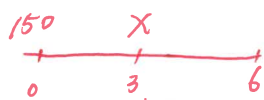


$$1. x e^{\int_3^x \delta(t) dt} + 150 e^{\int_0^3 \delta(t) dt} - (x + 150 e^{\int_0^3 \delta(t) dt}) = x$$



$$x e^{\frac{6-3^2}{200}} + 150 e^{\frac{6^2}{200}} - x - 150 e^{\frac{3^2}{200}} = x$$

$$1.14x + 179.58 - x - 156.90 = x$$

$$x \approx 26.37$$

$$2. \text{ Kelly: } a(t) = 1 + 0.04t$$

$$\text{Tara: } a'(t) = e^{\int_0^t \frac{1}{r+k} dt} = \frac{t+k}{k}$$

$$X[a(8) - a(4)] = X[a'(8) - a'(4)]$$

$$(1 + 0.04 \times 8) - (1 + 0.04 \times 4) = \frac{8+k}{k} - \frac{4+k}{k}$$

$$k = 25$$

$$3. 200(1+r)^3 e^{\int_3^6 \delta(t) dt} = 400$$

$$1 = \sqrt[3]{\frac{8}{7}} - 1 \approx 0.0455$$

$$4. e^{5r_{ef}} = e^{\int_0^5 \frac{2}{t+1} dt}$$

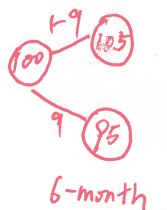
$$r_{ef} = \frac{\ln 36}{5} \approx 0.7167$$

5.



$$\text{(annual)} \\ r = 8\% \quad k = 78 \text{ (call)}$$

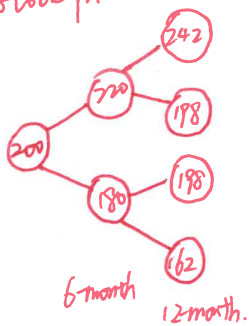
$$V_0 = e^{-rt} \left(\frac{S_+ - S_0 e^{rt}}{S_+ - S_-} V_- + \left(1 - \frac{S_+ - S_0 e^{rt}}{S_+ - S_-} \right) V_+ \right) \\ = e^{-8\% \cdot \frac{1}{2}} \left(\frac{84 - 80 e^{8\% \cdot \frac{1}{2}}}{84 - 76} \times 0 + \left(1 - \frac{84 - 80 e^{8\% \cdot \frac{1}{2}}}{84 - 76} \right) \times 6 \right) \\ \approx 3.39$$



$$\text{(annual continuous)} \\ r = 10\% \quad k = 100 \text{ (put)}$$

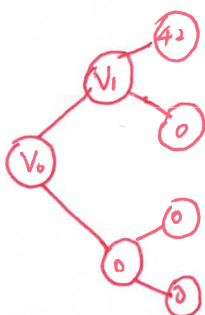
$$V_0 = e^{-rt} \left(\frac{S_+ - S_0 e^{rt}}{S_+ - S_-} V_- + \left(1 - \frac{S_+ - S_0 e^{rt}}{S_+ - S_-} \right) V_+ \right) \\ = e^{-10\% \cdot \frac{1}{2}} \left(\frac{105 - 100 e^{10\% \cdot \frac{1}{2}}}{105 - 95} \times 5 + \left(1 - \frac{105 - 100 e^{10\% \cdot \frac{1}{2}}}{105 - 95} \right) \times 0 \right) \\ x = 0.06 \quad \text{no value.}$$

7. Stock price.



$r = 8\%$ (annual continuous).

$K = 200$ (call)



$$V_1 = e^{-\frac{5\%}{2} \times \frac{1}{2}} \left(\frac{242 - 220e^{5\% \times \frac{1}{2}}}{242 - 198} \times 0 + \left(1 - \frac{242 - 220e^{5\% \times \frac{1}{2}}}{242 - 198} \right) \times 42 \right) \approx 25.81$$

$$V_0 = e^{-\frac{5\%}{2} \times \frac{1}{2}} \left(\frac{220 - 200e^{5\% \times \frac{1}{2}}}{220 - 180} \times 25.81 + \left(1 - \frac{220 - 200e^{5\% \times \frac{1}{2}}}{220 - 180} \right) \times 0 \right) \approx 15.86$$