



# Income and Spending

## Chapter #10

# Introduction

- Why output fluctuates around its potential level?
  - In business cycle booms and recessions, output rises and falls relative to the trend of potential output
- Model in this chapter assumes a mutual interaction between output and spending: spending determines output and income, but output and income also determine spending
- The Keynesian model develops the theory of AD
  - Assume that prices do not change at all and that firms are willing to sell any amount of output at the given level of prices  
→ AS curve is flat
  - Key finding: increases in autonomous spending generate additional increases in AD

# AD and Equilibrium Output

- AD is the total amount of goods demanded in the economy:

$$AD = C + I + G + NX$$

- Output is at its equilibrium level when the quantity of output produced is equal to the quantity demanded, or

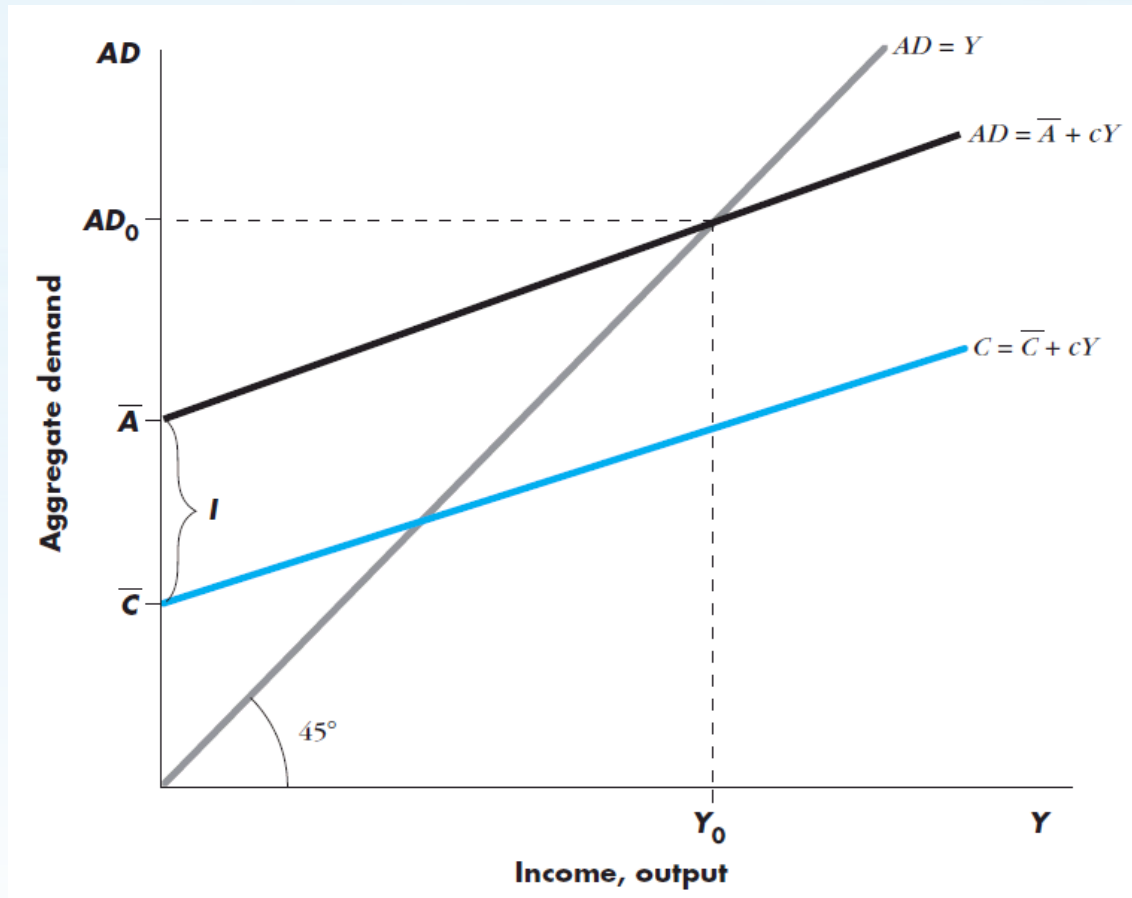
$$Y = AD = C + I + G + NX$$

- When AD is not equal to output there is unplanned inventory investment or disinvestment:  $IU = Y - AD$  (3), where IU is unplanned additions to inventory
  - If  $IU > 0$ , firms cut back on production until output and AD are again in equilibrium

