

ANALOGNO DOBA

MEHANIKA, VAKUUMSKE CIJEVI,
KONTINUIRANO PODRUČJE

- ① ŠTO JE SMISAO PREDMETA??
 - ② NACRTATI MODEL.
 - ③ VIZUALIZIRANJE U STVARNOM ŽIVOTU.
primjeri: VOPOKOTLIC, PARNI STROJ, PRETVARAČ + ASINK. MOTOR
- SINTEZA + ANALIZA \Rightarrow FIZIKALNI + MATEMATIČKI MODEL \Rightarrow JEDNADŽBE!

LABOS 1 \Rightarrow OPIS SUSTAVA POMOĆU DIFF. JEDNADŽBI

1. ZADATAK $\left\{ \begin{array}{l} \text{RLC KUG} \rightarrow \text{NAPONI } \overset{\{ \text{S DOMENA}\}}{\text{ČVOROVA}} \text{ ILI } \text{VREMENSKA DOMENA} \\ \text{NPR.} \\ \hookrightarrow \text{ODREDITI } \nabla^2 y'' + y' + y = y u' + u \Rightarrow \text{MOGUĆE ZBOG LINEARNOG SUSTAVA} \end{array} \right.$

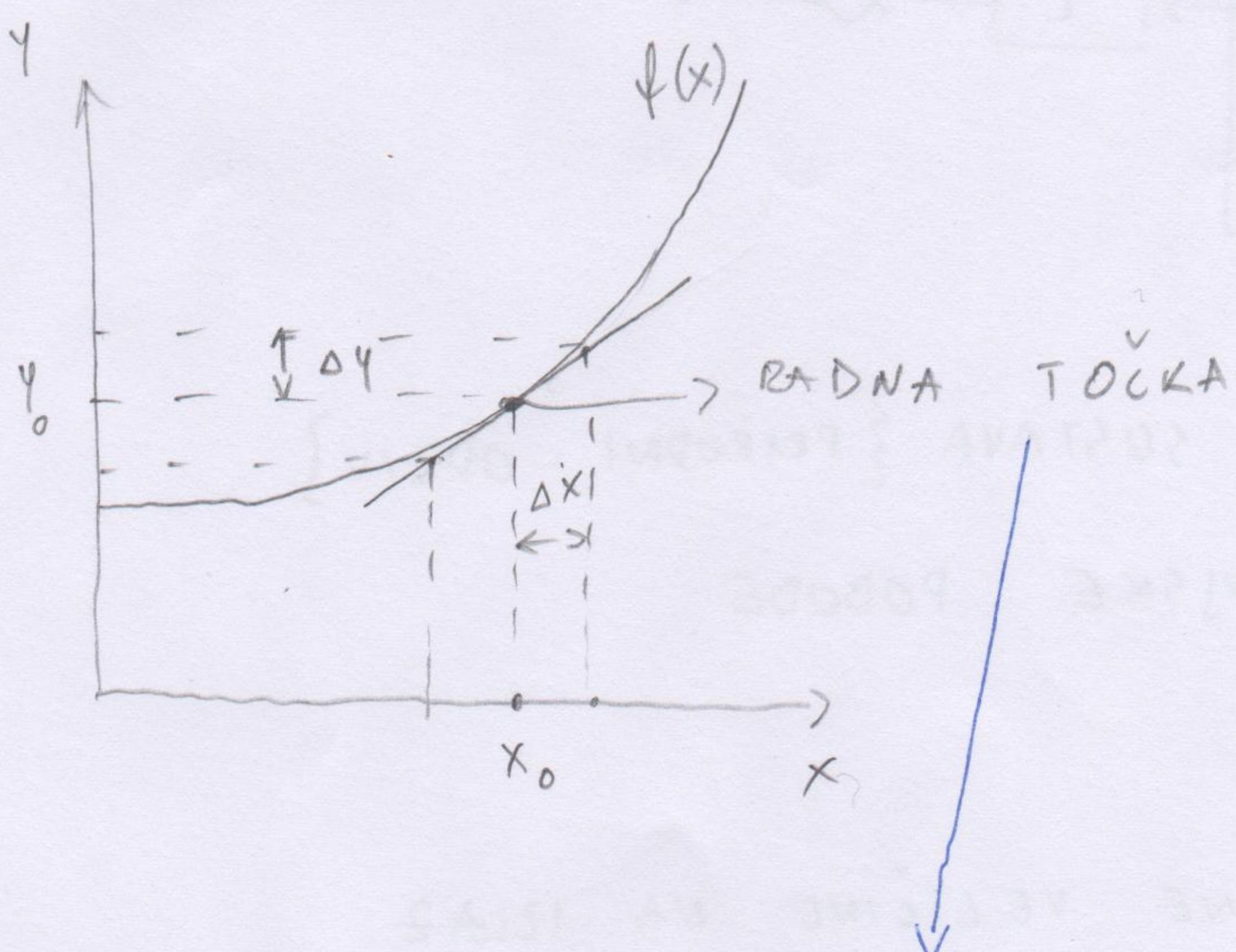
2. ZADATAK \rightarrow SVE ISTO SAMO JE SUSTAV NELINERAN
 $y'' + y' + y = y u' + \sqrt{u}$

7 LINEARIZACIJA

UVJETI LINEARNOSTI $\left\{ \begin{array}{l} \text{ADITIVNOST } f(x_1 + x_2) = f(x_1) + f(x_2) \rightarrow \forall x \in D \{f\} \\ \text{HOMOGENOST } f(\alpha x) = \alpha f(x) \rightarrow \forall x \in D \{f\} \text{ i } \forall \alpha \downarrow \text{SKALAR} \end{array} \right.$

LINEARNOST JE UVJET ZA LAPLACEA $\left\{ \begin{array}{l} \text{LINEARNA INTEGRALNA} \\ \text{TRANSFORMACIJA} \end{array} \right.$

$$F(s) = \int_0^\infty f(t) e^{-st} dt$$



$$y = f(x)$$

$$\left. \begin{array}{l} x = x_0 + \Delta x \\ y = y_0 + \Delta y \end{array} \right\} \text{IAKO ZUMIBANDO}$$

$$y = f(x_0 + \Delta x) \approx f(x_0) + K \Delta x$$

NAGIB PRAVCA

$$K = \left. \frac{dy}{dx} \right|_{x_0}$$

NPR. KOLIČINA VODE U POSUDI JE UVJEK KONSTANTNA

$$z = \frac{1+w}{1-w}$$

$$w = \frac{1-z}{1+z}$$

$$z = e^{-\gamma T}$$

$$\eta = j w$$

$$w = \frac{1 - e^{-\gamma T}}{1 + e^{-\gamma T}}$$

$$\frac{e^{-j\frac{T}{2}}}{e^{j\frac{T}{2}}}$$

$$\frac{e^{\gamma \frac{T}{2}} - e^{-\gamma \frac{T}{2}}}{e^{\gamma \frac{T}{2}} + e^{-\gamma \frac{T}{2}}} \nearrow$$

$$\frac{w_0 + j w_m - w_0 + j w_m}{w_0 + j w_m + w_0 - j w_m}$$

$$w = j \tan \omega \frac{T}{2} \quad \left\{ \begin{array}{l} w = j \sqrt{\dots} \end{array} \right.$$

FIKTIVNA PSEUDOFREKVENCIJA

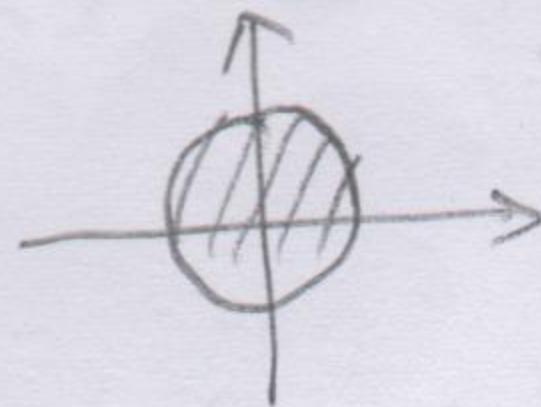
$z = e^{-\gamma T} \Rightarrow$ PADE OVA APROKSIMACIJA

$$n=1 \Rightarrow e^{-\gamma T} = \frac{1 - \frac{T_0}{2}}{1 + \frac{T_0}{2}}$$

$$e^{-\gamma T} = \lim_{n \rightarrow \infty} \left(\frac{1 - \frac{T_0}{2n}}{1 + \frac{T_0}{2n}} \right)^n$$

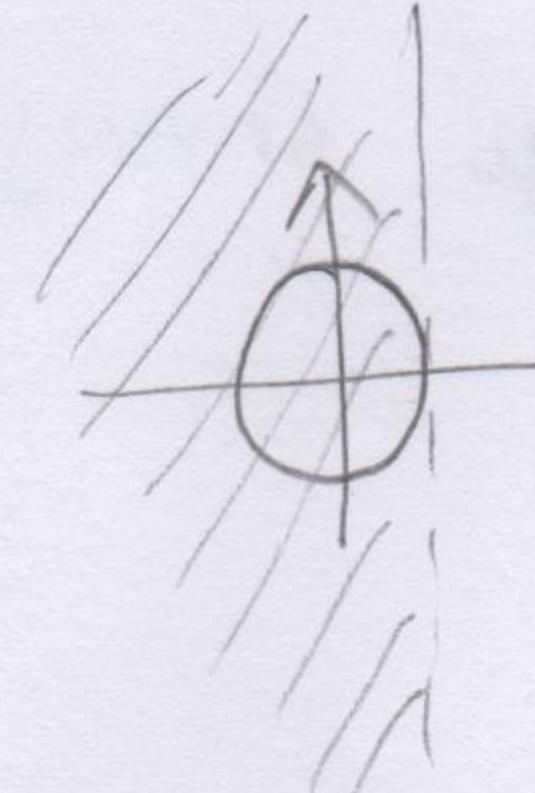
$$\text{MODIFIKIRAMO } \underline{\omega} = \frac{2}{T} \cdot w = \frac{2}{T} j \tan \omega \frac{T}{2} = w^* j \nearrow \text{ABSOLUTNA PSEUDOFREKVENCIJA}$$

TUŠTIN

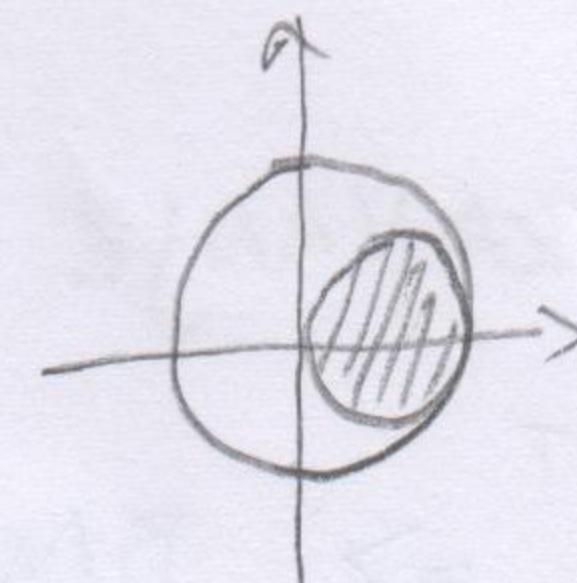


$$w^* = \frac{2}{T} \tan \frac{\omega T_0}{2}$$

EULER UNAPRIJEDNA (PREDIKCIJA)



EULER UNAZADNA (PROBLEM REZOLUCIJE)



5 LABOS

1. ZADATAK

SVI REGULATORI IMAJU JEDNAKE POLOVE

VAZNO:

- ODREĐIVANJE KONSTANTI PREMA UNAPRIJED ZADANIM PARAMETRIMA
- ODABIR VREMENA DISKRETIZACIJE
- STABILNOST PREKO JURYA

ODREDIMO $\sigma_m [\%]$, w_c , μ U $G_o(\eta)$

BODE IZ VJEŽBE

NAPRAVIMO TUŠTINA $G_o(\eta) \Rightarrow$ NACRTAMO BODEA $\{w^*\}$

↪ NADVIŠENJE SE POVEĆA μ BE SMANJI w_c JE ISTA t_m JE ISTO

DODAVANJEM POJAČANJA POVEĆAVAMO μ

AKO IZADEMO IZ DOPUŠTENOG INTERVALA T ODZN
SE VIŠE NE POKLAPA DOBRO SA KONTINUIRANM

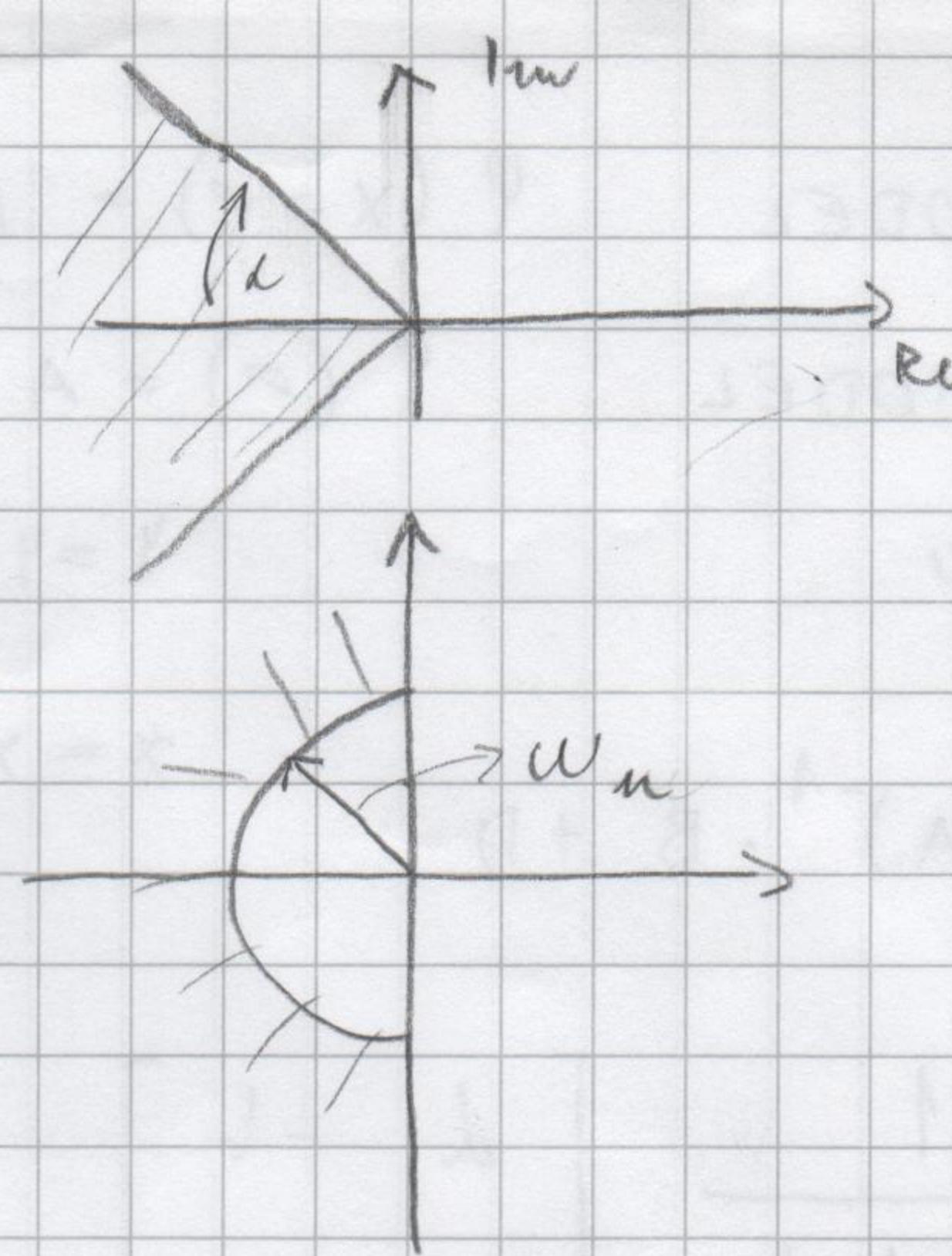
MAKSIMALNO NADVIŠENJE:

$$\sigma_m < \sigma_{\max} \rightarrow \sum_m \geq \sum_{\max}$$

$$\omega \leq \pi c \cos \sum_{\max}$$

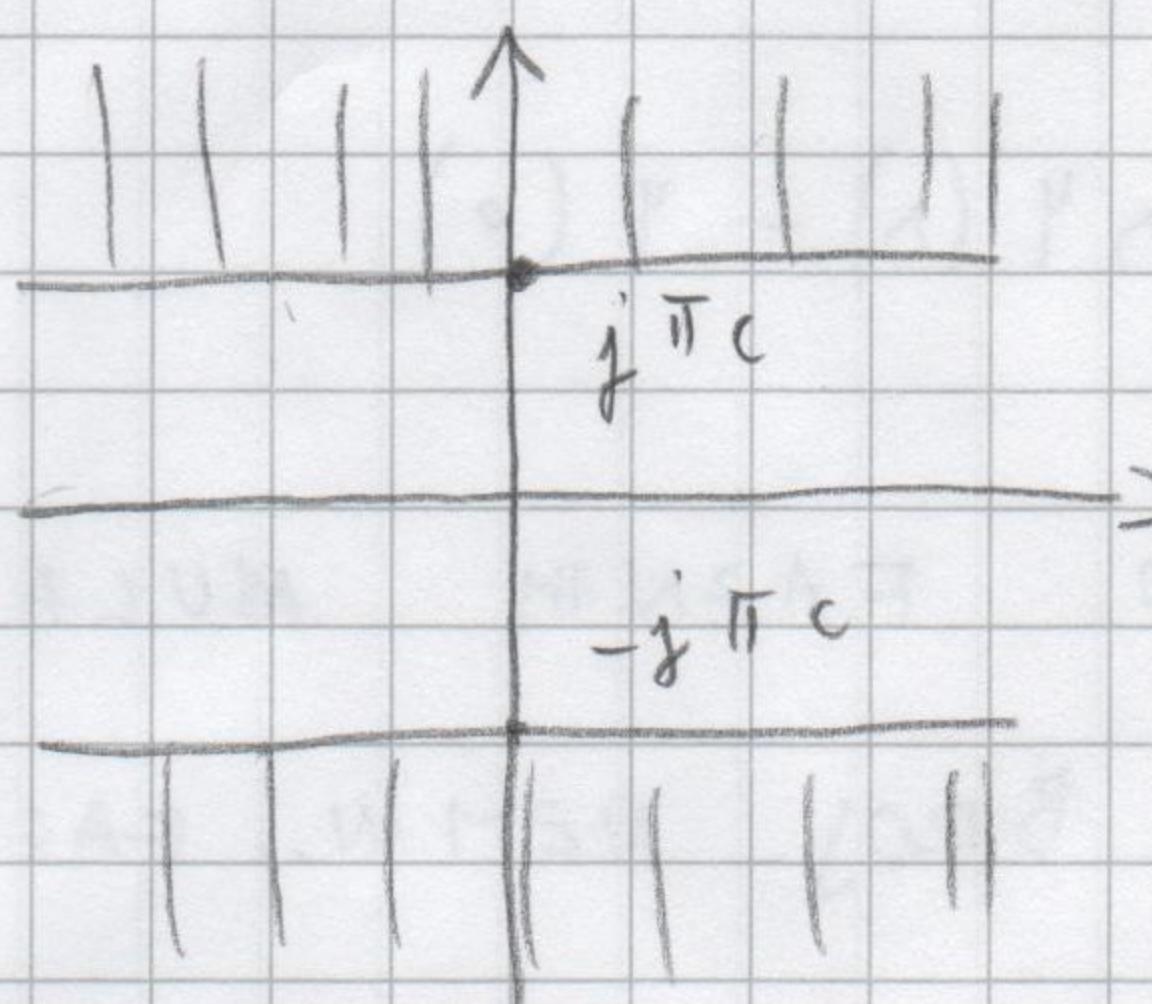
VRIJEME POBASTA:

