



Growth and Policy

Chapter #4

Introduction

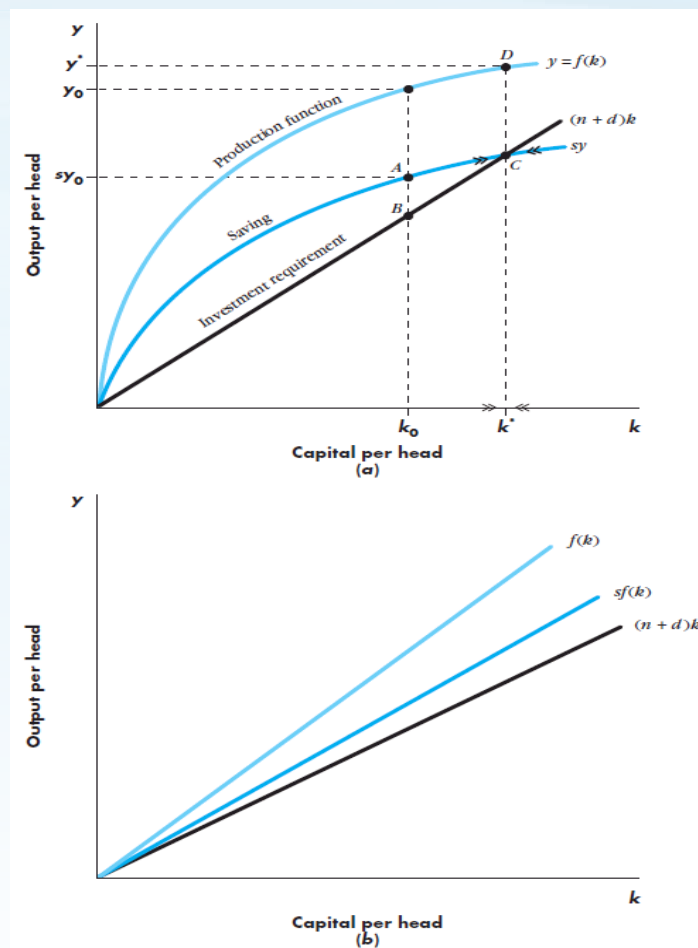
- Chapter 3 explained how GDP and GDP growth are determined by the savings rate, rate of population growth, and the rate of technological progress
- The question analyzed in this chapter is “How do society’s choices affect these parameters?”
 - In many developed countries, invention and advances in technology are the key determinants of growth
 - Technological advances are much less important for poor countries → more important to invest in human and physical capital and borrow technological advances from others
- Endogenous growth theory (Romer, Lucas) explains how society’s choices lead to technological progress and growth

Trouble With Neoclassical Growth Theory

- By the late 1980's there was great dissatisfaction with neoclassical growth theory since:
 1. It does not explain the economic determinants of technological progress
 2. It predicts that economic growth and savings rates are uncorrelated in the steady state
- Endogenous growth theory emphasizes different growth opportunities in physical and knowledge capital
 - Diminishing marginal returns to physical capital, but perhaps not knowledge capital
 - The idea that increased investment in human capital increases growth is key to linking higher savings rates to higher equilibrium growth rates

