Software DokumentationBeschreibung der Funktionen und Parameter

amr-Paket der FEDDLib

Implementierung einer parallelen adaptiven Gitterverfeinerung

Generated by Doxygen 1.8.13

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Chapter 1

Class Documentation

1.1 FEDD::AdaptiveMeshRefinement < SC, LO, GO, NO > Class Template Reference

Public Member Functions

AdaptiveMeshRefinement (string problemType, ParameterListPtr_Type parameter ← ListAll)

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType). This constructor is used if no exact solutions are known.

AdaptiveMeshRefinement (string problemType, ParameterListPtr_Type parameter

 ListAll, Func Type exactSolFunc)

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType).

AdaptiveMeshRefinement (string problemType, ParameterListPtr_Type parameter

 ListAll, Func_Type exactSolFuncU, Func_Type exactSolFuncP)

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType).

DomainPtr_Type globalAlgorithm (DomainPtr_Type domainP1, DomainPtr_Type domainP12, BlockMultiVectorConstPtr_Type solution, ProblemPtr_Type problem, RhsFunc Type rhsFunc)

Global Algorithm of Mesh Refinement.

DomainPtr_Type refineArea (DomainPtr_Type domainP1, vec2D_dbl_Type area, int level)

Initializing problem if only a certain area should be refined.

MultiVectorConstPtr_Type calcExactSolution ()

Calculating exact solution for velocity if possible with exactSolFunc_.

• MultiVectorConstPtr_Type calcExactSolutionP ()

Calculating exact solution for pressure if possible with exactSolPFunc_.

void identifyProblem (BlockMultiVectorConstPtr Type valuesSolution)

Identifying the problem with respect to the degrees of freedom and whether we calculate pressure. By telling how many blocks the MultiVector has, we can tell whether we calculate pressure or not. Depending on the numbers of entries within the solution vector, we can tell how many degreesOfFreedom (dofs) we have.

void calcErrorNorms (MultiVectorConstPtr_Type exactSolution, MultiVector ConstPtr_Type solutionP12, MultiVectorConstPtr_Type exactSolutionP)

Calculating error norms. If the exact solution is unknown we use approxmated error norm and error indicators.

void initExporter (ParameterListPtr_Type parameterListAll)

ParaViewExporter initiation. ParameterListAll contains most settings for Exporter← ParaView. ExporterParaViewAMR is an extension of ExportParaView and as such uses its setup.

void exportSolution (MeshUnstrPtr_Type mesh, MultiVectorConstPtr_Type exportSolutionMv, MultiVectorConstPtr_Type errorValues, MultiVectorConstPtr
 —Type exactSolutionMv, MultiVectorConstPtr_Type exportSolutionPMv, Multi
 VectorConstPtr Type exactSolutionPMv)

ParaViewExporter export of solutions and other error values on current mesh.

void exportError (MeshUnstrPtr_Type mesh, MultiVectorConstPtr_Type error
 ElConst, MultiVectorConstPtr_Type errorElConstH1, MultiVectorConstPtr_Type
 difH1Eta, MultiVectorConstPtr_Type vecDecompositionConst)

ParaViewExporter export of solutions and other error values on current mesh.

• void writeRefinementInfo ()

1.1.1.1 AdaptiveMeshRefinement() [1/3]

Writing refinement information at the end of mesh refinement.

1.1.1 Constructor & Destructor Documentation

```
template<class SC , class LO , class GO , class NO >
```

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType). This constructor is used if no exact solutions are known.

| in | problemType | Laplace, Stokes, NavierStokes. | |
|----|------------------|---|---|
| in | parameterListAll | Parameterlist as used as input parametersProblem.xml. | 1 |

1.1.1.2 AdaptiveMeshRefinement() [2/3]

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType).

Parameters

| in | problemType | Laplace, Stokes, NavierStokes. |
|----|-------------------|---|
| in | paramerterListAll | Parameterlist as used as input parametersProblem.xml. |
| in | exactSolFun | Exact solution function. |

1.1.1.3 AdaptiveMeshRefinement() [3/3]

Initializing problem with the kind of problem we are solving for determining the correct error estimation. ParameterListAll delivers all necessary information (i.e. dim, feType).

Parameters

| in | problemType | Laplace, Stokes, NavierStokes. | |
|----|-------------------|---|--|
| in | paramerterListAll | Parameterlist as used as input parametersProblem.xml. | |
| in | exactSolFunU | Exact solution for velocity u. | |
| in | exactSolFunP | Exact solution for velocity p. | |

1.1.2 Member Function Documentation

1.1.2.1 calcErrorNorms()

```
MultiVectorConstPtr_Type exactSolution,
MultiVectorConstPtr_Type solutionP12,
MultiVectorConstPtr_Type exactSolutionP )
```

Calculating error norms. If the exact solution is unknown we use approxmated error norm and error indicators.

