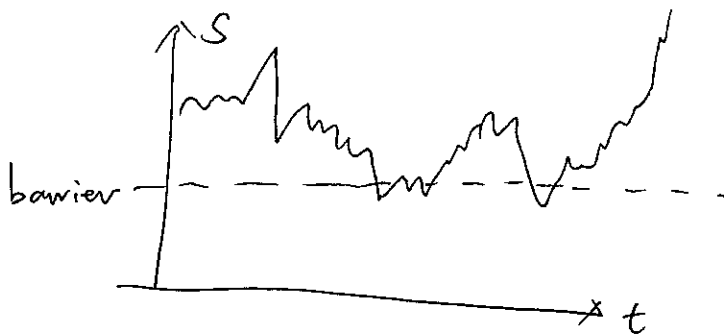


2017.3.7.

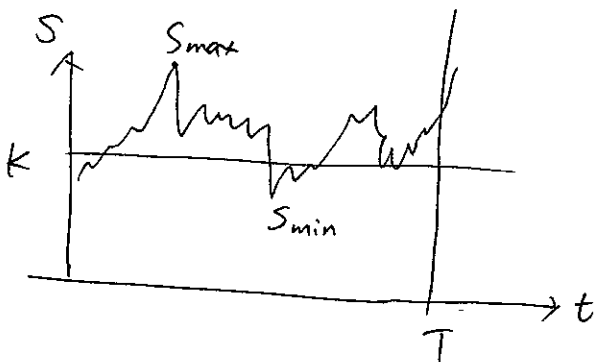
## ⑥ Parisian options:

A parisian option is a barrier option where the barrier option applies only once the price of the underlying instrument has spent at least a given period of time on the wrong side of the barrier.



## ⑦ Lookback option:

Lookback option has payoff that depends on the maximum or minimum value of the stock



Lookback rate call option

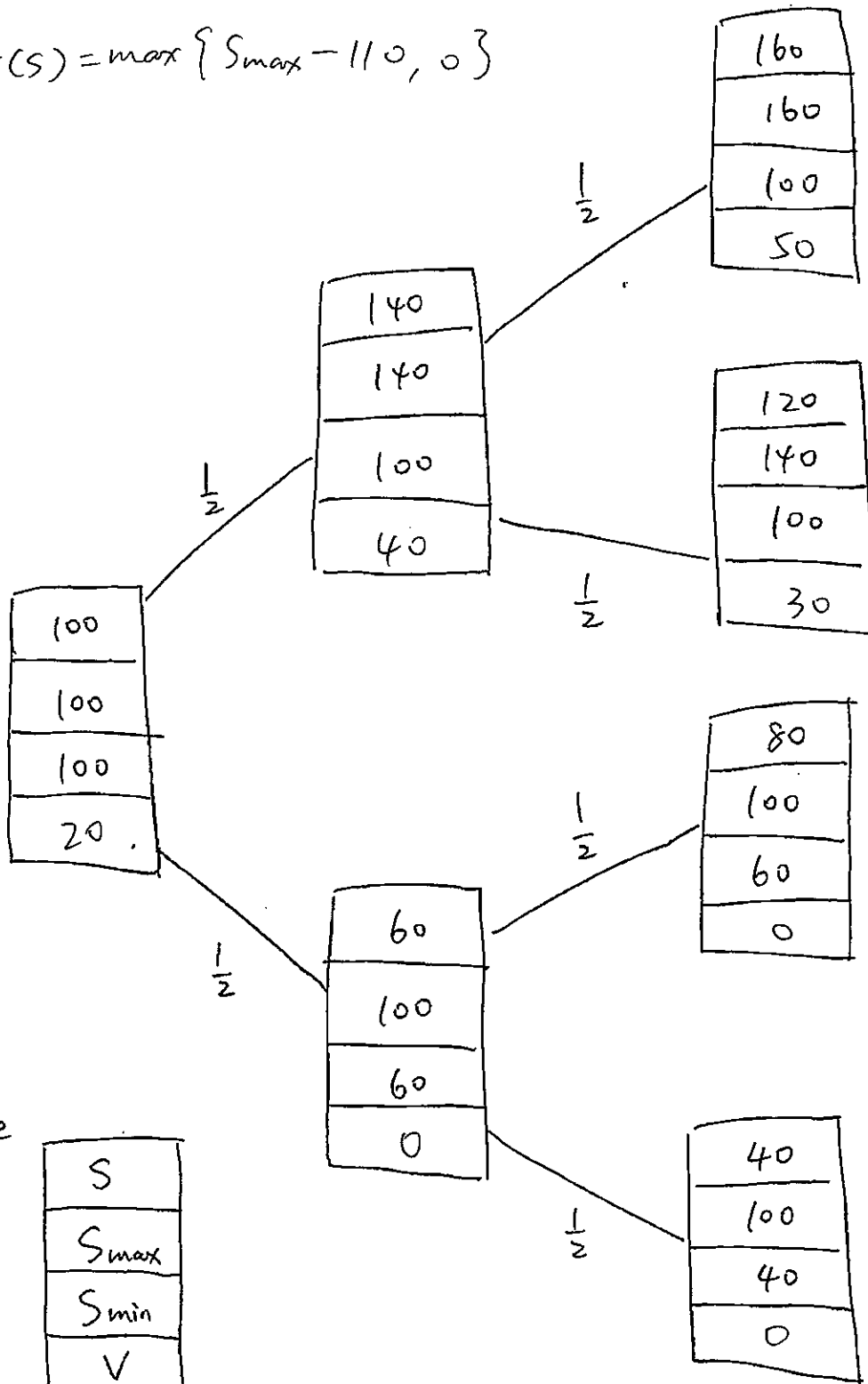
$$F(S, S_{\max}, K) = \max\{S_{\max} - K, 0\}$$