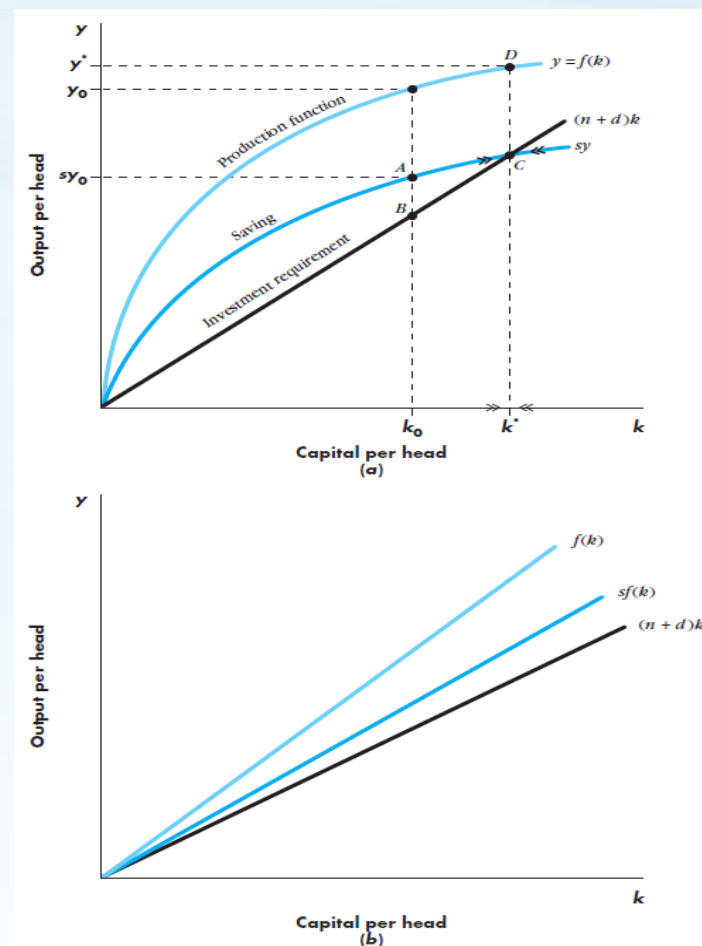
Mechanics of Endogenous Growth

- Need to modify the production function to allow for self-sustaining, endogenous growth
- Figure 4-1 (a) shows the Solow growth diagram, with the steady state at point C where savings equals required investment
 - If savings above required investment, economy is growing as more capital is added → process continues until savings equals required investment (reach the steady state)



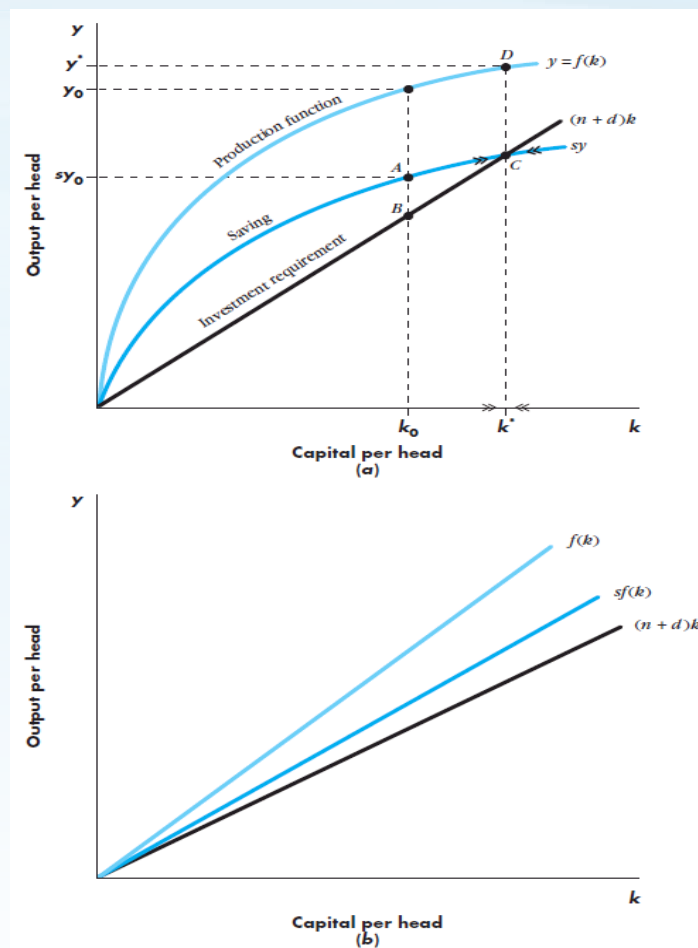
Mechanics of Endogenous Growth

- Need to modify the production function to allow for self-sustaining, endogenous growth
- Figure 4-1 (a) shows the Solow growth diagram, with the steady state at point C where savings equals required investment
 - Due to the diminishing MPK, the production function and savings function flatten out and cross the upward sloping required investment line once



