exercise2

June 8, 2020

1 Programming Exercise 2: Logistic Regression

1.1 Introduction

In this exercise, you will implement logistic regression and apply it to two different datasets. Before starting on the programming exercise, we strongly recommend watching the video lectures and completing the review questions for the associated topics.

All the information you need for solving this assignment is in this notebook, and all the code you will be implementing will take place within this notebook. The assignment can be promptly submitted to the coursera grader directly from this notebook (code and instructions are included below).

Before we begin with the exercises, we need to import all libraries required for this programming exercise. Throughout the course, we will be using numpy for all arrays and matrix operations, and matplotlib for plotting. In this assignment, we will also use scipy, which contains scientific and numerical computation functions and tools.

You can find instructions on how to install required libraries in the README file in the github repository.

```
In [1]: # used for manipulating directory paths
    import os

# Scientific and vector computation for python
import numpy as np

# Plotting library
from matplotlib import pyplot

# Optimization module in scipy
from scipy import optimize

# library written for this exercise providing additional functions for assignment subm
import utils

# define the submission/grader object for this exercise
grader = utils.Grader()
```

tells matplotlib to embed plots within the notebook

%matplotlib inline

1.2 Submission and Grading

After completing each part of the assignment, be sure to submit your solutions to the grader. The following is a breakdown of how each part of this exercise is scored.

Section	Part	Submission function	Points
1	Section ??	Section ??	5
2	Section ??	Section ??	30
3	Section ??	Section ??	30
4	Section ??	Section ??	5
5	Section ??	Section ??	15
6	Section ??	Section ??	15
	Total Points		100

You are allowed to submit your solutions multiple times, and we will take only the highest score into consideration.

At the end of each section in this notebook, we have a cell which contains code for submitting the solutions thus far to the grader. Execute the cell to see your score up to the current section. For all your work to be submitted properly, you must execute those cells at least once. They must also be re-executed everytime the submitted function is updated.

1.3 1 Logistic Regression

In this part of the exercise, you will build a logistic regression model to predict whether a student gets admitted into a university. Suppose that you are the administrator of a university department and you want to determine each applicant's chance of admission based on their results on two exams. You have historical data from previous applicants that you can use as a training set for logistic regression. For each training example, you have the applicant's scores on two exams and the admissions decision. Your task is to build a classification model that estimates an applicant's probability of admission based the scores from those two exams.

The following cell will load the data and corresponding labels:

1.3.1 1.1 Visualizing the data

Before starting to implement any learning algorithm, it is always good to visualize the data if possible. We display the data on a 2-dimensional plot by calling the function plotData. You will now complete the code in plotData so that it displays a figure where the axes are the two exam scores, and the positive and negative examples are shown with different markers.

To help you get more familiar with plotting, we have left plotData empty so you can try to implement it yourself. However, this is an optional (ungraded) exercise. We also provide our implementation below so you can copy it or refer to it. If you choose to copy our example,

