Extractive Text Summarization Using Word Similarity-Based Spectral Clustering

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Abstract

Extractive Text Summarization is the process of picking the best parts of a larger text without losing any key information. This is really necessary in this day and age to get concise information faster due to digital information overflow. Previous attempts at extractive text summarization, specially in Bengali, either relied on TF-IDF or used naive similarity measures both of these suffers expressing semantic relationship correctly. The objective of this paper is to develop an extractive text summarization method for Bengali language, that uses the latest NLP techniques and extended to other low resource languages. We developed a word Similarity-based Spectral Clustering (WSbSC) method for Bengali extractive text summarization. It extracts key sentences by grouping semantically similar sentences into clusters with a novel sentence similarity calculating algorithm. We took the geometric means of individual Gaussian similarity values using word embedding vectors to get the similarity between two sentences. Then, used TF-IDF ranking to pick the best sentence from each cluster. This method is tested on four datasets, and it outperformed other recent models by 43.2% on average ROUGE scores (ranging from 2.5% to 95.4%). The method is also experimented on Turkish, Marathi and Hindi language and found that the performance on those languages often exceeded the performance of Bengali. In addition, a new high quality dataset is provided for text summarization evaluation. We, believe this research is a crucial addition to Bengali Natural Language Processing, that can easily be extended into other languages.

1 Introduction

Text Summarization is the process of shortening a larger text without losing any key information to increase the readability and save time for the reader. But manually summarizing very large texts is a counter-productive task due to it being more time consuming and tedious. So, developing an Automatic Text Summarization (ATS) method that can summarize larger texts reliably is really necessary to alleviate this manual labour [32]. Using ATS to summarize textual data is thus becoming very important in various fields such as news articles, legal documents, health reports, research papers, social media contents etc. ATS helps the reader to quickly and efficiently get the essential information without needing to read through large amounts of texts [9]. So, ATS is being utilized in various fields, from automatic news summarization, content filtering, and recommendation systems to assisting legal professionals in going through long documents. And researchers in reviewing academic papers by condensing vast amount of informations. It can also play a critical role in personal assistants and chatbots, providing condensed information to users quickly and efficiently [30].

There are two main types of ATS: extractive and abstractive [30]. Extractive summarization, which is the focus of this paper, works by selecting a subset from the source document, maintaining the original wording and sentence structure [23]. In contrast, abstractive summarization involves synthesising new text that reflects information from the input document but does not

copy from it, similar to how a human summarizes a text [22]. Both of the method has their own advantage. The abstractive summarization can simulate the human language pattern very well thus increasing the natural flow and readability of the summary. But the extractive method requires much less computation than the abstractive method while also containing more key informations from the input [14].

The key approach to extractive summarization is implementing a sentence selection method to classify which sentences will belong in the summary. For this purpose, previously various simplistic ranking based methods were used to rank the sentences and identify the best sentences as the summary. These ranking methods used indexing [4], statistical [8] or Term Frequency-Inverse Document Frequency (TF-IDF) [6, 29, 28] based techniques to score the sentences and select the best scoring ones. But these methods fail to capture the semantic relationships between sentences of the input due to being simplistic in nature. To capture the semantic relationships between sentences, graph based extractive methods are effective due to the using of sentence similarity graph in their workflow [9]. Graph based methods represent the sentences as nodes of a graph, and the semantic similarity between two sentences as the edge between the nodes [23]. Popular graph based algorithms like LexRank [10] and TextRank [20] build graphs based on cosine similarity of the bag-of-word vectors. LexRank uses PageRank [24] method to score the sentences from the graph while TextRank uses random walk to determine which sentences are the most important to be in the summary. Graph-based methods like TextRank and LexRank offer a robust way to capture sentence importance and relationship, ensuring that the extracted summary covers the key information while minimizing redundancy [9].

Clustering-based approaches are a subset of graph-based approach to extractive text summarization. Here, sentences are grouped into clusters based on their semantic similarity to divide the document into topics, and one representative sentence from each cluster is chosen to form the summary [21]. Clustering reduces redundancy by ensuring that similar sentences are grouped together and only the most representative sentence is selected. This method is effective in summarization of documents with multiple topics or subtopics by picking sentences from each topic. An example of this method can be seen with COSUM [2] where the summarization is achieved using k-means clustering on the sentences and picking the most salient sentence from each cluster to compile in the final summary.

Despite the advancements of ATS in other languages, it remains an under-researched topic for Bengali due to Bengali being a low-resource language. Early attempts at Bengali text summarization relied on traditional methods like TF-IDF scoring to select the best scoring sentences to form the summary [1, 6, 28, 29]. These TF-IDF based approaches, while simple, faced challenges in capturing the true meaning of sentences. This is because TF-IDF based methods treats words as isolated terms resulting in synonyms of words being regarded as different terms [30]. To solve this problem, graph-based methods were introduced in Bengali to improve summarization quality by incorporating sentence similarity but they were still limited by the quality of word embeddings used for the Bengali language. With the advent of word embedding models like FastText [13], it became possible to represent words in a vector space model, thus enabling more accurate sentence similarity calculations. However, existing models that use word embeddings, such as Sentence Average Similarity-based Spectral Clustering (SASbSC) method [25], encountered issues with sentence-similarity calculation when averaging word vectors to represent the meaning of a sentence with a vector. This method failed in most similarity calculation cases because words in a sentence are complementary to each other rather than being similar, leading to inaccurate sentence representations after averaging these different word vectors. As a result, word-to-word relationships between sentences get lost, reducing the effectiveness of the method.

In this paper, we propose a new clustering-based text summarization approach to address the challenge of calculating sentence similarity accurately. Our method improves upon previous attempts at graph-based summarization methods [5, 25] by focusing on the individual similarity between word pairs in sentences rather than averaging word vectors. We showed that the use of this novel approach greatly improved the accuracy, coverage and reliability of the output summaries due to having a deeper understanding of the semantic similarity between sentences. To calculate sentence similarity, we used the geometric mean of individual word similarities. The individual word similarities were achieved using Gaussian kernel function on a pair of corresponding word vector from each sentence. The word pairs are selected by finding the word vector with the smallest Euclidean distance from the target sentence. Thus, we get the semantic similarity between two sentences which can be used to build an affinity matrix to graphically represent the relationship between the sentences. This graph is clustered into groups to divide the document into distinct topics. One sentence from every cluster is selected to reduce redundancy and increase topic coverage. This method consistently outperforms other graph based text summarization methods such as BenSumm [5], LexRank [10], SASbSC [25] using four datasets on ROUGE metrics [18] as shown in Figure 4 and Table 1. This method performs well in other low resource languages also such as Hindi, Marathi and Turkish due to the language independent nature, as shown in the Table 3.