Mechanics of Endogenous Growth

- Need to modify the production function to allow for self-sustaining, endogenous growth
- Economy illustrated in Figure 4-1 (b) is described by a production function with a constant MPK: $Y = aK$ (1)
 - K is the only factor, a is the MPK
 - Production function and savings curve become straight lines, and are always greater than required investment \rightarrow the higher the savings rate, the bigger the gap between savings and required investment = faster the growth



Mechanics of Endogenous Growth

- If the savings rate, s , is constant and there is neither population growth nor depreciation of capital, then the change in the capital stock is defined as:

$$\Delta K = sY = saK$$

$$\text{OR} \quad (2)$$

$$\frac{\Delta K}{K} = sa$$

→ Growth rate of capital is proportional to the savings rate

- Output is proportional to capital, thus the growth rate of output is

$$\frac{\Delta Y}{Y} = sa \quad (3)$$

→ The higher s , the higher the growth rate of output

Deeper Economics of Endogenous Growth

- Eliminating diminishing marginal returns to capital runs against prevailing microeconomic principles
 - If there are constant returns to capital alone, there will be increasing returns to scale to all factors taken together → larger and larger firms become increasingly efficient, and should see a single firm dominate the entire economy
 - Not realistic, so need to eliminate the possibility of increasing returns to scale to all factors, and constant returns to a single factor

Deeper Economics of Endogenous Growth

- Alternatively, a single firm may not capture all benefits of capital → some external to the firm (Romer)
 - When a firm increases K , firm's production increases, but so does the productivity of other firms
 - As long as private return has constant returns to all factors, there will be no tendency towards monopolization

Private vs. Social Returns to Capital

- Investment produces not only new machines, but also new ways of doing things
 - Firms DO capture the production benefits of a new machine (PRIVATE RETURNS)
 - Firms may NOT capture the benefits of new technologies and ideas, since they are easy to copy (SOCIAL RETURNS)
- Endogenous growth theory hinges on the notion that there are substantial external returns to capital
 - Not realistic for physical capital, but quite for human capital:
 1. Contribution of new knowledge only partially captured by creator
 2. From one new idea springs another → knowledge can grow indefinitely

N and the Endogenous Growth Model

Assume:

1. Technology is proportional to the level of capital per worker, or

$$A = \alpha \frac{K}{N} = \alpha k$$

2. Technology is labor augmenting, $Y = F(K, AN)$

3. Technology growth depends on capital growth, or

$$\frac{\Delta A}{A} = \frac{\Delta K}{K} - \frac{\Delta N}{N}$$

- The GDP growth equation from Chapter 3 was $\frac{\Delta y}{y} = \Theta \frac{\Delta k}{k} + (1 - \Theta) \frac{\Delta A}{A}$

$$\frac{\Delta y}{y} = \Theta \frac{\Delta k}{k} + (1 - \Theta) \frac{\Delta A}{A}$$

- If $\frac{\Delta A}{A} = \frac{\Delta K}{K} - \frac{\Delta N}{N} = \frac{\Delta k}{k}$, then $\frac{\Delta y}{y} = \Theta \frac{\Delta k}{k} + (1 - \Theta) \frac{\Delta k}{k}$

$$= \frac{\Delta k}{k}$$

N and the Endogenous Growth Model

- Since the numerator and denominator of y/k grow at equal rates, y/k is constant
 - What is that constant? Find by dividing the production function by K and simplifying:

$$\begin{aligned}
 \frac{y}{k} &= \frac{F(K, AN)}{K} \\
 &= F\left(\frac{K}{K}, A \frac{N}{K}\right) \\
 &= F\left(\frac{K}{K}, \alpha \frac{K}{N} \times \frac{N}{K}\right) \\
 &= F(1, \alpha) \equiv a
 \end{aligned}$$

- The equation for capital accumulation can be written as:

$$\frac{\Delta k}{k} = s \frac{y}{k} - (n + d)$$

- Making the substitution for y/k , the growth rate of y and k becomes:

$$\begin{aligned}
 \frac{\Delta y}{y} = \frac{\Delta k}{k} &= g = s \frac{y}{k} - (n + d) \\
 &= sa - (n + d)
 \end{aligned}$$

