## R Textbook Companion for Statistics for Business and Economics by Anderson, Sweeney, and Williams<sup>1</sup>

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# **Book Description**

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R numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means an R code whose theory is explained in Section 2.3 of the book.

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## Chapter 2

# Descriptive Statistics Tabular and Graphical Presentations

R code Exa 2.1a Summarizing Categorical Data Part 1

```
1
                                            # Page no. :
                                              33
3 # Frequency Distribution (Categorical Data)
5 # Dataset
  soft_drink_names <- c("Coke Classic", "Diet Coke", "</pre>
     Pepsi", "Diet Coke", "Coke Classic", "Coke Classic
                         "Dr. Pepper", "Diet Coke", "
8
                            Pepsi", "Pepsi", "Coke
                            Classic", "Dr. Pepper",
9
                         "Sprite", "Coke Classic", "Diet
                             Coke", "Coke Classic", "
                            Coke Classic", "Sprite",
                         "Coke Classic", "Diet Coke", "
10
                           Coke Classic", "Diet Coke",
                           "Coke Classic", "Sprite",
```

```
"Pepsi", "Coke Classic", "Coke
11
                            Classic", "Coke Classic", "
                         Pepsi", "Coke Classic",
"Sprite", "Dr. Pepper", "Pepsi"
12
                            , "Diet Coke", "Pepsi", "
                            Coke Classic",
                         "Coke Classic", "Coke Classic",
13
                             "Pepsi", "Dr. Pepper", "
                            Coke Classic", "Diet Coke",
                         "Pepsi", "Pepsi", "Pepsi", "
14
                            Pepsi", "Coke Classic", "Dr.
                             Pepper", "Pepsi", "Sprite")
15
16 soft_drink_table <- data.frame(table(soft_drink_
      names))
17
                                        # Page no. : 34
18
19
20 FD <- data.frame(Soft_drinks = soft_drink_table$soft
      _drink_names,
21
                     Frequency = soft_drink_table$Freq)
                          # Frequency Distribution
22
23
24 RF <- FD$Frequency / sum(FD$Frequency) # Relative
       Frequency
25
26 FD <- cbind(FD, Relative_frequency = RF)
27
28 PF <- FD$Relative_frequency * 100 # Percentage
      Frequency
29
30 FD <- cbind(FD, Percentage_frequency = PF)
31
              # Viewing the Frequency Distribution
32 View(FD)
      Table
33
34 # Total values of Frequency Distribution
```

```
35
36 total_freq <- sum(FD$Frequency)
37
38 total_rel_freq <- sum(FD$Relative_frequency)
39
40 total_per_freq <- sum(FD$Percentage_frequency)
41
42 cat("Total value for frequency is", total_freq, "\n")
43 cat("Total value for relative frequency is", total_rel_freq, "\n")
44 cat("Total value for percentage frequency is", total_per_freq)</pre>
```

#### R code Exa 2.1b Summarizing Categorical Data Part 2

```
1
                                          # Page no. :
                                              35
3 # Bar Charts and Pie Charts
5 # Dataset
  soft_drink_names <- c("Coke Classic", "Diet Coke", "</pre>
     Pepsi", "Diet Coke", "Coke Classic", "Coke Classic
                          "Dr. Pepper", "Diet Coke", "
8
                             Pepsi", "Pepsi", "Coke
                             Classic", "Dr. Pepper",
                          "Sprite", "Coke Classic", "
9
                             Diet Coke", "Coke Classic",
                             "Coke Classic", "Sprite",
                          "Coke Classic", "Diet Coke", "
10
                             Coke Classic", "Diet Coke",
                              "Coke Classic", "Sprite",
```

```
"Pepsi", "Coke Classic", "Coke
11
                              Classic", "Coke Classic",
                            "Pepsi", "Coke Classic",
                          "Sprite", "Dr. Pepper", "Pepsi
12
                            ", "Diet Coke", "Pepsi", "
                             Coke Classic",
                          "Coke Classic", "Coke Classic"
13
                             , "Pepsi", "Dr. Pepper", "
                            Coke Classic", "Diet Coke",
                          "Pepsi", "Pepsi", "Pepsi", "
14
                             Pepsi", "Coke Classic", "Dr
                             . Pepper", "Pepsi", "Sprite
15
16 soft_drink_table <- data.frame(table(soft_drink_
     names))
17
18 # Install Library if not installed
19
20 # install.packages("ggplot2")
21
22 # Import Library
23
24 library(ggplot2)
25
26 # Bar Chart
27
28 ggplot(soft_drink_table, aes(soft_drink_names, Freq,
      fill = soft_drink_names))+geom_bar(stat = "
      identity")+
29 labs(title="Bar chart", x = "Soft Drink", y = "
      Frequency")+ylim(0,20)
30
31 # Pie Chart
32
33 soft_drink_purchase_slices <- soft_drink_table$Freq
34 soft_drink_names_labels <- soft_drink_table$soft_
     drink_names
```

#### R code Exa 2.2a Summarizing Quantitative Data

```
1
                                              # Page no. :
                                                 39 - 40
3 # Frequency Distribution (Quantitative Data)
5 audit_data <- c
      (12, 15, 20, 22, 14, 14, 15, 27, 21, 18, 19, 18, 22, 33, 16, 18, 17, 23, 28, 13)
7 no_of_classes <- 5
  width <- (max(audit_data) - min(audit_data)) / no_of</pre>
      _classes
10
11 width <- ceiling(width) # Rounding up of the value
12
13 breaks \leftarrow seq(10,34,by = width)
14
15 class_range <- cut(audit_data, breaks, right=T)</pre>
16
```

```
17 frequency <- table(class_range)
18
19 frequency_distribution <- data.frame(frequency)</pre>
20
21 frequency_distribution <- data.frame(class_range =
      frequency_distribution$class_range,
22
                                          frequency =
                                             frequency_
                                             distribution
                                             $Freq)
23
24 # Note that :- Book answer will differ with my
     answer though number of classes and width of
25 # each class is same as in the book!!!
26
27
                                             # Page no. :
                                                  41
28
29 relative_frequency <- round(frequency_distribution$</pre>
      frequency / sum(frequency_distribution$frequency)
30
                                       ,2) # Rounding
                                          of data to 2
                                          digits
31
32 percentage_frequency <- relative_frequency * 100
33
34 audit_data_FD <- cbind(frequency_distribution,
35
                                  relative_frequency,
                                     percentage_frequency
                                     )
36
37 View(audit_data_FD)
38
39
                                             # Page no. :
                                                 41 - 42
40
41 # Dot Plot and Histogram
42
```

```
43 # Install Library if not installed
44
45 # install.packages("ggplot2")
46
47 # Import Library
48
  library(ggplot2)
49
50
51 # Dot Plot
52
  dotchart(audit_data, main = "Dot Plot for the Audit
     Time Data", xlab = "Audit Time (days)",
54
            cex = 0.5) # cex is for scaling
55
56 # Note that: Book dot plot is different from my dot
      plot.
57
58 # Histogram
59
  ggplot(audit_data_FD, aes(class_range, frequency,
     fill = class_range))+
     geom_histogram(stat = "identity")+labs(title="
61
        Histogram for the Audit Time Data"
                                              x = "Audit
62
                                                 Time (
                                                 days)",
                                                 y = "
                                                 Frequency
                                                 ")+ylim
                                                 (0,8)
```

