Learning Useful Representations of Recurrent Neural Network Weight Matrices

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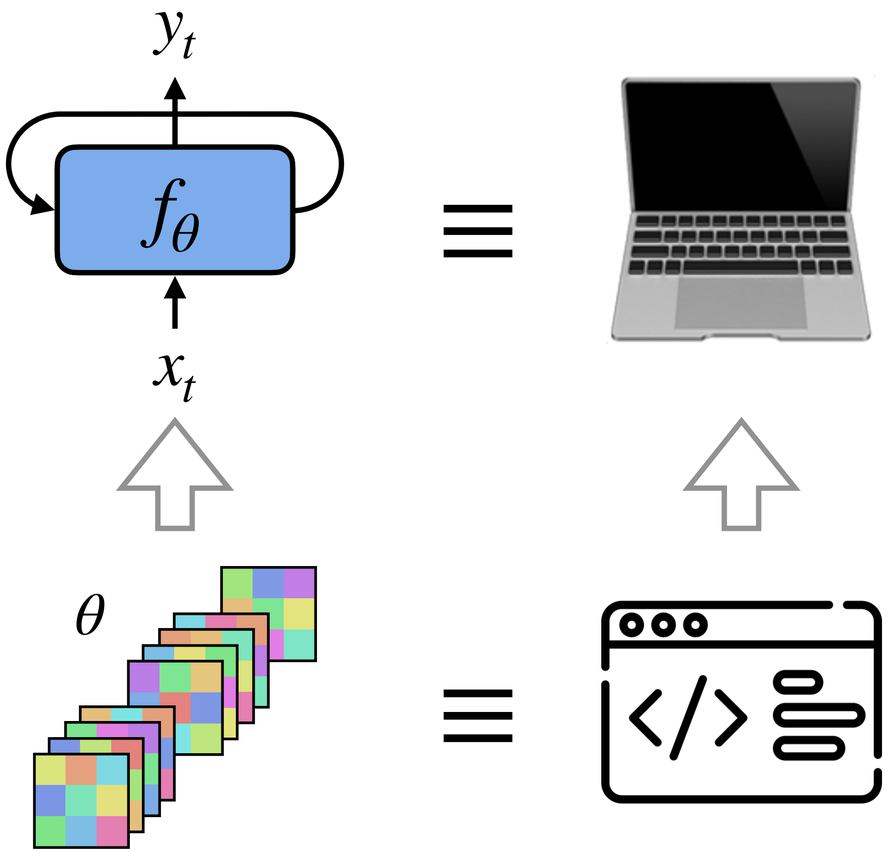
Learning RNN Weight Representations

- RNNs are universal computers
- Weight matrices are their program

Applications:

- Reinforcement Learning
- Implicit Neural Representations
- Interpretability
- …



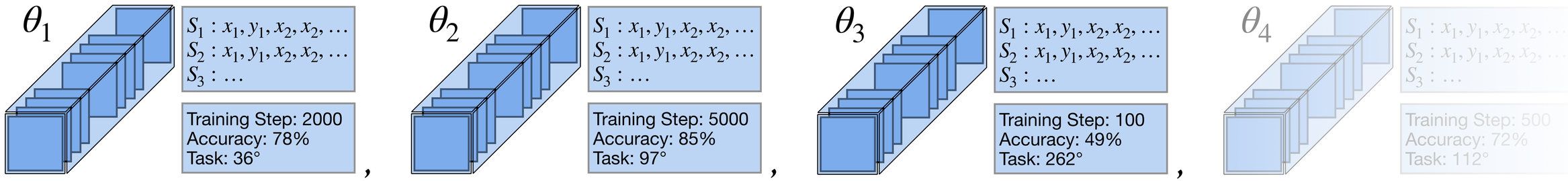
Three Ingredients

- **Datasets**
- **Learning / Pre-Training method**
- **RNN Weight encoder architecture**

Datasets

Two RNN ‘Model Zoos’

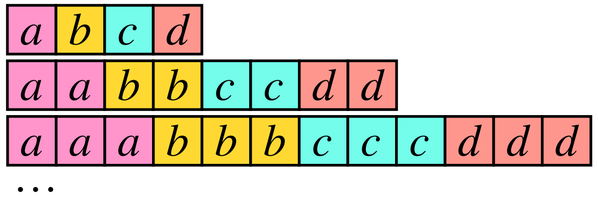
- 1000 LSTM training runs per dataset, 9 snapshots per run
- Each LSTM is trained on a different task from a task family
- Datapoint: LSTM weights, 100 rollouts/trajectories, metadata



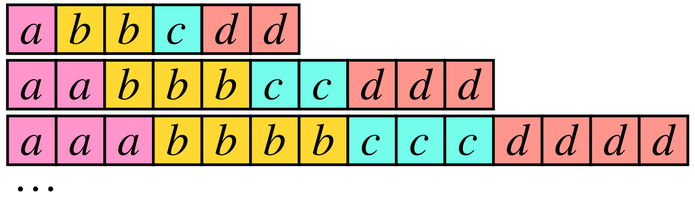
Formal Languages Dataset

- Autoregressive models of 216 different formal languages
- Language family: $L_{m_a,m_b,m_c,m_d} := \{a^{n+m_a}b^{n+m_b}c^{n+m_c}d^{n+m_d} \mid n \in \mathbb{N}\}$
- Examples

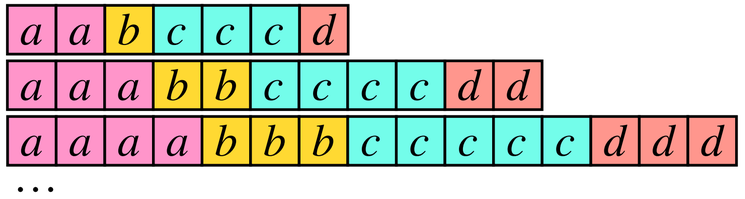
$L_{1,1,1,1}$:



$L_{1,2,1,2}$:



$L_{2,1,3,1}$:



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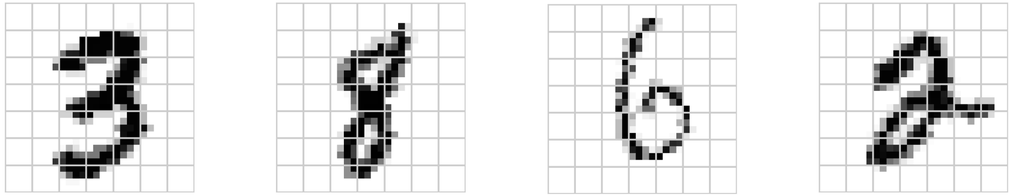
Tiled Sequential MNIST Dataset

- Classifiers of tiled sequentialised MNIST digits (prediction at every step)
- Every model is trained on a different rotation angle of the digits
- Examples

17° :



