Generative Programming	ST 17, Exercise 5
	Deadline: 09.06.2017, 10:30
Name	Effort in h
Points	Lecturer
	Programming  Name

## 1. Dynamic Generation of Proxies using Reflection.Emit

(6+6 Points)

The design pattern *Proxy* and its importance in, e.g., distributed applications (for example remote proxies) should be known to you; in order to make the usage of proxies as efficient and easy as possible, it would be nice to be able to generate proxies for arbitrary objects at runtime. Luckily, this can be realized using generative concepts:

- a) Use the NET Reflection. Emit API for generating proxy objects at runtime; implement the static class *ProxyGenerator* with the static method *Create* that takes the object, for which the proxy shall be generated, as parameter, and returns a reference to the generated proxy object.
  - Using Reflection.Emit the *Create* method shall dynamically generate a new type that stores a reference to the original object as well as implements all methods of the interfaces implemented by the original object. In these methods simply delegate the execution to the encapsulated object.
- b) Extend your implementation of dynamic proxies by implementing a mechanism for inducing arbitrary code before and after a call of the original object.

Write a simple interface *IInterception* that defines the methods *void Before()* and *void After()*, and extend the interface of the *Create* method of the *ProxyGenerator* by a parameter of this type. The proxy object generated by the *ProxyGenerator* shall then call the methods *Before* and *After* each time a method is called and delegated to the encapsulated object.

Test your implementation by implementing a class *LogInterception* that writes simple log messages to the console.

### 2. Dynamic Generation of Functions

(6+6 Points)

The basis of many applications in symbolic computation (as for example genetic programming) is the definition of functions and terminals. Functions are in this context entities that take inputs and calculate return values, whereas terminals read and return data from a data base.

a) First, your task is to use the NET CodeDOM API framework for implementing a mechanism that takes functions and terminals (i.e., their code), compiles these and returns compiled methods that are ready to use.

The basis of these functions and terminals shall be the following definitions:

```
public delegate double TerminalEvaluation(double[][] data,
  int sampleIndex, int variableIndex, double coefficient)
public delegate double FunctionEvaluation(double[] parameters)
```

For evaluating terminals we obviously need information, which variable of the data base and which sample shall be evaluated, whereas functions do not need any further parameters.

For generating test data you can for example use the following code:

```
int n = 1000;
double[][] testData = new double[4][];
for (int i = 0; i < 4; i++) {
   testData[i] = new double[n];
}
for (int i = 0; i < n; i++) {
   testData[0][i] = i + random.NextDouble() - 0.5;
   testData[1][i] = Math.Sin(i / 100.0 * 2.0 * Math.PI);
   testData[2][i] = testData[0][i] + testData[1][i];
   testData[3][i] = testData[2][i] * testData[1][i];
}</pre>
```

b) Develop a mechanism for representing formulas based on structure trees that use the functions and terminals generated in the previous task. The structure node is the core element of structure trees. Nodes shall be able to represent terminals as well as functions and store references to child nodes; additionally we want to manage relevant parameters for evaluating terminals (*VariableIndex*, *Coefficient*).

An exemplary formula, that should be able to be represented, could look as follows: ADD ( $[1.2*VAR_1]$ , MULT ( $[-2.9*VAR_0]$ ,  $[0.3*VAR_2]$ ))

The structure of the nodes developed here should be based on the following definition:

```
public class Node {
   public TerminalEvaluation TerminalEvaluation
   public FunctionEvaluation FunctionEvaluation
   public int VariableIndex
   public double Coefficient
   public List<Node> Children

   public Node(TerminalEvaluation TerminalEvaluation, int VariableIndex,
        double Coefficient)
   public Node(FunctionEvaluation FunctionEvaluation, List<Node> Children)
   public double Evaluate(double[][] Data, int SampleIndex)
}
```

*Please note:* - Test all implementations extensively

- Take care about the proper structuring of your code as well as comments



# 1 Dynamic Generation of Proxies using Reflection.Emit

Dieser Abschnitt behandelt die Aufgabenstellung Dynamic Generation of Proxies using Reflection. Emit.

### 1.1 Lösungsidee

Es wird die Klasse ProxyGenerator implementiert, welche die beiden generischen Methoden Create < T > (T obj) und Create < T > (T obj) und Create < T > (T obj) IInterception < T > interceptor) zur Verfügung stellt, die für das übergebene Objekt eine Proxyklasse und ein Proxyobjekt erstellen und das erstellte Proxyobjekt zurückliefern. Damit der Proxy auch bei einem Cast auf den implementierten Typ greift, müssen die implementierten Methoden der Schnitstelle in der implementierenden Klasse als virtual markiert werden, ansonsten wird die Implementierung implementierenden Klasse aufgerufen und nicht die überschriebenen Methoden des Proxy, was an der Art und Weise der Handhabung von der dynamischen Bindung in C# liegt.

Es werden alle Methoden im Proxy überschrieben, jedoch wird der Interceptor nur bei den Methoden, die im Typ T zur Verfügung stehen eingefügt. Ein Interceptor wird durch die Schnittstelle IIntercepton spezifiziert, wobei die beiden Methoden Before und After von einem Interceptor implementiert werden müssen. Diese beiden Methoden Before und After bekommen das Objekt vom Typ T und den Methodennamen übergeben, sodass der Interceptor mit dem Objekt interagieren kann und auch die Information hat welche Methode abgefangen wird.

Es wird die Klasse LogInterception implementiert, welche die Schnittstelle IInterception implementiert und bei einem Aufruf der Methoden Before und After Logs generiert.

### 1.2 Quelltexte

Dieser Abschnitt beinhaltet die implementierten Quelltexte und das Testprogramm.