R code Exa 2.3a Scatter Plot and Tradeline

```
1 # Page no. : 57-58
```

```
3 # Dataset
5 week <-c(1,2,3,4,5,6,7,8,9,10)
6 \times (2,5,1,3,4,1,5,3,4,2)
7 y \leftarrow c(50,57,41,54,54,38,63,48,59,46)
8 data <- data.frame(week,x,y)</pre>
10 # Install Library if not installed
12 # install.packages("ggplot2")
14 # Import Library
15
16 library(ggplot2)
17
18 # Scatter Plot
20 ggplot(data, aes(x,y)) + geom_point() + geom_smooth(
      method = "lm", se = F) +
21 labs(title = "Scatter Plot and Tradeline for the
      Stereo and Sound Equipment Store",
22
                                                           Х
                                                             Number
                                                              o f
                                                              Commercials
23
                                                           У
```

```
"Sales
(
$ 100
s
)
"
```

#### R code Exa 2.4a Cumulative Distributions

```
1
                                          # Page no. :
                                             44
3 # Cumulative Distributions
5 audit_time <- c("Less than or equal to 14", "Less
     than or equal to 19", "Less than or equal to 24",
                   "Less than or equal to 29", "Less
6
                      than or equal to 34")
7 frequency \leftarrow c(4,8,5,2,1) # Refer to table no. 2.5
      page no. 40
8 cumulative_freq <- cumsum(frequency)</pre>
10 DF <- data.frame(audit_time, frequency, cumulative_
     freq)
11
12 CRF <- DF$cumulative_freq / sum(DF$frequency)
     Cumulative Relative Frequency
13
14 CPF <- CRF * 100 # Cumulative Percentage Frequency
```

```
15
  DF <- cbind(DF, CRF, CPF)
16
   View(DF)
18
   breaks \leftarrow seq(9, 34, by = 5)
   cumfreq0 <- c(0, DF$cumulative_freq)</pre>
20
21
22 DF2 <- data.frame(breaks, cumfreq0)
23
24 # Install Library if not installed
25
26 # install.packages("ggplot2")
27
28 # Import Library
29
30 library(ggplot2)
31
  ggplot(DF2, aes(breaks, cumfreq0, group = 1)) + geom
      _point() + geom_line() +
     xlim(c(0,35)) + labs(title = "Ogive For the Audit)
33
        Time Data", x = "Audit Time (Days)",
        y = "Cumulative Frequency")
34
```

R code Exa 2.5a Exploratory Data Analysis The Stem and Leaf Display

```
# Page no.:
49

2
3 # Exploratory Data Analysis : The Stem - and - Leaf
    Display

4
5 data <- c(112, 72, 69, 97, 107, 73, 92, 76, 86, 73,
    126, 128, 118, 127, 124, 82, 104, 132, 134, 83,
    92, 108, 96, 100, 92, 115, 76, 91, 102,
    81, 95, 141, 81, 80, 106, 84, 119, 113,</pre>
```

```
98, 75,
7
             68, 98, 115, 106, 95, 100, 85, 94, 106,
                119)
8
9 stem(data)
10
                                          # Page no. :
11
                                             51
12
13 data2 <- c(1565, 1852, 1644, 1766, 1888, 1912, 2044,
       1812, 1790, 1679, 2008, 1852, 1967, 1954,
14
              1733)
                 # Answer is varing from the book
15 stem(data2)
```

## Chapter 3

# Descriptive Statistics Numerical Measures

R code Exa 3.1a Measures of Location Mean Part 1

```
# Page no.:
87

2
3 # Mean
4
5 x <- c(46, 54, 42, 46, 32)
6
7 sample_mean <- mean(x)
8
9 cat("Sample mean for x is ", sample_mean)</pre>
```

R code Exa 3.1b Measures of Location Mean Part 2

```
1 # Page no. :
88
```

#### R code Exa 3.1c Measures of Location Median Part 1

R code Exa 3.1d Measures of Location Median Part 2

#### R code Exa 3.1e Measures of Location Percentiles and Quartiles

```
1
                                               # Page no.
                                                  : 90-91
3 salary <- c
      (3450, 3550, 3650, 3480, 3355, 3310, 3490, 3730, 3540, 3925, 3520, 3480)
5 # 85th and 50th Percentiles
7 solution \leftarrow quantile(salary, probs = c(0.85, 0.5))
  cat ("Value for 85th and 50th percentile are",
      solution[1], ",", solution[2])
10
11 # Note that: 85th percentile value is different from
       the book
12
13
14 # 25th, 50th, 75th Percentiles (First, Second, Third
       Quartiles)
```

```
15
16 values <- quantile(salary, probs = c(0.25, 0.5, 0.75))
17
18 cat("Value for first, second, third quartiles are ", values[1], ",", values[2], ",", values[3])
19
20 # Note that: First and Second Quartile values are different from the book</pre>
```

#### R code Exa 3.2a Measures of Variability Range and IQR

```
1
                                                 # Page no. :
                                                     96 - 97
3 salary <- c
      (3450, 3550, 3650, 3480, 3355, 3310, 3490, 3730, 3540, 3925, 3520, 3480)
5 # Range
7 range <- range(salary)</pre>
8 diff <- range[2] - range[1]</pre>
10 cat("Range is", diff)
11
12 # Inter-Quartile Range
13
14 IQR <- IQR(salary)</pre>
15
16 cat("IQR is ", IQR)
17
18 # Note that : IQR value of Book is different.
```