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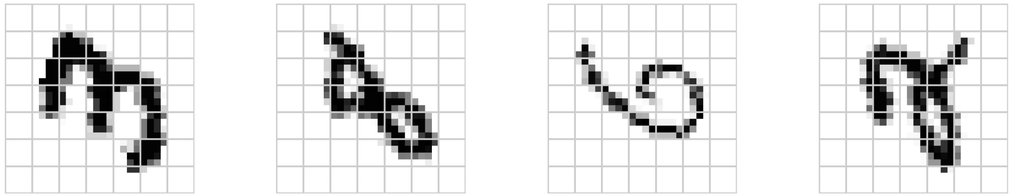
74° :



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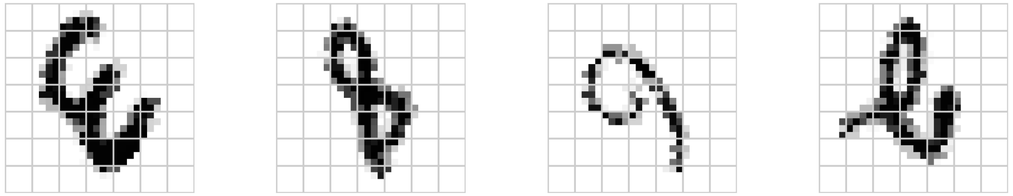
231° :



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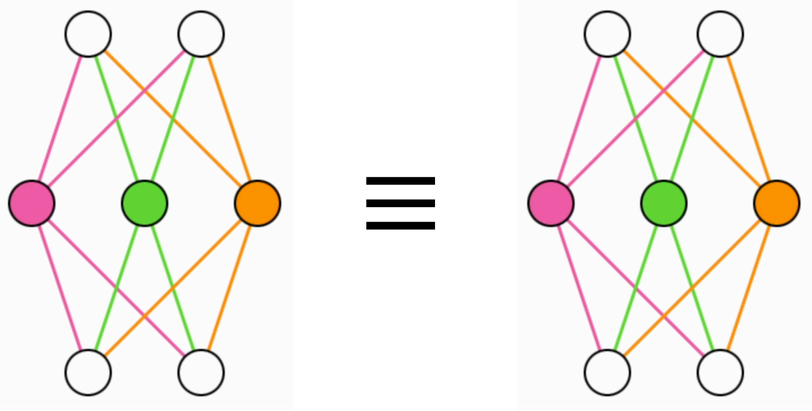
Weight Space Symmetries

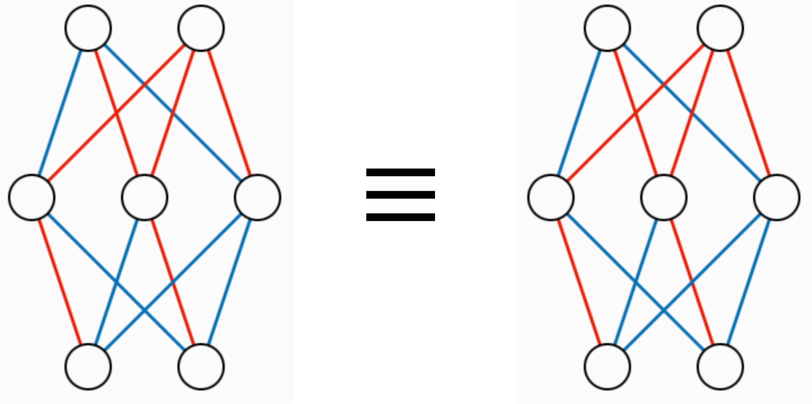
Challenge or Opportunity?

Huge number of equivalent networks

- Hidden Neuron Permutation

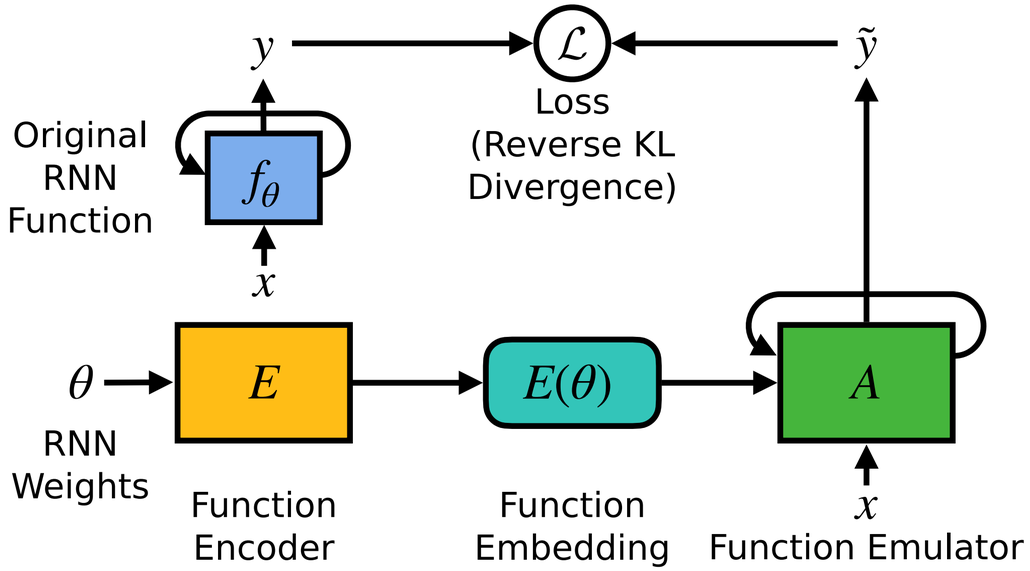


- Sign Flip / Scaling
  (depends on non-linearity)



