

## Adaptive Mesh Refinement

Generated by Doxygen 1.8.13

## Contents

### 1 Hierarchical Index

#### 1.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

<b>AdaptiveMeshRefinement</b> < SC, LO, GO, NO >	??
<b>ErrorEstimation</b> < SC, LO, GO, NO > ExporterParaView	??
<b>ExporterParaViewAMR</b> < SC, LO, GO, NO > MeshUnstructured	??
<b>RefinementFactory</b> < SC, LO, GO, NO >	??

### 2 Data Structure Index

#### 2.1 Data Structures

Here are the data structures with brief descriptions:

<b>AdaptiveMeshRefinement</b> < SC, LO, GO, NO >	??
<b>ErrorEstimation</b> < SC, LO, GO, NO >	??
<b>ExporterParaViewAMR</b> < SC, LO, GO, NO >	??
<b>RefinementFactory</b> < SC, LO, GO, NO >	??

### 3 Namespace Documentation

#### 3.1 FEDD Namespace Reference

##### Data Structures

- class [AdaptiveMeshRefinement](#)
- class [ErrorEstimation](#)
- class [ExporterParaViewAMR](#)
- class [RefinementFactory](#)

### 3.1.1 Detailed Description

RefinementFactory.

ExporterParaView.

ErrorEstimation.

Declaration of Adaptive Mesh Refinement

#### Author

Lea Saßmannshausen

Declaration of ErrorEstimation

#### Author

Lea Saßmannshausen

#### Version

1.0

#### Copyright

CH

Declaration of ExporterParaViewAMR

#### Author

Lea Saßmannshausen

Declaration of RefinementFactory

#### Author

Lea Saßmannshausen

#### Version

1.0

#### Copyright

CH

## 4 Data Structure Documentation

### 4.1 AdaptiveMeshRefinement< SC, LO, GO, NO > Class Template Reference

#### Public Types

- typedef Mesh< SC, LO, GO, NO > **Mesh\_Type**
- typedef MeshUnstructured< SC, LO, GO, NO > **MeshUnstr\_Type**
- typedef Teuchos::RCP< MeshUnstructured< SC, LO, GO, NO > > **MeshUnstrPtr\_Type**
- typedef std::vector< MeshUnstrPtr\_Type > **MeshUnstrPtrArray\_Type**
- typedef MeshUnstructuredRefinement< SC, LO, GO, NO > **MeshUnstrRef\_Type**
- typedef Teuchos::RCP< MeshUnstrRef\_Type > **MeshUnstrRefPtr\_Type**
- typedef std::vector< MeshUnstrRefPtr\_Type > **MeshUnstrRefPtrArray\_Type**
- typedef Mesh\_Type::CommPtr\_Type **CommPtr\_Type**
- typedef Mesh\_Type::CommConstPtr\_Type **CommConstPtr\_Type**
- typedef Elements **Elements\_Type**
- typedef Teuchos::RCP< Elements\_Type > **ElementsPtr\_Type**
- typedef SurfaceElements **SurfaceElements\_Type**
- typedef Teuchos::RCP< SurfaceElements\_Type > **SurfaceElementsPtr\_Type**
- typedef EdgeElements **EdgeElements\_Type**
- typedef Teuchos::RCP< EdgeElements\_Type > **EdgeElementsPtr\_Type**
- typedef MeshInterface< SC, LO, GO, NO > **MeshInterface\_Type**
- typedef Teuchos::RCP< MeshInterface\_Type > **MeshInterfacePtr\_Type**
- typedef Map< LO, GO, NO > **Map\_Type**
- typedef Map\_Type::MapPtr\_Type **MapPtr\_Type**
- typedef Map\_Type::MapConstPtr\_Type **MapConstPtr\_Type**
- typedef MultiVector< SC, LO, GO, NO > **MultiVector\_Type**
- typedef Teuchos::RCP< MultiVector\_Type > **MultiVectorPtr\_Type**
- typedef MultiVector< LO, LO, GO, NO > **MultiVectorLO\_Type**
- typedef Teuchos::RCP< MultiVectorLO\_Type > **MultiVectorLOPtr\_Type**
- typedef MultiVector< GO, LO, GO, NO > **MultiVectorGO\_Type**
- typedef Teuchos::RCP< MultiVectorGO\_Type > **MultiVectorGOPtr\_Type**
- typedef Teuchos::RCP< const MultiVector\_Type > **MultiVectorConstPtr\_Type**
- typedef Teuchos::OrdinalTraits< LO > **OTLO**
- typedef Matrix< SC, LO, GO, NO > **Matrix\_Type**
- typedef Teuchos::RCP< Matrix\_Type > **MatrixPtr\_Type**
- typedef [ExporterParaViewAMR](#)< SC, LO, GO, NO > **Exporter\_Type**
- typedef Teuchos::RCP< [Exporter\\_Type](#) > **ExporterPtr\_Type**
- typedef Teuchos::RCP< ExporterTxt > **ExporterTxtPtr\_Type**
- typedef Problem< SC, LO, GO, NO > **Problem\_Type**
- typedef Teuchos::RCP< Problem\_Type > **ProblemPtr\_Type**
- typedef Domain< SC, LO, GO, NO > **Domain\_Type**
- typedef Teuchos::RCP< Domain\_Type > **DomainPtr\_Type**
- typedef std::vector< DomainPtr\_Type > **DomainPtrArray\_Type**
- typedef std::vector< MultiVectorPtr\_Type > **MultiVectorPtrArray\_Type**
- typedef BlockMultiVector< SC, LO, GO, NO > **BlockMultiVector\_Type**
- typedef Teuchos::RCP< BlockMultiVector\_Type > **BlockMultiVectorPtr\_Type**
- typedef Teuchos::RCP< const BlockMultiVector\_Type > **BlockMultiVectorConstPtr\_Type**