$$F(S, S_{\min}, K) = \max\{S_{\min} - K, 0\}$$

Lookback rate Call

$$K = 110$$

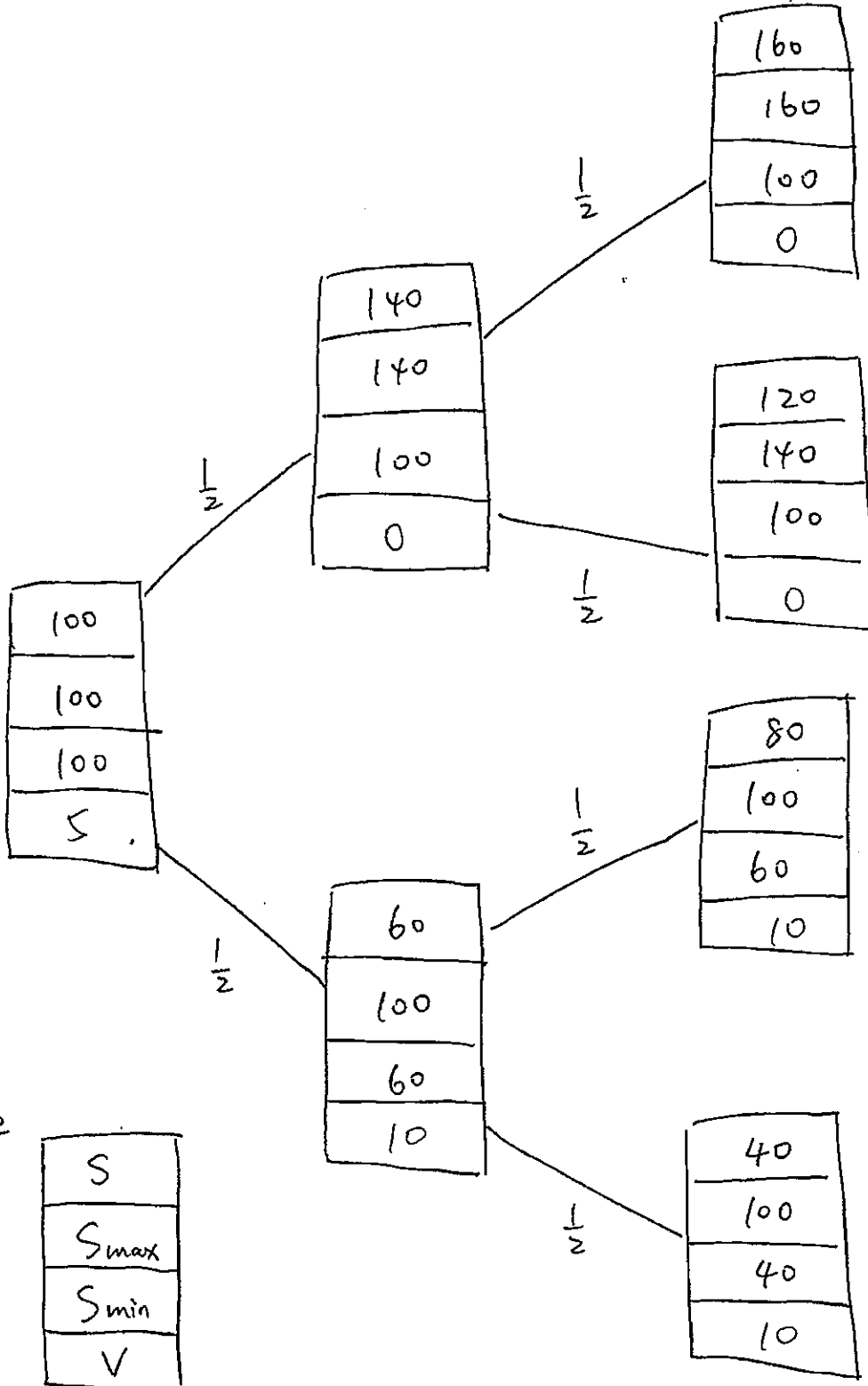
$$F(S) = \max \{ S_{\max} - 110, 0 \}$$



The price at the node is not only a function of  $t$  and  $S$ , but also a function of  $S_{\max}$ .