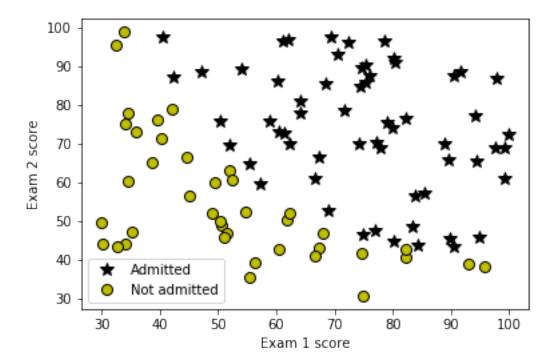
make sure you learn what each of its commands is doing by consulting the matplotlib and numpy documentation.

```
# Find Indices of Positive and Negative Examples
pos = y == 1
neg = y == 0
# Plot Examples
pyplot.plot(X[pos, 0], X[pos, 1], 'k*', lw=2, ms=10)
pyplot.plot(X[neg, 0], X[neg, 1], 'ko', mfc='y', ms=8, mec='k', mew=1)
In [4]: def plotData(X, y):
           11 11 11
          Plots the data points X and y into a new figure. Plots the data
          points with * for the positive examples and o for the negative examples.
          Parameters
           ____
          X : array_like
              An Mx2 matrix representing the dataset.
          y : array_like
              Label values for the dataset. A vector of size (M, ).
          Instructions
          _____
          Plot the positive and negative examples on a 2D plot, using the
          option 'k*' for the positive examples and 'ko' for the negative examples.
          n n n
          # Create New Figure
          fig = pyplot.figure()
          # Find Indices of Positive and Negative Examples
          pos = y == 1
          neg = y == 0
          # Plot Examples
          pyplot.plot(X[pos, 0], X[pos, 1], 'k*', lw=2, ms=10)
          pyplot.plot(X[neg, 0], X[neg, 1], 'ko', mfc='y', ms=8, mec='k', mew=1)
```

Now, we call the implemented function to display the loaded data:

```
In [5]: plotData(X, y)
          # add axes labels
          pyplot.xlabel('Exam 1 score')
```

```
pyplot.ylabel('Exam 2 score')
pyplot.legend(['Admitted', 'Not admitted'])
pass
```



1.2 Implementation

1.2.1 Warmup exercise: sigmoid function Before you start with the actual cost function, recall that the logistic regression hypothesis is defined as:

$$h_{\theta}(x) = g(\theta^T x)$$

where function *g* is the sigmoid function. The sigmoid function is defined as:

$$g(z) = \frac{1}{1 + e^{-z}}$$

Your first step is to implement this function sigmoid so it can be called by the rest of your program. When you are finished, try testing a few values by calling sigmoid(x) in a new cell. For large positive values of x, the sigmoid should be close to 1, while for large negative values, the sigmoid should be close to 0. Evaluating sigmoid(0) should give you exactly 0.5. Your code should also work with vectors and matrices. For a matrix, your function should perform the sigmoid function on every element.

```
Parameters
z : array_like
   The input to the sigmoid function. This can be a 1-D vector
   or a 2-D matrix.
Returns
-----
g: array_like
   The computed sigmoid function. q has the same shape as z, since
   the sigmoid is computed element-wise on z.
Instructions
Compute the sigmoid of each value of z (z can be a matrix, vector or scalar).
# convert input to a numpy array
z = np.array(z)
# You need to return the following variables correctly
g = np.zeros(z.shape)
g = 1 / (1 + np.exp(-z))
# -----
return g
```

The following cell evaluates the sigmoid function at z=0. You should get a value of 0.5. You can also try different values for z to experiment with the sigmoid function.

```
In [7]: # Test the implementation of sigmoid function here
    z = 0
    g = sigmoid(z)
    print('g(', z, ') = ', g)
g( 0 ) = 0.5
```

After completing a part of the exercise, you can submit your solutions for grading by first adding the function you modified to the submission object, and then sending your function to Coursera for grading.

The submission script will prompt you for your login e-mail and submission token. You can obtain a submission token from the web page for the assignment. You are allowed to submit your solutions multiple times, and we will take only the highest score into consideration.

Execute the following cell to grade your solution to the first part of this exercise.

You should now submit your solutions.

In [8]: # appends the implemented function in part 1 to the grader object
 grader[1] = sigmoid

send the added functions to coursera grader for getting a grade on this part grader.grade()

Submitting Solutions | Programming Exercise logistic-regression

Login (email address): saurabh.takle@gmail.com

Token: nOK1BM2i4WJLIYgG

1.2.2 Cost function and gradient

Now you will implement the cost function and gradient for logistic regression. Before proceeding we add the intercept term to X.

```
In [9]: # Setup the data matrix appropriately, and add ones for the intercept term
    m, n = X.shape

# Add intercept term to X
X = np.concatenate([np.ones((m, 1)), X], axis=1)
```