Parameters

| in | exactSolution | If known, otherwise a dummy vector with all zeros is input. |
|----|----------------|---|
| in | solutionP12 | Finite element solution u_h and maybe p_h. |
| in | exactSolutionP | If known, otherwise a vector with all zeros is input. |

1.1.2.2 exportError()

ParaViewExporter export of solutions and other error values on current mesh.

Parameters

| in | mesh | The current mesh on which refinement is performed. |
|----|-----------------------|---|
| in | errorElConst | Estimated error eta_T. |
| in | errorElConstH1 | H1 error elmentwise. |
| in | difH1Eta | eta_T- u_h _T difference between estimated error an H1-error. |
| in | vecDecompositionConst | Information of distribution of elements among processors. |

1.1.2.3 exportSolution()

```
MultiVectorConstPtr_Type exportSolutionPMv,
MultiVectorConstPtr_Type exactSolutionPMv )
```

ParaViewExporter export of solutions and other error values on current mesh.

Parameters

| in | mesh | The current mesh on which refinement is performed. |
|----|-------------------|--|
| in | exportSolutionMv | Export vector of velocity fe solution. |
| in | exportSolutionPMv | Export vector of pressure fe solution. |
| in | errorValue | u-u_h on domainP12. |
| in | exactSolutionMv | Export vector of exact velocity solution. |
| in | exactSolutionPMv | Export vector of exact pressure solution. |

1.1.2.4 globalAlgorithm()

Global Algorithm of Mesh Refinement.

Given domains and solutions depending on problem a global mesh refinement algorithm and error estimation is performed. For example if to solve simple laplace problem, we have only one solution to put in, if to estimate error for Navier-Stokes equation we need pressure and velocity solutions.

| in | domainP1 | Domain with P_1 discretization, always neccesary as refinement is performed on P_1 mesh. |
|----|-----------|---|
| in | domainP12 | Domain with P_1 or P_2 discretization if available, otherwise input domainP1. |
| in | solution | Solution of problem on P_1 or P_2 discretization, can contain velocity and pressure solution. |
| in | problem | The problem itself as the problemPtr. Contains Laplace, Stokes or Navier-Stokes problem. |
| in | rhs | Right hand side function from the pde system. Necessary for error estimation. |

1.1.2.5 identifyProblem()

Identifying the problem with respect to the degrees of freedom and whether we calculate pressure. By telling how many blocks the MultiVector has, we can tell whether we calculate pressure or not. Depending on the numbers of entries within the solution vector, we can tell how many degreesOfFreedom (dofs) we have.

Parameters

| in | valuesSolution | Block that contains solution for velocity and as the case | |
|----|----------------|---|--|
| | | may be pressure. | |

1.1.2.6 refineArea()

Initializing problem if only a certain area should be refined.

Parameters

| in | domainP1 | P_1 Domain |
|----|----------|---|
| in | area | Area that is suppose to be refined. If is a vector defining the area as follows: row1:[x_0,x_1] x-limits, row2: [y_0,y_1] y-limits, row3: [z_0,z_1] z-limits. |
| in | level | intensity of refinement. Number of levels equals number of performed refinements. |

The documentation for this class was generated from the following files:

- · AdaptiveMeshRefinement_decl.hpp
- · AdaptiveMeshRefinement def.hpp

1.2 FEDD::ErrorEstimation < SC, LO, GO, NO > Class Template Reference

Public Member Functions

• ErrorEstimation (int dim, string problemType)

ErrorEstimation is initiated with the dimension and problemType, as it is necessary to fit errorEstimation to the problem at hand.

• MultiVectorPtr_Type estimateError (MeshUnstrPtr_Type inputMeshP12, Mesh UnstrPtr_Type inputMeshP1, BlockMultiVectorConstPtr_Type valuesSolution, RhsFunc Type rhsFunc, string FEType)

Main Function for a posteriori error estimation.

void identifyProblem (BlockMultiVectorConstPtr Type valuesSolution)

Identifying the problem with respect to the degrees of freedom and whether we calculate pressure. By telling how many block the MultiVector has, we can tell whether we calculate pressure or not. Depending on the numbers of entries within the solution vector, we can tell how many degreesOfFreedom (dofs) we have.