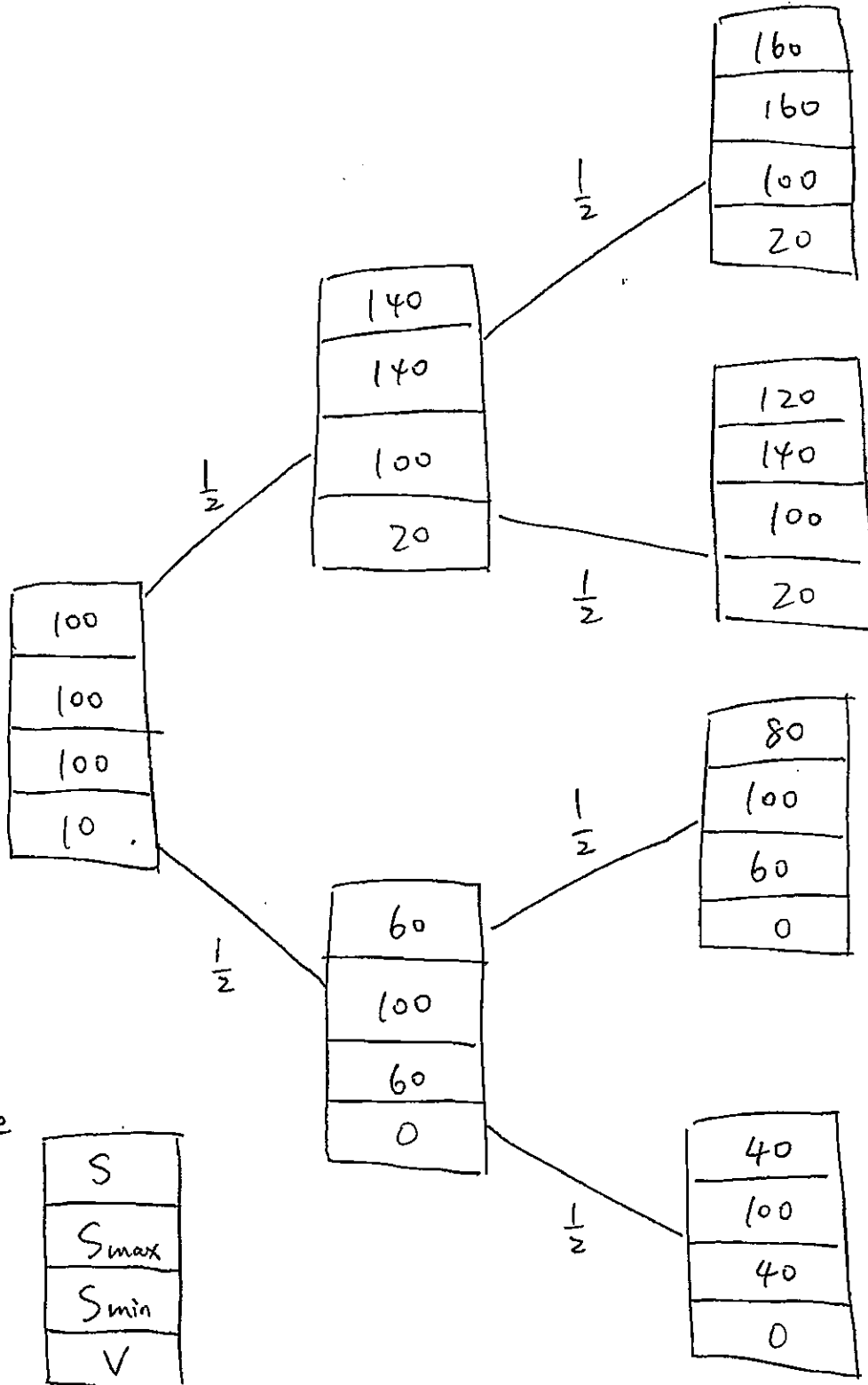
Lookback rate put option

$$F(s) = \max \{110 - S_{\max}, 0\}$$



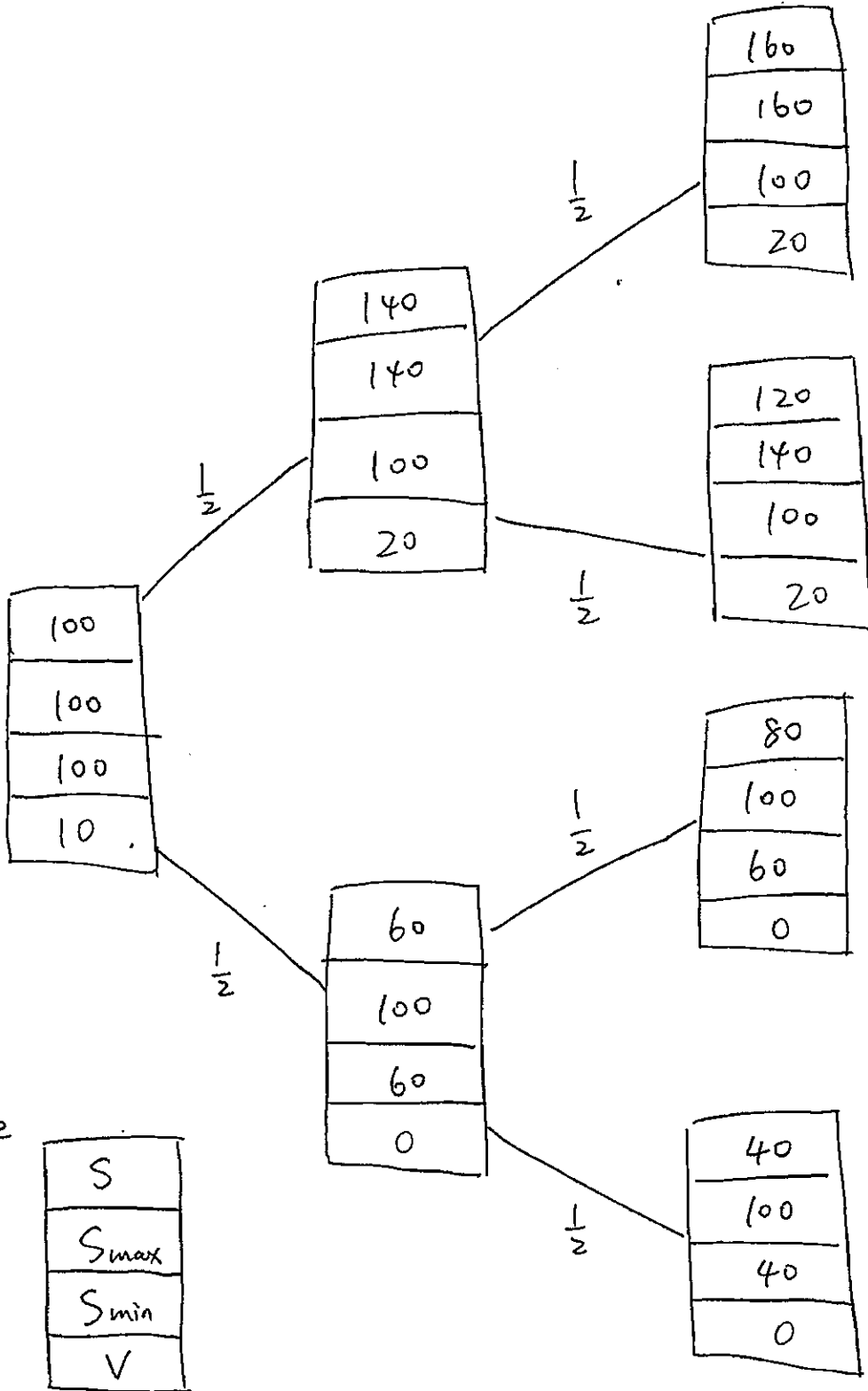
Look back rate call with  $S_{min}$

$$F(S) = \max \{ S_{min} - 80, 0 \}$$