Listing 1: IInterception.cs

```
using System;
   using System.Collections.Generic;
 2
   using System.Linq;
 3
   using System. Text;
   using System. Threading. Tasks;
   namespace Reflection.Emit
 7
   {
 8
       /// <summaru>
 9
       /// Specifies an interceptor which can perform before and after actions
10
       /// on a intercepted method invocation.
11
       /// </summary>
12
       public interface IInterception<in T>
13
14
            /// <summary>
15
            /// Action performed before the actual method execution.
16
            /// </summary>
17
            /// <param name="intercepted">the intercepted object</param>
18
            /// <param name="methodName">the intercepted method name</param>
19
            void Before(T intercepted, string methodName);
20
21
22
            /// <summary>
            /// Action performed after the actual method execution
23
24
            /// <param name="intercepted">the intercepted object</param>
25
            /// <param name="methodName">the intercepted method name</param>
```

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```
void After(T intercepted, string methodName);

Representation of the string methodName);

Representation of the string methodName);
```

Listing 2: Interfaces.cs

```
using System;
2
   namespace Reflection.Emit
 4
        /// <summary>
 5
        /// Test interface for implementing class to be proxied
 6
       /// </summary>
       public interface ITest
 9
            int DoStuff(int i, int j);
10
11
12
            void DoVoidStuff();
        }
13
14
        /// <summary>
15
        /// Second interface wich gets not intercepted
16
        /// </summary>
17
       public interface ISecondTest
18
19
            string DoOtherStuff();
20
21
            void DoOtherVoidStuff();
23
        }
   }
```

Listing 3: LogInterception.cs

```
using System;
   using System.Collections.Generic;
   using System.Linq;
   using System.Text;
   using System. Threading. Tasks;
   namespace Reflection.Emit
7
   {
8
       /// <summary>
9
       /// Implemention of IInterception for logging the method interception.
10
       /// </summary>
11
       public class LogInterception<T> : IInterception<T>
13
           private readonly string _typeFullName;
14
15
           public LogInterception()
16
17
                var type = typeof(LogInterception<T>);
18
                _typeFullName = type.Namespace + "." + type.Name;
19
20
21
22
           public void After(T intercepted, string methodName)
23
                Console.WriteLine($|"{_typeFullName}#After called for '{intercepted}#{methodName}'");
24
25
26
            public void Before(T intercepted, string methodName)
```

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Listing 4: Test.cs

```
using System;
   namespace Reflection.Emit
 5
        /// <summary>
        /// Implemention for testing proxied instance.
 6
        /// Methods are marked as virtual, so that proxy class can override them.
        /// </summary>
       public class Test : ITest, ISecondTest
 9
10
            public virtual int DoStuff(int i, int j)
11
12
                return i + j;
13
14
15
            public virtual void DoVoidStuff()
16
17
                Console.WriteLine("void DoVoidStuff() called");
18
            }
19
20
21
            public virtual string DoOtherStuff()
22
23
                return "string DoOtherStuff() called";
24
            }
25
26
27
            public virtual void DoOtherVoidStuff()
28
            {
                Console.WriteLine("void DoOtherVoidStuff() called");
29
            }
30
        }
31
   }
32
```

Listing 5: ProxyGenerator.cs

```
using System;
   using System.Collections;
   using System.Linq;
   using System.Reflection;
   using System.Reflection.Emit;
   using Reflection.Emit;
   namespace Reflection.Emit
9
   {
       /// <summary>
10
       /// This class provides methods for generating a proxy for any object instance.
11
       /// </summary>
12
       public static class ProxyGenerator
13
14
           private static readonly string AssemblyName = typeof(ProxyGenerator).Namespace + ".Proxy";
15
           private static readonly string ModuleName = AssemblyName;
16
           private static readonly string AssemblyFullName = AssemblyName + ".dll";
```

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```
private const string WrappedFieldName = "proxied";
18
            private const string InterceptorFieldName = "interceptor";
19
20
            /// <summary>
21
            /// Creates the proxied object for the given object.
22
            /// </summary>
23
            /// <typeparam name="T">the type of the given, proxied and intercepted object</typeparam>
24
            /// <param name="obj">the object to proxy</param>
25
            /// <returns>the proxied object</returns>
26
           public static T Create<T>(T obj)
27
28
            {
29
                return Create<T>(obj, null);
            }
30
31
            /// <summary>
32
            /// Creates the proxied object for the given object and applies the interceptor to the
33
            \hookrightarrow methods
            /// accessible by the Type T.
34
            /// </summary>
35
            /// <typeparam name="T">the type of the given, proxied and intercepted object</typeparam>
36
            /// <param name="obj">the object to proxy</param>
37
            /// <param name="interceptor">the interceptor applied to the proxied object method
38
                invocations</param>
39
            /// <returns>the proxied object</returns>
40
            public static T Create<T>(T obj, IInterception<T> interceptor)
41
                var wrappedType = obj.GetType();
42
                var interceptorType = typeof(IInterception<T>);
43
                FieldBuilder wrappedFieldBuilder, interceptorFieldBuilder;
44
45
                #region Create dynamic assembly
46
47
                var assemblyBuilder = AppDomain.CurrentDomain.DefineDynamicAssembly(new
48
                    AssemblyName(AssemblyName),
                    AssemblyBuilderAccess.RunAndSave);
49
50
                var moduleBuilder = assemblyBuilder.DefineDynamicModule(ModuleName, AssemblyFullName);
51
52
53
                #endregion
54
                #region Create type builder
55
56
                var typeBuilder = moduleBuilder.DefineType(
57
                    wrappedType.FullName + "Proxy", wrappedType.Attributes, wrappedType,
58
                     → wrappedType.GetInterfaces());
59
                #endregion
60
61
                #region Create wrapped and interceptor field builder
62
63
                wrappedFieldBuilder = typeBuilder.DefineField(
64
                    WrappedFieldName, wrappedType, FieldAttributes.Private |
65

→ FieldAttributes.InitOnly);
                interceptorFieldBuilder = typeBuilder.DefineField(
66
                    InterceptorFieldName, interceptorType, FieldAttributes.Private
67

→ FieldAttributes.InitOnly);
                #endregion
69
70
                #region Create proxy constructor
71
72
                var constructorBuilder = typeBuilder.DefineConstructor(
73
                    MethodAttributes.Public | MethodAttributes.HideBySig,
74
```

