

Sisteme cu membrane (2)

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Sumar

- kernel P sisteme
- Medii de simulare pentru sistemele cu membrane
- kP-Lingua si kPWorkbench
- Simulare si verificare folosind kPWorkbench
- Exemple in kP-Lingua si simulare in kPWorkbench

Sisteme cu Membrane

Un model de calcul inspirat (bazat) pe structura si functionarea celulei vii (**Membrane or P systems**)

Trei caracteristici esentiale ale Sistemelor cu Membrane:

- *structura* (ierarhica, dar nu numai) de **membrane** delimitand regiuni/compartimente (*arbore*)
- *multiseturi de obiecte* si
- *seturi finite de reguli* asociate compartimentelor

Un P sistem **calculeaza**, evoluand de la o configuratie (stare) la alta, aplicand regulile, in compartimente, utilizand strategia **paralelismului maxim**

Regulile pot rescrie sau muta obiecte dintr-un compartiment in altul, dar pot modifica structura (introducand/stergand compartimente)

Sistem cu Membrane – Definitie

$P = (O, \mu, w_1, \dots, w_n, R_1, \dots, R_n, i_0)$ - P system

where

O – an **alphabet** (finite set)

μ – a **membrane structure** with n membranes (regions)

w_1, \dots, w_n – **multisets** over O ; w_i – initial values

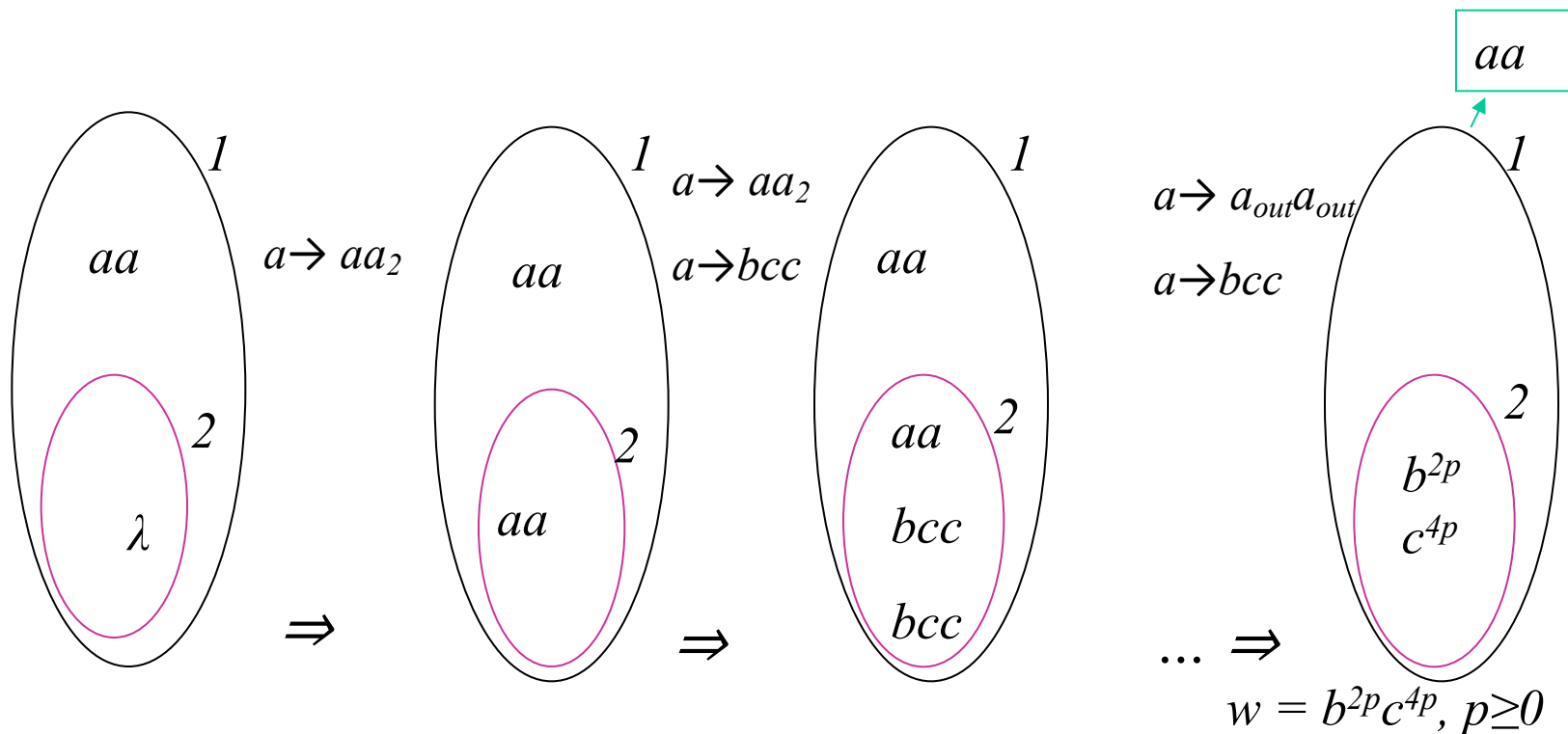
R_1, \dots, R_n – **sets of rules**

i_0 – the **output cell (or environment)**

R_i – **evolution and communication rules**: $v \rightarrow w$; v, w – strings over O + some indications of target regions in w

Exemplu – Doua compartimente

$$P = (\{a,b,c\}, [{}_1[{}_2]_2]_1, aa, \lambda, \{a \rightarrow aa_2, aa \rightarrow a_{out}a_{out}\}, \{a \rightarrow bcc\}, 2)$$



Caracteristici:

structura ierarhica (arbore); reguli de rescriere si comunicare; nedeterminism; paralelism maxim. Rezultatul: multiset ($b: 2p$ & $c: 4p$)

Kernel P System – Introducere Informala

- Structura dinamica, sub forma de graf
- Utilizeaza multiseturi de obiecte
- Regulile pot avea garzi (conditii booleene)
 - rescriere si comunicare
 - structurale (ex. diviziune celulara/de membrane (compartimente); creare/stergere legaturi intre compartimente)
- Fiecare compartiment are un tip din care deriva, iar tipul compartimentului defineste setul de reguli. Fiecare instanta are propriul multiset initial.

Definition (Kernel P systems)

A **kP system** of degree n is a tuple $k\Pi = (A, \mu, C_1, \dots, C_n, i_0)$, where

- A is a finite set of elements called objects;
- μ defines the membrane structure, which is a graph, (V, L) , where V is a set of vertices representing components (compartments), and L is a set of edges, i. e., links between components;
- $C_i = (t_i, w_{i,0})$, $1 \leq i \leq n$, is a compartment of the system consisting of a *compartment type*, t_i , from a set T and an initial multiset, $w_{i,0}$ over A ; the type $t_i = (R_i, \delta_i)$ consists of a set of evolution rules, R_i , and an execution strategy, δ_i ;
- i_0 is the output compartment where the result is obtained.

Rule types

Within the kP systems framework, the following types of evolution rules have been considered so far:

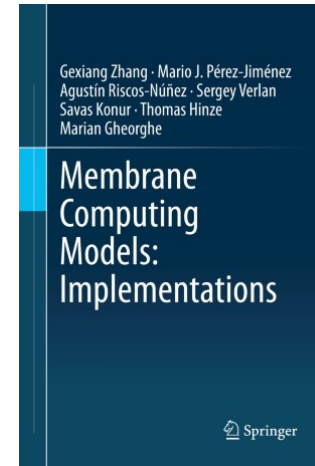
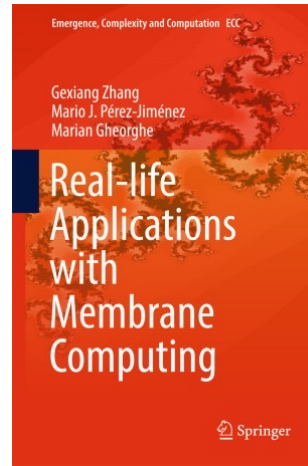
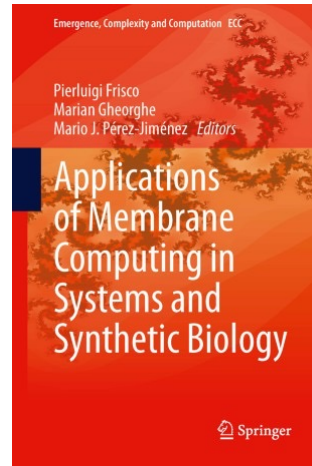
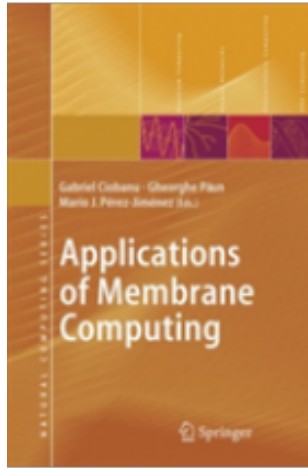
- *rewriting and communication* rules
- *structure changing* rules: membrane division, membrane dissolution, link creation and link destruction rules.