• void makeRepeatedSolution (BlockMultiVectorConstPtr_Type valuesSolution)

We split the solution from the BlockMultiVector valuesSolution into one or more seperate blocks, where the blocks represent the different dimensions.

vec3D_dbl_Type calcNPhi (string phiDerivative, int dofsSol, string FEType)

Function that calculates the jump part for nabla u or p.

vec_dbl_Type calculateJump ()

Part of the error estimator that calculates the jump part of the estimation. What kind of jump is calculated depends on the problemType we have at hand.

vec2D dbl Type gradPhi (int dim, int intFE, vec dbl Type &p)

Calcutlating the gradient of phi depending on quad points p.

vec_dbl_Type phi (int dim, int intFE, vec_dbl_Type &p)

Calcutlating phi depending on quad points p.

 MultiVectorPtr_Type determineCoarseningError (MeshUnstrPtr_Type mesh_k, MeshUnstrPtr_Type mesh_k_m, MultiVectorPtr_Type errorElementMv_k, string distribution, string markingStrategy, double theta)

DetermineCoarseningError is the essential part of the mesh coarsening process.

double determineResElement (FiniteElement element, RhsFunc Type rhsFunc)

Function that that determines $| u_h + f | (L2(T)), | u_h + f - p_h | T \text{ or } | u_h + f - p_h - (u_h)u_h | T \text{ for an Element T.}$

· double determineDivU (FiniteElement element)

Function that that determines | | div(u) | |_T for a Element T.

 vec2D_dbl_Type getQuadValues (int dim, string FEType, string Type, vec_dbl_←
 Type &QuadW, FiniteElement surface)

Returns neccesary quadrature Values. Is distinguishes between needing Element or Surface information.

 void markElements (MultiVectorPtr_Type errorElementMv, double theta, string strategy, MeshUnstrPtr Type meshUnstr)

Function that marks the elements for refinement.

vec_dbl_Type determineVolTet (ElementsPtr_Type elements, vec2D_dbl_ptr_
 —
 Type points)

function, that determines volume of tetrahedra.

vec_dbl_Type calcDiamTriangles (ElementsPtr_Type elements, vec2D_dbl_ptr
 —Type points, vec_dbl_Type &areaTriangles, vec_dbl_Type &rho_T, vec_dbl_Type
 &C_T)

Calculating the diameter of triangles.

Calculating the diameter of triangles.

vec_dbl_Type calcDiamTetraeder (ElementsPtr_Type elements, vec2D_dbl_ptr
 —Type points, vec_dbl_Type volTet)

Calculating the circumdiameter of tetraeder.

vec_dbl_Type calcRhoTetraeder (ElementsPtr_Type elements, Surface
 ElementsPtr_Type surfaceTriangleElements, vec_dbl_Type volTet, vec_dbl_Type
 areaTriangles)

Calcutlating the incircumdiameter of tetrahedra.

vec_dbl_Type determineAreaTriangles (ElementsPtr_Type elements, Edge
 ElementsPtr_Type edgeElements, SurfaceElementsPtr_Type surfaceElements,
 vec2D_dbl_ptr_Type points)

Calculating the area of the triangle elements of tetrahedra.

void buildTriangleMap ()

Build Surface Map. Contrary to building the edge map, building the surface map is somewhat simpler as elementsOfSurfaceGlobal and elementsOfSurfaceLocal already exist. Via elementsOfSurface global each surface can be uniquely determined by the two elements it connects.

UpdateElementsOfSurfaceLocalAndGlobal is performed here instead of in mesh—Refinement, as the information is only needed in case of error estimation. Equivalent function as updateElementsOfEdgeGlobal but with the important destinction, that it runs without communication and only relies on local information.

void tagArea (MeshUnstrPtr_Type meshUnstr, vec2D_dbl_Type area)

Tags only a certain Area for refinement and is independent of any error estimation.

1.2.1 Constructor & Destructor Documentation

1.2.1.1 ErrorEstimation()

ErrorEstimation is initiated with the dimension and problemType, as it is necessary to fit errorEstimation to the problem at hand.

| in | dim | Dimension of problem. | |
|----|-------------|---|--|
| in | problemType | Type of problem. Choose between Laplace, Stokes and | |
| | | NavierStokes | |

1.2.2 Member Function Documentation

1.2.2.1 buildTriangleMap()

```
template<class SC , class LO , class GO , class NO >
void FEDD::ErrorEstimation< SC, LO, GO, NO >::buildTriangleMap ( )
```

Build Surface Map. Contrary to building the edge map, building the surface map is somewhat simpler as elementsOfSurfaceGlobal and elementsOfSurfaceLocal already exist. Via elementsOfSurface global each surface can be uniquely determined by the two elements it connects.

The surfacemap is only used for error estimation. Thus it is only build here and not in the refinementFactory.

1.2.2.2 calcDiamTetraeder()

Calculating the circumdiameter of tetraeder.