Convergence

- Do economies with different initial levels of output eventually grow to equal standards of living or *converge*?
 - Neoclassical growth theory predicts *absolute convergence* for economies with equal rates of saving and population growth and with access to the same technology → should all reach the same steady state level of income
 - *Conditional convergence* is predicted for economies with different rates of savings and/or population growth → steady state level of income will differ, but the growth rates will eventually converge
- Endogenous growth theory predicts that a high savings rate leads to a high growth rate

Convergence

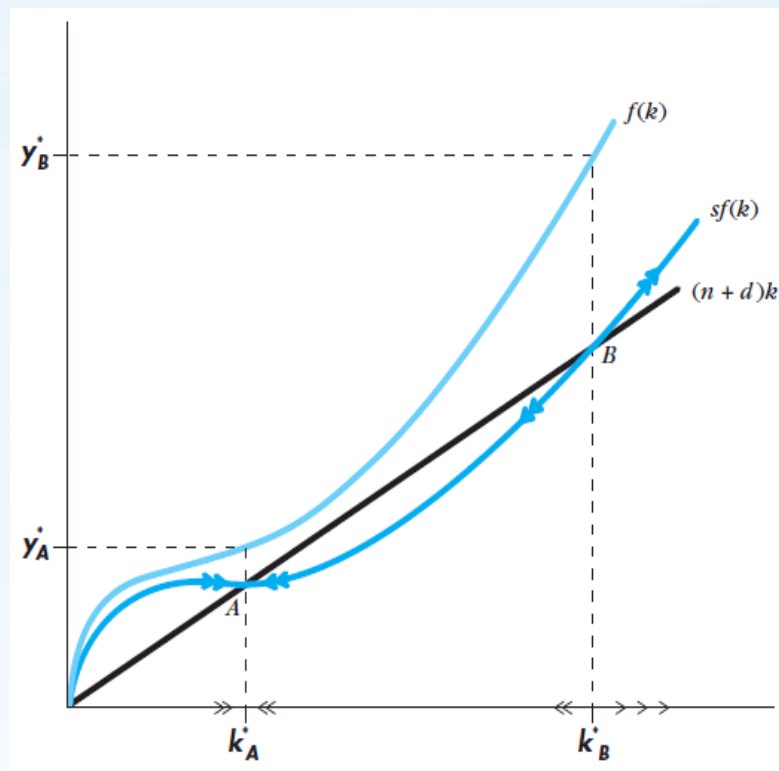
- Do economies with different initial levels of output eventually grow to equal standards of living or *converge*?
 - Robert Barro tested these competing theories, and found that:
 1. Countries with higher levels of investment tend to grow faster
 2. The impact of higher investment on growth is however transitory
 - Countries with higher investment will end in a steady state with higher per capita income, but not with a higher growth rate
 - Countries do appear to converge conditionally, and thus endogenous growth theory is not very useful for explaining international differences in growth rates

Growth Traps and Two Sector Models

- How do we explain a world with BOTH no growth AND high growth countries?
 - Ghana is an example of an economy that has experienced no growth since 1900
 - China is an example of an economy that has experienced rapid growth in recent years
- Need a model in which there is a possibility of both a no growth, low income equilibrium AND a high growth, high income equilibrium
 - Elements of both neoclassical and endogenous growth theories