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```
CallingConventions.Standard, new[] {wrappedType, interceptorType});
75
 76
                 var il = constructorBuilder.GetILGenerator();
 77
                 // call this.base()
 78
 79
                 il.Emit(OpCodes.Ldarg_0);
                 il.Emit(OpCodes.Call, wrappedType.GetConstructor(new Type[0]));
 80
 81
                 // store argument obj into wrapped
 82
                 il.Emit(OpCodes.Ldarg_0); // this
83
                 il.Emit(OpCodes.Ldarg_1); // wrapped
84
                 il.Emit(OpCodes.Stfld, wrappedFieldBuilder);
85
                 il.Emit(OpCodes.Ldarg_0); // this
86
                 il.Emit(OpCodes.Ldarg_2); // interceptor
87
                 il.Emit(OpCodes.Stfld, interceptorFieldBuilder);
                 il.Emit(OpCodes.Ret);
 89
 90
91
                 #endregion
92
                 #region Create proxied methods
93
94
                 // only intercept interface methods visible to interceptor
95
                 IList interceptableInterfaces;
96
97
                 if (typeof(T).IsInterface)
 98
 99
                     interceptableInterfaces = new ArrayList()
100
101
                          typeof(T)
                     };
102
                 }
103
                 else
104
                 {
105
                     interceptableInterfaces = new ArrayList(wrappedType.GetInterfaces());
106
                 }
107
108
                 foreach (var interfaceType in wrappedType.GetInterfaces())
109
110
                     foreach (var method in interfaceType.GetMethods())
111
112
                     {
113
                          var methodInfo = wrappedType.GetMethod(method.Name);
                          var parameterTypes = methodInfo
114
                              .GetParameters()
115
                              .Select(x => x.ParameterType)
116
                              .ToArray();
117
                          var methodBuilder = typeBuilder.DefineMethod(
118
                              methodInfo.Name,
119
                              methodInfo.Attributes,
120
                              methodInfo.ReturnType,
121
122
                              parameterTypes);
123
                          // Ensure that proxied method is called, even when proxied object is cast to
124
                          \hookrightarrow implementation class
                          // Needs the implementation class to mark methods as virtual
125
                          if (methodInfo.IsVirtual)
126
                          {
127
                              typeBuilder.DefineMethodOverride(methodBuilder, methodInfo);
128
                          }
130
                          il = methodBuilder.GetILGenerator();
131
132
                          // before interceptor call if interceptor is present
133
                          if ((interceptor != null) &&
134
                               (interceptableInterfaces.Contains(interfaceType)))
                          {
135
```

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```
il.Emit(OpCodes.Ldarg_0); // load this
136
                              il.Emit(OpCodes.Ldfld, interceptorFieldBuilder); // load interceptor field
137
                              il.Emit(OpCodes.Ldarg_0); // load this
                              il.Emit(OpCodes.Ldfld, wrappedFieldBuilder);
                                                                                  // load wrapper field
                              il.Emit(OpCodes.Ldstr, methodInfo.Name);
                                                                                  // load intercepted
140
                               \hookrightarrow method name
                              il.Emit(OpCodes.Callvirt,
141
                                  interceptorFieldBuilder.FieldType.GetMethod(nameof(IInterception<T>.Before)));
                          }
142
143
                          il.Emit(OpCodes.Ldarg_0); // load this
144
                          il.Emit(OpCodes.Ldfld, wrappedFieldBuilder); // load wrapper field
145
                          // load all parameters
146
                         for (byte i = 1; i <= parameterTypes.Length; i++)</pre>
                          {
148
                              il.Emit(OpCodes.Ldarg_S, i);
149
150
                          }
                          il.Emit(OpCodes.Callvirt,
151
                          → wrappedFieldBuilder.FieldType.GetMethod(methodInfo.Name));
152
                          // Void return type cannot be saved as local variable in method body
153
                          if (typeof(void) != methodInfo.ReturnType)
154
155
                              var localBuilder = il.DeclareLocal(methodInfo.ReturnType);
                              il.Emit(OpCodes.Stloc, localBuilder);
158
                              il.Emit(OpCodes.Ldloc, localBuilder);
                          }
159
160
                          // after interceptor call if interceptor is present
161
                          if ((interceptor != null) &&
162
                               (interceptableInterfaces.Contains(interfaceType)))
                          {
163
                              il.Emit(OpCodes.Ldarg_0); // load this
164
                              il.Emit(OpCodes.Ldfld, interceptorFieldBuilder); // load interceptor field
165
                              il.Emit(OpCodes.Ldarg_0); // load this
166
                              il.Emit(OpCodes.Ldfld, wrappedFieldBuilder);
                                                                                  // load wrapper field
167
                              il.Emit(OpCodes.Ldstr, methodInfo.Name);
                                                                                  // load intercepted
168
                              \hookrightarrow \quad \textit{method name}
169
                              il.Emit(OpCodes.Callvirt,
                                  interceptorFieldBuilder.FieldType.GetMethod(nameof(IInterception<T>.After)));
170
171
                          il.Emit(OpCodes.Ret);
172
                     }
173
                 }
174
175
                 #endregion
176
177
                 var createdType = typeBuilder.CreateType();
178
                 assemblyBuilder.Save(AssemblyFullName);
179
                 return (T) Activator.CreateInstance(createdType, obj, interceptor);
180
             }
181
        }
182
    }
183
```

Listing 6: Program.cs

```
using System;

namespace Reflection.Emit

{
    /// <summary>
```

