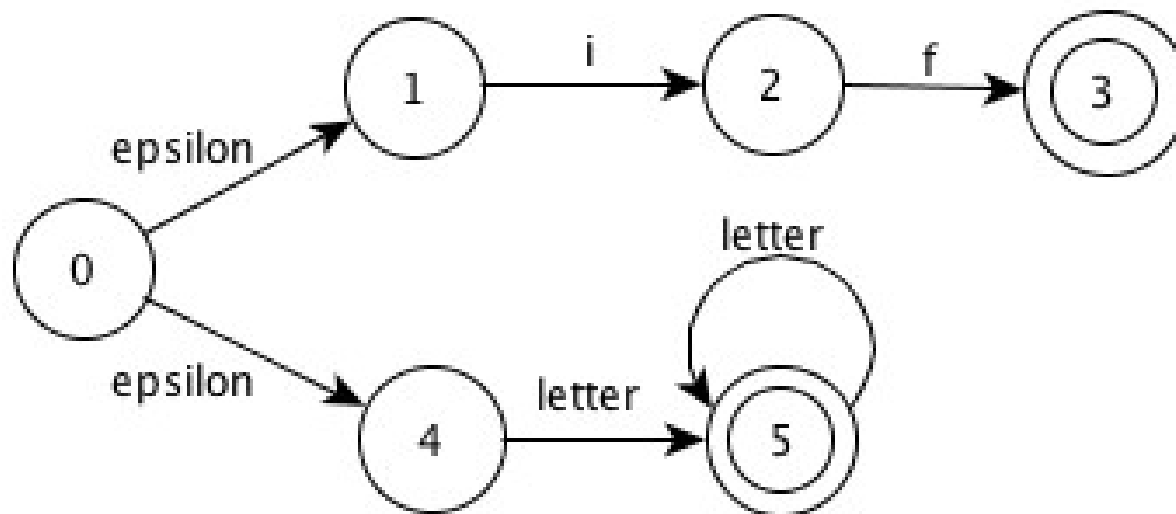
## Week 3 作业

- **教材P109 3.8.1** : Suppose we have two tokens: (1) the keyword `if` , and (2) identifiers, which are strings of letters other than `i` `f` . Show:
  - a) The NFA for these tokens, and
  - b) The DFA for these tokens.

## Week 3 作业

### ■ The NFA for these tokens.

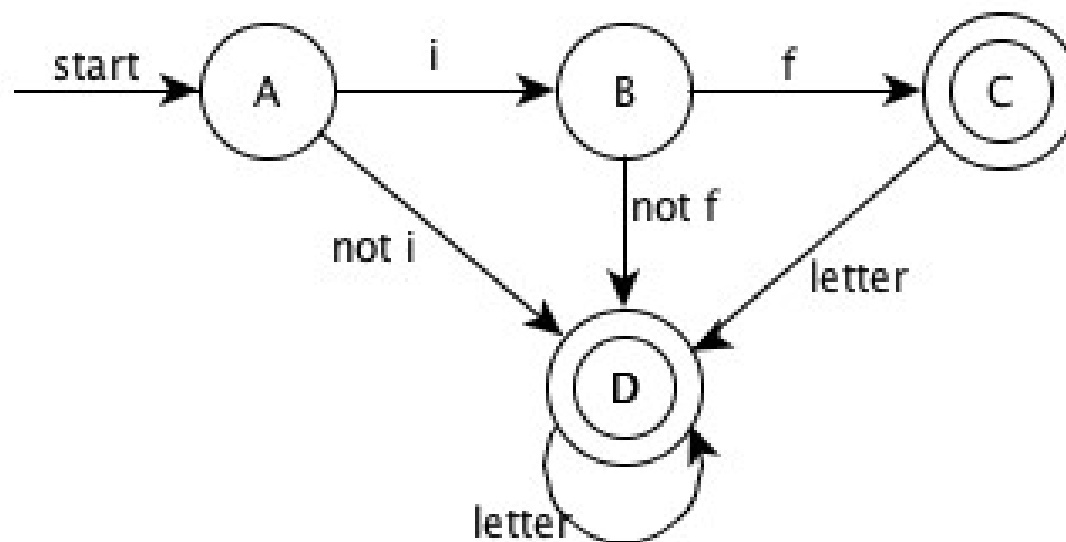
- NOTE: this NFA has potential conflict, we can decide the matched lexeme by 1. take the longest 2. take the first listed.