## Public Member Functions

- [AdaptiveMeshRefinement](#) (string problemType, ParameterListPtr\_Type parameterListAll)
- [AdaptiveMeshRefinement](#) (string problemType, ParameterListPtr\_Type parameterListAll, Func\_Type exactSolFunc)
- DomainPtr\_Type [globalAlgorithm](#) (DomainPtr\_Type domainP1, DomainPtr\_Type domainP12, BlockMultiVectorConstPtr\_Type solution, ProblemPtr\_Type problem, RhsFunc\_Type rhsFunc)
- DomainPtr\_Type [refineArea](#) (DomainPtr\_Type domainP1, vec2D\_dbl\_Type area, int level)
- MultiVectorConstPtr\_Type [calcExactSolution](#) ()
- void [identifyProblem](#) (BlockMultiVectorConstPtr\_Type valuesSolution)
- void [calcErrorNorms](#) (MultiVectorConstPtr\_Type exactSolution, MultiVectorConstPtr\_Type solutionP12)
- void [initExporter](#) (ParameterListPtr\_Type parameterListAll)
- void [exportSolution](#) (MeshUnstrPtr\_Type mesh, MultiVectorConstPtr\_Type exportSolutionMv, MultiVectorConstPtr\_Type errorValues, MultiVectorConstPtr\_Type exactSolutionMv)
- void [exportError](#) (MeshUnstrPtr\_Type mesh, MultiVectorConstPtr\_Type errorElConst, MultiVectorConstPtr\_Type vecDecompositionConst)
- void [writeRefinementInfo](#) ()
- void [buildSurfaceTriangleElements](#) (ElementsPtr\_Type elements, EdgeElementsPtr\_Type edgeElements, SurfaceElementsPtr\_Type surfaceTriangleElements)
- vec\_bool\_Type [checkInterfaceSurface](#) (EdgeElementsPtr\_Type edgeElements, vec\_int\_Type originFlag, vec\_int\_Type edgeNumbers, int indexElement)

## Private Attributes

- RhsFunc\_Type [rhsFunc\\_](#)
- Func\_Type [exactSolFunc\\_](#)
- MeshUnstrPtr\_Type [inputMeshP1\\_](#)
- MeshUnstrPtr\_Type [inputMeshP12\\_](#)
- MeshUnstrPtr\_Type [outputMesh\\_](#)
- MultiVectorPtrArray\_Type [errorEstimationMv\\_](#)
- MultiVectorPtr\_Type [errorElementsMv\\_](#)
- MultiVectorConstPtr\_Type [errorNodesMv\\_](#)
- BlockMultiVectorConstPtr\_Type [solution\\_](#)
- CommConstPtr\_Type [comm\\_](#)
- bool [exportWithParaview\\_](#) = true
- bool [initExporter\\_](#) = false
- ExporterPtr\_Type [exporterSol\\_](#)
- ExporterPtr\_Type [exporterError\\_](#)
- DomainPtrArray\_Type [domainsP1\\_](#)
- DomainPtrArray\_Type [domainsP12\\_](#)
- DomainPtr\_Type [domainP1\\_](#)
- DomainPtr\_Type [domainP12\\_](#)
- ProblemPtr\_Type [problem\\_](#)
- string [refinementRestriction\\_](#) = "keepRegularity"
- string [markingStrategy\\_](#) = "Maximum"
- double [theta\\_](#) = 0.5
- double [tol\\_](#) = 0.001
- bool [meshQualityPrint\\_](#) = "false"
- bool [timeTablePrint\\_](#) = "false"
- int [refinement3DDiagonal\\_](#) = 0
- string [problemType\\_](#)
- int [dim\\_](#)
- int [currentIter\\_](#)
- int [maxIter\\_](#) = 5

- int **maxRank\_**
- string **FType1\_**
- string **FType2\_**
- vec\_dbl\_Type **maxErrorEl**
- vec\_dbl\_Type **maxErrorKn**
- vec\_int\_Type **numElements**
- vec\_int\_Type **numElementsProc**
- vec\_dbl\_Type **relError**
- vec\_dbl\_Type **eRelError**
- vec\_dbl\_Type **errorH1**
- vec\_dbl\_Type **errorL2**
- vec\_int\_Type **numNodes**
- bool **writeRefinementTime\_** = true
- bool **writeMeshQuality\_** = true
- ParameterListPtr\_Type **parameterListAll\_**
- int **dofs\_**
- int **dofsP\_**

#### 4.1.1 Constructor & Destructor Documentation

##### 4.1.1.1 AdaptiveMeshRefinement() [1/2]

```
AdaptiveMeshRefinement (
    string problemType,
    ParameterListPtr_Type parameterListAll )
```

Initializing problem with the kind of problem (e.g. Laplace, Stokes) for determining the correct error estimation and the dimension

##### Parameters

in	<i>problemType</i> , <i>dim</i>	
----	---------------------------------	--

##### 4.1.1.2 AdaptiveMeshRefinement() [2/2]

```
AdaptiveMeshRefinement (
    string problemType,
    ParameterListPtr_Type parameterListAll,
    Func_Type exactSolFunc )
```

Initializing problem with the kind of problem, dimension and refinement specific parameters

#### 4.1.2 Member Function Documentation

#### 4.1.2.1 calcErrorNorms()

```
void calcErrorNorms (
    MultiVectorConstPtr_Type exactSolution,
    MultiVectorConstPtr_Type solutionPl2 )
```

Calculating error norms. If the exact solution is unknown we use approximated errorNorm and error indicators

##### Parameters

in	<i>exact</i>	solution if known
in	<i>FE</i>	solution
in	<i>error</i>	estimation

#### 4.1.2.2 exportError()

```
void exportError (
    MeshUnstrPtr_Type mesh,
    MultiVectorConstPtr_Type errorElConst,
    MultiVectorConstPtr_Type vecDecompositionConst )
```

ParaView exporter export of error values and element distribution on current mesh

#### 4.1.2.3 exportSolution()

```
void exportSolution (
    MeshUnstrPtr_Type mesh,
    MultiVectorConstPtr_Type exportSolutionMv,
    MultiVectorConstPtr_Type errorValues,
    MultiVectorConstPtr_Type exactSolutionMv )
```

ParaView exporter export of solution on current mesh

#### 4.1.2.4 globalAlgorithm()

```
AdaptiveMeshRefinement< SC, LO, GO, NO >::DomainPtr_Type globalAlgorithm (
    DomainPtr_Type domainPl,
    DomainPtr_Type domainPl2,
    BlockMultiVectorConstPtr_Type solution,
    ProblemPtr_Type problem,
    RhsFunc_Type rhsFunc )
```

Global Algorithm of Mesh Refinement.