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```
/// Test programm for testing the generated proxy and interceptor
6
     class Program
        static void Main(string[] args)
10
11
           var firstObj = new Test();
12
           var secondObj = new Test();
13
           var thirdObj = new Test();
14
           var firstInterceptor = new LogInterception<ITest>();
15
           var secondInterceptor = new LogInterception<ISecondTest>();
16
           var thirdInterceptor = new LogInterception<Test>();
17
18
19
           try
           {
20
              Console.WriteLine("-----");
21
              Console.WriteLine("DynamicProxy Tests ProxyGenerator.Create<ITest>():");
22
              Console.WriteLine("-----");
23
              Console.WriteLine("-----"):
24
              Console.WriteLine("testNoInterceptor:");
25
              Console.WriteLine("-----");
26
              InvokeMethodsITest(firstObj);
27
              Console.WriteLine("-----
28
              Console.WriteLine("testWithInterceptor:");
30
              Console.WriteLine("-----
              // Create proxy and apply interceptor on ITest interface methods
31
32
              firstObj = (Test)ProxyGenerator.Create(firstObj, firstInterceptor);
33
              InvokeMethodsITest(firstObj);
              Console.WriteLine("----"):
34
              Console.WriteLine(""):
35
36
              Console.WriteLine("----");
37
              Console.WriteLine("DynamicProxy Tests ProxyGenerator.Create<ISecondTest>():");
38
              Console.WriteLine("-----");
39
              Console.WriteLine("-----");
40
              Console.WriteLine("testNoInterceptor:");
41
              Console.WriteLine("----"):
42
              InvokeMethodsITest(secondObj);
43
              Console.WriteLine("----"):
44
              Console.WriteLine("testWithInterceptor:");
45
              Console.WriteLine("-----");
46
              // Create proxy and apply interceptor on ISecondTest interface methods
47
              secondObj = (Test)ProxyGenerator.Create(secondObj, secondInterceptor);
48
              InvokeMethodsITest(secondObj);
49
              Console.WriteLine("----");
50
51
              Console.WriteLine("-----");
52
              Console.WriteLine("DynamicProxy Tests ProxyGenerator.Create<Test>():");
53
              Console.WriteLine("----");
54
              Console.WriteLine("-----"):
55
              Console.WriteLine("testNoInterceptor:");
56
              Console.WriteLine("-----"):
57
              InvokeMethodsITest(thirdObj);
58
              Console.WriteLine("----");
59
              Console.WriteLine("testWithInterceptor:");
60
              Console.WriteLine("-----");
61
              // Create proxy and apply interceptor on Test methods
              thirdObj = ProxyGenerator.Create(thirdObj, thirdInterceptor);
63
              InvokeMethodsITest(thirdObj);
64
              Console.WriteLine("----"):
65
           }
66
           catch (Exception e)
67
68
```

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```
Console.WriteLine($"Exception occured: {e}");
69
                }
70
            }
71
72
            /// <summary>
73
            /// Performs method invocation on ITest instances.
74
            /// </summary>
75
            /// <param name="obj">the ITest instance</param>
76
            private static void InvokeMethodsITest(Test obj)
77
78
                 // ITest methods
79
                Console.WriteLine($"DoStuff(1, 2): {obj.DoStuff(1, 2)}");
80
                Console.WriteLine($"DoStuff(2, 2): {obj.DoStuff(2, 2)}");
81
                Console.WriteLine($"DoStuff(4, 4): {obj.DoStuff(4, 4)}");
82
                obj.DoVoidStuff();
83
                 \begin{subarray}{ll} // & ISecondTest & methods \end{subarray}
84
                Console.WriteLine($"DoOtherStuff: {obj.DoOtherStuff()}");
85
                Console.WriteLine($"DoOtherStuff: {obj.DoOtherStuff()}");
86
                 Console.WriteLine($ "DoOtherStuff: {obj.DoOtherStuff()}");
87
                 obj.DoOtherVoidStuff();
88
            }
89
        }
90
   }
```

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1.3 Tests

Übung 3

Dieser Abschnitt behandelt die Tests in Form von Ausgaben der Logs.

```
DynamicProxy Tests ProxyGenerator.Create<ITest>():
testNoInterceptor:
                   -----
DoStuff(1, 2): 3
DoStuff(2, 2): 4
DoStuff(4, 4): 8
void DoVoidStuff() called
DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
void DoOtherVoidStuff() called
testWithInterceptor:
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff'
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(1, 2): 3
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(2, 2): 4
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(4, 4): 8
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoVoidStuff'
void DoVoidStuff() called
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoVoidStuff'
DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
void DoOtherVoidStuff() called
                          -----
```

Abbildung 1: Test für Interception von ITest

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```
DynamicProxy Tests ProxyGenerator.Create<ISecondTest>():
 testNoInterceptor:
 DoStuff(1, 2): 3
DoStuff(2, 2): 4
DoStuff(4, 4): 8
void DoVoidStuff() called
DoOtherStuff: string DoOtherStuff() called DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
void DoOtherVoidStuff() called
testWithInterceptor:
                      _____
DoStuff(1, 2): 3
DoStuff(2, 2): 4
DoStuff(4, 4): 8
void DoVoidStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherVoidStuff'
void DoOtherVoidStuff() called
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherVoidStuff'
```

Abbildung 2: Test für Interception von ISecondTest

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```
DynamicProxy Tests ProxyGenerator.Create<Test>():
testNoInterceptor:
                          ______
DoStuff(1, 2): 3
DoStuff(2, 2): 4
DoStuff(4, 4): 8
void DoVoidStuff() called
DoOtherStuff: string DoOtherStuff() called DoOtherStuff: string DoOtherStuff() called
DoOtherStuff: string DoOtherStuff() called
void DoOtherVoidStuff() called
testWithInterceptor:
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(1, 2): 3
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(2, 2): 4
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoStuff'
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoStuff'
DoStuff(4, 4): 8
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoVoidStuff'
void DoVoidStuff() called
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoVoidStuff' Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff'
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff'
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherStuff' Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherStuff'
DoOtherStuff: string DoOtherStuff() called
Reflection.Emit.LogInterception`1#Before called for 'Reflection.Emit.Test#DoOtherVoidStuff'
void DoOtherVoidStuff() called
Reflection.Emit.LogInterception`1#After called for 'Reflection.Emit.Test#DoOtherVoidStuff'
```

Abbildung 3: Test für Interception von Test

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# 2 Dynamic Generation of Functions

Dieser Abschnitt behandelt die Aufgabenstellung Dynamic Generation of Functions.

