Tail calls

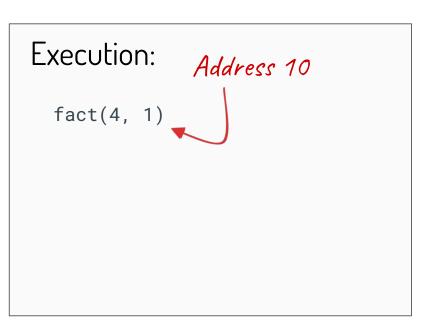
```
function fact(n, acc) {
   if (n == 0) {
      return acc
   }
   return fact(n - 1, n * acc)
}
```

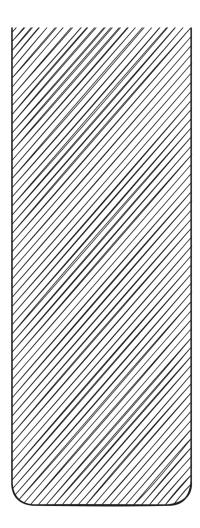
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function fact(n, acc) {
    if (n == 0) {
        return acc
    }
    return fact(n - 1, n * acc)
}
```

```
function fact(n, acc) {
    if (n == 0) {
        return acc
    }
20:    return fact(n - 1, n * acc)
    }
```

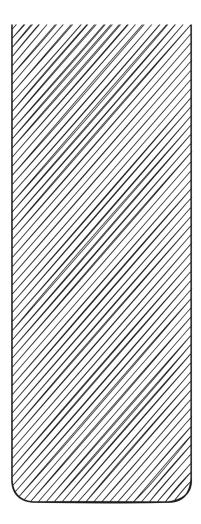
```
function fact(n, acc) {
    if (n == 0) {
        return acc
    }

20:    return fact(n - 1, n * acc)
    }
```

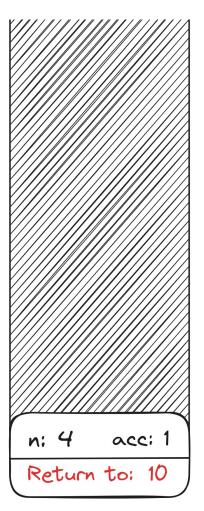


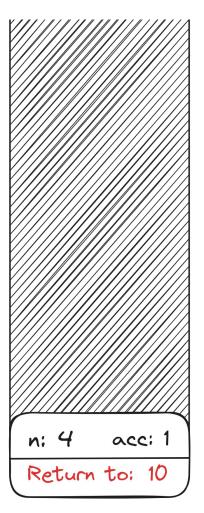


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function fact(n, acc) {
    if (n == 0) {
        return acc
    }
20:    return fact(n - 1, n * acc)
    }
```



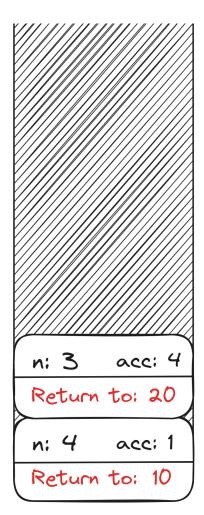
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function fact(n, acc) {
    if (n == 0) {
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    }
20:    return fact(n - 1, n * acc)
    }
```



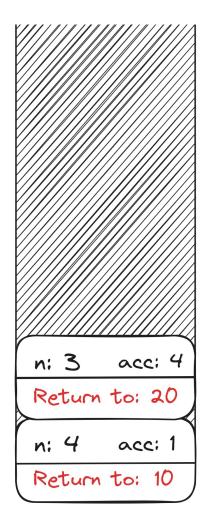


```
function fact(n, acc) {
    if (n == 0) {
        return acc
    }
20:    return fact(n - 1, n * acc)
    }
```

```
Execution:
10: fact(4, 1)
    → fact(3, 4)
```



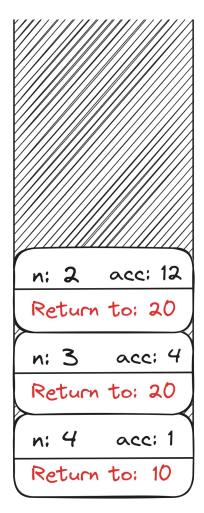
Execution: **10:** fact(4, 1) → fact(3, 4)



```
function fact(n, acc) {
      if (n == 0) {
          return acc
     return fact(n - 1, n * acc)
20:
   Execution:
  10: fact(4, 1)
      → fact(3, 4)
         9 fact(2, 12)
```