Complex *guards* can be incorporated, using multisets over A with relational and Boolean operators.

Execution strategies: for each compartment type / block

- *sequential*
- *choice*
- *arbitrary*
- *maximal parallel*

Aplicatii ale P sistemelor



- Diferite arii si domenii
- Implica specificare (modelare) si simulare, dar si analiza (verificare), testare

Medii de Specificare/Simulare

- Generale

1. P-Lingua, acopera un set de modele de tipul sisteme de membrane: <http://www.cs.us.es/~ignacio/curso-plingua/doc/paper2.pdf>
2. MeCoSim – mediu de dezvoltare atasat la P-Lingua: <http://www.p-lingua.org/mecosim/doc/>

- Specifice

1. Infobiotics – aplicatii in biologie: <https://infobiotics.org/>
2. Meta PLab – aplicatii scrise in metabolic P systems: <http://mplab.sci.univr.it/index.html>
3. kPWorkbench - kP sisteme specificare, simulare, verificare: <https://github.com/Kernel-P-Systems/kPWorkbench>

P-Lingua. Exemplu: transition P system.

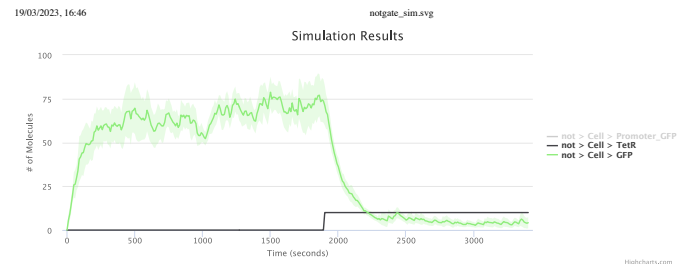
```
@model<transition>
def main()
{
  @mu = [[[[]'3 []'4]'2]'1;
  @ms(3) = a,f;

  [a --> a,bp]'3;
  [a --> bp,@d]'3;
  [f --> f*2]'3;

  [bp --> b]'2;
  [b []'4 --> b [c]'4]'2;
  [f*2 --> f]'2;
  [f --> a,@d]'2;
}
```

IBL. Exemplul – NOT Gate.