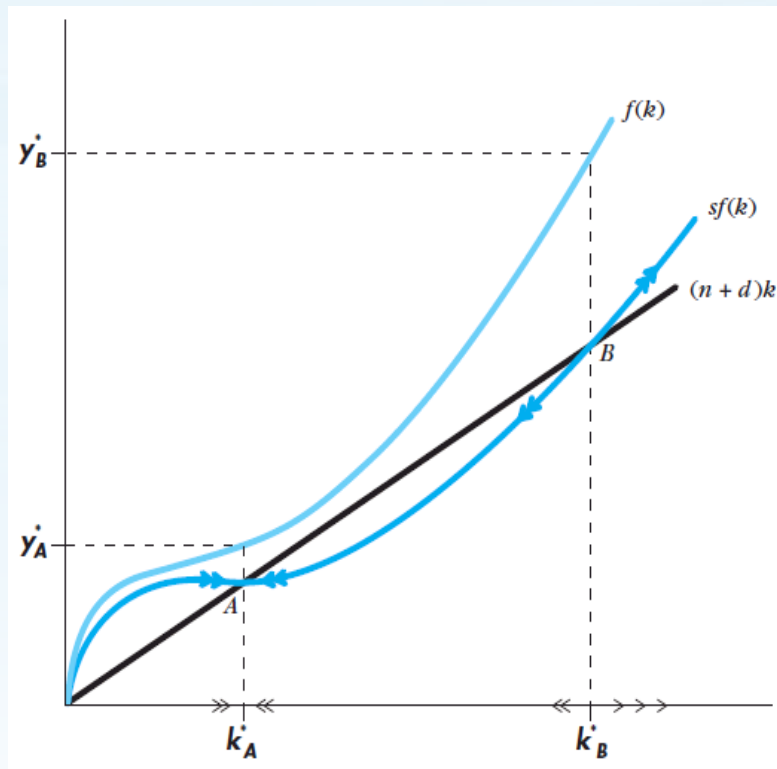
Growth Traps and Two-Sector Models

- Suppose there are two types of investment opportunities:
 1. Those with diminishing MPK at low income levels
 2. Those with constant MPK at high income levels
- Figure 4-2 illustrates such a situation
 - The production function has a curved segment at low levels of income and an upward sloping line at high levels
 - Point A is a neoclassical steady state equilibrium, while past point B there is ongoing growth (endogenous growth theory)



Growth Traps and Two-Sector Models

- Suppose there are two types of investment opportunities:
 1. Those with diminishing MPK at low income levels
 2. Those with constant MPK at high income levels
- With two outlets for investment, society must choose not only total investment, but also the division between the two
 - Societies that direct I towards research and development will have ongoing growth
 - Societies that direct I toward physical capital may have higher output in the short run at the expense of lower long run growth

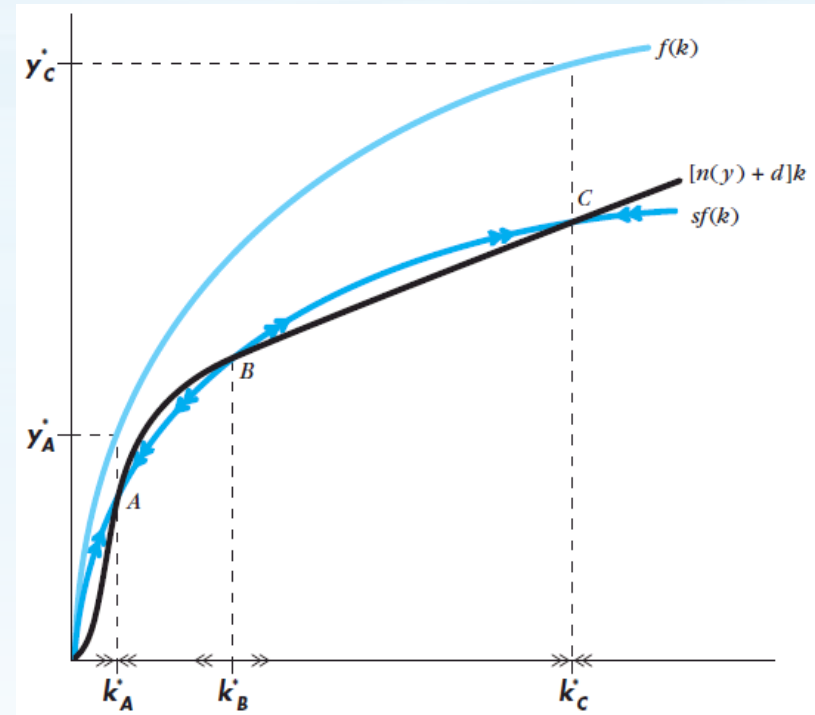


Solow Model with Endogenous Population Growth

- One of the oldest ideas in economics is that population growth works against the achievement of high income
 - The Solow growth model predicts that high population growth, n , means lower steady state income as each worker will have less capital to work with
- Over a wide range of incomes, population growth itself depends on income, $n(y)$
 - Very poor countries have high birth rates and high death rates, resulting in moderately high population growth
 - As income rises, death rates fall and population growth increases
 - At very high incomes, birth rates fall, some even approaching zero population growth (ZPG)