Given domains and solutions depending on problem global mesh refinement algorithm and error estimation is performed

i.e. if to solve simple laplace problem, we have only one solution to put in, if to estimate error for Navier-Stokes equation we need pressure and velocity solution

## Parameters

in	<i>domainP1</i>	domain with P1 discretization, always necessary as refinement is performed on P1 Mesh
in	<i>domainP12</i>	domain with P1 or P2 discretization if available, otherwise input domainP1
in	<i>solution1</i>	solution of problem on P1 or P2 discretization
in	<i>solution2</i>	solution of problem on P1 or P2 discretization if available, otherwise input solutionP1

## 4.1.2.5 initExporter()

```
void initExporter (
    ParameterListPtr_Type parameterListAll )
```

ParaView exporter setup

## 4.1.2.6 writeRefinementInfo()

```
void writeRefinementInfo ( )
```

Writing refinement information

The documentation for this class was generated from the following files:

- AdaptiveMeshRefinement\_decl.hpp
- AdaptiveMeshRefinement\_def.hpp

## 4.2 ErrorEstimation&lt; SC, LO, GO, NO &gt; Class Template Reference

## Public Types

- typedef Mesh< SC, LO, GO, NO > **Mesh\_Type**
- typedef Teuchos::RCP< MeshUnstructured< SC, LO, GO, NO > > **MeshUnstrPtr\_Type**
- typedef std::vector< MeshUnstrPtr\_Type > **MeshUnstrPtrArray\_Type**
- typedef Mesh\_Type::CommPtr\_Type **CommPtr\_Type**
- typedef Mesh\_Type::CommConstPtr\_Type **CommConstPtr\_Type**
- typedef Mesh\_Type::Elements\_Type **Elements\_Type**
- typedef Mesh\_Type::ElementsPtr\_Type **ElementsPtr\_Type**
- typedef EdgeElements **EdgeElements\_Type**
- typedef Teuchos::RCP< EdgeElements\_Type > **EdgeElementsPtr\_Type**
- typedef SurfaceElements **SurfaceElements\_Type**
- typedef Teuchos::RCP< SurfaceElements\_Type > **SurfaceElementsPtr\_Type**
- typedef MeshInterface< SC, LO, GO, NO > **MeshInterface\_Type**
- typedef Teuchos::RCP< MeshInterface\_Type > **MeshInterfacePtr\_Type**
- typedef Map< LO, GO, NO > **Map\_Type**
- typedef Map\_Type::MapPtr\_Type **MapPtr\_Type**
- typedef Map\_Type::MapConstPtr\_Type **MapConstPtr\_Type**
- typedef MultiVector< SC, LO, GO, NO > **MultiVector\_Type**
- typedef Teuchos::RCP< MultiVector\_Type > **MultiVectorPtr\_Type**
- typedef MultiVector< LO, LO, GO, NO > **MultiVectorLO\_Type**
- typedef Teuchos::RCP< MultiVectorLO\_Type > **MultiVectorLOPtr\_Type**
- typedef MultiVector< GO, LO, GO, NO > **MultiVectorGO\_Type**
- typedef Teuchos::RCP< MultiVectorGO\_Type > **MultiVectorGOPtr\_Type**
- typedef Teuchos::RCP< const MultiVector\_Type > **MultiVectorConstPtr\_Type**
- typedef Teuchos::OrdinalTraits< LO > **OTLO**
- typedef Matrix< SC, LO, GO, NO > **Matrix\_Type**
- typedef Teuchos::RCP< Matrix\_Type > **MatrixPtr\_Type**
- typedef BlockMultiVector< SC, LO, GO, NO > **BlockMultiVector\_Type**
- typedef Teuchos::RCP< BlockMultiVector\_Type > **BlockMultiVectorPtr\_Type**
- typedef Teuchos::RCP< const BlockMultiVector\_Type > **BlockMultiVectorConstPtr\_Type**



## Public Member Functions

- **ErrorEstimation** (int dim, string problemType)
- MultiVectorPtr\_Type **estimateError** (MeshUnstrPtr\_Type inputMeshP12, MeshUnstrPtr\_Type inputMeshP1, BlockMultiVectorConstPtr\_Type valuesSolution, RhsFunc\_Type rhsFunc, string FEType)
- void **identifyProblem** (BlockMultiVectorConstPtr\_Type valuesSolution)
- void **makeRepeatedSolution** (BlockMultiVectorConstPtr\_Type valuesSolution)
- vec3D\_dbl\_Type **calcNPhi** (string phiDerivative, int dofsSol, string FEType)
- vec\_dbl\_Type **calculateJump** ()
- vec2D\_dbl\_Type **gradPhi** (int dim, int intFE, vec\_dbl\_Type &p)
- vec\_dbl\_Type **phi** (int dim, int intFE, vec\_dbl\_Type &p)
- vec\_dbl\_Type **divPhi** (int dim, int intFE, vec\_dbl\_Type &p)
- MultiVectorPtr\_Type **determineCoarseningError** (MeshUnstrPtr\_Type mesh\_k, MeshUnstrPtr\_Type mesh\_k\_m, MultiVectorPtr\_Type errorElementMv\_k, string distribution, string markingStrategy, double theta)
- double **determineResElement** (FiniteElement element, RhsFunc\_Type rhsFunc)
- double **determineDivU** (FiniteElement element)
- vec2D\_dbl\_Type **getQuadValues** (int dim, string FEType, string Type, vec\_dbl\_Type &QuadW, FiniteElement surface)
- void **markElements** (MultiVectorPtr\_Type errorElementMv, double theta, string strategy, MeshUnstrPtr\_Type meshUnstr)
- vec\_dbl\_Type **determineH\_T\_min** (ElementsPtr\_Type elements, EdgeElementsPtr\_Type edgeElements, vec2D\_dbl\_ptr\_Type points, vec\_dbl\_Type &volTetraeder)
- vec\_dbl\_Type **calcDiamElements** (ElementsPtr\_Type elements, vec2D\_dbl\_ptr\_Type points)
- vec\_dbl\_Type **determineAreaTriangles** (ElementsPtr\_Type elements, EdgeElementsPtr\_Type edgeElements, SurfaceElementsPtr\_Type surfaceElements, vec2D\_dbl\_ptr\_Type points)
- void **buildTriangleMap** ()
- void **updateElementsOfSurfaceLocalAndGlobal** (EdgeElementsPtr\_Type edgeElements, SurfaceElementsPtr\_Type surfaceTriangleElements)
- void **setErrorEstimate** (MultiVectorPtr\_Type errorElements)
- MultiVectorPtr\_Type **getErrorEstimate** ()
- void **tagArea** (MeshUnstrPtr\_Type meshUnstr, vec2D\_dbl\_Type area)