# The Consumption Function

- Consumption is the largest component of AD
  - Consumption increases with income → the relationship between consumption and income is described by the consumption function
  - If  $C$  is consumption and  $Y$  is income, the consumption function is  $C = \bar{C} + cY$  (4), where  $\bar{C} > 0$  and  $0 < c < 1$
  - The intercept of equation (4) is the level of consumption when income is zero → this is greater than zero since there is a subsistence level of consumption
  - The slope of equation (4) is known as the marginal propensity to consume (MPC) → the increase in consumption per unit increase in income

# The Consumption Function



# Consumption and Savings

- Income is either spent or saved → a theory that explains consumption is equivalently explaining the behavior of saving
  - More formally,  $S \equiv Y - C$  (5) → a budget constraint
- Combining (4) and (5) yields the savings function:
$$S \equiv Y - C = Y - \bar{C} - cY = -\bar{C} + (1 - c)Y \quad (6)$$
  - Saving is an increasing function of the level of income because the marginal propensity to save (MPS),  $s = 1 - c$ , is positive
    - Savings increases as income rises
    - Ex. If MPS is 0.1, for every extra dollar of income, savings increases by \$0.10 OR consumers save 10% of an extra dollar of income



# Consumption, AD, and Autonomous Spending

- Now we incorporate the other components of AD: G, I, taxes, and foreign trade (assume autonomous)

- Consumption now depends on disposable income,

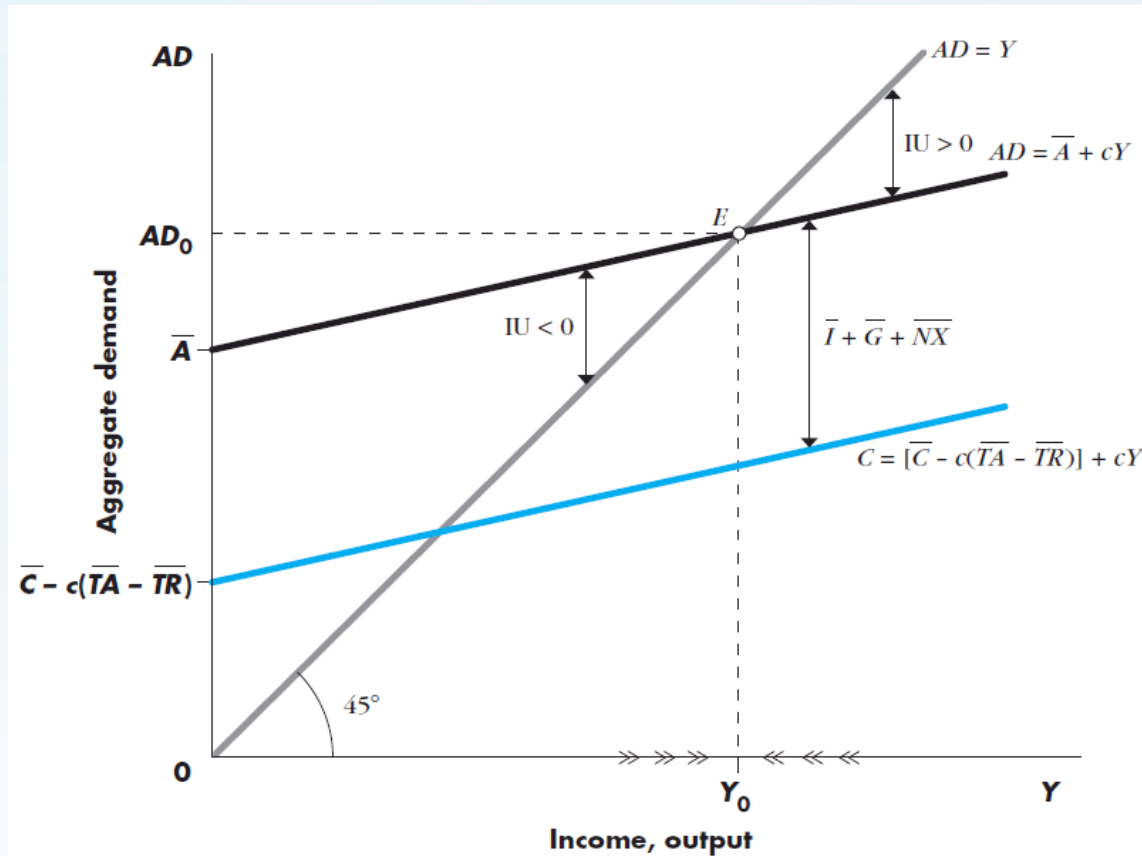
$$YD = Y - TA + TR \quad (7) \quad \text{and} \quad C = \bar{C} + cYD = \bar{C} + c(Y + TR - TA) \quad (8)$$