Lookback rate put with  $S_{\min}$

$$F(S) = \max \{ S_{\min} - 80, 0 \}$$

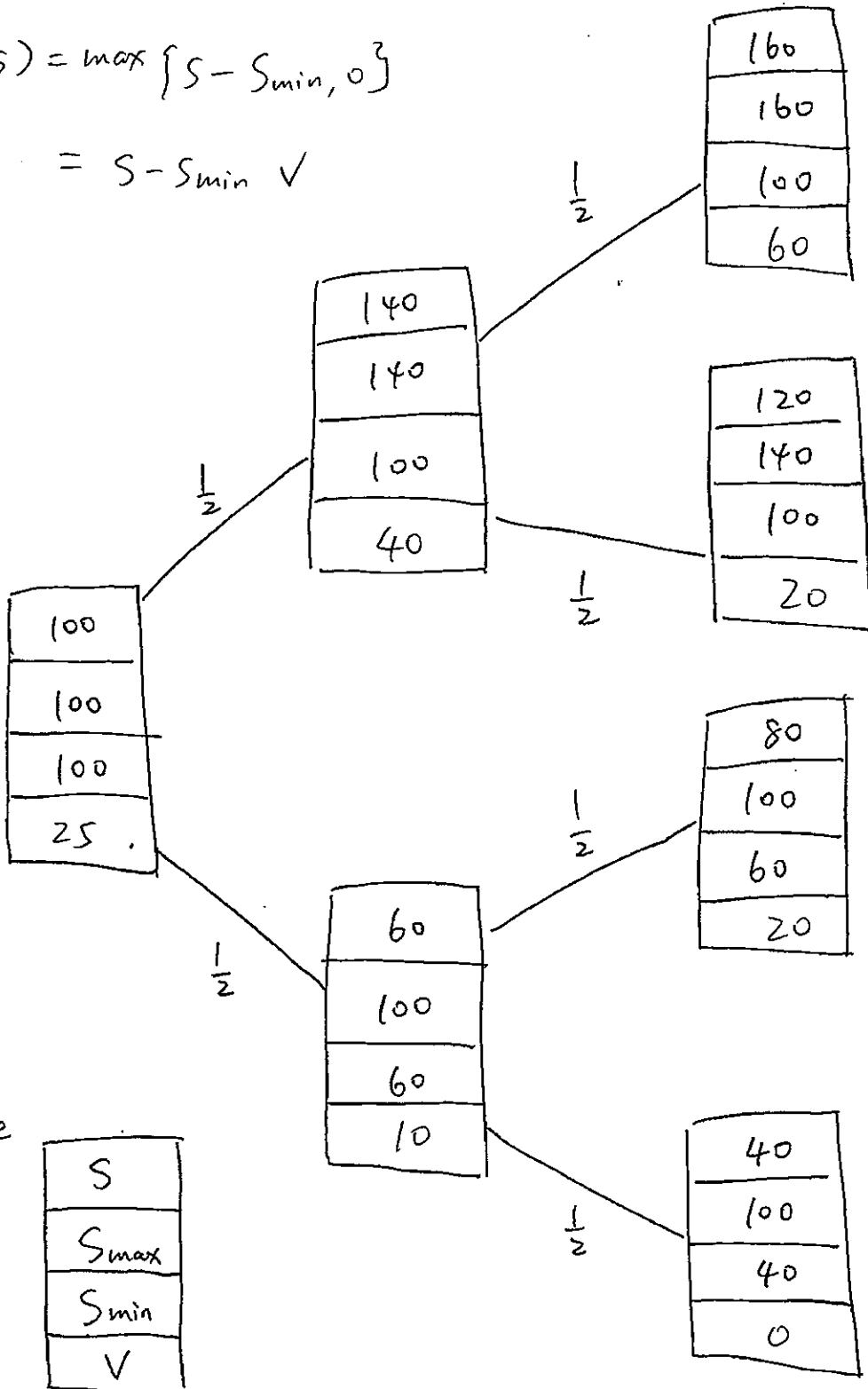


# Lookback strike call

if  $F(S) = \max \{ \underbrace{S - S_{\max}}_{\leq 0}, 0 \} = 0$ , no meaning.