The main contributions of this paper are: (I) Proposed a new way to calculate similarity between two sentences. (II) Contributes a novel methodology for extractive text summarization for the Bengali language; by improving sentence similarity calculations and enhancing clustering techniques. (III) It offers a generalizable solution for creating less redundant and information rich summaries across languages. (IV) It provides a publicly available high quality dataset of 500 human generated summaries.

The rest of the paper is organized as follows: The Related works and Methodology are described in section 2 and 3 respectively. Section 4 illustrates the result of the performance evaluation for this work. Section 5 discusses the findings of the paper in more depth, and section 6 concludes the paper.

2 Related Work

Text summarization has been an important necessity for textual data consumption for a long time because of its ability to compress a given input text into a shortened version without losing any key information. For this reason, automating the text summarization process has been a research problem for NLP. Thus researchers attempted automatic text summarization for a long time too. At first, indexing-based text summarization methods were attempted such as the work by Baxendale [4]. This method scored sentences based on the presence of indexing terms in the sentence and picked the sentences with the best score. But this type of method failed to capture the topic and essence of the input text as we wouldn't have the topic keywords of an unforeseen input document. To solve this issue, text summarization with statistical methods like TF-IDF became very popular due to its ability to capture the important topic words of a document in an unsupervised manner. Edmundson [8] proposed a method which can focus on the central topic of a document by using the TF-IDF measure. It uses two metrics, Term Frequency (how many times a term appears in the input) and Inverse Document Frequency (inverse of how many documents the term appears in a large text corpus) to calculate the importance of a term in a document. Using TF-IDF helps to identify the words that are common in the input text but not as common in the language in general and thus classifying them as the central topic of the document. But this method is also error-prone due to its consideration of every word as a

unique isolated term without any semantic relation with other words. This leads to the method often missing some central topic if it gets divided into too many synonyms.

The problems faced by topic-based summarization methods were alleviated by graph-based extractive text summarization methods which brought new modern breakthroughs. Graph-based methods like LexRank [10] and TextRank [20] were able to capture the relationship between sentences more accurately due to use of sentence similarity graph in their process. LexRank [10] calculates the similarity graph by using cosine similarity of bag-of-words vectors between two sentences from the input. The most important sentences from the graph are classified using the PageRank [24] algorithm on the graph. PageRank ranks those sentences higher who are more similar with other high ranked sentences. Another graph-based method, TextRank [20] also uses a similar approach while building the similarity graph. In the graph for every sentence, TextRank distributed the score of that sentence to its neighbours using a random walk. This process is repeated over and over until the scores converge. Then the method picks the sentences with the best scores as the summary. Although graph-based methods such as LexRank and TextRank models are Ground-breaking compared to their time, they still lacked fundamental understanding of the words involved in a sentence due to not using any vector representation of the semantic relationship between the words involved.

To solve the problem of representing semantic relationship, a mathematical abstraction called Word Vector Embedding was conceptualized by the seminal work of Salton et al. [27]. Word Vector Embedding uses a word vector space as a mathematical abstraction of a lexicon where the closer two words are semantically, the closer they are in the vector space. Using word vector for graph based text summarization has only been started to be attempted recently [17] due to the lack of fully developed word embedding datasets.

Although text summarization have been a forefront of NLP research, text summarization research in Bengali is a more recent development than in other high resource languages. So, a lot of sophisticated approaches from other languages haven't been attempted at Bengali yet. Earlier bengali extractive methods have been focused on some derivative of TF-IDF based text summarization such as the methods developed by Chowdhury et al. [5], Dash et al. [6], Sarkar [28] etc. Sarkar [28] used a simple TF-IDF score of each sentence to rank them and pick the best sentences to generate the output summary. Dash et al. [6] used weighted TF-IDF along with some other sentence features like sentence position to rank the sentences. Chowdhury et al. [5] however, used TF-IDF matrix of a document to build a graph and perform hierarchical clustering to group sentences together and pick one sentence from each group. One shortcoming of this method is that TF-IDF matrix is not semantically equivalent to the actual sentences due to the fundamental issues with TF-IDF. So, the TF-IDF doesn't perfectly represent the semantic relationship between the sentences in the generated graph. Using word vector embedding for Bengali has solved this problem of semantic representation. Word embedding datasets such as FastText [13] dataset[1] with word vector embeddings in 157 languages, including Bengali. Using this dataset, SASbSC [25] proposed a model where they replaced all the words from the input with their respective vector, then averaged the word vectors in a sentence to get a vector representation for the sentence. The sentence average vectors are then used to get the similarity between two sentences using the Gaussian similarity function to build an affinity matrix. This affinity matrix is used to cluster the sentences using spectral clustering to group sentences into distinct topics. The summary is generated after picking one sentence from each cluster to reduce redundancy and increase coverage.

But the sentence average method suffers critically due to its inability in capturing accurate

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[1] *https://fasttext.cc/docs/en/crawl-vectors.html*

Figure 1: A scenario where sentence averaging method fails. Dots in the figure represent word vectors and are grouped by colours if they are from the same sentence. (a) and (c) shows a scenario where the distance between sentence average vectors are larger than (b) and (d) despite the word vectors being more closely related.

relationship between sentences. This happens due to words in a sentence generally not having similar meaning with each other, instead they express different parts of one whole meaning of a sentence. This makes the words more complementary instead of being similar leading to word vectors being scattered throughout the word vector space. This characteristics makes the sentence average vectors always tending towards the centre and not representing the semantic similarity accurately. An example of this happening is shown in Figure 1 where the distance between the sentence average vectors are being misleading. In the figure, scenario (a) shows two sentence with word vectors very closely corresponding with each other. On the other hand, scenario (b) shows two sentences without any significant word correspondence. The distance between the sentence average vectors from (a) and (b) are shown in figure (c) and (d) respectively. We can see that the scenario (a) and (c) have a larger distance between sentence average vectors than scenario (b) and (d) despite having more word correspondence. This larger distance makes the Gaussian similarity between the sentences lower due to the inverse exponential nature of the function. The lower similarity leads to the graphical representation being less accurate and thus failing to capture the true semantic relationship within the sentences. This shortcoming of the method has been one of the key motivations for this research.