Parameters

| in | elements | Elements. |
|-----|--------------|---------------------------------|
| in | points | Points. |
| in | volTet | Volume of tetrahedra. |
| out | diamElements | Uncircumdiameter of tetrahedra. |

1.2.2.3 calcDiamTriangles()

Calculating the diameter of triangles.

| in | elements | Elements |
|-----|--------------|---|
| in | points | Points |
| out | diamElements | Diameter of triangles (Uncirclediameter). |
| out | rho_T | Incirclediameter. |
| out | C_T | Shape parameter. |

1.2.2.4 calcDiamTriangles3D()

Calculating the diameter of triangles.

Parameters

| in | elements | Elements. |
|-----|--------------|------------------------|
| in | points | Points. |
| out | diamElements | Diameter of triangles. |

1.2.2.5 calcNPhi()

Function that calculates the jump part for nabla u or p.

| in | phiDerivative | phiDerivative is either 'Gradient' or 'None' and what kind of |
|----|---------------|---|
| | | jump is calculated depends on the problemType we have at |
| | | hand. If phiDerivative is 'Gradient' the nabla u jump part is |
| | | caluculated and if its 'None' then the pressure jump. |

| in | dofsSol | Degree of freedom of the caluclated jump part. The pressure dof is always 1 whereas velocity dof can vary depending on the problem. |
|----|---------|---|
| in | FEType | Finite element type of the calculated jump part. |

1.2.2.6 calcRhoTetraeder()

Calcutlating the incircumdiameter of tetrahedra.

Parameters

| in | elements | Elements. |
|-----|-------------------------|---------------------------------|
| in | surfaceTriangleElements | TriangleElements. |
| in | volTet | Volume of tetrahedra. |
| in | areaTriangles | Area of faces of tetrahedra. |
| out | rhoElements | Incircumdiameter of tetrahedra. |

1.2.2.7 determineAreaTriangles()

Calculating the area of the triangle elements of tetrahedra.

| in | elements | Elements. |
|-----|-----------------|--------------------|
| in | edgeElements | Edges. |
| in | surfaceElements | Triangle Elements. |
| in | points | Points. |
| out | areaTriangles | Area of triangles. |

1.2.2.8 determineCoarseningError()

DetermineCoarseningError is the essential part of the mesh coarsening process.

Instead of calulating an error for mesh level k, we redestribute it to lower mesh levels and refining those. We execute this function with an estimated error from level k. With this calculated error, we mark the elements according to that error and refine afterwards. If we decide to coarsen a certain mesh level, we take that level, look at the k-m level and refine that to the point where we are at the same level we wanted to perform the coarsening on.

| in | mesh_k | Current mesh of level k. | |
|----|-------------------------|---|--|
| in | mesh_k_m | Mesh of refinement level k-m. | |
| in | errorElementMv <i>⊷</i> | The error estimation of mesh level k. | |
| | _k | | |
| in | distribution | Either 'forwards' or 'backwards'. We determine the error estimate in level k-m with redistributing backwards. if we are in level k-m we calculate the k-m+1 mesh level error estimation via redistributing the k-m error forward. | |
| in | markingStrategy | The strategy with which element are marked. | |
| in | theta | Marking threshold. | |

1.2.2.9 determineDivU()

Function that that determines | | div(u) | |_T for a Element T.

Parameters

| | in | element | FiniteElement element where $ \operatorname{div}(u) _T$ is calculated on. |
|---|----|------------------------------|---|
| out divElement Divergence of u_h on element | | Divergence of u_h on element | |

1.2.2.10 determineResElement()

Function that that determines $| | u_h + f | |_{L2(T)}, | | u_h + f - p_h | |_{T}$ or $| | u_h + f - p_h | |_{T}$ for an Element T.

Parameters

| | in | element | FiniteElement element where div(u) _T is calculated on. |
|---|----|--|--|
| | in | rhsFunc The right hand side function of the pde. | |
| out resElement Residual of element according to pro | | resElement | Residual of element according to problemType |

1.2.2.11 determineVolTet()

function, that determines volume of tetrahedra.

| j | in | elements | Elements. |
|---|-----|------------------|-----------------------|
| j | in | edgeElements | Edges. |
| j | in | points | Points. |
| | out | volumeTetrahedra | Volume of tetrahedras |

1.2.2.12 estimateError()

Main Function for a posteriori error estimation. Depending on the problem the the error estimation is calculated accordingly.