$$F(S) = \max \{ S - S_{\min}, 0 \}$$

$$= S - S_{\min} \checkmark$$

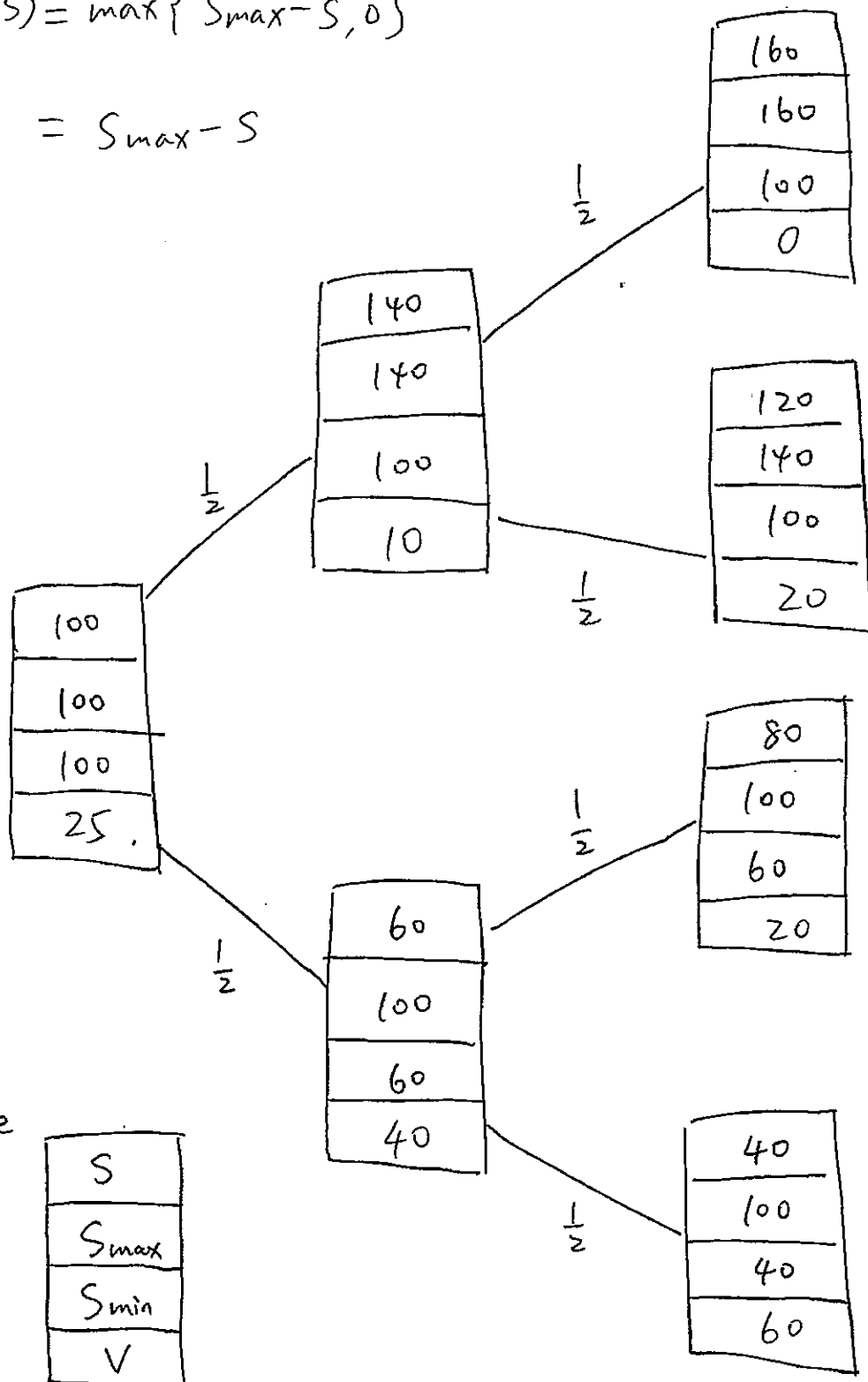


Lookback strike put

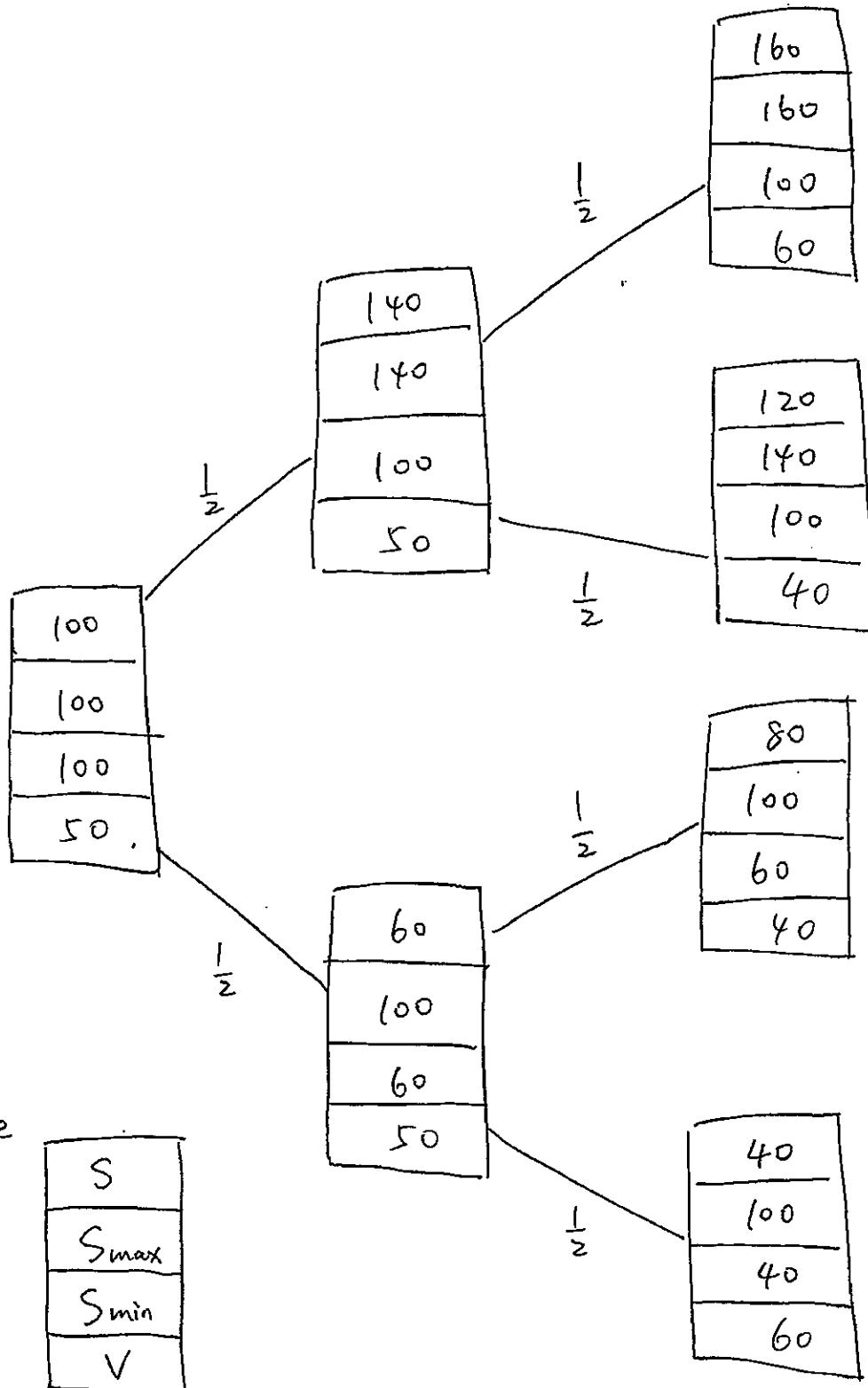
If  $F(S) = \max\{S_{\min} - S, 0\} = 0$ , no meaning.

