

**2022-23 Second Semester  
MATH1083 Calculus II (1002)**

Assignment 4

Due Date: 11:30am 15/Mar/2021(Wed).

- Write down your **Chinese name** and **student number**. Write neatly on **A4-sized** paper and **show your steps**.
- **Late submissions or answers without details will not be graded.**

1. [Taylor Remainder Theorem]

- (a) Find the first degree Taylor polynomial  $p_3(x)$  of function  $f(x) = x^{1/3}$  about  $a = 27$  radius of convergence and interval of convergence of the power series.
- (b) Find the value of  $\sqrt[3]{28}$  using  $p_1(x)$
- (c) Estimate the error  $R_1(x)$

2. Evaluate the limit using **Taylor series**

$$\lim_{x \rightarrow 0} \frac{e^{x^2} - x^2 - 1}{x^4}$$

3. Expand  $1/\sqrt[4]{1+x}$  as a power series and estimate  $1/\sqrt[4]{1.1}$  to **three decimal places**.