

1D Heat equation

Author

Today

Consider the evolution equation for the variable $c(x, t)$:

$$\frac{\partial c}{\partial t} = \nu \frac{\partial^2 c}{\partial x^2} \quad (1)$$

With the initial condition :

$$c(x, 0) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp(-x^2/(2\sigma^2)) \quad (2)$$

and boundary condition

$$c(0, t) = 0 \text{ and } c(L, t) = 0 \quad \forall t \quad (3)$$

Taking the Fourier transform of (1) :

$$\frac{\partial \hat{c}}{\partial t} = -\nu k^2 \hat{c} \quad (4)$$

That we easily can solve numerically.