Now, complete the code for the function costFunction to return the cost and gradient. Recall that the cost function in logistic regression is

$$J(\theta) = \frac{1}{m} \sum_{i=1}^{m} \left[-y^{(i)} \log \left(h_{\theta} \left(x^{(i)} \right) \right) - \left(1 - y^{(i)} \right) \log \left(1 - h_{\theta} \left(x^{(i)} \right) \right) \right]$$

and the gradient of the cost is a vector of the same length as θ where the j^{th} element (for $j = 0, 1, \dots, n$) is defined as follows:

$$\frac{\partial J(\theta)}{\partial \theta_i} = \frac{1}{m} \sum_{i=1}^{m} \left(h_{\theta} \left(x^{(i)} \right) - y^{(i)} \right) x_j^{(i)}$$

Note that while this gradient looks identical to the linear regression gradient, the formula is actually different because linear and logistic regression have different definitions of $h_{\theta}(x)$.

```
In [10]: def costFunction(theta, X, y):
            Compute cost and gradient for logistic regression.
            Parameters
            _____
            theta: array like
                The parameters for logistic regression. This a vector
                of shape (n+1, ).
            X : array_like
                The input dataset of shape (m \times n+1) where m is the total number
                of data points and n is the number of features. We assume the
                intercept has already been added to the input.
            y : arra\_like
                Labels for the input. This is a vector of shape (m, ).
            Returns
            ____
            J: float
                The computed value for the cost function.
            grad : array_like
                A vector of shape (n+1, ) which is the gradient of the cost
                function with respect to theta, at the current values of theta.
            Instructions
            Compute the cost of a particular choice of theta. You should set J to
            the cost. Compute the partial derivatives and set grad to the partial
            derivatives of the cost w.r.t. each parameter in theta.
            11 11 11
            # Initialize some useful values
            m = y.size # number of training examples
            # You need to return the following variables correctly
            grad = np.zeros(theta.shape)
            h = sigmoid(X.dot(theta.T))
            J = (1 / m) * (np.sum(-y.dot(np.log(h)) - (1-y).dot(np.log(1-h))))
            grad = (1 / m) * (h - y).dot(X)
```

Once you are done call your costFunction using two test cases for θ by executing the next cell.

```
In [11]: # Initialize fitting parameters
         initial_theta = np.zeros(n+1)
         cost, grad = costFunction(initial_theta, X, y)
        print('Cost at initial theta (zeros): {:.3f}'.format(cost))
        print('Expected cost (approx): 0.693\n')
        print('Gradient at initial theta (zeros):')
        print('\t[{:.4f}, {:.4f}]'.format(*grad))
        print('Expected gradients (approx):\n\t[-0.1000, -12.0092, -11.2628]\n')
         # Compute and display cost and gradient with non-zero theta
        test_theta = np.array([-24, 0.2, 0.2])
         cost, grad = costFunction(test_theta, X, y)
        print('Cost at test theta: {:.3f}'.format(cost))
        print('Expected cost (approx): 0.218\n')
        print('Gradient at test theta:')
        print('\t[{:.3f}, {:.3f}]'.format(*grad))
        print('Expected gradients (approx):\n\t[0.043, 2.566, 2.647]')
Cost at initial theta (zeros): 0.693
Expected cost (approx): 0.693
Gradient at initial theta (zeros):
        [-0.1000, -12.0092, -11.2628]
Expected gradients (approx):
        [-0.1000, -12.0092, -11.2628]
Cost at test theta: 0.218
Expected cost (approx): 0.218
Gradient at test theta:
        [0.043, 2.566, 2.647]
Expected gradients (approx):
        [0.043, 2.566, 2.647]
   You should now submit your solutions.
In [12]: grader[2] = costFunction
         grader[3] = costFunction
        grader.grade()
```

1.2.3 Learning parameters using scipy.optimize In the previous assignment, you found the optimal parameters of a linear regression model by implementing gradient descent. You wrote a cost function and calculated its gradient, then took a gradient descent step accordingly. This time, instead of taking gradient descent steps, you will use the scipy.optimize module. SciPy is a numerical computing library for python. It provides an optimization module for root finding and minimization. As of scipy 1.0, the function scipy.optimize.minimize is the method to use for optimization problems(both constrained and unconstrained).