3   Methodology

The summarization process followed here can be boiled down as two basic steps, grouping all the close sentences together based on their meaning to minimize redundancy and picking one sentence from each group to maximize sentence coverage. To group semantically similar sentences into clusters, we build a sentence similarity graph and perform spectral clustering on it [25]. The sentence similarity graph is produced using a novel sentence similarity calculation algorithm that uses geometric mean of Gaussian similarity between individual word pairs from
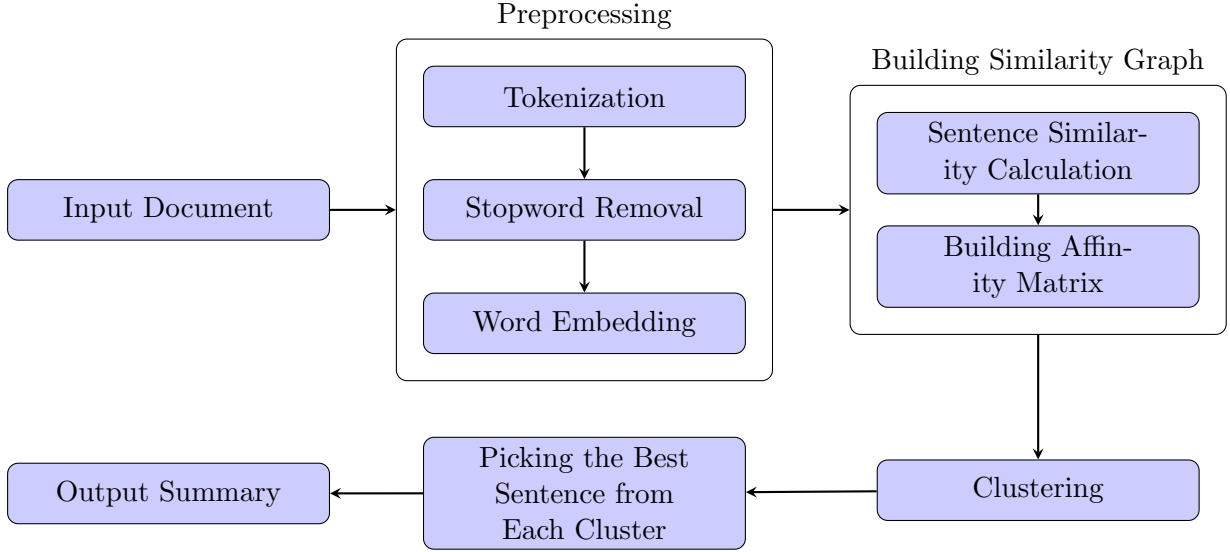
Figure 2: Process Flow Diagram

the two sentences. The Gaussian similarity is calculated using the vector embedding representations of the words. On the other hand, we used TF-IDF scores to pick the highest ranked sentences from a cluster [1, 6, 28, 29]. The summarization process followed here involves 4 steps. These are, Pre-processing, Sentence similarity calculation, Clustering and Summary generation. These steps are illustrated in Figure 2 and further discussed in the following subsections.

3.1 Preprocessing

Preprocessing is the standard process of NLP that transforms raw human language inputs into a format that can be used by a computer algorithm. In this step, the document is transformed into a few set of vectors where each word is represented with a vector, each sentence is represented as a set of vectors and the whole document as a list containing those sets. To achieve this representation, the preprocessing follows three steps. These are tokenization, stop word removal, and word embedding. A very common step in preprocessing, word stemming, isn't used here as the word embedding dataset works best for the whole word instead of the root word. These steps are further discussed below.

Tokenization is the step of dividing an input document into sentences and words to transform it into a more usable format. Here, the input document is represented as a list of sentence and the sentences are represented as a list of words. Stop words, such as prepositions and conjunctions, add sentence fluidity but don't carry significant meaning. Removing these words allows the algorithm to focus on more impactful words. Word Embedding is the process of representing words as vector in a vector space. In this vector space, semantically similar words are placed closer together so that the similarity relation between words can be expressed in an abstract mathematical way. Each word from the tokenized and filtered list is replaced with their corresponding vectors. If some words aren't present in the dataset, they are considered too rare and thus ignored. Following these steps, the input document is transformed into a set of vectors to be used in sentence similarity calculation.

3.2 Sentence Similarity Calculation

Sentence similarity is the key criteria to build a graphical representation of the semantic relationship in the input document. This graphical representation is expressed via an affinity matrix to cluster the semantically similar sentences. The nodes in the affinity matrix represents the sentences of the input and the edges of the matrix represents the similarity between two sentence. Here, we proposed a novel sentence similarity calculation technique using individual Gaussian similarity of word-pairs to construct an affinity matrix. To calculate the sentence similarity between two sentences, we adhere to the following steps.

Firstly, for every word of a sentence, we find its closest counterpart from the other sentence to build a word pair. The Euclidean distance between the vector representation of the word-pairs is defined as the Most Similar Word Distance (D_{msw}). The process of calculating the D_{msw} is shown in the Equation 1. In this equation, for every word vector x, in a sentence X, we find the Euclidean distance ($d(x, y_i)$) between the word vectors x and y_i where y_i is a word vector from the sentence Y. The lowest possible distance in this set of Euclidean distance is the D_{msw}.

$$D_{msw}(x, Y) = min(\{d(x, y_i) : y_i \in Y\}) \tag{1}$$

Then, we calculate the D_{msw} for every word of the two sentences X and Y to make the sentence similarity calculation symmetric. This process is shown in the Equation 2 where D is a set containing all the D_{msw} from both X and Y that would be used in the later steps.

$$D = \{D_{msw}(x, Y) : x \in X\} \cup \{D_{msw}(y, X) : y \in Y\} \tag{2}$$

After this, the word similarity between the word pairs is calculated to get the degree of correspondence between the two sentences. Here, the word similarity is calculated using Gaussian kernel function for the elements of the set D; Gaussian kernel functions provides a smooth, flexible and most representative similarity between two vectors [3]. The process of calculating word similarity (W_{sim}) is given in the Equation 3. In this equation, for every element D_i in set D, we calculate the Gaussian similarity to obtain word similarity. In the formula for Gaussian similarity, σ denotes the standard deviation that can be used as a control variable. The standard deviation represents the blurring effect of the kernel function. A lower value for σ represents a high noise sensitivity of the function [3]. The value of sigma was fine-tuned to be 5×10^{-11} which gives the best similarity measurement. The process of fine-tuning is described in the experimentation section (section 4.5.1).