## Week 3 作业

### ■ The DFA for these tokens.



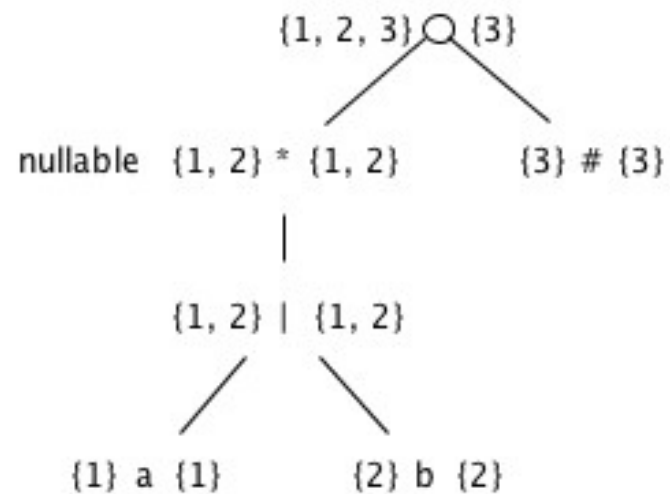
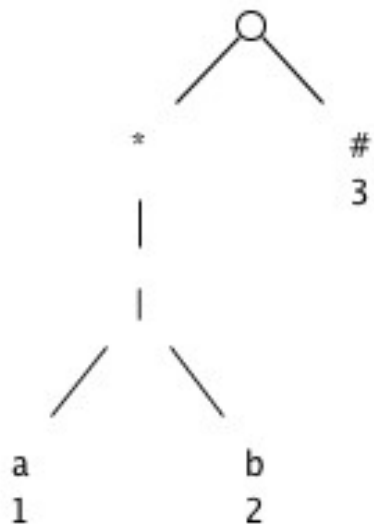
## Week 3 作业

- **教材P118 3.9.3** : We can prove that two regular expressions are equivalent by showing that their minimum-state DFA's are the same up to renaming of states. Show in this way that the following regular expressions:  $(a|b)^*$ ,  $(a^*|b^*)^*$ , and  $((\epsilon|a)b^*)^*$  are all equivalent. (**Algorithm 3.36**)

## Week 3 作业

### ■ $(a|b)^*$

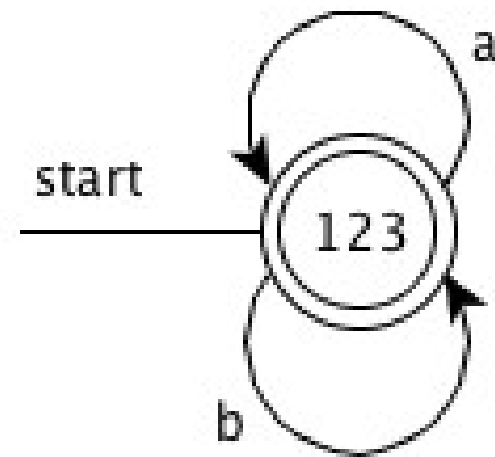
#### ■ Syntax tree



## Week 3 作业

### ■ $(a|b)^*$

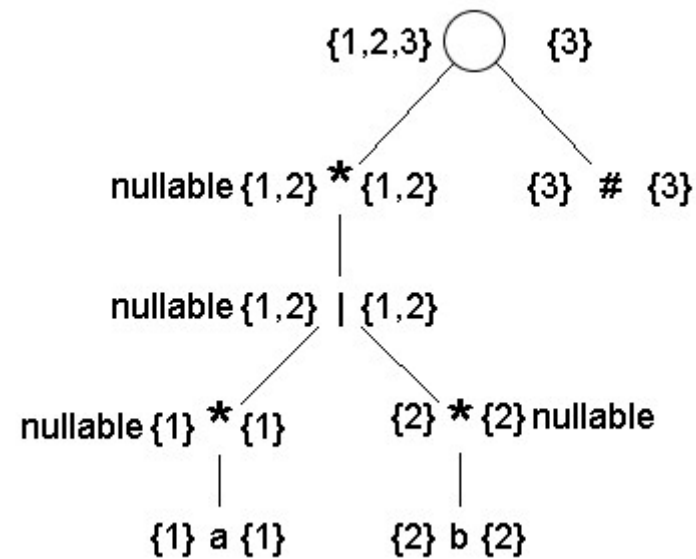
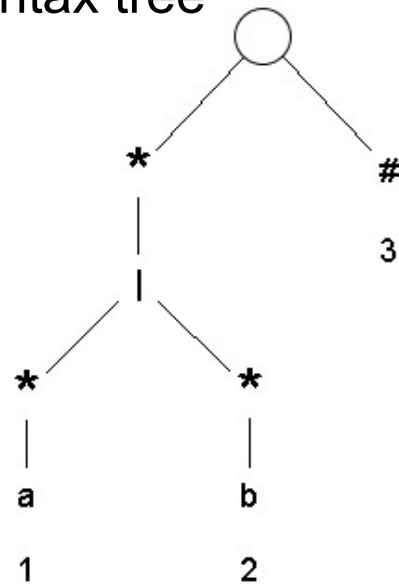
node n	followpos(n)
1	{1, 2, 3}
2	{1, 2, 3}
3	$\emptyset$