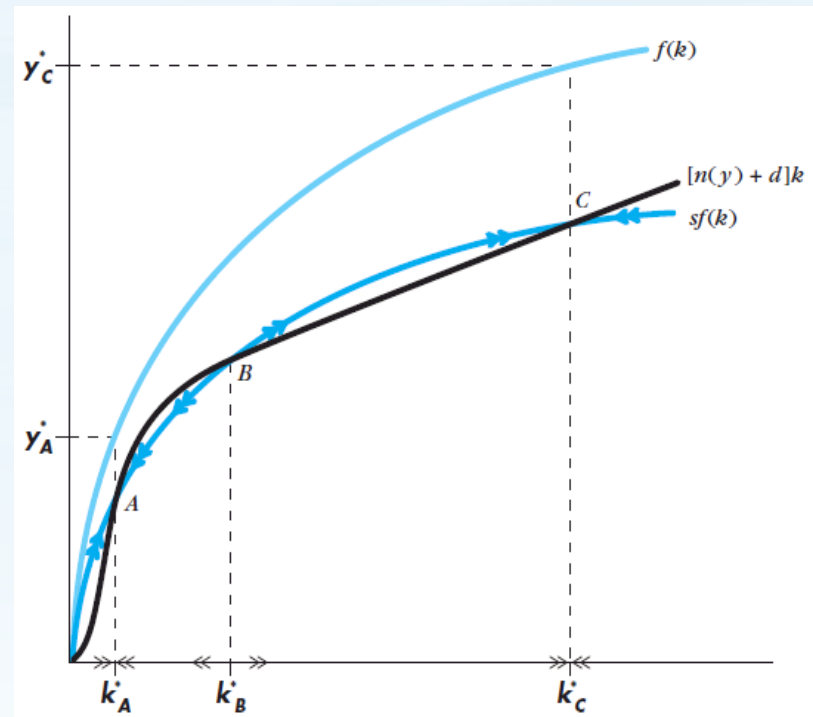
Solow Model with Endogenous Population Growth

- Figure 4-3 illustrates the modified investment requirement line on the Solow diagram to account for n as a function of y
- The investment requirement line, $[n(y) + d]k$, rises slowly at low levels of income, then sharply at higher levels, and finally levels off at high levels of income



Solow Model with Endogenous Population Growth

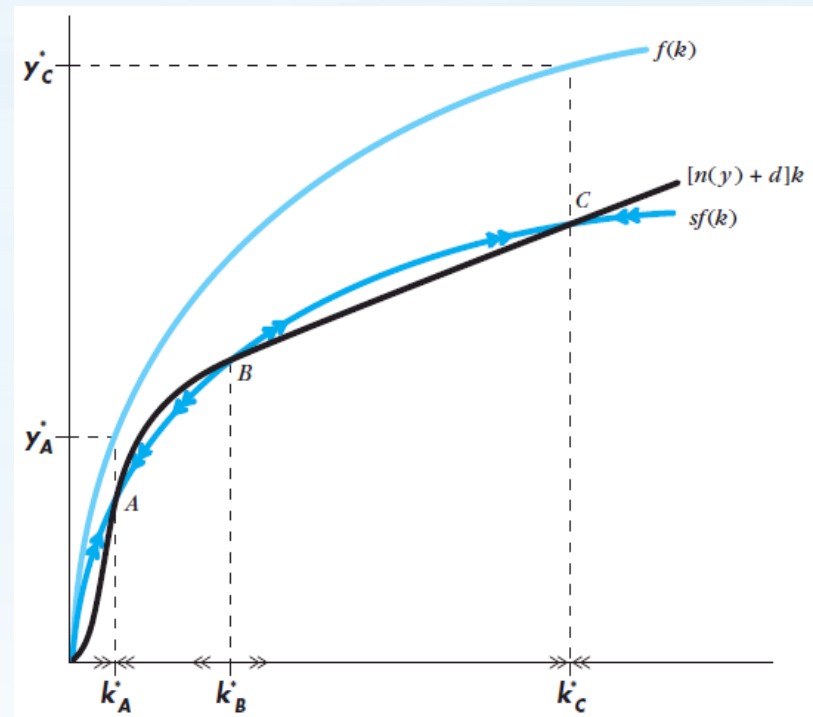
- The investment requirement line crosses the savings curve at points A, B, and C
 - Point A is a poverty trap with high population growth and low incomes
 - Point C has low population growth at high incomes
 - Points A and C are stable equilibriums because the economy moves towards these points
 - Point B is an unstable equilibrium since the economy moves away from it