```
n: 2 acc: 12
Return to: 20
n: 3
       acc: 4
Return to: 20
n: 4
       acc: 1
Return to: 10
```

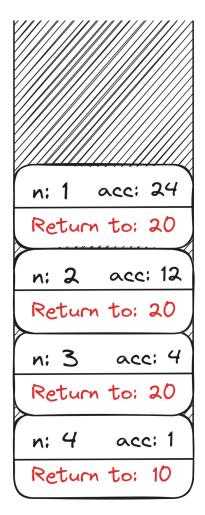
Execution: *10:* fact(4, 1) → fact(3, 4) → fact(2, 12)



```
function fact(n, acc) {
       if (n == 0) {
           return acc
20:
      return fact(n - 1, n * acc)
   Execution:
  10: fact(4, 1)
      \rightarrow fact(3, 4)
          → fact(2, 12)
             → fact(1, 24)
```

```
acc: 24
Return to: 20
       acc: 12
Return to: 20
       acc: 4
n: 3
Return to: 20
n: 4
       acc: 1
Return to: 10
```

Execution: *10:* fact(4, 1) \rightarrow fact(3, 4) → fact(2, 12) → fact(1, 24)



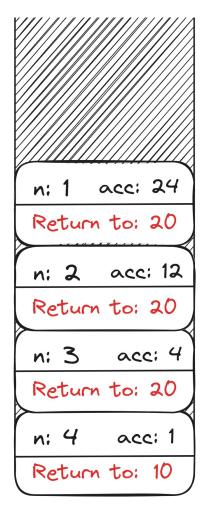
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function fact(n, acc) {
       if (n == 0) {
           return acc
20:
      return fact(n - 1, n * acc)
   Execution:
  10: fact(4, 1)
       \rightarrow fact(3, 4)
          → fact(2, 12)
             → fact(1, 24)
                → fact(0, 24)
```

```
n: 0 acc: 24
Return to: 20
     acc: 24
Return to: 20
      acc: 12
Return to: 20
       acc: 4
n: 3
Return to: 20
n: 4
       acc: 1
Return to: 10
```

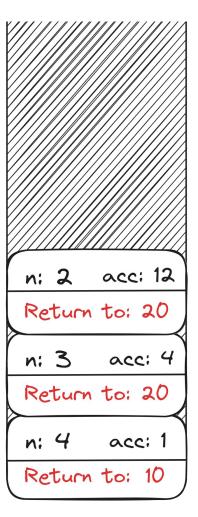
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function fact(n, acc) {
       if (n == 0) {
           return acc
20:
      return fact(n - 1, n * acc)
   Execution:
  10: fact(4, 1)
       \rightarrow fact(3, 4)
          → fact(2, 12)
              → fact(1, 24)
                 \Rightarrow fact(0, 24) = 24
```

```
n: 0 acc: 24
Return to: 20
     acc: 24
Return to: 20
      acc: 12
Return to: 20
       acc: 4
n: 3
Return to: 20
n: 4
       acc: 1
Return to: 10
```

```
function fact(n, acc) {
       if (n == 0) {
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   Execution:
  10: fact(4, 1)
       \rightarrow fact(3, 4)
          → fact(2, 12)
              \Rightarrow fact(1, 24) = 24
```



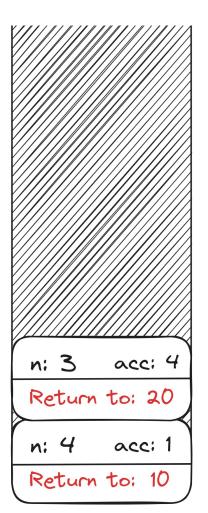
Execution: *10:* fact(4, 1) \rightarrow fact(3, 4) \Rightarrow fact(2, 12) = 24



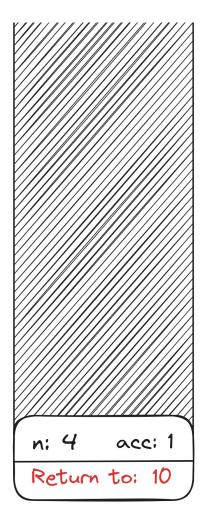
```
function fact(n, acc) {
     if (n == 0) {
         return acc
    return fact(n - 1, n * acc)
20:
```

10: fact(4, 1)

 \Rightarrow fact(3, 4) = 24

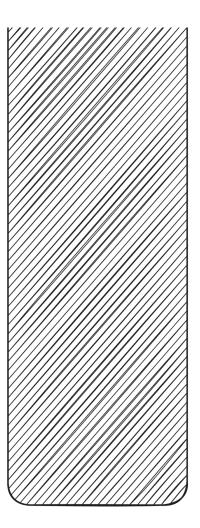


10: fact(4, 1) = 24



```
function fact(n, acc) {
    if (n == 0) {
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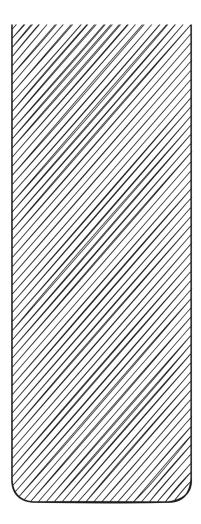
10: 24