$$F(S) = \max\{S_{\max} - S, 0\}$$

$$= S_{\max} - S$$



$$F(S) = S_{\max} - S_{\min}$$

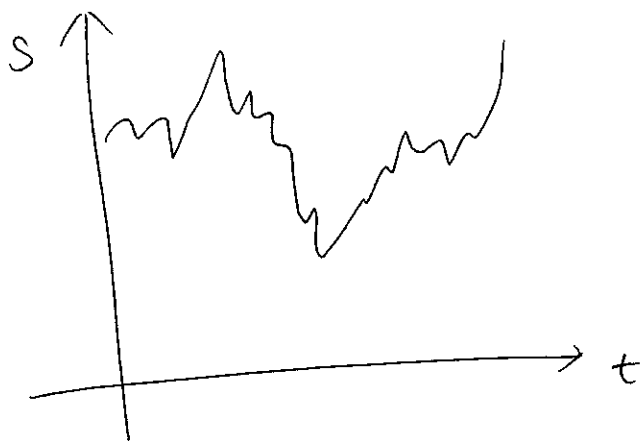


Lookback option is path-dependant option.



## ⑧ Asian option

Asian option are options with payoff depending on the average value of the stock price. (Starts in Hong Kong, Japan)



$$\bar{S}_T = \frac{1}{T} \int_0^T S(t) dt$$

$$\begin{aligned}\bar{S}_t &= \frac{1}{t} \int_0^t S(t') dt' \\ &= \frac{1}{k+1} \sum_{i=0}^k S_i\end{aligned}$$

Average rate call

$$F(S) = \max \{ \bar{S} - K, 0 \}$$

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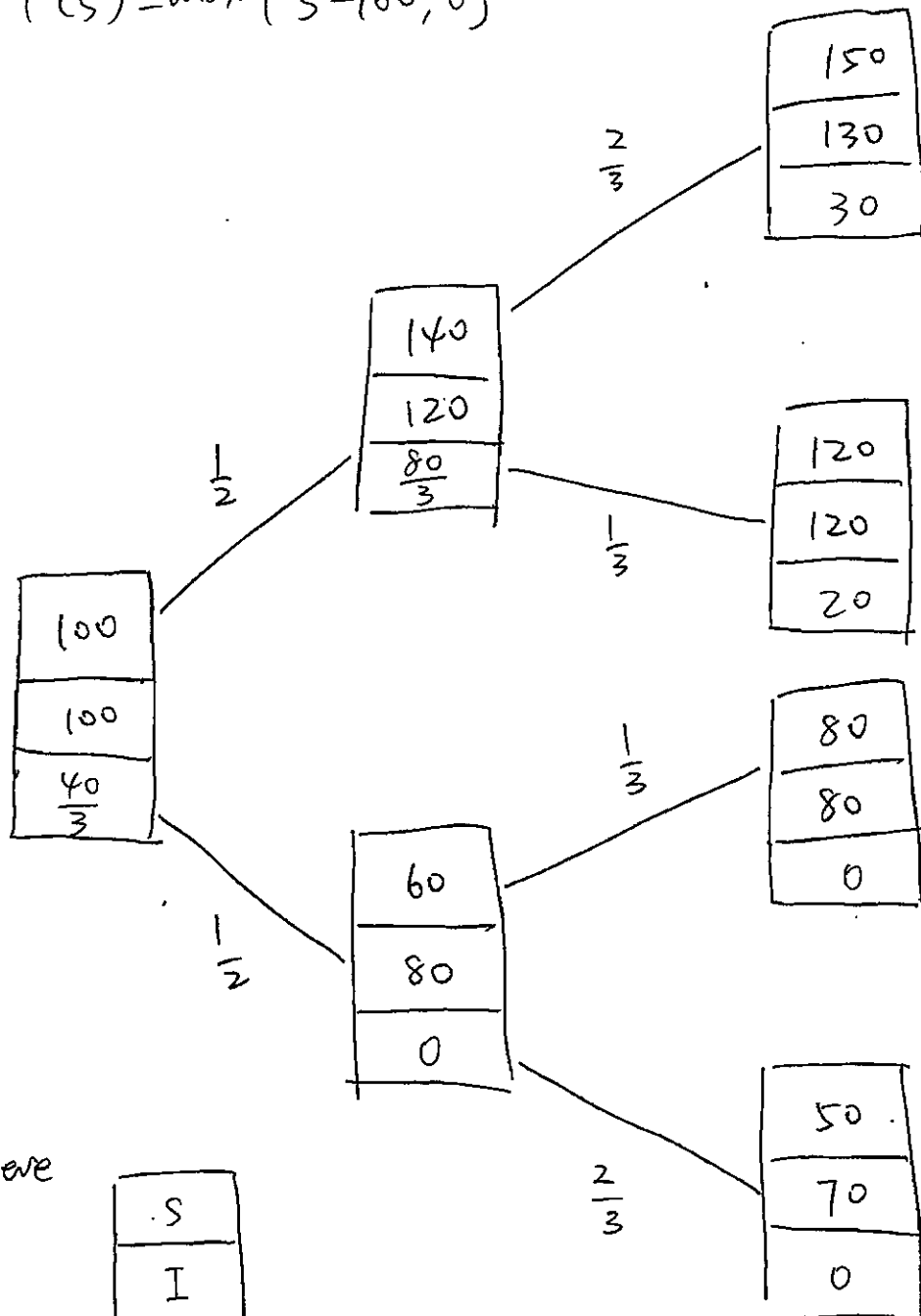
Geometric average:

$$\bar{S}_{\text{geo}} = e^{\frac{1}{k+1} \sum_{i=0}^k \ln S_i} = (S_0 S_1 \cdots S_k)^{\frac{1}{k+1}}$$