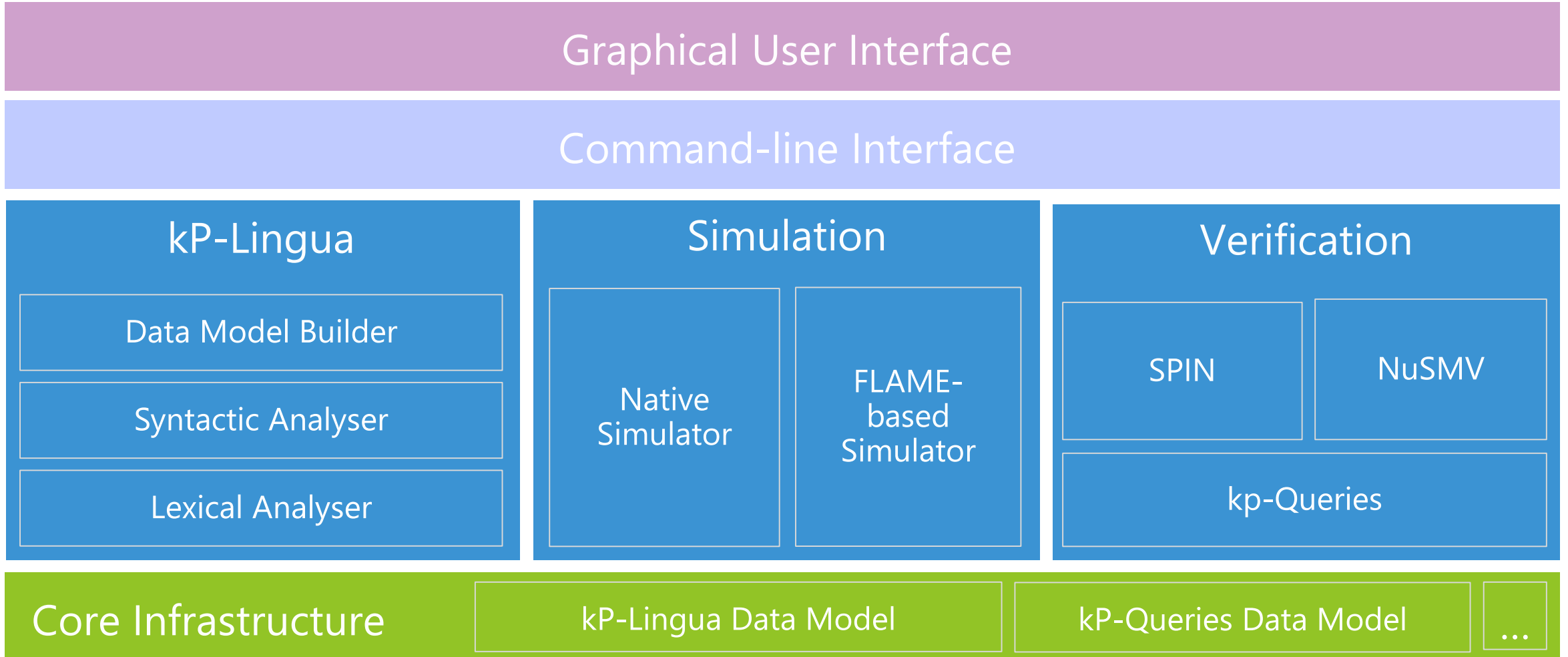
```
define Cell typeof CELL() {  
  
    // Species  
    Promoter_GFP = MOLECULE(concentration=2.0 molecules)  
    TetR = MOLECULE(concentration=0.0 molecules)  
    GFP = MOLECULE(concentration=0.0 molecules)  
  
    // Rules  
    RULE Degradation_GFP : GFP ->  
    Degradation_GFP.forwardRate = '0.0075*[GFP]'  
  
    RULE R_abstracted_production_Promoter_GFP : -> GFP + GFP + GFP + GFP + GFP + GFP + GFP + GFP + GFP + GFP  
    R_abstracted_production_Promoter_GFP.forwardRate =  
    '0.05*2.0*0.033*30.0/((1+0.033*30.0)+(0.5*[TetR])^2.0)'  
  
    EVENT [TetR = 10 molecules] WHEN [TIME >= 1900 s]  
}  
  
define not typeof REGION () {  
    CELL Cell = new Cell()  
}
```



kP-Lingua

- Limbaj pentru specificarea kP sistemelor
- Inclus in kP Workbench – specificarea modelor, simulare si verificare

KPWorkbench tool stack



kP-Lingua constructs

```
type C1 {  
  2a, 3b -> c .  
  arbitrary {  
    >= 2c & > 2b : b, c -> a .  
  }  
  choice {  
    b -> 2b .  
    < 3b : b -> 3b .  
  }  
  max {  
    a -> a, a(C2), {a, 2b}(C3) .  
  }  
  2c -> - (C2) .  
  2b -> \- (C2) .  
  = 5a : a -> [3a, 3b](C1) [3b](C2) .  
}
```

```
m1 {2x, b} (C1) .  
m2 {x} (C2) .
```

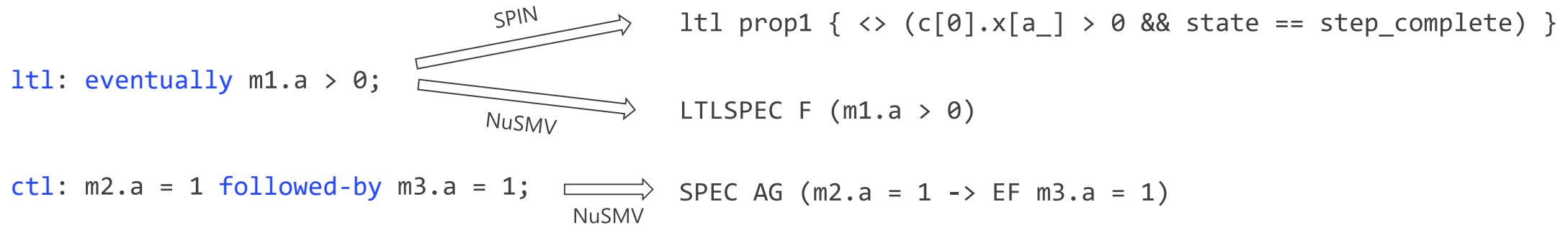
```
m1 - m2 .
```

- Compartment type definitions
- Rewriting and communication rules
- Rule guards
- Membrane division
- Link creation and destruction
- Sequential, arbitrary, choice and maximal parallelism execution strategies