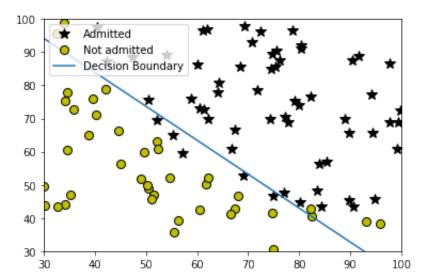
For logistic regression, you want to optimize the cost function $J(\theta)$ with parameters θ . Concretely, you are going to use optimize.minimize to find the best parameters θ for the logistic regression cost function, given a fixed dataset (of X and y values). You will pass to optimize.minimize the following inputs: - costFunction: A cost function that, when given the training set and a particular θ , computes the logistic regression cost and gradient with respect to θ for the dataset (X, y). It is important to note that we only pass the name of the function without the parenthesis. This indicates that we are only providing a reference to this function, and not evaluating the result from this function. - initial_theta: The initial values of the parameters we are trying to optimize. - (X, y): These are additional arguments to the cost function. - jac: Indication if the cost function returns the Jacobian (gradient) along with cost value. (True) - method: Optimization method/algorithm to use - options: Additional options which might be specific to the specific optimization method. In the following, we only tell the algorithm the maximum number of iterations before it terminates.

If you have completed the costFunction correctly, optimize.minimize will converge on the right optimization parameters and return the final values of the cost and θ in a class object. Notice that by using optimize.minimize, you did not have to write any loops yourself, or set a learning rate like you did for gradient descent. This is all done by optimize.minimize: you only needed to provide a function calculating the cost and the gradient.

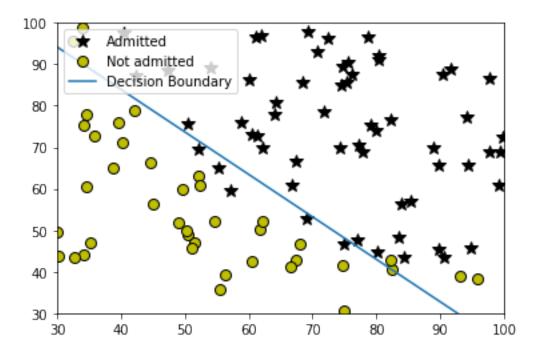
In the following, we already have code written to call optimize.minimize with the correct arguments.

```
# see documention for scipy's optimize.minimize for description about
         # the different parameters
         # The function returns an object `OptimizeResult`
         # We use truncated Newton algorithm for optimization which is
         # equivalent to MATLAB's fminunc
         # See https://stackoverflow.com/questions/18801002/fminunc-alternate-in-numpy
        res = optimize.minimize(costFunction,
                                 initial_theta,
                                 (X, y),
                                 jac=True,
                                 method='TNC',
                                 options=options)
         # the fun property of `OptimizeResult` object returns
         # the value of costFunction at optimized theta
         cost = res.fun
         # the optimized theta is in the x property
        theta = res.x
         # Print theta to screen
        print('Cost at theta found by optimize.minimize: {:.3f}'.format(cost))
        print('Expected cost (approx): 0.203\n');
        print('theta:')
        print('\t[{:.3f}, {:.3f}]'.format(*theta))
        print('Expected theta (approx):\n\t[-25.161, 0.206, 0.201]')
Cost at theta found by optimize.minimize: 0.203
Expected cost (approx): 0.203
theta:
        [-25.161, 0.206, 0.201]
Expected theta (approx):
        [-25.161, 0.206, 0.201]
```

Once optimize minimize completes, we want to use the final value for θ to visualize the decision boundary on the training data as shown in the figure below.