## Data Fields

- string **refinementRestriction\_** = "none"
- string **markingStrategy\_** = "Maximum"
- double **theta\_** = 0.5
- bool **meshQualityPrint\_** = "false"
- bool **timeTablePrint\_** = "false"
- int **refinement3DDiagonal\_** = 0
- int **dim\_**
- string **problemType\_**

## Protected Attributes

- vec\_GO\_Type **globalInterfaceIDs\_**
- MultiVectorPtr\_Type **errorEstimation\_**
- vec\_dbl\_Type **areaTriangles\_**
- vec\_dbl\_Type **volTetraeders\_**
- vec\_dbl\_Type **h\_T\_diam\_E\_**
- vec\_dbl\_Type **h\_T\_min\_**
- MapConstPtr\_Type **surfaceTriangleMap\_**
- SurfaceElementsPtr\_Type **surfaceElements\_**
- int **dofs\_**
- int **dofsP\_**
- bool **calculatePressure\_** = false
- BlockMultiVectorConstPtr\_Type **valuesSolutionRepVel\_**
- BlockMultiVectorConstPtr\_Type **valuesSolutionRepPre\_**

## Private Attributes

- MeshUnstrPtr\_Type **inputMesh\_**
- MeshUnstrPtr\_Type **inputMeshP1\_**
- string **FType1\_**
- string **FType2\_**

## 4.2.1 Member Function Documentation

## 4.2.1.1 calcDiamElements()

```
vec_dbl_Type calcDiamElements (
    ElementsPtr_Type elements,
    vec2D_dbl_ptr_Type points )
```

Calculating the diameter of elements. This is necessary for 2D A-posteriori error estimation.

## Parameters

in	<i>elements</i>	
in	<i>points</i>	

## 4.2.1.2 calcNPhi()

```
vec3D_dbl_Type calcNPhi (
    string phiDerivative,
    int dofsSol,
    string FType )
```

Function that calculates the jump part for nabla u or p.

## Parameters

in	<i>phiDerivative</i>	is either 'Gradient' or 'None' and what kind of jump is calculated depends on the problemType we have at hand. If phiDerivative is 'Gradient' the nabla u jump part is calculated and if its 'None' then the p-
in	<i>dofsSol</i>	is the degree of freedom of the calculated jump part. p's dof is typically 1 whereas u's dof can vary depending on the problem
in	<i>FType</i>	of the calculated jump part.

## 4.2.1.3 calculateJump()

```
vec_dbl_Type calculateJump ( )
```

Part of the error estimator that calculates the jump part of the estimation.

**Parameters**

in	<i>none,as</i>	all necessary parameters for the calculation are already part of the Error estimation class.
----	----------------	--

What kind of jump is calculated depends on the `problemType` we have at hand.

**4.2.1.4 determineAreaTriangles()**

```
vec_dbl_Type determineAreaTriangles (
    ElementsPtr_Type elements,
    EdgeElementsPtr_Type edgeElements,
    SurfaceElementsPtr_Type surfaceElements,
    vec2D_dbl_ptr_Type points )
```

Calculating the area of the triangle elements of tetrahedra.

**Parameters**

in	<i>elements</i>	
in	<i>edgeElements</i>	
in	<i>surfaceElements</i>	
in	<i>points</i>	

**4.2.1.5 determineCoarseningError()**

```
ErrorEstimation< SC, LO, GO, NO >::MultiVectorPtr_Type determineCoarseningError (
    MeshUnstrPtr_Type mesh_k,
    MeshUnstrPtr_Type mesh_k_m,
    MultiVectorPtr_Type errorElementMv_k,
    string distribution,
    string markingStrategy,
    double theta )
```

`determineCoarseningError` is the essential part of the mesh coarsening process.

instead of calculating a error of mesh level  $k$ , we redistribute it to lower mesh levels and defining those.// We execute this function with an estimated error from the above 'estimateCoarseningError' function. With this error, we mark the elements according to that error and refine afterwards If we decide to coarsen a certain mesh level, we take that level, look at the  $k-m$  level and refine that to the point where we are at the same level we wanted to perform the coarsening on

**Parameters**

in	<i>mesh_k</i>	the current mesh of level $k$
in	<i>mesh_k_m</i>	the mesh of refinement level $k-m$
in	<i>errorElementMv_k</i>	as the error estimation of mesh level $k$
in	<i>distribution</i>	is either 'forwards' or 'backwards'. We determine the error estimate in level $k-m$ with redistributing backwards. if we are in level $k-m$ we calculate the $k-m+1$ mesh level error estimation via redistributing the $k-m$ error forward.
in	<i>markingStrategy</i>	the strategy with which element are marked
in	<i>theta</i>	as the a marking threshold

## 4.2.1.6 determineDivU()

```
double determineDivU (
    FiniteElement element )
```

Function that that determines  $\| \text{div}(u) \|_{T}$  for a Element T.