Average rate call

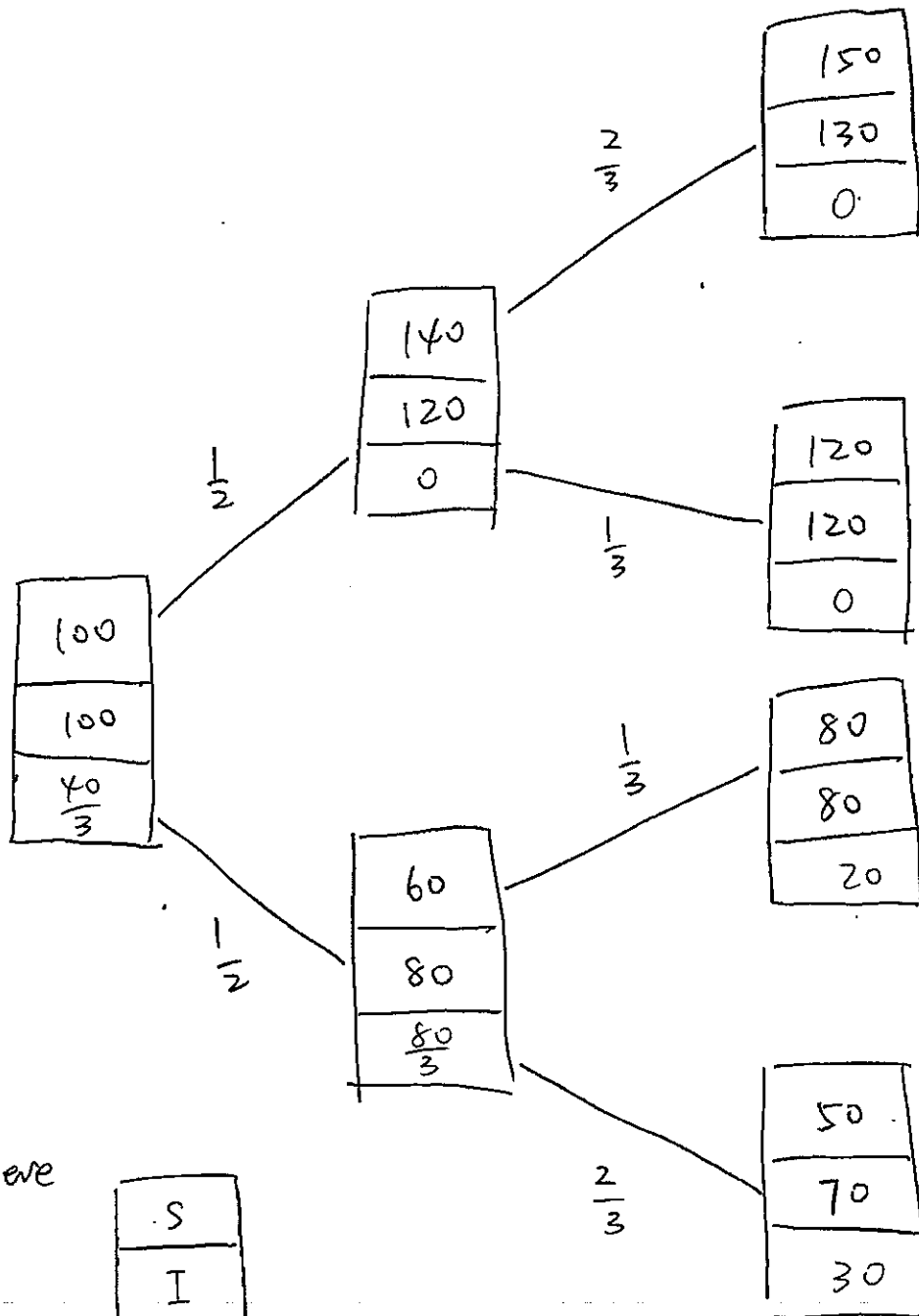
$$K=100$$

$$F(S) = \max \{ \bar{S} - 100, 0 \}$$



Average rate put

$$F(S) = \max\{100 - \bar{S}, 0\}$$

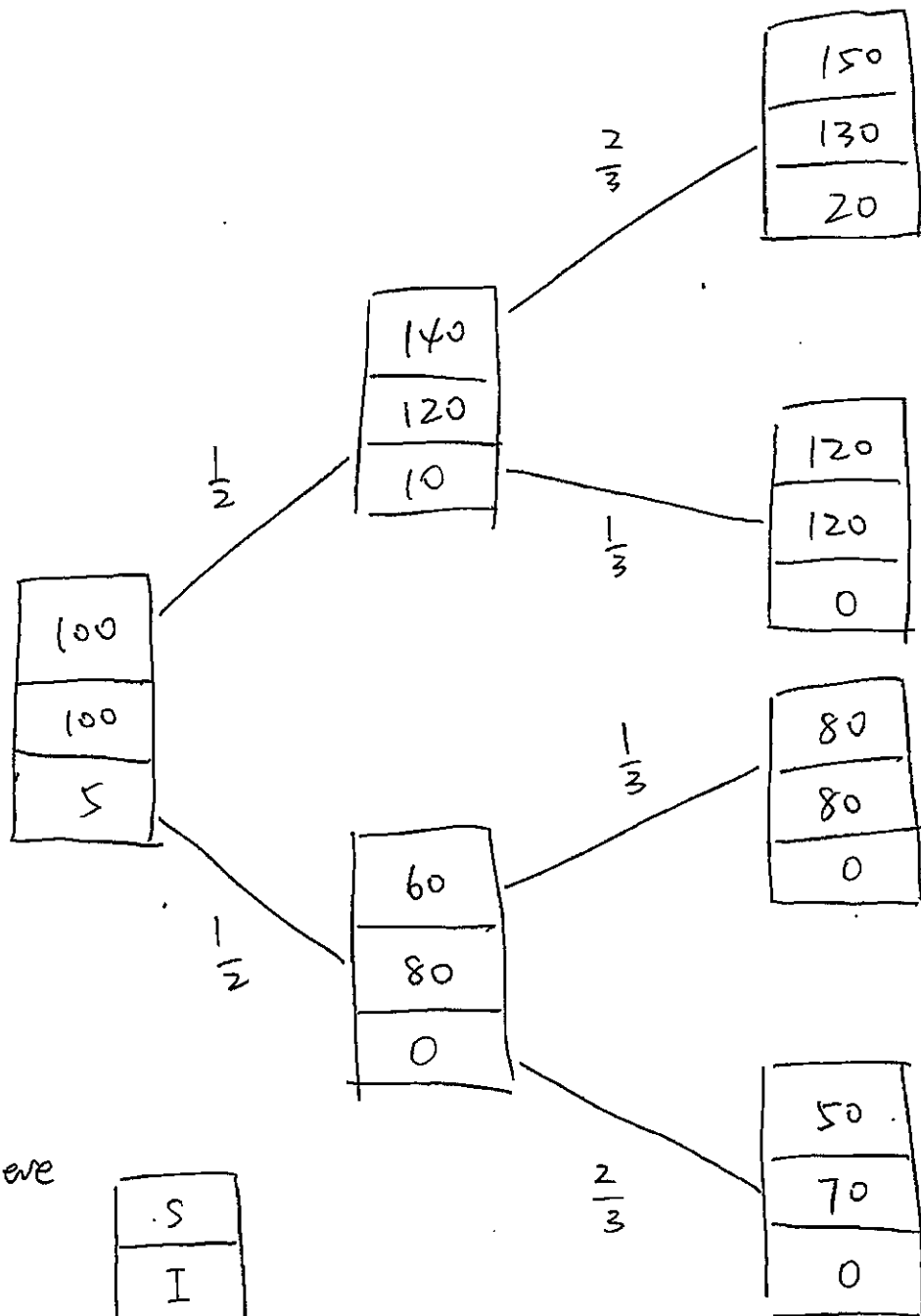


where

S
I
V

Average strike call

$$F(S) = \max\{S - \bar{S}, 0\}$$