$$W_{sim} = \{exp\left(\frac{-D_i^2}{2\sigma^2}\right) : D_i \in D\} \tag{3}$$

Finally, the sentence similarity between the two sentences $Sim(X, Y)$ is calculated using geometric mean of the word similarities to construct an affinity matrix. The geometric mean makes the similarity value less prone to effects of outliers thus it makes the calculation more reliable. This process is shown in the Equation 4; the geometric mean of each w_{sim} value for the two sentences is simplified in the Equation 4 to make the calculation process more computation
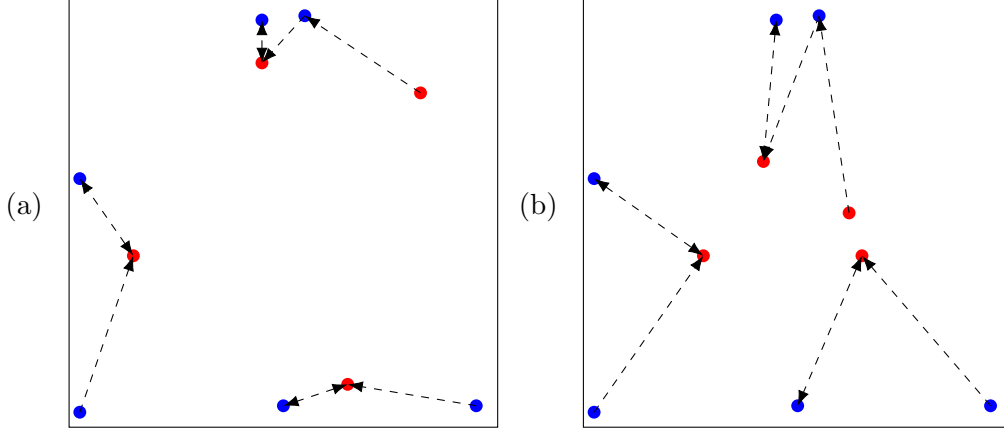
Figure 3: Local word correspondence of D_{msw} method. Dots in the figure represent word vectors and are coloured with the same colour if they are from the same sentence. Black dashed arrows represent the D_{msw} from its destination word vector. Here, scenario (a) will have larger similarity due to it having smaller D_{msw} than scenario (b)

friendly.

$$
\begin{aligned}
Sim(X,Y) &= \left(\prod_{i=1}^{n} W_{Sim_i} \right)^{\frac{1}{n}} \\
&= \left(e^{\frac{-D_1^2}{2\sigma^2}} \cdot e^{\frac{-D_2^2}{2\sigma^2}} \cdot \ldots \cdot e^{\frac{-D_n^2}{2\sigma^2}} \right)^{\frac{1}{n}} \\
&= exp\left(-\frac{D_1^2 + D_2^2 + \ldots + D_n^2}{2n\sigma^2} \right) \\
&= exp\left(-\frac{\sum_{i=1}^{n} D_i^2}{2n\sigma^2} \right)
\end{aligned}
\tag{4}
$$

By following steps described above, we get a similarity value for two sentences. This value solves the lack of local word correspondence problem faced by the word averaging based similarity calculation method [25]. Figure 3 demonstrates the merit of the method claimed above. Figure 3 shows that the proposed method can solve the local word correspondence problem faced by word averaging method. In the figure, the scenario 3(a) has a set of smaller D_{msw} than the scenario 3(b). Having smaller D_{msw} makes the individual word similarities W_{sim} larger due to the nature of Gaussian kernel function. These values would result in a higher sentence similarity for the sentences in the scenario 3(a) than in the scenario 3(b). This solved the problem showed in the Figure 1 where the scenario 1(a) has a larger sentence average distance than 1(b) resulting in 1(a) having a smaller sentence similarity than 1(b).

The whole process of sentence similarity calculation is shown in the Algorithm 1. In this algorithm, we calculate an affinity matrix using the input word vector list. We took the most similar word distance D_{msw} in line 8–13 and 18–23 for each word (line 7 and 17) of a sentence pair (line 3 and 6). Sum of D^2 from Equation 4 is calculated in the lines 14 and 24 to be used in the calculation of sentence similarity (line 27). The similarity is used to construct an affinity matrix A (line 28).

3.3 Clustering

Clustering is a key corner stone of the proposed method where we aim to cluster semantically similar sentences together to divide the input document into multiple topics. Clustering the

Algorithm 1 Sentence Similarity Calculation

1: $l \leftarrow$ length(WordVectorList)
2: $A \leftarrow [[0] * l] * l$
3: **for** each sentence$_i$ in WordVectorList **do**
4:      $D_{Square} \leftarrow 0$
5:      n $\leftarrow 0$
6:      **for** each sentence$_j$ in WordVectorList **do**
7:          **for** each word$_i$ in sentence$_i$ **do**
8:              $D_{msw} \leftarrow \infty$
9:              **for** each word$_j$ in sentence$_j$ **do**
10:                  **if** Distance(word$_i$, word$_j$) $< D_{msw}$ **then**
11:                      $D_{msw} \leftarrow$ distance(word$_i$, word$_j$)
12:                  **end if**
13:              **end for**
14:              $D_{Square} \leftarrow D_{Square} + D_{msw}^2$
15:              $n \leftarrow n + 1$
16:          **end for**
17:          **for** each word$_j$ in sentence$_j$ **do**
18:              $D_{msw} \leftarrow \infty$
19:              **for** each word$_i$ in sentence$_i$ **do**
20:                  **if** Distance(word$_i$, word$_j$) $< D_{msw}$ **then**
21:                      $D_{msw} \leftarrow$ distance(word$_i$, word$_j$)
22:                  **end if**
23:              **end for**
24:              $D_{Square} \leftarrow D_{Square} + D_{msw}^2$
25:              $n \leftarrow n + 1$
26:          **end for**
27:          similarity $\leftarrow \exp\left(\frac{-D_{Square}}{2 \times n \times \sigma^2}\right)$
28:          $A[i][j] \leftarrow A[j][i] \leftarrow$ similarity
29:      **end for**
30: **end for**
31: **Return** A

document minimizes redundancy in the output summary by ignoring multiple sentences from the same topic. For clustering, spectral and DBSCAN methods were considered due to their capability of being able to cluster irregular shapes. However, spectral clustering was found to perform better than DBSCAN because, smaller input documents have lower density which hinders DBSCAN [25].