$$t_p \leq t_{\max} \quad w_m \geq w_{\max}$$



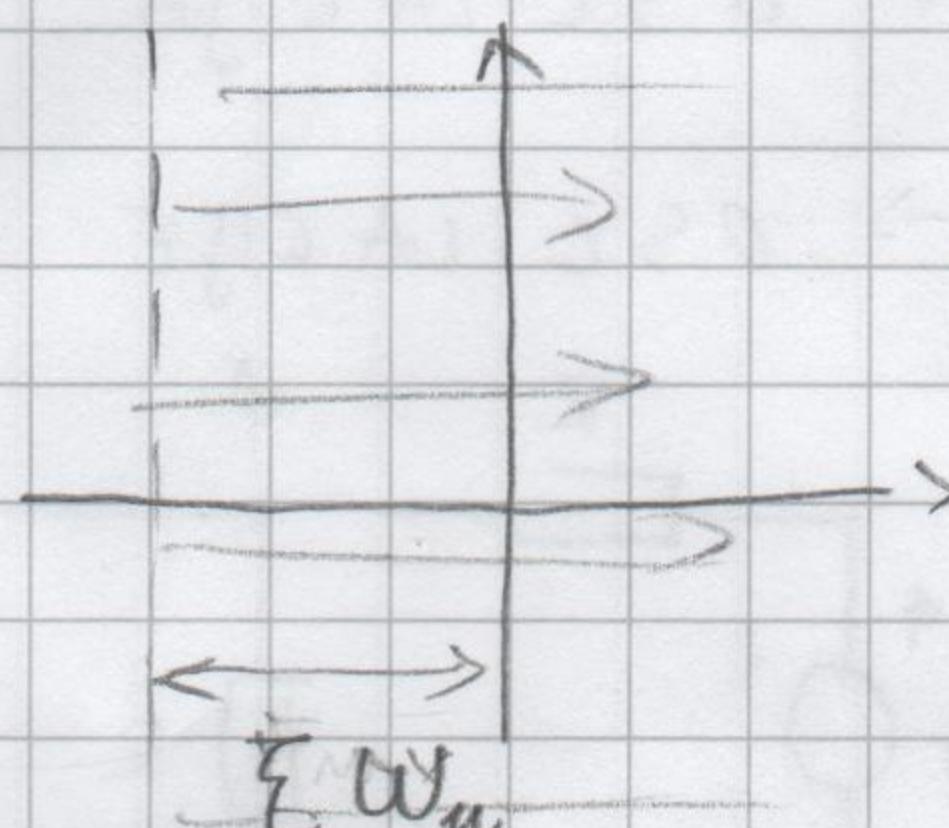
$$t_m < c$$

$$w_m \sqrt{1-\varepsilon^2} > \pi \cdot c$$



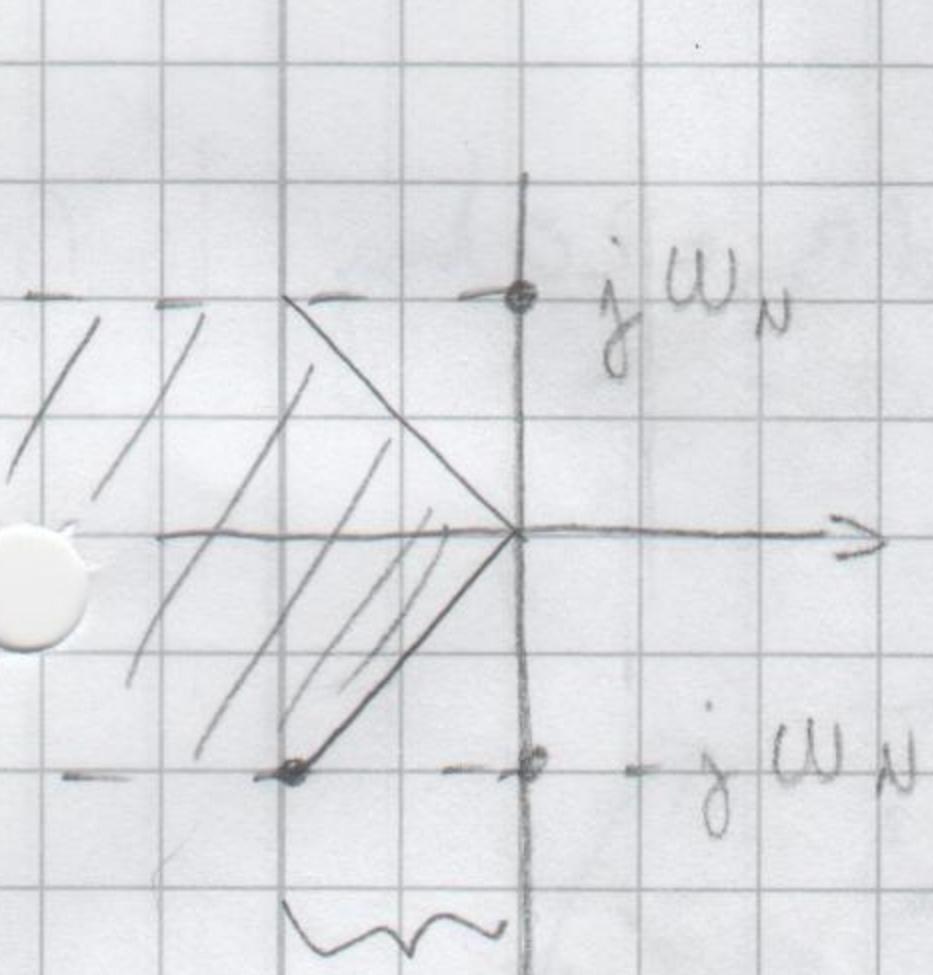
VRIJEME USTALJIVANJA:

$$t_e \leq t_{\max} \rightarrow \sigma \geq \sigma_{\max}$$

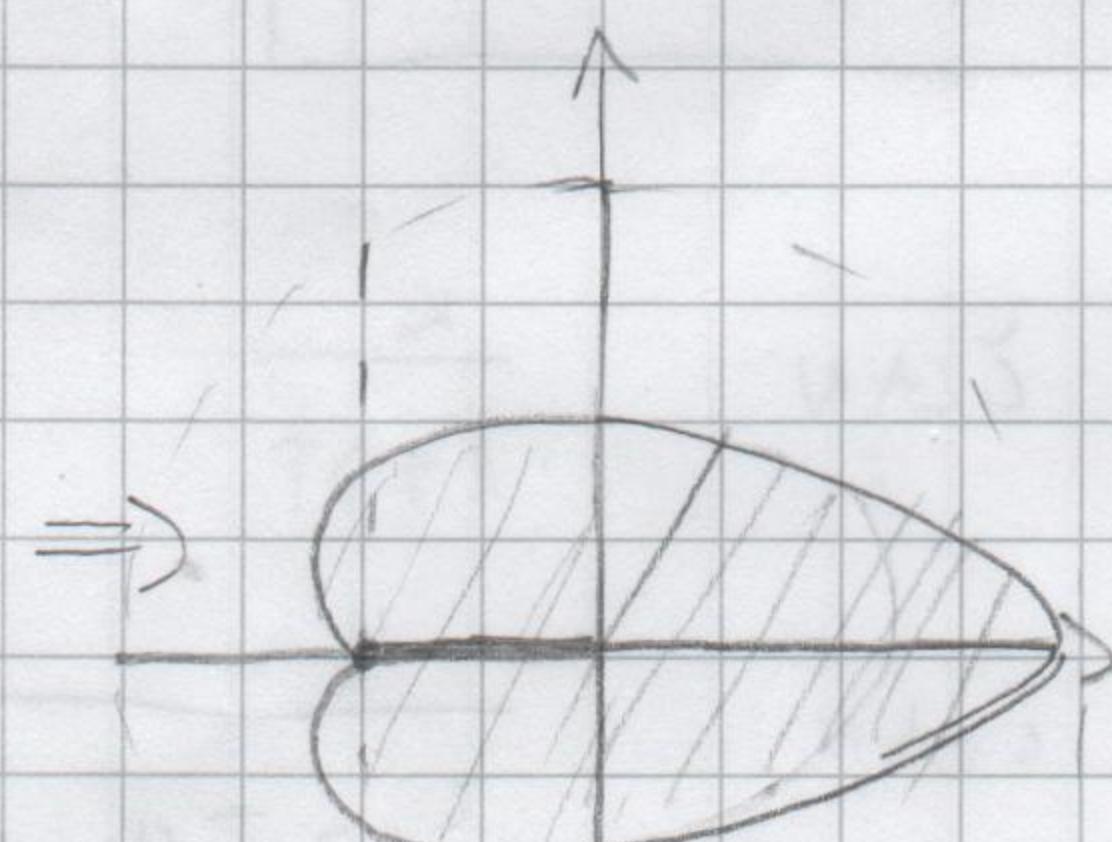


$$\lim_{s \rightarrow 0} |G(s)| = \lim_{z \rightarrow 1} |G(z)|$$

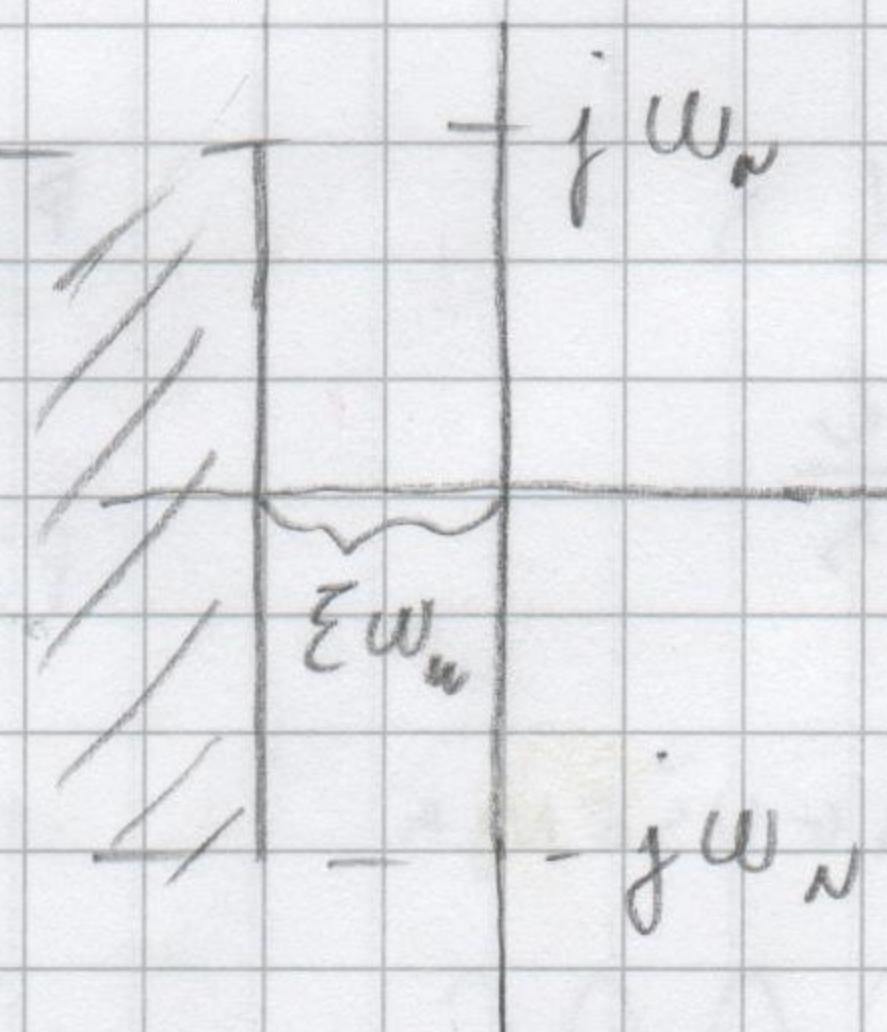
$$= \lim_{z \rightarrow 1} (1-z^2) E(z)$$



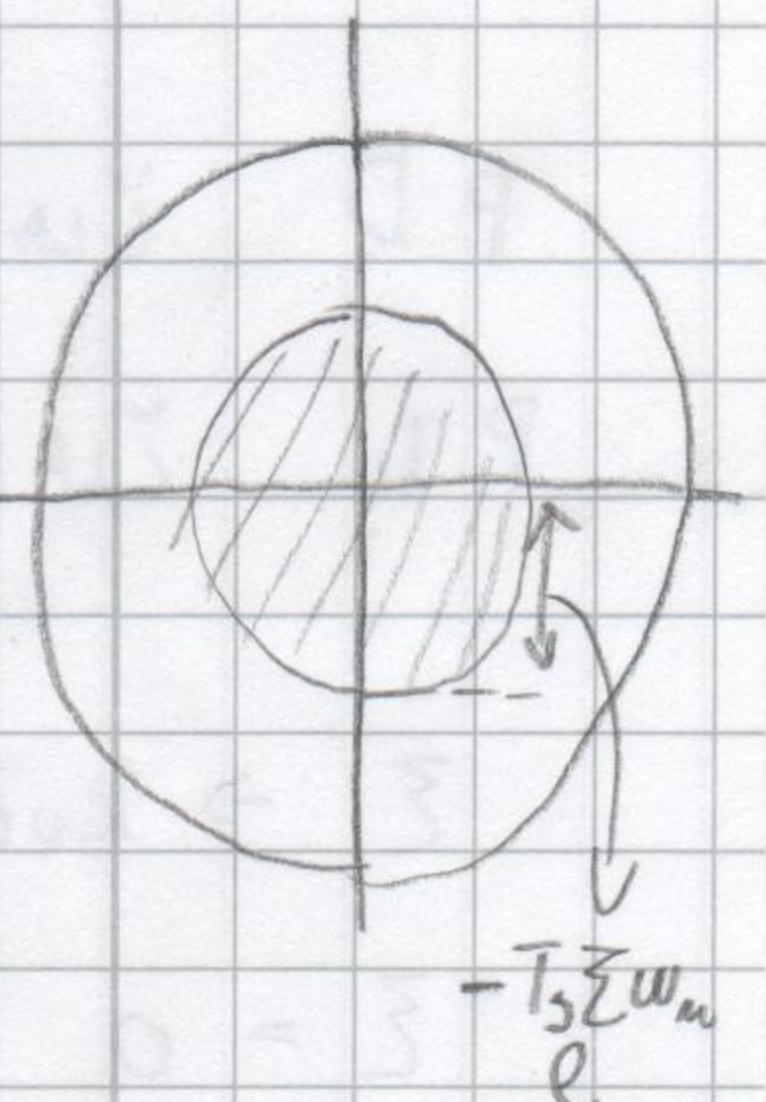
$$\sigma = \frac{\varepsilon}{\sqrt{1-\varepsilon^2}} w_n$$



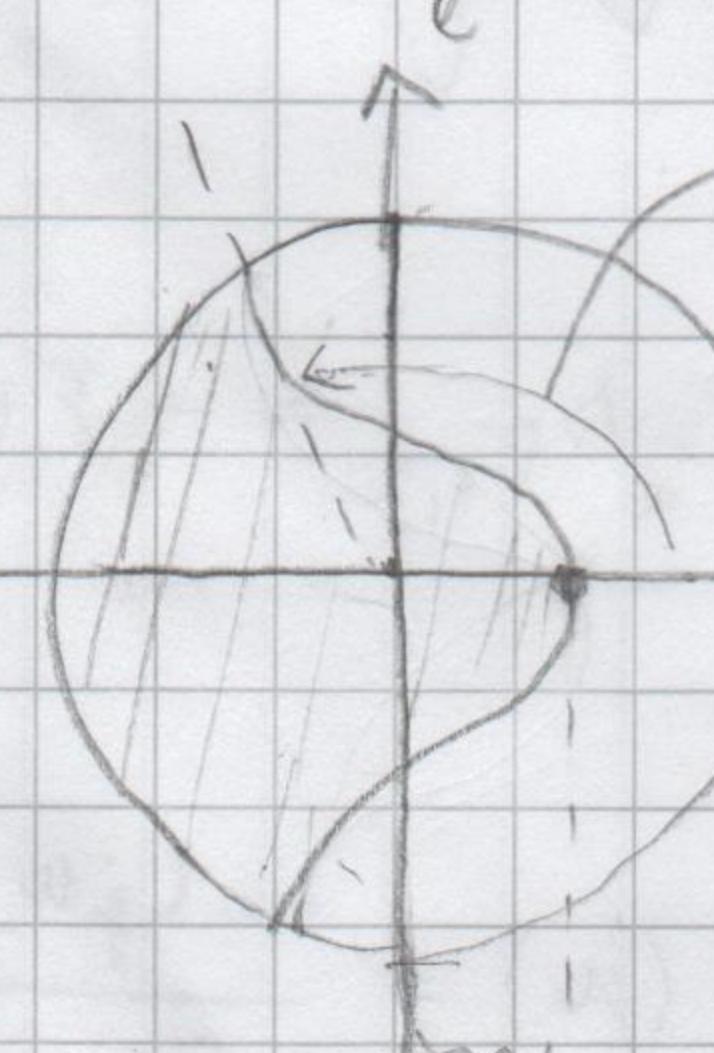
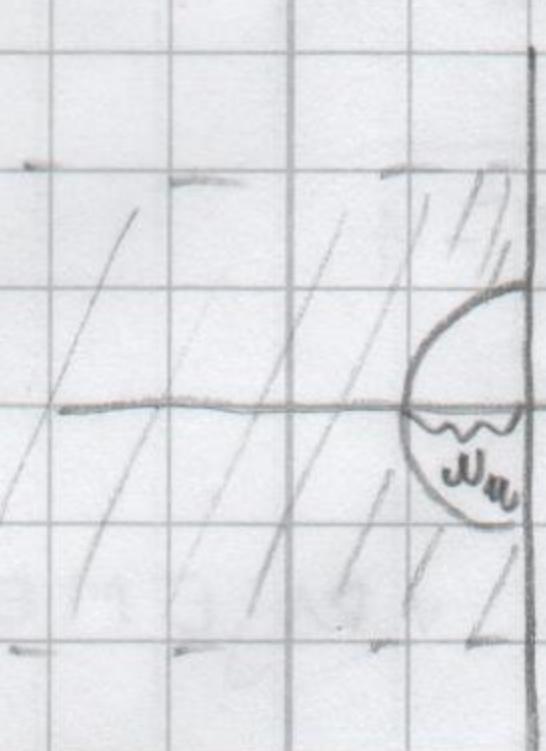
$$-\bar{\varepsilon} T_3$$