## Week 3 作业

### ■ $(a^* | b^*)^*$

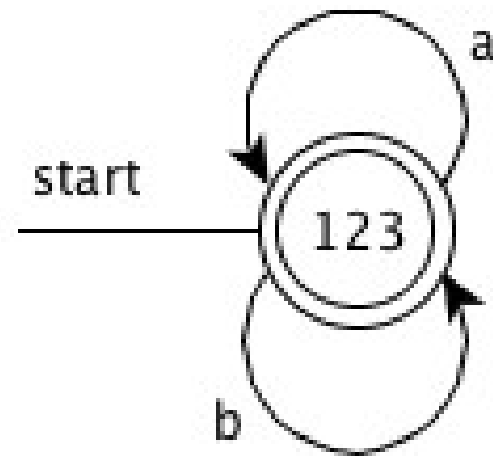
#### ■ Syntax tree



## Week 3 作业

### ■ $(a^* | b^*)^*$

node n	followpos(n)
1	{1, 2, 3}
2	{1, 2, 3}
3	$\emptyset$

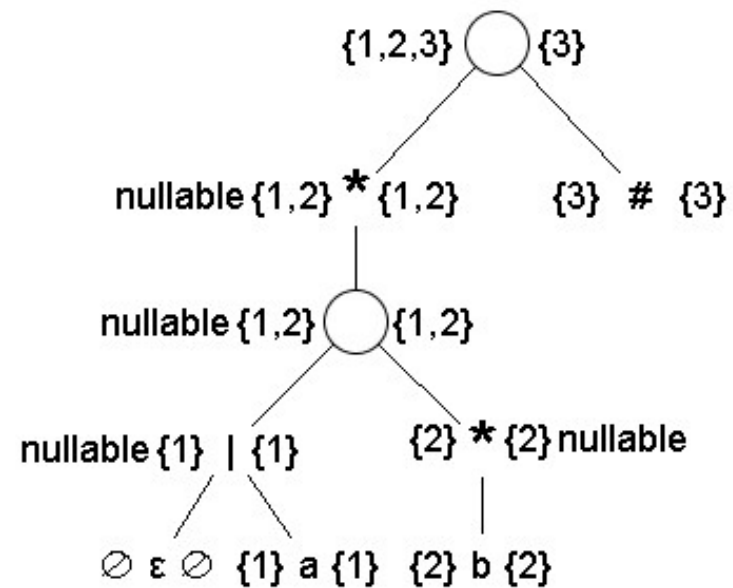
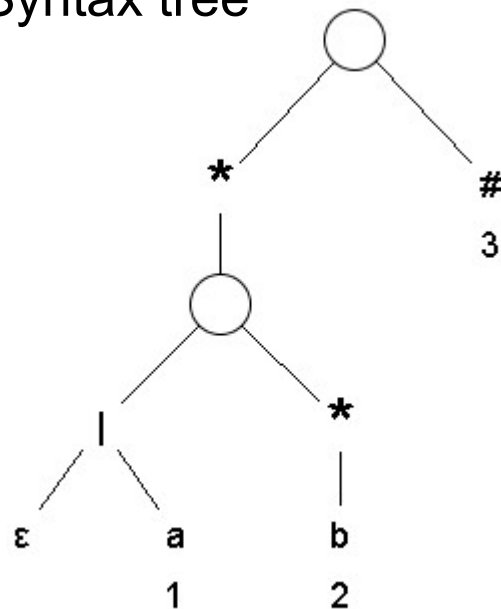