On the contrary, spectral clustering takes the affinity matrix of a graph as input and returns the grouping of graph nodes by transforming the graph into its eigenspace [31]. The following Equation 5 shows the process of building an affinity matrix. Here, for every sentence pair S_i and S_j, we calculate their sentence similarity and place it in both A_{ij} and A_{ji} of the affinity matrix A.

$$A_{ij} = A_{ji} = Sim(S_i, S_j) \tag{5}$$

The affinity matrix is clustered into a reasonable, $k = \lceil N/5 \rceil$ groups to achieve an output summary. This summary, is short while the sentence groups resulting from clustering is also not too broad.

3.4 Summary Generation

Output summary is generated by selecting one sentence from each cluster achieved in the previous step to minimize topic redundancy and maximize topic coverage. To select one sentence from a cluster, we perform TF-IDF ranking on the sentences inside a cluster and pick the sentence with the highest TF-IDF score. To get the TF-IDF score of a sentence, we take the sum of all TF-IDF values for the words in that sentence. The TF-IDF value for a word is achieved by multiplying how many time the word appeared in the input document (Term Frequency, TF) and the inverse of how many document does the word appear in a corpus (Inverse Document Frequency, IDF). The process of scoring sentences are shown in the Equation 6 where, for each word W_i in a sentence S and a corpus C, we calculate the TF-IDF score of a sentence.

$$\text{TFIDF}(S) = \sum_{i=1}^{\text{length}(S)} \text{TF}(W_i) \times \text{IDF}(W_i, C) \tag{6}$$

The sentences with the best TF-IDF score from each clusters are then compiled as the output summary in their order of appearance in the input document to preserve the original flow of information. The process of generating output summary is further expanded in the Algorithm 2. After the clustering step (line 2), we took the TF-IDF score (line 7) of each sentence in a cluster (line 6). For each cluster (line 4), we pick the best scoring sentence (line 9). These sentences are then ordered (line 11) and concatenated (line 13–15) to generate the output summary.

4 Result

The performance of the proposed method has been compared against three Bengali text summarization methods to evaluate the correctness of generated summaries. The three methods, which have been used as a benchmark, are BenSumm [5], LexRank [10] and SASbSC [25]. All of these methods have been evaluated using four datasets to test the robustness of the model for Bengali text summarization for input from different sources. For evaluation, the Recall-Oriented Understudy for Gisting Evaluation (ROUGE) [18] metric has been used. Details about the models, datasets and evaluation metrics are provided in the following sections.

4.1 Text Summarization Models

We implemented Bensumm [5] and SASbSC [25], two recent Bengali extractive models, and LexRank [10], a popular benchmarking model for extractive text summarization to evaluate

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Algorithm 2 Summary Generation

1: $k \leftarrow \lceil$ length(A) / 5 $\rceil$
2: clusters $\leftarrow$ spectral_clustering(adjacency = A, k)
3: indexes $\leftarrow$ {}
4: **for** each cluster$_i$ in clusters **do**
5:     TFIDF $\leftarrow$ {}
6:     **for** each index in cluster$_i$ **do**
7:         TFIDF.append(tfidf_sum(sentences[index]))
8:     **end for**
9:     indexes.append(indexof(max(TFIDF)))
10: **end for**
11: sort(indexes)
12: $S \leftarrow$ ""
13: **for** each i in indexes **do**
14:     $S \leftarrow S+$ sentences[i]
15: **end for**
16: **Return** S
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the effectiveness of the proposed WSbSC method. These methods are further discussed in the following section.

WSbSC is the proposed model for this research. We find the Gaussian similarity for word-pairs from two sentences and take their geometric mean to get the similarity between two sentences. We use the similarity value to perfom spectral clustering to group sentences into groups and extract a representative sentence using TF-IDF score. The extracted sentences are used to generate the output summary which minimizes redundancy and maximizes coverage.

SASbSC [25] is the first method that introduced the approach of clustering sentences using sentence similarity. However, it uses the average of word vectors in a sentence for calculating similarity. After clustering the sentences based on their similarity, cosine similarity between the average vectors are used to pick the best sentence from a cluster.

BenSumm [5] is another recent research that describes an extractive and an abstractive text summarization technique. We compared the extractive technique with our model to ensure a fair and balanced comparison. Here, similarity matrix is built using TF-IDF which groups the sentences using agglomerative clustering. A Github implementation[2] provided by the authors is used in the comparison process.

LexRank [10] uses a TF-IDF based matrix and Googles PageRank algorithm [24] to rank sentences. Then the top ranked sentences are selected and arranged into summary. An implemented version of this method is available as lexrank[3] which is used in the comparison process using a large Bengali wikipedia corpus[4].

4.2   Evaluation Datasets

We used four evaluation dataset with varying quality, size and source to examine the robustness of the methods being tested. The first dataset is a **self-curated** extractive dataset that we developed to evaluate the performance of our proposed method. An expert linguistic team of

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[2]*https://github.com/tafseer-nayeem/BengaliSummarization*
[3]*https://pypi.org/project/lexrank/*
[4]*https://www.kaggle.com/datasets/shazol/bangla-wikipedia-corpus*

ten members summarized 250 news articles of varying sizes to diversify the dataset. Each article is summarized twice by two different experts to minimize human bias in the summary. In total, 500 different document-summary pairs are present in this dataset. The dataset is publicly available on Github[5] for reproducibility.

The second dataset is collected from **Kaggle** dataset[6] which is a collection of summary-article pair from "The Daily Prothom Alo" newspaper. The dataset is vast in size however the quality of the summaries are poor. All the articles smaller than 50 characters were discarded from the dataset. The articles with unrelated summaries were also removed from the dataset to improve the quality. After filtering, total 10,204 articles remained, each with two summaries in the dataset.

The third dataset we used for evaluation is **BNLPC** which is a collection of news article summaries [15]. This was collected from GitHub[7] for experimentation that contains one hundred articles with three different summaries for each article.

The fourth dataset is collected from **Github**[8]. The dataset contains 200 documents each with two human generated summaries. These documents were collected from several different Bengali news portals. The summaries were generated by linguistic experts which ensures the high quality of the dataset.