#### R code Exa 3.2b Measures of Variability Variance

```
# Page no.:
97-98

students <- c(46, 54, 42, 46, 32)

# Variance

variance <- var(students)

cat("Variance of students is ", variance)
```

#### R code Exa 3.2c Measures of Variability Standard Deviation

#### R code Exa 3.3a Z Score

```
1
                                                    # Page
                                                       no.:
                                                         104
3 \# Z-score
5 students <- c(46,54,42,46,32)
7 deviation <- students - mean(students)
9 sample_variance <- var(students)</pre>
10
11 dataset <- data.frame(students, deviation)</pre>
12
13 z <- c()
14
15 for(i in 1:length(dataset$students)){
     z[i] <- deviation[i]/sqrt(sample_variance)</pre>
16
17 }
18
19 dataset <- cbind(dataset, zScore = z)</pre>
20
21 View(dataset)
```

#### R code Exa 3.4a Boxplot

```
1 # Page no.
: 110
```

#### R code Exa 3.5a Covariance and Correlation Coefficient

```
15
16 # Correlation Coefficient
17
18 correlation <- cor(dataset$x,dataset$y)
19
20 cat("Value of correlation coefficient is ", correlation)
```

#### R code Exa 3.5b Sample Correlation Coefficient

#### R code Exa 3.6a Weighted Mean

```
6  cost <- c(3.00,3.40,2.80,2.90,3.25)
7  pound <- c(1200,500,2750,1000,800)
8
9  dataset <- data.frame(purchase,cost,pound)
10
11  # Weighted Mean
12
13  mean <- weighted.mean(dataset$cost,dataset$pound)
14
15  cat("Weigted mean for the dataset is",mean)</pre>
```

#### R code Exa 3.6b Grouped Data Mean and Sample Variance

```
1
                                                # Page no.
                                                    : 126
                                                   -127
3 # Data
5 audit \leftarrow c("10-14", "15-19", "20-24", "25-29", "30-34")
6 midpoint \leftarrow c(12,17,22,27,32)
7 frequency <-c(4,8,5,2,1)
9 dataset <- data.frame(audit, midpoint, frequency)
10
11 # Mean for Grouped Data
12
13 mean <- weighted.mean(dataset$midpoint,dataset$
      frequency)
14
15 cat ("Mean for grouped data is", mean)
17 # Sample Variance for Grouped Data
18
19 var <- sum(dataset$frequency*((dataset$midpoint -
```

```
mean)**2)) / (sum(dataset$frequency) - 1)
20
21 # Note that : Grouped sample variance has no inbuild
    function
22
23 cat("Sample variance for grouped data is", var)
```

## Chapter 4

## Introduction to Probability

#### R code Exa 4.1a Combinations

```
1
                                               # Page no. :
                                                   154
3 # Combinations
5 # Eg. 1
7 N <- 5
8 n <- 2
10 combinations <- choose(n = N, k = n)
11
12 cat("The total combinations are", combinations)
13
14 # Eg. 2
15
16 N <- 53
17 n <- 6
18
19 combinations \leftarrow choose (n = N, k = n)
20
```

```
21 cat("The total combinations are", combinations)
```

#### R code Exa 4.1b Permutations

#### R code Exa 4.1c Assigning Probabilities

```
# Page no.: 155
- 156

2
3 # Assigning Probabilities
4
5 x <- c(0,1,2,3,4)
6 y <- c(2,5,6,4,3)
7
8 DF <- data.frame(x,y)
9
10 y_sum <- sum(DF$y)
11
12 prob <- DF$y / y_sum
13
14 DF <- cbind(DF,prob)
```

```
15
16 View(DF)
```

#### R code Exa 4.1d Probabilities Assigning Example

```
1
                                            # Page no. :
                                               157 - 158
3 # Probabilities Assigning Example
5 \times (2,2,2,3,3,3,4,4,4)
6 y \leftarrow c(6,7,8,6,7,8,6,7,8)
7
8
  z = list()
10 for(i in 1:length(x))
11 {
     z[i] <- list(c(x[i],y[i]))</pre>
12
13 }
14
15 past_project \leftarrow c(6,6,2,4,8,2,2,4,6)
16
17 DF <- data.frame(x,y,I(z),past_project)
18
19 past_project_sum <- sum(DF$past_project)</pre>
20
21 p <- DF$past_project / past_project_sum
22
23 DF <- cbind(DF,p)
24
25 total_probability <- sum(DF$p)
26
27 cat ("Total probability for the Sample Point is",
      total_probability)
28
```

#### R code Exa 4.2a Probability of an Event

```
1
                                              # Page no. :
                                                 161
3 # Probability of an Event
5 # C denotes the event that is completed in 10 months
       or less
7 C \leftarrow c(list(c(2,6)), list(c(2,7)), list(c(2,8)),
      list(c(3,7)), list(c(3,8)), list(c(4,6)))
8 prob \leftarrow c(0.15,0.15,0.05,0.10,0.20,0.05)
10 dataset <- data.frame(I(C),prob)</pre>
11
12 event <- sum(dataset$prob)
13
14 # P(C) = P(2,6) + P(2,7) + P(2,8) + P(3,7) + P(3,8)
     + P(4,6)
15
16 cat("Probability of an event P(C) is", event)
17
18 # L denotes the event that is completed in less than
       10 months
19
20 L \leftarrow c(list(c(2,6)), list(c(2,7)), list(c(3,7)))
21 prob \leftarrow c(0.15,0.15,0.10)
22
23 dataset <- data.frame(I(L),prob)
24
25 \# P(L) = P(2,6) + P(2,7) + P(3,7)
26
```

```
27 event2 <- sum(dataset$prob)
28
  cat("Probability of an event P(L) is", event2)
29
30
31 # M denotes the event that is completed in more than
       10 months
32
33 M \leftarrow c(list(c(3,8)), list(c(4,7)), list(c(4,8)))
34 \text{ prob} \leftarrow c(0.05, 0.10, 0.15)
35
36
  dataset <- data.frame(I(M),prob)</pre>
37
38 \# P(M) = P(3,8) + P(4,7) + P(4,8)
39
40 event3 <- sum(dataset$prob)
42 cat ("Probability of an event P(L) is", event3)
```