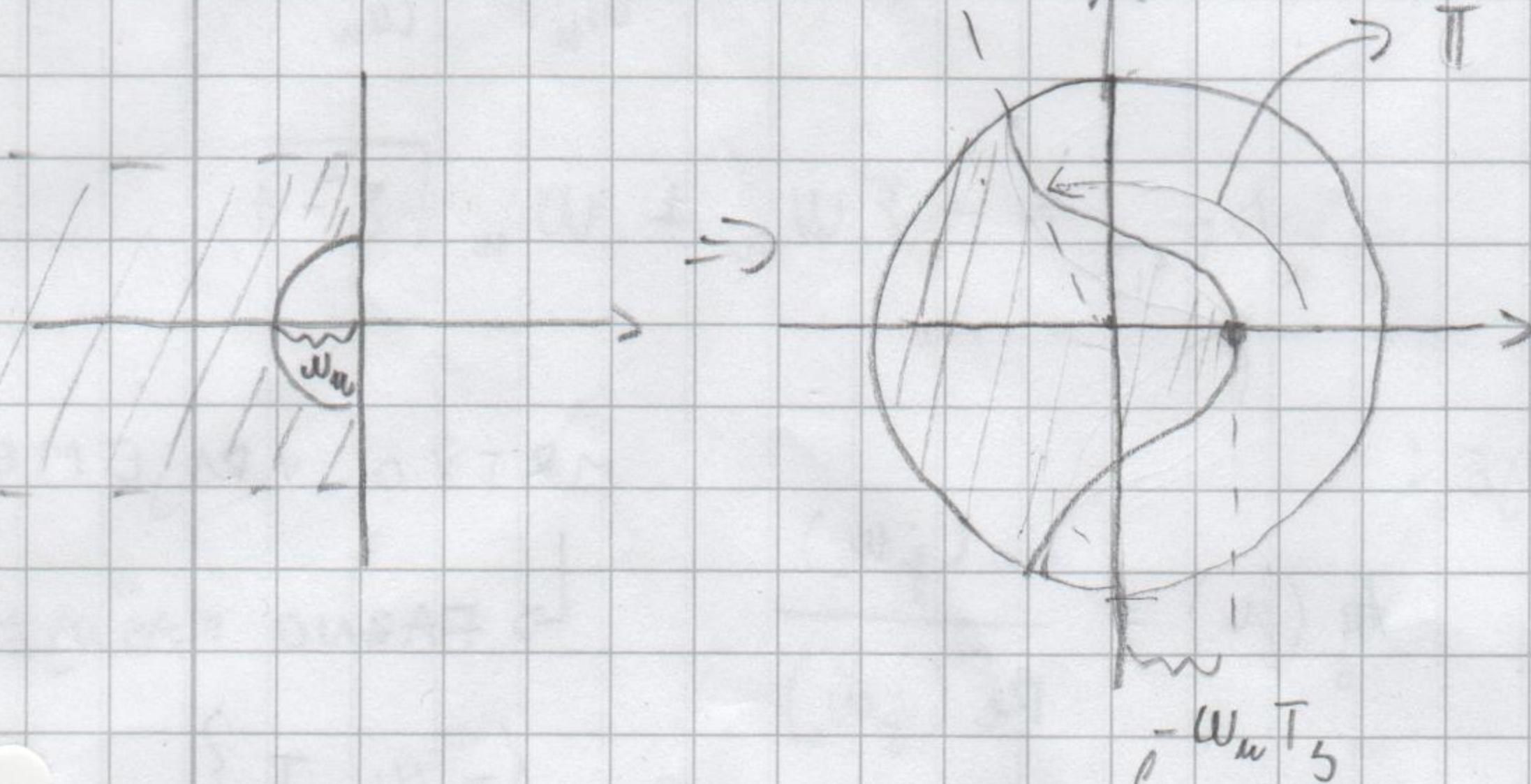
$$\bar{\varepsilon} w_n$$



$$-T_3 \bar{\varepsilon} w_n$$



$$\frac{w_n}{w_N} \text{ ili } 180^\circ \frac{w_n}{w_N}$$



$\Im \{G(j)\} \Rightarrow \text{ČUVA TEŽINSKU FJU. } \{G(j)\} \text{ TUSTIN} \Rightarrow \text{ČUVA PREŠJEĆNU FREKVENCIJU}$

$ZOM \Rightarrow \text{ČUVA PRIJELAZNU FJU. } \{G(j)\}$

NELINEARNI MODEL $y(x=\infty) = A(0) + A(\infty) \Rightarrow$ DERIVACIJE SU NULA

LINEARIZIRANI MODEL

$$y(\infty) = A(0) + \underbrace{\Delta A(\infty)}$$

$$\dot{x} = Ax + Bu$$

$$y = c x + du \quad y = y_0 + \Delta y \quad \text{iz PREJENOSNE FUNKCIJE}$$

$$G(s) = C(sI - A)^{-1} \cdot B + D$$

$$x = x_0 + \Delta x$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$y(t) = i(t)$$

$h(t) \Rightarrow$ PRIJELAZNA

FUNKCIJA $y(t) \cdot s(t)$

$$G(s) = sH(s)$$

$$\mathcal{L}(y) = sY(s) - y(0)$$

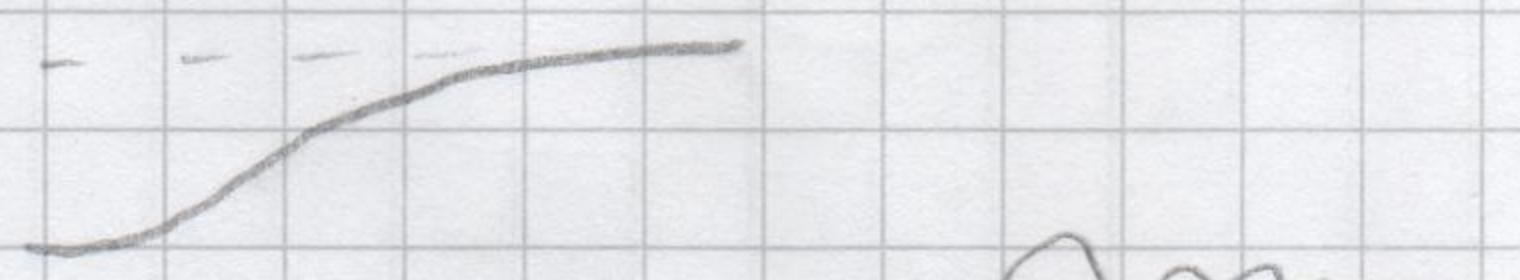
$$\mathcal{L}(\ddot{y}) = s^2 Y(s) - s\dot{y}(0) - y(0)$$

NE PARNI BROJ

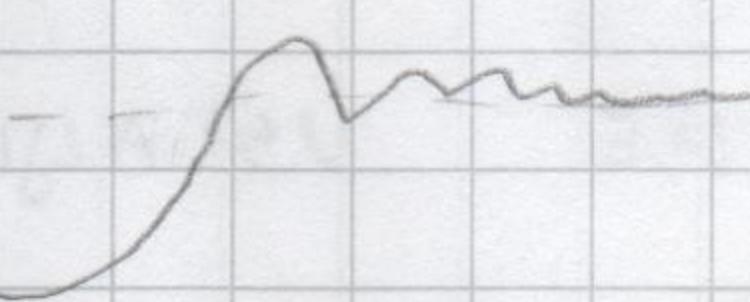
NE MINIMALNO FAZNIH NULA NPR. $(n-1) \Rightarrow$ PODFAČAJ

↪ PARNI BROJ NEMIN. FAZNIH NULA \Rightarrow NE MA PODFAČAJA

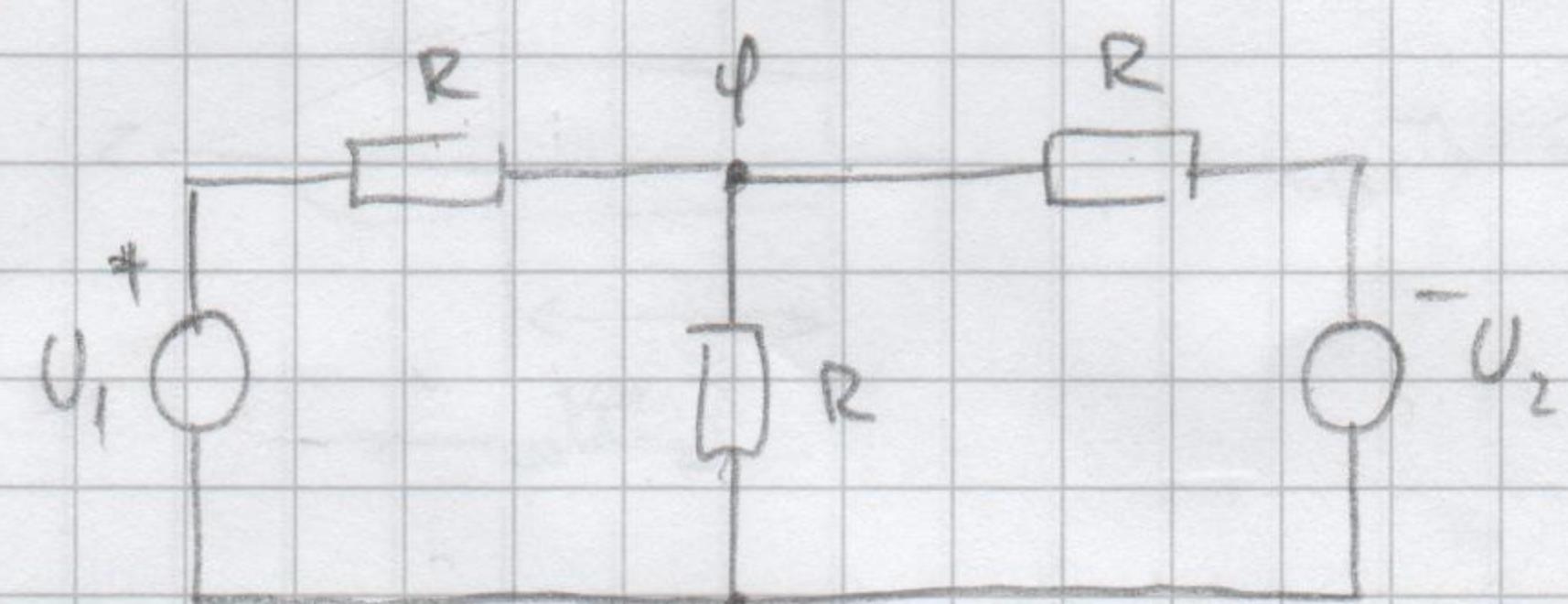
POLLOVI \Rightarrow REALNI \Rightarrow NE MA OSCILACIJA



↪ KOMPL. KONJ. \Rightarrow OSCILACIJE I PREBAČAJ



POTENCIJAL ČLANA



$$P(U) = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) U = \frac{U_1 - U_2}{R_3}$$

PD ČLAN

$$d \propto$$

PT₁ ČLAN

$$\frac{k}{1+sT}$$

$$-3 \text{ dB} = 20 \log |G(j\omega_n)|$$

PI ČLAN

$$\frac{1}{s}$$

PT₂ ČLAN

$$\frac{k}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

$\zeta \rightarrow$ KOEF. PRAGUŠENJA

$$\zeta = 0 \rightarrow$$

$$\zeta < 0 \rightarrow$$

$$\frac{1}{\frac{s^2}{\omega_n^2} + \frac{2\zeta}{\omega_n} s + 1}$$

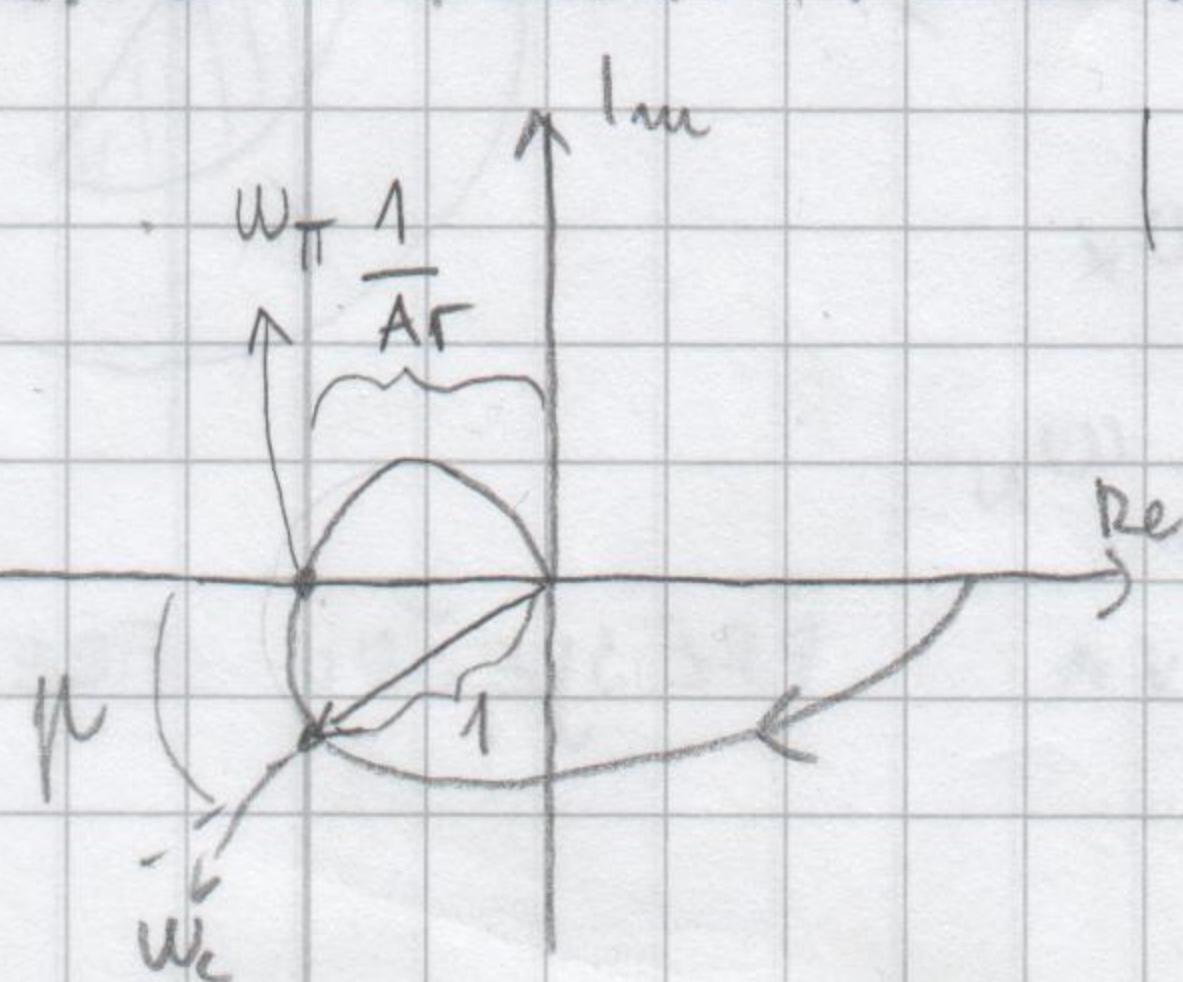
$\omega_n \rightarrow$ FREKVENCIJA

TRAJNIH OSCILACIJA

$$\omega_{p1,2} = -\zeta\omega_n \pm \omega_n \sqrt{\zeta^2 - 1}$$

FAZNO I AMPLITUDNO OSIGURANJE:

MRT VO VRIJEME



$$|G_0(j\omega_c)| = 1 \quad tg(\mu) = \frac{\text{Im}(j\omega_c)}{\text{Re}(j\omega_c)}$$

$$\text{Im}(j\omega_\pi) = 0 \quad = -180^\circ$$

$$\{-\omega_c T\}$$

$$\left\{ \omega_\pi > \omega_c \Rightarrow \text{SUSTAV JE STABILAN} \right\}$$

↪ FAZNO KASNJENJE

Sistematisacija osnovnih članova za prikaz amplitudno-frekvencijske i fazno-frekvencijske karakteristike Bodeovim načinom prikazana je u Tablici 4.3.