4.3   Evaluation Metrics

To evaluate the correctness of generated summaries against human written summaries, ROUGE metric [18] is used. The method compares a reference summary with a machine generated summary to evaluate alignment between the two. It uses N-gram-based overlapping to calculate a precision, recall and F-1 score of each summary. The Rouge package[9] is used to evaluate the proposed models against human generated summaries. The package has three different metrics for comparison of summaries. These are are:

1. **ROUGE-1** uses unigram matching to find how similar two summaries are. It calculates total common characters between the summaries to evaluate the performance. But using this metric also can be misleading as very large texts will share a very high proportion of uni-grams between them.

2. **ROUGE-2** uses bi-gram matching to find how much similar the two summaries are in a word level. Having more common bigrams between two summaries indicates a deeper syntactic similarity between them. Using this in combination with the ROUGE-1 is a standard practice to evaluate machine generated summaries [9].

3. **ROUGE-LCS** finds the longest common sub-sequence between two summaries to calculate the rouge scores. It focuses on finding similarity in the flow of information in the sentence level between two summaries.

In this study, we compared the F-1 scores from each of these metrics for the four models.

Dataset	Model	Rouge-1	Rouge-2	Rouge-LCS
Self-curated	WSbSC (Proposed)	**0.47**	**0.36**	**0.43**
	BenSumm [5]	0.41	0.29	0.36
	SASbSC [25]	0.42	0.29	0.37
	LexRank [10]	0.22	0.14	0.20
Kaggle	WSbSC (Proposed)	**0.49**	**0.43**	**0.48**
	BenSumm [5]	0.29	0.22	0.26
	SASbSC [25]	0.23	0.12	0.18
	LexRank [10]	0.24	0.16	0.22
BNLPC	WSbSC (Proposed)	**0.41**	**0.34**	**0.40**
	BenSumm [5]	0.36	0.28	0.34
	SASbSC [25]	**0.41**	0.33	0.39
	LexRank [10]	0.26	0.19	0.24
Github	WSbSC (Proposed)	**0.49**	**0.41**	**0.47**
	BenSumm [5]	0.31	0.22	0.28
	SASbSC [25]	0.30	0.18	0.24
	LexRank [10]	0.22	0.14	0.20

Table 1: Comparison of average Rouge scores between graph based extractive summarization models on 4 datasets

4.4 Comparison

We calculated the avaerage F-1 scores for three Rouge metrics (Rouge-1, Rouge-2, Rouge-LCS) for four extractive text summarization models (WSbSC (proposed), BenSumm [5], SASbSC [25], LexRank [10]) on four datasets (Self-Curated (SC), Kaggle, BNLPC, Github). The result of this evaluation is shown in table 1. In this table, we can see that our proposed model performs 11.9%, 24.1% and 16.2% better than the 2nd best method (SASbSC) in Rouge-1, Rouge-2 and Rouge-LCS respectively on our self-curated dataset. It performs 68.9%, 95.4% and 84.6% better respectively than the 2nd best method (BenSumm) on the Kaggle dataset. It also performs a tie in R-1, 3% better in R-2 and 2.6% better than the 2nd best method (SASbSC) on R-LCS using the BNLPC dataset. It performs 58%, 86.4%, and 67.9% better than the 2nd best method (BenSumm) on the Github dataset in all three metrics.

These results are further visualized into three radar charts in figure 4 to compare the performance of the models using all four datasets to compare them on individual metrics. In these charts, we can see that proposed method performs more consistently and uniformly across all the datasets regardless of the quality of the dataset. But other models, such as BenSumm performs well in some datasets (SC, GitHub, BNLPC) but also fails in the Kaggle dataset. Similarly, SASbSC performs well in SC and BNLPC datasets but the performance decreases sharply in Kaggle and GitHub datasets. LexRank although performs similarly across all datasets but is far lower on average.

4.5 Experimentation

We experimented on our model with different ranking techniques and different values for standard deviation (σ) for the equation 4 to get the best rouge values for a summary. The standard deviation (σ) for the Gaussian Similarity represents a smoothing factor that can be used as a control variable to be fine-tuned for the best result. On the other hand, ranking methods pick the most representative sentence from a cluster after the clustering step. We checked lead extracting and TF-IDF ranking methods for to pick the a representative sentence from each cluster. These experimentations are discussed with more detail below.

Method	Rouge-1	Rouge-2	Rouge-LCS
Lead extraction	0.47	0.36	0.43
TF-IDF ranking	**0.50**	**0.40**	**0.46**

Table 2: Comparison of Result of different ranking techniques

Language	Rouge-1	Rouge-2	Rouge-LCS
Bengali (Self-curated)	0.47	0.36	0.43
Bengali (Kaggle)	0.49	0.43	0.48
Bengali (BNLPC)	0.41	0.34	0.40
Bengali (Github)	0.49	0.41	0.47
Bengali (Average)	0.47	0.38	0.44
Hindi	0.40	0.26	0.36
Marathi	0.50	0.42	0.50
Turkish	0.48	0.39	0.47

Table 3: Comparison of Result of proposed summarization method in other low-resource languages

4.5.1 Fine-tuning Standard Deviation (σ)

We checked for different Standard Deviation (σ) on equation 4 to pick the best σ. Sixty-three different values for σ from 10^{-12} to 10 on regular intervals have been experimented on and can be seen that 5×10^{-11} works best as the value for σ on our self-curated dataset. The result for fine-tuning process is shown in the following line chart (Figure 5).

4.5.2 Different Sentence Extraction Techniques Inside Clusters

We implemented two sentence extraction methods to pick the most representative sentence from each cluster. Firstly, the lead extraction method is used where we just select the sentence that appears first in the input document because generally the earlier sentences in an input has more information on the context of the input document. The second extraction method is the TF-IDF ranking method, where we ranked the sentences by their TF-IDF scores and picked the sentence with the most TF-IDF score. We can see in the table 2 that the TF-IDF performs better on a high quality dataset like the self-curated dataset.

4.6 Implementation Into Other Languages

The proposed model is not language-dependent because it does not rely on any language specific features to summarize the input documents, thus it can be extended into other languages too. To implement this method into a language, we only need a language-specific tokenizer, a list of stop-words and a word vector embedding dataset. We implemented this model on three more languages to show the language independent nature of the model. To evaluate the quality of the sentence extraction, we tried to find evaluation datasets for summarization on other low resource languages, but could only find relevant datasets in three other languages. These languages are Hindi, Marathi and Turkish. We adopted the proposed model into these three low resource languages to check how well it performs.