## Parameters

in	<i>FiniteElement</i>	element where $\  \text{div}(u) \ _{T}$ is calculated on
----	----------------------	--

## 4.2.1.7 determineH\_T\_min()

```
vec_dbl_Type determineH_T_min (
    ElementsPtr_Type elements,
    EdgeElementsPtr_Type edgeElements,
    vec2D_dbl_ptr_Type points,
    vec_dbl_Type & volTetraeder )
```

function, that determines  $h_T$  as the shortest vector inside a tetraeder as propose in...

## Parameters

in	<i>elements</i>	
in	<i>edgeelements</i>	
in	<i>points</i>	
in	<i>volTetraeder</i>	is calculated along the way and also usefull at another part of 3D jump calculation

## 4.2.1.8 determineResElement()

```
double determineResElement (
    FiniteElement element,
    RhsFunc_Type rhsFunc )
```

Function that that determines  $\| u_h + f \|_{L^2(T)}$  or  $\| u_h + f - p \|_{T}$  for a Element T.

## Parameters

in	<i>FiniteElement</i>	element where $\  \text{div}(u) \ _{T}$ is calculated on
in	<i>RhsFunc_Type</i>	rhsFunc which is the function used for the rhs of the pde

#### 4.2.1.9 estimateError()

```
ErrorEstimation< SC, LO, GO, NO >::MultiVectorPtr_Type estimateError (
    MeshUnstrPtr_Type inputMeshP12,
    MeshUnstrPtr_Type inputMeshP1,
    BlockMultiVectorConstPtr_Type valuesSolution,
    RhsFunc_Type rhsFunc,
    string FETypeV )
```

Main Function for A-posteriori Error Estimation.

depending on the problem the the error estimation is calculated accordingly

##### Parameters

in	<i>inputMeshP1</i>	the P1 Mesh that is used for later refinement
in	<i>inputMeshP12</i>	the possible P2 Mesh, if one of the solutions is of P2 Discretisation, otherwise both meshes are P1
in	<i>solution</i>	of the PDE in BlockMultiVector Format (Block 0: Velocity, Block 1: Pressure)
in	<i>rhs</i>	Function
in	<i>FETypeV</i>	as the maximum FEType for the Velocity, pressure is assumed to be P1

#### 4.2.1.10 getQuadValues()

```
vec2D_dbl_Type getQuadValues (
    int dim,
    string FEType,
    string Type,
    vec_dbl_Type & QuadW,
    FiniteElement surface )
```

Returns necessary quadrature Values. Is distinguishes between needing Element or Surface information.

##### Parameters

in	<i>dim</i>	for which the quadrature points are needed
in	<i>FEType</i>	for which the quadrature points are needed
in	<i>Type</i>	of quadrature points are need. Either 'Element' if you integrate over an element or 'Surface' if you need to integrate over a surface (i.e. for calculating the jump)
in	<i>QuadW</i>	Vector to be filled with the quadrature weights accordingly
in	<i>FiniteElement</i>	surface for which you need the quadrature points in case if 'Surface' type, as it is needed for figuring out the quadrature points

#### 4.2.1.11 markElements()

```
void markElements (
    MultiVectorPtr_Type errorElementMv,
    double theta,
```

```
string strategy,
MeshUnstrPtr_Type meshP1 )
```

Function that marks the elements for refinement.

#### Parameters

in	<i>errorElementMv</i>	is the MultiVector that contains the estimated error for each element
in	<i>theta</i>	is a parameter determining a certain error bound for marking
in	<i>markingStrategy</i>	is the strategy with which the elements are marked. Implemented Strategies 'Doerfler' or 'Maximum'
in	<i>meshP1</i>	is the P1 mesh which is used for later refinement and has to be the one beeing marked

!! it is essential that the meshP1 mesh inserted here is the mesh that will be used for mesh refinement, as it contains the elementwise-information determining refinement. !!

#### 4.2.1.12 tagArea()

```
void tagArea (
    MeshUnstrPtr_Type inputMeshP1,
    vec2D_dbl_Type area )
```

Tags only a certain Area for refinement and is independent of any error estimation.

#### Parameters

in	<i>inputMeshP1</i>	the P1 Mesh that is used for later refinement
in	<i>the</i>	area, that is suppose to be refined. If is a vector defining the area as follows: row1:[x_0,x_1] x-limits, row2: [y_0,y_1] y-limits, row3: [z_0,z_1] z-limits

#### 4.2.1.13 updateElementsOfSurfaceLocalAndGlobal()

```
void updateElementsOfSurfaceLocalAndGlobal (
    EdgeElementsPtr_Type edgeElements,
    SurfaceElementsPtr_Type surfaceTriangleElements )
```

updateElementsOfSurfaceLocalAndGlobal is performed here instead of in meshRefinement, as the information is only needed in case of error estimation

#### Parameters

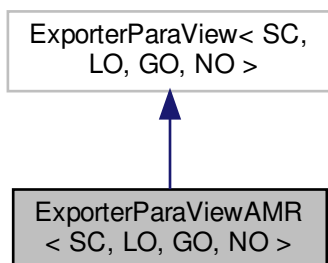
in	<i>edgeElements</i>	
in	<i>surfaceTriangleElements</i>	

The documentation for this class was generated from the following files:

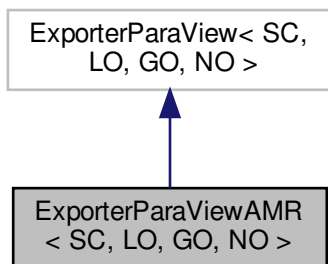
- ErrorEstimation\_decl.hpp
- ErrorEstimation\_def.hpp

### 4.3 ExporterParaViewAMR< SC, LO, GO, NO > Class Template Reference

Inheritance diagram for ExporterParaViewAMR< SC, LO, GO, NO >:



Collaboration diagram for ExporterParaViewAMR< SC, LO, GO, NO >:



