

$$8. L = \{ a^n b^m c^k \mid n \geq m \geq k \geq 0 \}$$

~~Pick~~

Assume L is a CFL. That means I can pick

a word $w = a^p b^p c^p$. $|w| \geq p$

where p is the same pumping length.

~~From the~~

From the pumping lemma, $w = uvxyz$
where

$$(1) |vxy| \leq p$$

$$(2) v \neq \epsilon \text{ or } y \neq \epsilon$$

$$(3) \forall n, uv^n x y^n z \in L.$$

(n is whole
#)

8 (cont):

Case 1: $|vxy|$ consists only of a's:

→ pump down, resulting in $a^0 b^p c^p \notin L$

Case 2: $|vxy|$ consists only of b's:

→ pump down, resulting in $a^p b^0 c^p \notin L$

Case 3: $|vxy|$ consists only of c's

→ pump up, resulting in $a^p b^p c^{2p} \notin L$.

Case 4: $|vxy|$ consists of b's & c's

→ pump up, resulting in $a^p b^{2p} c^{2p} \notin L$

Case 5: $|vxy|$ consists of a's & b's

→ pump down, resulting in $a^0 b^0 c^p \notin L$.

$|vxy| \neq \varepsilon$ (by 2) & $|vxy| \neq$ a's & c's (by 1).

∴ w cannot be pumped.

→ ∴ L is not context-free.