To do so, we have written a function plotDecisionBoundary for plotting the decision boundary on top of training data. You do not need to write any code for plotting the decision boundary, but we also encourage you to look at the code in plotDecisionBoundary to see how to plot such a boundary using the θ values. You can find this function in the utils.py file which comes with this assignment.



1.2.4 Evaluating logistic regression

After learning the parameters, you can use the model to predict whether a particular student will be admitted. For a student with an Exam 1 score of 45 and an Exam 2 score of 85, you

should expect to see an admission probability of 0.776. Another way to evaluate the quality of the parameters we have found is to see how well the learned model predicts on our training set. In this part, your task is to complete the code in function predict. The predict function will produce "1" or "0" predictions given a dataset and a learned parameter vector θ .

```
In [15]: def predict(theta, X):
           Predict whether the label is 0 or 1 using learned logistic regression.
           Computes the predictions for X using a threshold at 0.5
           (i.e., if sigmoid(theta.T*x) >= 0.5, predict 1)
           Parameters
           _____
           theta: array_like
               Parameters for logistic regression. A vecotor of shape (n+1, ).
           X : array_like
               The data to use for computing predictions. The rows is the number
               of points to compute predictions, and columns is the number of
               features.
           Returns
           p : array_like
              Predictions and 0 or 1 for each row in X.
           Instructions
           _____
           Complete the following code to make predictions using your learned
           logistic regression parameters. You should set p to a vector of O's and 1's
           m = X.shape[0] # Number of training examples
           # You need to return the following variables correctly
           p = np.zeros(m)
           p = np.round(sigmoid(X.dot(theta.T)))
           # ------
           return p
```

After you have completed the code in predict, we proceed to report the training accuracy of your classifier by computing the percentage of examples it got correct.

```
prob = sigmoid(np.dot([1, 45, 85], theta))
        print('For a student with scores 45 and 85,'
              'we predict an admission probability of {:.3f}'.format(prob))
        print('Expected value: 0.775 +/- 0.002\n')
        # Compute accuracy on our training set
        p = predict(theta, X)
        print('Train Accuracy: {:.2f} %'.format(np.mean(p == y) * 100))
        print('Expected accuracy (approx): 89.00 %')
For a student with scores 45 and 85, we predict an admission probability of 0.776
Expected value: 0.775 +/- 0.002
Train Accuracy: 89.00 %
Expected accuracy (approx): 89.00 %
  You should now submit your solutions.
In [17]: grader[4] = predict
        grader.grade()
Submitting Solutions | Programming Exercise logistic-regression
Use token from last successful submission (saurabh.takle@gmail.com)? (Y/n): y
                                Part Name | Score | Feedback
                                ----- | ----- |
                          Sigmoid Function | 5 / 5 | Nice work!
                  Logistic Regression Cost | 30 / 30 | Nice work!
              Logistic Regression Gradient | 30 / 30 | Nice work!
                                  Predict | 5 / 5 | Nice work!
      Regularized Logistic Regression Cost | 0 / 15 |
  Regularized Logistic Regression Gradient | 0 / 15 |
                                _____
                                          | 70 / 100 |
```

1.4 2 Regularized logistic regression

In this part of the exercise, you will implement regularized logistic regression to predict whether microchips from a fabrication plant passes quality assurance (QA). During QA, each microchip goes through various tests to ensure it is functioning correctly. Suppose you are the product manager of the factory and you have the test results for some microchips on two different tests. From these two tests, you would like to determine whether the microchips should be accepted or rejected. To help you make the decision, you have a dataset of test results on past microchips, from which you can build a logistic regression model.

