

R Textbook Companion for
Introduction to Probability and Statistics
by William Mendenhall, Robert J Beaver, and
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May 14, 2020

¹Funded by a grant from the National Mission on Education through ICT
- <http://spoken-tutorial.org/NMEICT-Intro>. This Textbook Companion and R
codes written in it can be downloaded from the "Textbook Companion Project"
section at the website - <https://r.fossee.in>.

Book Description

Title: Introduction to Probability and Statistics

Author: William Mendenhall, Robert J Beaver, and Barbara M Beaver

Publisher: Brooks Cole, USA

Edition: 13

Year: 2008

ISBN: 9780495389538

R numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means an R code whose theory is explained in Section 2.3 of the book.

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Chapter 1

DESCRIBING DATA WITH GRAPHS

R code Exa 1.3 Pie and Bar Chart

```
1 rating<-c("A","B","C","D")
2 frequency<-c(35,260,93,12)
3 total<-sum(frequency)
4 relative_frequency_percent<-c(frequency/total)*100
5 label<-paste(rating,relative_frequency_percent)
6 label<-paste(label,"%",sep=" ")
7 par(mfrow=c(1,2))
8 pie(relative_frequency_percent,labels = label,
      clockwise = TRUE)
9 DF<-data.frame(rating,frequency)
10 barplot(frequency, ylab="frequency",xlab="rating",
      names.arg = c("A","B","C","D"))
11 #The answer may slightly vary due to rounding off
    values
```

R code Exa 1.4 Pareto Chart of Candies Problem

```

1 color<-c("Brown","Green","Brown","Blue","Red","Red",
  "Green","Brown","Yellow","Orange","Green","Blue",
  "Brown","Blue","Blue","Brown","Orange","Blue",
  "Brown","Orange","Yellow")
2 color.frequency<-table(color)
3 barplot(color.frequency[order(color.frequency,
  decreasing = T)],ylab = "frequency",xlab = "color
  ")
4 #please zoom the plot to view the plot clearly

```

R code Exa 1.5 Bar and Pie Chart

```

1 category<-c("Military personnel","Operation and
  maintenance","Procurement","Research and
  development","Military construction","Other")
2 amount<-c(127.5,188.1,82.3,65.7,5.3,5.5)
3 label<-paste(category,amount)
4 label<-paste(label,"%",sep=" ")
5 par(mfrow=c(1,2))
6 pie(amount,labels = label,clockwise = TRUE)
7 barplot(amount, ylab="amount(in Billions)",xlab="
  category",ylim=c(0,200),names.arg = c("Military
  personnel","Operation and maintenance","
  Procurement","Research and development","Military
  construction","Other"))

```

R code Exa 1.6 Line Chart

```

1 years <- c(2010,2020,2030,2040,2050)
2 equal_85_and_over <- c(6.1,7.3,9.6,15.4,20.9)
3 par(mfrow=c(1,2))
4 plot(years,equal_85_and_over,type = "b")

```

```
5 plot(years, equal_85_and_over, ylim=c(0,100), type = "b
    ")
```

R code Exa 1.7 Stem and Leaf Plot

```
1 prices<-c
  (90,65,75,70,70,68,70,70,60,68,70,74,65,75,70,40,70,95,65)
2 stem(prices, scale = 2)
```

R code Exa 1.8 Stem and Leaf Plot for Weights

```
1 weights<-c
  (7.2,7.8,6.8,6.2,8.2,8.0,8.2,5.6,8.6,7.1,8.2,7.7,7.5,7.2,7.7,5.8,
2 stem(weights)
```

R code Exa 1.10 Dotplot

```
1 GPAs<-c(2.8,3.0,3.0,3.3,2.4,3.4,3.0,0.21)
2 stripchart(GPAs, method = "stack")
3 summary(GPAs)
4 #summary function is used to find the outlier
```

R code Exa 1.11 Relative Frequency Histogram

```
1 visits <- c
  (6,4,6,5,3,7,6,5,5,5,1,4,6,5,7,5,6,3,7,5,6,8,4,6,5)

2 h<-hist(visits, plot=F)
3 h$counts <- h$counts / sum(h$counts)
4 plot(h, freq=TRUE, ylab="Relative Frequency")
```

Chapter 2

DESCRIBING DATA WITH NUMERICAL MEASURES

R code Exa 2.1 Dotplot and Sample Mean

```
1 measurement<-c(2,9,11,5,6)
2 stripchart(measurement, xlab = "Measurements")
3 sample_mean<-mean(measurement)
4 cat("sample mean is",sample_mean)
```

R code Exa 2.2 Median

```
1 set<-c(2,9,11,5,6)
2 median<-median(set)
3 cat("median is",median)
```

R code Exa 2.3 Median for Set

```
1 set<-c(2,9,11,5,6,27)
```

```
2 median <- median(set)
3 cat("Median for the set of measurements is",median)
```

R code Exa 2.5 Variance and Standard Deviation

```
1 measurement<-c(5,7,1,2,4)
2 variance <- var(measurement)
3 standard_deviation <- sd(measurement)
4 cat("the variance is",variance)
5 cat("the standard deviation is",standard_deviation)
```

R code Exa 2.6 Tchebysheff theorem

```
1 x_bar <- 75
2 variance <- 100
3 standard_deviation <- sqrt(variance)
4 lower1 <- x_bar - 2 * standard_deviation
5 upper1 <- x_bar + 2 * standard_deviation
6 lower2 <- x_bar - 3 * standard_deviation
7 upper2 <- x_bar + 3 * standard_deviation
8 cat("atleast 3/4 of the 25 measurements lie in the
    interval",lower1,"to",upper1,".")
9 cat("atleast 8/9 of the 25 measurements lie in the
    interval",lower2,"to",upper2,".")
```

R code Exa 2.7 Empirical Rule

```
1 x_bar <- 12.8
2 standard_deviation <- 1.7
3 lower1 <- x_bar - 1 * standard_deviation
```



```

4 upper1 <- x_bar + 1 * standard_deviation
5 lower2 <- x_bar - 2 * standard_deviation
6 upper2 <- x_bar + 2 * standard_deviation
7 lower3 <- x_bar - 3 * standard_deviation
8 upper3 <- x_bar + 3 * standard_deviation
9 cat("approximately 68% of measurements lie in the
    interval", lower1, "to", upper1, ".")
10 cat("approximately 95% of measurements lie in the
    interval", lower2, "to", upper2, ".")
11 cat("approximately 99.7% of measurements lie in the
    interval", lower3, "to", upper3, ".")

```

R code Exa 2.9 Range Approximation

```

1 measurements <- c(5, 7, 1, 2, 4)
2 x <- range(measurements)
3 range <- x[2] - x[1]
4 sd <- range / 4
5 cat("standard deviation from range approximation is"
    , sd)
6 #the value of standard deviation from range
    approximation is not accurate

```

R code Exa 2.10 Range Approximation

```

1 data <- c
    (26.1, 26.0, 14.5, 29.3, 19.7, 22.1, 21.2, 26.6, 31.9, 25.0, 15.9, 20.8, 20.2)
2 x <- range(data)
3 range <- x[2] - x[1]
4 sd <- range / 4
5 cat("standard deviation from range approximation is"
    , sd)

```

R code Exa 2.11 Z Score

```
1 measurement<-c(1,1,0,15,2,3,4,0,1,3)
2 mean <- mean(measurement)
3 s <- sd(measurement)
4 x <- 15
5 cat("z_score is", (x-mean)/s)
```

R code Exa 2.13 Lower and Upper Quartiles

```
1 measurement<-c(16,25,4,18,11,13,20,8,11,9)
2 cat("Lower quantile is", quantile(measurement, 0.25))
3 cat("Upper quantile is", quantile(measurement, 0.75))
4 cat("IQR =", IQR(measurement))
5 summary(measurement)
6 #the answers provided in the textbook is wrong
```

R code Exa 2.14 Box Plot and Outlier

```
1 data<-c(340,300,520,340,320,290,260,330)
2 boxplot(data, horizontal = TRUE)
3 summary(data)
4 cat("q1 =", quantile(data, 0.25))
5 cat("m =", quantile(data, 0.50))
6 cat("q3 =", quantile(data, 0.75))
7 IQR(data)
8 boxplot.stats(data)
9 #outlier is 520
10 #the answers provided in the textbook is wrong
```


Chapter 3

DESCRIBING BIVARIATE DATA

R code Exa 3.1 Side by Side Bar Chart

```
1 data<- matrix(c(94.8,65.9,56.4,118.1,76.0,65.1),ncol
  =3,byrow=TRUE)
2 colnames(data) <- c("Full Professor","Associate
  Professor","Assistant Professor")
3 rownames(data) <- c("public","private")
4 data <- as.table(data)
5 data
6 barplot(data, ylab="Average Salary ($ Thousands)",
  ylim=c(0,120), col=c("blue","grey"),
7      legend = c("public","private"), beside=TRUE)
```

R code Exa 3.2 Comparative Charts

```
1 public<-c(24,57,69)
2 private<-c(60,78,112)
3 private_percent<-(private*100)/250
```

```

4 public_percent<-(public*100)/150
5 private_percent
6 label<-paste(public_percent,"%",sep=" ")
7 label1<-paste(private_percent,"%",sep=" ")
8 par(mfrow = c(1,2))
9 color<-c("white","aliceblue","cadetblue1")
10 pie(private_percent,labels = label1,clockwise = TRUE
      ,main="Private",col = color)
11 legend("bottomleft",c("Full Professor","Associate
      Professor","Assistant Professor"),cex=0.35,fill =
      color)
12 pie(public_percent,labels = label,clockwise = TRUE,
      main="Public",col = color)
13 legend("bottomleft",c("Full Professor","Associate
      Professor","Assistant Professor"),cex=0.35,fill =
      color)
14 cat("proportion of assistant professor is roughly
      same for both private and public colleges")
15 cat("public colleges have smaller proportion of full
      professors and a large proportion of associate
      professors")

```

R code Exa 3.3 Scatterplot

```

1 x<-c(2,2,3,4,1,5)
2 y<-c(95.75,110.19,118.33,150.92,85.86,180.62)
3 plot(x,y)

```

R code Exa 3.4 Scatterplot for Data

```

1 #install package("ggplot2")
2 #install library("ggplot2")
3 cases<-c(23,21,19,18,15,17,19,20,25,24)

```

```

4 price<-c(10,10,11,11,12,12,13,13,14,14)
5 DF<-data.frame(price,cases)
6 library(ggplot2)
7 #read library("ggplot2")
8 ggplot(DF,aes(price,cases)) + geom_point()
9 cat("there exists Linear relationship ")

```

R code Exa 3.5 Scatter Plot for Size of Living Area and Selling Price

```

1 x<-c
  (1360,1940,1750,1550,1790,1750,2230,1600,1450,1870,2210,1480)

2 y<-c
  (278.5,375.7,339.5,329.8,295.6,310.3,460.5,305.2,288.6,365.7,425.3)

3 plot(x,y)
4 cat("Plot represents the linear pattern in data")

```

R code Exa 3.6 Correlation Coefficient

```

1 x<-c
  (1360,1940,1750,1550,1790,1750,2230,1600,1450,1870,2210,1480)

2 y<-c
  (278.5,375.7,339.5,329.8,295.6,310.3,460.5,305.2,288.6,365.7,425.3)

3 correlation_Coefficient <- round(cor(x, y),4)
4 cat("correlation coefficient of x and y is",
  correlation_Coefficient)

```

R code Exa 3.7 Line and Dataplot

```
1 #install package("ggplot2")
2 #install library("ggplot2")
3 x<-c(2,3,4,5,6,7)
4 y<-c(6.00,7.50,8.00,12.00,13.00,15.50)
5 install.packages("ggplot2")
6 DF<-data.frame(x,y)
7 library(ggplot2)
8 #read library("ggplot2")
9 ggplot(DF,aes(x,y))+geom_point()+geom_smooth(method=
  "lm" , se= F)
```

Chapter 4

PROBABILITY AND PROBABILITY DISTRIBUTIONS

R code Exa 4.5 Probabilities Using Simple Events

```
1 E2 <- 1/4;  
2 E3 <- 1/4;  
3 cat("Probability of observing exactly one head in  
  two tosses is",E2+E3)
```

R code Exa 4.6 Probabilities of Blood Phenotypes

```
1 A <- 0.41;  
2 B <- 0.10;  
3 AB <- 0.04;  
4 o <- 0.45;  
5 cat("Probability that person is either type A or  
  type AB is",A+AB)
```

R code Exa 4.7 Probability of Candies Problem

```
1 R1R2 <- 1/6;  
2 R2R1 <- 1/6;  
3 cat("Probability that both candies are red is",R1R2  
    + R2R1)
```

R code Exa 4.8 Probability Using Counting Rules

```
1 m <- 6;  
2 n <- 6;  
3 cat("Total number of simple events in the sample  
    space S are",m*n)
```

R code Exa 4.9 Candy Dish

```
1 first_candy <- 3;  
2 second_candy <- 2;  
3 cat("Simple events in the sample space S are",first_  
    candy * second_candy)
```

R code Exa 4.10 Simple Events of Coins

```
1 coin_ways <- 2  
2 cat("Simple events in the sample space when three  
    coins are tossed are",coin_ways * coin_ways *  
    coin_ways)
```

R code Exa 4.11 Routes

```
1 Routes_A_B <- 3;
2 Routes_B_C <- 4;
3 Routes_C_D <- 3;
4 cat("Possible A to D routes are",Routes_A_B * Routes
    _B_C * Routes_C_D)
```

R code Exa 4.12 Simple Events Using Permutation

```
1 simple_events <- factorial(50)/factorial(50-3);
2 cat("Total Simple events are",simple_events)
```

R code Exa 4.13 Permutaion of Tests

```
1 Total_tests <- factorial(5)/factorial(5-5);
2 cat("Total number of tests are",Total_tests)
```

R code Exa 4.14 Counting Rule for Combinations

```
1 suppliers <- 5
2 choose <- 3
3 cat("Total number of ways in which three suppliers
    are to be choosen from five are",choose(suppliers
    , choose))
```

R code Exa 4.15 Manufacturers Problem

```
1 Total_ways <- 10;
2 Two_out_of_best <- choose(3, 2);
3 one_out_of_not_best <- choose(2, 1);
4 cat("Probability of selecting exactly two of best
      three are", (Two_out_of_best * one_out_of_not_best
      ) / Total_ways)
```

R code Exa 4.17 Oil Prospecting Firm Problem

```
1 Prob_A <- 0.80;
2 Prob_B <- 0.18;
3 Prob_c <- 0.02;
4 cat("probability of A or B", Prob_A + Prob_B)
5 cat("probability of B or C", Prob_B + Prob_c)
```

R code Exa 4.18 College Education Expenses Problem

```
1 Child_Too_High <- 0.35;
2 Child_Right_Amount <- 0.08;
3 Child_Too_Little <- 0.01;
4 No_Child_Too_High <- 0.25;
5 No_Child_Right_Amount <- 0.20;
6 No_Child_Too_Little <- 0.11;
7 too_high <- 0.60;
8 right_ammount <- 0.28;
9 too_little <- 0.12;
10 child_college <- Child_Too_High + Child_Too_Little +
    Child_Right_Amount;
```

```

11 cat("probability that respondent has a child in
    college is",child_college)
12 cat("probability that respondent does not have a
    child in college is",1-child_college)
13 cat("probability that respondent has child in
    college and with too high load is",too_high +
    child_college - Child_Too_High)

```

R code Exa 4.19 Multiplication Rule for Probability

```

1 prob_r <- 2/8;
2 prob_g <- 6/8;
3 prob_rr <- 1/7;
4 prob_rg <- 6/7;
5 prob_gr <- 2/7;
6 prob_gg <- 5/7;
7 cat("probability that child choose the two red toys
    is",prob_r * prob_rr)

```

R code Exa 4.20 Independent Events

```

1 s <- c("hh","ht","th","tt")
2 prob_a <- 1/2
3 prob_b <- 1/2
4 prob_a_and_b <- 1/4
5 if((prob_a * prob_b) == prob_a_and_b){
6   print("events must be independent")
7 }else{
8   print("events are not independent")
9 }

```

R code Exa 4.21 Multiplication Rule for Independent Events

```
1 Child_Too <- 0.35;
2 Child_Right_Amount <- 0.08;
3 Child_Too_Little <- 0.01;
4 No_Child_Too_High <- 0.25;
5 No_Child_Right_Amount <- 0.20;
6 No_Child_Too_Little <- 0.11;
7 too_high <- 0.60;
8 right_amount <- 0.28;
9 too_little <- 0.12;
10 child_college <- 0.44;
11 No_child_college <- 0.56;
12 x = too_high * child_college
13 cat("x and child_college values are not same so both
      events are dependent ")
```

R code Exa 4.22 Cards Problem

```
1 ace_on_first <- 4/52;
2 ten_on_second_when_ace_on_first <- 4/51;
3 ten_on_first <- 4/52;
4 ace_on_Second <- 4/51;
5 x <- ace_on_first * ten_on_second_when_ace_on_first
6 y <- ten_on_first * ace_on_Second
7 cat("probability of ace on first and ten on second
      draw",x)
8 cat("probability of ten on first and ace on second
      draw",y)
9 cat("probability that the draw includes an ace and a
      ten is",x+y)
```

R code Exa 4.23 Law of Total Probability

```

1 pg1 <- 0.09
2 pg2 <- 0.20
3 pg3 <- 0.31
4 pg4 <- 0.23
5 pg5 <- 0.17
6 p_a_g1 <- 0.26
7 p_a_g2 <- 0.20
8 p_a_g3 <- 0.13
9 p_a_g4 <- 0.18
10 p_a_g5 <- 0.14
11 pA <- (pg1 * p_a_g1) + (pg2 * p_a_g2) +(pg3 * p_a_g3
    ) +(pg4 * p_a_g4) +(pg5 * p_a_g5)
12 cat("the required probability is",pA)

```

R code Exa 4.24 Sneakers Problem

```

1 pg1 <- 0.09
2 pg2 <- 0.20
3 pg3 <- 0.31
4 pg4 <- 0.23
5 pg5 <- 0.17
6 p_a_g1 <- 0.26
7 p_a_g2 <- 0.20
8 p_a_g3 <- 0.13
9 p_a_g4 <- 0.18
10 p_a_g5 <- 0.14
11 required_probability <- (pg5 * p_a_g5) / ((pg1 * p_a
    _g1) + (pg2 * p_a_g2) +(pg3 * p_a_g3) +(pg4 * p_a
    _g4) +(pg5 * p_a_g5))
12 cat("the required probability is",required_
    probability)

```

R code Exa 4.26 Mean Variance and Standard Deviation

```

1 x <- c(0,1,2,3,4,5)
2 prob_x <- c(0.10,0.40,0.20,0.15,0.10,0.05)
3 k<- c(x*prob_x)
4 mean <- weighted.mean(x, prob_x)
5 l <- c((x-mean)*(x-mean))
6 m <- c(l*prob_x)
7 variance <- sum(m)
8 standard_deviation=round(sqrt(variance),2)
9 cat("mean is",mean)
10 cat("variance is",variance)
11 cat("standard deviation is",standard_deviation)

```

R code Exa 4.27 Expected Gain

```

1 gain<-c(-20,23980)
2 prob_gain<-c((7998/8000),(2/8000))
3 prob_gain
4 expected_gain <- weighted.mean(gain, prob_gain)
5 #expected_gain is in dollar
6 cat("expected gain per lottery would be a loss of",
      expected_gain)

```

Chapter 5

SEVERAL USEFUL DISCRETE DISTRIBUTIONS

R code Exa 5.3 Binomial Probability Distribution

```
1 x <- 2;
2 n<- 10;
3 p <- 0.1;
4 prob <- round((dbinom(x,n,p)),4)
5 cat("the required probability is",prob)
```

R code Exa 5.4 Probabilities for free throws

```
1 total_throws <- 4;
2 prob <- 0.8;
3 x <- 2;
4 y <- 0;
5 case_one <- dbinom(x,total_throws,prob)
6 cat("probability that he will make exactly two free
    throws is",case_one)
7 case_two <- 1-dbinom(y,total_throws,prob)
```



```
8 cat("probability that he will make atleast one free  
   throw is",case_two)
```

R code Exa 5.5 Probabilities for Successes

```
1 total <- 5;  
2 prob <- 0.6;  
3 x <- 3;  
4 y <- 2  
5 case_one <- pbinom(x,total,prob)-pbinom(y,total,prob  
   )  
6 cat("probability of exactly three successes is",case_  
   _one)  
7 case_two <- 1-pbinom(y,total,prob)  
8 cat("probability of three or ore successes is",case_  
   two)  
9 #the answer may slightly vary due to rounding off  
   values
```

R code Exa 5.6 Probability of Survivors

```
1 total <- 10;  
2 prob <- 0.5;  
3 x <- 7;  
4 eight_or_more <- 1 - pbinom(x,10,0.5)  
5 cat("probability of exactly three success is",eight_  
   or_more)
```

R code Exa 5.7 Multiple Choice Test

```

1 prob_correct <- 0.2
2 prob_incorrect <- 1 - prob_correct
3 n <- 100
4 mu0 <- n * prob_correct
5 sigma <- sqrt(n * prob_correct * prob_incorrect)
6 cat("a large proportion of score will lie within two
      standard deviations of the mean, or from", (mu0 -
        2 * sigma), "to", (mu0 + 2 * sigma), "." )
7 cat("almost all the score will lie within three
      standard deviations of the mean, or from", (mu0 -
        3 * sigma), "to", (mu0 + 3 * sigma), "." )
8 cat("guessing will be better than zero score but the
      student will not pass the exam")

```

R code Exa 5.8 Traffic Accidents using Poisson Distribution

```

1 mean <- 2;
2 accidents_in_case_one <- 0;
3 case_one <- round((dpois(accidents_in_case_one, mean)
  ),6)
4 cat("probability of no accident on this section of
      highway during a 1-week period is", case_one)
5 case_two_mean <- 2*mean;
6 case_two_mean
7 case_two <- round((dpois(0, case_two_mean)+ dpois(1,
  case_two_mean) + dpois(2, case_two_mean) + dpois
  (3, case_two_mean)),6)
8 cat("probability of atmost three accidetns on this
      section of highway during a 2-week period is",
      case_two)

```

R code Exa 5.9 Life Insurance Company

```

1 total_men <- 5000;
2 prob <- 0.001;
3 claims <- 4;
4 mean <- total_men * prob
5 exact_prob <- round((dpois(claims,mean)),3)
6 cat("probability that the company will have to pay 4
      claims during a given year is",exact_prob)

```

R code Exa 5.10 Lawn Mowers Problem

```

1 total <- 1000;
2 prob <- 0.001;
3 mean <- total * prob;
4 none_defective <- dpois(0,mean)
5 cat("probability that none is defective is",none_
      defective)
6 three_defective <- dpois(3,mean)
7 cat("probability that three is defective",three_
      defective)
8 four_defective <- dpois(4,mean)
9 cat("probability that four are defective",four_
      defective)
10 #the asnwer may slightly vary due to rounding off

```

R code Exa 5.11 Probability Distribution Mean Variance

```

1 total_bottles <- 12;
2 spoiled_wine <- 3;
3 sample <- 4;
4 prob_zero <- (choose(spoiled_wine,0) * choose(total_
      bottles - spoiled_wine,(sample - 0)))/choose(
      total_bottles,sample)

```

```

5 cat("probability distribution of no bottle of
   spoiled wine is",prob_zero)
6 prob_one <- (choose(spoiled_wine,1) * choose(total_
   bottles - spoiled_wine,(sample - 1)))/choose(
   total_bottles,sample)
7 cat("probability distribution of one bottle of
   spoiled wine in sample is",prob_one)
8 prob_two <- (choose(spoiled_wine,2) * choose(total_
   bottles - spoiled_wine,(sample - 2)))/choose(
   total_bottles,sample)
9 cat("probability distribution of two bottle of
   spoiled wine in sample is",prob_two)
10 prob_three <- (choose(spoiled_wine,3) * choose(total_
   _bottles - spoiled_wine,(sample - 3)))/choose(
   total_bottles,sample)
11 cat("probability distribution of three bottle of
   spoiled wine in sample is",prob_three)
12 mean = sample * (spoiled_wine/total_bottles)
13 cat("mean is",mean)
14 variance <- sample * (spoiled_wine/total_bottles)*
   (9/total_bottles)*((total_bottles-sample)/11)
15 cat("variance is",variance)
16 # "The answer may slightly vary due to rounding off
   values"

```

R code Exa 5.12 Hypergeometric Probability Distribution

```

1 total_items <- 20;
2 sample_items <- 5;
3 defective <- 4;
4 prob_accept_lot <- choose(defective,0) * choose(
   total_items - defective,(sample_items - 0))/
   choose(total_items,sample_items) + choose(
   defective,1) * choose(total_items - defective,(
   sample_items - 1))/choose(total_items,sample_

```

```
    items)  
5 cat("probability of get accepted is",prob_accept_lot  
    )
```

Chapter 6

THE NORMAL PROBABILITY DISTRIBUTION

R code Exa 6.1 Probability

```
1 given_value <- 0.2
2 required_probability <- punif(given_value, max =
    0.5, min = -0.5) - punif(- given_value, max =
    0.5, min = -0.5)
3 cat("required probability is",required_probability)
```

R code Exa 6.2 Probability of waiting time

```
1 average_waiting_time <- 5
2 waiting_time <- 10
3 required_probability <- 1 - pexp(waiting_time, rate
    = 1 / average_waiting_time)
4 cat("the required probability is",required_
    probability)
```

R code Exa 6.3 Normal Probability Distribution

```
1 point <- 1.63;
2 prob <- round((pnorm(point)),4);
3 cat("the required probability is",prob)
```

R code Exa 6.4 Normal Probability Distribution

```
1 point <- -0.5;
2 prob <- 1-pnorm(point);
3 cat("the required probability is",round(prob,4))
```

R code Exa 6.5 Normal Probability Distribution

```
1 point_one <- -0.5;
2 point_two <- 1.0;
3 prob_one <- pnorm(point_one);
4 prob_two <- pnorm(point_two);
5 prob <- round((prob_two - prob_one),4);
6 cat("The required probability is",prob)
```

R code Exa 6.6 Normal Probability Distribution

```
1 point_one <- 1;
2 point_two <- 2;
3 prob_one <- round(pnorm(point_one) - pnorm(-point_
  one),5);
```

```

4 prob_two <- round(pnorm(point_two) - pnorm(-point_
    two),4);
5 cat(" probability that a normally distributed random
    variable will fall within One standard deviation
    of its mean",prob_one)
6 cat(" probability that a normally distributed random
    variable will fall within Two standard
    deviations of its mean",prob_two)
7 #the answers may slightly vary due to rounding off
    values

```

R code Exa 6.7 z value

```

1 shaded_area <- 0.95
2 A1 <- (1 - shaded_area) / 2
3 cumulative_Area_left_of_z0 <- shaded_area + A1
4 z_value <- round(qnorm(cumulative_Area_left_of_z0)
    ,2)
5 cat("the required z value is",z_value)

```

R code Exa 6.8 Normal Distributed Random Variable

```

1 mean <- 10;
2 standard_deviation <- 2;
3 lower_X <- 11;
4 upper_x <- 13.6;
5 prob <- round((pnorm(upper_x, mean, standard_
    deviation) - pnorm(lower_X, mean, standard_
    deviation)),4);
6 cat("the required probability is",prob)

```

R code Exa 6.9 Gasoline use for Compact car

```
1 mean <- 25.5;
2 standard_deviation <- 4.5;
3 value_x <- 30;
4 prob <- 1 - pnorm(value_x, mean, standard_deviation)
  ;
5 percentage <- prob *100;
6 cat("the required percentage is",round(percentage,2)
  )
```

R code Exa 6.10 Gasoline Use Rate

```
1 mean <- 25.5;
2 standard_deviation <- 4.5;
3 percent <- 95 / 100;
4 cat("The gasoline use rate for the new car must be",
  qnorm(percent, mean, standard_deviation))
```

R code Exa 6.11 Normal Approximation to Binomial Distribution

```
1 total <- 25;
2 prob <- 0.5;
3 actual_prob <- round((pbinom(10,total,prob)-pbinom
  (7,total,prob)),4)
4 mean <- total * prob;
5 standard_deviation <- sqrt(total*prob*0.5)
6 x_lower <- 7.5;
7 x_upper <- 10.5;
8 approx_prob <- round(pnorm(x_upper, mean, standard_
  deviation) - pnorm(x_lower, mean, standard_
  deviation) ,4)
9 cat("actual probability is",actual_prob)
```

```
10 cat("approximate probability is",approx_prob)
11 cat("approximate and actual probability are quite
    close")
```

R code Exa 6.12 Electric Fuse

```
1 x_value <- 26.5;
2 total <- 1000;
3 defective <- 0.02;
4 reliability <- 0.98;
5 mean = total * defective;
6 standard_deviation <- round( sqrt((total * defective)
    * reliability),2)
7 approx_prob <- 1 - round(pnorm(x_value, mean,
    standard_deviation),4)
8 cat("Approximate probability of observing 27 or more
    defective is",approx_prob)
9 #the answers may slightly vary due to rounding off
    values
```

R code Exa 6.13 Soft Drinks Brand

```
1 consumers <- 2500;
2 brand_share <- 10;
3 prob_correct <- brand_share/100;
4 prob_not_correct <- 1 - prob_correct;
5 mean = consumers * prob_correct;
6 standard_deviation <- sqrt(consumers * prob_correct
    * prob_not_correct)
7 x_value <- 211.5;
8 required_prob <- round((pnorm(x_value, mean,
    standard_deviation)),4)
```

```
9 cat("probability of observing 211 or fewer consumers  
   who prefer her band of soft drink is",required_  
   prob)
```

Chapter 7

SAMPLING DISTRIBUTIONS

R code Exa 7.1 Simple Random Sample

```
1 N <- 1000
2 n <- 5
3 sample(N, n, replace = FALSE, prob = NULL)
```

R code Exa 7.4 Alzheimer disease

```
1 sample_size <- 30;
2 x_value <- 7;
3 mean <- 8;
4 sd <- 4;
5 prob_less_7 <- round(pnorm(x_value, mean, round((sd
  / sqrt(sample_size)),2)),6)
6 cat("The approximate probability duration for
  average duration is less than 7 years is",prob_
  less_7)
7 prob_exceed_7 <- round((1 - prob_less_7),5)
8 cat("The approximate probability for average duation
  exceeds 7 years is",prob_exceed_7)
```

```

9 x1_value <- 9;
10 prob_of_interest <- (pnorm(x1_value, mean, round((sd
    / sqrt(sample_size)),2))) - (pnorm(x_value, mean
    , round((sd / sqrt(sample_size)),2)))
11 cat("The approximate probability for average
    duration lies within 1 year of the population
    mean=8 is",prob_of_interest)
12 #"The answers may slightly vary due to rounding off
    values"

```

R code Exa 7.5 Sample Distribution of Sample Mean

```

1 no_of_bottles <- 10;
2 mean <- 12.1;
3 x_value <- 12;
4 standard_Deviation <- 0.2;
5 standard_error <- standard_Deviation/sqrt(no_of_
    bottles)
6 required_prob <- round((pnorm(x_value, mean,
    standard_error)),4)
7 cat("The required probability is",required_prob)

```

R code Exa 7.6 Sample Distribution of Sample Proportion

```

1 sample_space <- 500;
2 mean <- 0.60;
3 standard_error <- sqrt((mean * (1-mean))/sample_
    space)
4 standard_error <- round(standard_error,3)
5 cat("standard error is",standard_error)
6 p <- 2 * standard_error
7 cat("required value is",p)

```

R code Exa 7.7 Probability for Sample Proportion

```
1 # textbook refered to example 7.6 for values
2 sample_space <- 500;
3 proportion <- 0.55;
4 observed_value <- 0.60;
5 standard_error <- round(sqrt((proportion * (1-
    proportion))/sample_space),4)
6 cat("standard error is",standard_error)
7 req_prob <- round(1 - pnorm(observed_value,
    proportion, standard_error),4)
8 cat("probobality of observing a sample proportion as
    large as or larger than the observed value is",
    req_prob)
```

R code Exa 7.8 Xbar Chart

```
1 #install package (" qicharts")
2 #install library (" qicharts")
3 install.packages(" qicharts")
4 library(qicharts)
5 n <- 4
6 bearing1 <- c
    (0.992,1.015,0.988,0.996,1.015,1.000,0.989,0.994,1.018,0.997,1.020)
7 bearing2 <- c
    (1.007,0.984,0.993,1.020,1.006,0.982,1.009,1.010,1.016,1.005,0.980)
8 bearing3 <- c
    (1.016,0.976,1.011,1.004,1.002,1.005,1.019,1.009,0.990,0.989,1.000)
```

```

9 bearing4 <- c
  (0.991,1.000,0.981,0.999,1.001,0.989,0.994,0.990,1.011,1.001,0.98
10 sample <- c(1:25)
11 measurement <- c(bearing1 + bearing2 + bearing3 +
  bearing4)
12 sample_mean <- c((bearing1 + bearing2 + bearing3 +
  bearing4) / n)
13 df <- data.frame(sample, bearing1, bearing2,
  bearing3, bearing4,sample_mean)
14 df
15 qic(sample_mean, x = sample, data = df, chart = 'i',
  main = 'Xbar chart of Diameter', xlab = 'sample',
  ylab = 'sample mean')
16 #The results may slightly vary due to rounding off
  values

```

R code Exa 7.9 Control Chart

```

1 #install package ("qcc")
2 #install library ("qcc")
3 install.packages("qcc")
4 library(qcc)
5 proportion <- c
  (0.0200,0.0125,0.0225,0.0100,0.0150,0.0200,0.0275,0.0175,0.0200,0
6 n <- 400
7 defects <- c(proportion * n)
8 qcc(defects, type = "p", sizes = n, xlab = "day",
  ylab = "proportion")

```

Chapter 8

LARGE SAMPLE ESTIMATION

R code Exa 8.4 Point Estimation of Population Parameter

```
1 sample <- 50;
2 standard_deviation <- 105;
3 margin_of_error <- 1.96 * (standard_deviation/sqrt(
  sample))
4 margin_of_error
5 cat("the average weight of all arctic polar bears
  are within more or less of 29 pounds of sample
  estimate of 980 pounds")
```

R code Exa 8.5 Estimation of True Population

```
1 sample <- 100;
2 p <- 0.73;
3 q <- 1 - p;
4 k <- sqrt((p * q)/sample);
5 margin_of_error <- round((1.96 * k),2)
```



```
6 cat("margin of error is",margin_of_error)
```

R code Exa 8.6 Construction of Confidence Interval

```
1 sample_mean <- 756;
2 sample_size <- 50;
3 standard_deviation <- 35;
4 standard_error <- qnorm(0.975) *( standard_deviation
  / sqrt(sample_size))
5 left <- round((sample_mean - standard_error),2);
6 right <- round((sample_mean + standard_error),2);
7 cat("95% confidence interval for sample mean is from
  ",left, "to" ,right," grams")
```

R code Exa 8.7 99 percent Confidence Interval

```
1 sample_mean <- 756;
2 sample_size <- 50;
3 standard_deviation <- 35;
4 z <- round((qnorm(0.995,lower.tail = T)),2);    #99%
  confidence interval-> 1 - 0.005 = 0.995
5 standard_error <- z *( standard_deviation / sqrt(
  sample_size))
6 left <- sample_mean - standard_error;
7 right <- sample_mean + standard_error;
8 cat("99% confidence interval is from ",left, "to" ,
  right, "grams per day")
```

R code Exa 8.8 Large Sample Confidence Interval

```

1 sample_size <- 985;
2 vote_for_republican <- 592;
3 point_estimate <- vote_for_republican/sample_size;
4 standard_error <- sqrt((point_estimate * (1 - point_
  estimate))/sample_size)
5 standard_error
6 point_estimate
7 coin_interval <- 90/100;
8 z <- qt((1+coin_interval)/2,df=sample_size-1)
9 value <- z * standard_error
10 left <- round((point_estimate - value),3);
11 right <- round((point_estimate + value),3);
12 cat("90% confidence interval is from ",left, "to" ,
  right)

```

R code Exa 8.9 Difference Between Two Sample Mean

```

1 miles_cover_by_type1 <- 26400;
2 miles_cover_by_type2 <- 25100;
3 type1_sample <- 100;
4 type2_sample <- 100;
5 variance1 <- 1440000;
6 variance2 <- 1960000;
7 point_estimate <- miles_cover_by_type1 - miles_cover
  _by_type2;
8 standard_error <- sqrt(((variance1)/type1_sample) +
  (variance2)/type2_sample);
9 confidence_interval_percent <- 0.99;
10 z_value <- round((qnorm(0.995)),2)
11 value <- z_value * standard_error;
12 left <- point_estimate - value;
13 right <- point_estimate + value;
14 cat("The difference in the average miles to wearout
  for the two types of tires is estimated to lie
  between ",left,"and",right,"miles of wear")

```

R code Exa 8.10 Confidence Interval for Difference

```
1 sample_size_men <- 50;
2 sample_size_women <- 50;
3 sample_mean_men <- 756;
4 sample_mean_women <- 762;
5 sample_standard_Deviation_men <- 35;
6 sample_standard_Deviation_women <- 30;
7 z_value <- 1.96
8 #we know from z table that for 95% confidence
   interval the z value is 1.96;
9 point_estimate <- sample_mean_men - sample_mean_women
   ;
10 standard_error <- sqrt(((sample_standard_Deviation_
   men * sample_standard_Deviation_men)/sample_size_
   men + (sample_standard_Deviation_women * sample_
   standard_Deviation_women)/sample_size_women))
11 value <- z_value * standard_error;
12 left <- round((point_estimate - value),2);
13 right <- round((point_estimate + value),2);
14 cat("The 95% confidence interval is from",left,"to",
   right)
```

R code Exa 8.11 Bond proposal problem

```
1 p1_cap <- 0.76
2 p2_cap <- 0.65
3 q1_cap <- 0.24
4 q2_cap <- 0.35
5 n1 <- 50
6 n2 <- 100
```

```

7 p1_cap - p2_cap
8 standard_error <- round(sqrt(((p1_cap * q1_cap) / n1
    ) + ((p2_cap * q2_cap) / n2 )),4)
9 standard_error
10 alpha <- 0.01          #at 99% confidence interval
    alpha = 0.01
11 z_0.005 <- qnorm( 1 - alpha/2)
12 lower_value <- (p1_cap - p2_cap) - z_0.005 *
    standard_error
13 upper_value <- (p1_cap - p2_cap) + z_0.005 *
    standard_error
14 cat("the interval is from",lower_value,"to",upper_
    value)
15 n <- 150
16 point_estimation <- 103/n
17 margin_of_error <- 1.96 * sqrt((point_estimation *
    (1 - point_estimation) / n))
18 margin_of_error1 <- - 1.96 * sqrt((point_estimation
    * (1 - point_estimation) / n))
19 cat("margin of error is",margin_of_error,"and",
    margin_of_error1, ".")
20 cat("interval is from",point_estimation - margin_of_
    error,"to",point_estimation + margin_of_error, ".")
    )

```

R code Exa 8.12 95 percent upper confidence bound

```

1 alpha <- 0.05  #at 95% confidence interval the alpha
    = 0.05
2 x_bar <- 10.3
3 n <- 40
4 s <- 0.31
5 se <- s / sqrt(n)
6 z_0.05 <- qnorm(1 - alpha)
7 z_0.05

```

```

8 ucb <- x_bar + z_0.05 * se
9 ucb
10 cat("the 95% upper confidence bound is",ucb)

```

R code Exa 8.13 Plastic Pipe

```

1 bound_b <- 0.04
2 alpha <- 0.10      #at 0.90 confidence coefficient
3 z_0.05 <- qnorm(1 - alpha/2)
4 z_0.05
5 p <- q <- 0.5
6 n <- ((z_0.05 * 0.5) / bound_b) ** 2
7 cat("the producer must include atleast",round(n,0),"
    wholesalers in survey")

```

R code Exa 8.14 Workers in Training groups

```

1 range <- 8
2 sigma1 <- sigma2 <- sigma <- range / 4
3 alpha <- 1 - 0.95 # at 0.95 confidence coefficient
4 z_0.05 <- qnorm(1 - alpha/2)
5 z_0.05
6 n <- (z_0.05 * sqrt(8)) ** 2
7 cat("there should be atleast",round(n,0),"workers in
    each group.")

```

Chapter 9

LARGE SAMPLE TESTS OF HYPOTHESES

R code Exa 9.3 Test Statistic

```
1 mean <- 14
2 s <- 2
3 n <- 100
4 se <- s / sqrt(n)
5 x_bar <- 15
6 z <- (x_bar - mean) / se
7 z
8 p_value <- 2 * pnorm(-abs(z))
9 cat("p-value is approximately zero")
```

R code Exa 9.4 Appropriate Hypothesis

```
1 xbar <- 725;           # sample mean
2 mu0 <- 670;            # hypothesized value
3 sigma <- 102;          # standard deviation
4 sample_size <- 40;     # sample size
```

```

5 z <- (xbar - mu0)/(sigma/sqrt(sample_size))
6 z                                     # test statistic
7 alpha <- .01
8 z.alpha <- qnorm(1 - alpha)
9 z.alpha                               # critical value
10 cat("The value of z is",z)
11 cat("critical value is",z.alpha)
12 cat("null hypothesis rejected ")
13 cat("average weekly earning for male are higher than
    average for female")
14 #the answer may slightly vary due to rounding off
    values

```

R code Exa 9.5 Appropriate Hypothesis

```

1 sample_mean <- 871;                  # sample mean
2 hypothesized_value <- 880;          #
    hypothesized value
3 sigma <- 21;                        # standard deviation
4 sample_size <- 50;                  # sample size
5 z <- round(((sample_mean - hypothesized_value)/(
    sigma/sqrt(sample_size))),2)
6 z                                   # test statistic
7 alpha <- .05
8 z.alpha <- round((qnorm(1 - alpha/2)),2)
9 z.alpha                             # critical value
10 cat("The value of z is",z)
11 cat("critical value is",z.alpha)
12 cat("null hypothesis can be rejected")
13 cat("she is reasonably confident that the decision
    is correct")

```

R code Exa 9.6 Calculation P Value

```

1 sample_mean <- 871;           # sample mean
2 hypothesized_value <- 880;    #
  hypothesized value
3 sigma <- 21;                 # standard deviation
4 sample_size <- 50;           # sample size
5 z_value <- (sample_mean - hypothesized_value)/(sigma
  /sqrt(sample_size))
6 z_value                      #test statistics
7 p_value <- round((1 - pnorm(-z_value)) + pnorm(z_
  value),4)
8 cat("p value is",p_value)
9 cat("reject null hypothesis at either 5% or 1%
  level of significance")

```

R code Exa 9.7 Daily Sodium Intake

```

1 sample_mean <- 3400;         # sample mean
2 hypothesized_value <- 3300;  #
  hypothesized value
3 sigma <- 1100;               # standard deviation
4 sample_size <- 100;          # sample size
5 z_value <- (sample_mean - hypothesized_value)/(sigma
  /sqrt(sample_size))
6 z_value                      # test statistic
7 alpha <- 0.05
8 z.alpha <- qnorm(1 - alpha)
9 z.alpha                      # critical value
10 cat("The value of z is",z_value)
11 cat("critical value is",z.alpha)
12 p_value <- 1 - pnorm(z_value)
13 cat("p value is",p_value)
14 cat("null hypothesis is not rejected")
15 cat("not enough evidence ")
16 #the answer may slightly vary due to rounding off
  values

```

R code Exa 9.8 Beta and power of beta

```
1 sample_mean <- 871;           # sample mean
2 hypothesized_value <- 880;    #
   hypothesized value
3 sigma <- 21;                 # standard deviation
4 sample_size <- 50;          # sample size
5 alpha <- .05
6 z.alpha <- round((qnorm(1 - alpha/2)),2)
7 z.alpha           # critical value
8 lower <- round(hypothesized_value - z.alpha * ((
   sigma/sqrt(sample_size))),2)
9 lower
10 upper <- round(hypothesized_value + z.alpha * ((
   sigma/sqrt(sample_size))),2)
11 upper
12 mu <- 870
13 z1 <- round(((lower - mu)/(sigma/sqrt(sample_size)))
   ,2)
14 z1
15 z2 <- round(((upper - mu)/(sigma/sqrt(sample_size)))
   ,2)
16 z2
17 beta <- round( 1 - pnorm( z1),4)
18 power_of_test <- 1 - beta
19 cat("beta is",beta)
20 cat("power of test is",power_of_test)
```

R code Exa 9.9 Car Ownership Affect

```
1 non_owners <- 100;
```

```

2 owners <- 100;
3 average_non_owner <- 2.70;
4 average_owner <- 2.54;
5 variance_non_owner <- 0.36;
6 variance_owner <- 0.40;
7 d_nod <- 0;
8 point_estimate <- average_non_owner - average_owner
;
9 standard_error <- sqrt(((variance_non_owner)/non_
    owners) + (variance_owner)/owners);
10 z = round(((point_estimate - d_nod)/standard_error)
    ,2);
11 cat("value of z is",z)
12 alpha <- .05
13 z.alpha <- round((qnorm(1 - alpha/2)),2)
14 z.alpha # critical value
15 cat("The value of z is",z)
16 cat("critical value is",z.alpha)
17 p_value <- round(((1-pnorm(z)) + pnorm(-z)),4)
18 cat("p value is",p_value)
19 cat("null hypothesis cannot be rejected and there
    is insufficient evidence")

```

R code Exa 9.10 Hypothesis Testing and Confidence Interval

```

1 # In textbook values are referred to example 9.9
2 non_owners <- 100;
3 owners <- 100;
4 average_non_owner <- 2.70;
5 average_owner <- 2.54;
6 variance_non_owner <- 0.36;
7 variance_owner <- 0.40;
8 d_nod <- 0;
9 point_estimate <- average_non_owner - average_owner
;

```

```

10 standard_error <- sqrt(((variance_non_owner)/non_
    owners) + (variance_owner)/owners);
11 confidence_interval_percent <- 0.95;
12 z_value <- qnorm(1-(1 - confidence_interval_percent)
    /2)
13 value = z_value * standard_error;
14 left = round((point_estimate - value),2);
15 right = round((point_estimate + value),2);
16 cat("The confidence interval is approximated from",
    left,"to",right)
17 cat("there is not enough evidence so we cannot
    conclude")

```

R code Exa 9.11 Hypothesis Testing and P Value

```

1 hypothesized_value <- 0.2;
2 observed_value <- 15/100;
3 standard_error <- sqrt((hypothesized_value * (1-
    hypothesized_value))/100)
4 z_value <- (observed_value - hypothesized_value)/
    standard_error;
5 p_value <- pnorm(z_value)
6 cat("pvalue is",p_value)
7 cat("null hypothesis cannot be rejected so there is
    insufficient evidence to make conclusion")

```

R code Exa 9.12 Hypothesis Test for Difference Between Two Binomial Proportions

```

1 admitted_men <- 52;
2 admitted_women <- 23;
3 sample_men <- 1000;
4 sample_women <- 1000;

```

```

5 p1_value <- admitted_men/sample_men;
6 p2_value <- admitted_women/sample_women;
7 pooled_estimate <- (admitted_men + admitted_women)/(
    sample_men + sample_women);
8 standard_error <- sqrt(pooled_estimate * (1 - pooled
    _estimate) * ((1/1000) + (1/1000)))
9 test_statistics <- (p1_value - p2_value)/standard_
    error
10 test_statistics
11 alpha <- 0.05;
12 k <- abs(qnorm(alpha))
13 lower_bound <- (p1_value - p2_value) - k * sqrt((p1
    _value * (1 - p1_value)/sample_men) + (p2_value *
    (1 - p2_value)/sample_women))
14 cat("Lowest likely value for the difference is",
    lower_bound)
15 cat("the data present sufficient evidence to
    indicate that the percentage of men entering the
    hospital because of heart disease is higher than
    women")

```

Chapter 10

INFERENCE FROM SMALL SAMPLES

R code Exa 10.2 Students T Distribution

```
1 sample_size <- 10;  
2 t <- round((qt(p = 0.01, df = sample_size - 1 ,lower  
   .tail = T)),3)  
3 cat("value of t is",t)
```

R code Exa 10.3 Average Weight of Diamonds

```
1 weights <- c(0.46,0.61,0.52,0.48,0.57,0.54)  
2 t.test(weights, mu = 0.5, alternative = "greater",  
   conf.level = 0.95)  
3 cat("the range of possible values of mean is both  
   greater and smaller than 0.5 so there is no  
   sufficient evidence and our test fails.")
```

R code Exa 10.4 P value of paint problem

```
1 data <- c(310,311,412,368,447,376,303,410,365,350)
2 mean <- mean(data)
3 s <- sd(data)
4 mu0 <- 400
5 t.test(data,mu = mu0)
6 p.value <- t.test(data,mu = mu0)$p.value
7 p.value
8 cat(p.value < 0.05)
9 cat("Since p-value is less than 0.05 so null
    hypothesis is rejected and there is sufficient
    evidence to indicate the coverage differs from
    400")
```

R code Exa 10.5 Hypothesis Testing and T Value for Student grades

```
1 online <- c(32,37,35,28,41,44,35,31,34)
2 classroom <- c(35,31,29,25,34,40,27,32,31)
3 alpha <- 0.05
4 df <- length(online) + length(classroom) - 2
5 stem(online)
6 stem(classroom)
7 cat("stem and leaf plot of the data show at least a
    mounding pattern so the assumption of normality
    is not unreasonable.")
8 critical_value <- round((qt(p = 1 -alpha,df,lower.
    tail = T)),3)
9 cat("critical value is",critical_value)
10 t.test(online,classroom,alternative = "greater")
11 t <- t.test(online,classroom,alternative = "greater"
    )$statistic
12 if(t > critical_value){
13   print("reject the null hypothesis")
14 }else{
```

```

15 print("cannot reject the null hypothesis so there is
    insufficient evidence to indicate that the
    online course grades are higher than the
    conventional course grades at the 5 % level of
    significance.")
16 }

```

R code Exa 10.6 P Value For Student Grades

```

1 #values are referred to example 10.5 in textbook
2 online <-c (32,37,35,28,41,44,35,31,34)
3 classroom <-c (35,31,29,25,34,40,27,32,31)
4 p_value <- t.test(online,classroom,alternative = "
    greater")$p.value
5 cat("p-value =",p_value,"is geater than 0.05 ,most
    researchers would report the result as not
    significant.")

```

R code Exa 10.7 Lower confidence bound

```

1 online <- c(32,37,35,28,41,44,35,31,34)
2 classroom <- c(35,31,29,25,34,40,27,32,31)
3 t.test(online,classroom,alternative = "greater")
4 lower <- t.test(online,classroom,alternative = "
    greater")$conf.int[1]
5 cat("lower confidence bound is",lower)
6 cat("since the difference of equal means is included
    in the confidence interval so it is possible
    that two means are equal so there is insufficient
    evidence to indicate that the online average is
    higher than the classroom average.")
7 #the results may slightly vary due to rounding off
    values in textbook.

```

R code Exa 10.8 Tire problem

```
1 tire_A <- c(10.6,9.8,12.3,9.7,8.8)
2 tire_B <- c(10.2,9.4,11.8,9.1,8.3)
3 alpha <- 0.05
4 critical_value <- qt( 1 - alpha/2,df = 4)
5 k <- t.test(tire_A,tire_B, paired = TRUE,
              alternative = "two.sided")
6 test_statistics <- k[1]
7 cat(test_statistics > critical_value)
8 cat("test statistics from t.test() is larger than
      critical value hence there is difference in the
      mean wear for tire type A and B")
```

R code Exa 10.9 95 percent confidence interval

```
1 tire_A <- c(10.6,9.8,12.3,9.7,8.8)
2 tire_B <- c(10.2,9.4,11.8,9.1,8.3)
3 t.test(tire_A,tire_B, paired = TRUE, alternative = "
        two.sided")
```

R code Exa 10.11 Cement manufacturer

```
1 sigma_square <- 100
2 n <- 10
3 xbar <- 312
4 s_square <- 195
5 x_square <- ((n -1) * s_square)/sigma_square
6 alpha <- 0.05
```



```

7 df <- n - 1
8 x_square_0.05 <- qchisq(1 - alpha, df)
9 if(x_square > x_square_0.05){
10   print("reject the null hypothesis and the range of
      concrete strength measurements exceeds the
      manufacturer's claim")
11 }else{
12   print("accept the null hypothesis")
13 }

```

R code Exa 10.12 90 percent confidence interval

```

1 sigma_square <- 4
2 n <- 3
3 df <- n - 1
4 measurements <- c(4.1,5.2,10.2)
5 s_square <- var(measurements)
6 s_square
7 x_square <- ((n - 1) * s_square) / sigma_square
8 cat("p-value is greater than 0.10 so accept the null
      hypothesis")
9 alpha <- 0.10      #at 90% confidence interval alpha
      = 0.10
10 x_square_0.95 <- qchisq(alpha/2,df)
11 x_square_0.05 <- qchisq(1-alpha/2,df)
12 x_square_0.05
13 lower_value <- round((n - 1) * s_square/x_square_
      0.05,2)
14 upper_value <- round((n - 1) * s_square/x_square_
      0.95,2)
15 cat("the interval is from",lower_value,"to",upper_
      value)

```

R code Exa 10.13 F Value

```
1 f1 <- round(qf(0.95,6,9),2)           #1 - 0.05 = 0.95
2 f2 <- round(qf(0.95,5,10),2)
3 f3 <- round(qf(0.99,6,9),2)           #1 - 0.01 = 0.99
4 cat("value of f in case 1 is",f1)
5 cat("value of f in case 2 is",f2)
6 cat("value of f in case 3 is",f3)
```

R code Exa 10.14 Hypothesis Test For Equality of two Population Variances

```
1 variance1 <- 7.14;
2 variance2 <- 3.21;
3 n1 <- 10;
4 n2 <- 8;
5 df1 <- n1 - 1
6 df2 <- n2 - 1
7 alpha <- 0.05
8 rejection_region <- round(qf(1 - (alpha / 2), df1,
   df2),2)
9 rejection_region
10 test_statistics <- variance1/variance2;
11 cat("the calculated value of test statistics is",
   test_statistics)
12 if(test_statistics > rejection_region){
13   print("reject the null hypothesis")
14 }else{
15   print("Cannot reject null hypothesis and there is
   sufficient evidence to indicate a difference in
   the population variance")
16 }
```

R code Exa 10.15 Confidence Interval Estimate

```
1 variance1 <- 7.14;
2 variance2 <- 3.21;
3 n1 <- 10;
4 n2 <- 8;
5 df1 <- n1 - 1
6 df2 <- n2 - 1
7 alpha <- 0.05
8 f97 <- round(qf( 0.95, df1=9, df2=7),2)
9 f79 <- round(qf(.95, df1=7, df2=9),2)
10 lower_value <- round((variance1 / variance2) * (1 /
    f97),2)
11 upper_value <- round((variance1 / variance2) * (f79)
    ,2)
12 cat("the interval is between ",lower_value,"and",
    upper_value)
```

R code Exa 10.16 Impurities in the batch of chemical

```
1 x1bar <- 302
2 x2bar <- 3.0
3 s1_square <- 1.04
4 s2_square <- 0.51
5 n1 <- n2 <- 25
6 f <- (s1_square / s2_square)
7 df1 <- df2 <- n1 - 1
8 f_0.050 <- qf(1 - 0.050,df1,df2)
9 f_0.025 <- qf(1 - 0.025,df1,df2)
10 if(f > f_0.050 & f < f_0.025){
11     print("p-value lies between 0.025 and 0.05 and
        hence at 5% level null hypothesis is rejected")
12 }else{
13     print("null hypothesis is accepted")
14 }
```


Chapter 11

THE ANALYSIS OF VARIANCE

R code Exa 11.4 Analysis of Variance Table

```
1 no_breakfast<-c(8,7,9,13,10)
2 light_breakfast<-c(14,16,12,17,11)
3 full_breakfast<-c(10,12,16,15,12)
4
5 k <- 3;
6 n1 <- n2 <- n3 <- 5
7 n <- 15;
8
9
10 sum_square_X <- sum(no_breakfast) + sum(light_
    breakfast) + sum(full_breakfast)
11 cm <- (sum_square_X * sum_square_X)/n
12 cm
13 x <- sum(no_breakfast)
14 y <- sum(light_breakfast)
15 z <- sum(full_breakfast)
16 total_ss <- (8*8 + 7*7 + 9*9 + 13*13 + 10*10 + 14*14
    + 16*16 + 12*12 + 17*17 + 11*11 + 10*10 + 12*12
    + 16*16 + 15*15 + 12*12 ) - cm
```

```

17 total_ss
18 degree_of_freedom <- n-1
19 degree_of_freedom
20 sst <- ((x*x + y*y + z*z)/5) - cm
21 sst
22 df <- k - 1
23 sse <- total_ss -sst
24 sse
25 deg_of_freedom <- n - k
26 deg_of_freedom
27
28 combined<-data.frame(cbind(no_breakfast,light_
    breakfast,full_breakfast))
29 stacked<-stack(combined)
30 stacked
31 Anova_Results<-aov(values ~ ind,data = stacked)
32 summary(Anova_Results)

```

R code Exa 11.5 F test

```

1 no_breakfast<-c(8,7,9,13,10)
2 light_breakfast<-c(14,16,12,17,11)
3 full_breakfast<-c(10,12,16,15,12)
4
5 k <- 3;
6 n1 <- n2 <- n3 <- 5
7 n <- 15;
8
9
10 sum_square_X <- sum(no_breakfast) + sum(light_
    breakfast) + sum(full_breakfast)
11 cm <- (sum_square_X * sum_square_X)/n
12 cm
13 x <- sum(no_breakfast)
14 y <- sum(light_breakfast)

```

```

15 z <- sum(full_breakfast)
16 total_ss <- (8*8 + 7*7 + 9*9 + 13*13 + 10*10 + 14*14
      + 16*16 + 12*12 + 17*17 + 11*11 + 10*10 + 12*12
      + 16*16 + 15*15 + 12*12 ) - cm
17 total_ss
18 degree_of_freedom <- n-1
19 degree_of_freedom
20 sst <- ((x*x + y*y + z*z)/5) - cm
21 sst
22 df1 <- k - 1
23 df1
24 sse <- total_ss -sst
25 sse
26 df2 <- n - k
27 df2
28
29 combined<-data.frame(cbind(no_breakfast,light_
      breakfast,full_breakfast))
30 stacked<-stack(combined)
31 stacked
32 Anova_Results<-aov(values ~ ind,data = stacked)
33 summary(Anova_Results)
34 mse <- sse / (n - k)
35 mse
36 mst <- sst / (k - 1)
37 mst
38 f <- mst / mse
39 f
40 alpha <- 0.05
41 f_0.05 <- qf(1 - alpha, df1, df2)
42 if(f > f_0.05){
43   print("reject h0, there is sufficient evidence to
      indicate that at least one of the three average
      attention spans is different from at least one
      of the others")
44 }

```

R code Exa 11.6 CONFIDENCE INTERVALS FOR A SINGLE TREATMENT MEAN AND THE DIFFERENCE BETWEEN TWO TREATMENT MEANS

```
1 #values are referred to example 11_4in the textbook
2 no_breakfast<-c(8,7,9,13,10)
3 light_breakfast<-c(14,16,12,17,11)
4 full_breakfast<-c(10,12,16,15,12)
5 x1_bar <- mean(no_breakfast)
6 x2_bar <- mean(light_breakfast)
7 x3_bar <- mean(full_breakfast)
8
9 k <- 3;
10 n1 <- n2 <- n3 <- 5
11 n <- 15;
12
13
14 total_ss <- (8*8 + 7*7 + 9*9 + 13*13 + 10*10 + 14*14
15             + 16*16 + 12*12 + 17*17 + 11*11 + 10*10 + 12*12
16             + 16*16 + 15*15 + 12*12 ) - cm
17 total_ss
18 degree_of_freedom <- n-k
19 degree_of_freedom
20 sst <- ((x*x + y*y + z*z)/5) - cm
21 sst
22 sse <- total_ss -sst
23 sse
24 mse <- sse/(n-k)
25 s2 <- mse
26 s <- sqrt(s2)
27 alpha <- 0.05/2;
28 t_value <- qt(1-alpha,degree_of_freedom)
29 t_value
30 left1 <- round(x1_bar - (t_value * (s/sqrt(n1))),2)
```



```

29 right1 <- round(x1_bar + (t_value * (s/sqrt(n1))),2)
30 cat("confidence interval for no breakfast are
    between",left1,"and",right1,"minutes")
31 left2 <- round((x2_bar - x3_bar) - t_value*(sqrt(s2*
    ((1/n2) + (1/n3)))),2)
32 right2 <- round((x2_bar - x3_bar) + t_value*(sqrt(s2*
    *((1/n2) + (1/n3)))),2)
33 cat("confidence interval for the difference in the
    average attention spans for light versus full
    breakfast eaters are between",left2,"and",right2,
    "minutes")

```

R code Exa 11.7 Tukey method for paired comparison

```

1 no_breakfast<-c(8,7,9,13,10)
2 light_breakfast<-c(14,16,12,17,11)
3 full_breakfast<-c(10,12,16,15,12)
4
5 k <- 3;
6 n1 <- n2 <- n3 <- 5
7 n <- 15;
8
9 sum_square_X <- sum(no_breakfast) + sum(light_
    breakfast) + sum(full_breakfast)
10 cm <- (sum_square_X * sum_square_X)/n
11 cm
12 x <- sum(no_breakfast)
13 y <- sum(light_breakfast)
14 z <- sum(full_breakfast)
15 total_ss <- (8*8 + 7*7 + 9*9 + 13*13 + 10*10 + 14*14
    + 16*16 + 12*12 + 17*17 + 11*11 + 10*10 + 12*12
    + 16*16 + 15*15 + 12*12 ) - cm
16 total_ss
17 sst <- ((x*x + y*y + z*z)/5) - cm
18 sst

```

```

19 sse <- total_ss - sst
20 sse
21 df <- n - k
22 df
23 mse <- sse / (n - k)
24 mse
25 mst <- sst / (k - 1)
26 mst
27 f <- mst / mse
28 f
29 s <- sqrt(mse)
30 s
31 alpha <- 0.05
32 w <- (qtukey(1 - alpha, k, df)) * (s / sqrt(n1))
33 w
34 cat("the difference between no break fast and light
      breakfas exceeds w = ",w," so no breakfast and
      light breakfast are declared significantly
      different ")

```

R code Exa 11.8 Randomized Block Design

```

1 b <- 3
2 k <- 4
3 low <- c(27,24,31,23)
4 middle <- c(68,76,65,67)
5 high <- c(308,326,312,300)
6 df <- data.frame(low, middle, high)
7 data <- c((as.matrix(df)))
8 data
9 f <- c("a", "b", "c", "d")
10 company <- gl(k,1, b*k, factor(f))
11 usage <- gl(b, k, k * b)
12 model <- aov(data ~ usage + company)
13 model

```

```
14 summary(model)
```

R code Exa 11.9 Evidence Indication

```
1 b <- 3
2 k <- 4
3 low <- c(27,24,31,23)
4 middle <- c(68,76,65,67)
5 high <- c(308,326,312,300)
6 df <- data.frame(low, middle, high)
7 data <- c((as.matrix(df)))
8 data
9 f <- c("a","b","c","d")
10 company <- gl(k,1, b*k, factor(f))
11 usage <- gl(b, k, k * b)
12 model <- aov(data ~ usage + company)
13 model
14 summary(model)
15 p.value <- summary(model)[[1]][["Pr(>F)"]][[2]]
16 p.value
17 cat("since the p-value from anova test p.value=",p.
      value,"is too large to allow rejection of null
      hypothesis.")
18 cat("hence there is insufficient evidence to
      indicate a difference in the average monthly costs
      for the four companies.")
```

R code Exa 11.10 cell phone cost

```
1 A <- c(27,68,308)
2 B <- c(24,76,326)
3 C <- c(31,65,312)
4 D <- c(23,67,300)
```

```

5 t1 <- sum(A)
6 t2 <- sum(B)
7 t3 <- sum(C)
8 t4 <- sum(D)
9 b1 <- 105
10 b2 <- 276
11 b3 <- 1246
12 k <- 4;
13 n1 <- n2 <- n3 <- n4 <- 3
14 n <- 12;
15 b <- 3
16
17 sum_square_X <- sum(A) + sum(B) + sum(C) + sum(D)
18 sum_square_X
19 cm <- (sum_square_X * sum_square_X)/n
20 cm
21
22 l <- c(A,B,C,D)
23 l
24 sum_of_all <-sum( c(l * l))
25 sum_of_all
26 total_ss <- sum_of_all - cm
27 total_ss
28 sst <- (( t1 * t1 + t2 * t2 + t3 * t3 + t4 * t4)/ n1
    )- cm
29 sst
30 ssb <- ((b1 * b1 + b2 * b2 + b3 * b3) / k ) - cm
31 ssb
32 sse <- total_ss - sst - ssb
33 sse
34 t2_bar <- t2 / n2
35 t3_bar <- t3 / n3
36 mse <- sse / ((b - 1) * (k - 1))
37 mse
38 alpha <- 0.05
39 df <- (b - 1) * (k - 1)
40 lower_range <- round((t2_bar - t3_bar) - qt(1 -
    alpha/2,df) * sqrt(mse * (2 / b)),2)

```

```

41 upper_range <- round((t2_bar - t3_bar) + qt(1 - alpha
    /2,df) * sqrt(mse * (2 / b)),2)
42 cat("the difference between two average costs is
    estimated as betwen",lower_range,"and",upper_
    range, ".")

```

R code Exa 11.12 Two Way ANOVA

```

1 observation <- c
    (571,480,470,610,474,430,625,540,450,480,625,630,516,600,680,465,
2 supervisor <- c(1,1,1,1,1,1,1,1,1,2,2,2,2,2,2,2,2)
3 shift <- c("day","swing","night","day","swing","
    night","day","swing","night","day","swing","night
    ","day","swing","night","day","swing","night")
4 model <- aov(observation ~ supervisor * shift)
5 model
6 summary(model)

```

Chapter 12

LINEAR REGRESSION AND CORRELATION

R code Exa 12.1 Least Squares Prediction Line

```
1 x <- c(39,43,21,64,57,47,28,75,34,52)
2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 df <- data.frame(x, y)
4 lm(y ~ x, df)
5 cat("least square regression line is: ycap = 40.7842
    + 0.7656x")
```

R code Exa 12.2 Hypothesis Test for Linear Relationship

```
1 x <- c(39,43,21,64,57,47,28,75,34,52)
2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 x_square <- c(x**2)
4 y_square <- c(y**2)
5 xy <- c(x*y)
6 n <- 10;
7 sum_x <- sum(x)
```

```

8 sum_y <- sum(y)
9 sum_x_square <- sum(x_square)
10 sum_y_square <- sum(y_square)
11 sum_xy <- sum(xy)
12 s_xx <- sum_x_square - (sum_x * sum_x)/n
13 s_yy <- sum_y_square - (sum_y * sum_y)/n
14 s_xy <- sum_xy - (sum_x * sum_y)/n
15 y_bar <- sum(y)/n
16 x_bar <- sum(x)/n
17 b <- (s_xy/s_xx)
18 a <- y_bar - b*x_bar
19 a
20 b
21 total_ss <- s_yy
22 ssr <- (s_xy * s_xy)/s_xx
23 sse <- total_ss - ssr
24 mse <- sse / (n - 2)
25 mse
26 sse
27 test_statistics <- round(((b - 0)/sqrt(mse / s_xx))
,2)
28 cat("test statistics is",test_statistics)
29 alpha <- 0.05 # 5% significance level
30 range <- round(qt(1 - alpha/2, df = 8),3)
31 range
32 cat("rejection region is greater than",range,"or",
less than",-range)
33 cat("there is significant linear relationship")

```

R code Exa 12.3 Confidence Interval Estimate

```

1 x <- c(39,43,21,64,57,47,28,75,34,52)
2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 df <- data.frame(x, y)
4 cat("interval is from",left,"to",right)

```

```

5 m <- lm(y ~ x, df)
6 m
7 confint(m, level = 0.95)
8 print(paste0("The 95% confidence interval is ",
  sprintf("[ %4.3f, %4.3f ]", confint(m, level =
    0.95)[2], confint(m, level = 0.95)[4])));
9 #the answers may slightly vary due to rounding off
  values.

```

R code Exa 12.4 Average Calculus Grade

```

1 x <- c(39,43,21,64,57,47,28,75,34,52)
2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 x0 <- 50
4 df <- data.frame(x, y)
5 lmresult <- lm(y ~ x, data = df)
6 lmresult
7 df2 <- data.frame(x = 50)
8 df2
9 ycap <- predict(lmresult, df2, interval = "
  confidence")[1]
10 ycap
11 lower <- predict(lmresult, df2, interval = "
  confidence")[2]
12 upper <- predict(lmresult, df2, interval = "
  confidence")[3]
13 cat("the average calculus grade for students who
  score 50 on the achievement test will lie between
  ", lower, " and ", upper)

```

R code Exa 12.5 Student Achievement test

```

1 x <- c(39,43,21,64,57,47,28,75,34,52)

```



```

2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 x0 <- 50
4 df <- data.frame(x, y)
5 lmresult <- lm(y ~ x, data = df)
6 lmresult
7 df2 <- data.frame(x = 50)
8 df2
9 ycap <- predict(lmresult, df2, interval = "
  prediction")[1]
10 ycap
11 lower <- predict(lmresult, df2, interval = "
  prediction")[2]
12 upper <- predict(lmresult, df2, interval = "
  prediction")[3]
13 cat("the 95% confidence interval is from",lower,"to"
  ,upper)

```

R code Exa 12.6 Grade Achievement test

```

1 x <- c(39,43,21,64,57,47,28,75,34,52)
2 y <- c(65,78,52,82,92,89,73,98,56,75)
3 x0 <- 0
4 df <- data.frame(x, y)
5 lmresult <- lm(y ~ x, data = df)
6 lmresult
7 df2 <- data.frame(x = 0)
8 df2
9 ycap <- predict(lmresult, df2, interval = "
  confidence")[1]
10 ycap
11 lower <- predict(lmresult, df2, interval = "
  confidence")[2]
12 upper <- predict(lmresult, df2, interval = "
  confidence")[3]
13 cat("the 95% confidence interval is from",lower,"to"

```

```
      ,upper)
14 cat(", this interval does not contain the value
      alpha = 0 hence y intercept cannot be 0.")
15 cat("data does not support the hypothesis of 0
      intercept")
```

R code Exa 12.7 Correlation Coefficient

```
1 x <- c(73,71,75,72,72,75,67,69,71,69)
2 y <- c(185,175,200,210,190,195,150,170,180,175)
3 r <- cor(x, y)
4 cat("correlation coefficient is",r)
```

R code Exa 12.8 Correlation Coefficient

```
1 #refer to example 12.7 for height and weight values
2 height <- c(73,71,75,72,72,75,67,69,71,69)
3 weight <- c(185,175,200,210,190,195,150,170,180,175)
4 cor.test(height, weight, method = "pearson",
      alternative = "two.sided")
5 print(cor.test(height, weight, method = "pearson",
      alternative = "two.sided")[3])
6 cat("correlation is declared significant at 1% level
      ")
```

Chapter 13

Multiple Regression Analysis

R code Exa 13.2 Multiple Regression Analysis

```
1 y <- c
  (169.0,218.5,216.5,225.5,229.9,235.0,239.9,247.9,260.0,269.9,234.9)

2 x1 <- c(6,10,10,11,13,13,13,17,19,18,13,18,17,20,21)
3 x2 <- c(1,1,1,1,1,2,1,2,2,1,1,1,2,2,2)
4 x3 <- c(2,2,3,3,3,3,3,3,3,3,4,4,4,4,4)
5 x4 <- c(1,2,2,2,1.7,2.5,2,2.5,2,2,2,2,3,3,3)
6 df = data.frame(y, x1, x2, x3, x4)
7 df
8 model <- lm(y~x1+x2+x3+x4, data = df)
9 model
10 #The results may slightly vary due to rounding off
    values
```

R code Exa 13.3 Productivity of Retail Grocery Outlets

```
1 y <- c
  (4.08,3.40,3.51,3.09,2.92,1.94,4.11,3.16,3.75,3.60)
```

```

2 x <- c
  (21.0,12.0,25.2,10.4,30.9,6.8,19.6,14.5,25.0,19.1)

3 plot(x,y)
4 cat("The relationship appears to be curvilinear and
  a quadratic model will provide more accurate
  estimations and predictions")

```

R code Exa 13.4 Productivity of Retail Grocery Outlets

```

1 y <- c
  (4.08,3.40,3.51,3.09,2.92,1.94,4.11,3.16,3.75,3.60)

2 x <- c
  (21.0,12.0,25.2,10.4,30.9,6.8,19.6,14.5,25.0,19.1)

3 model <- lm(y ~ x + I(x^2))
4 model
5 summary(model)
6 cat("quadratic model provide accurate prediction")

```

R code Exa 13.6 Regression Analysis

```

1 salary <- c(60710,NA
  ,63160,63210,64140,65760,65590,59510,60440,61340,61760,62750,63200,
  NA)
2 x1 <- c(1,2,3,3,4,5,5,1,2,3,3,4,5,5)
3 x2 <- c(1,1,1,1,1,1,1,0,0,0,0,0,0,0)
4 df <- data.frame(salary, x1, x2)
5 df
6 model <- lm(salary ~ x1 * x2, data = df)
7 summary(model)
8 model

```

```

9 model1 <- aov(model, data = df)
10 model1
11 summary(model1)
12 par(mfrow=c(1,2))
13 plot(model, pch=16, which=1)
14 plot(model, pch=16, which=2)
15 #the textbook's f-value from anova table is wrong
    and rest all of the values are correct

```

R code Exa 13.7 Sufficient Evidence Test

```

1 salary <- c(60710, NA
    ,63160,63210,64140,65760,65590,59510,60440,61340,61760,62750,63200
    NA)
2 x1 <- c(1,2,3,3,4,5,5,1,2,3,3,4,5,5)
3 x2 <- c(1,1,1,1,1,1,1,1,0,0,0,0,0,0)
4 df <- data.frame(salary, x1, x2)
5 df
6 model <- aov(salary ~ x1 * x2, data = df)
7 model
8 summary(model)
9 p_value <- summary(model)[[1]][["Pr(>F)"]][[3]]
10 p_value
11 cat("the p-value =",p_value,"is twice of what it
    would be for one- tailed test so null hypothesis
    is rejected ")
12 cat("So there is sufficient evidence to indicate
    that the annual rate of increase in men's faculty
    salaries exceeds the rate for women")

```

R code Exa 13.8 Real Estate Data

```

1 y <- c
  (169.0,218.5,216.5,225.5,229.9,235.0,239.9,247.9,260.0,269.9,234.9)

2 x1 <- c(6,10,10,11,13,13,13,17,19,18,13,18,17,20,21)
3 x2 <- c(1,1,1,1,1,2,1,2,2,1,1,1,2,2,2)
4 x3 <- c(2,2,3,3,3,3,3,3,3,3,4,4,4,4,4)
5 x4 <- c(1,2,2,2,1.7,2.5,2,2.5,2,2,2,2,3,3,3)
6 k <- 4
7 r <- 1
8 df = data.frame(y, x1, x2, x3, x4)
9 df
10 model <- lm(y~x1+x2+x3+x4, data = df)
11 model
12 summary(model)
13 aov(model)
14 summary(aov(model))
15 sr <- (summary(aov(model)))
16 model1 <- lm(y ~ x1)
17 model1
18 aov(model1)
19 s <- (summary(aov(model1)))
20 s
21 sse1 <- s[[1]][[2]][[2]]
22 sse2 <- sr[[1]][[2]][[5]]
23 sse2
24 mse2 <- sr[[1]][[3]][[5]]
25 mse2
26 f <- round(((sse1 - sse2) / ((k - r))/mse2),1)
27 cat("test statistics is",f)
28 alpha <- 0.05
29 critical_value_f <- qf(1 - alpha, df1 = 3, df2 = 10)
30 critical_value_f
31 if(f > critical_value_f){
32   print("reject the null hypothesis")
33 }else{
34   print("cannot reject null hypothesis")
35 }
36 #The results may slightly vary due to rounding off

```

values

Chapter 14

Analysis of Categorical Data

R code Exa 14.1 Rat problem

```
1 df1 <- data.frame(green <- 20, red <- 39, blue <-  
  31)  
2 chisq <- chisq.test(df1)  
3 n <- 90  
4 p_value <- chisq$p.value  
5 p_value  
6 cat("since the p-value is less than 0.05 so the null  
  hypothesis is rejected")  
7 cat("So there is sufficient evidence to indicate  
  that the rat has a preference for one of the  
  three doors")
```

R code Exa 14.2 Blood phenotype

```
1 o1 <- 89  
2 o2 <- 18  
3 o3 <- 12  
4 o4 <- 81
```



```

5 e1 <- 82
6 e2 <- 20
7 e3 <- 8
8 e4 <- 90
9 p1 <- 0.41
10 p2 <- 0.10
11 p3 <- 0.04
12 p4 <- 0.45
13 k <- 4
14 df <- k - 1
15 alpha <- 0.100
16 x_square_observed <- ((o1 - e1) * (o1 - e1) / e1) +
  ((o2 - e2) * (o2 - e2) / e2) + ((o3 - e3) * (o3 -
  e3) / e3) + ((o4 - e4) * (o4 - e4) / e4)
17 x_square_observed
18 x_square_0.100 <- qchisq(1 - alpha, df) #x-square
  at alpha = 0.100 using chi-square
19 x_square_0.100
20 if(x_square_observed < x_square_0.100){
21   print("p-value is greater than 0.100, do not have
  sufficient evidence to reject null h0")
22 }else{
23   print("reject the h0")
24 }

```

R code Exa 14.4 Furniture defect

```

1 shift1 <- c(15,21,45,13)
2 shift2 <- c(26,31,34,5)
3 shift3 <- c(33,17,49,20)
4 data <- data.frame(shift1, shift2, shift3)
5 data
6 chisq.test(data)
7 p_value <- chisq.test(data)$p.value
8 cat(p_value < 0.05)

```

```

9  cat("since p-value is less than 0.005 so null
    hypothesis can be rejected and there is
    sufficient evidence that the proportion of defect
    types vary shift to shift")
10 #the answers may slightly vary due to rounding off
    values

```

R code Exa 14.5 Flu Vaccine

```

1  survey <- matrix(c(24,9,13,289,100,565),ncol = 3,
    byrow = TRUE)
2  colnames(survey) <- c("No Vaccine","One Shot","Two
    Shots")
3  rownames(survey) <- c("Flu","No Flu")
4  survey <- as.table(survey)
5  survey
6  chisq.test(survey,correct = F)
7  cat("null hypothesis is rejected so there is
    sufficient evidence to indicate a relationship
    between treatment and influence of flu")

```

R code Exa 14.7 Survey of Voter

```

1  voter <- matrix(c(76,53,59,48,124,147,141,152),ncol
    = 4, byrow = TRUE)
2  colnames(voter) <- c("1","2","3","4")
3  rownames(voter) <- c("Favor A","Do Not Favor A")
4  voter <- as.table(voter)
5  voter
6  chisq.test(voter,correct = F)
7  cat("X-squared value is too large so null hypothesis
    is rejected")

```

Chapter 15

Nonparametric Statistics

R code Exa 15.1 Euglossine bees

```
1 species1 <- c(235,225,190,188);
2 species2 <- c(180,169,180,185,178,182);
3 n1 <-length(species1);
4 n2 <- length(species2);
5 data <- c(species1,species2);
6 rank1 <- rank(sort(data))
7 t1 <- 7+8+9+10;
8 t1_ <- n1 * (n1 + n2 + 1) - t1
9 t1_                                     #for n1=4
    and n2=6, the critical value of T at alpha = 0.05
    is 12
10 if(t1_ <= 12){
11   print("Reject the Null Hypothesis")
12 }else{
13   print("Accept the Null Hypothesis")
14 }
```

R code Exa 15.2 Kraft papers

```

1 standard1 <- c
  (1.21,1.43,1.35,1.51,1.39,1.17,1.48,1.42,1.29,1.40)

2 treated2 <- c
  (1.49,1.37,1.67,1.50,1.31,1.29,1.52,1.37,1.44,1.53)

3 n1 <- length(standard1)
4 n2 <- length(treated2)
5 alpha = 0.05
6 x <- c(standard1,treated2)
7 ranksum<-function(x,start,end){
8   return(sum(x[start:end]))
9 }
10 rank <- rank(x)
11 t1 <- ranksum(rank,1,n1)
12 t2 <- n1 * (n1 + n2 + 1) - t1
13 if(t1 <= 82){                                     #critical value
  of T at n1=n2=10 at alpha = 0.05 is 82
14   print("Reject the hypothesis")
15 }else{
16   print("Insufficient evidence to conclude that the
      treated kraft paper is stronger than the
      standard paper")
17 }
18 muo_t <- (n1 * (n1 * n2 + 1))/2
19 sigma_sqr_t <- ((n1 * n2) *(n1 + n2 +1))/12
20 sigma_t <- sqrt(sigma_sqr_t)
21 z <- (t1 - muo_t)/sigma_t;
22 p_value <- 0.5 - 0.4292
23 p_value
24 if(p_value <= alpha){
25   print("Reject the hypothesis")
26 }else{
27   print("Cannot conclude the treated kraft paper is
      stronger than the standard paper")
28 }

```

R code Exa 15.3 Defective Electrical Fuses

```
1 line_A <- c(170,164,140,184,174,142,191,169,161,200)
  ;
2 line_B <- c(201,179,159,195,177,170,183,179,170,212)
  ;
3 n = 10;
4 x = 1
5 p_value = 2 * round(pbinom(x,n,0.5),3)           #
  hypothesized value of p is 0.5
6 p_value
7 cat(" Reject the hypothesis at 5% level ")
```

R code Exa 15.4 Employee accident rates

```
1 x <- 63;
2 n <- 100;
3 alpha <- 0.05;
4 z <- (x - 0.5 * n)/(0.5 * sqrt(n));
5 z_expected <- qnorm(1-alpha/2)
6 if(z == z_expected ){
7   print(" Accept the null hypothesis")
8 }else{
9   print(" Reject the null hypothesis and the data
  provide sufficient evidence")
10 }
```

R code Exa 15.5 Densities of cakes

```

1 x_A <- c(.135,.102,.098,.141,.131,.144)
2 x_B <- c(.129,.120,.112,.152,.135,.163)
3 alpha <- 0.10
4 t0 <- round(qt(1 - alpha/2,5),1)
5 boxplot(x_A - x_B,horizontal = TRUE,xlab = "
  Differences")
6 wilcox.test(x_A,x_B,paired = T)
7 t_positive <- wilcox.test(x_A,x_B,paired = T)$
  statistic
8 t0
9 t_positive
10 if(t_positive <= t0){
11   print("Reject the null hypothesis so two
    population frequency distribution of cake
    densities differ")
12 }else{
13   print("Accept the hypothesis")
14 }

```

R code Exa 15.6 Kruskal Wallis H test

```

1 one <- c(65,87,73,79,81,69)
2 two <- c(75,69,83,81,72,79,90)
3 three <- c(59,78,67,62,83,76)
4 four <- c(94,89,80,88)
5 k <- 4
6 kruskal.test(list(one, two, three, four))
7 h <- kruskal.test(list(one, two, three, four))$
  statistic
8 h
9 df <- k - 1
10 alpha <- 0.05
11 x_square_0.05 <- qchisq(1 - alpha, df)
12 x_square_0.05
13 if(h >= x_square_0.05){

```

```

14   print("sufficient evidence to indicate differences"
      )
15 }else{
16   print("there is insufficient evidence to indicate
      differences in the distributions of achievement
      test scores for the four teaching techniques")
17 }
18 #the answers may slightly vary due to rounding off
    values

```

R code Exa 15.8 Friedman Fr test

```

1  a <- c(.6,.7,.9,.5)
2  B <- c(.9,1.1,1.3,.7)
3  c <- c(.8,.7,1.0,.8)
4  d <- c(.7,.8,1.0,.6)
5  e <- c(.5,.5,.7,.4)
6  f <- c(.6,.5,.8,.6)
7  g <- c(a,B,c,d,e,f)
8  rank_a <- c(2.5,3.5,3,2)
9  rank_b <- c(6,6,6,5)
10 rank_c <- c(5,3.5,4.5,6)
11 rank_d <- c(4,5,4.5,3.5)
12 rank_e <- c(1,1.5,1,1)
13 rank_f <- c(2.5,1.5,2,3.5)
14 t1 <- sum(rank_a)
15 t2 <- sum(rank_b)
16 t3 <- sum(rank_c)
17 t4 <- sum(rank_d)
18 t5 <- sum(rank_e)
19 t6 <- sum(rank_f)
20 k <- 6
21 b <- 4
22 fr <- 12 / (b * k * (k + 1)) * (t1 * t1 + t2 * t2 +
    t3 * t3 + t4 * t4 + t5 * t5 + t6 * t6 ) - (3 * b

```

```

      * (k + 1))
23 fr
24 df <- k - 1
25 alpha <- 0.05
26 x_square <- qchisq(1 - alpha, 5)      #sampling
      distribution of fr
27 if(fr > x_square){
28   print("reject null hypothesis, so the distribution
      of reaction times differ in location for at
      least two stimuli")
29 }else{
30   print("accept the null hypothesis ")
31 }

```

R code Exa 15.9 P value

```

1 a <- c(.6,.7,.9,.5)
2 B <- c(.9,1.1,1.3,.7)
3 c <- c(.8,.7,1.0,.8)
4 d <- c(.7,.8,1.0,.6)
5 e <- c(.5,.5,.7,.4)
6 f <- c(.6,.5,.8,.6)
7 data2 <- matrix(c
  (.6,.9,.8,.7,.5,.6,.7,1.1,.7,.8,.5,.5,.9,1.3,1.0,1.0,.7,.8,.5,.7,
  ,nrow = 4, ncol = 6,byrow = T)
8 dimnames(data2) = list(c(1,2,3,4), c("a","b","c","d"
  ,"e","f"))
9 friedman.test(data2)
10 p_value <- friedman.test(data2)$p.value
11 cat(" Approximate p-value = ",p_value," ,which is
  slightly less than 0.005")

```

R code Exa 15.10 Spearman rank correlation coefficient


```

1 xi <- c(7,4,2,6,1,3,8,5)
2 yi <- c(1,5,3,4,8,7,2,6)
3 di <- c(xi - yi)
4 n <- 8;
5 di_square <- c(di * di)
6 total = sum(di_square)
7 total
8 rs <- 1 - (6 * total)/((n) * (n * n - 1 ))
9 cat("rs is ",rs)

```

R code Exa 15.11 Hypothesis Test of no association

```

1 xi <- c(7,4,2,6,1,3,8,5)
2 yi <- c(1,5,3,4,8,7,2,6)
3 alpha <- 0.05
4 cor.test(xi, yi)
5 rs <- cor.test(xi, yi)$estimate
6 cat("rs is",rs)
7 p_value <- cor.test(xi, yi)$p.value
8 if(p_value <= alpha){
9   print("null hypothesis is rejected")
10 }else{
11   print("null hypothesis is accepted")
12 }

```