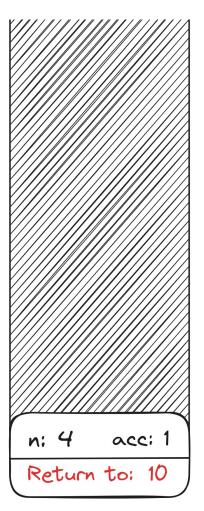
Questions

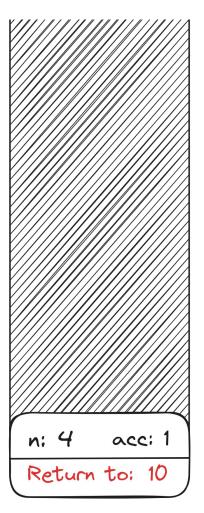
- Time?
- Space?
- Can we do better?

```
function fact(n, acc) {
    if (n == 0) {
        return acc
    }
20:    return fact(n - 1, n * acc)
    }
```



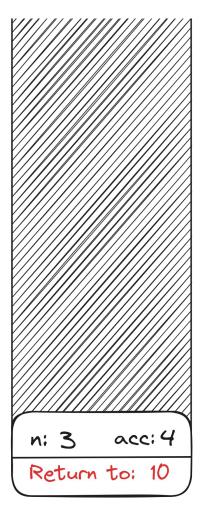
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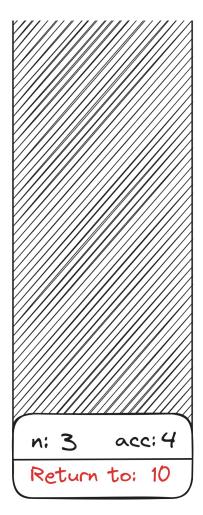


```
function fact(n, acc) {
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```

Execution: **10:** fact(4, 1) → fact(3, 4)

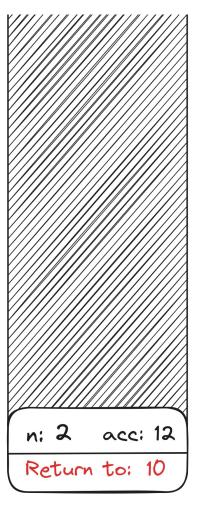


Execution: **10:** fact(4, 1) → fact(3, 4)

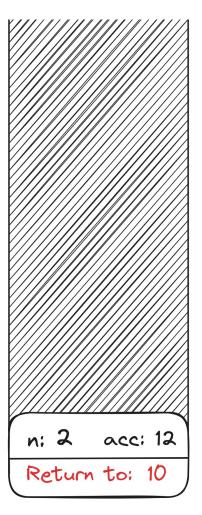


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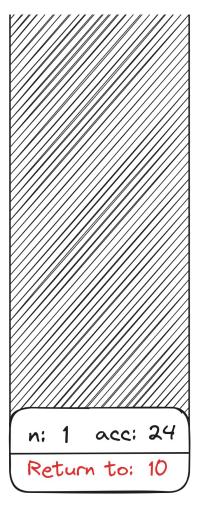
```
Execution:
10: fact(4, 1)
    → fact(3, 4)
       9 fact(2, 12)
```



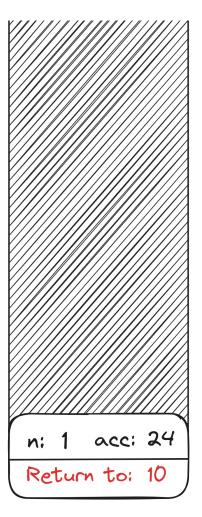
Execution: **10:** fact(4, 1) → fact(3, 4) 9 fact(2, 12)



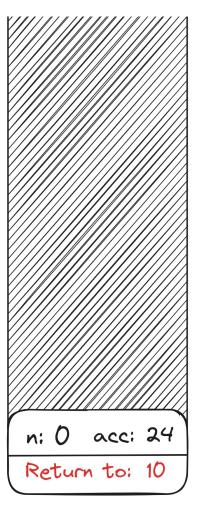
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         → fact(2, 12)
            → fact(1, 24)
```



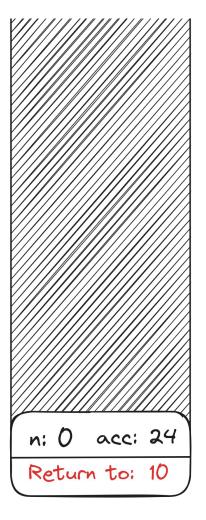
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    }
```

10: 24