- AD then becomes  $AD = C + I + G + NX$

$$\begin{aligned} &= \bar{C} + c(Y - TA + TR) + I + G + NX \\ &= [\bar{C} - c(TA - TR) + I + G + NX] + cY \quad (9) \\ &= \bar{A} + cY \end{aligned}$$

where A is independent of the level of income, or autonomous

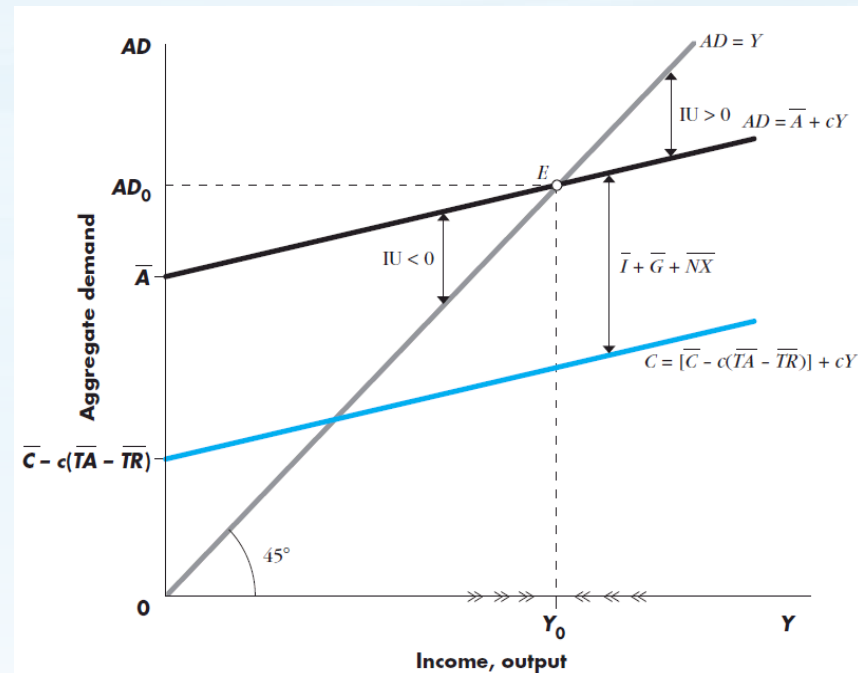
# Consumption, AD, and Autonomous Spending





# Equilibrium Income and Output

- Equilibrium occurs where  $Y=AD$ , which is illustrated by the  $45^\circ$  line  $\rightarrow$  point E
- The arrows show how the economy reaches equilibrium
  - At any level of output below  $Y_0$ , firms' inventories decline, and they increase production
  - At any level of output above  $Y_0$ , firms' inventories increase, and they decrease production



# The Formula for Equilibrium Output

- Can solve for the equilibrium level of output,  $Y_0$ , algebraically:
  - The equilibrium condition is  $Y = AD$  (10)
  - Substituting (9) into (10) yields  $Y = \bar{A} + cY$  (11)
  - Solve for  $Y$  to find the equilibrium level of output:

$$Y - cY = \bar{A}$$
$$Y(1 - c) = \bar{A} \quad (12)$$
$$Y_0 = \frac{1}{(1 - c)} \bar{A}$$