#### 2.1 Lösungsidee

Ein Großteil der Implementierungen wurde bereits in der Übung implementiert, jedoch wurden die folgenden Veränderungen vorgenommen.

Die Methode CompileTerminal verlangt die Argumente in Form eines Strings Arrays und den Datentyp des Resultats der zu erzeugenden Methode, damit der Aufrufer nicht abhängig ist von statische Definitionen in der Implementierung dieser Methode.

Die Methode CompileFunction verlangt das Argument in Form eines Strings und den Datentyp des Resultats der zu erzeugenden Methode, damit der Aufrufer nicht abhängig ist von statische Definitionen in der Implementierung dieser Methode.

Die delegate Definitionen wurden in die Datei Node.cs verschoben, da die delegates die unterstützten Evaluierungsmethoden darstellen, die von den implementierten Nodes unterstützt werden. Die Methoden CompileTerminal und CompileFunctional liefern ein Objekt des Datentyps T und sind daher unabhängig von der konkreten Ausprägung der Terminal- und Funktionsmethode.

Es wird die Schnittstelle *INode* implementiert, die eine Node im Evaluierungsbaum darstellt. Es wird die abstrakte Klasse *BaseNode* implementiert, die alle gemeinsamen *Properties* kapselt. Es werden die Klassen *FunctionalNode* und *TerminalNode* implementiert, welche die Knoten der zwei Typen von Evaluierungsmethoden repräsentieren und die spezifischen Evaluierungen dieser Knotentypen implementieren.

### 2.2 Quelltexte

Dieser Abschnitt beinhaltet die implementierten Quelltexte und das Testprogramm.

Listing 7: AssertDouble.cs

```
using System;
 2
   namespace Symbolic.Computation
 3
 4
       /// <summaru>
 5
       /// Utility class for double assertion.
 6
       /// </summary>
 7
       public static class AssertDouble
 8
            /// <summary>
10
            /// Asserts if the two double values are almost equal.
            /// </summary>
12
            /// <param name="actual">the actual value</param>
13
            /// <param name="expected">the almost expected value</param>
14
            /// <param name="epsilon">the epsilon value</param>
15
            /// <returns>true if almost equal, false otherwise</returns>
16
           public static bool AssertAlmostEqual(this double actual, double expected, double epsilon =
17
                1.0E-12)
            {
18
                if (double.IsInfinity(actual))
19
                    return actual > 0
20
                        ? double. Is Positive Infinity (expected)
21
                         : double.IsNegativeInfinity(expected);
22
```

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```
return Math.Abs(actual - expected) < epsilon;

yellow return Math.Abs(actual - expected) < epsilon;

y
```

### Listing 8: Node.cs

```
using System;
 1
   using System.Collections.Generic;
 2
   using System.Linq;
   using System.Runtime.Remoting.Messaging;
 4
   using System. Text;
   using System. Threading. Tasks;
 8
   namespace Symbolic.Computation
10
        #region Supported Evaluation methods
       public delegate double TerminalEvaluation(double[][] data, int variableIndex, int sampleIndex,
11

→ double coefficient);

12
       public delegate double FunctionEvaluation(double[] parameters);
13
       #endregion
14
15
       #region Node specification
16
       /// <summary>
17
       /// Interface which specifies a Node.
18
       /// </summary>
19
20
       public interface INode
21
       {
            double Evaluate(double[][] data, int sampleIdx);
22
       }
23
24
       /// <summary>
25
       /// The abstract implementation of the INode interface which encapsulates the common members
26
27
       public abstract class BaseNode<T> : INode where T : class
28
29
           protected readonly T Evaluation;
30
31
            /// <summary>
32
            /// Sets the evaluation for the node
33
            /// </summary>
34
            /// <param name="evaluation">to evaluation for this node</param>
35
           protected BaseNode(T evaluation)
36
            {
37
                Evaluation = evaluation ?? throw new ArgumentException("Node must hold an
38
                 ⇔ evaluation");
           }
39
40
            /// <summary>
41
            /// Evaluates the subtree started from this node.
42
            /// </summary>
43
            /// <param name="data">the data for the terminal evaluation</param>
44
            /// <param name="sampleIdx">the idx of the data sample contained in Data[][]</param>
45
            /// <returns></returns>
46
           public abstract double Evaluate(double[][] data, int sampleIdx);
47
48
       #endregion
49
50
       #region Node implementation
51
        /// <summary>
52
       /// Node implementation for functional evaluations
```

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```
/// </summary>
54
        public class FunctionalNode : BaseNode<FunctionEvaluation>
55
56
            private readonly List<INode> _children;
57
58
            /// <summary>
59
            /// Constructs a functional node.
60
            /// </summary>
61
            /// <param name="evaluation">the functional evaluation for this node</param>
62
            /// <param name="children">the children of the functional node</param>
63
            public FunctionalNode(FunctionEvaluation evaluation, List<INode> children) :
64
                base(evaluation)
            {
65
                 this._children = children
66
                                  ?? throw new ArgumentException("Children list must not be null on a
67

    functional node");
                 if (children.Count == 0)
68
69
                     throw new ArgumentException("Children list must not be empty on a functional
70
                     → node");
                }
71
            }
72
73
 74
            public override double Evaluate(double[][] data, int sampleIdx)
 75
                 return Evaluation(_children.Select(child => child.Evaluate(data,
76
                     sampleIdx)).ToArray());
            }
77
        }
78
79
        /// <summary>
80
        /// Node implementation for terminal evaluations
81
        /// </summary>
82
        public class TerminalNode : BaseNode<TerminalEvaluation>
83
            private readonly int _variableIdx;
            private readonly double _coefficient;
87
88
            /// <summary>
            /// Constructs a Node for a terminal evaluation
89
            /// </summary>
90
            /// <param name="evaluation">the terminal evaluation bound to this node</param>
91
            /// <param name="variableIdx">the index of the variable</param>
92
            /// <param name="coefficient">the coefficient for the terminal evaluation</param>
93
            public TerminalNode(TerminalEvaluation evaluation, int variableIdx, double coefficient) :
94
             \hookrightarrow base(evaluation)
                 this._variableIdx = variableIdx;
96
                 this._coefficient = coefficient;
97
            }
98
99
            public override double Evaluate(double[][] data, int sampleIdx)
100
101
                return Evaluation(data, _variableIdx, sampleIdx, _coefficient);
102
            }
103
        }
104
        #endregion
105
    }
106
```