R code Exa 4.3a Probability Computation using Complement

```
# Page no.:
165

probability Computation using Complement

p_comp_A <- 0.80

p_A <- 1 - p_comp_A

cat("Probability for A is",p_A)</pre>
```

R code Exa 4.3b Intersection and Union of Events

```
\# Pahe no. : 167
1
2
3 # Intersection and Union of Events
5 a <- 5
6 n <- 50
7 c <- 6
8 d <- 2
10 p_L <- a / n
11
12 p_D <- c / n
13
14 p_L_and_D \leftarrow d / n
15
16
17 cat("Probability for L intersection D is",p_L_and_D)
19 p_L_or_D \leftarrow p_L + p_D - p_L_and_D
20
21 cat("Probability for L union D is",p_L_or_D)
```

### R code Exa 4.3c Addition Law

```
# Page no.:
168

2
3 # Addition Law
4

5 p_S <- 0.30
6 p_W <- 0.20
7 p_S_and_W <- 0.12
8

9 p_S_or_W <- p_S + p_W - p_S_and_W
10
```

```
11 cat("Probability after applying addition law is ",p_S_or_W)
```

### R code Exa 4.4a Conditional Probability

```
1
                                          # Page no. :
                                             171 - 174
3 # Conditional Probability
5 position <- c("Promoted", "Not Promoted")
6 gender <- c("Men", "Women")
7 number1 <-c(288, 36)
                           # Promoted
8 number2 <- c(672, 204) # Not Promoted
10 DF <- data.frame(position, gender, number1, number2)
11
12 table <- round(prop.table(DF[,3:4]), 2)
13 table <- as.matrix(table)</pre>
14 table
15
16 position <- c("Promoted", "Not Promoted")
17 men <- c(table[1,1][[1]], table[1,2][[1]])
18 women <- c(table[2,1][[1]], table[2,2][[1]])
19
20 DF2 <- data.frame(position, men, women)
21 View(DF2)
22
23 columnSums <- apply(DF2[,2:3],2, sum)
24 rowSums \leftarrow apply(DF2[,2:3], 1, sum)
25
26 cat ("Total Probability For having Men is",
      columnSums[1])
27 cat ("Total Probability For having Women is",
      columnSums [2])
```

```
28 cat ("Total Probability For Promotion", rowSums[1])
29 cat ("Total Probability For Not a Promotion", rowSums
      [2])
30
31 cond1 <- DF2$men[1]
                         / columnSums[1]
32
33 cat ("Conditional Probability for Men and getting
      Promoted given the Probability
       of Total Men is", cond1)
34
35
36 \text{ cond2} \leftarrow DF2\$\text{women}[1] / \text{columnSums}[2]
37
38 cat ("Conditional Probability for Women and getting
      Promoted given the Probability
       of Total Women is", cond2)
39
```

### R code Exa 4.4b Multiplication Law

```
16
17 # Multiplication Law for Independent Events
18
19 A <- 0.80
20
21 B <- 0.80
22
23 A_and_B <- A * B
24
25 cat("After applying multiplication law for independent events A and B we get", A_and_B)</pre>
```

### R code Exa 4.5a Bayes Theorem Tabular Approach

```
# Page no. : 182
1
2
3 # Tabular Approach for Bayes' Theorem
5 events <- c("A1", "A2")
6 prior_probabilities <- c(0.65,0.35)
8 conditional_probabilities \leftarrow c(0.02,0.05)
  joint_probabilities <- prior_probabilities *</pre>
      conditional_probabilities
11
12 total_joint_probability <- sum(joint_probabilities)</pre>
14 posterior_probabilities <- joint_probabilities /
      total_joint_probability
15
16 DF <- data.frame(events, prior_probabilities,</pre>
      conditional_probabilities
17
                      , joint_probabilities, posterior_
                        probabilities)
```

## Chapter 5

# Discrete Probability Distribution

R code Exa 5.1a Discrete Probability Distribution Graph Expected value Variance and Standard Deviation

```
18 ggplot(dataset, aes(x = x, y = prob_of_x)) + geom_
     bar(stat = "identity", fill = "blue") + labs(
     title = "Graphical representation of the
19
        Probability Distribution",
20
     x = "Number of Automobiles", y = "Probability")
21
22
                                       # Page no. : 203
23
24 # Expected value
25
26 exp_values <- dataset$x * dataset$prob_of_x
27
28 dataset <- data.frame(cbind(dataset, exp_values))
29
30 expected_value <- sum(dataset$exp_values)
31 cat ("Expected value for the given problem is",
     expected_value)
32
                                      # Page no. : 204 -
33
                                          205
34
35 # Variance and Standard Deviation
36
37 deviation_of_x <- (dataset$x - expected_value)
38
39 deviation_square <- (deviation_of_x) ** 2
40 variance <- sum(dataset$prob_of_x * deviation_square
41 standard_deviation <- sqrt(variance)
42
43 cat ("Variance is", variance)
44 cat("Standard Deviation is", standard_deviation)
```

R code Exa 5.2a Binomial Probability Distribution

```
# Page no. : 211

# Binomial Probability Distribution

no_of_trials <- 3
no_of_successes <- 2
BPD <- choose(n = no_of_trials, k = no_of_successes)

cat("Answer is",BPD)

no_of_successes <- 3
BPD <- choose(n = no_of_trials, k = no_of_successes)

at("Answer is",BPD)</pre>
```