Tablica 4.3: Osnovni članovi Bodeovih dijagrama

Amplitudna i fazna karakteristika (Bodeov prikaz)	Prijenosna funkcija člana
	$G(j\omega) = K$ $A_{dB}(\omega) = 20 \log K $ $\phi(\omega) = \begin{cases} 0, & K > 0 \\ \pi, & K < 0 \end{cases}$
	$G(j\omega) = j\omega$ $A_{dB}(\omega) = 20 \log \omega$ $\phi(\omega) = \frac{\pi}{2}$
	$G(j\omega) = \frac{1}{j\omega}$ $A_{dB}(\omega) = -20 \log \omega$ $\phi(\omega) = -\frac{\pi}{2}$
	$G(j\omega) = 1 + j\frac{\omega}{\omega_p}$ $A_{dB}(\omega) = 20 \log \sqrt{1 + (\frac{\omega}{\omega_p})^2}$ $\phi(\omega) = \arctan \frac{\omega}{\omega_p}$
	$G(j\omega) = \frac{1}{1+j\frac{\omega}{\omega_p}}$ $A_{dB}(\omega) = -20 \log \sqrt{1 + (\frac{\omega}{\omega_p})^2}$ $\phi(\omega) = -\arctan \frac{\omega}{\omega_p}$
	$G(j\omega) = \frac{1}{1+2\xi j(\frac{\omega}{\omega_p})+(j\frac{\omega}{\omega_p})^2}$ $A_{dB}(\omega) \approx -40 \log \sqrt{1 + (\frac{\omega}{\omega_n})^2}$ $\phi(\omega) \approx -2 \arctan \frac{\omega}{\omega_n}$
	VAŽNO

NEMINIMALNA FAZA

$$\sigma_m \% = \frac{\ln(\omega_m) - K}{K} \cdot 100 = 100 e^{-\frac{E \pi}{V_1 - E^2}}$$

$$\omega_m = \frac{\pi}{w_n \sqrt{1-E^2}} \quad T_f \approx \frac{1.8}{w_n}$$

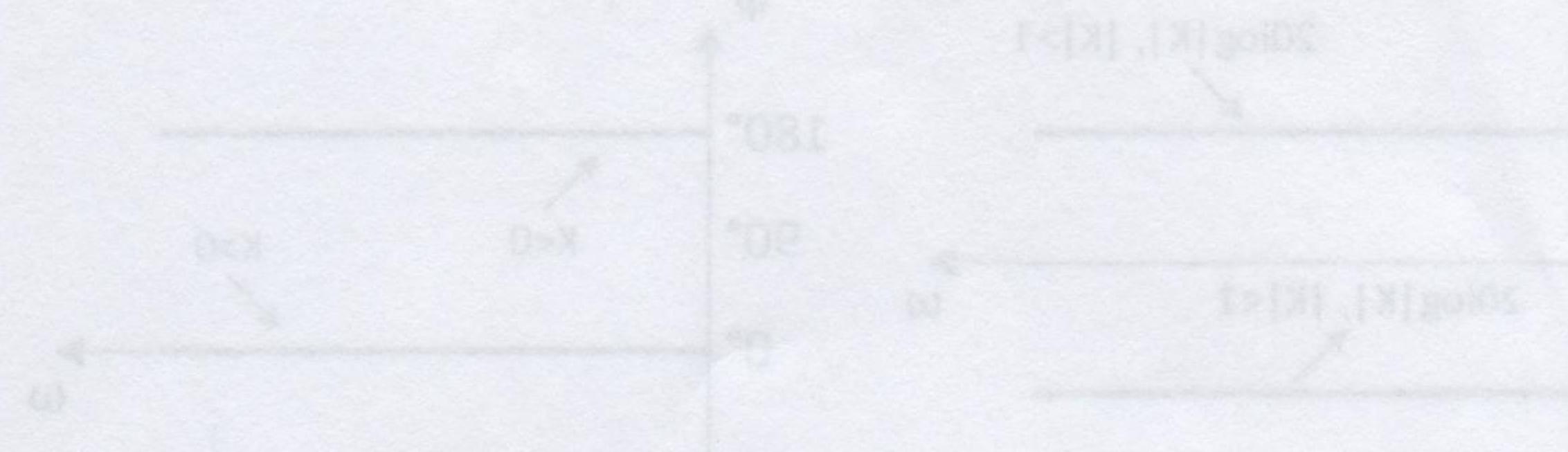
$$T_E \approx \frac{4.6}{E w_n}$$

$$\begin{cases} \lambda < 0 \\ 0 < \lambda < \pi \\ 0 > \lambda > \pi \end{cases} = (\omega)_0$$