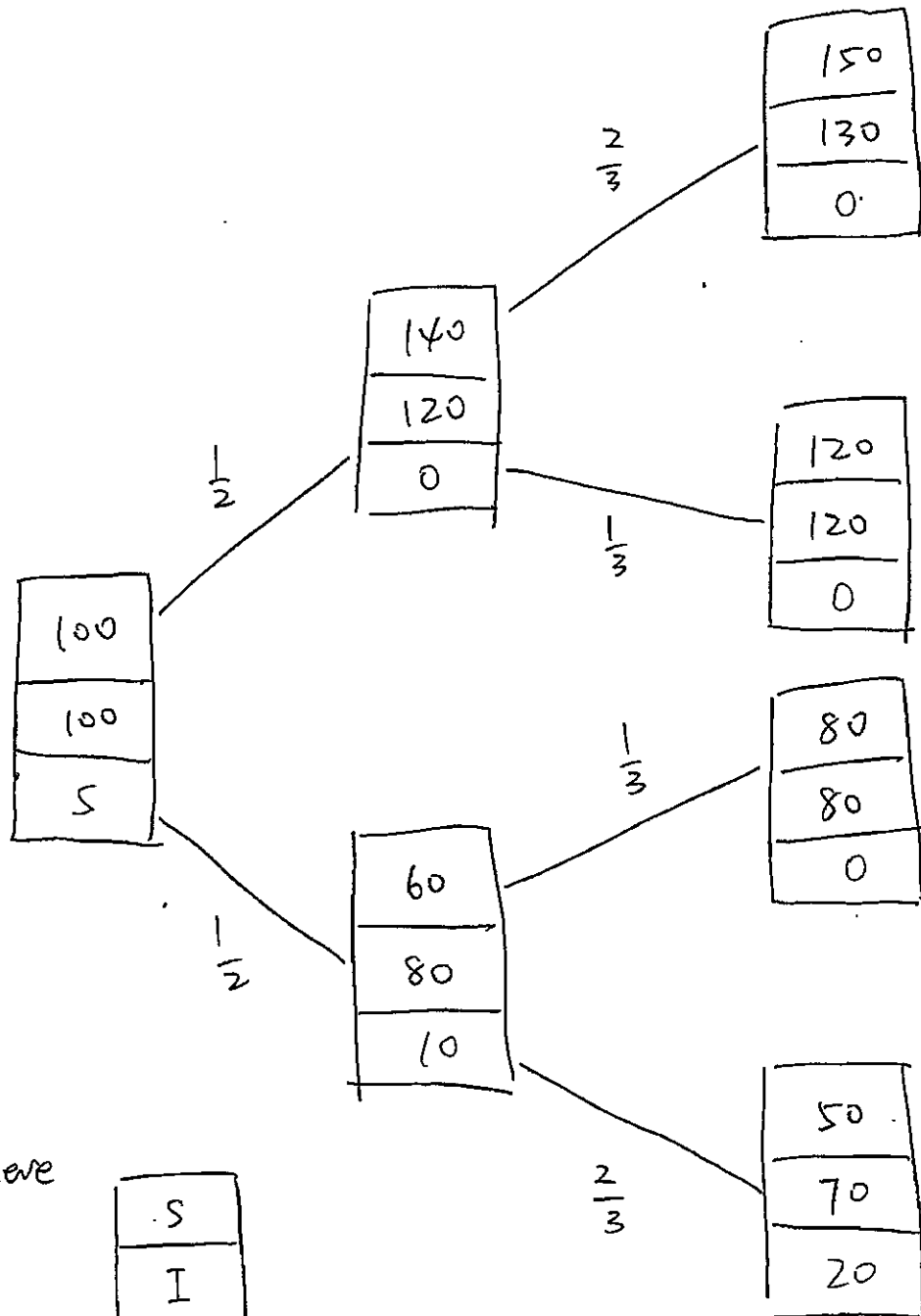


where

S
I
V

Average strike put

$$F(S) = \max\{\bar{S} - S, 0\}$$



where

S
I
V

⑨ Forward start option :

Forward start option has strike price determined by the stock price some specified time later on.