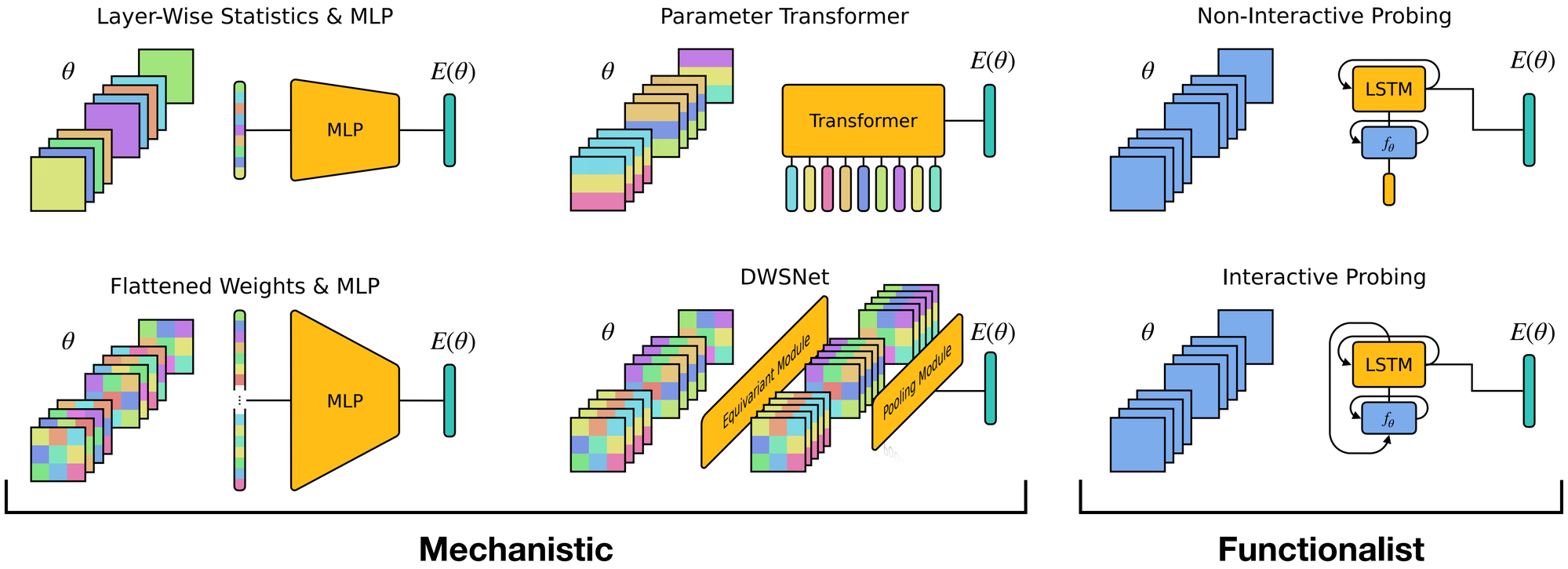
Self-Supervised Training Method

- Reconstruction or naive contrastive methods? 🚨*Weight Space Symmetries*🚨
- *Instead*: Emulate the functionality of the network!
- Encoder E generates representation $E(\theta)$ of RNN f_θ
- Emulator A is conditioned on $E(\theta)$ and imitates f_θ



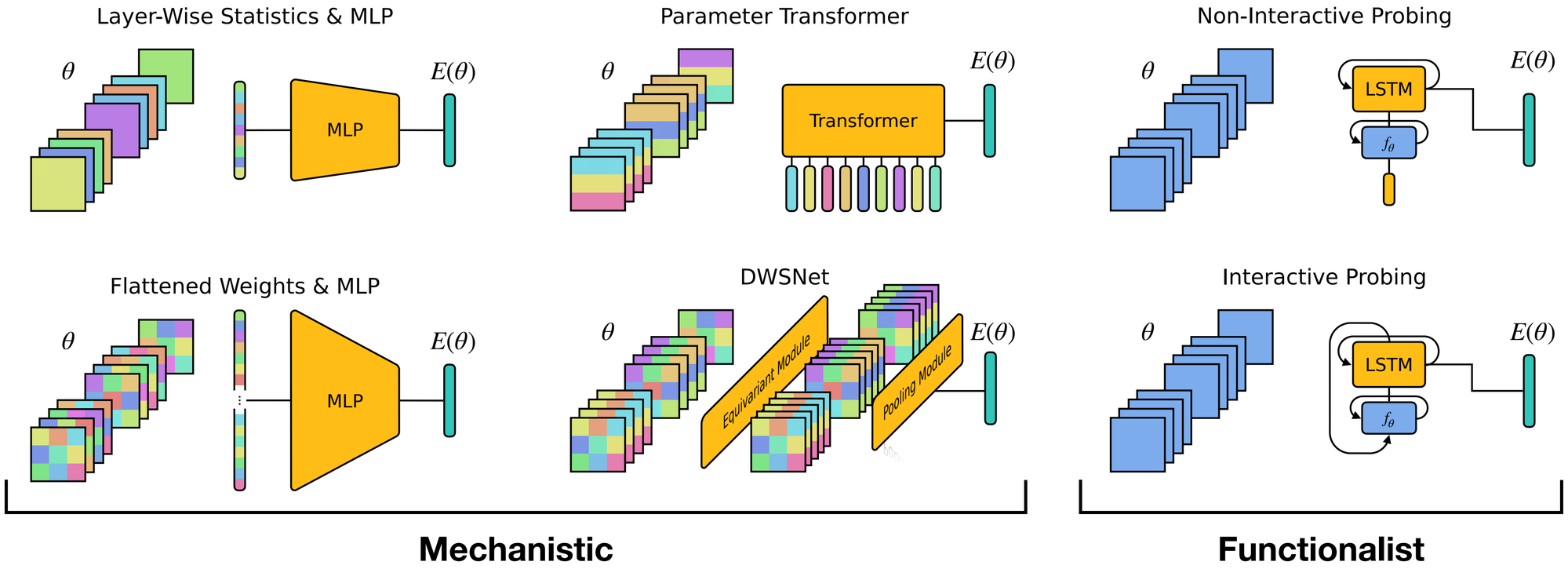
RNN Weight Encoder Architectures

- Distinction: Mechanistic Encoders & Functionalist Encoders
- **Mechanistic** encoders look at the weights θ directly
- **Functionalist** encoders look at the input-output mapping of f_θ



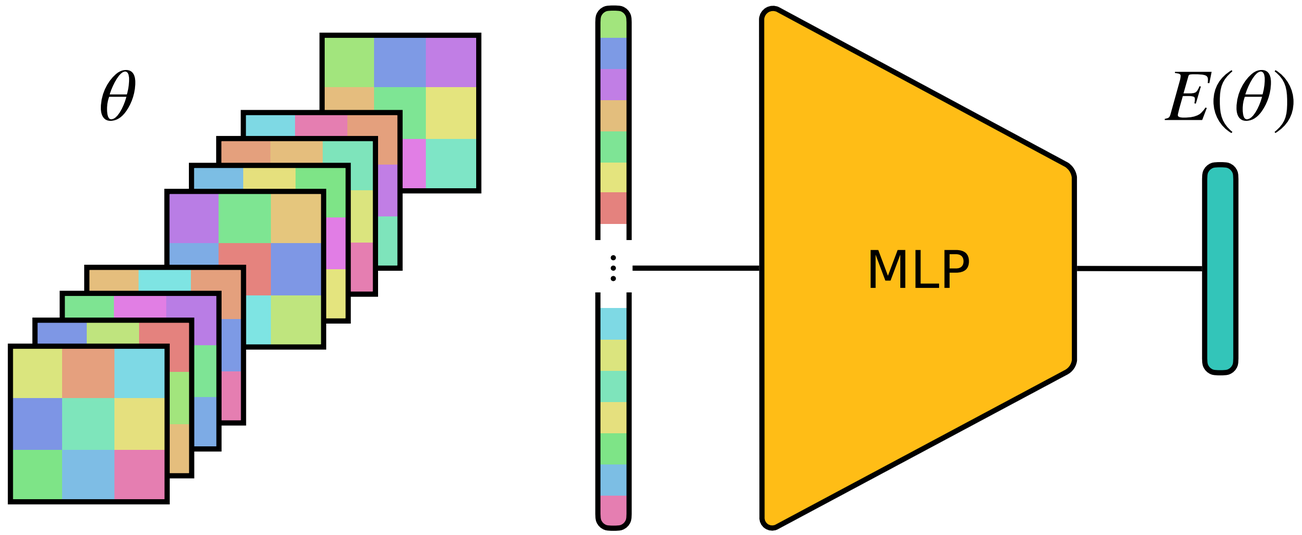
Layer-Wise Statistics & MLP (Mechanistic)