SUSTAV

2. REDA BEZ

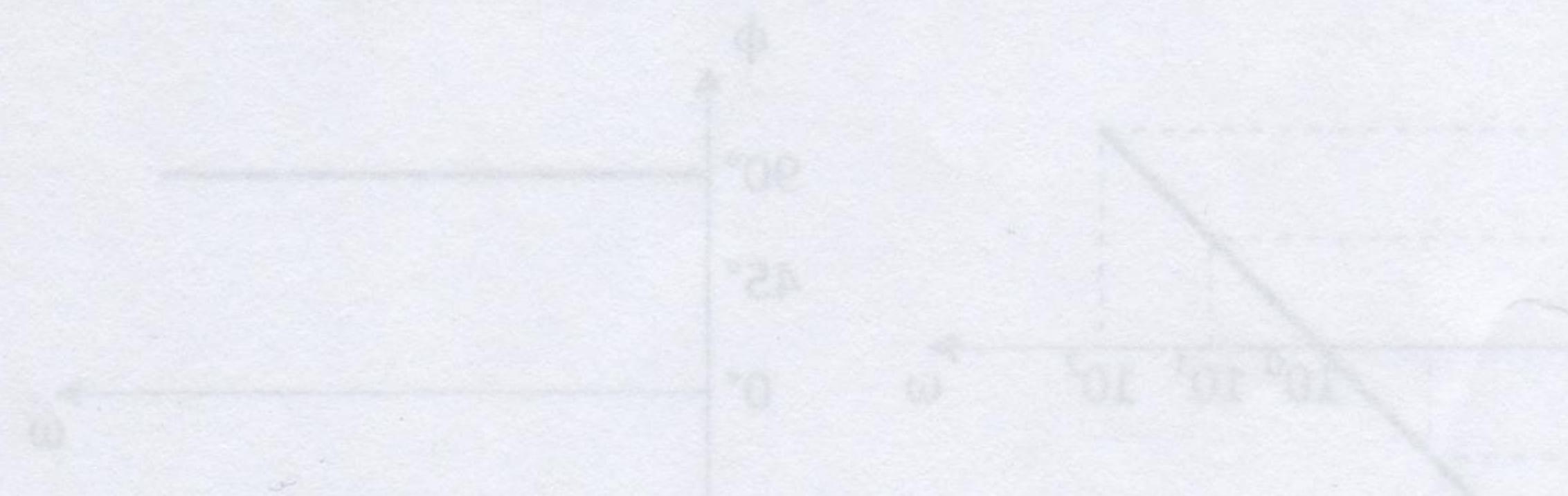
NULA



$$\omega_c = (\omega)_0$$

$$\omega_{\text{gol}} = (\omega)_{\text{gol}}$$

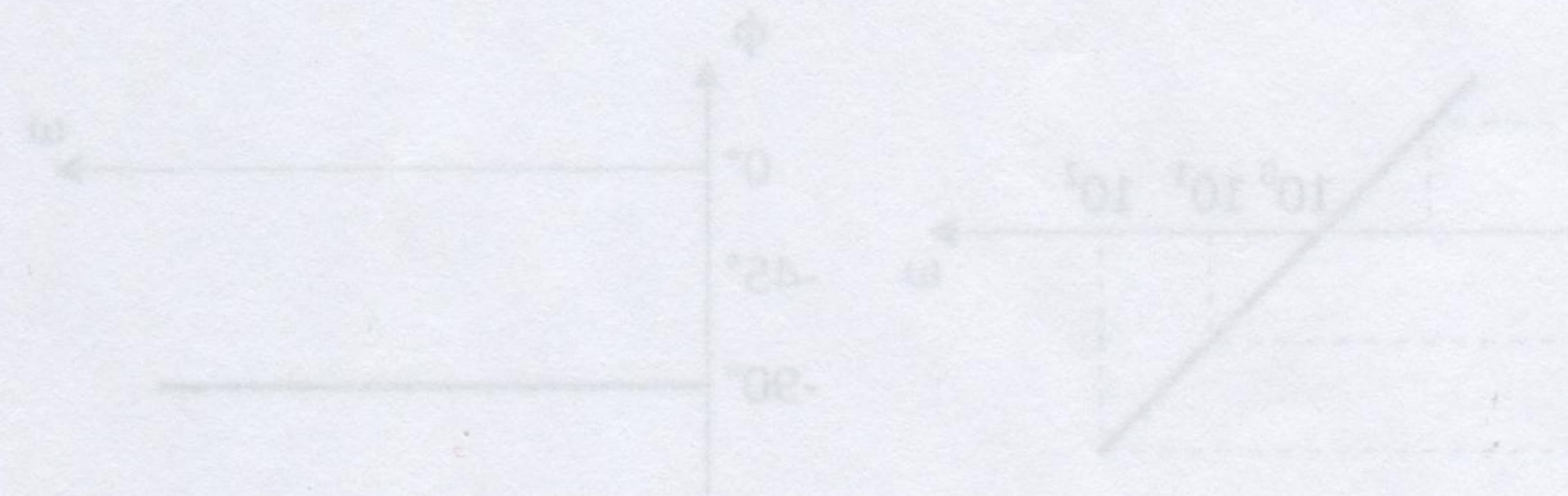
$$\omega_c = (\omega)_0$$



$$\omega_c = (\omega)_0$$

$$\omega_{\text{gol}} = (\omega)_{\text{gol}}$$

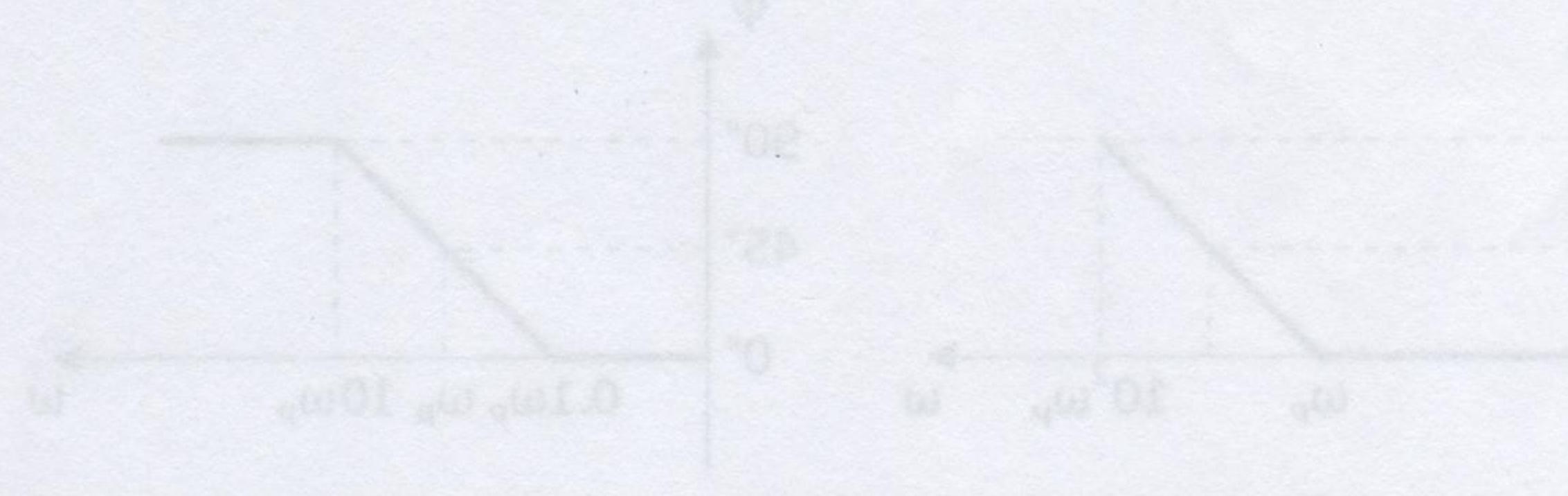
$$\omega_c = (\omega)_0$$



$$\omega_c = (\omega)_0$$

$$R(\omega) + jI(\omega) = (\omega)_{\text{m}}$$

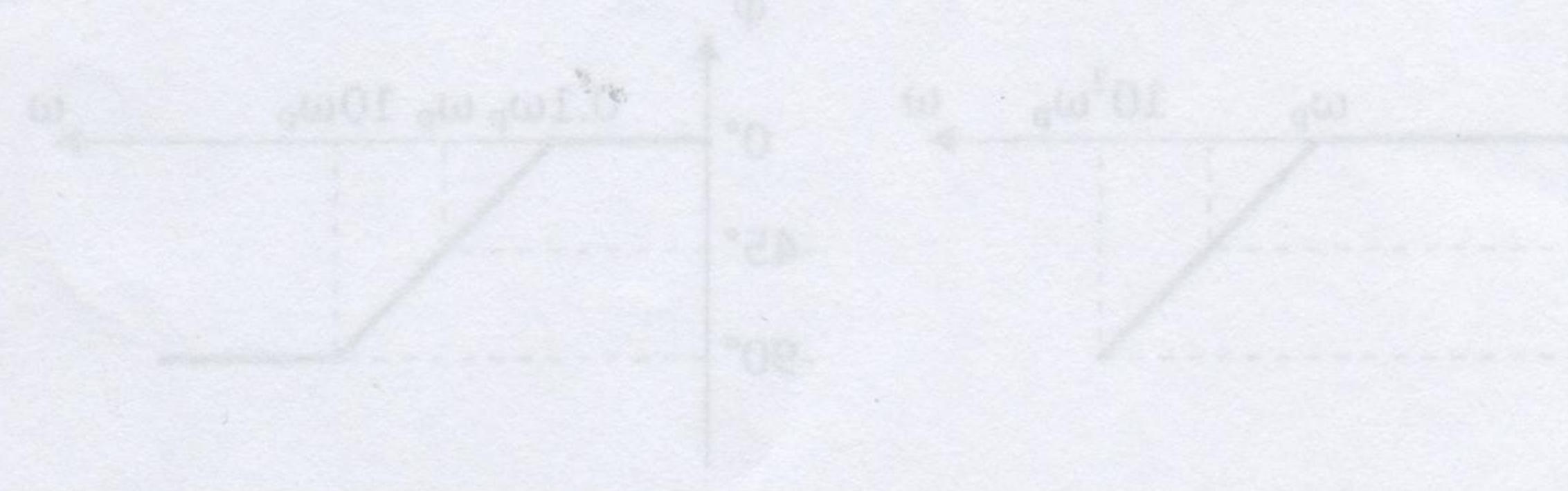
$$\omega_{\text{m}} = (\omega)_0$$



$$\omega_c = (\omega)_0$$

$$R(\omega) + jI(\omega) = (\omega)_{\text{m}}$$

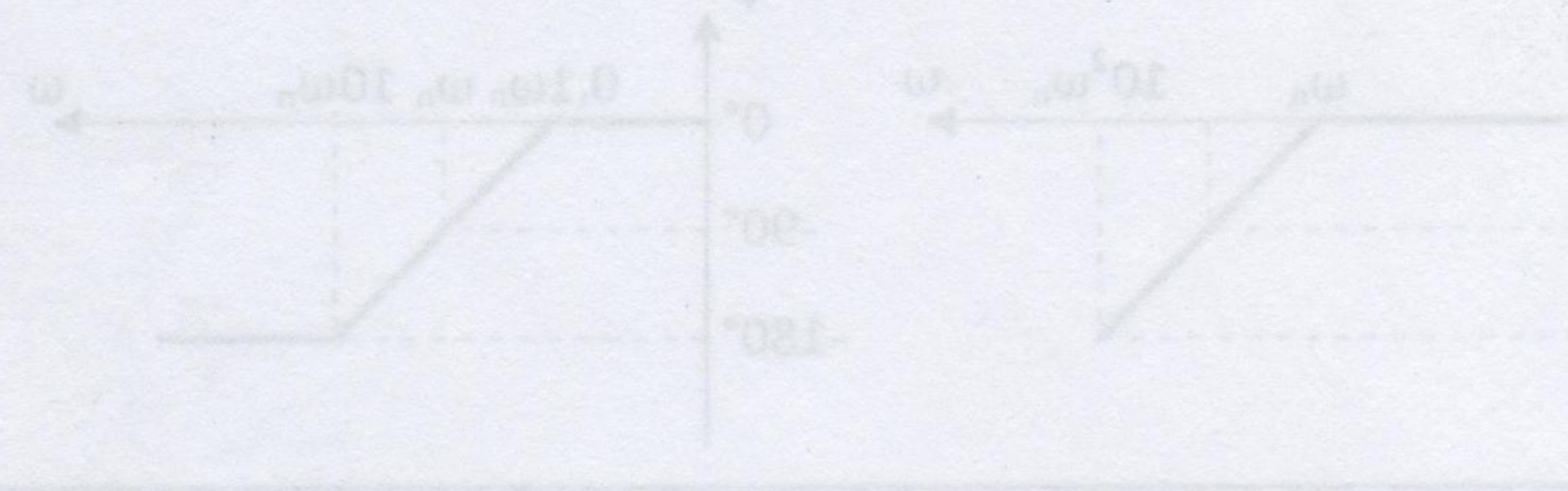
$$\omega_c = (\omega)_0$$



$$\omega_c = (\omega)_0$$

$$R(\omega) + jI(\omega) = (\omega)_{\text{m}}$$

$$\omega_c = (\omega)_0$$



ASAF - ALAMINDE

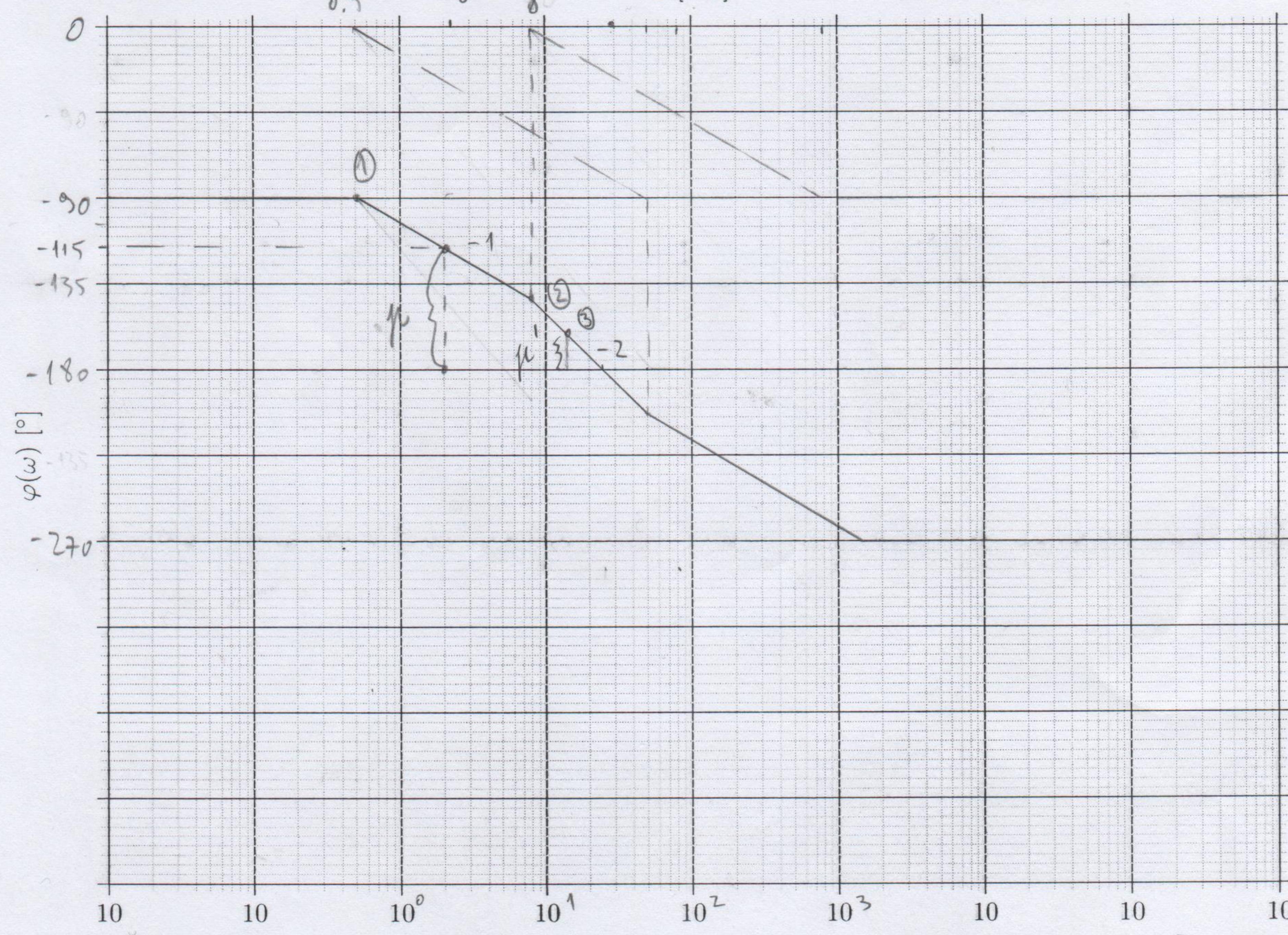
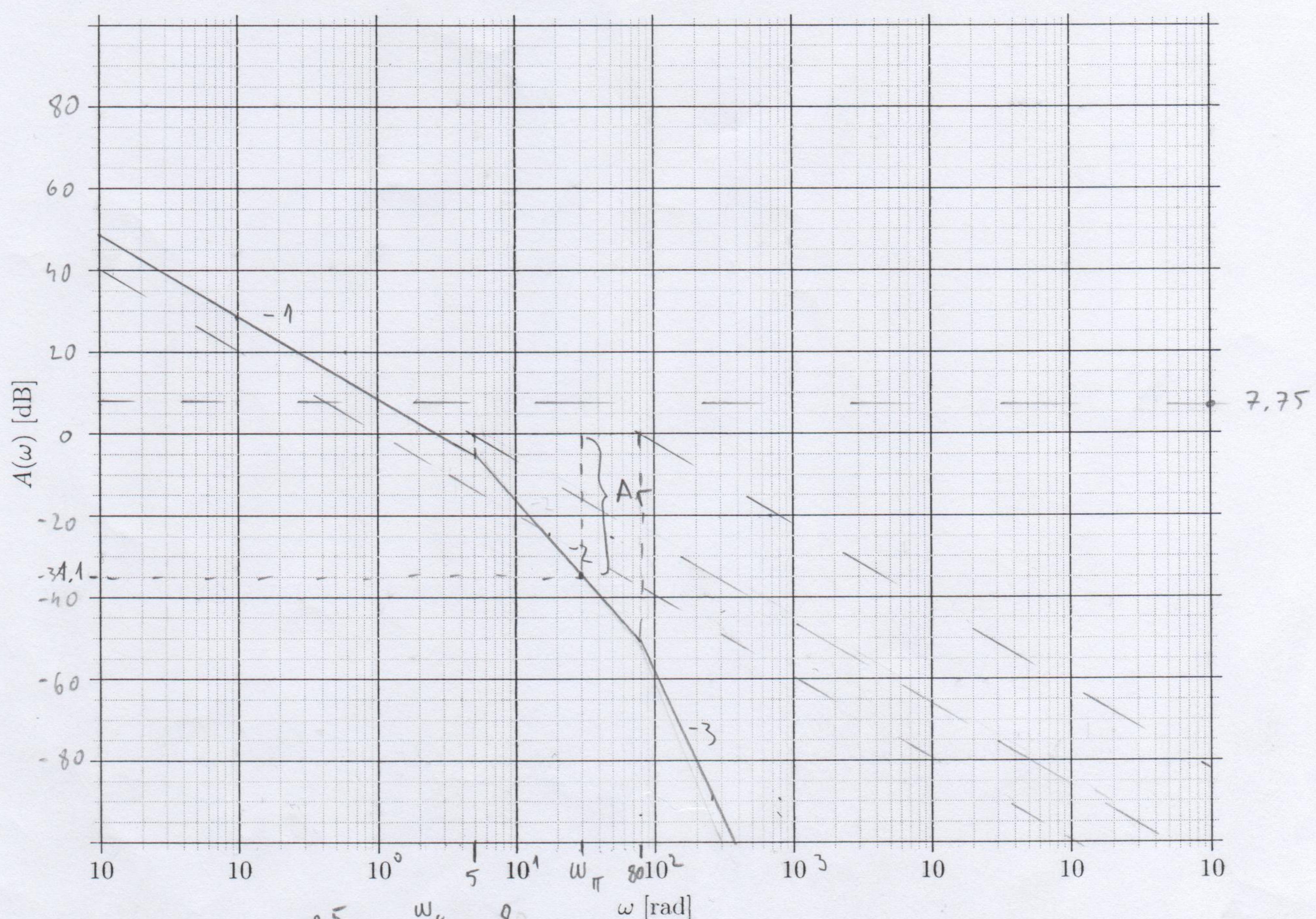
$$(1) \cdot \frac{1}{s} = (\alpha)H$$

$$\frac{1}{s} = \frac{1}{s+1} \Rightarrow s = -1$$

$$(1) \cdot \frac{1}{s} = (\alpha)H$$

$$\frac{1}{s} = \frac{1}{s+1} \Rightarrow s = -1$$

$$\frac{1}{s} = \frac{1}{s+1} \Rightarrow s = -1$$



$$\mu - 180^\circ = -115^\circ$$

$$\psi^1 = 15^\circ$$

$\omega_\pi > \omega_c \rightarrow$ PREŠEK $A(\omega) = 0$
 PREŠEK S $\varphi = -180^\circ$ \hookrightarrow SUSTAV JE
 STABILAN

LABOS 2

1^o ZADATAK { LINEARIZIRATI JEDNADŽBU
PRIJENOSNA FJA } $\rightarrow g(s) = \frac{Y(s)}{X(s)} \rightarrow \frac{Y(s) + \Delta Y}{X(s) + \Delta X}$

\hookrightarrow IZLAZ KOJI DOBIJEMO SIMULACIJOM $\{\Delta Y\}$ ZBROJIMO
NA $Y_0 \rightarrow Y = Y_0 + \Delta Y$

2^o ZADATAK \rightarrow LINEARIZIRATI SUSTAV IZ PRVOG LABOSA \checkmark , NAPRAVITI MATLAB MODEL
JEDNADŽBE STANJA PREKO UNAPRIJEĐENIH ZADANIH PARAMETARA
ODREDITI

\rightarrow PARALELNO SIMULIRATI LINEARIZIRANI I NELIN. MODEL ZA
ZADANU RADNU TOČKU $\{\text{TREBAJO BITI Približno jednaki}\}$

\rightarrow POUKA: MODEL VRISEDI SAMO ZA PRORAČUNATO RADNU TOČKU

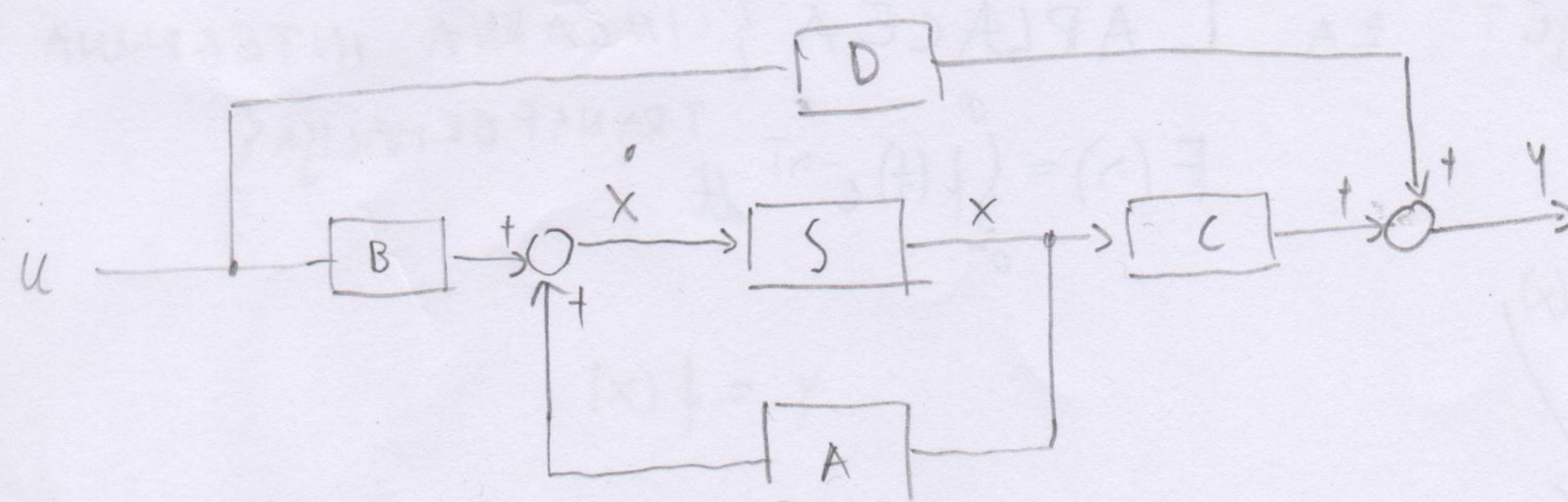
⑤ PRIKAZ U PROSTORU STANJA

$\{\text{koristimo za kompleksne sustave}\}$

PRIMJER \rightarrow MATRICE NAPONA I STRUJA IZ ELEKTRIČNIH KRUGOVA

MOGUĆE PITANJE: NACRTAJ BLOKOVSKI PRIKAZ JEDN. STANJA

$$\dot{x} = Ax + Bu \quad y = Cx + Du$$



A \rightarrow VLASTITO VLADANJE SUSTAVA $\{\text{prirodni odziv}\}$

B \rightarrow OPIS DJELOVANJA VANJSKE POBODE

C \rightarrow IZLZNA JEDNADŽBA

D \rightarrow PROSLIJEĐUJE ULAZNE VELIČINE NA IZLAZ

6 FREKVENCIJSKA DOMENA I STABILNOST

KAUZALNI
SUSTAVI

$$g(t) \rightarrow \text{TEŽINSKA FJA} \Rightarrow \text{ODZIV NA } \delta(t) \quad t \geq 0$$

$$h(t) \rightarrow \text{PRIJELAZNA FJA} \Rightarrow \text{ODZIV NA } \mu(t)$$

$$y(t) = h(t) \quad G(s) = H(s)$$

SLOBODNI I PRISLJUČNI ODZIV

$$Y^1 + Y = H U^1 \Rightarrow Y = Y_{SL} + Y_{PRISLJUČNI}$$

RUB STABILNOSTI

$$Y(s) = \frac{B(s)}{N(s)} + \frac{B'(s)}{N'(s)} \cdot U(s)$$

UVODI SE POJAM

NEMINIMALNO FAZNA NULA ili POL

NFN \rightarrow PARNI BROJ NEMA PODBAČAJA

POLOVI $\begin{cases} \rightarrow \text{REALNI} \rightarrow \text{NEMA OSCILACIJA} \\ \rightarrow \text{KOMP. KONJ.} \rightarrow \text{OSCILACIJE} \end{cases}$



$$y(\infty) = \lim_{s \rightarrow 0} G(s)$$

$$y(0^+) = \lim_{s \rightarrow \infty} G(s)$$

NE UZIMAMO $\delta(t)$

U OBZIR

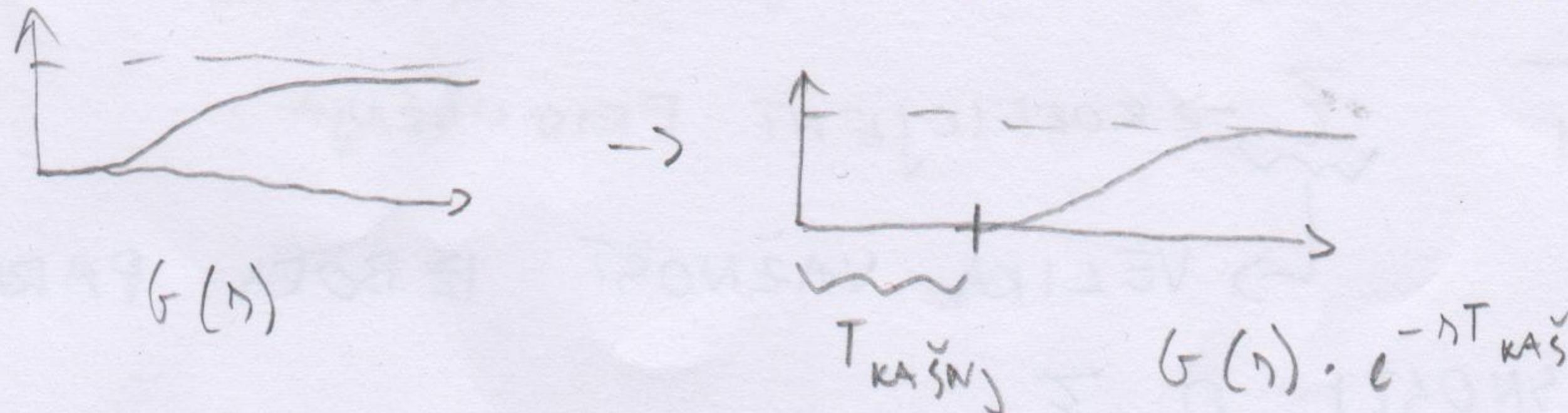
\downarrow
ODZIV NA HARMONIJSKO
POBODU $y = 1 + \text{mewat}$

VIZUALIZACIJA PREKO ASINKRONOG MOTORA

$$\begin{cases} A_y = A_u A_g \\ \phi_y = \phi_u + \phi_g \end{cases}$$

MRTVO VRIJEME $\{ \text{TRANSPORTNO KAŠNJENJE} \} e^{-\sigma T}$

\hookrightarrow U SUSTAVIMA U KOJIM SE PRENOŠI MASA, ENERGIJA, PODATCI

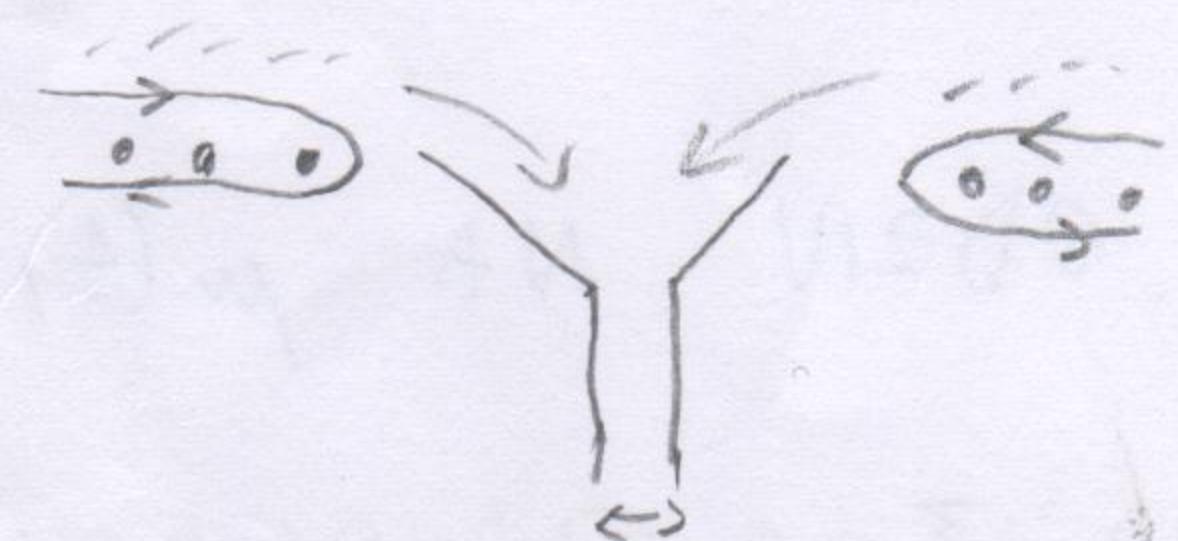


NE MIJENJA AMPLITUDU ALI UTJEĆE NA FAZU

$$A = 1 = |e^{-\sigma T}|$$

$$\varphi \rightarrow e^{-j\omega NT} = \cos \omega NT - j \sin \omega NT \quad \varphi = -\arctg \frac{\sin \omega NT}{\cos \omega NT} = -\omega NT$$

DOPUSTENO je SAMO KONALNO KAŠNJENJE



⑧ ALATI ZA ODREĐIVANJE STABILNOSTI

↳ BIO JE POTREBAN NAČIN ODREĐIVANJA STABILNOSTI \hookrightarrow SE MOGAO KORISTITI U PRAKSI
ALGEBARSKI \rightarrow HURWITZ

NYQUIST I BODE \rightarrow SNIMANJEM FREKV KARAKT. LAGANO ODREĐIVANJE STABILNOSTI SUSTAVA

⑨ NYQUIST \Rightarrow PARAMETARSKI ZAPIS PRIJENOSNE FJE $\{G_o\}$

$$G(j\omega) = A(\omega) e^{j\phi(\omega)} \quad \hookrightarrow \text{ZATVORENA KRIVULJA}$$

$G(0) = A(0) \Rightarrow$ STATIČKO POJAČANJE

POVEZANOST S BODE OM $\{ \text{ODMAH SE VIDI ULAZ } w = \infty \}$

⑩ BODE \rightarrow APROKSIMACIJA PRAVCIMA \Rightarrow UVJEK SE ZAJEDNO CRTAJU A + φ KARAKT ZBOG MOGUĆIH NEMINIMALNO FAZNIH NULA

UZMI PAPIR

↳ ⑪ PRIKAZ U LOG SKALI

⑫ PT2 ČLAN \rightarrow U PRAKSI NASVAŽNIJI ČLAN $\{ \text{OPISUJE PONAŠANJE OSCILATORA} \}$

↳ POSJEDUJE MODOVE $\{ \text{KOMPL.-KONJ. POLOVI} \} \Rightarrow$ UZROKUJE TITRANJE

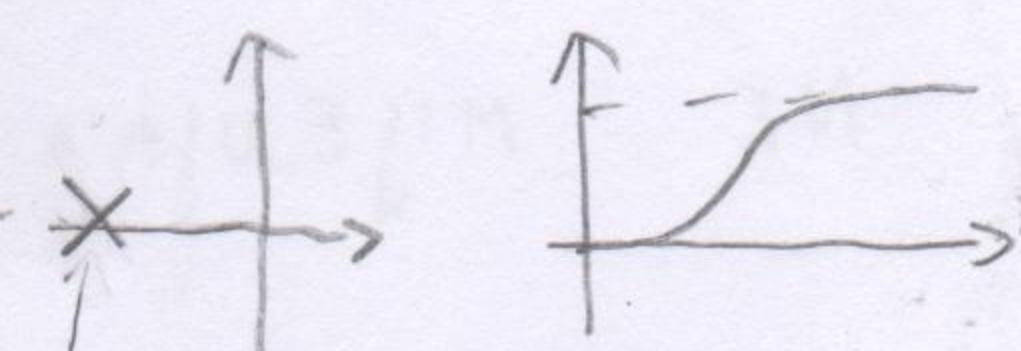
\rightarrow LJUDSKA TEHNOLOGIJA SE TEMELJI NA TITRAJnim KRUGOVIMA $\{ \text{😊} \}$

$$G(j) = \frac{K}{\frac{\zeta^2}{\omega_n^2} + \frac{2\zeta}{\omega_n} j + 1} \quad \omega_n \rightarrow \text{FREKVENCIJA NEPRIGOŠENIH OSCILACIJA}$$

