#### **Title**

Multi-Agent Scaling Game Analysis (MASGA): Optimizing Neural Scaling Laws for Large Language Models

#### **Problem Statement**

Existing approaches to neural scaling laws often treat the training process as a single-agent optimization problem, failing to capture the complex dynamics between different components of large language models during training. This oversimplification may lead to suboptimal scaling strategies and inefficient resource allocation in model development.

#### **Motivation**

Traditional power-law regression models and empirical observations of aggregate model performance across different scales do not account for the intricate interactions between model components. By viewing different components of a language model (e.g., attention heads, feed-forward layers) as individual agents in a multi-agent system, we can leverage game theory to better understand and optimize the scaling behavior of these models. This approach allows us to capture the competitive and cooperative dynamics between model components, potentially leading to more efficient and effective scaling strategies.

# **Proposed Method**

We introduce Multi-Agent Scaling Game Analysis (MASGA) for optimizing neural scaling laws. MASGA involves five key steps: 1) Modeling each major component of the language model as an agent with its own utility function based on its contribution to overall model performance. 2) Formulating the training process as a multi-agent game, where agents compete and cooperate to maximize their utilities. 3) Applying techniques from evolutionary game theory to analyze the dynamics of this game across different model scales. 4) Developing a meta-learning algorithm that optimizes the rules of the game (i.e., the training protocol) to achieve desired scaling properties. 5) Implementing a dynamic architecture search method guided by the equilibrium states of the multi-agent game at different scales.

# **Step-by-Step Experiment Plan**

### **Step 1: Model Component Identification**

Identify and categorize major components of language models (e.g., attention heads, feed-forward layers, embedding layers) that will be treated as individual agents in the MASGA framework.

### **Step 2: Utility Function Design**

Design utility functions for each agent type based on their contribution to overall model performance. This may include metrics such as perplexity improvement, attention entropy, or gradient flow.

### **Step 3: Multi-Agent Game Formulation**

Formulate the training process as a multi-agent game, defining the action space for each agent (e.g., parameter updates, attention patterns) and the rules of interaction between agents.

### **Step 4: Evolutionary Game Theory Analysis**

Implement evolutionary game theory algorithms to analyze the dynamics of the multi-agent game across different model scales. This includes studying Nash equilibria, evolutionary stable strategies, and replicator dynamics.

#### Step 5: Meta-Learning Algorithm Development

Develop a meta-learning algorithm that optimizes the rules of the game (i.e., the training protocol) to achieve desired scaling properties. This may involve techniques such as population-based training or neural architecture search.

#### Step 6: Dynamic Architecture Search

Implement a dynamic architecture search method guided by the equilibrium states of the multi-agent game at different scales. This should allow for adaptive model scaling based on the game-theoretic analysis.

#### Step 7: Baseline Model Training

Train baseline language models of various sizes (e.g., 100M, 1B, 10B parameters) using standard training procedures on a diverse corpus of text data.

#### **Step 8: MASGA Model Training**

Train language models of the same sizes as the baselines using the MASGA framework, including the meta-learning algorithm and dynamic architecture search.

### **Step 9: Performance Evaluation**

Evaluate both baseline and MASGA models on a range of downstream tasks, including language modeling, question answering, and text summarization. Use standard metrics such as perplexity, BLEU score, and F1 score.

### Step 10: Scaling Law Analysis

Analyze the scaling behavior of both baseline and MASGA models, comparing their performance across different model sizes and computational budgets.

### **Step 11: Ablation Studies**

Conduct ablation studies to assess the impact of individual components of the MASGA framework, such as the utility function design, evolutionary game theory analysis, and dynamic architecture search.

### **Step 12: Computational Efficiency Analysis**

Compare the computational efficiency of MASGA models with baseline models, considering factors such as training time, inference speed, and resource utilization.

### Step 13: Interpretability Analysis

Analyze the learned strategies and equilibria in the MASGA framework to gain insights into the scaling behavior of different model components and their interactions.

#### **Step 14: Generalization Study**

Investigate the generalization capabilities of MASGA models compared to baselines, particularly on out-of-distribution tasks and low-resource languages.

#### **Step 15: Results Compilation and Analysis**

Compile all experimental results, perform statistical analyses, and prepare visualizations to illustrate the effectiveness of the MASGA approach in optimizing neural scaling laws.

# **Test Case Examples**

#### **Baseline Prompt Input**

Train a 1B parameter language model using standard training procedures on the C4 dataset.

#### **Baseline Prompt Expected Output**

A 1B parameter language model trained using standard procedures, achieving a perplexity of 15.6 on the validation set after 500,000 training steps.

### **Proposed Prompt Input**

Train a 1B parameter language model using the MASGA framework on the C4 dataset.

# **Proposed Prompt Expected Output**

A 1B parameter language model trained using MASGA, achieving a perplexity of 14.2 on the validation set after 450,000 training steps. The model demonstrates improved scaling efficiency, with attention heads and feed-forward layers showing distinct specialization patterns as predicted by the game-theoretic analysis.

## **Explanation**

The MASGA approach leads to improved performance (lower perplexity) and faster convergence (fewer training steps) compared to the baseline. The specialized behavior of model components aligns with the predictions of the game-theoretic analysis, demonstrating the effectiveness of the multi-agent perspective in optimizing neural scaling laws.

## **Fallback Plan**

If the proposed MASGA method does not yield significant improvements over baseline scaling laws, we can pivot the project towards an in-depth analysis of the multi-agent dynamics observed during training. This could involve studying the emergent behaviors and strategies of different model components across scales, even if they don't directly translate to performance gains. We can also investigate whether certain subcomponents or specific tasks benefit more from the MASGA approach, potentially uncovering insights about the heterogeneous nature of scaling in different parts of language models.

Additionally, we could explore alternative formulations of the multi-agent game, such as hierarchical or nested games, to better capture the complex interactions within language models. Finally, we could focus on the interpretability aspects of MASGA, using the game-theoretic framework to provide novel visualizations and explanations of how different components contribute to overall model performance as scale increases.

Ranking Score: 6