The Table-3 shows the result of the proposed WSbSC method for extractive summarization in other low resource languages. In this table, We can see that the results on Marathi and Turkish are slightly better than the result on Bengali. Although it performs slightly lower on Hindi, The score is still similar to Bengali. To evaluate the result on Hindi language, we used
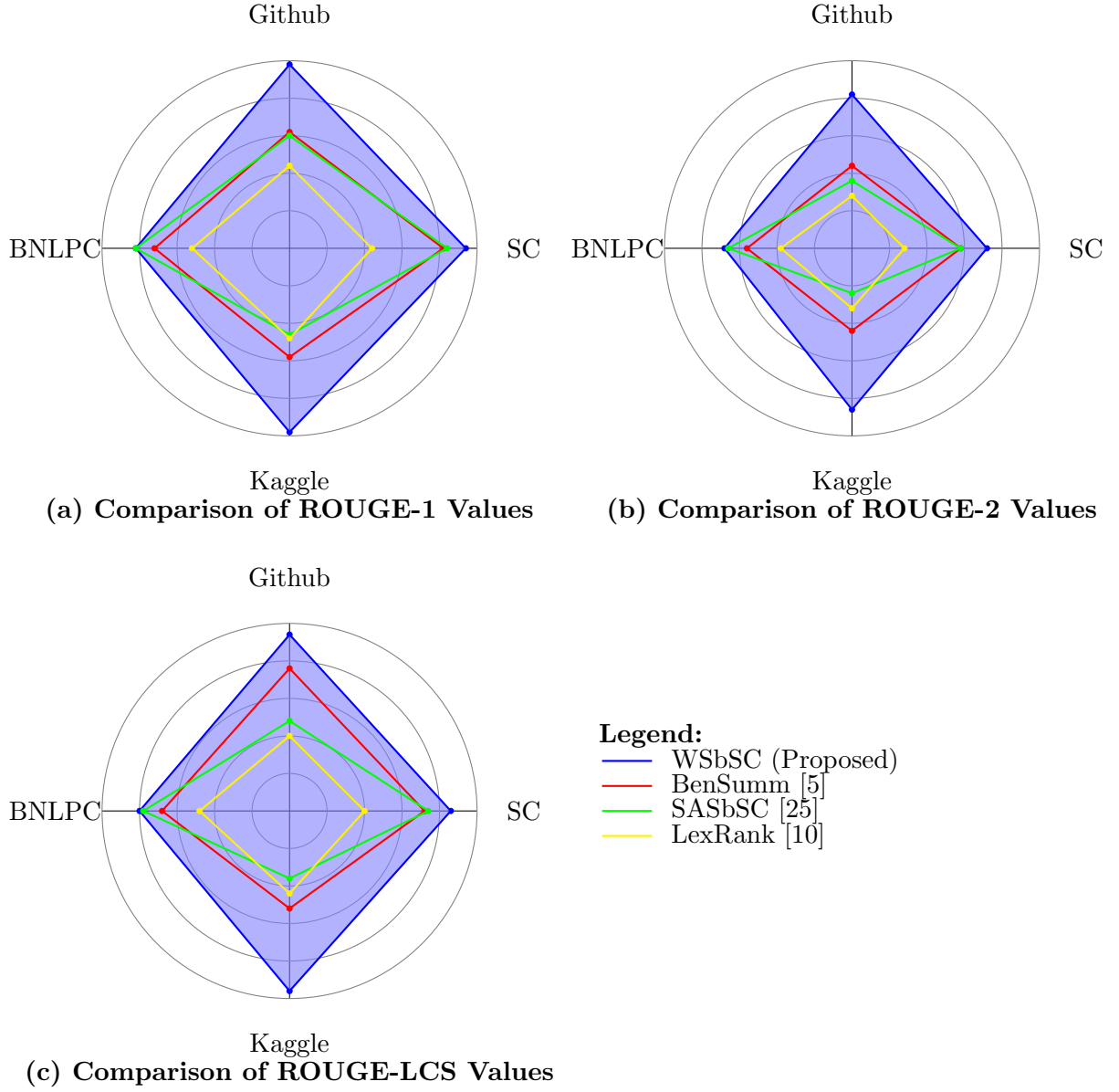
(a) Comparison of ROUGE-1 Values

(b) Comparison of ROUGE-2 Values

(c) Comparison of ROUGE-LCS Values

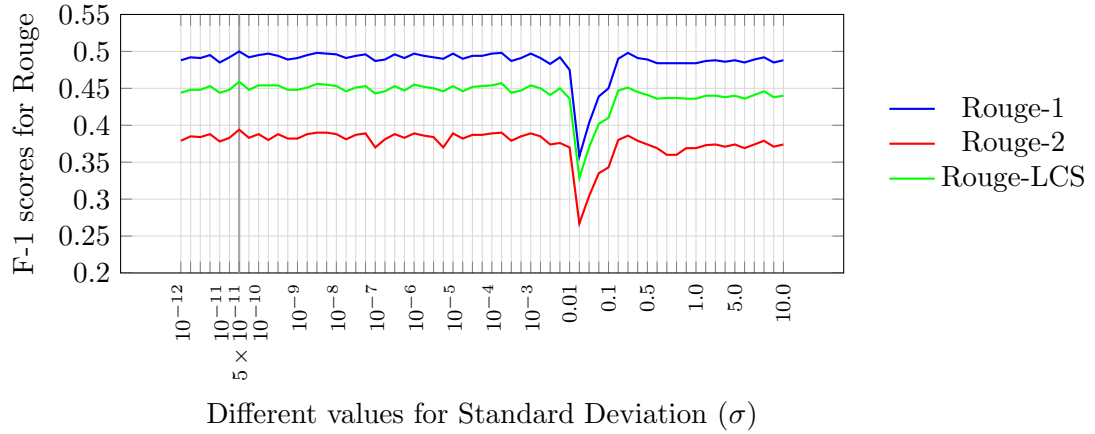Figure 4: The Radar chart of the models of being compared on four datasets at once

Figure 5: Fine-tuning for different standard deviation (σ) values

a Kaggle dataset[10] produced by Gaurav Arora. For the Marathi language, we used another Kaggle dataset[11] produced by Ketki Nirantar. For the Turkish language, we used a GitHub dataset[12] produced by the XTINGE [7] team for evaluation.