## Week 3 作业

### ■ $((\epsilon | a)b^*)^*$

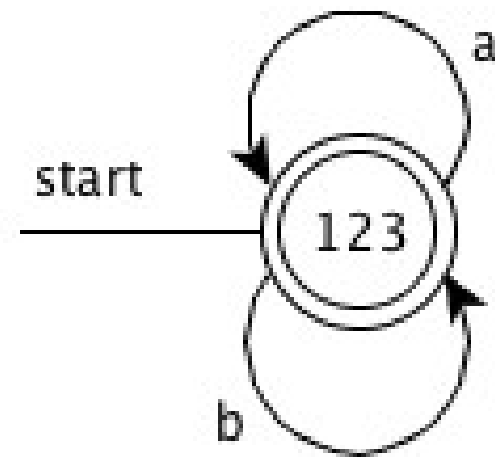
#### ■ Syntax tree



## Week 3 作业

### ■ $((\epsilon | a)b^*)^*$

node n	followpos(n)
1	{1, 2, 3}
2	{1, 2, 3}
3	$\emptyset$



## Week 3 作业

- **教材P109 3.8.1** : Construct the minimum-state DFA's for the following regular expressions:

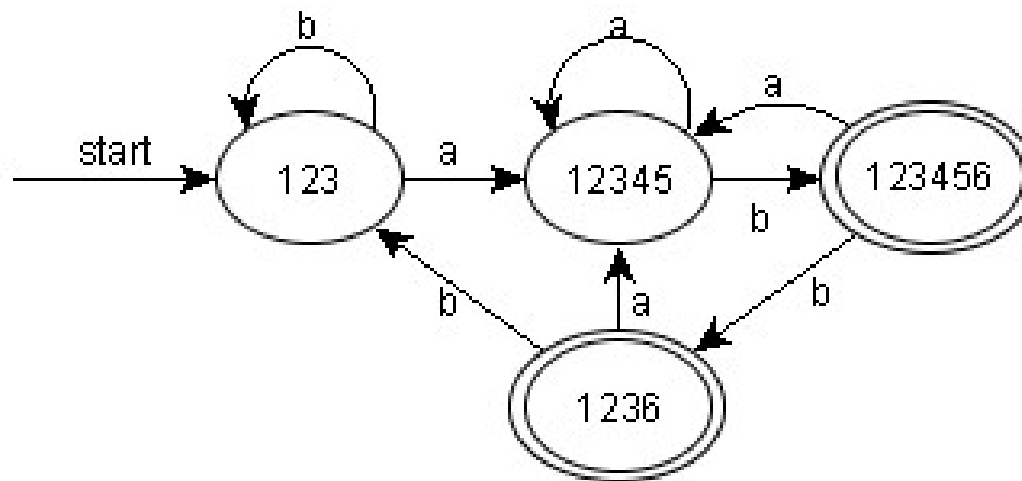
- 1.  $(a|b)^*a(a|b)$
- 2.  $(a|b)^*a(a|b)(a|b)$
- 3.  $(a|b)^*a(a|b)(a|b)(a|b)$

Do you see a pattern?