Parameters

| in | inputMeshP1 | The P1 Mesh that is used for later refinement. | |
|----|--------------|--|--|
| in | inputMeshP12 | The possible P2 Mesh, if one of the solutions is of P2 | |
| | | Discretisation, otherwise both meshes are P1. | |
| in | solution | Solution of the PDE in BlockMultiVector Format (Block 0: | |
| | | Velocity, Block 1: Pressure). | |
| in | rhs | The right hand side function of the pde. | |
| in | FETypeV | Finite element type as the maximum FEType for the | |
| | | Velocity, pressure is assumed to be P1 always. | |

1.2.2.13 getQuadValues()

```
template<class SC , class LO , class GO , class NO >
vec2D_dbl_Type FEDD::ErrorEstimation< SC, LO, GO, NO >::getQuadValues (
    int dim,
    string FEType,
    string Type,
    vec_dbl_Type & QuadW,
    FiniteElement surface )
```

Returns neccesary quadrature Values. Is distinguishes between needing Element or Surface information.

| in | dim | Dimension for which the quadrature points are needed. |
|-----|---------------|--|
| in | FEType | Finite element type for which the quadrature points are needed. |
| in | Туре | Type of quadrature points are need. Either 'Element' if you integrate over an element or 'Surface' if you need to integrate over a surface (i.e. for calculating the jump) |
| in | QuadW | Vector to be filled with the quadrature weights accordingly |
| in | FiniteElement | surface for which you need the quadrature points in case if 'Surface' type, as it is needed for figuring out the quadrature points |
| out | QuadPts | Quadrature points |
| out | QuadW | Quadrature weights Keep in mind that elementwise quadPoint are defined on reference element whereas surface quadPoints are defined on the input surface, which is typically not the reference Element. |

1.2.2.14 gradPhi()

Calcutlating the gradient of phi depending on quad points p.

Parameters

| in | dim | Dimension. | |
|-----|---------|--|--|
| in | intFE | Integer value of discretisation P1 (1) or P2(2). | |
| in | р | Quadpoints or other points for which phi is suppose to be evaluated. | |
| out | gradPhi | Gradient of phi with evaluated values p. | |

1.2.2.15 identifyProblem()

BlockMultiVectorConstPtr_Type valuesSolution) Identifying the problem with respect to the degrees of freedom and whether we calculate pressure. By telling how many block the MultiVector has, we can tell whether we calculate pressure or not. Depending on the numbers of entries within the solution vector, we can tell how many degreesOfFreedom (dofs) we have.

| i | n | valuesSolution | Blocks that contains solution for velocity and as the case |
|---|---|----------------|--|
| | | | may be pressure. |

1.2.2.16 makeRepeatedSolution()

```
\label{localization} $$\operatorname{LO}$, class GO , class NO > $$\operatorname{PEDD}$::ErrorEstimation< SC, LO, GO, NO >::makeRepeatedSolution ( $$\operatorname{BlockMultiVectorConstPtr_Type}$ valuesSolution )
```

We split the solution from the BlockMultiVector valuesSolution into one or more seperate blocks, where the blocks represent the different dimensions.

Parameters

| in | valuesSolution | Block that contains solution for velocity and as the case | |
|----|----------------|---|--|
| | | may be pressure. | |

1.2.2.17 markElements()

Function that marks the elements for refinement.

Parameters

| in | errorElementMv | MultiVector that contains the estimated error for each |
|----|-----------------|--|
| | | element. |
| in | theta | Parameter determining for marking strategies. |
| in | markingStrategy | Strategy with which the elements are marked. |
| | | Implemented Strategies 'Doerfler' or 'Maximum'. |
| in | meshP1 | P1 mesh which is used for later refinement and has to be |
| | | the one beeing marked. |

!! it is essential that the meshP1 mesh inserted here is the mesh that will be used for mesh refinement, as it contains the elementwise-information determining refinement. !!

1.2.2.18 phi()

```
template<class SC , class LO , class GO , class NO >
vec_dbl_Type FEDD::ErrorEstimation< SC, LO, GO, NO >::phi (
    int dim,
    int intFE,
    vec_dbl_Type & p )
```

Calcutlating phi depending on quad points p.

Parameters

| in | dim. | |
|-----|-------|--|
| in | intFE | integer value of discretisation P1 (1) or P2(2). |
| in | р | Quadpoints or other points for which phi is to be evaluated. |
| out | phi | Phi with evaluated values p. |

1.2.2.19 tagArea()

Tags only a certain Area for refinement and is independent of any error estimation.

Parameters

| in | inputMeshP1 | The P1 Mesh that is used for later refinement. |
|----|-------------|--|
| in | area | Area that is suppose to be refined. If is a vector defining the area as follows: row1:[x_0,x_1] x-limits, row2: [y_0,y_1] y-limits, row3: [z_0,z_1] z-limits . |

1.2.2.20 updateElementsOfSurfaceLocalAndGlobal()

UpdateElementsOfSurfaceLocalAndGlobal is performed here instead of in mesh← Refinement, as the information is only needed in case of error estimation. Equivalent function as updateElementsOfEdgeGlobal but with the important destinction, that it runs without communication and only relies on local information.