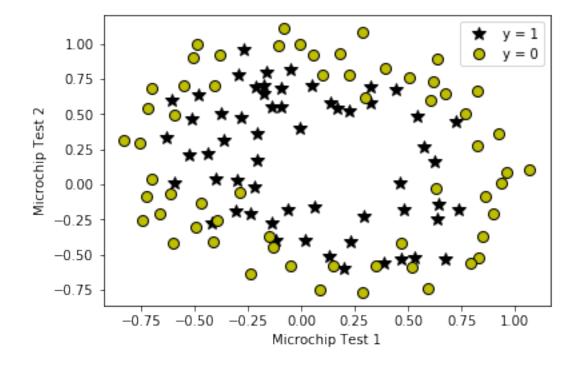
First, we load the data from a CSV file:

1.4.1 2.1 Visualize the data

Similar to the previous parts of this exercise, plotData is used to generate a figure, where the axes are the two test scores, and the positive (y = 1, accepted) and negative (y = 0, rejected) examples are shown with different markers.

```
In [19]: plotData(X, y)
    # Labels and Legend
    pyplot.xlabel('Microchip Test 1')
    pyplot.ylabel('Microchip Test 2')

# Specified in plot order
    pyplot.legend(['y = 1', 'y = 0'], loc='upper right')
    pass
```



The above figure shows that our dataset cannot be separated into positive and negative examples by a straight-line through the plot. Therefore, a straight-forward application of logistic regression will not perform well on this dataset since logistic regression will only be able to find a linear decision boundary.

1.4.2 2.2 Feature mapping

One way to fit the data better is to create more features from each data point. In the function mapFeature defined in the file utils.py, we will map the features into all polynomial terms of x_1 and x_2 up to the sixth power.

mapFeature(
$$x$$
) = $\begin{bmatrix} 1 & x_1 & x_2 & x_1^2 & x_1x_2 & x_2^2 & x_1^3 & \dots & x_1x_2^5 & x_2^6 \end{bmatrix}^T$

As a result of this mapping, our vector of two features (the scores on two QA tests) has been transformed into a 28-dimensional vector. A logistic regression classifier trained on this higher-dimension feature vector will have a more complex decision boundary and will appear nonlinear when drawn in our 2-dimensional plot. While the feature mapping allows us to build a more expressive classifier, it also more susceptible to overfitting. In the next parts of the exercise, you will implement regularized logistic regression to fit the data and also see for yourself how regularization can help combat the overfitting problem.

2.3 Cost function and gradient

Now you will implement code to compute the cost function and gradient for regularized logistic regression. Complete the code for the function costFunctionReg below to return the cost and gradient.

Recall that the regularized cost function in logistic regression is

$$J(\theta) = \frac{1}{m} \sum_{i=1}^{m} \left[-y^{(i)} \log \left(h_{\theta} \left(x^{(i)} \right) \right) - \left(1 - y^{(i)} \right) \log \left(1 - h_{\theta} \left(x^{(i)} \right) \right) \right] + \frac{\lambda}{2m} \sum_{j=1}^{n} \theta_{j}^{2}$$

Note that you should not regularize the parameters θ_0 . The gradient of the cost function is a vector where the j^{th} element is defined as follows:

$$\frac{\partial J(\theta)}{\partial \theta_0} = \frac{1}{m} \sum_{i=1}^{m} \left(h_{\theta} \left(x^{(i)} \right) - y^{(i)} \right) x_j^{(i)} \quad \text{for } j = 0$$

$$\frac{\partial J(\theta)}{\partial \theta_j} = \left(\frac{1}{m} \sum_{i=1}^m \left(h_\theta\left(x^{(i)}\right) - y^{(i)}\right) x_j^{(i)}\right) + \frac{\lambda}{m} \theta_j \quad \text{for } j \ge 1$$

In [21]: def costFunctionReg(theta, X, y, lambda_):

Compute cost and gradient for logistic regression with regularization.