### R code Exa 5.2b Binomial Probability Distribution Eg2

```
1
                                                # Page no
                                                    . :
                                                   211
3 # Binomial Probability Distribution Eg-2
5 # Data
6 customer1 <- c("Purchase", "Purchase", "No Purchase")
7 customer2 <- c("Purchase", "No Purchase", "Purchase")
8 customer3 <- c("No Purchase", "Purchase", "Purchase")
10 customer <- data.frame(customer1, customer2, customer3
     )
11
12 len <- nrow(customer) # Trial
14 x \leftarrow 1 # For purchase
15 y <- 0 # For no purchase
16
```

```
17 p <- 0.30
18 q <- 1 - p
19 outcome <- c()
20
21 # Install Library if not installed
22
23 install.packages("Rlab")
24
25 # Import Library
26
27 library(Rlab) # For dbern
28
29 for(i in 1:len)
30 {
     if(customer1[i] == "Purchase" && customer2[i] == "
31
       Purchase" && customer3[i] == "Purchase")
32
       outcome[i] = dbern(x,p) * dbern(x,p) * dbern(x,p)
33
     } else if(customer1[i] == "Purchase" && customer2[
34
       i] == "Purchase" && customer3[i] == "No
       Purchase")
35
     {
       outcome[i] = dbern(x,p) * dbern(x,p) * dbern(y,p)
36
     } else if(customer1[i] == "Purchase" && customer2[
37
        i] == "No Purchase" && customer3[i] == "
       Purchase")
38
       outcome[i] = dbern(x,p) * dbern(y,p) * dbern(x,p)
39
     } else if(customer1[i] == "Purchase" && customer2[
40
        i] == "No Purchase" && customer3[i] == "No
       Purchase")
41
       outcome[i] = dbern(x,p) * dbern(y,p) * dbern(y,p)
42
     } else if(customer1[i] == "No Purchase" &&
43
```

```
customer2[i] == "Purchase" && customer3[i] == "
        Purchase")
44
       outcome[i] = dbern(y,p) * dbern(x,p) * dbern(x,p)
45
          )
     } else if(customer1[i] == "No Purchase" &&
46
        customer2[i] == "Purchase" && customer3[i] == "
        No Purchase")
47
       outcome[i] = dbern(y,p) * dbern(x,p) * dbern(y,p
48
          )
     } else if(customer1[i] == "No Purchase" &&
49
        customer2[i] == "No Purchase" && customer3[i]
        == "Purchase")
50
       outcome[i] = dbern(y,p) * dbern(y,p) * dbern(x,p
51
          )
     } else
52
53
       outcome[i] = dbern(y,p) * dbern(y,p) * dbern(y,p)
54
          )
     }
55
56 }
57
58 customer <- cbind(customer,outcome)
59
60 View (customer)
61
62
                                              # Page no. :
                                                  212 -
                                                 213
63
64 # Binomial Probability Function
65
66 \times (-c(0,1,2,3))
67 fun <- c()
68
69 for (i in 0:length(x)) {
```

```
fun[i] <- dbinom(x[i],len,p)</pre>
70
71 }
72
73 dataset <- data.frame(x, fun)
74 View(dataset)
75
76 # Install Library if not installed
77
78 # install.packages("ggplot2")
79
80 # Import Library
81
82 library(ggplot2)
83
84 ggplot(dataset, aes(x = x, y = fun)) + geom_bar(stat
      = "identity", fill = "blue") + labs(
     title = "Graphical representation of the
85
        Probability Distribution",
     x = "Number of Customers", y = "Probability")
86
87
88
                                             # Page no. :
                                                 214 -
                                                215
89
90 # Expected Value, Variance and Standard Deviation
     for Binomial Probability Distribution
91
92 expected_value <- len * p
93 variance <- len * p * q
94 standard_deviation <- sqrt(variance)
95
96 cat("Expected value is", expected_value)
97 cat ("Variance is", variance)
98 cat("Standard deviation is", standard_deviation)
```

### R code Exa 5.3a Poisson Probability Distribution

### R code Exa 5.4a Hypergeometric Probability Distribution

```
# Page no. : 222
- 223

# Hypergeometric Probability Distribution

# Probability for 1 defective item

N <- 12

n <- 3

r <- 5

HPD <- dhyper(x = x,m = r,n = N-r,k = n)

cat("Answer is", HPD)

# Probability for atleast one defective item
```

```
17
18 HPD <- dhyper(x = 0, m = r, n = N-r, k = n) #
      Probability for no defective item
19
20 cat("Answer is",1 - HPD) # Probability for atleast
      one defective item
21
22 # Expected value, Variance and Standard Deviation
23
24 expected_value \leftarrow n * (r / N)
25 variance <- expected_value * (1 - (r/N)) * ((N-n)/(N)
26 standard_deviation <- sqrt(variance)</pre>
27
28 cat ("Expected value", expected_value)
29 cat ("Variance", variance)
30 cat("standard deviation", standard_deviation)
```

### R code Exa 5.5a Expected Value and Variance

```
15 deviation <- DF$x - expected_mean
16 sq_deviation <- deviation ** 2
17 expected_value2 <- DF$prob_of_x * sq_deviation
18
19 DF <- cbind(DF, deviation, sq_deviation, expected_value2)
20 View(DF)
21
22 expected_variance <- sum(DF$expected_value2)
23
24 cat("Expected variance is", expected_variance)
25
26 expected_SD <- sqrt(expected_variance)
27
28 cat("Expected SD is", expected_SD)</pre>
```

## Chapter 6

# Continuous Probability Distribution

R code Exa 6.1a Uniform Probability Distribution

```
1
                                      # Page no. : 234 -
                                          236
3 # Uniform Probability Distribution
5 a <- 120
6 b <- 140
7 fun_over_x <- 1/20
9 # Since uniform probability is symmetric we can
      split it into left and right parts which
10 # are symmetric in nature
11
12 c \leftarrow 130 # (120+140)/2 = 130
13
14 # Probability of uniform probability distribution
     is the area of the figure (rectangle)
15
16 # Area for the left symmetric part of the figure
```

```
17
18 area <- punif(c,a,b)
19 area_full <- 2 * area
20
21 cat("Probability is",area_full)
22
23 # Expected value, Variance and standard Deviation
24
25 expected_value <- (a + b) / 2
26 variance <- (b - a) ** 2 / 12
27 standard_deviation <- sqrt(variance)
28
29 cat("Expected value is",expected_value)
30 cat("Variance is",variance)
31 cat("Standard deviation is",standard_deviation)
```

### R code Exa 6.2a Normal Probability Distribution

```
15 z_value <- round(qnorm(probability), 2) # Round it
          to 2 decimal place
16 x <- (sigma * z_value) + mean
17
18 cat("Value of x for not more than 10% of area is
          selected is",x)</pre>
```

### R code Exa 6.3a Normal Approximation of Binomial Probabilities

```
1
                                          # Page no. : 251 -
                                              252
3 # Normal Approximation of Binomial Probabilities
5 n <- 100
6 p <- 0.1
7 q < -1 - p
9 mu <- n * p
10 sigma <- sqrt(mu * q)
11
12 \# P(x = 12) \implies P(11.5 \le x \le 12.5)
13
14 x1 <- 12.5
15 x2 <- 11.5
16 \text{ z\_value1} \leftarrow (x1 - mu) / sigma
17 \text{ z_value2} \leftarrow (x2 - mu) / sigma
18
19 area1 <- pnorm(z_value1)</pre>
20 area2 <- pnorm(z_value2)
21
22 diff <- area1 - area2
23
24 cat ("The normal approximation to the probability of
      12 successes in 100 trials is ", diff)
```

```
25
26 # Probability for 13
27
28 x <- 13.5
29 z <- (x - mu) / sigma
30 ans <- pnorm(z)
31
32 cat("Answer is", ans)
```

### R code Exa 6.4a Exponential Probability Distribution

```
# Page no. :
1
                                                255
3 # Exponential Probability Distribution
5 mu <- 15
6 x1 <- 6
7 x2 <- 18
9 \# P(x <= 6)
10
11 EPD \leftarrow pexp(x1,1/mu)
12
13 \# P(x \le 18)
14
15 EPD2 \leftarrow pexp(x2, 1/mu)
16
17 diff <- EPD2 - EPD
18
19 cat ("The probability that loading a truck will take
      between 6 and 18 minutes is ", diff)
20
21 SD <- mu
22 sigma <- SD ** 2
```

23 24 cat("Variance is", sigma)

## Chapter 7

# Sampling and Sampling Distribution

R code Exa 7.1a Point Estimator

```
1
                                                  # Page no
                                                     274
3 # Sample Mean and Sample Standard Deviation
5 annual_salary <- c
      (49094.30,53263.90,49643.50,49894.90,47621.60,55924.00,49092.30,5
                        55109.70,45922.60,57268.40,55688.80,51564.70,5618
6
7
                        51932.60,52973.00,45120.90,51753.00,54391.80,5016
8
                        50979.40,55860.90,57309.10)
  program <- c("Yes","Yes","Yes","Yes","No","Yes","Yes</pre>
      ", "Yes", "Yes", "Yes", "Yes", "No", "Yes", "No", "No", "No", "
      Yes",
               "No", "Yes", "Yes", "Yes", "Yes", "Yes", "No", "
11
```

```
No", "No", "No", "No", "Yes", "Yes", "No")
12
13
  dataset <- data.frame(annual_salary, program)</pre>
14
15 sample_mean <- mean(dataset$annual_salary)</pre>
16 sample_sd <- sd(dataset$annual_salary)</pre>
17
18 cat("Sample mean of the data is", sample_mean)
19 cat ("Sample saturdard deviation is", sample_sd)
20
21 # Note that : Book SD is different from our SD
22
23 # Sample Proportion
24
25 n <- nrow(dataset)
26 x <- 19
27
28 sample_proportion <- x / n
29
30 cat("Sample Proportion is", sample_proportion)
```

### R code Exa 7.2a Sampling Distribution

```
# Page no. 277
- 278

2
3 # Sampling Distribution

5 mean_annual_salary <- c("49500.00-49999.99","
50000.00-50499.99","50500.00-50999.99","
51000.00-51499.99",

6 "51500.00-51999.99","
52000.00-52499.99","
52500.00-52999.99","
53000.00-53499.99",
```

```
53500.00 - 53999.99")
7
8 frequency <- c(2,16,52,101,133,110,54,26,6)
9 relative_frequency <- c</pre>
      (.004,.032,.104,.202,.266,.220,.108,.052,.012)
10
11 DF <- data.frame(mean_annual_salary, frequency,</pre>
      relative_frequency)
12
  library(ggplot2)
13
14
  ggplot(DF, aes(mean_annual_salary, relative_frequency)
15
16
     geom_histogram(stat = "identity", fill = "purple")
         + labs(title = "Relative Frequency Histogram",
                                      x = " Mean Salary"
17
                                          y = "frequency"
```

### R code Exa 7.3a Sampling Distribution of Sample Mean

```
1
                                             # Page no. :
                                                281
3 # Sampling Distribution of xbar
5 sigma <- 4000
6 N <- 2500
7 n <- 30
8 \times - n / N
9
                    # Condition to include finite
10 \quad if(x > 0.05)
      population factor or not (< 5\%)
11 {
12
     standard_error \leftarrow sqrt((N-n)/(N-1)) * (sigma /
        sqrt(n))
```

```
13 } else{
     standard_error <- sigma / sqrt(n)</pre>
15 }
16
17 cat ("Standard deviation of sample mean is", standard_
      error)
18
                                          # Page no. : 284
19
20
21 # To find probability that xbar is between 51300 and
       52300
22
23 xbar1 <- 52300
24 xbar2 <- 51300
25 mu <- 51800
26
27 z1 <- (xbar1 - mu) / standard_error
28 z2 <- (xbar2 - mu) / standard_error
29
30 p1 <- pnorm(z1, lower.tail = T)
31 p2 <- pnorm(z2, lower.tail = T)
32
33 diff <- p1 - p2
34
35 cat ("Probability that xbar is between 51300 and
      52300 \, \text{is} ", diff)
```

R code Exa 7.3b Relationship between Sample Size and Sampling Distribution of xbar

#### Distribution of xbar

```
5 \text{ sigma} \leftarrow 4000
6 n <- 100
7 population_mean <- 51800
9 standard_error <- sigma / sqrt(n)
10
11 xbar1 <- 52300
12 xbar2 <- 51300
13
14 z1 <- (xbar1 - population_mean) / standard_error
15 z2 <- (xbar2 - population_mean) / standard_error
16
17 p1 <- pnorm(z1, lower.tail = T)
18 p2 \leftarrow pnorm(z2, lower.tail = T)
19
20 diff <- p1 - p2
21
22 cat ("Probability that xbar is between 51300 and
      52300 with increased sample size is", diff)
```

### R code Exa 7.4a Sampling Distribution of Sample Proportion

```
# Page no.
: 290

2
3 # Sampling Distribution of pbar

4
5 population_proportion <- 0.60
6 n <- 30
7 N <- 2500
8
9 x <- n / N
10
```

```
11 if(x > 0.05)
                 # Condition to include finite
      population or not (<5\%)
12 {
     standard_deviation <- sqrt((N-n)(N-1)) * sqrt((</pre>
13
        population_proportion *
                                                          (1
14
                                                             population
                                                             proportion
                                                             )
                                                             n
                                                             )
15 } else{
     standard_deviation <- sqrt((population_proportion</pre>
16
        * (1 - population_proportion)) / n)
17 }
18
19 cat ("Standard deviation for sample proportion is",
      standard_deviation)
```

R code Exa 7.4b Practical value of the Sampling Distribution of Sample Proportion

```
1 # Page no. : 291
2 3 # Practical value of the Sampling Distribution of pbar
```

```
4
5 population_proportion <- 0.60
6 standard_error <- 0.0894
7 sample_proportion <- 0.65
9 z_value <- (sample_proportion - population_
     proportion) / standard_error
10
11 prob1 <- pnorm(sample_proportion, population_
     proportion, standard_error, lower.tail =T)
12
13 sample_proportion2 <- 0.55</pre>
14
15 z_value <- (sample_proportion2 - population_
     proportion) / standard_error
16
17 prob2 <- pnorm(sample_proportion2, population_
     proportion, standard_error, lower.tail =T)
18
19 final_prob <- prob1 - prob2
20
21 cat("The final probability is", final_prob)
```

R code Exa 7.4c Practical value of the Sampling Distribution of Sample Proportion Eg2

```
# Page no. : 292 -
293

2
3 # Practical value of the Sampling Distribution of
    pbar Eg-2

4
5 population_proportion <- 0.60
6 n <- 100</pre>
```

```
8 standard_error <- sqrt(population_proportion*(1 -</pre>
     population_proportion)/(n))
9
10 sample_proportion <- 0.65
11
12 z_value <- (sample_proportion - population_
     proportion) / standard_error
13
14 prob1 <- pnorm(sample_proportion, population_
     proportion, standard_error, lower.tail =T)
15
16 sample_proportion2 <- 0.55
17
18 z_value <- (sample_proportion2 - population_
     proportion) / standard_error
19
20 prob2 <- pnorm(sample_proportion2, population_
     proportion, standard_error, lower.tail =T)
21
22 final_prob <- prob1 - prob2
23
24 cat("The final probability is", final_prob)
```

## Chapter 8

### Interval Estimation

R code Exa 8.1a Population Mean Sigma Known

```
1
                                         # Page no. :
                                            310 - 314
2 # Population Mean Sigma known
4 pop_sd <- 20
5 sample_size <- 100
6 sample_mean <- 82
8 standard_error <- pop_sd / sqrt(sample_size)</pre>
10 # 95% confidence interval
11
12 margin_of_error <- qnorm(0.975)*standard_error
     95\% confidence interval --> 1 - 0.025 = 0.975
13
14 IE <- sample_mean + c(-margin_of_error, margin_of_
     error)
15
16 cat ("The margin of error is given by", margin_of_
17 cat ("The 95% interval estimate is given by", IE)
```

```
18
19 # 90% confidence interval
20
21 margin_of_error <- qnorm(0.95)*standard_error
      90\% confidence interval \longrightarrow 1 - 0.05 = 0.95
22
23 IE <- sample_mean + c(-margin_of_error, margin_of_
      error)
24
  cat ("The margin of error is given by", margin_of_
      error)
  cat ("The 90% interval estimate is given by", IE)
26
27
28 # 99% confidence interval
29
30 margin_of_error <- qnorm(0.995)*standard_error</pre>
      99% confidence interval --> 1 - 0.005 = 0.995
31
32 IE <- sample_mean + c(-margin_of_error, margin_of_
      error)
33
34 cat ("The margin of error is given by", margin_of_
      error)
35 cat ("The 99% interval estimate is given by", IE)
```

### R code Exa 8.2a Population Mean Sigma Unknown

### R code Exa 8.2b Population Mean Sigma Unknown Eg2

### R code Exa 8.3a Determining the Sample Size

```
# Page no.:

326 - 327

# Determining the Sample Size

margin_of_error <- 2

z_value <- 1.96  # 95% Level of Confidence Interval

sample_standard_deviation <- 9.65

sample_size <- ((z_value)**2) * ((sample_standard_deviation)**2) / (margin_of_error)**2

cat("Sample size is",ceiling(sample_size))

# If Sample Size is not integer then we round up to next higher integer
```

### R code Exa 8.4a Population Proportion

```
# Page no.:
329

2
3 # Population Proportion
4
5 N <- 900
6 n <- 396</pre>
```

```
7
8 p <- n / N
9 q <- 1 - p
10
11 # Confidence Interval is 95%
12
13 \text{ z_value } \leftarrow \text{qnorm}(0.975)
                               # 95% confidence interval
     --> 1 - 0.025 = 0.975
14
15 margin_of_error <- z_value * sqrt((p*q)/N)
16 IE <- p + c(-margin_of_error, margin_of_error)</pre>
17
18 cat ("The margin of error is given by", margin_of_
      error)
19 cat ("The 95% interval estimate is given by", IE)
```

### R code Exa 8.4b Determining the Sample Size

```
1
                                            # Page no. :
                                               330
3 # Determining the Sample Size
4
5 margin_of_error <- 0.025</pre>
6 z_value <- 1.96 # 95% Level of Confidence Interval
8 p < -0.44
9 q <- 1 - p
10
11 sample_size <- ((z_value)**2 * p * q) / (margin_of_
     error) **2
12
13 cat("Sample size is", ceiling(sample_size))
14 # If Sample Size is not integer then we round up to
     next higher integer
```

```
15
                                          # Page no. :
16
                                              331
17
18 margin_of_error <- 0.025</pre>
19 z_value <- 1.96 # 95% Level of Confidence Interval
20
21 p <- 0.50
22 q <- 1 - p
23
24 sample_size <- ((z_value)**2 * p * q) / (margin_of_
      error)**2
25
26 cat("Sample size is", ceiling(sample_size))
27 # If Sample Size is not integer then we round up to
     next higher integer
```