- Concatenate various global statistics of each weight matrix and feed into MLP
- Invariant to hidden neuron permutation 👍
- Not universal 👎



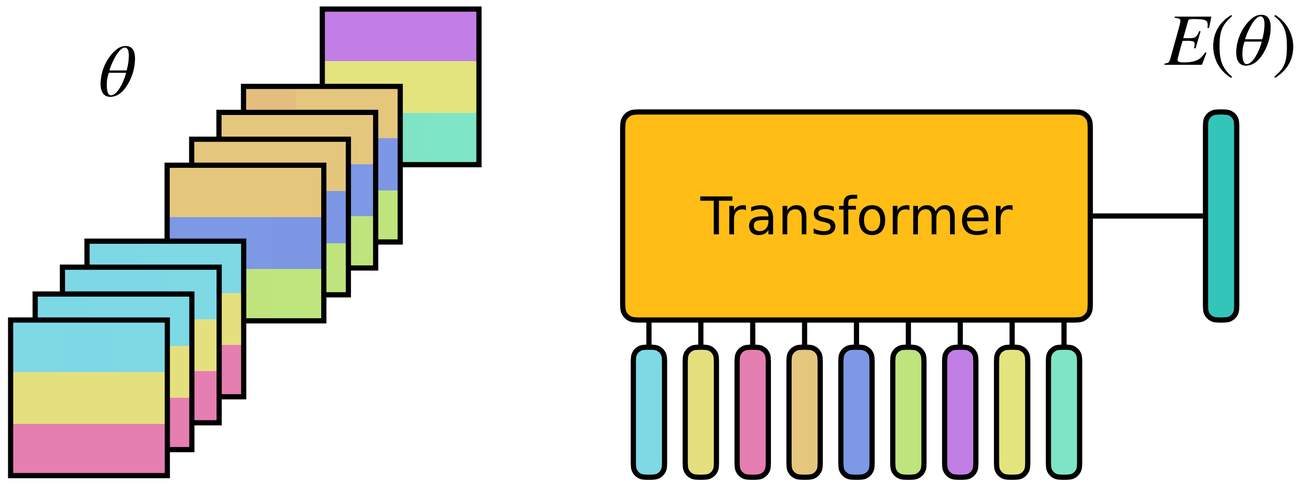
Flattened Weights & MLP (Mechanistic)

- Flatten all weights into one big vector and feed into MLP
- Not invariant to hidden neuron permutation 👎
- Universal 👍



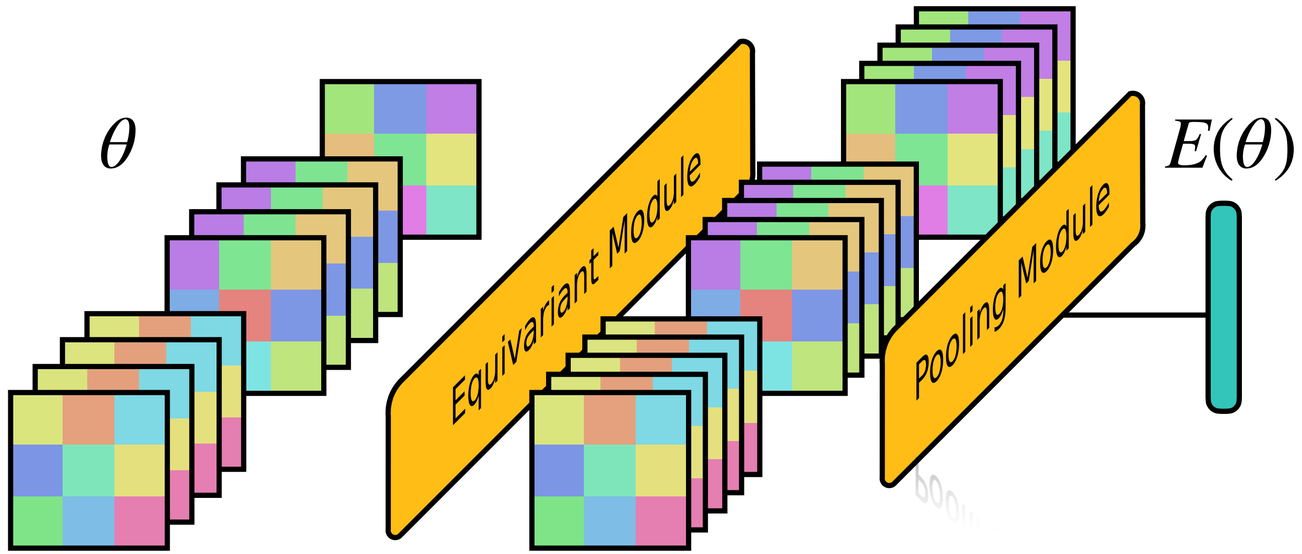
Parameter Transformer (Mechanistic)

- Feed neuron weight vectors as sequence to a transformer model
- Not invariant to hidden neuron permutation 👎
- Universal 👍



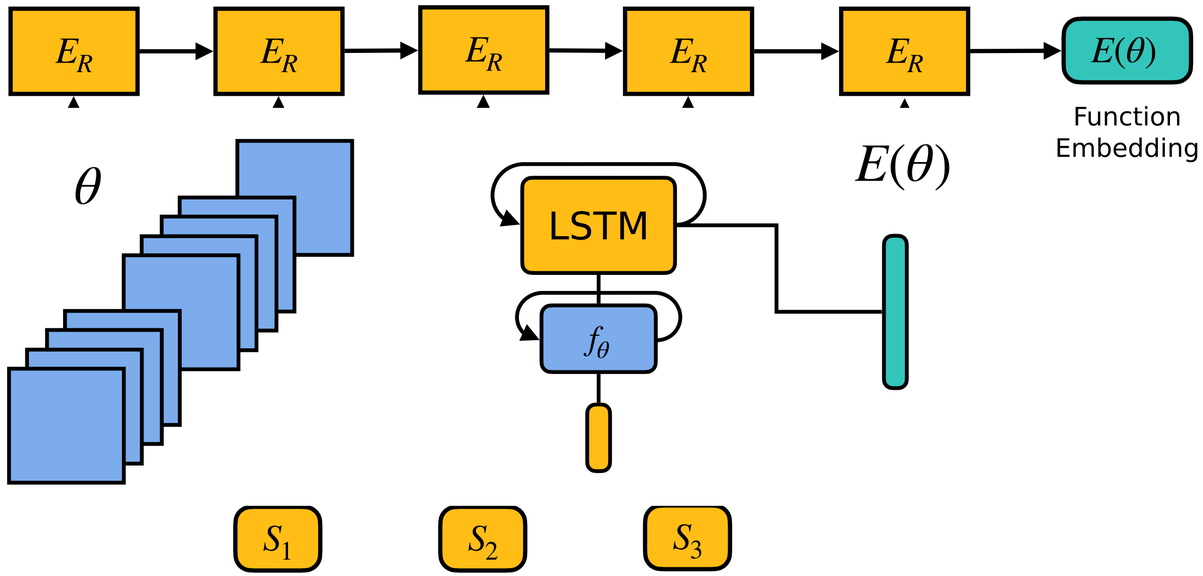
Deep Weight Space Net (Mechanistic)