Parameters

theta : array_like

Logistic regression parameters. A vector with shape (n,). n is the number of features including any intercept. If we have mapped our initial features into polynomial features, then n is the total

number of polynomial features.

```
X : array_like
   The data set with shape (m \ x \ n). m is the number of examples, and
   n is the number of features (after feature mapping).
y : array_like
   The data labels. A vector with shape (m, ).
lambda_{-}: float
   The regularization parameter.
Returns
_____
J:float
   The computed value for the regularized cost function.
grad : array_like
   A vector of shape (n, ) which is the gradient of the cost
   function with respect to theta, at the current values of theta.
Instructions
Compute the cost `J` of a particular choice of theta.
Compute the partial derivatives and set `grad` to the partial
derivatives of the cost w.r.t. each parameter in theta.
# Initialize some useful values
m = y.size # number of training examples
# You need to return the following variables correctly
J = 0
grad = np.zeros(theta.shape)
h = sigmoid(X.dot(theta.T))
temp = theta
temp[0] = 0
grad = (1 / m) * (h - y).dot(X)
grad = grad + ((lambda_ / m) * temp)
# -----
return J, grad
```

Once you are done with the costFunctionReg, we call it below using the initial value of θ

(initialized to all zeros), and also another test case where θ is all ones.

```
In [22]: # Initialize fitting parameters
        initial_theta = np.zeros(X.shape[1])
        # Set regularization parameter lambda to 1
        # DO NOT use `lambda` as a variable name in python
        # because it is a python keyword
        lambda_ = 1
        # Compute and display initial cost and gradient for regularized logistic
        cost, grad = costFunctionReg(initial_theta, X, y, lambda_)
        print('Cost at initial theta (zeros): {:.3f}'.format(cost))
        print('Expected cost (approx) : 0.693\n')
        print('Gradient at initial theta (zeros) - first five values only:')
        print('\t[{:.4f}, {:.4f}, {:.4f}, {:.4f}]'.format(*grad[:5]))
        print('Expected gradients (approx) - first five values only:')
        print('\t[0.0085, 0.0188, 0.0001, 0.0503, 0.0115]\n')
        # Compute and display cost and gradient
        # with all-ones theta and lambda = 10
        test theta = np.ones(X.shape[1])
        cost, grad = costFunctionReg(test_theta, X, y, 10)
        print('----\n')
        print('Cost at test theta : {:.2f}'.format(cost))
        print('Expected cost (approx): 3.16\n')
        print('Gradient at initial theta (zeros) - first five values only:')
        print('\t[{:.4f}, {:.4f}, {:.4f}, {:.4f}]'.format(*grad[:5]))
        print('Expected gradients (approx) - first five values only:')
        print('\t[0.3460, 0.1614, 0.1948, 0.2269, 0.0922]')
Cost at initial theta (zeros): 0.693
Expected cost (approx)
                       : 0.693
Gradient at initial theta (zeros) - first five values only:
       [0.0085, 0.0188, 0.0001, 0.0503, 0.0115]
Expected gradients (approx) - first five values only:
       [0.0085, 0.0188, 0.0001, 0.0503, 0.0115]
 _____
Cost at test theta : 3.16
```

```
Expected cost (approx): 3.16
Gradient at initial theta (zeros) - first five values only:
       [0.3460, 0.1614, 0.1948, 0.2269, 0.0922]
Expected gradients (approx) - first five values only:
       [0.3460, 0.1614, 0.1948, 0.2269, 0.0922]
  You should now submit your solutions.
In [23]: grader[5] = costFunctionReg
        grader[6] = costFunctionReg
        grader.grade()
Submitting Solutions | Programming Exercise logistic-regression
Use token from last successful submission (saurabh.takle@gmail.com)? (Y/n): y
                                Part Name | Score | Feedback
                                -----|
                                              ----- | -----
                         Sigmoid Function | 5 / 5 | Nice work!
                  Logistic Regression Cost | 30 / 30 | Nice work!
              Logistic Regression Gradient | 30 / 30 | Nice work!
                                  Predict | 5 / 5 | Nice work!
      Regularized Logistic Regression Cost | 15 / 15 | Nice work!
  Regularized Logistic Regression Gradient | 15 / 15 | Nice work!
                                _____
                                          | 100 / 100 |
```

2.3.1 Learning parameters using scipy.optimize.minimize Similar to the previous parts, you will use optimize.minimize to learn the optimal parameters θ . If you have completed the cost and gradient for regularized logistic regression (costFunctionReg) correctly, you should be able to step through the next part of to learn the parameters θ using optimize.minimize.