#### Public Types

- typedef std::vector< double > **vec\_dbl**
- typedef std::vector< std::vector< double > > **vec2D\_dbl**
- typedef std::vector< std::vector< int > > **vec2D\_int**
- typedef std::vector< std::vector< long long > > **vec2D\_longlong**
- typedef Teuchos::RCP< std::vector< int > > **vec\_int\_ptr**
- typedef Teuchos::RCP< std::vector< long long > > **vec\_longlong\_ptr**
- typedef Teuchos::RCP< vec\_dbl > **vec\_dbl\_ptr**
- typedef Teuchos::RCP< std::vector< std::vector< double > > > **vec2D\_dbl\_ptr**
- typedef Teuchos::RCP< std::vector< std::vector< int > > > **vec2D\_int\_ptr**
- typedef Teuchos::RCP< vec2D\_longlong > **vec2D\_longlong\_ptr**
- typedef Teuchos::RCP< Epetra\_Vector > **EpetraVec\_ptr**
- typedef Teuchos::RCP< Epetra\_MpiComm > **EpetraComm\_ptr**
- typedef Teuchos::RCP< Epetra\_IntVector > **EpetraVecInt\_ptr**

- typedef Teuchos::RCP< Epetra\_LongLongVector > **EpetraVecLongLong\_ptr**
- typedef Teuchos::RCP< Epetra\_MultiVector > **EpetraMVPtr\_Type**
- typedef Teuchos::RCP< Epetra\_Map > **EpetraMapPtr\_Type**
- typedef EpetraExt::HDF5 **HDF5\_Type**
- typedef Teuchos::RCP< HDF5\_Type > **HDF5Ptr\_Type**
- typedef Teuchos::Comm< int > **Comm\_Type**
- typedef Teuchos::RCP< const Comm\_Type > **CommConstPtr\_Type**
- typedef const Teuchos::RCP< const Comm\_Type > **CommConstPtrConst\_Type**
- typedef Map< LO, GO, NO > **Map\_Type**
- typedef Teuchos::RCP< const Map\_Type > **MapConstPtr\_Type**
- typedef const MapConstPtr\_Type **MapConstPtrConst\_Type**
- typedef MultiVector< SC, LO, GO, NO > **MultiVector\_Type**
- typedef Teuchos::RCP< const MultiVector\_Type > **MultiVectorConstPtr\_Type**
- typedef const MultiVectorConstPtr\_Type **MultiVectorConstPtrConst\_Type**
- typedef Mesh< SC, LO, GO, NO > **Mesh\_Type**
- typedef Teuchos::RCP< Mesh\_Type > **MeshPtr\_Type**
- typedef Mesh\_Type::ElementsPtr\_Type **ElementsPtr\_Type**

#### Public Member Functions

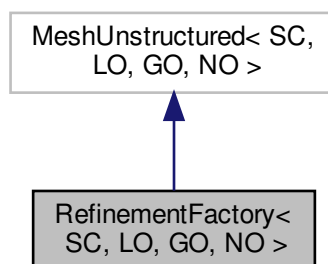
- void **updateVariables** (MultiVectorConstPtr\_Type &u, std::string varName)
- void **reSetup** (MeshPtr\_Type mesh)

The documentation for this class was generated from the following files:

- ExporterParaViewAMR\_decl.hpp
- ExporterParaViewAMR\_def.hpp

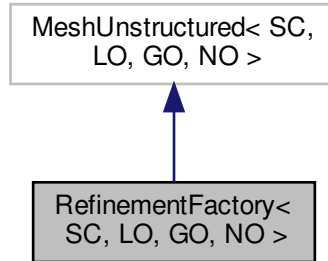
#### 4.4 RefinementFactory< SC, LO, GO, NO > Class Template Reference

Inheritance diagram for RefinementFactory< SC, LO, GO, NO >:





Collaboration diagram for RefinementFactory< SC, LO, GO, NO >:



#### Public Types

- typedef Mesh< SC, LO, GO, NO > **Mesh\_Type**
- typedef MeshUnstructured< SC, LO, GO, NO > **MeshUnstr\_Type**
- typedef Teuchos::RCP< MeshUnstructured< SC, LO, GO, NO > > **MeshUnstrPtr\_Type**
- typedef std::vector< MeshUnstrPtr\_Type > **MeshUnstrPtrArray\_Type**
- typedef Mesh\_Type::CommPtr\_Type **CommPtr\_Type**
- typedef Mesh\_Type::CommConstPtr\_Type **CommConstPtr\_Type**
- typedef Elements **Elements\_Type**
- typedef Teuchos::RCP< Elements\_Type > **ElementsPtr\_Type**
- typedef SurfaceElements **SurfaceElements\_Type**
- typedef Teuchos::RCP< SurfaceElements\_Type > **SurfaceElementsPtr\_Type**
- typedef EdgeElements **EdgeElements\_Type**
- typedef Teuchos::RCP< EdgeElements\_Type > **EdgeElementsPtr\_Type**
- typedef MeshInterface< SC, LO, GO, NO > **MeshInterface\_Type**
- typedef Teuchos::RCP< MeshInterface\_Type > **MeshInterfacePtr\_Type**
- typedef Map< LO, GO, NO > **Map\_Type**
- typedef Map\_Type::MapPtr\_Type **MapPtr\_Type**
- typedef Map\_Type::MapConstPtr\_Type **MapConstPtr\_Type**
- typedef MultiVector< SC, LO, GO, NO > **MultiVector\_Type**
- typedef Teuchos::RCP< MultiVector\_Type > **MultiVectorPtr\_Type**
- typedef MultiVector< LO, LO, GO, NO > **MultiVectorLO\_Type**
- typedef Teuchos::RCP< MultiVectorLO\_Type > **MultiVectorLOPtr\_Type**
- typedef MultiVector< GO, LO, GO, NO > **MultiVectorGO\_Type**
- typedef Teuchos::RCP< MultiVectorGO\_Type > **MultiVectorGOPtr\_Type**
- typedef Teuchos::RCP< const MultiVector\_Type > **MultiVectorPtrConst\_Type**
- typedef Teuchos::OrdinalTraits< LO > **OTLO**
- typedef Matrix< SC, LO, GO, NO > **Matrix\_Type**
- typedef Teuchos::RCP< Matrix\_Type > **MatrixPtr\_Type**