- Equivariant weight processing modules followed by invariant pooling layer
- Invariant precisely to hidden neuron permutation 👍
- Universal 👍



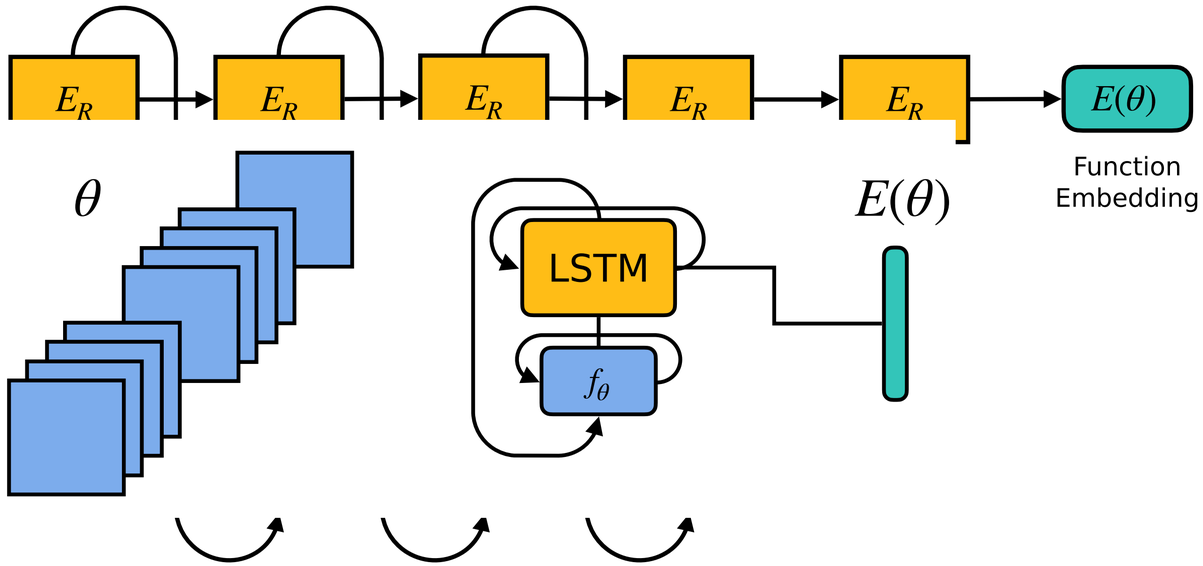
Non-Interactive Probing (Functionalist)

- Fixed but learnable probing sequences are given to f_θ
- Based on the corresponding probing outputs, $E(\theta)$ is computed
- Invariant to everything that leaves f_θ's functionality intact 👍
- Not fully universal 👎



Interactive Probing (Functionalist)

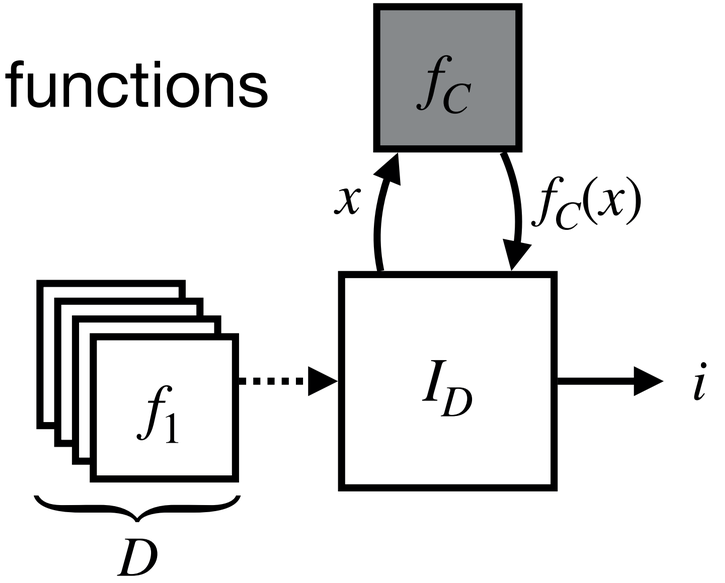
- Probing sequences are dynamically generated by core LSTM
- Next probing inputs depend on f_θ's response to all previous probing inputs
- Invariant to everything that leaves f_θ's functionality intact 👍
- Not fully universal 👎



Functionalist Approach: Theoretical Results

Setup

- Interrogator I_D has to identify f_C from a known set D of functions
- Use as few interactions with f_C as possible



What's the difference between interactive and non-interactive probing?

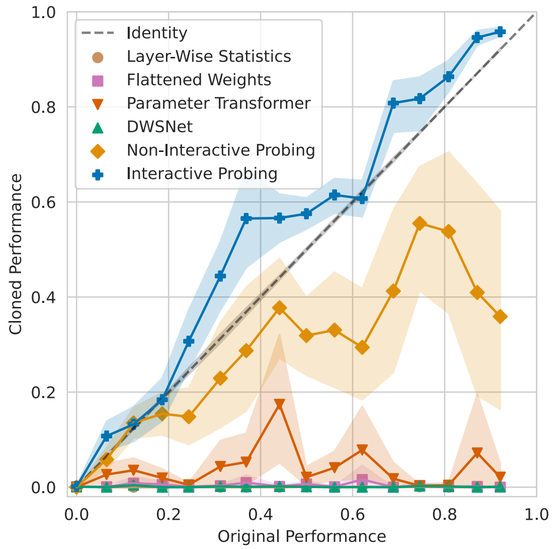
Results

- General upper bound for required interactions is the same
- For certain function sets, interactive probing is exponentially more efficient