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### ■ $(a|b)^*a(a|b)$

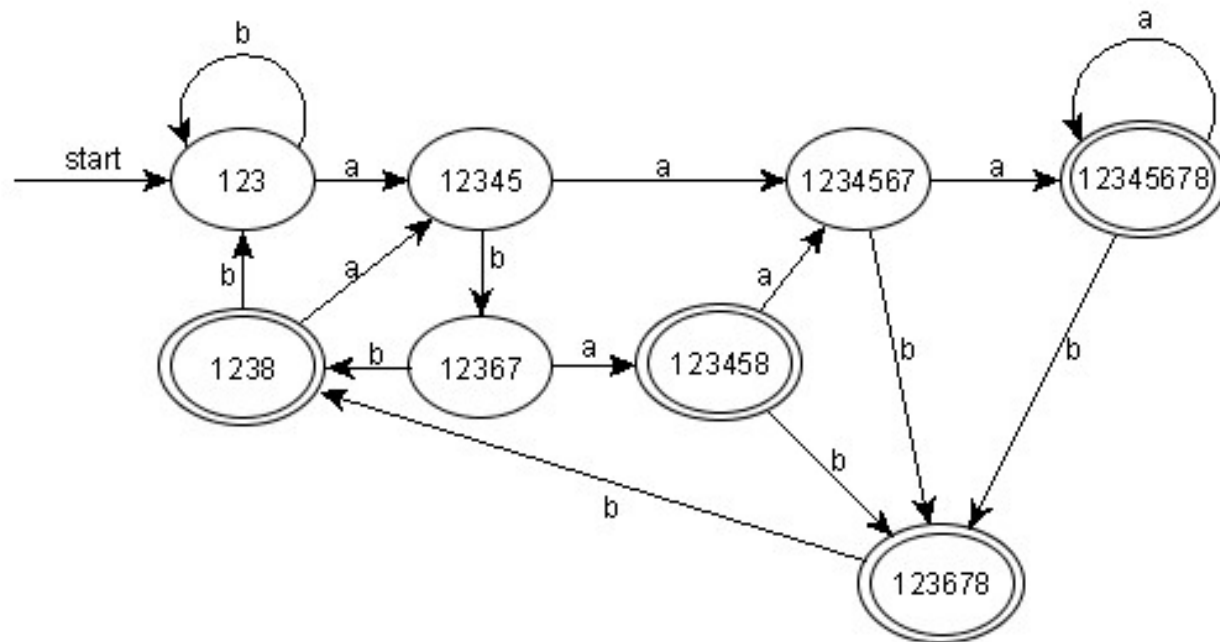
#### ■ 4个状态



## Week 3 作业

### ■ $(a|b)^*a(a|b)(a|b)$

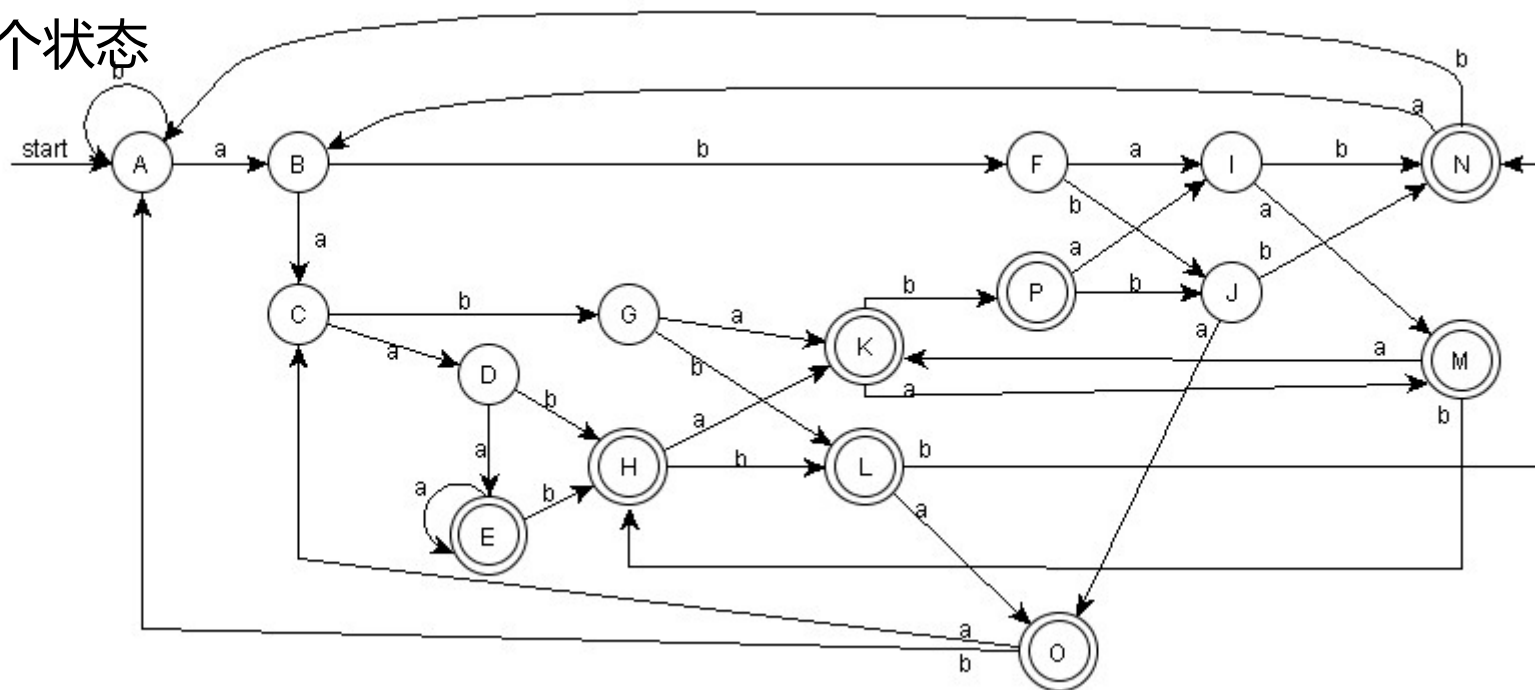
#### ■ 8个状态



## Week 3 作业

### ■ $(a|b)^*a(a|b)(a|b)(a|b)$

#### ■ 16个状态







*Thank you!*