Solow Model with Endogenous Population Growth

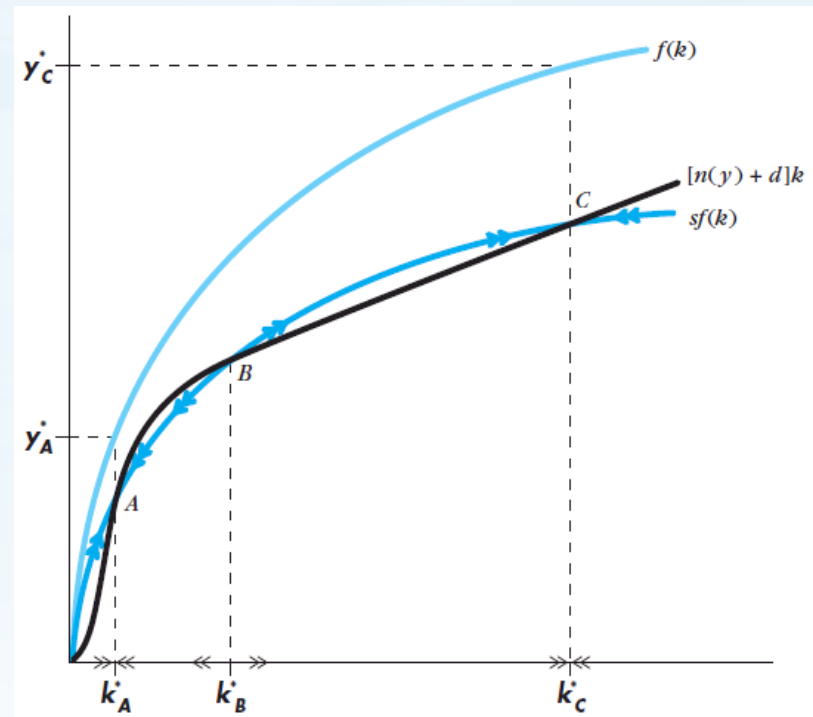
- How can an economy escape from the low-level equilibrium? There are two possibilities.

- If a country can put on a “big push” that increases income past point B, the economy will continue unaided to the high-level at point C
- A nation can effectively eliminate the low-level trap by moving the savings curve up or the investment requirement line down so that they no longer touch at points A or B
 - raising productivity or increasing the savings rate raises the savings line
 - population control policies lower the investment requirement line



Solow Model with Endogenous Population Growth

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Truly Poor Countries

- Ghana, and many other countries, experienced very little growth in recent years
 - Income is so low that most of the population lives on the border of subsistence
 - Can the Solow growth model explain these countries' experiences? YES
 - Savings in Ghana is quite low (9.3% of GDP vs. 34.3% and 19.4% of GDP in Japan and the US respectively)
 - Population growth is very high in Ghana and other poor countries relative to the US and Japan
- *The effect of low savings rates and high population growth rates are as predicted by the Solow growth model: low levels of income and capital per capita*