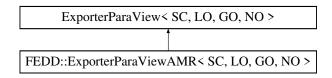
| in | edgeElements | Edes. |
|----|-------------------------|--------------------|
| in | surfaceTriangleElements | Triangle elements. |

The documentation for this class was generated from the following files:

- · ErrorEstimation_decl.hpp
- · ErrorEstimation_def.hpp

1.3 FEDD::ExporterParaViewAMR< SC, LO, GO, NO > Class Template Reference

Inheritance diagram for FEDD::ExporterParaViewAMR< SC, LO, GO, NO >:

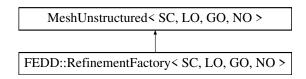


The documentation for this class was generated from the following files:

- ExporterParaViewAMR_decl.hpp
- ExporterParaViewAMR_def.hpp

1.4 FEDD::RefinementFactory< SC, LO, GO, NO > Class Template Reference

Inheritance diagram for FEDD::RefinementFactory< SC, LO, GO, NO >:



Public Member Functions

- RefinementFactory (CommConstPtr_Type comm, int volumeID=10)
 Initiating RefinementFactory via MeshUnstructured.
- RefinementFactory (CommConstPtr_Type comm, int volumeID, string refinement

 — Restriction, int refinement3DDiagonal=0, int restrictionLayer =2)
 - Initiating RefinementFactory via MeshUnstructured with additional information for mesh refinement.
- void refineMesh (MeshUnstrPtr_Type meshP1, int iteration, MeshUnstrPtr_Type outputMesh, string refinementMode)
 - Main function of RefinementFactory, performs one complete mesh refinement, according to red-green refinement (Verfuerth) or tetrahedral grid refinement (Bey).
- void assignEdgeFlags (MeshUnstrPtr_Type meshP1, EdgeElementsPtr_Type edgeElements)
 - Not all edges are marked with a flag in the beginning. In order to set the correct flags to new points we assign the edge flag of the edge they originated from, similar to the function determineEdgeFlagP2New, but this function uses the edgeMap.
- void refineRegular (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int i, SurfaceElementsPtr_Type surfaceTriangleElements)
 - 2D and 3D regular refinement. Chosen by error estimator or otherwise elements are refined regular by connecting edge midpoints.
- void refineGreen (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int i)
 - 2D green refinement: refining the element according to green scheme connecting node on refined edge with the opposite node.
- void refineBlue (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int i)
 - 2D blue refinement: refining element according to blue refinement scheme connecting nodes of shorter edge with midpoint of longer tagged edge and connect that with opposite corner
- void refineRed (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int i)
 - 2D red refinement: refining the element red by connecting all tagged edges midpoints. one element is refined into 4.
- void refineType1 (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElement, SurfaceElementsPtr_Type surfaceTriangleElements)
 - 3D Type(1) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955
- void refineType2 (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElement, SurfaceElementsPtr Type surfaceTriangleElements)
 - 3D Type(2) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955
- void refineType3 (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElement, SurfaceElementsPtr Type surfaceTriangleElements)
 - 3D Type(3) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955
- void refineType4 (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElement, SurfaceElementsPtr_Type surfaceTriangleElements)

3D Type(4) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

• void addMidpoint (EdgeElementsPtr_Type edgeElements, int i)

Adding a Midpoint on an edge.

int determineLongestEdge (EdgeElementsPtr_Type edgeElements, vec_int_Type edgeVec, vec2D_dbl_ptr_Type points)

Eetermine longest edge in triangle.

void buildEdgeMap (MapConstPtr_Type mapGlobalProc, MapConstPtr_Type mapProc)

Building edgeMap after refinement.

 void buildNodeMap (EdgeElementsPtr_Type edgeElements, MapConstPtr_Type mapGlobalProc, MapConstPtr_Type mapProc, int newPoints, int newPoints Repeated)

Building nodemap after refinement.

void updateElementsOfEdgesLocalAndGlobal (int maxRank, MapConstPtr_Type edgeMap)

Updating ElementsOfEdgesLocal and ElementsOfEdgesGlobal.

 vec_bool_Type checkInterfaceSurface (EdgeElementsPtr_Type edgeElements, vec_int_Type originFlag, vec_int_Type edgeNumbers, int indexElement)

Checking if surfaces are part of the interface. Done by checking if all edges of a triangle are part of the interface and if both elements connected to the surface are on different processors.

void refinementRestrictions (MeshUnstrPtr_Type meshP1, ElementsPtr_Type elements, EdgeElementsPtr_Type edgeElements, SurfaceElementsPtr_Type surfaceTriangleElements, int &newPoints, int &newPointsCommon, vec_GO
 __Type &globalInterfaceIDsTagged, MapConstPtr_Type mapInterfaceEdges, int &newElements)

Refinement Restrictions.

 void refineMeshRegIreg (ElementsPtr_Type elements, EdgeElementsPtr_Type edgeElements, int &newElements, MapConstPtr_Type edgeMap, Surface← ElementsPtr_Type surfaceTriangleElements)

Refinement performed according to the set of rules determined by Bey or Verfürth.