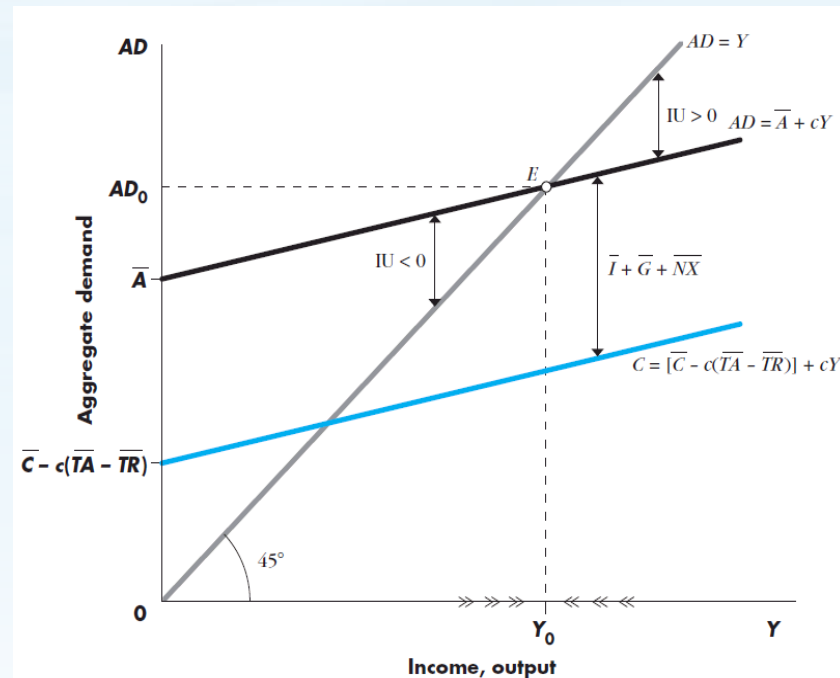
The equilibrium level of output is higher the larger the MPC and the higher the level of autonomous spending.

# The Formula for Equilibrium Output

- Equation (12) shows the level of output as a function of the MPC and A
  - Frequently we are interested in knowing how a *change* in some component of autonomous spending would *change* output
  - Relate changes in output to changes in autonomous spending through  $\Delta Y = \frac{1}{(1-c)} \Delta A$  (13)
    - Ex. If the MPC = 0.9, then  $1/(1-c) = 10 \rightarrow$  an increase in government spending by \$1 billion results in an increase in output by \$10 billion
    - Recipients of increased government spending increase their own spending, the recipients of that spending increase their spending and so on

# Saving and Investment

- In equilibrium, planned investment equals saving in an economy with no government or trade
    - Vertical distance between the AD and consumption schedules equal to planned investment spending,  $I$
    - The vertical distance between the consumption schedule and the  $45^\circ$  line measures saving at each level of income
- at  $Y_0$  the two vertical distances are equal and  $S = I$



# Saving and Investment

- The equality between planned investment and saving can be seen directly from national income accounting
  - Income is either spent or saved:  $Y = C + S$
  - Without  $G$  or trade,  $Y = C + I$
  - Putting the two together:  $C + S = C + I$   
 $S = I$

# Saving and Investment

- With government and foreign trade in the model:
  - Income is either spent, saved, or paid in taxes:  $Y = C + S + TA - TR$
  - Complete aggregate demand is  $AD = C + I + G + NX$
  - Putting the two together:

$$C + I + G + NX = C + S + TA - TR$$

$$I = S + (TA - TR - G) - NX$$

(14)

# The Multiplier

- By how much does a \$1 increase in autonomous spending raise the equilibrium level of income? → The answer is not \$1
  - Out of an additional dollar in income, \$c is consumed
  - Output increases to meet increased expenditure; change in output =  $(1+c)$
  - Expansion in output and income results in further increases