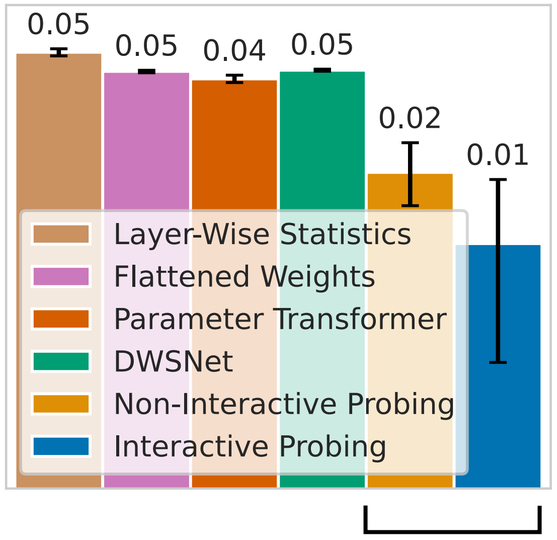
Pre-Training Results

Formal Languages

Original vs. Emulated



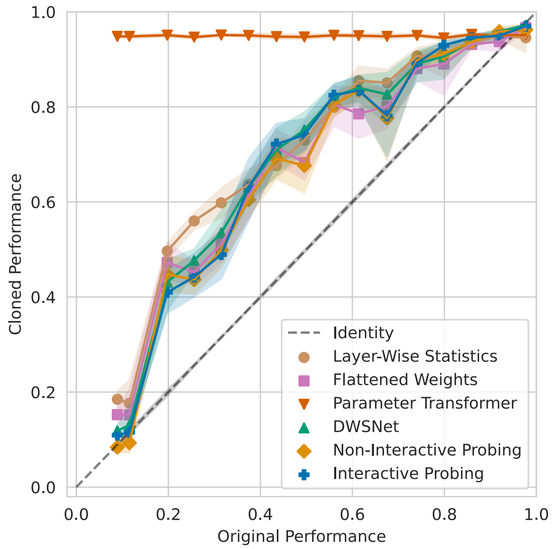
Validation Loss



Functionalist

Sequential MNIST

Original vs. Emulated



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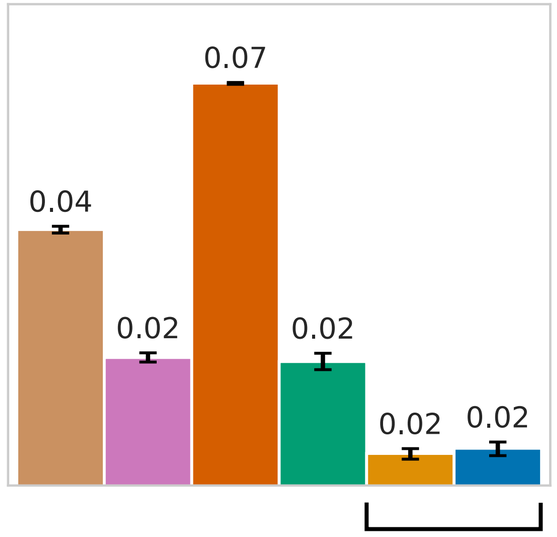
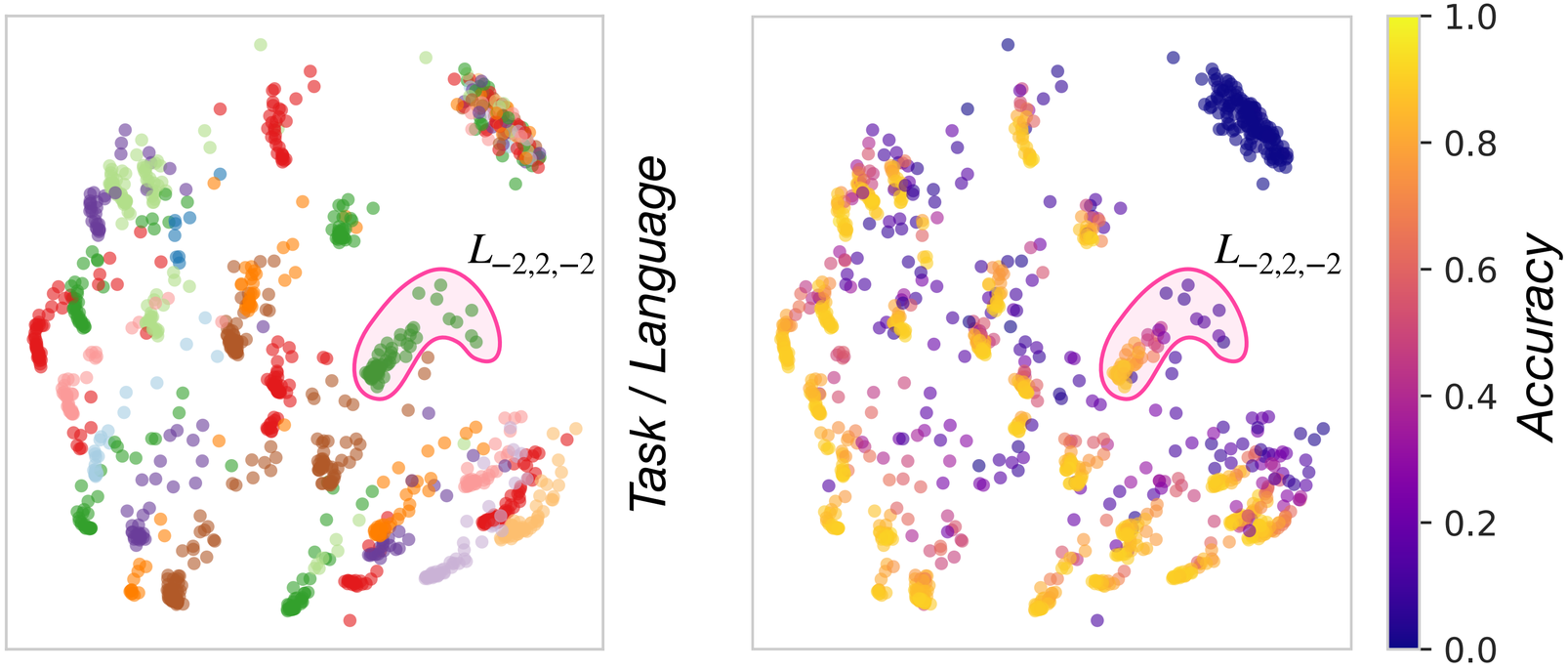


Functionalist

Learned Embedding Spaces

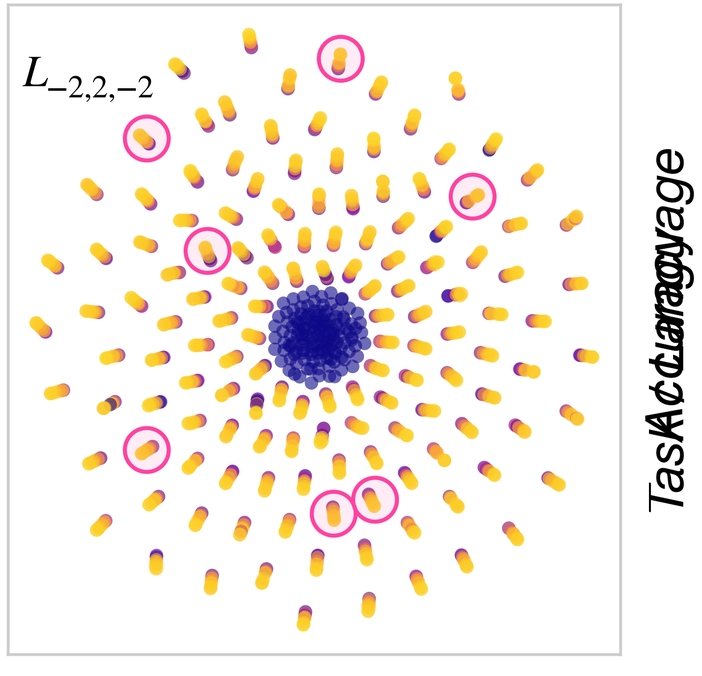
Formal Languages

Interactive Fingerprinting Embeddings (PCA)