Building surface triangle elements, as they are not originally part of the mesh information provided by mesh partitioner.

void bisectEdges (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElement, SurfaceElementsPtr_Type surfaceTriangleElements, string mode="default")

2D and 3D that bisects the edges of tagged Elements. Chosen by error estimator or otherwise elements are refined regular by connecting edge midpoints.

 void bisectElement3 (EdgeElementsPtr_Type edgeElements, ElementsPtr_Type elements, int indexElementp)

2D refinement by bisection of tagged Elements with three tagged Edges.

1.4.1 Constructor & Destructor Documentation

1.4.1.1 RefinementFactory() [1/2]

Initiating RefinementFactory via MeshUnstructured.

Parameters

| in | comm | CommPtr. |
|----|----------|---|
| in | volumeID | The flag ID of triangles in 2D or tetrahedra in 3D. Usually 10. |

1.4.1.2 RefinementFactory() [2/2]

Initiating RefinementFactory via MeshUnstructured with additional information for mesh refinement.

Parameters

| in | comm | CommPtr |
|----|-----------------------|---|
| in | volumeID | The flag ID of triangles in 2D or tetrahedra in 3D. |
| | | Usually 10. |
| in | refinementRestriction | Restriction for repeated refinement steps. |
| in | refinement3DDiagonal | 3D diagonal pick for regular refinement |

1.4.2 Member Function Documentation

1.4.2.1 addMidpoint()

Adding a Midpoint on an edge.

Parameters

| in | edgeElements | Edges. |
|----|--------------|--|
| in | edgeID | Edge ids where the midpoints is added. |

1.4.2.2 assignEdgeFlags()

Not all edges are marked with a flag in the beginning. In order to set the correct flags to new points we assign the edge flag of the edge they originated from, similar to the function determineEdgeFlagP2New, but this function uses the edgeMap.

Parameters

| in | meshP1 | InputMesh, always P1. |
|----|--------------|---------------------------|
| in | edgeElements | Edges that receive flags. |

1.4.2.3 bisectEdges()

2D and 3D that bisects the edges of tagged Elements. Chosen by error estimator or otherwise elements are refined regular by connecting edge midpoints.

${\it 1.4~FEDD::} Refinement Factory < SC,\,LO,\,GO,\,NO > Class~Template~Reference~~23$

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.4 bisectElement3()

2D refinement by bisection of tagged Elements with three tagged Edges.

Parameters

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.5 buildEdgeMap()

Building edgeMap after refinement.

Parameters

| in | mapGlobalProc | Map of global processor numbers |
|----|---------------|---------------------------------|
| in | mapProc | Map of local processor number |

1.4.2.6 buildNodeMap()

Building nodemap after refinement.

| in | edgeElements | Edges. |
|----|-------------------|---|
| in | mapGlobalProc | Map of global processor numbers. |
| in | mapProc | Map of local processor numbers. |
| in | newPoints | Number of new points per refinement iteration. |
| in | newPointsRepeated | Number of new repeated points per refinement iteration. |

1.4.2.7 buildSurfaceTriangleElements()

Building surface triangle elements, as they are not originally part of the mesh information provided by mesh partitioner.

Parameters

| in | elements | Elements. |
|----|-------------------------|-----------------------------------|
| in | edgeElements | Edges. |
| in | surfaceTriangleElements | Pointer which will be filled with |
| | | surfaceTriangleElements. |
| in | edgeMap | Global Mapping of edges |
| in | elementMap | Global Mapping of elements. |

1.4.2.8 checkInterfaceSurface()

Checking if surfaces are part of the interface. Done by checking if all edges of a triangle are part of the interface and if both elements connected to the surface are on different processors.

| in | edgeElements | Edges. |
|----|--------------|-------------------------------------|
| in | originFlag | Flags of surfaces of indexElement. |
| in | edgeNumbers | Numbers of inserted surfaces edges. |
| in | indexElement | Index of element in question. |

1.4.2.9 determineLongestEdge()

Eetermine longest edge in triangle.