**TABLE 10-1 The Multiplier**

ROUND	INCREASE IN DEMAND THIS ROUND	INCREASE IN PRODUCTION THIS ROUND	TOTAL INCREASE IN INCOME (ALL ROUNDS)
1	$\Delta \bar{A}$	$\Delta \bar{A}$	$\Delta \bar{A}$
2	$c\Delta \bar{A}$	$c\Delta \bar{A}$	$(1 + c)\Delta \bar{A}$
3	$c^2\Delta \bar{A}$	$c^2\Delta \bar{A}$	$(1 + c + c^2)\Delta \bar{A}$
4	$c^3\Delta \bar{A}$	$c^3\Delta \bar{A}$	$(1 + c + c^2 + c^3)\Delta \bar{A}$
...	...	...	...
...	...	...	...
...	...	...	$\frac{1}{1 - c}\Delta \bar{A}$



# The Multiplier

- If we write out the successive rounds of increased spending, starting with the initial increase in autonomous demand, we have:

$$\begin{aligned}\Delta AD &= \Delta \bar{A} + c\Delta \bar{A} + c^2\Delta \bar{A} + c^3\Delta \bar{A} + \dots \\ &= \Delta \bar{A}(1 + c + c^2 + c^3 + \dots)\end{aligned}\quad (15)$$

- This is a geometric series, where  $c < 1$ , that simplifies to:

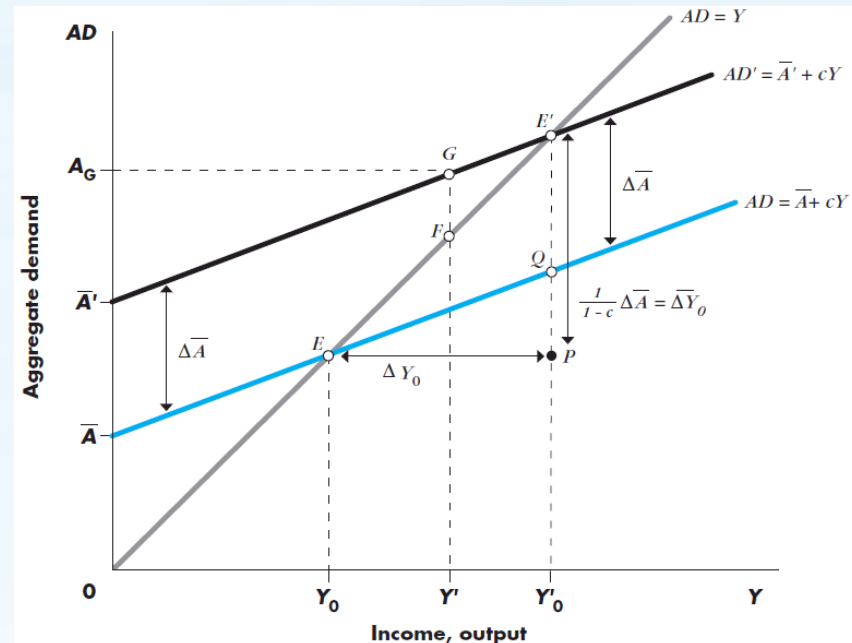
$$\Delta AD = \frac{1}{(1 - c)} \Delta \bar{A} = \Delta Y_0 \quad (16)$$

- Multiplier = amount by which equilibrium output changes when autonomous aggregate demand increases by 1 unit
- The general definition of the multiplier is

$$\frac{\Delta Y}{\Delta A} = \alpha = \frac{1}{(1 - c)} \quad (17)$$

# The Multiplier

- Effect of an increase in autonomous spending on the equilibrium level of output:
  - The initial equilibrium is at point E, with income at  $Y_0$
  - If autonomous spending increases, the AD curve shifts up by  $\Delta \bar{A}$ , and income increases to  $Y'$
  - The new equilibrium is at E' with income at  $\Delta Y_0 = Y' - Y_0$



# The Government Sector

- The government affects the level of equilibrium output in two ways:
  1. Government expenditures (component of AD)
  2. Taxes and transfers
- Fiscal policy is the policy of the government with regards to  $G$ ,  $TR$ , and  $TA$ 
  - Assume  $G$  and  $TR$  are constant, and that there is a proportional income tax ( $t$ )
  - The consumption function becomes: 
$$C = \bar{C} + c(Y + TR - tY) \quad (19)$$
$$= \bar{C} + cTR + c(1 - t)Y$$