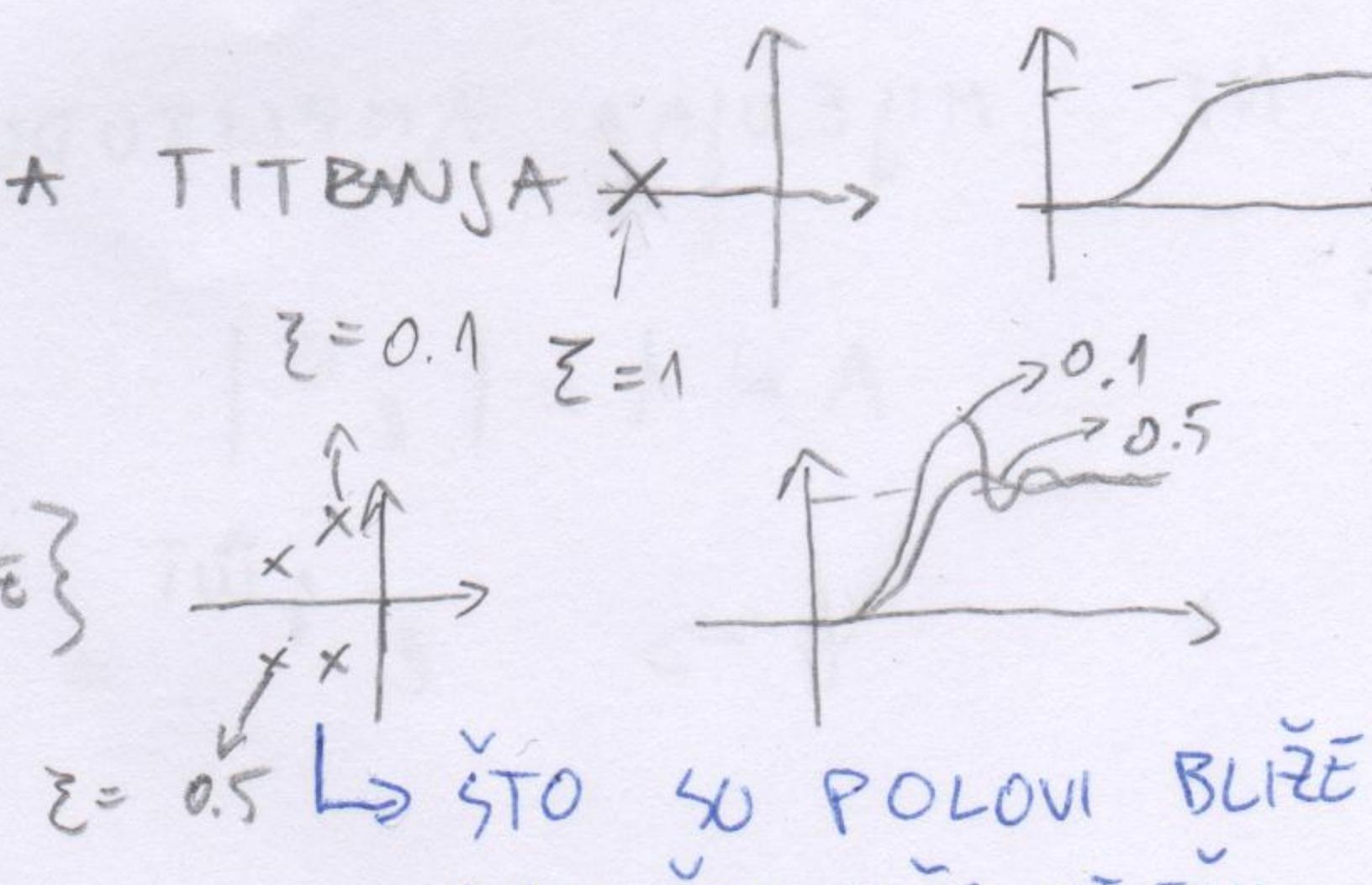
$\zeta \rightarrow$ KOEFICIJENT PRIGOŠENJA

\hookrightarrow VELIKA VAŽNOST IZ BORA PARAMETARA

ODZIV NA $\mu(t)$ U OVISNOSTI O ζ

$$\zeta = 1 \Rightarrow \text{DUOSTRUKI POL} \quad G(j) = \frac{K}{\left(\frac{j}{\omega_n} + 1\right)^2} \Rightarrow \text{NEMA TITRANJA}$$


$0 < \zeta < 1 \Rightarrow$ IMAMO TITRANJE $\{ \text{MANJI } \zeta \text{ VEĆE TITRANJE} \}$



$\zeta = 0 \rightarrow$ JEDNOSTRUKI POLOVI U ISMODISTU \rightarrow POB STABILNOSTI

$\zeta < 0 \rightarrow$ NESTABILNOST

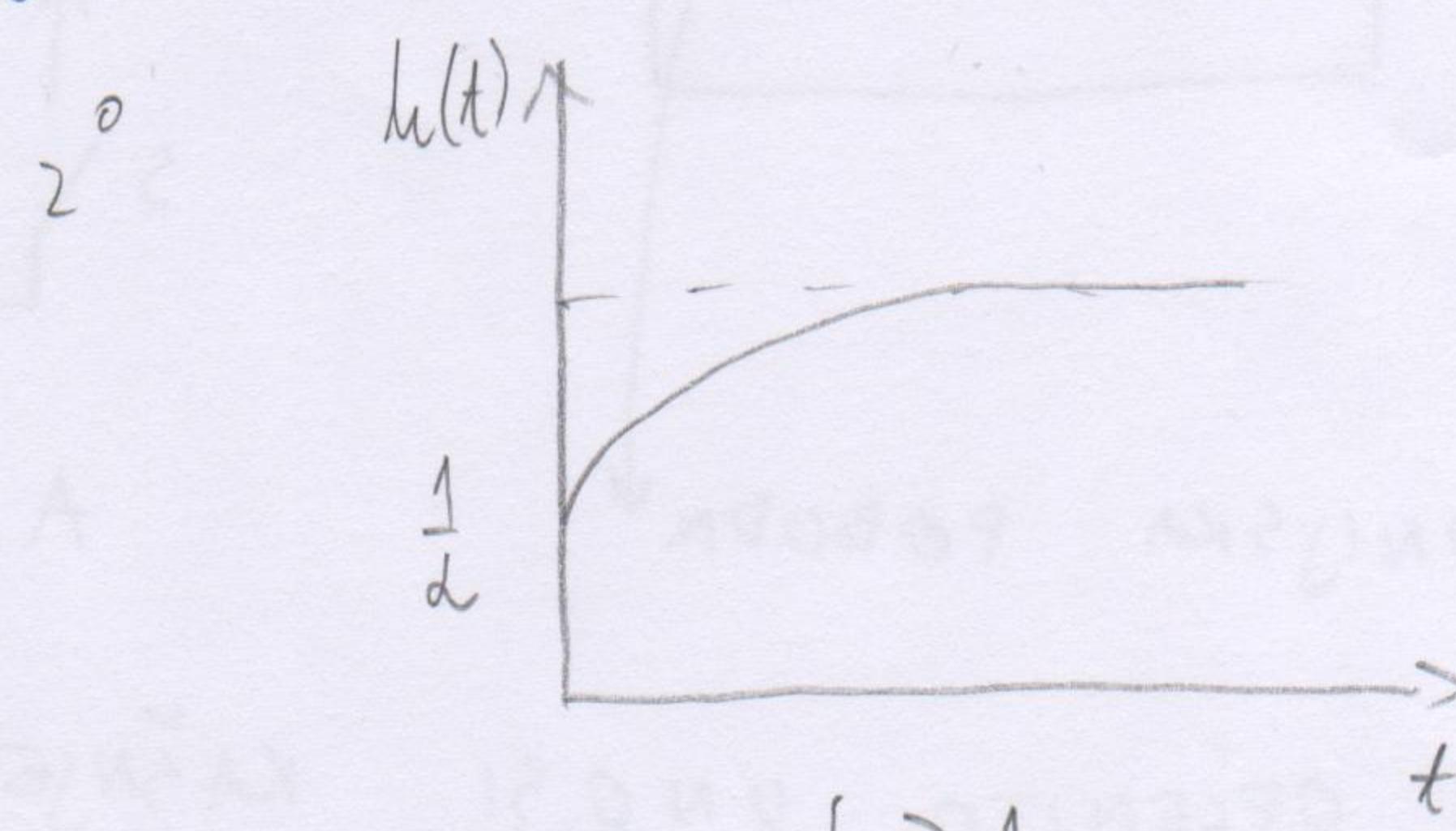
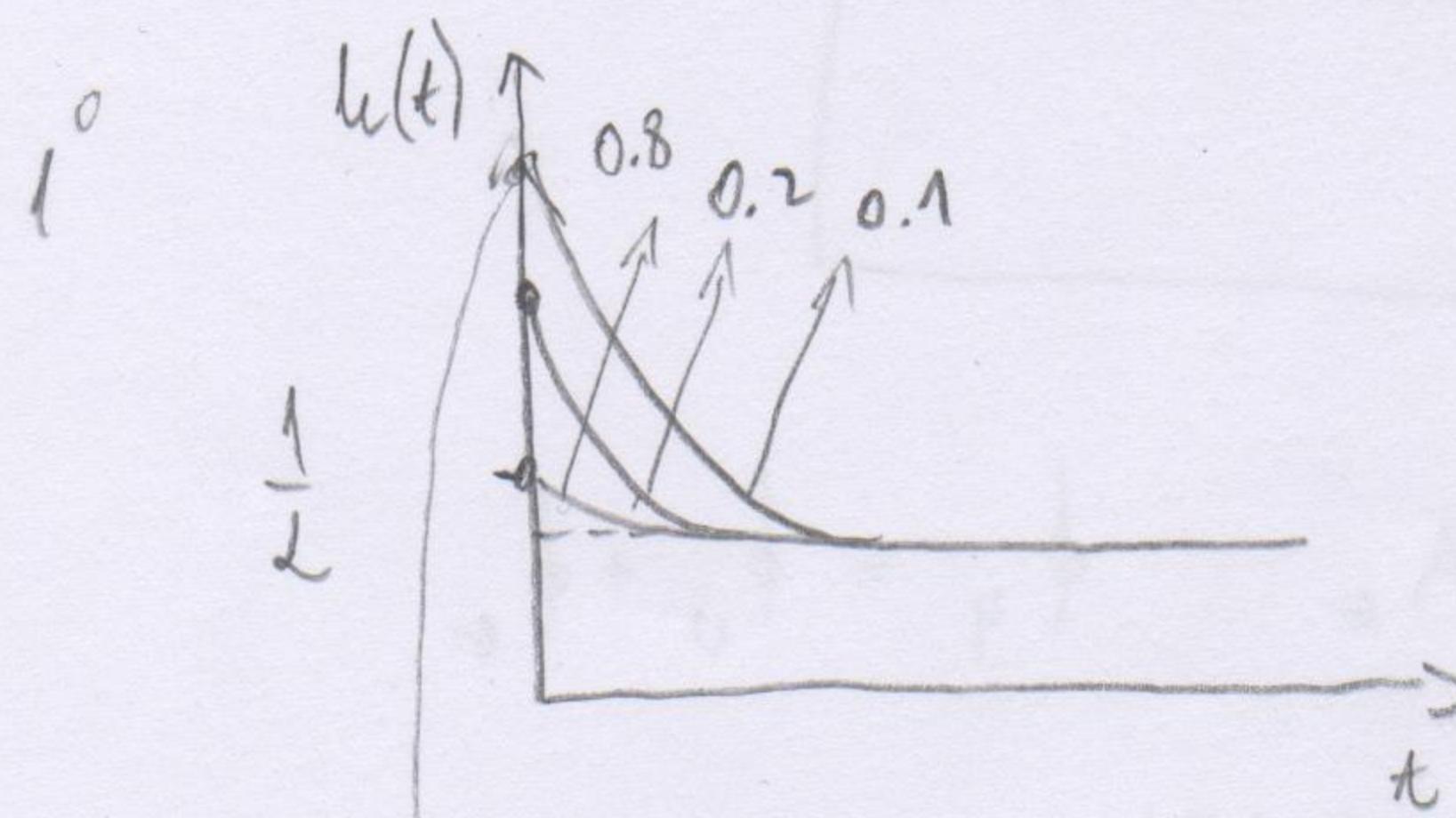


$\zeta < 0 \rightarrow$ NESTABILNOST

(13)

UTJECAJ POLOVA NA ODZIV

$$\text{PRIMJER: } G(\zeta) = \frac{1+\zeta}{1+2\zeta} \quad h(t) = 1 + \left(\frac{1}{2} - 1\right) e^{-\frac{t}{2}}$$

 $\zeta \rightarrow \text{PARAMETAR ZA PREMJEŠTANJE POLE U S RAVNNI}$ 

$$\zeta \in [0, 1]$$

\hookrightarrow ŠTO JE ζ BLIŽE NULI IMAMO VEĆI "SPIC"

\hookrightarrow POTENCIJALNA NESTABILNOST

POUKA: SMANJUJUĆI ζ UDALJAVAMO POLOVE OD ISHODIŠTA \hookrightarrow ŽNAČI DA SMANJUJEMO NJIHOVU "DOMINANTNOST" $\left\{ \begin{array}{l} \text{SUSTAV POSTAJE} \\ \text{STABILNIJI} \end{array} \right\}$

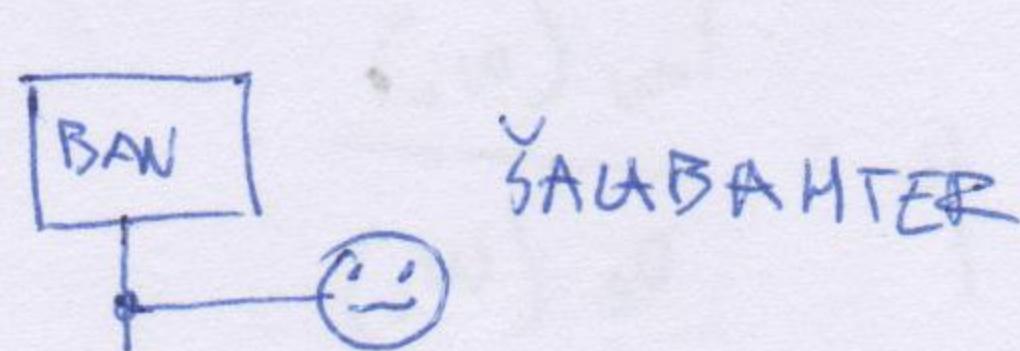
VIZUALIZACIJA \rightarrow PREVELIKI POČETNI MOMENT $\left\{ \begin{array}{l} \text{KIDAMO OSOVINU} \\ \text{PREVODIMO U VREMENSKI} \end{array} \right\}$

~~XXX~~ PRIMJER: $G(\zeta) = \frac{2}{(\zeta+1)(\zeta+2)} \Rightarrow h(t) = 1 - 2e^{-t} + e^{-2t} \quad t \geq 0$

$$\sigma_{P_1} = -1 \quad \sigma_{P_2} = -2$$

\hookrightarrow RASPORED NULA DIREKTNO UTJEĆE NA TRAJANJE "PRIJEZAZA" PRIJELAZNE FJE \hookrightarrow ŠTO SU BLIŽE ISHODIŠTU NADVIŠENJE JE VEĆE

DOLAZIMO DO DINAMIČKIH POKAZATELJA KVALITETE

\hookrightarrow VRIJEME ZA 

LABOS 3

1. ZADATAK

CRTANJE BODEOVOG DIJAGRAMA I USPOREDBA NYQUIST

ODZIV NA MARMONIJSKO POKLONJU

$$G(\zeta) = \frac{a\zeta + 1}{(\zeta + 1)(\zeta + 2)}$$

2. ZADATAK

UTJECAJ NULA NA ODZIV
 \hookrightarrow VEĆI $a \rightarrow$ NULA BLIŽE ISHODIŠTU \rightarrow VEĆI ŠILJAK (NADVIŠENJE)

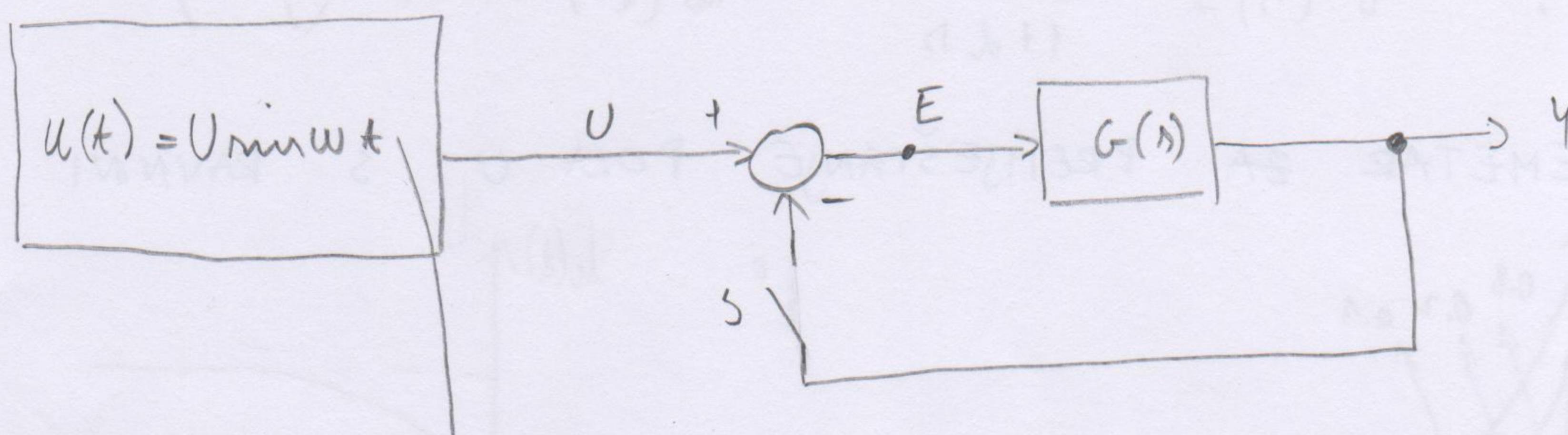
$$a < 1 \rightarrow \text{PODRAGAJ}$$

3. ZADATAK

PTZ ČLAN OVISNO O ZADANIM OGRAĐENJIMA \downarrow SLUŽBENI SAUBAHTER

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FIZIKALNO OBJAŠNJE PARMETARA STABILNOSTI



HARMONIJSKA POBODA

$$A_y = A_u \cdot A_g \quad \phi_y = \phi_u + \phi_g$$

SUSTAV OPĆENITO UNOSI KAŠNJEЊE U FAZI

AKO JE FAZA ODZIVA $\xrightarrow{\omega_{\pi}} -180^\circ \Rightarrow Y = A_y \underbrace{L 180^\circ}_{E = U - Y}$