## Public Member Functions

- [RefinementFactory](#) (CommConstPtr\_Type comm, int volumeID=10)
- [RefinementFactory](#) (CommConstPtr\_Type comm, int volumeID, string refinementRestriction, int refinement3D↵  
DDiagonal=0)
- void [refineMesh](#) (MeshUnstrPtr\_Type meshP1, int iteration, MeshUnstrPtr\_Type outputMesh)
- void [assignEdgeFlags](#) (MeshUnstrPtr\_Type meshP1, EdgeElementsPtr\_Type edgeElements)
- void [refineRegular](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int i)
- void [refineGreen](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int i)
- void [refineBlue](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int i)
- void [refineRed](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int i)
- void [refineType1](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int indexElement)
- void [refineType2](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int indexElement)
- void [refineType3](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int indexElement)
- void [refineType4](#) (EdgeElementsPtr\_Type edgeElements, ElementsPtr\_Type elements, int indexElement)
- void [addMidpoint](#) (EdgeElementsPtr\_Type edgeElements, int i)
- int [determineLongestEdge](#) (EdgeElementsPtr\_Type edgeElements, vec\_int\_Type edgeVec, vec2D\_dbl\_ptr↵  
\_Type points)
- void [buildEdgeMap](#) (MapConstPtr\_Type mapGlobalProc, MapConstPtr\_Type mapProc)
- void [buildNodeMap](#) (EdgeElementsPtr\_Type edgeElements, MapConstPtr\_Type mapGlobalProc, Map↵  
ConstPtr\_Type mapProc, int newPoints, int newPointsRepeated)
- void [updateElementsOfEdgesLocalAndGlobal](#) (int maxRank, MapConstPtr\_Type edgeMap)
- void [updateElementsOfSurfaceLocalAndGlobal](#) (EdgeElementsPtr\_Type edgeElements)
- vec\_bool\_Type [checkInterfaceSurface](#) (EdgeElementsPtr\_Type edgeElements, vec\_int\_Type originFlag,  
vec\_int\_Type edgeNumbers, int indexElement)
- void [refinementRestrictions](#) (MeshUnstrPtr\_Type meshP1, ElementsPtr\_Type elements, EdgeElementsPtr↵  
\_Type edgeElements, int iteration, int &newPoints, int &newPointsCommon, vec\_GO\_Type &globalInterface↵  
IDsTagged, MapConstPtr\_Type mapInterfaceEdges, string restriction, int &newElements)
- void [refineIrregular](#) (ElementsPtr\_Type elements, EdgeElementsPtr\_Type edgeElements, int &newElements,  
MapConstPtr\_Type edgeMap, SurfaceElementsPtr\_Type surfaceTriangleElements)
- void [buildSurfaceTriangleElements](#) (ElementsPtr\_Type elements, EdgeElementsPtr\_Type edgeElements,  
SurfaceElementsPtr\_Type surfaceTriangleElements, MapConstPtr\_Type edgeMap, MapConstPtr\_Type  
elementMap)
- void [setErrorEstimate](#) (vec\_dbl\_Type errorElements)
- vec\_dbl\_Type [getErrorEstimate](#) ()

## Data Fields

- string [refinementRestriction\\_](#) = "none"
- string [markingStrategy\\_](#) = "Maximum"
- double [theta\\_](#) = 0.5
- bool [meshQualityPrint\\_](#) = "false"
- bool [timeTablePrint\\_](#) = "false"
- int [refinement3DDiagonal\\_](#) = 0

## Protected Attributes

- vec\_GO\_Type [globalInterfaceIDs\\_](#)
- vec\_dbl\_Type [errorEstimation\\_](#)
- vec\_dbl\_Type [areaTriangles\\_](#)
- vec\_dbl\_Type [volTetraeders\\_](#)
- vec\_dbl\_Type [h\\_T\\_diam\\_E\\_](#)
- vec\_dbl\_Type [h\\_T\\_min\\_](#)
- MapConstPtr\_Type [surfaceTriangleMap\\_](#)

#### 4.4.1 Constructor & Destructor Documentation

##### 4.4.1.1 RefinementFactory() [1/2]

```
RefinementFactory (
    CommConstPtr_Type comm,
    int volumeID = 10 )
```

###### Parameters

in	<i>comm</i>	
in	<i>volumeID</i>	

##### 4.4.1.2 RefinementFactory() [2/2]

```
RefinementFactory (
    CommConstPtr_Type comm,
    int volumeID,
    string refinementRestriction,
    int refinement3DDiagonal = 0 )
```

###### Parameters

in	<i>comm</i>	
in	<i>volumeID</i>	
in	<i>refinementRestriction</i>	for repeated refinement steps
in	<i>refinement3DDiagonal</i>	

#### 4.4.2 Member Function Documentation

##### 4.4.2.1 addMidpoint()

```
void addMidpoint (
    EdgeElementsPtr_Type edgeElements,
    int edgeID )
```

adding a Midpoint on an edge

###### Parameters

in	<i>edgeElements</i>	
in	<i>edgeID</i>	

## 4.4.2.2 assignEdgeFlags()

```
void assignEdgeFlags (
    MeshUnstrPtr_Type meshP1,
    EdgeElementsPtr_Type edgeElements )
```

Not all edges are marked with a flag in the beginning. In order to set the correct flags to new points we assign the edge flag of the edge they originated from, similar to the function determineEdgeFlagP2New, but uses the edgeMap.