# The Government Sector

- Combining (19) with AD:  $AD = C + I + G + NX$   

$$= [\bar{C} + cTR + c(1-t)Y] + I + G + NX \quad (20)$$

$$= A + c(1-t)Y$$
- Using the equilibrium condition,  $Y=AD$ , and equation (19), the equilibrium level of output is:  $Y = \bar{A} + c(1-t)Y$   

$$Y - c(1-t)Y = \bar{A}$$

$$Y[1 - c(1-t)] = \bar{A} \quad (21)$$

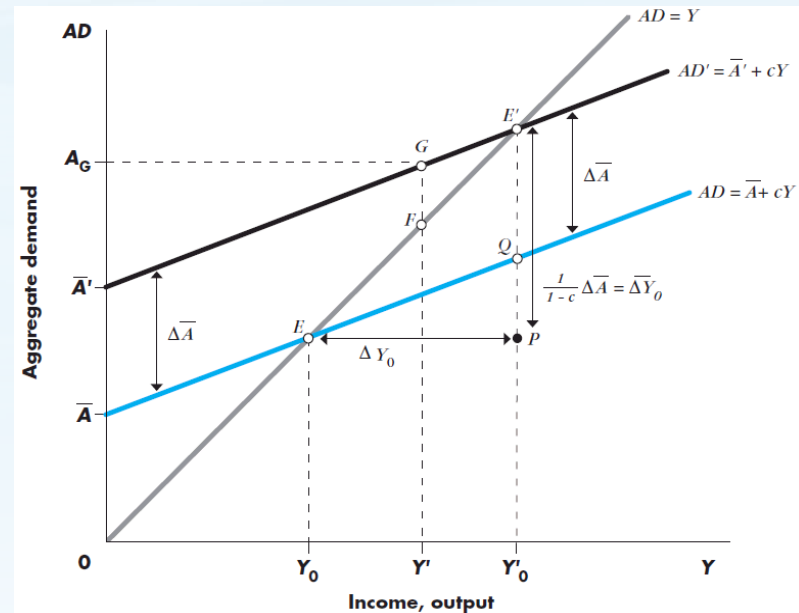
$$Y_0 = \frac{\bar{A}}{1 - c(1-t)}$$
- The presence of the government sector flattens the AD curve and reduces the multiplier to  $\frac{1}{(1 - c(1-t))}$

# Income Taxes as an Automatic Stabilizer

- Automatic stabilizer is any mechanism in the economy that automatically (without case-by-case government intervention) reduces the amount by which output changes in response to a change in autonomous demand
  - One explanation of the business cycle is that it is caused by shifts in autonomous demand, especially investment
  - Swings in investment demand have a smaller effect on output when automatic stabilizers are in place (ex. Proportional income tax)
    - Unemployment benefits are another example of an automatic stabilizer → enables unemployed to continue consuming even though they do not have a job

# Effects of a Change in Fiscal Policy

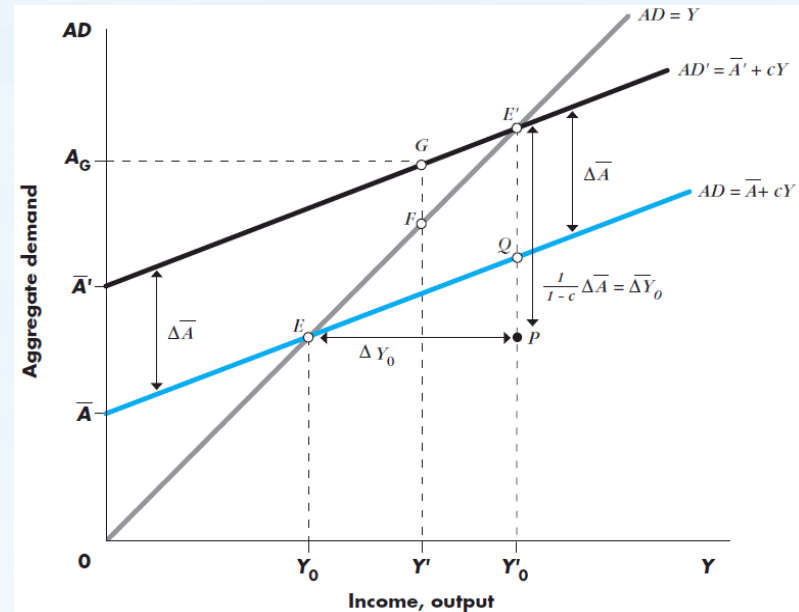
- Suppose government expenditures increase
  - Results in a change in autonomous spending and shifts the AD schedule upward by the amount of that change
  - At the initial level of output,  $Y_0$ , the demand for goods > output, and firms increase production until reach new equilibrium ( $E'$ )
- How much does income expand? The change in equilibrium income is:
 