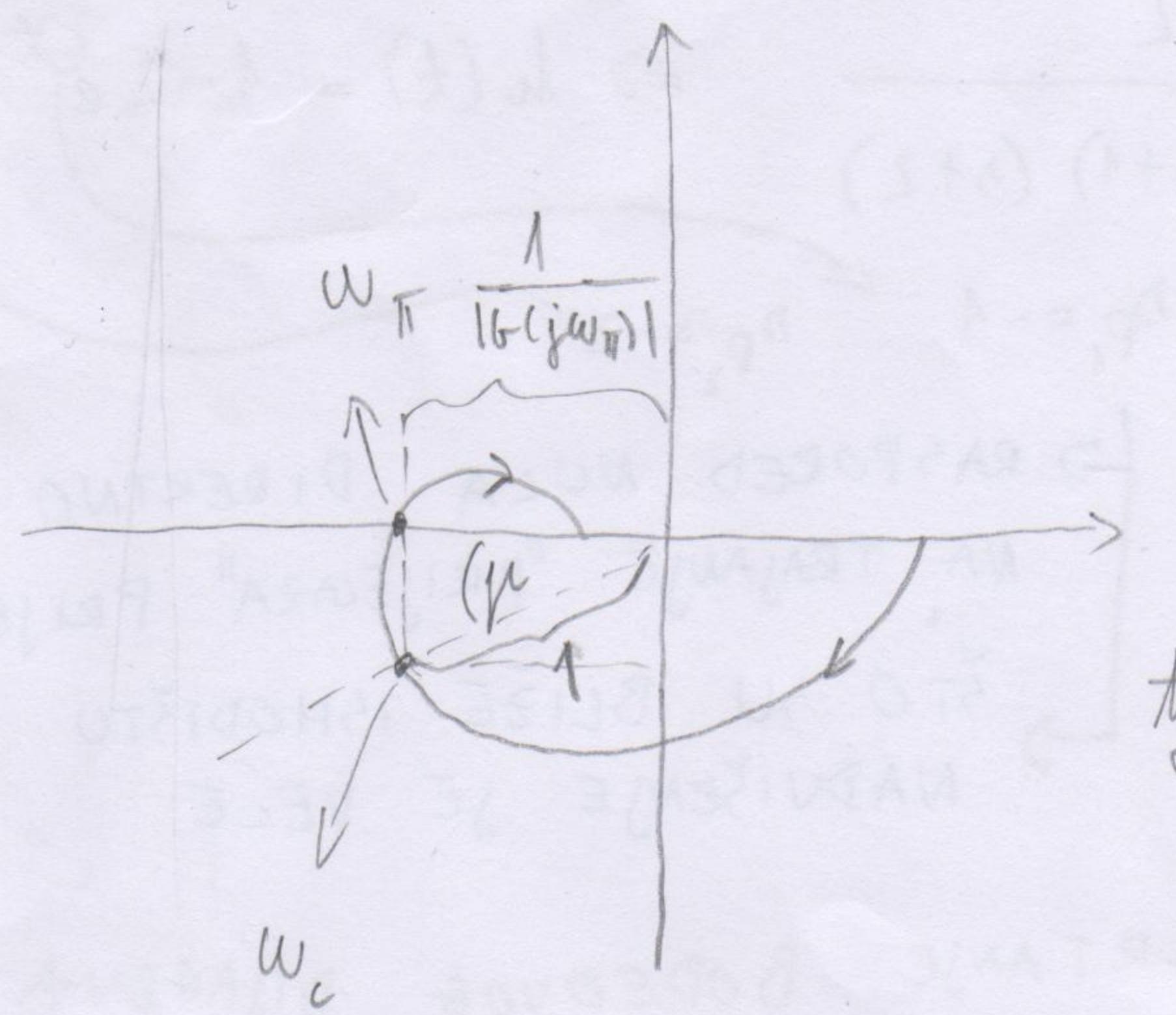
AKO JE $A_y < 1 \Rightarrow$ NEMA PROBLEMA $U = A_u \underbrace{L \varphi}_{E = A_u(\varphi) + A_y}$

ODZIV ĆE SE USTALITI NA NEKOJ VEJEDNOSTI $A_y = 1 \Rightarrow$ RUB STABILNOSTI

$A_y > 1 \Rightarrow$ NESTABILNOST $w_c \Rightarrow$ POSAČANJE = 1

15

FAZNO I AMPLITUDNO OSIGURANJE



$$w_c < \omega_{\pi}$$

UVJET STABILNOSTI

$$\text{tg } \mu = \frac{\text{Im}(w_c)}{\text{Re}(w_c)}$$

BODE \Rightarrow UTJECAJ MRTVOG VREMENA, POJAČANJA NA FAZNO

I AMPLITUDNO OSIGURANJE \Rightarrow ŠALABAHTER

UZMI GRAF

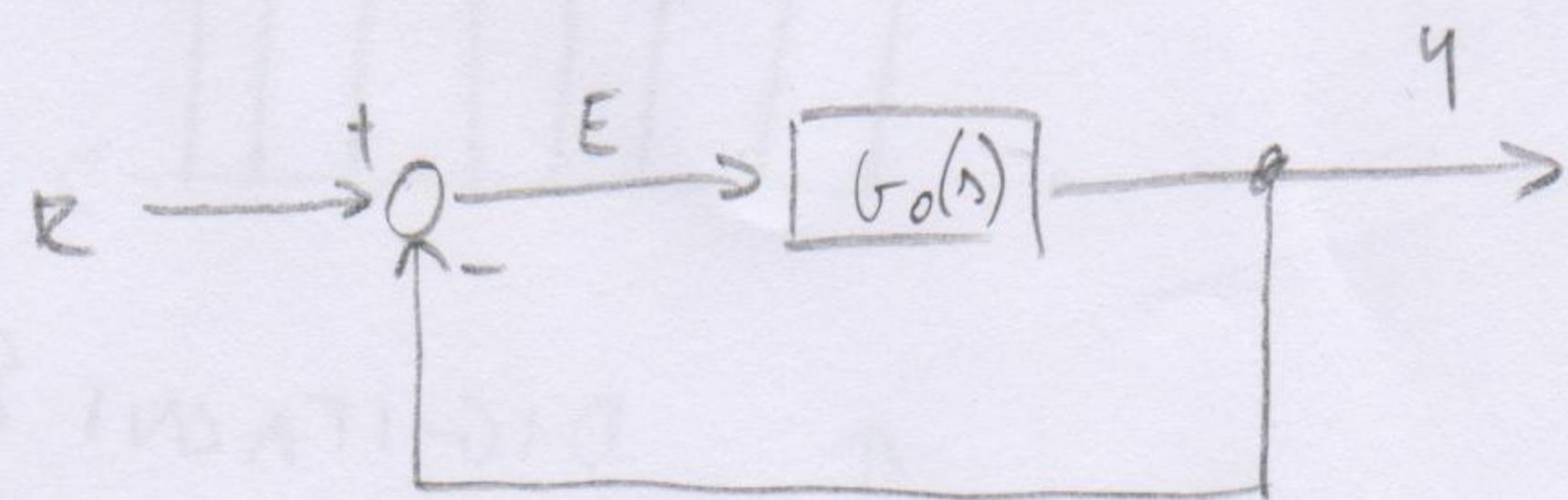
16 REGULACIJSKO ODSTUPANJE { CILJ POSTIĆI ŠTO MANJE ODSTUPANJE }

↪ LAGANO SE RAČUNA POMOĆU TEOREMA KONACNE
POČETNE VRIJEĐNOSTI

→ OVISI O REFERENCI I TIPO SUSTAVA { PRIJENOSNOJ FUNKCIJI }

→ OVISI O MJESTU DJELOVANJA REFERENCE

→ ASTATIZAM



$$G_o(s) = \frac{1}{s^k N(s)}$$

$$R = \frac{1}{s^d} \left\{ \begin{array}{l} \text{STEP } L=1 \\ \text{RAMPA } L=2 \\ \text{PARABOLA } L=3 \end{array} \right.$$

$$E = R - Y \quad Y = E \cdot G_o \quad \bar{E} = \frac{R}{1 + G_o(s)}$$

$$E = \frac{\frac{1}{s^d}}{\frac{s^k N(s) + 1}{s^k N(s)}} = \frac{s^k N(s)}{s^d (s^k N(s) + 1)}$$

$$\ell(0) = \lim_{n \rightarrow \infty} \bar{E}(n)$$

$$\ell(0) = \lim_{n \rightarrow \infty} \frac{s^{k+1}}{s^d} \frac{N(n)}{s^k N(n) + 1}$$

$k=0 \Rightarrow$ NEMA ASTATIZAM

$k=1 \Rightarrow$ ASTATIZAM 1. REDA

POUKA: MIJENJAJUĆI REFERENCI UTJEĆEMO NA REGULACIJSKO ODSTUPANJE

LABOS 4

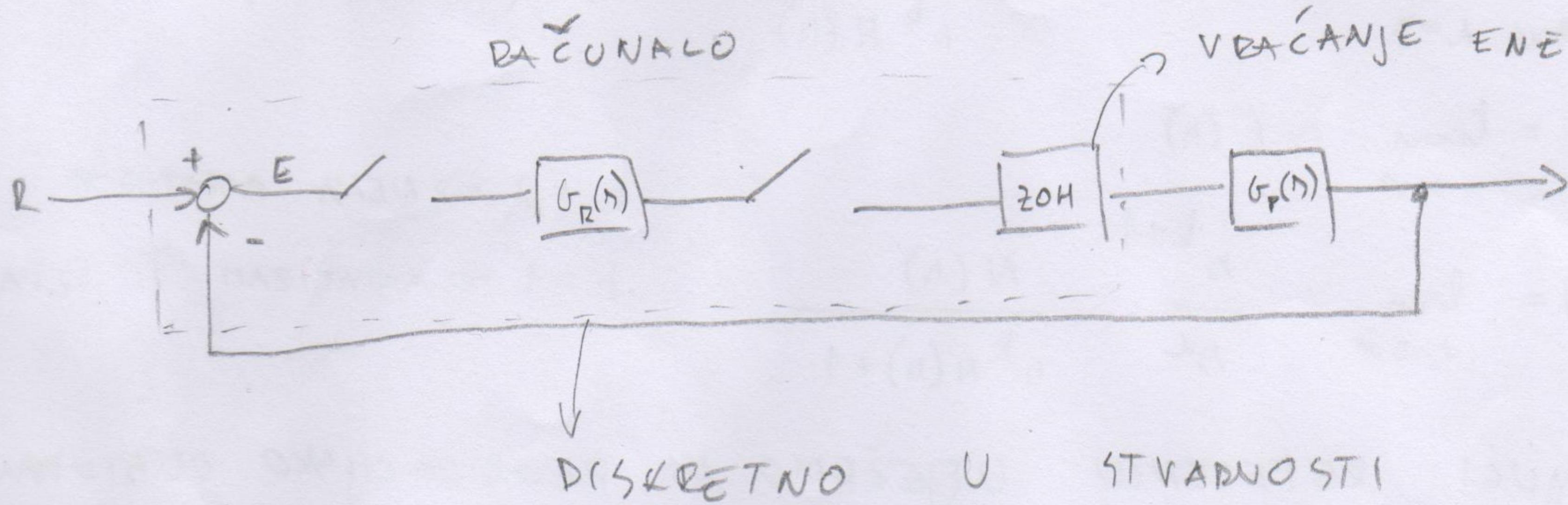
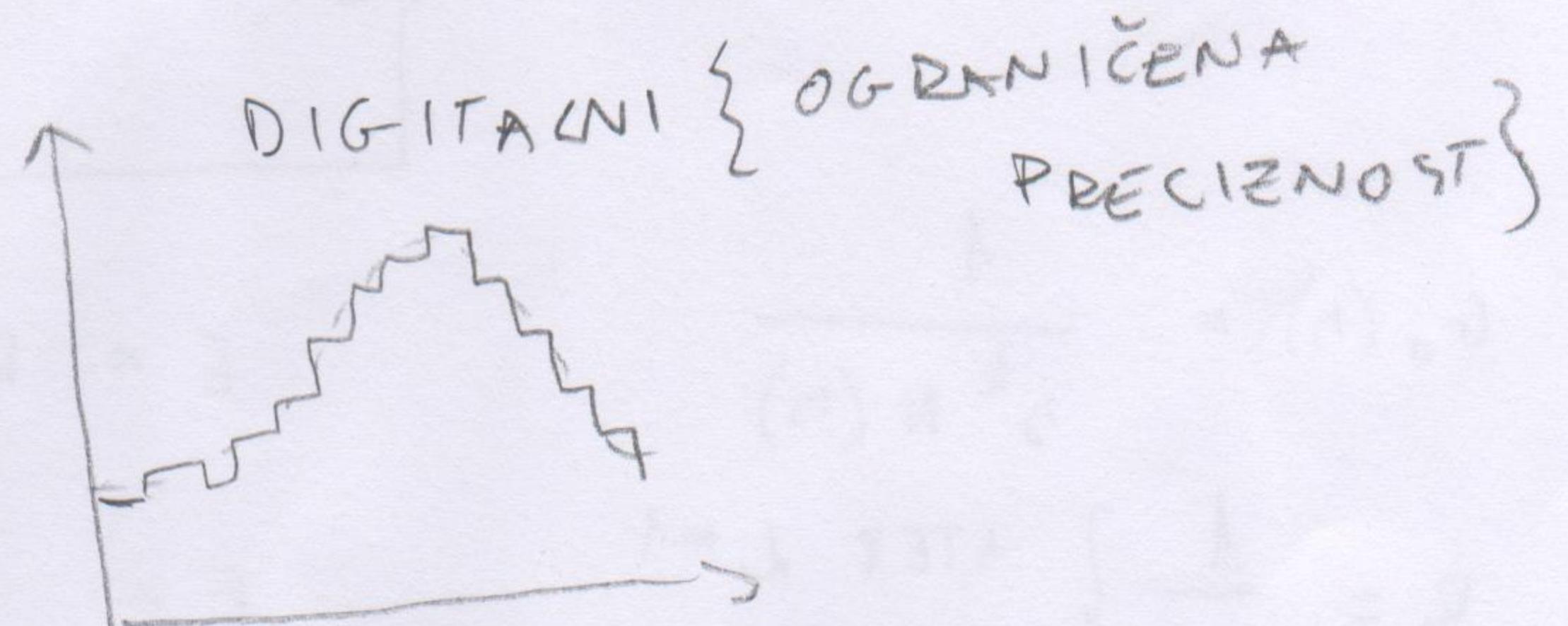
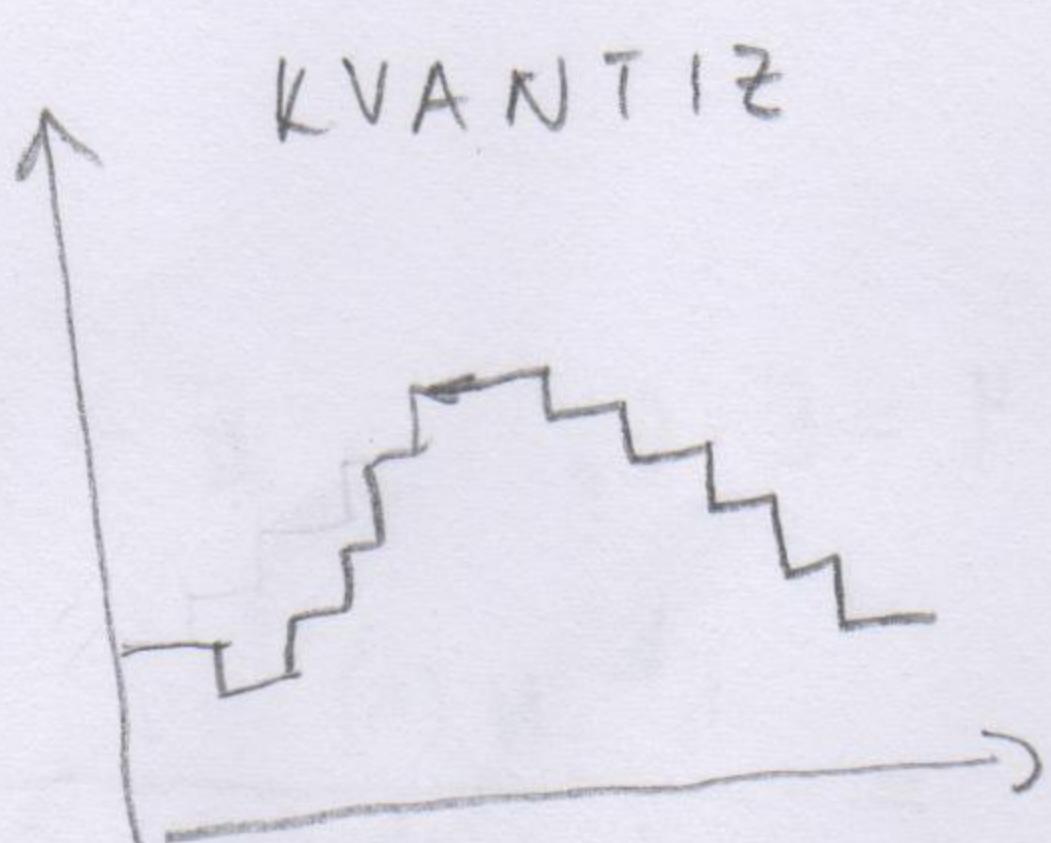
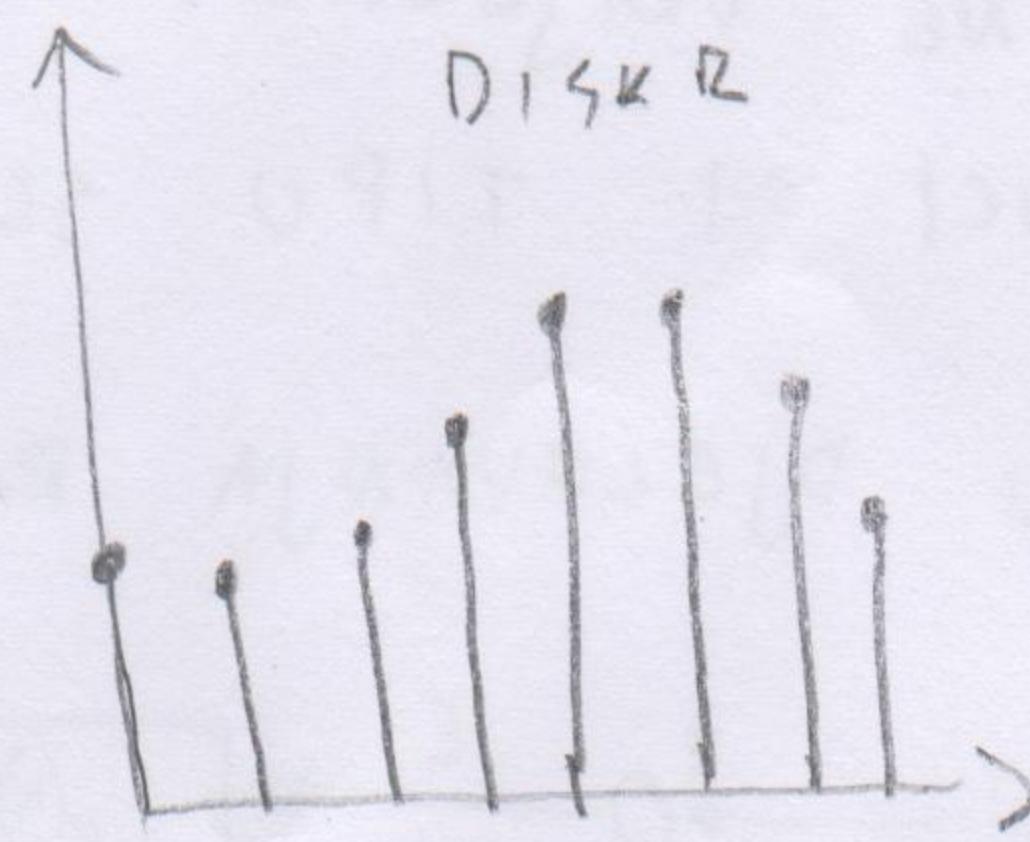
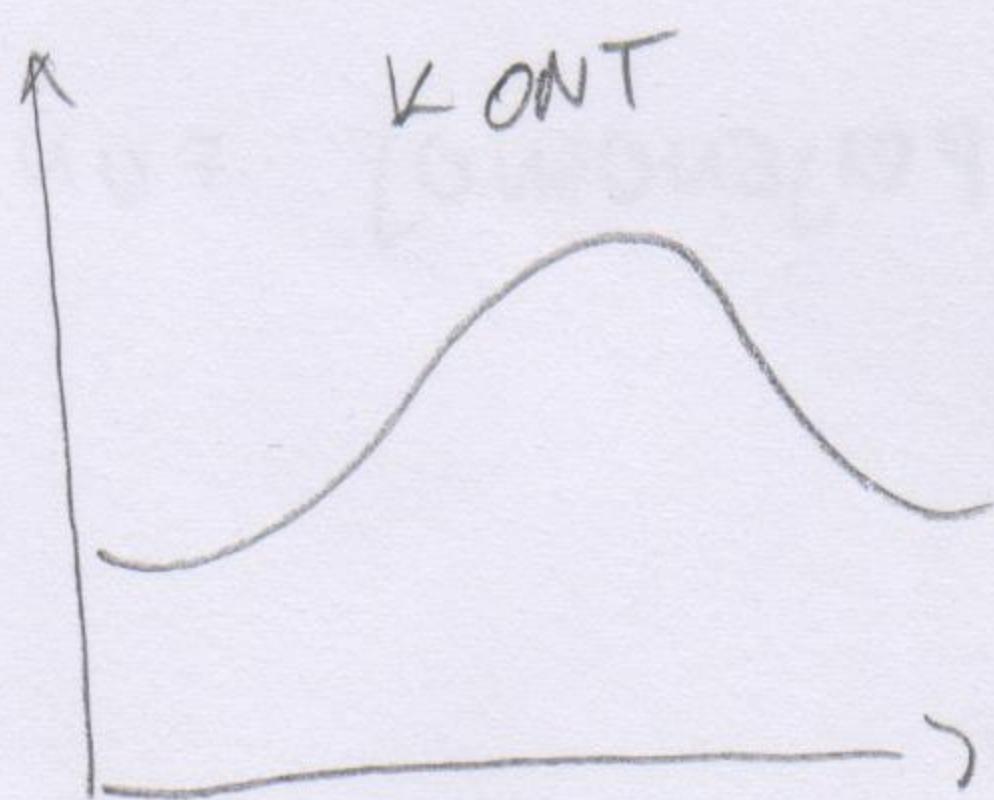
1. ZADATAK \rightarrow MURWITZ