Parameters

| in | edgeElements | Edges. |
|-----|--------------|-----------------------------------|
| in | edgeVec | Vector with edge ids of triangle. |
| in | points | Points. |
| out | Local | edgeID of the longest edge. |

1.4.2.10 refineBlue()

2D blue refinement: refining element according to blue refinement scheme - connecting nodes of shorter edge with midpoint of longer tagged edge and connect that with opposite corner

| - | in <i>edgeElements</i> | | Edges |
|---|------------------------|--------------|----------------------|
| | in | elements | Elements. |
| - | in | indexELement | Element in question. |

1.4.2.11 refineGreen()

2D green refinement: refining the element according to green scheme - connecting node on refined edge with the opposite node.

Parameters

| in | edgeElements | Edges. |
|----|--------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |

1.4.2.12 refinementRestrictions()

Refinement Restrictions.

In 2D we can add some Restrictions to the Mesh Refinement: Bisection: this will keep the regularity of the Mesh by only refining whith a irregular strategy when the longest edge is involved. If not we add a node to the longest edge, whereby the irregular refinement strategy is changed. GreenTags: this will only check tagged green Elements, if its irregular refinement tag from the previous refinement is 'green' and if so not refine it green again but add a node to the longest edge and thus refine it blue. In the 3D Case we simply never refine an element irregularly twice, this strategy is called simply 'Bey'. If an element is refined regular, its refinement tag changes from eventually 'irregular' to regular. If those elements should still not be refined irregular we use the strategy 'Beylrregular'.

Furthermore if there is no fitting irrregular refinement strategy (Type(1)-Type(4) don't fit) we refine regular instead.

| in | meshP1 | P_1 Mesh. |
|----|--------------------------|--|
| in | elements | Element. |
| in | edgeElements | Edges. |
| in | iteration | Current iteration. |
| in | newPoints | Number of new unique points originating from restrictions. |
| in | newPointsCommon | Number of new repeated points originating from restrictions. |
| in | globalInterfaceIDsTagged | List of global IDs of tagged interface edges. |
| in | mapInterfaceEdges | Map of interface edges. |
| in | restriction | The kind of restriction we want to apply. |
| in | newElements | Number of new elements orginating from restrictions. |

1.4.2.13 refineMesh()

Main function of RefinementFactory, performs one complete mesh refinement, according to red-green refinement (Verfuerth) or tetrahedral grid refinement (Bey).

Parameters

| in | meshP1 | InputMesh P1. |
|-----|----------------|--|
| in | iteration | Current Iteration. |
| in | refinementMode | In 2D we can choose between 'Regular' (red-green) or 'Bisection. In 3D only 'Regular' is possible, which is also the default mode. |
| out | outputMesh | Refined mesh. |

1.4.2.14 refineMeshRegIreg()

```
EdgeElementsPtr_Type edgeElements,
int & newElements,
MapConstPtr_Type edgeMap,
SurfaceElementsPtr_Type surfaceTriangleElements )
```

Refinement performed according to the set of rules determined by Bey or Verfürth.

Parameters

| in | elements | Elements. |
|----|-------------------------|---|
| in | edgeElements | Edges. |
| in | newElements | Number of new elements originating from refinement. |
| in | edgeMap | Map of global edge ids. |
| in | surfaceTriangleElements | Triangle elements (3D case). |

1.4.2.15 refineRed()

2D red refinement: refining the element red by connecting all tagged edges midpoints. one element is refined into 4.

Parameters

| in | edgeElements | Edges |
|----|--------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |

1.4.2.16 refineRegular()

2D and 3D regular refinement. Chosen by error estimator or otherwise elements are refined regular by connecting edge midpoints.

3D regular refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.17 refineType1()

3D Type(1) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

Parameters

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.18 refineType2()

3D Type(2) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.19 refineType3()

3D Type(3) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

Parameters

| in | edgeElements | Edges. |
|----|-------------------------|----------------------|
| in | elements | Elements. |
| in | indexELement | Element in question. |
| in | surfaceTriangleElements | Triangle elements. |

1.4.2.20 refineType4()

3D Type(4) refinement as defined in "Tetrahedral Grid Refinement" by J. Bey 'Algorithm Regular Refinement' in Computing, Springer Verlag 1955

| | in | edgeElements | Edges. |
|---|----|-------------------------|----------------------|
| ĺ | in | elements | Elements. |
| | in | indexELement | Element in question. |
| | in | surfaceTriangleElements | Triangle elements. |

1.4.2.21 updateElementsOfEdgesLocalAndGlobal()

Updating ElementsOfEdgesLocal and ElementsOfEdgesGlobal.

Parameters

| in | maxRank | The maximal processor rank. |
|----|---------|-----------------------------|
| in | edgeMap | Map of global edge ids. |

The documentation for this class was generated from the following files:

- RefinementFactory_decl.hpp
- RefinementFactory_def.hpp