Comparison:

t-SNE of weights

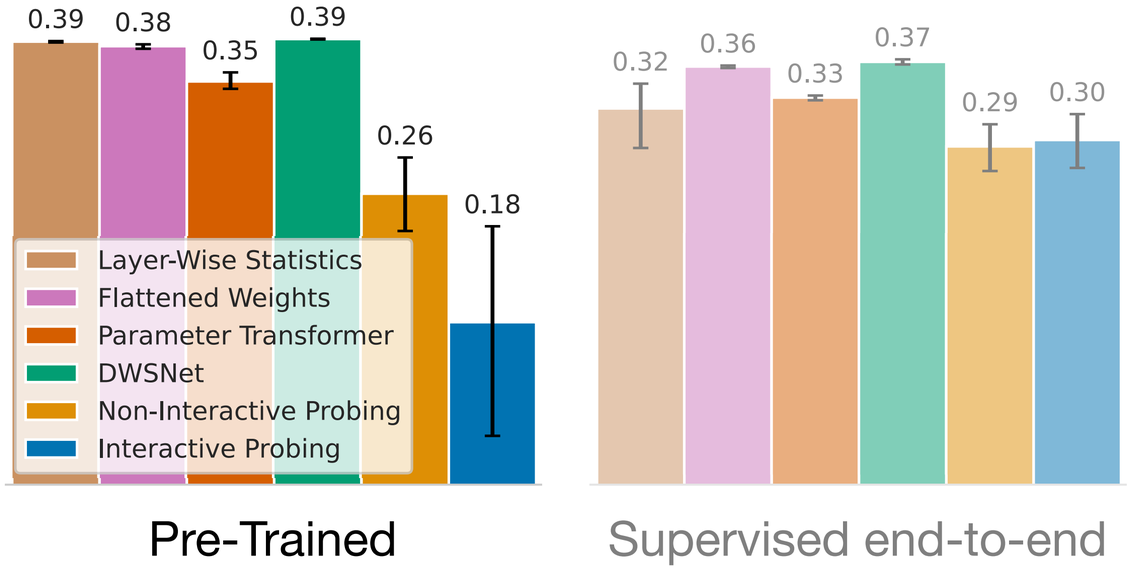


Downstream Results

Predictor MLP on top of learned representations

Formal Languages

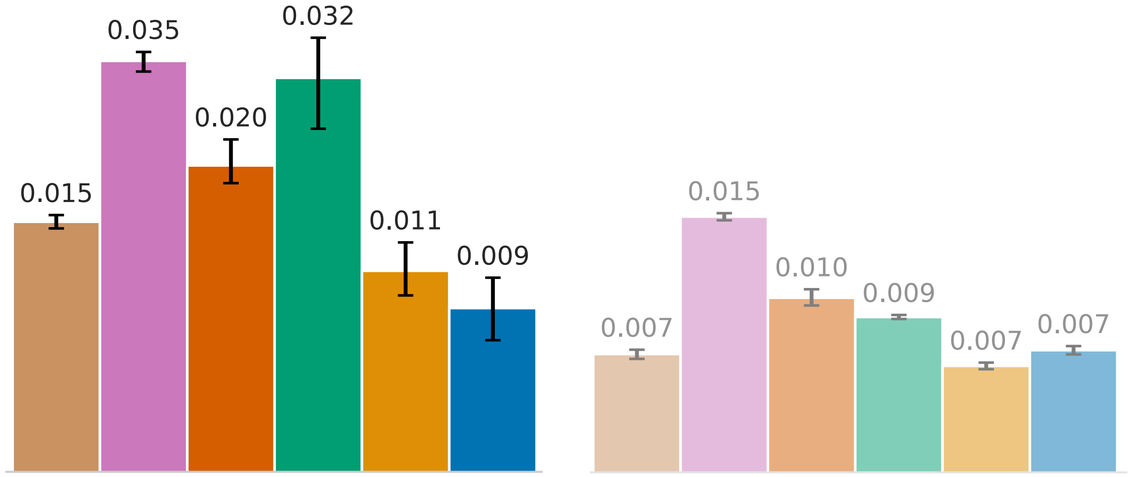
Task prediction loss



Pre-Trained

Supervised end-to-end

Accuracy prediction loss



Pre-Trained

Supervised end-to-end

Conclusion

Learning RNN Weight Representations

- Two RNN ‘Model Zoo’ datasets
- Emulation-based pre-training method
- Distinction between **mechanistic** and **functionalist** weight encoders
- Two novel functionalist encoder types
- Comparison of six different RNN weight encoder architectures

Functionalist encoders are superior at complex tasks

Thank you!

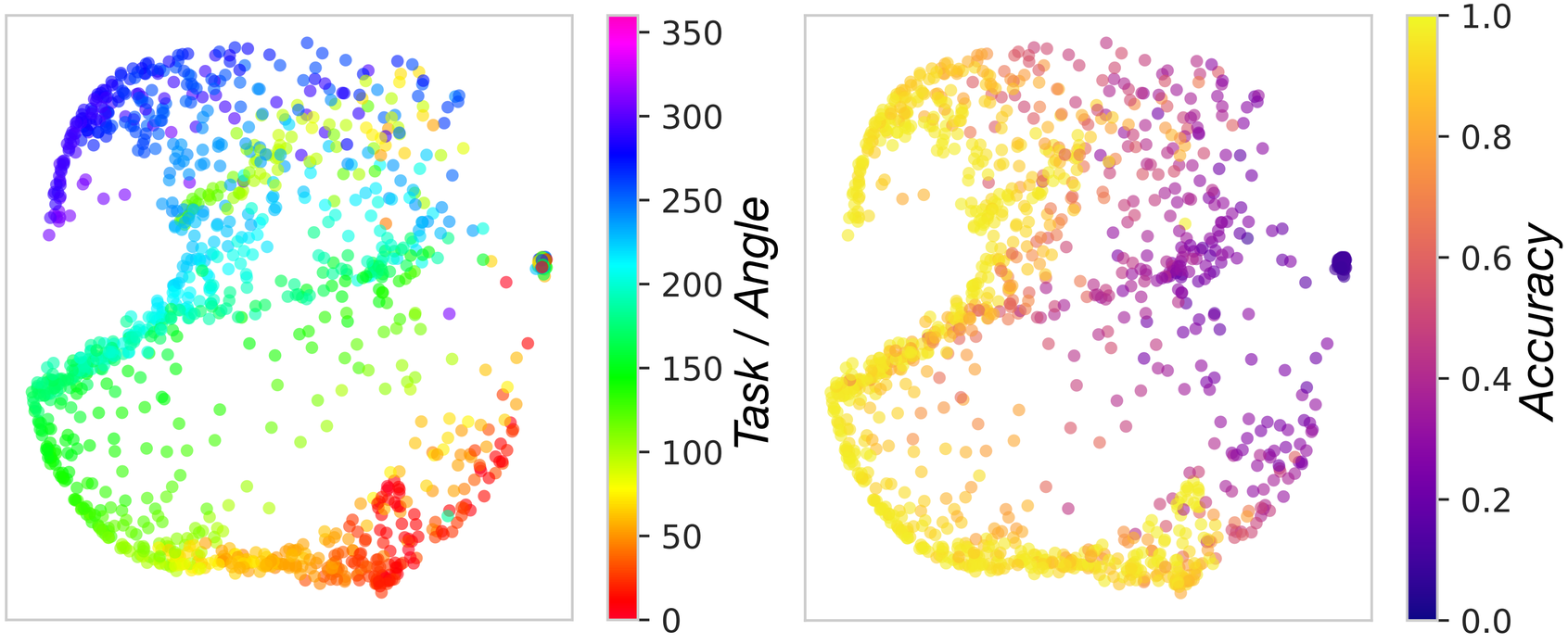
Paper

Code & Datasets

Learned Embedding Spaces

Sequential MNIST

Interactive Fingerprinting Embeddings (PCA)