\rightarrow REGULACIJSKO ODSTUPANJE OVISNO O POBUDI
{ ASTATIZAM }

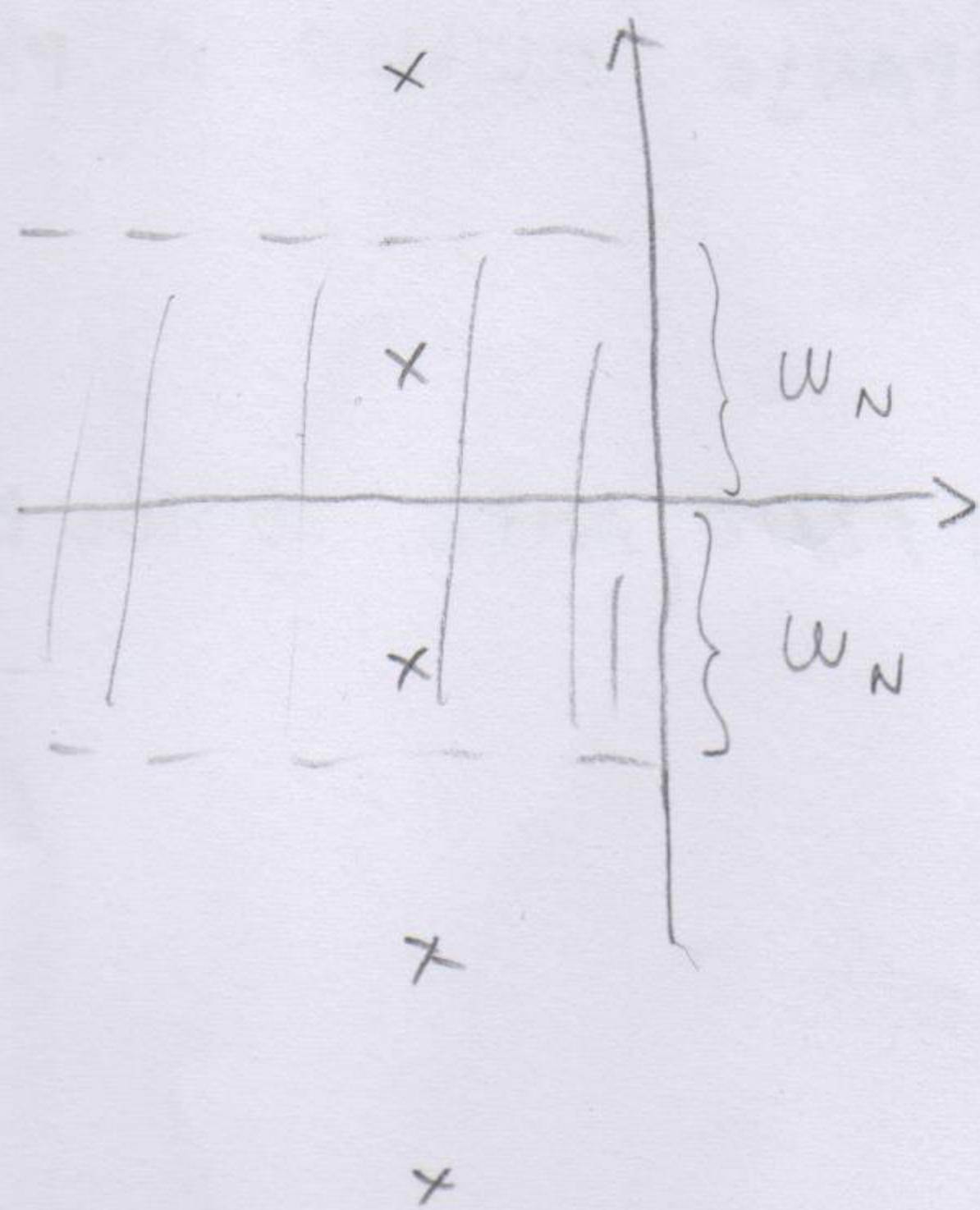
2. ZADATAK \rightarrow BODE, NYQUIST \rightarrow FAZNO, AMPL. OSIGURANJE

DIGITALNA ERA

⑦ DISKRETNO PODRUČJE { ZAŠTO ? }



ČITAVANJE



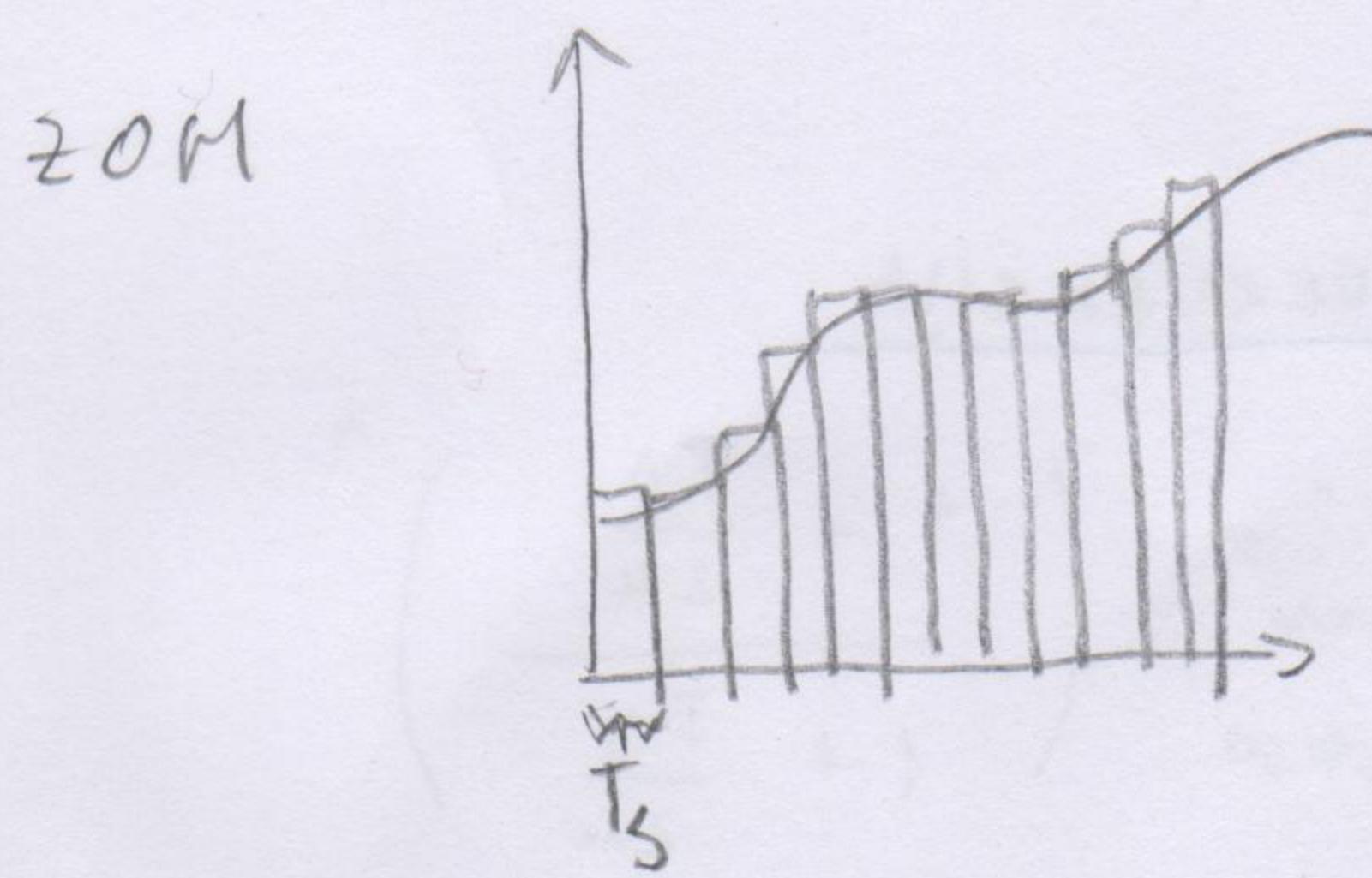
$$e^{j\omega_N T_s} = e^{j(\omega_N T_s + 2k\pi)}$$

$\omega_N = \frac{\pi}{T_s}$

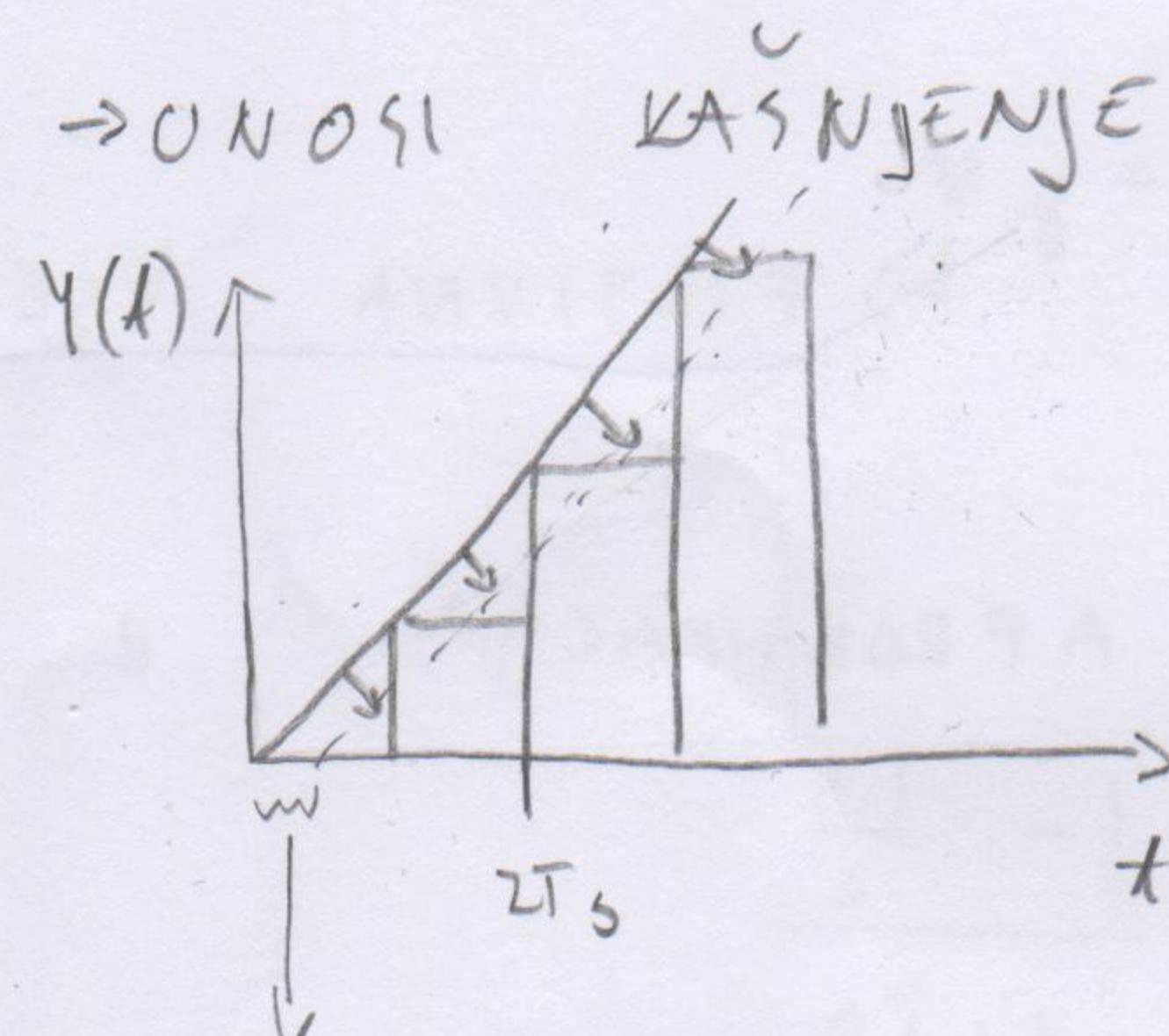
ALIASING
 $\omega_s > 2\omega_{\text{Najveće}}$

(18) METODE UZORKOVANJA

- IDEALNI IMPULSNI ELEMENT $\left\{ \text{Kronekerov niz} \right\}$ DOBIJEMO \Rightarrow ČUVA TEŽINSKU FUNKCIJU
- ZOH, FOH \rightarrow REKONSTRUKTORI $\left\{ \text{D/A} \right\}$ $ZOH = (1 - z^{-1}) \sum \left\{ \frac{G(n)}{n} \right\}$



$$\left\{ \frac{1}{s} - \frac{1}{s} e^{-nT_s} \right\} \text{ STEPOMI}$$



$$\frac{T_s}{2} \Rightarrow \text{NADOMJESNO MRTVO VRIJEME}$$

$e^{-n \frac{T_s}{2}}$
SPUŠTA FAZU $\omega_c \frac{T_s}{2}$ I POVEĆAVA NADVIŠENJE

IZVOD PREPORUČENOG VREMENATIČKOG OČITAVANJA

$$\rightarrow \text{ŽELIMO DA SE } \mu \text{ SMANJI}^{\text{MAX}} \quad \mu [^\circ] = 70 - \sigma_m [\%]$$

$$\Delta \mu [^\circ] = \omega_c \frac{T_s}{2} \cdot \frac{180}{\pi}$$

$$(5^\circ \text{ DO } 10^\circ) = \frac{180}{\pi} \omega_c \frac{T_s}{2}$$

19. PRESLIKAVANJE NULA I POLOVA

$$z = e^{-j\omega T} \Rightarrow \text{BAN ŽALABAHTER}$$

$$T_s = (0.17 \text{ DO } 0.34) \frac{1}{\omega_c}$$

20. POSTUPCI DISKRETIZACIJE

- 1^o ZADRŽAVANJE TIŽINSKE FJE $\rightarrow z$
- 2^o ZADRŽAVANJE PROJELAZNE FJE $\rightarrow ZOH$

3^o USKLADENE NULE I POLOVI

$$G(z) = \frac{(n+1)^m B(n)}{(n+2)^m N(n)} \quad n-m > 1 \rightarrow \text{NAPRAVIMO } z \text{ TRANSFORMACIJU}$$

DODAJEMO $n-m-1$ NULA U $z=-1$

\rightarrow MODIFIKIRANA BILINEARNA

4^o OČUVANJE PRESJEČNE FREKVENCIJE (TUSTIN)