backpropagation实现.md 5/13/2018

backpropation算法python代码实现讲解

具体神经网络参见第一个笔记

$$egin{aligned} w_k &
ightarrow w_k' = w_k - \eta rac{\partial C}{\partial w_k} \ \ b_l &
ightarrow b_l' = b_l - \eta rac{\partial C}{\partial b_l}. \end{aligned}$$

批量梯度更新

```
class Network(object):
   #参数, mini_batch:要批量更新的输入实例的集合;eta:学习率
   def update_mini_batch(self, mini_batch, eta):
   # nable w、nable b分别用来装对每层权重矩阵和偏向向量求的偏导数
      nabla_b = [np.zeros(b.shape) for b in self.biases]
      nabla w = [np.zeros(w.shape) for w in self.weights]
      # x是输入实例, y是输出标签,对mini batch的所有实例求偏导
      for x, y in mini batch:
      # 通过backpropagation算法求出对权重和偏向的偏导数
          delta_nabla_b, delta_nabla_w = self.backprop(x, y)
          # 对所有实例的偏导数进行累加(因为是随机梯度下降)
          # nb:一层的偏向向量的累积和,nw一层的权重矩阵的累积和, dnb:一层的偏向向量的
偏导数, dnw,一层的矩阵矩阵的偏导数
          nabla_b = [nb+dnb for nb, dnb in zip(nabla_b, delta_nabla_b)]
          nabla_w = [nw+dnw for nw, dnw in zip(nabla_w, delta_nabla_w)]
          # 随机梯度下降需要除mini batch的size
      # 根据公式计算最后的每层的权重矩阵和偏向向量
      # weights:保存每层的权重矩阵, biases:保存每层的偏向向量
      self.weights = [w-(eta/len(mini_batch))*nw
                    for w, nw in zip(self.weights, nabla_w)]
      self.biases = [b-(eta/len(mini_batch))*nb
                   for b, nb in zip(self.biases, nabla_b)]
```

backpropagation算法

```
class Network(object):
...
   def backprop(self, x, y):
        nabla_b = [np.zeros(b.shape) for b in self.biases]
        nabla_w = [np.zeros(w.shape) for w in self.weights]
        # feedforward (正向更新)
        # 输入层的activation
```

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```
activation = x
   # 用来存储神经网络每层的activation值(包括输入层,隐藏层,输出层)
   activations = [x]
   # 一个list用来存储每层中间变量
   zs = []
   for b, w in zip(self.biases, self.weights):
       # 求出中间变量的值
       z = np.dot(w, activation)+b
       #添加到list中
       zs.append(z)
       # 求出该层activation
       activation = sigmoid(z)
       #添加到activations中
       activations.append(activation)
   # backward pass (反向更新参数)
   # 根据公式求出输出层的error
   delta = self.cost_derivative(activations[-1], y) * \
       sigmoid prime(zs[-1])
   # 根据公式求出输出层的偏导数 dC/dw和dC/dw
   nabla b[-1] = delta
   nabla_w[-1] = np.dot(delta, activations[-2].transpose())
   # 从倒数第二层向第二层反向更新
   for 1 in xrange(2, self.num_layers):
       # 中间变量,对应-1层的activation(注意-1)
       z = zs[-1]
       # 求出-1层激活函数导函数值
       sp = sigmoid_prime(z)
       # 根据公式计算出-1层的error
       delta = np.dot(self.weights[-l+1].transpose(), delta) * sp
       # 根据公式求出-1层的偏导数 dC/dw和dC/dw
       nabla b[-1] = delta
       nabla_w[-1] = np.dot(delta, activations[-1-1].transpose())
   # 返回计算好的2-L层的所有对权重和偏向的偏导数
   return (nabla_b, nabla_w)
# Cost对最后一层activation求导
def cost_derivative(self, output_activations, y):
# 根据Cost函数:cost = 1/2 * (y-a)^2, 求导得出cost'= a-y
   return (output_activations-y)
# 激活函数
def sigmoid(z):
   """The sigmoid function."""
   return 1.0/(1.0+np.exp(-z))
# 激活函数的导函数
def sigmoid prime(z):
   return sigmoid(z)*(1-sigmoid(z))
```

backpropagation算法步骤

- 1. 输入\$x\$:设置输入层相应的activation \$a^{1}\$
- 2. 正向更新 对于每层\$I = 2, 3, \$Idots, L\$ 计算: $$$z^{I} = w^{I} a^{I-1}+b^{I}$ \$quad $$\{I\} = y^{I}$ \$\$

- 3. 计算输出层的error \$\footnote{\text{delta}\L\} = \text{\text{nabla_a C \text{\te}\text{\texi{\texi}\text{\text{\text{\texi}\text{\text{\text{\text{\text{\text{\tir}\tint{\text{\texi}\tint{\
- 4. 反向更新error(Backpropagate the error) 对于每层 \$I = L-1, L-2,¥Idots,2\$ 计算: $\$\$4delta^{I} = ((w^{I+1})^T *4delta^{I+1})$ $\$5dot *4delta^{I}$
- 5. 输出每层的偏导数(\$l=2,3,\$ldots,L\$) 更新公式: $\$\$\$frac\{\$partial C\}\{\$partial w^l_{jk}\} = a^{l-1}_k \$delta^l_j \$quad \$text{和}\$quad \$frac\{\$partial C\}\{\$partial b^l_j\} = \$delta^l_j\$\$$.
- 6. 返回所有的偏导数(nabla_b,nabla_w)