$$\Delta Y_0 = \frac{1}{1 - c(1 - t)} \Delta \bar{G} = \alpha_G \Delta \bar{G} \quad (22)$$



# Effects of a Change in Fiscal Policy

$$\Delta Y_0 = \frac{1}{1 - c(1 - t)} \Delta \bar{G} = \alpha_G \Delta \bar{G} \quad (22)$$

- A \$1 increase in G will lead to an increase in income in excess of a dollar
  - If  $c = 0.80$  and  $t = 0.25$ , the multiplier is 2.5
  - A \$1 increase in G results in an increase in equilibrium income of \$2.50
  - $\Delta G$ ,  $\Delta Y$  shown in Figure 10-3





# Effects of a Change in Fiscal Policy

- Suppose government increases TR instead
  - Autonomous spending would increase by only  $c\Delta TR$ , so output would increase by  $\alpha_G c\Delta TR$
  - The multiplier for transfer payments is smaller than that for  $G$  by a factor of  $c$ 
    - Part of any increase in TR is saved (since considered income)
- If the government increases marginal tax rates, two things happen:
  - The direct effect is that AD is reduced since disposable income decreases, and thus consumption falls
  - The multiplier is smaller, and the shock will have a smaller effect on AD

# The Budget

- Government budget deficits have been the norm in the U.S. since the 1960s
- Is there a reason for concern over a budget deficit?
  - The fear is that the government's borrowing makes it difficult for private firms to borrow and invest → slows economic growth



FIGURE 10-5 U.S. GOVERNMENT BUDGET DEFICIT AS A PERCENTAGE OF GDP, 1900–2011.

# The Budget

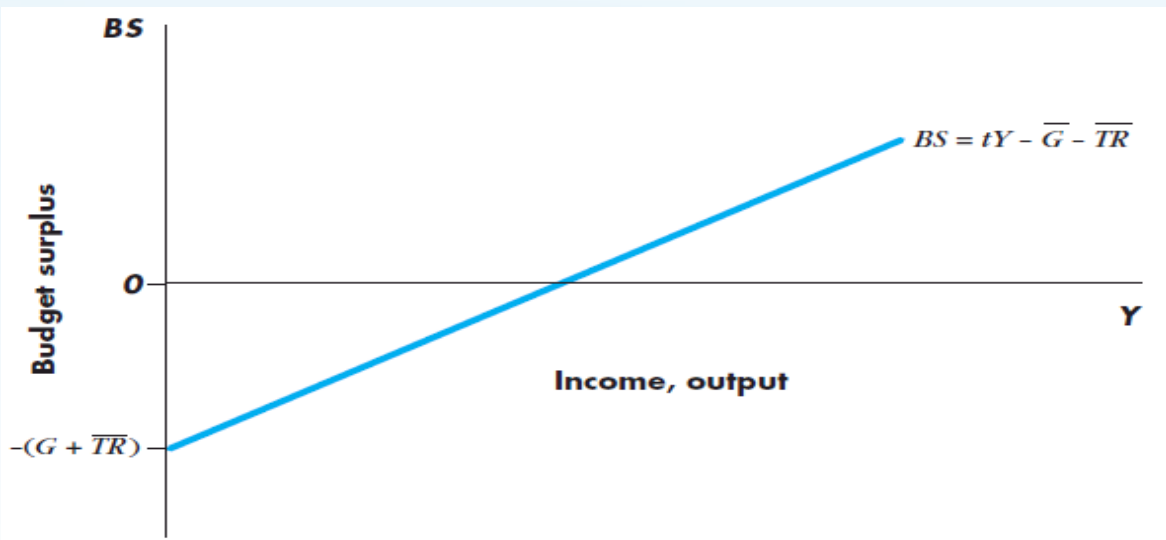
- The budget surplus is the excess of the government's revenues,  $TA$ , over its initial expenditures consisting of purchases of goods and services and  $TR$ :  $BS \equiv TA - G - TR$  (24)
  - A negative budget surplus is a budget deficit



FIGURE 10-5 U.S. GOVERNMENT BUDGET DEFICIT AS A PERCENTAGE OF GDP, 1900–2011.

