

(2)

$$J = (\hat{Y} - P_d)^T Q (\hat{Y} - P_d) + \Delta \hat{U}_{mpc}^T R \Delta \hat{U}_{mpc} + \hat{U}_{mpc}^T \bar{R} \hat{U}_{mpc} \quad (1)$$

$$\hat{Y} = \int_y x(k) + P_y \hat{U}_{mpc} \quad (2)$$

$$\hat{U}_{mpc} = \int_u u_{mpc}(k-1) + P_u \Delta \hat{U}_{mpc} \quad (3)$$

(3) \rightarrow (2)

$$\hat{Y} = \int_y x(k) + P_y \int_u u_{mpc}(k-1) + P_y P_u \Delta \hat{U}_{mpc} \quad (4)$$

(4), (3) \rightarrow (1)

$$J = \left(\int_y x(k) + P_y \int_u u_{mpc}(k-1) + P_y P_u \Delta \hat{U}_{mpc} \right)^T \left(\int_y x(k) + P_y \int_u u_{mpc}(k-1) + P_y P_u \Delta \hat{U}_{mpc} \right) \\ + \Delta \hat{U}_{mpc}^T R \Delta \hat{U}_{mpc} + \\ + \left(\int_u u_{mpc}(k-1) + P_u \Delta \hat{U}_{mpc} \right)^T \bar{R} \left(\int_u u_{mpc}(k-1) + P_u \Delta \hat{U}_{mpc} \right)$$

$$J = \Delta \hat{U}_{mpc}^T P_u^T P_y^T Q P_y P_u \Delta \hat{U}_{mpc} + 2 \left(\int_y x(k) + P_y \int_u u_{mpc}(k-1) \right)^T Q P_y P_u \Delta \hat{U}_{mpc} + \\ + \Delta \hat{U}_{mpc}^T R \Delta \hat{U}_{mpc} + \\ + \Delta \hat{U}_{mpc}^T P_u^T \bar{R} P_u \Delta \hat{U}_{mpc} + 2 \left(\int_u u_{mpc}(k-1) \right)^T \bar{R} P_u \Delta \hat{U}_{mpc} + cte$$

$$J = \Delta \hat{U}_{mpc} \left(P_0^T P_y^T Q P_y P_0 + R + P_0^T \bar{R} P_0 \right) \Delta \hat{U}_{mpc} +$$

$$+ 2 \left(\begin{bmatrix} I & f_y & f_u \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} x(n) \\ u_{mpc}(n-1) \end{bmatrix} \right)^T Q P_y P_0 + \left(f_u^T u_{mpc}(n-1) \right)^T \bar{R} P_0 \Delta \hat{U}_{mpc} + \text{cte}$$

$$J = \Delta \hat{U}_{mpc}^T \underbrace{\left(P_0^T P_y^T Q P_y P_0 + R + P_0^T \bar{R} P_0 \right)}_{H_{mpc}} \Delta \hat{U}_{mpc} +$$

$$+ 2 \left(\begin{bmatrix} x^T(n) & u_{mpc}^T(n-1) \end{bmatrix} \begin{bmatrix} f_y^T \\ h^T P_y^T \end{bmatrix} Q P_y P_0 + u_{mpc}^T(n-1) f_u^T \bar{R} P_0 \right) \Delta \hat{U}_{mpc} + \text{cte}$$

$$J = \Delta \hat{U}_{mpc}^T H_{mpc} \Delta \hat{U}_{mpc} +$$

$$+ 2 \left(\begin{bmatrix} x^T(n) & u_{mpc}^T(n-1) \end{bmatrix} \begin{bmatrix} f_y^T \\ h^T P_y^T \end{bmatrix} Q P_y P_0 + \begin{bmatrix} x^T(n) & u_{mpc}^T(n-1) \end{bmatrix} \begin{bmatrix} C_{mpc} \\ f_u^T \end{bmatrix} \bar{R} P_0 \right) \Delta \hat{U}_{mpc} + \text{cte}$$

$$J = \Delta \hat{U}_{mpc}^T H_{mpc} \Delta \hat{U}_{mpc} +$$

$$+ \underbrace{\begin{bmatrix} x^T(n) & u_{mpc}^T(n-1) \end{bmatrix} \cdot 2 \left(\begin{bmatrix} f_y^T \\ h^T P_y^T \end{bmatrix} Q P_y P_0 + \begin{bmatrix} C_{mpc} \\ f_u^T \end{bmatrix} \bar{R} P_0 \right)}_{f_{mpc}} \Delta \hat{U}_{mpc} + \text{cte}$$

$$\bar{U} = \Delta \hat{U}_{mpc}^T H_{zp} \Delta \hat{U}_{mpc} + \left[x^T(n) \hat{U}_{mpc}^T(n-1) \right] l_{zp} \Delta \hat{U}_{mpc} + cte \quad (23)$$

sendo

$$H_{zp} = P_u^T P_y^T Q P_y P_u + R + P_u^T \bar{R} P_u$$

$$l_{zp} = 2 \left(\begin{bmatrix} l_y^T \\ l_u^T P_y^T \end{bmatrix} Q P_y P_u + \begin{bmatrix} 0_{n_u, n_u} \\ l_u^T \end{bmatrix} l_u^T \bar{R} P_u \right)$$

Importante

$$\bar{R} = \begin{bmatrix} \bar{r} & & 0 \\ & \bar{r} & \\ 0 & & \ddots \\ & & & \bar{r} \end{bmatrix}, \quad \bar{r} \in \mathbb{R}^{n_u, n_u}$$

↑ peso dos controles totais

adotor

$$\bar{r} = [\alpha_1 \quad \alpha_2 \quad 0]$$

↑
peso dos
tiffs

↑ peso do incremento
ξ que é somado a
ambos motores.

Deve ser nulo