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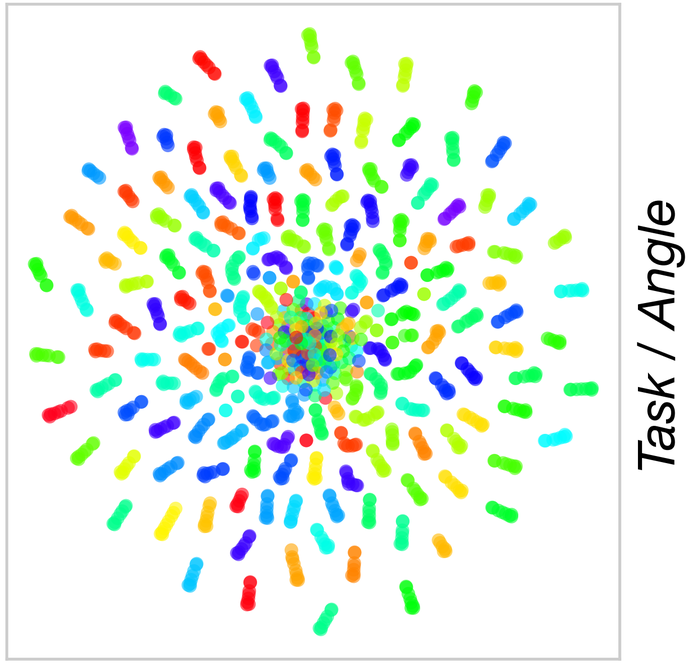
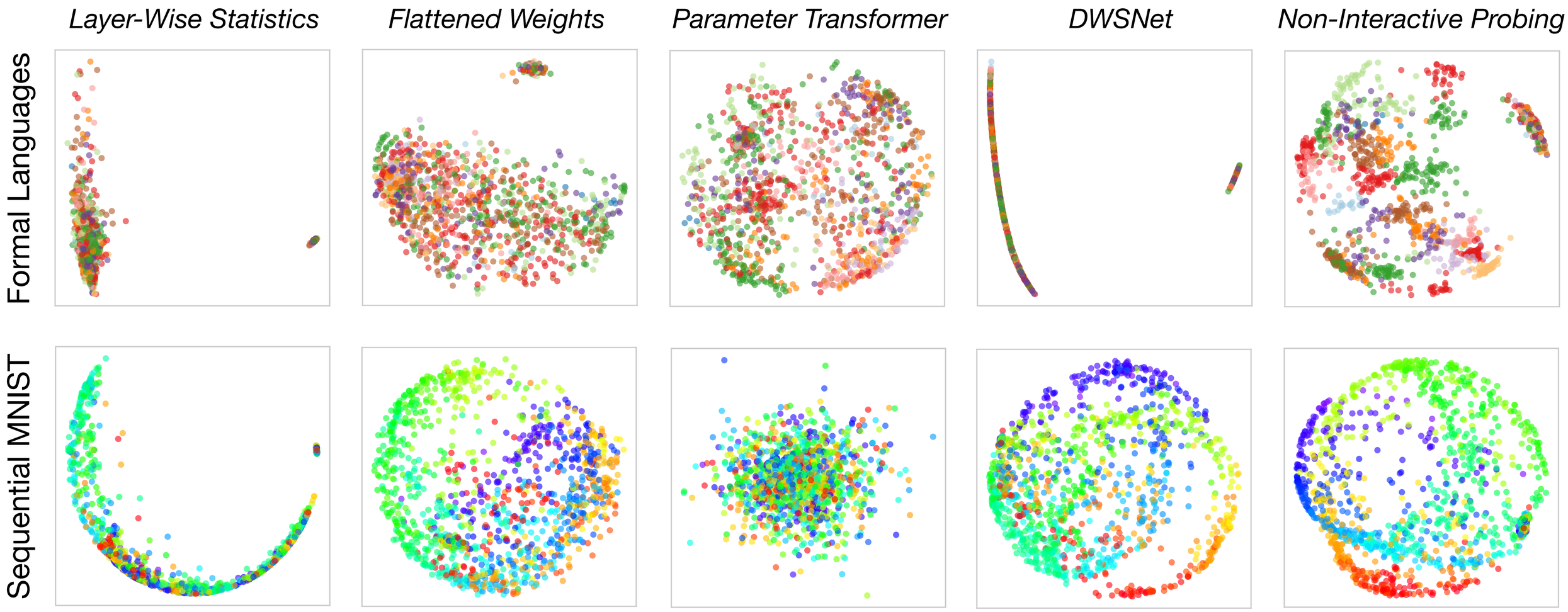


Learned Embedding Spaces

Other encoder architectures, coloured by task



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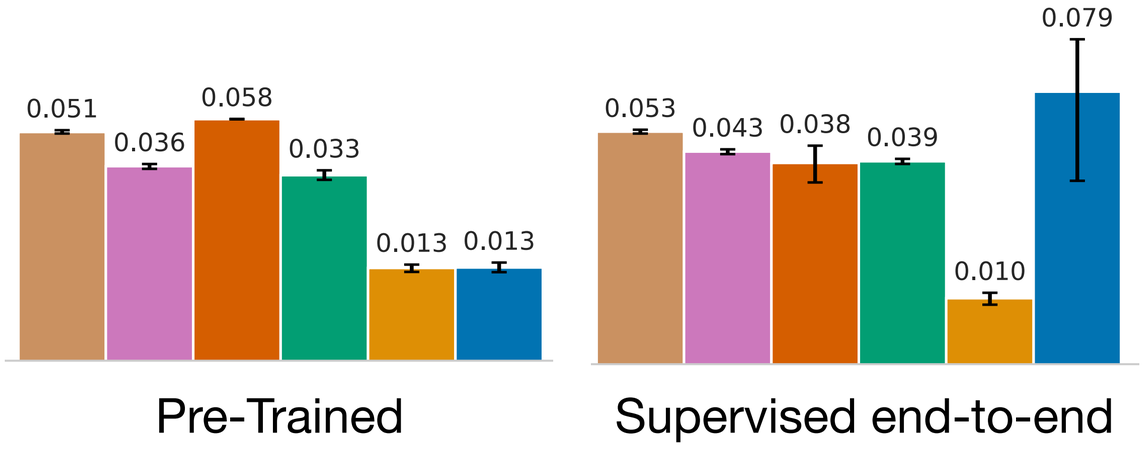

Accuracy prediction loss