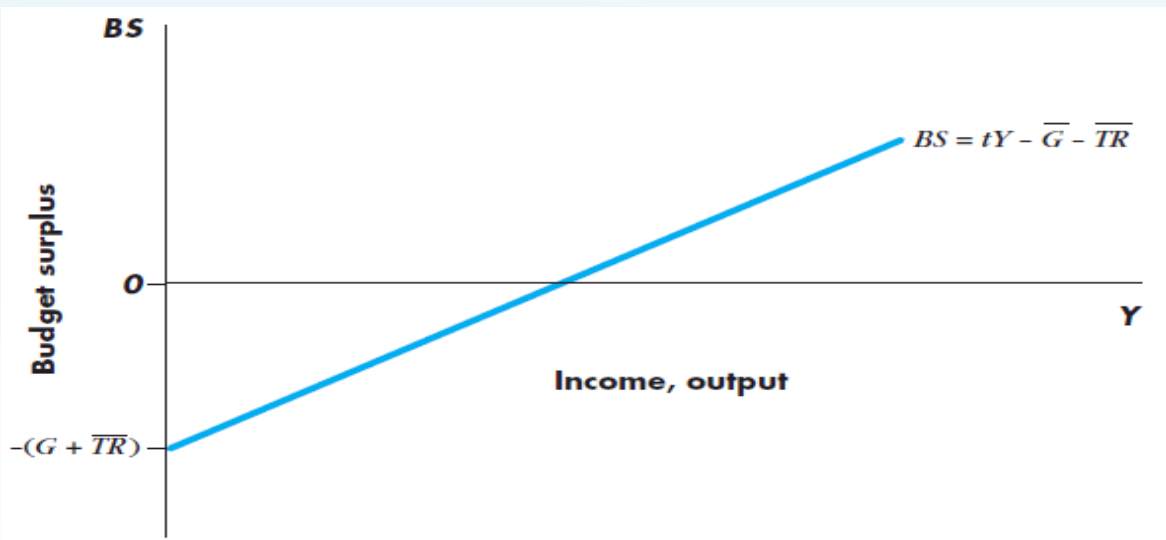
# The Budget

- If  $TA = tY$ , the budget surplus is defined as:  $BS \equiv tY - G - TR$  (24a)
- Figure 10-6 plots the BS as a function of the level of income for given  $G$ ,  $TR$ , and  $t$ 
  - At low levels of income, the budget is in deficit since spends more than it receives in income
  - At high levels of income, the budget is in surplus since the government receives more in income than it spends



# The Budget

- Figure 10-6 shows that the budget deficit depends on the government's policy choices ( $G$ ,  $t$ , and  $TR$ ) and also anything else that shifts the level of income
  - Ex. Suppose that there is an increase in  $I$  demand that increases the level of output
  - *budget deficit will fall as tax revenues increase*



# Effects of Government Purchases and Tax Changes on the BS

- How do changes in fiscal policy affect the budget? OR  
Must an increase in  $G$  reduce the BS?
    - An increase in  $G$  reduces the surplus, but also increases income, and thus tax revenues
- *Possibility that increased tax collections > increase in  $G$*

# Effects of Government Purchases and Tax Changes on the BS

- The change in income due to increased  $G$  is equal to  $\Delta Y_0 \equiv \alpha_G \Delta G$ , a fraction of which is collected in taxes

– Tax revenues increases by  $t\alpha_G \Delta G$

– The change in BS is 
$$\begin{aligned}\Delta BS &= \Delta TA - \Delta G \\ &= t\alpha_G \Delta G - \Delta G \\ &= -\frac{(1-c)(1-t)}{1-c(1-t)} \Delta G\end{aligned}$$

(25)