5 Discussion

The results presented in the previous sections highlight the effectiveness of the proposed WSbSC model for extractive text summarization in Bengali, as well as its adaptability to other low-resource languages. This section analyses the comparative results, the strengths and limitations of the proposed method, and potential areas for further research.

As evidenced by the results shown in Table 1 and Figure 4, the WSbSC model consistently outperforms other graph-based extractive text summarization models, namely BenSumm [6], LexRank [10], and SASbSC [25], across multiple datasets (Self-curated, Kaggle, BNLPC, GitHub) of varying sizes and source. The proposed model shows performance improvement in three ROUGE metrics (Rouge-1, Rouge-2, Rouge-LCS). This performance improvement can largely be attributed to the novel approach of calculating sentence similarity due to being one of the key change from the SASbSC method [25]. While calculating sentence similarity, taking the geometric mean of individual similarity between word pairs overcomes the lack of local word correspondence faced by the averaging vector method. The Gaussian similarity-based approach used to calculate the word similarities provides a novel and precise method for capturing the semantic relationships between sentences to further contribute in the performance improvement. Another reason for performance improvement is the usage of spectral clustering which is very effective in capturing irregular cluster shapes.

To calculate the similarity, we developed a novel method that can calculate the similarity between two set of vectors and is relevant in the context of languages. Our proposed strategy is more suited for this task than other strategies that can compare two sets of vectors such as Earth Movers Distance (EMD) [26], Hausdorff Distance [16], Procrustes Analysis [12] due to it focusing on the context of language more. EMD [26] tries to find the lowest amount of "work" needed to transform one set into the other one to calculate similarity. It considers adding a new vector to a set, removing a vector from a set, scaling a set, moving a vector in the set, rotating the set etc. as "work". This process is very computationally expensive as hundreds of thousands separate possibilities have to be checked for each vector in each set. EMD also focuses on scaling and rotating, which are not relevant in word vector space as rotating a sentence does not hold any semantic meaning. Another method, Hausdorff distance [16] takes the worst case scenario and calculates the highest distance between two vectors each from a set. This method needs the same amount of calculation as the proposed method but it is easily influenced by outliers due to only considering the worst case scenario. It also does not have any local vector correspondence and wasn't used because words tend to spread out over the whole word space and it would suffer from the same problem as the averaging method. Procrustes Analysis [12] tries to find the lowest amount of misalignment after scaling and rotating the two sets. But both scaling and rotating are irrelevant in the context of word vectors.

On the other hand, the proposed method focuses on local vector correspondence between two sets which is more important for words. The Gaussian similarity function captures the proximity of points smoothly, providing a continuous value for similarity between two words in a

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normalized way. Gaussian similarity is also robust against small outliers due to being a soft similarity measure. Taking geometric mean also helps smooth over similarity values for outlier words.

One of the key strengths of this proposed method is the reduction of redundancy, which is a common issue in extractive summarization methods. By grouping sentences with similar meanings and selecting a representative sentence from each group, the model ensures that the summary covers a broad range of topics without repeating itself. The use of spectral clustering in the model is also well-suited for the clustering task because spectral method does not assume a specific cluster shape and can infer the number of clusters using the eigen gap method. Our proposed model also has an improved sentence similarity calculation technique. Using the geometric mean of individual word similarities offers a more precise measure of how closely two sentences are related. This is a significant improvement over other traditional methods that rely on word averaging, which often dilute the semantic meaning of a sentence. Another key strength is the scalability across languages. WSbSC can be easily adapted to other languages due to it requiring very few language-specific resources. This scalability is demonstrated in the experiments with Hindi, Marathi, and Turkish languages (Table 3). This generalizability makes the model highly versatile and valuable for extractive summarization in low-resource languages. Despite differences in language structure, the model's core methodology remained effective, yielding results that were consistent with the Bengali dataset evaluations. This underscores the potential of WSbSC as a generalizable approach for extractive summarization across different languages, if appropriate pre-processing tools and word embedding datasets are available.

Despite its advantages, the WSbSC model does face some challenges. The model heavily relies on pre-trained word embeddings, which may not always capture the full details of certain domains or newly coined terms. The FastText [13] dataset used here is heavily reliant on wikipedia for training which could introduce some small unforeseen biases. In cases where the word embeddings do not have some words of a given document, the model's performance could degrade as it leaves those words out of the calculation process. The model also does not take into account the order in which words appear in a sentence or when they form special noun or verb groups. So it can be a little naive in some highly specialized fields.

The proposed WSbSC model represents a significant advancement in Bengali extractive text summarization. Its ability to accurately capture sentence similarity, reduce redundancy, maximize coverage and generalize across languages makes it a valuable tool for summarizing text in low-resource languages. While there are still challenges to be addressed, the results of this study demonstrate the robustness and adaptability of the WSbSC model, offering a promising direction for future research in multilingual extractive summarization.

6 Conclusion

In this study, we proposed a Word Similarity-based Spectral Clustering (WSbSC) method for Bengali extractive text summarization which can also be used in other low resource languages. the proposed method used geometric mean of Gaussian similarities between individual word pairs to identify deeper semantic relationship within two sentences. This method for calculating sentence similarity helps WSbSC to significantly outperform other recent graph based extractive text summarization methods on four varying datasets with different sizes and sources. This improvement in performance is also helped by the use of spectral clustering which helps to improve coherence and relevance of the generated summaries by minimizing redundancy and maximizing topic coverage. High performance across three ROUGE metrics on four datasets prove the versatility and robustness of the proposed method. WSbSC can also be extended

into other languages as shown through our experimentations on Hindi, Marathi and Turkish languages proving the generalizability of the method. This method addresses the need for an effective summarization technique in Bengali language as Bengali remains under-represented in NLP research despite it being the 7th largest language in the world.

Through results of extensive experimentations, we showed the strengths of the proposed WSbSC method as it outperforms several baseline techniques using a better approach to grouping sentences into key topics. Despite these promising results, there are areas with limitation that requires further improvement. WSbSC may face limitations on highly specialized or domain-specific texts, where deeper linguistic features beyond word similarity could be considered. The lack of consideration for word order in a sentence is also a key limitation which could be explored in the future. Future works could also explore hybrid models that integrate modern post-processing techniques to improve the flow of the output.

In conclusion, this work contributes to the growing body of computational linguistics research focused on low-resource languages like Bengali. The WSbSC method offers a novel approach for extractive summarization by using a new algorithm for calculating similarity between two sentences and sets the stage for further advancements in both Bengali text processing and multilingual summarization techniques.

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