Listing 9: FunctionalBasis.cs

```
using System;
using System.CodeDom.Compiler;
```

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```
using Microsoft.CSharp;
3
 4
   namespace Symbolic.Computation
 5
        /// <summary>
       /// This class provides static methods for creating evaluation methods
       /// </summary>
 9
       public static class FunctionalBasis
10
11
           private const string ClassName = "Definitions";
12
13
            /// <summary>
14
            /// Compiles a terminal evaluation method
15
            /// </summary>
16
            /// <typeparam name="T">The type of the create terminal method</typeparam>
17
            /// <param name="methodCode">the code for the method body</param>
            /// <param name="arguments">the string array representing the methd arguments</param>
19
            /// <param name="compilationResults">the out parameter holding the comiplation
20
            \hookrightarrow result</param>
            /// <returns>the created terminal evaluation delegate</returns>
21
            /// <summary>
22
            public static T CompileTerminal<T>(
23
                string methodCode, string[] arguments, Type resType, out CompilationResults
24
                    compilationResults) where T:class
25
                string namespaceName = typeof(TerminalEvaluation).Namespace;
26
27
                string methodName = typeof(TerminalEvaluation).Name;
28
                string resultType = resType.Name;
                string argumentsCode = string.Join(",", arguments);
29
30
                return Compile<T>(
31
                    namespaceName, ClassName, methodName, resultType, argumentsCode, methodCode,
32
                    out compilationResults);
33
           }
34
35
            /// <summary>
36
            /// Creates a functional evaluation method.
37
38
            /// </summaru>
            /// <typeparam name="T">The type of the create functional method</typeparam>
39
            /// <param name="methodCode">the code for the method body</param>
40
41
            /// <param name="argument">the string representing the method argument</param>
42
            /// <param name="resType">the type of the method result</param>
            /// <param name="compilationResults">the out parameter holding the compilation
43
                result</param>
            /// <returns>the created functional evaluation delegate</returns>
44
            public static T CompileFunction<T>(
45
                string methodCode, string argument, Type resType, out CompilationResults
46
                \hookrightarrow compilationResults) where T : class
47
                string namespaceName = typeof(TerminalEvaluation).Namespace;
48
                string methodName = typeof(TerminalEvaluation).Name;
49
                string resultType = resType.Name;
50
                string argumentsCode = argument;
51
52
                return Compile<T>(
53
                    namespaceName, ClassName, methodName, resultType, argumentsCode, methodCode,
54
                    out compilationResults);
55
           }
56
57
            /// <summary>
58
            /// Compiles a evaluation method
59
60
            /// </summary>
            /// <typeparam name="T">the concrete type of the compilation result</typeparam>
```

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```
/// <param name="namespaceName">the name of the namespace the owning class is in</param>
62
            /// <param name="className">the name of the class</param>
63
            /// <param name="methodName">the name of the method</param>
64
            /// <param name="resultType">the type of the method result</param>
65
            /// <param name="argumentsCode">the code representing the arguments</param>
            /// <param name="methodCode">the code of the method body</param>
67
            /// <param name="compilationResults">the out parameter holding the compilation
68
                result</param>
            /// <returns>the compiled evaluation method</returns>
69
            private static T Compile<T>(string namespaceName, string className,
70
71
                string methodName, string resultType, string argumentsCode, string methodCode,
72
                out CompilationResults compilationResults) where T : class
73
                string code = Auxiliary.CompilableCode(
74
75
                    namespaceName, className, methodName, resultType,
76
                    argumentsCode, methodCode);
77
                var provider = new CSharpCodeProvider();
78
79
                var parameters = new CompilerParameters
80
                    GenerateInMemory = true,
81
                    TreatWarningsAsErrors = false
82
                };
83
84
                var compilerResults = provider.CompileAssemblyFromSource(parameters, code);
85
                var result = default(T);
86
87
                if (!compilerResults.Errors.HasErrors)
88
                    var assembly = compilerResults.CompiledAssembly;
90
                    var definitionsClass = assembly.GetType(
                         string.Format("{0}.{1}", namespaceName, className));
91
                    var methodInfo = definitionsClass.GetMethod(methodName);
92
                    result = Delegate.CreateDelegate(typeof(T), methodInfo) as T;
93
94
                compilationResults = new CompilationResults(compilerResults, code);
95
96
                return result;
97
            }
98
        }
   }
100
```

Listing 10: Program.cs

```
using System;
   using System.Collections.Generic;
3
   namespace Symbolic.Computation
4
   {
5
       /// <summary>
6
       /// Console application for testing the implementations
       /// </summary>
       class Program
9
10
            static void Main(string[] args)
11
12
                // create varaible function
13
                TerminalEvaluation variable = CreateTerminal(new []{
14
                    "double[][] data",
15
                    "int varIdx",
16
                    "int sampleIdx"
17
                    "double coefficient"
18
                }, typeof(double), "return data[varIdx][sampleIdx] * coefficient;");
```

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```
20
             // create addition function
21
            FunctionEvaluation addition = CreateFunctional("double[] data", typeof(double),
22
                "double result = 0.0; for (int i = 0; i < data.Length; i++) result += data[i];
23

→ return result;");
24
             // create multiplication function
25
            FunctionEvaluation multiplication = CreateFunctional("double[] data", typeof(double),
26
                "double result = 1.0; for (int i = 0; i < data.Length; i++) result *= data[i];
27
                → return result;");
28
            Console.WriteLine("-----");
29
             Console.WriteLine("Test functions:");
30
             Console.WriteLine("-----
31
             double[][] data = CreateTestData(4, 4);
32
             Console.WriteLine("TestEvaluation(() => addition([1,2,3]))");
33
             Console WriteLine("-----
34
             TestEvaluation(()=> addition(new double[]{1,2,3}), 6.0);
35
             Console.WriteLine("-----
36
            Console.WriteLine("TestEvaluation(() => multiplication([1,2,3]))");
37
             Console.WriteLine("-----");
38
             TestEvaluation(() => multiplication(new double[] { 1, 2, 3 }), 6.0);
39
             Console.WriteLine("------
40
41
             Console.WriteLine("TestEvaluation(() => varaible([1,2,3], 0, 2, 2))");
42
             Console.WriteLine("-----
             TestEvaluation(() => variable(data, 0, 2, 2.0), (data[0][2] * 2.0));
43
             Console.WriteLine("-----"):
44
             Console.WriteLine():
45
46
            Console.WriteLine("----");
47
             Console.WriteLine("Test evaluation trees:");
48
             Console.WriteLine("-----
49
             Console.WriteLine("TestExample1()");
50
             Console.WriteLine("-----");
51
             TestExample1(addition, multiplication, variable);
             Console.WriteLine("-----");
53
             Console.WriteLine("TestExample2()");
             Console.WriteLine("-----");
55
56
             TestExample2(addition, multiplication, variable);
            Console.WriteLine("-----
57
         }
58
59
         /// <summary>
60
         /// Tests the evaluation methods created via CodeDOM
61
62
         /// <param name="function">the function executing the evaluation method</param>
63
         /// <param name="expected">the expected result</param>
64
         private static void TestEvaluation(Func<double> function, double expected)
65
66
             double actual = function();
67
             Console.WriteLine($"actual:{actual} / expected: {actual} /
68
             → result={actual.AssertAlmostEqual(expected)}");
         }
69
70
         /// <summary>
71
         /// Tests with the first formula
72
         /// </summary>
73
         private static void TestExample1(FunctionEvaluation addition, FunctionEvaluation
74

→ multiplication.

            TerminalEvaluation variable)
75
76
            Console.WriteLine("ADD([1.2*VAR_1], MULT([-2.9*VAR_0], [0.3*VAR_2]))");
77
            Console.WriteLine("----");
```

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```
79
                 const int variableCount = 3;
80
                 const int sampleCount = 5;
 81
                 double[][] data = CreateTestData(variableCount, sampleCount);
 82
 83
                 INode multNode = new FunctionalNode(multiplication, new List<INode>()
 84
85
                     new TerminalNode(variable, 2, 0.3),
86
                     new TerminalNode(variable, 0, -2.9)
87
                 });
88
                 INode rootNode = new FunctionalNode(addition, new List<INode>()
89
90
91
                     multNode.
                     new TerminalNode(variable, 1, 1.2)
92
                 });
 93
 94
                 for (var sampleIdx = 0; sampleIdx < sampleCount; sampleIdx++)</pre>
95
96
                     double actual = rootNode.Evaluate(data, sampleIdx);
97
                     double expected = ((1.2 * data[1][sampleIdx]) + (-2.9 * data[0][sampleIdx] * 0.3 *
98

    data[2][sampleIdx]));
                     Console.WriteLine(
99
                         $"ADD([1.2*{data[1][sampleIdx]}], "
100
                         + $\"MULT([-2.9*{data[0][sampleIdx]}], [0.3*{data[2][sampleIdx]}])) "
101
                         + $"= {actual} "
102
                         + $"= {expected} "
103
                         + $ "= {actual.AssertAlmostEqual(expected)} ");
104
105
            }
106
107
             /// <summary>
108
109
             /// Tests with the second formula
110
             /// </summary>
            private static void TestExample2(FunctionEvaluation addition, FunctionEvaluation
111

→ multiplication,

                 TerminalEvaluation variable)
112
             {
113
                 Console.WriteLine("ADD([2*VAR_0], MULT([4*VAR_1], ADD([-2*VAR_2], MULT([4*VAR_3],
114
                  \hookrightarrow [-2*VAR_4])))");
115
                 Console.WriteLine("---
117
                 const int variableCount = 5;
118
                 const int sampleCount = 5;
                 double[][] data = CreateTestData(variableCount, sampleCount);
119
120
                 INode multONode = new FunctionalNode(multiplication, new List<INode>()
121
122
                     new TerminalNode(variable, 4, -2),
123
                     new TerminalNode(variable, 3, 4)
124
                 });
125
                 INode add1Node = new FunctionalNode(addition, new List<INode>()
126
127
128
                     multONode,
129
                     new TerminalNode(variable, 2, -2)
                 });
130
                 INode mult2Node = new FunctionalNode(multiplication, new List<INode>()
131
132
                     add1Node,
133
                     new TerminalNode(variable, 1, 4)
134
135
                 INode rootNode = new FunctionalNode(addition, new List<INode>()
136
137
                 {
138
                     mult2Node,
```

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```
new TerminalNode(variable, 0, 2)
139
                });
140
                for (var sampleIdx = 0; sampleIdx < sampleCount; sampleIdx++)</pre>
143
                     double actual = rootNode.Evaluate(data, sampleIdx);
144
                     double expected = ((2 * data[0][sampleIdx]) +
145
                                         ((4 * data[1][sampleIdx]) *
146
                                          (((-2) * data[2][sampleIdx]) +
147
                                            (4 * data[3][sampleIdx] * (-2) * data[4][sampleIdx]))));
148
                     Console.WriteLine(
149
                         $"ADD([2*{data[0][sampleIdx]}], "
150
                           $"MULT([4*{data[1][sampleIdx]}], "
151
                         + $ "ADD([-2*{data[2][sampleIdx]}], "
152
                         + $"MULT([4*{data[3][sampleIdx]}], [-2*{data[4][sampleIdx]}])))) "
153
                         + $ "= {actual} "
154
                         + $"= {expected} "
155
                         + $ "= {actual.AssertAlmostEqual(expected)} ");
156
157
                }
            }
158
159
            /// <summary>
160
161
            /// Creates the deterministic test data array
162
            /// </summary>
163
            /// <param name="variableCount">the count of variables to create data for</param>
            /// <param name="sampleCount">the count of samples to create for the varaibles</param>
164
165
            /// <returns>the created deterministic test data array</returns>
166
            private static double[][] CreateTestData(int variableCount, int sampleCount)
            {
167
                double[][] testData = new double[variableCount][];
168
169
170
                for (int i = 1; i <= variableCount; i++)</pre>
                 {
171
                     int iIdx = i - 1;
172
173
                     testData[iIdx] = new double[sampleCount];
                     for (int j = 1; j \le sampleCount; j++)
174
                     {
175
                         int jIdx = j - 1;
176
                         testData[iIdx][jIdx] = i * j;
177
                     }
178
                }
179
                return testData;
180
            }
181
182
            /// <summary>
183
            /// Creates a terminal evaluation method
184
            /// </summary>
            /\!/\!/ <\! param\ name = "arguments" >\! the\ string[]\ representing\ the\ method\ arguments <\! /param>
186
            /// <param name="resultType">the method result type</param>
187
            /// <param name="code">the source code of the method body</param>
188
            /// <returns>the created terminal evaluation method delegate</returns>
189
            private static TerminalEvaluation CreateTerminal(string[] arguments, Type resultType,
190
                 string code)
            {
191
                 CompilationResults compilationResults;
192
193
                TerminalEvaluation variable =FunctionalBasis.CompileTerminalCode,(code,
                     arguments, resultType, out compilationResults);
194
                 if (compilationResults.HasErrors)
195
                 {
                     throw new InvalidProgramException(
196
                         $ "Variable terminal evaluation creation failes: Error:
197
                             {compilationResults.ErrorsExplanation}");
                }
```

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```
199
                                                    return variable;
200
                                       }
201
202
                                        /// <summary>
203
                                        /// Creates a functional evaluation method
204
                                        /// </summary>
205
                                        /// <param name="argument">the string representing the method argument</param>
206
                                        /// <param name="resultType">the method result type</param>
207
                                        /// <param name="code">the source code of the method body</param>
208
                                        /// <returns>the create functional evaluation method delegate</returns>
209
                                       private static FunctionEvaluation CreateFunctional(string argument, Type resultType,
210
                                                     string code)
                                        {
211
                                                    CompilationResults compilationResults;
212
213
                                                    FunctionEvaluation function =
                                                       {\scriptstyle \hookrightarrow} \quad \texttt{FunctionalBasis.CompileFunction} {\scriptstyle <} \texttt{FunctionEvaluation} {\scriptstyle >} (\texttt{code, argument, resultType, or argument, resultType, resultType

→ out compilationResults);

                                                    if (compilationResults.HasErrors)
214
215
                                                                  throw new InvalidProgramException(
216
                                                                               $ "Addition terminal evaluation failes: Error:
217
                                                                                 }
218
219
                                                    return function;
220
                                       }
221
                          }
222
223
             }
```

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#### 2.3 Tests

Dieser Abschnitt beinhaltet die implementierten Quelltexte und das Testprogramm.

```
Test functions:
TestEvaluation(() => addition([1,2,3]))
actual:6 / expected: 6 / result=True
TestEvaluation(() => multiplication([1,2,3]))
actual:6 / expected: 6 / result=True
TestEvaluation(() => varaible([1,2,3], 0, 2, 2))
actual:6 / expected: 6 / result=True
 Test evaluation trees:
TestExample1()
ADD([1.2*VAR_1], MULT([-2.9*VAR_0], [0.3*VAR_2]))
ADD([1.2*2], MULT([-2.9*1], [0.3*3])) = -0.21 = -0.21 = True
ADD([1.2*4], MULT([-2.9*2], [0.3*6])) = -5.64 = -5.64 = True

ADD([1.2*6], MULT([-2.9*3], [0.3*9])) = -16.29 = -16.29 = True
ADD([1.2*8], MULT([-2.9*4], [0.3*12])) = -32.16 = -32.16 = True
ADD([1.2*10], MULT([-2.9*5], [0.3*15])) = -53.25 = -53.25 = True
TestExample2()
ADD([2*VAR_0], MULT([4*VAR_1], ADD([-2*VAR_2], MULT([4*VAR_3], [-2*VAR_4]))))
ADD([2*1], MULT([4*2], ADD([-2*3], MULT([4*4], [-2*5])))) = -1326 = -1326 = True
ADD([2*2], MULT([4*4], ADD([-2*6], MULT([4*8], [-2*10])))) = -10428 = -10428 = True ADD([2*3], MULT([4*6], ADD([-2*9], MULT([4*12], [-2*15])))) = -34986 = -34986 = True ADD([2*4], MULT([4*8], ADD([-2*12], MULT([4*16], [-2*20])))) = -82680 = -82680 = True
ADD([2*5], MULT([4*10], ADD([-2*15], MULT([4*20], [-2*25])))) = -161190 = -161190 = True
```

Abbildung 4: Ausgabe des Testprogramms

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