- Membrane instantiations

- Link between compartments

kP-Queries



Pattern	kP-Query	LTL	CTL
Next	<code>next p</code>	$X p$	$EX p$
Existence	<code>eventually p</code>	$F p$	$EF p$
Absence	<code>never p</code>	$\neg(F p)$	$\neg(EF p)$
Universality	<code>always p</code>	$G p$	$AG p$
Recurrence	<code>infinitely-often p</code>	$G F p$	$AG EF p$
Steady-state	<code>steady-state p</code>	$F G p$	$AF AG p$
Until	<code>p until q</code>	$p U q$	$A (p U q)$
Response	<code>p followed-by q</code>	$G (p \rightarrow F q)$	$AG (p \rightarrow EF q)$
Precedence	<code>p preceded-by q</code>	$\neg(\neg p U (\neg p \wedge q))$	$\neg(E (\neg p U (\neg p \wedge q)))$

Square numbers generation

```
type main {  
  max {  
    = t: a -> {} .  
    < t: a -> a, 2b, s, i .  
    < t: a -> a, s, t, i .  
    < t: b -> b, s .  
  }  
}  
  
m {a} (main) .
```

```
/* LTL Properties */  
ltl: always m.t <= 1;  
ltl: steady-state (m.a = 0 implies m.t = 1);  
ltl: never m.s = 15;  
  
ltl: always m.s == m.i * m.i; // Invariant
```

```
/* CTL Properties */  
ctl: eventually m.a = 0;  
ctl: eventually m.t = 1;  
ctl: m.a = 0 preceded-by m.t = 1;  
ctl: m.a > 0 followed-by m.a = 0;  
ctl: m.t = 1 followed-by m.a = 0;  
ctl: always m.t <= 1;  
ctl: never m.s = 15;
```

kP Sisteme. Exemplul 1.

Scaderea a doua numere intregi positive. kP sistemul are 4 componente: C_1, C_2, C_3, C_4 . Tipurile asociate sunt t_1, t_2, t_3, t_4 .
 t_1 cu regula $a \rightarrow (a, t_3)$ aplicata cf paralelismului maxim
 t_2 cu regula $a \rightarrow (b, t_3)$ aplicata cf paralelismului maxim
 t_3 cu regulile de mai jos aplicate
 $\{ab \rightarrow \varepsilon\}^T \{b \rightarrow (am, t_4)\}^C \{a \rightarrow (a, t_4), b \rightarrow (a, t_4)\}^T$; o secventa de 3 sub-executii, unde T este parallelism maxim, iar C este alegere (choice)
 t_4 este tipul vid.
Multiseturile initiale sunt n elemente a in C_1 si m elemente a in C_2 .
Restul sunt vide.
 C_1, C_2 sunt legate de C_3 care este legat de C_4
Ideea modelului. Cele n elemente a in C_1 si m elemente a in C_2 trec in C_3 sub forma de a si b . In C_3 se face diferenta, cu semn, care trece in C_4

kP Lingua. Exemplul 1.

```
type t1 {  
  max {  
    a -> a (t3).  
  }  
}
```

```
type t2 {  
  max {  
    a -> b (t3).  
  }  
}
```

```
type t3 {  
  max {  
    a, b -> {}.  
  }  
  choice {  
    b -> {a, m} (t4).  
  }  
  max {  
    a -> a (t4).  
    b -> a (t4).  
  }  
}
```

```
type t4 {  
}
```

C1 {3a} (t1) – C3 {} (t3).
C2 {5a} (t2) – C3.
C3 - {} (t4).

Concluzii

- Kernel P sisteme
- kP-Lingua si kPWorkbench
- Exemple
- **Proiecte** bazate pe kP sisteme (modelare, simulare)
- **Directii de cercetare** (master, doctorat): simulare eficienta (arhitecturi paralele), verificare, testare