## Parameters

in	<i>meshP1</i>	inputMesh
in	<i>edgeElements</i>	that receive flags

## 4.4.2.3 buildEdgeMap()

```
void buildEdgeMap (
    MapConstPtr_Type mapGlobalProc,
    MapConstPtr_Type mapProc )
```

building edgeMap after refinement

## Parameters

in	<i>mapGlobalProc</i>	
in	<i>mapProc</i>	

## 4.4.2.4 buildNodeMap()

```
void buildNodeMap (
    EdgeElementsPtr_Type edgeElements,
    MapConstPtr_Type mapGlobalProc,
    MapConstPtr_Type mapProc,
    int newPoints,
    int newPointsRepeated )
```

building nodemap after refinement

## Parameters

in	<i>edgeElements</i>	
in	<i>mapGlobalProc</i>	
in	<i>mapProc</i>	
in	<i>newPoints</i>	
in	<i>newPointsRepeated</i>	

#### 4.4.2.5 buildSurfaceTriangleElements()

```
void buildSurfaceTriangleElements (
    ElementsPtr_Type elements,
    EdgeElementsPtr_Type edgeElements,
    SurfaceElementsPtr_Type surfaceTriangleElements,
    MapConstPtr_Type edgeMap,
    MapConstPtr_Type elementMap )
```

building surface triangle elements, as they are not originally part of the mesh information provided by mesh partitioner

##### Parameters

in	<i>elements</i>	
in	<i>edgeElements</i>	
in	<i>surfaceTriangleElements</i>	pointer which will be filled with surfaceTriangleElements
in	<i>edgeMap</i>	
in	<i>elementMap</i>	

#### 4.4.2.6 determineLongestEdge()

```
int determineLongestEdge (
    EdgeElementsPtr_Type edgeElements,
    vec_int_Type edgeVec,
    vec2D_dbl_ptr_Type points )
```

determine longest edge in triangle

##### Parameters

in	<i>edgeElements</i>	
in	<i>edgeVec</i>	
in	<i>points</i>	
out	<i>local</i>	edgeID of the longest edge

#### 4.4.2.7 refineBlue()

```
void refineBlue (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

2D blue refinement: refining element according to blue refinement scheme - connecting nodes of shorter edge with midpoint of longer tagged edge and connect that with opposite corner

## Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

## 4.4.2.8 refineGreen()

```
void refineGreen (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

2D green refinement: refining the element according to green scheme - connecting node on refined edge with the opposite node

## Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

## 4.4.2.9 refineIrregular()

```
void refineIrregular (
    ElementsPtr_Type elements,
    EdgeElementsPtr_Type edgeElements,
    int & newElements,
    MapConstPtr_Type edgeMap,
    SurfaceElementsPtr_Type surfaceTriangleElements )
```

irregular refinement performed according to set rules determined by Bey or Verfürth

## Parameters

in	<i>elements</i>	
in	<i>edgeElements</i>	
in	<i>newElements</i>	
in	<i>edgeMap</i>	
in	<i>surfaceTriangleElements</i>	

## 4.4.2.10 refinementRestrictions()

```
void refinementRestrictions (
    MeshUnstrPtr_Type meshPl,
```

```

ElementsPtr_Type elements,
EdgeElementsPtr_Type edgeElements,
int iteration,
int & newPoints,
int & newPointsCommon,
vec_GO_Type & globalInterfaceIDsTagged,
MapConstPtr_Type mapInterfaceEdges,
string restriction,
int & newElements )

```

Refinement Restrictions In 2D we can add some Restrictions to the Mesh Refinement: KeepRegularity: this will keep the regularity of the Mesh by only refining with a irregular strategy when the longest edge is involved. If not we add a node to the longest edge, whereby the irregular refinement strategy is changed CheckGreenTags: this will only check tagged green Elements, if its irregular refinement tag from the previous refinement is 'green' and if so not refine it green again but add a node to the longest edge and thus refine it blue In the 3D Case we simply never refine an element irregularly twice, this strategy is called simply 'Bey'. If an element is refined regular, its refinement tag changes from eventually 'irregular' to regular. If those elements should still not be refined irregular we use the strategy 'Beylrregular'.

Furthermore if there is no fitting irregular refinement strategy (Type(1)-Type(4) don't fit) we refine regular instead.

#### Parameters

in	<i>meshP1</i>	
in	<i>elements</i>	
in	<i>edgeElements</i>	
in	<i>iteration</i>	
in	<i>newPoints</i>	
in	<i>newPointsCommon</i>	
in	<i>globalInterfaceIDsTagged</i>	
in	<i>mapInterfaceEdges</i>	
in	<i>restriction</i>	
in	<i>newElements</i>	

#### 4.4.2.11 refineMesh()

```

void refineMesh (
    MeshUnstrPtr_Type meshP1,
    int iteration,
    MeshUnstrPtr_Type outputMesh )

```

main function of RefinementFactory, performs one complete mesh refinement

#### Parameters

in	<i>meshP1</i>	inputMesh
in	<i>iteration</i>	current Iteration
in	<i>outputMesh</i>	refined mesh

## 4.4.2.12 refineRed()

```
void refineRed (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

2D red refinement: refining the element red by connecting all tagged edges midpoints. one element is refined into 4

## Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

## 4.4.2.13 refineRegular()

```
void refineRegular (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

2D and 3D regular refinement. Chosen by error estimator or otherwise elements are refined regular by connecting edge midpoints.

## Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

## 4.4.2.14 refineType1()

```
void refineType1 (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

3D Type(1) refinement

## Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	



#### 4.4.2.15 refineType2()

```
void refineType2 (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

#### 3D Type(2) refinement

##### Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

#### 4.4.2.16 refineType3()

```
void refineType3 (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

#### 3D Type(3) refinement

##### Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

#### 4.4.2.17 refineType4()

```
void refineType4 (
    EdgeElementsPtr_Type edgeElements,
    ElementsPtr_Type elements,
    int indexElement )
```

#### 3D Type(4) refinement

##### Parameters

in	<i>edgeElements</i>	
in	<i>elements</i>	
in	<i>indexElement</i>	

## 4.4.2.18 updateElementsOfEdgesLocalAndGlobal()

```
void updateElementsOfEdgesLocalAndGlobal (
    int maxRank,
    MapConstPtr_Type edgeMap )
```

Updating ElementsOfEdgesLocal and ElementsOfEdgesGlobal.

**Parameters**

in	<i>maxRank</i>	
in	<i>edgeMap</i>	

The documentation for this class was generated from the following files:

- RefinementFactory\_decl.hpp
- RefinementFactory\_def.hpp