1.4.3 2.4 Plotting the decision boundary

To help you visualize the model learned by this classifier, we have provided the function plotDecisionBoundary which plots the (non-linear) decision boundary that separates the positive and negative examples. In plotDecisionBoundary, we plot the non-linear decision boundary by computing the classifier's predictions on an evenly spaced grid and then and draw a contour plot where the predictions change from y = 0 to y = 1.

1.4.4 2.5 Optional (ungraded) exercises

In this part of the exercise, you will get to try out different regularization parameters for the dataset to understand how regularization prevents overfitting.

Notice the changes in the decision boundary as you vary λ . With a small λ , you should find that the classifier gets almost every training example correct, but draws a very complicated boundary, thus overfitting the data. See the following figures for the decision boundaries you should get for different values of λ .

No regularization (overfitting)

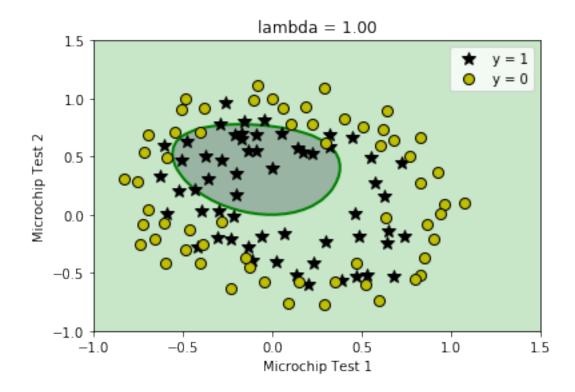
Decision boundary with regularization

Decision boundary with too much regularization

This is not a good decision boundary: for example, it predicts that a point at x=(0.25,1.5) is accepted (y=1), which seems to be an incorrect decision given the training set. With a larger λ , you should see a plot that shows an simpler decision boundary which still separates the positives and negatives fairly well. However, if λ is set to too high a value, you will not get a good fit and the decision boundary will not follow the data so well, thus underfitting the data.

```
In [26]: # Initialize fitting parameters
         initial_theta = np.zeros(X.shape[1])
         # Set regularization parameter lambda to 1 (you should vary this)
         lambda_{-} = 1
         # set options for optimize.minimize
         options= {'maxiter': 100}
         res = optimize.minimize(costFunctionReg,
                                 initial_theta,
                                 (X, y, lambda_),
                                 jac=True,
                                 method='TNC',
                                 options=options)
         # the fun property of OptimizeResult object returns
         # the value of costFunction at optimized theta
         cost = res.fun
         # the optimized theta is in the x property of the result
         theta = res.x
         utils.plotDecisionBoundary(plotData, theta, X, y)
         pyplot.xlabel('Microchip Test 1')
         pyplot.ylabel('Microchip Test 2')
         pyplot.legend(['y = 1', 'y = 0'])
         pyplot.grid(False)
         pyplot.title('lambda = %0.2f' % lambda_)
         # Compute accuracy on our training set
         p = predict(theta, X)
         print('Train Accuracy: %.1f %%' % (np.mean(p == y) * 100))
         print('Expected accuracy (with lambda = 1): 83.1 % (approx)\n')
```

Train Accuracy: 66.1 %
Expected accuracy (with lambda = 1): 83.1 % (approx)



You do not need to submit any solutions for these optional (ungraded) exercises.

In []: