# Experiment8-董皓彧

环境:

```
gcc.exe (x86_64-win32-seh-rev0, Built by MinGW-W64 project) 8.1.0 Visual Stdio Code 1.83.1
```

作业仓库地址:

https://github.com/FHYQ-Dong/Tsinghua-Program-Design-Assignments/tree/main/Experiment8

# 必做题

# **Experiment8-1**

题目:

39 个犹太人与约瑟夫躲到山洞,39 个犹太人决定宁死也不要被敌人抓到,于是决定了自杀方式:40 个人排成一个圆圈,由第 1 个人开始报数,每报到第 3 人该人就必须自杀,然后再由下一个重新报数,直到所有人都自杀身亡为止。然而约瑟夫并不想死,他站在某个位置上,最终逃过了这场死亡游戏。试问:这个位置是哪个编号?(说明:完成此题时,编号规定从0开始,即 40 个人的编号为 0-39)

输入格式:

无

输出格式:

四行:

前两行: 递归解法: 第一行为答案, 第二行为耗时; 后两行: 循环解法: 第三行为答案, 第四行为耗时

代码:

```
#include <stdio.h>
#include <windows.h>

typedef struct Node {
    int idx;
    struct Node *next;
} Node;
typedef struct Loop {
    Node *head, *tail, *cur;
    int size;
    void (*init)(struct Loop *this, int _size);
} Loop;

double run_time;
LARGE_INTEGER time_start, time_over; //开始时间,结束时间double dqFreq; //计时器频率
```

```
LARGE_INTEGER f;
int cnt = 40, ans = 0;
void _init_loop(Loop *this, int _size) {
    this->head = NULL;
    this->tail = NULL;
    this->cur = (Node*)malloc(sizeof(Node));
    this->size = _size;
    for(int i=this->size-1; i>=0; --i) {
        Node *tmp = (Node*)malloc(sizeof(Node));
        tmp->idx = i;
        tmp->next = this->head;
        this->head = tmp;
        if(i == this->size-1) this->tail = tmp;
        this->tail->next = this->head;
    }
    this->cur = this->head;
    return;
}
void get_ans_loop(Loop *people, int cnt, int *ans) {
    while(people->size > 1) {
        people->cur = people->cur->next;
        Node *tmp = people->cur->next;
        people->cur->next = tmp->next;
        free(tmp);
        people->cur = people->cur->next;
        --people->size;
    }
    *ans = people->cur->idx;
    free(people->cur);
    return;
}
void get_ans_recurrence(Loop *people, int cur_alive, int *ans) {
    if (cur_alive == 1) {
        *ans = people->cur->idx;
        free(people->cur);
        return;
    }
    people->cur = people->cur->next;
    Node *tmp = people->cur->next;
    people->cur->next = tmp->next;
    free(tmp);
    people->cur = people->cur->next;
    --people->size;
    get_ans_recurrence(people, cur_alive-1, ans);
    return;
}
void timer_init() {
    QueryPerformanceFrequency(&f);
    dqFreq=(double)f.QuadPart;
    QueryPerformanceCounter(&time_start);
}
```

```
int main() {
   Loop *people = (Loop*)malloc(sizeof(Loop));
   people->init = _init_loop;
   timer_init();
   people->init(people, cnt);
   QueryPerformanceCounter(&time_start); //计时开始
   get_ans_loop(people, cnt, &ans);
   QueryPerformanceCounter(&time_over); //计时结束
   printf("Answer_loop: %d\n", ans);
   run_time=1000*(time_over.QuadPart-time_start.QuadPart)/dqFreq;
   printf("Time_loop: %lfms\n", run_time);
   people->init(people, cnt);
   QueryPerformanceCounter(&time_start); //计时开始
   get_ans_recurrence(people, cnt, &ans);
   QueryPerformanceCounter(&time_over); //计时结束
   printf("Answer_recurrence: %d\n", ans);
   run_time=1000*(time_over.QuadPart-time_start.QuadPart)/dqFreq;
   printf("Time_recurrence: %lfms\n", run_time);
   return 0;
}
```

#### 输出1:

```
Answer_loop: 27
Time_loop: 0.001500ms
Answer_recurrence: 27
Time_recurrence: 0.000800ms
```

# **Experiment8-2**

#### 题目:

从楼上走到楼下共有n级台阶,每一步有三种走法,走一级、走两级或走三级台阶。问恰好走完这n级台阶共有多少种不同的方案。

#### 输入格式:

```
一行,一个整数,为台阶数 n
```

#### 输出格式:

```
四行:
前两行:递归解法:第一行为答案,第二行为耗时;
后两行:循环解法:第三行为答案,第四行为耗时
```

```
#include<stdio.h>
#include<time.h>
#include<Windows.h>
#include<stdlib.h>
int ans[50+1];
int n;
double run_time;
LARGE_INTEGER time_start, time_over; //开始时间, 结束时间
double dqFreq;
                  //计时器频率
LARGE_INTEGER f;
int GoDown_recurrence(int x) {
    if(!ans[x]) ans[x] = GoDown\_recurrence(x-1) + GoDown\_recurrence(x-2) +
GoDown_recurrence(x-3);
    return ans[x];
}
int GoDown_loop(int x) {
   for(int i = 4; i \le x; i++) ans[i] = ans[i-1] + ans[i-2] + ans[i-3];
    return ans[x];
}
void timer_init() {
   QueryPerformanceFrequency(&f);
   dqFreq=(double)f.QuadPart;
   QueryPerformanceCounter(&time_start);
}
void solve_recurrence() {
   memset(ans, 0, sizeof(ans));
    ans[1] = 1; ans[2] = 2; ans[3] = 4;
   timer_init();
   QueryPerformanceCounter(&time_start); //计时开始
    printf("Answer_recurrence: %d\n", GoDown_recurrence(n));
   QueryPerformanceCounter(&time_over); //计时结束
    run_time=1000*(time_over.QuadPart-time_start.QuadPart)/dqFreq;
    printf("Time_recurrence: %lfms\n", run_time);
    return;
}
void solve_loop() {
   memset(ans, 0, sizeof(ans));
    ans[1] = 1; ans[2] = 2; ans[3] = 4;
   timer_init();
   QueryPerformanceCounter(&time_start); //计时开始
    printf("Answer_loop: %d\n", GoDown_loop(n));
   QueryPerformanceCounter(&time_over);
                                          //计时结束
    run_time=1000*(time_over.QuadPart-time_start.QuadPart)/dqFreq;
    printf("Time_loop: %lfms\n", run_time);
    return;
```

```
int main() {
    scanf("%d", &n);
    solve_recurrence();
    solve_loop();
    return 0;
}
```

```
5
```

### 输出1:

```
Answer_recurrence: 13
Time_recurrence: 0.004100ms
Answer_loop: 13
Time_loop: 0.000200ms
```

### 输入2:

```
6
```

### 输出2:

```
Answer_recurrence: 24
Time_recurrence: 0.003900ms
Answer_loop: 24
Time_loop: 0.000200ms
```

### 输入3:

```
7
```

#### 输出3:

```
Answer_recurrence: 44
Time_recurrence: 0.003600ms
Answer_loop: 44
Time_loop: 0.000200ms
```

### 输入4:

```
8
```

#### 输出4:

Answer\_recurrence: 81

Time\_recurrence: 0.003300ms

Answer\_loop: 81

Time\_loop: 0.000200ms

### 输入5:

9

#### 输出5:

Answer\_recurrence: 149
Time\_recurrence: 0.003600ms

Answer\_loop: 149
Time\_loop: 0.000200ms

#### 输入6:

10

#### 输出6:

Answer\_recurrence: 274

Time\_recurrence: 0.004200ms

Answer\_loop: 274
Time\_loop: 0.000300ms

## 输入7:

11

### 输出7:

Answer\_recurrence: 504

Time\_recurrence: 0.005900ms

Answer\_loop: 504
Time\_loop: 0.000200ms

### 输入8:

12

#### 输出8:

Answer\_recurrence: 927

Time\_recurrence: 0.003900ms

Answer\_loop: 927
Time\_loop: 0.000200ms

#### 输入9:

### 输出9:

Answer\_recurrence: 1705
Time\_recurrence: 0.003600ms

Answer\_loop: 1705
Time\_loop: 0.000200ms

#### 输入10:

14

#### 输出10:

Answer\_recurrence: 3136
Time\_recurrence: 0.003200ms

Answer\_loop: 3136
Time\_loop: 0.000200ms

#### 输入11:

15

#### 输出11:

Answer\_recurrence: 5768
Time\_recurrence: 0.003400ms

Answer\_loop: 5768
Time\_loop: 0.000300ms

### 输入12:

16

#### 输出12:

Answer\_recurrence: 10609 Time\_recurrence: 0.003400ms

Answer\_loop: 10609 Time\_loop: 0.000200ms

#### 输入13:

17

### 输出13:

Answer\_recurrence: 19513
Time\_recurrence: 0.003400ms

Answer\_loop: 19513 Time\_loop: 0.000300ms

### 输入14:

18

#### 输出14:

Answer\_recurrence: 35890 Time\_recurrence: 0.003700ms

Answer\_loop: 35890 Time\_loop: 0.000300ms

#### 输入15:

19

#### 输出15:

Answer\_recurrence: 66012 Time\_recurrence: 0.003500ms

Answer\_loop: 66012 Time\_loop: 0.000200ms

## 输入16:

20

### 输出16:

Answer\_recurrence: 121415
Time\_recurrence: 0.003400ms

Answer\_loop: 121415 Time\_loop: 0.000300ms

### 输入17:

25

#### 输出17:

Answer\_recurrence: 2555757 Time\_recurrence: 0.003500ms

Answer\_loop: 2555757 Time\_loop: 0.000300ms

#### 输入18:

#### 输出18:

```
Answer_recurrence: 1132436852
Time_recurrence: 0.003500ms
Answer_loop: 1132436852
Time_loop: 0.000300ms
```

# 选做题

# **Optional-Experiment8-1**

题目:

```
有一群鸡和一群兔,两种动物只数相同。两种动物的脚的总数都是三位数,且这两个三位数的六个数字分别是0,1,2,3,4,5。编程求鸡和兔的只数是多少? 它们的脚数各是多少?
```

输入格式:

```
无
```

输出格式:

```
若干行,每行为一个可能解,依次输出鸡的数目、鸡的脚数、兔的数目、兔的脚数
```

代码:

```
#include <stdio.h>
#define true 1
#define false 0
typedef char bool;
int chick_feet[720+1], rabbit_feet[720+1], tmp_perm[6];
bool visit[6]:
int cnt, rabbit_cnt, chick_cnt;
void all_permutation(int depth) {
    if (depth == 6) {
        int sum_chick = 0, sum_rabbit = 0;
        for (int i = 0; i < 3; i++) {
            sum_chick *= 10; sum_rabbit *= 10;
            sum_chick += tmp_perm[i]; sum_rabbit += tmp_perm[i+3];
        chick_feet[++cnt] = sum_chick; rabbit_feet[cnt] = sum_rabbit;
        return;
    for (int i = 0; i < 6; i++) {
        if (visit[i]) continue;
        visit[i] = 1;
        tmp_perm[depth] = i;
        all_permutation(depth+1);
```

```
visit[i] = 0;
    }
   return;
}
int main() {
   all_permutation(0);
    for (int i=1; i<=cnt; i++) {
        if (!(chick_feet[i] / 100) || !(rabbit_feet[i] / 100)) continue;
        if (chick_feet[i] % 2 || rabbit_feet[i] % 4) continue;
        chick_cnt = chick_feet[i] / 2; rabbit_cnt = rabbit_feet[i] / 4;
        if (chick_cnt == rabbit_cnt) {
            printf("Chick: %d, Chick_feet: %d, Rabbit: %d, Rabbit_feet: %d\n", \
                chick_cnt, chick_feet[i], rabbit_cnt, rabbit_feet[i]);
        }
    }
   return 0;
}
```

输出1:

```
Chick: 76, Chick_feet: 152, Rabbit: 76, Rabbit_feet: 304
```

# **Optional-Experiment8-2**

题目:

```
编程计算 n=50 时 S 与 NS 的值,并比较大小: 如果 S>NS,输出 1; S=NS,输出 0; S<NS,输出 -1。
```

输入格式:

```
无
```

输出格式:

```
一行,一个整数,总罐头数
```

代码:

```
#include <stdio.h>

double calc_S(int n) {
   int S = 0, sub_S = 0;
   for(int k=1; k<=n; ++k) {
      sub_S += k * k;
      S += sub_S * k;
   }
}</pre>
```

```
return S;
}

double calc_NS(int n) {
    return (double)(n) * (n+1) * (n+2) * (8*n*n + 11*n + 1) / 120;
}

int main() {
    int n = 50;
    double S = calc_S(n), NS = calc_NS(n);
    if (S>NS) puts("1");
    else if (S<NS) puts("-1");
    else puts("0");
    return 0;
}</pre>
```

输出1:

0