## Chapter 9

## Hypothesis Testing

R code Exa 9.1a Population Mean Sigma Known One Tailed Test

```
1
                                           # Page no. :
                                               359 - 360
3 # Population Mean Sigma Known One Tailed Test
5 sigma <- 0.18
6 n <- 36
7 xbar <- 2.92
8 mu <- 3
10 z_value <- (xbar - mu) / (sigma / sqrt(n))
11 z_value <- round(z_value,2)</pre>
12
13 alpha <- 0.01
14
15 # P Value Approch (Lower-Tail Test)
16
17 pval <- pnorm(z_value)
18
19 if (pval > alpha)
20 {
```

```
cat("Since p-value ", pval ," is greater than 0.01,
21
        therefore we will accept null hypothesis")
22 } else {
     cat("Since p-value ", pval ," is less than 0.01,
23
        therefore we will reject null hypothesis and
        accept
         alternative hypothesis.")
24
25 }
26
27 # Critical Value Approch (Lower-Tail Test)
28
29 z_{alpha} \leftarrow qnorm(1 - (alpha))
                                     # Area of 0.01 to
      the left (1 - 0.01 = 0.99)
30 critical_approch <- -z_alpha
31
32 if(z_value <= critical_approch)</pre>
33 {
     cat("Since z-value", z_value ,"is less then or
34
        equal to", critical_approch, "therefore we
        reject
         the null hypothesis and accept the alternative
35
             hypothesis.")
36 } else{
     cat("Since z-value", z_value ,"is more than",
37
        critical_approch, "therefore we accept the null
        hypothesis.")
38 }
```

R code Exa 9.1b Population Mean Sigma Known Two Tailed Test

```
4
5 sample_size <- 50</pre>
6 sample_mean <- 297.6
7 population_mean <- 295
8 significance_level <- 0.05 # alpha
9 population_sd <- 12</pre>
10
                                              # Page no. :
11
                                                  364
12
13 ## Critical value approch
15 z_value <- (sample_mean - population_mean) / (
      population_sd / sqrt(sample_size))
16
17 z_half_alpha <- qnorm(1 - (significance_level/2))
18 critical_value_1 <- -z_half_alpha
19 critical_value_2 <- z_half_alpha</pre>
20
21 if(z_value >= critical_value_2 || z_value <=
      critical_value_1)
22 {
     \mathtt{cat}("Since z-value", z\_value ,"does not lie in the
23
         range", critical_value_1 , "and", critical_
        value 2
         ,"therefore we reject the null hypothesis and
24
            accept the alternative hypothesis.")
25 } else{
     cat("Since z-value", z_value ,"lies in the range",
         critical_value_1 , "and", critical_value_2
         ," therefore we accept the null hypothesis.")
27
28 }
29
30
                                             # Page no. :
                                                363 - 364
31
32 ## P-value approch
33
```

```
34 area_under_curve <- 1 - pnorm(z_value)
35 pval <- 2 * area_under_curve # P-value
36 if(pval > 0.05)
37 {
38    cat("Since p-value ",pval ,"is greater than 0.05,
        therefore we will accept null hypothesis")
39 } else {
40    cat("Since p-value ",pval ,"is less than 0.05,
        therefore we will reject null hypothesis and
        accept
41        alternative hypothesis.")
42 }
```

R code Exa 9.1c Relationship between Interval Estimation and Hypothesis Testing

```
1
                                          # Page no. :
                                             366 - 367
3 # Relationship between Interval Estimation and
     Hypothesis Testing
4
5 mu <- 295
6 alpha <- 0.05
7 n <- 50
8 xbar <- 297.6
9 sigma <- 12
10
11 z_value <- 1.96 # alpha = 0.05 so alpha/2 = 0.05/
     2 = 0.025 (z-value is for 0.025)
12
13 # 95% Confidence Interval
14
15 margin_of_error <- z_value * (sigma / sqrt(n))
16
```

R code Exa 9.2a Population Mean Sigma Unknown One Tailed Test

```
1
                                            # Page no. :
                                                371 -
                                               372
3 # Population Mean Sigma Unknown One Tailed Test
5 mu0 <- 7
6 alpha <- 0.05
7 xbar <- 7.25
8 s <- 1.052
9 n <- 60
11 t_value <- (xbar - mu0) / (s / sqrt(n))
12
13 df <- n - 1
14
15 # Upper Tail Test
16
17 pval <- pt(t_value, df = df, lower.tail = F) # Book
     answer is 0.354
```

R code Exa 9.2b Population Mean Sigma Unknown Two Tailed Test

```
1
                                           # Page no. :
                                               372 - 373
3 # Population Mean Sigma Unknown Two Tailed Test
5 mu0 <- 40
6 alpha <- 0.05
7 xbar <- 37.4
8 s <- 11.79
9 n <- 25
10
11 t_value <- (xbar - mu0) / (s / sqrt(n))
12
13 df <- n - 1 # Degree of Freedom
14
15 # Two Tail Test
16 # P - value Approach
17
18 pval \leftarrow 2 *(1 - pt(t_value, df = df, lower.tail = F))
        # Book answer is
                           0.2822
19
```

```
20 if (pval > alpha)
21 {
     \mathtt{cat} ("Since p-value", \mathtt{pval}, "is greater than 0.05,
22
        therefore we will accept null hypothesis")
23 } else {
24
     cat ("Since p-value", pval, "is less than 0.05,
        therefore we will reject null hypothesis and
        accept
         alternative hypothesis.")
25
26 }
27
28 # Critical Value Approach
29
30 t_half_alpha \leftarrow qt(1 - (alpha/2), df)
31 critical_value_1 <- -t_half_alpha
32 critical_value_2 <- t_half_alpha
33
34 if(t_value >= critical_value_2 || t_value <=
      critical_value_1)
35 {
     cat ("Since t-value", t_value, "does not lie in the
36
         range", critical_value_1 , "and", critical_
        value_2
         ," therefore we reject the null hypothesis and
37
            accept the alternative hypothesis.")
38 } else{
39
     cat("Since t-value", t_value, "lies in the range",
         critical_value_1 , "and", critical_value_2
         ,"therefore we accept the null hypothesis.")
40
41 }
```

#### R code Exa 9.3a Population Proportion

```
# Page no. : 377 - 378
```

```
3 # Population Proportion
5 p0 <- 0.20
6 alpha <- 0.05
7 n <- 400
8 x <- 100
10 p_bar <- x / n
12 z_value <- (p_bar - p0) / sqrt((p0*(1 - p0)) / n)
14 # Upper Tail Test
15
16 # P-value Approach
17
18 pval <- pnorm(z_value,lower.tail = F)</pre>
19 if (pval > alpha)
20 {
     cat("Since p-value ", pval ," is greater than 0.05,
21
        therefore we will accept null hypothesis")
22 } else {
     cat("Since p-value", pval," is less than 0.05,
23
        therefore we will reject null hypothesis and
        accept
         alternative hypothesis.")
24
25 }
26
27 # Critical Value Approach
28
29 z_alpha <- qnorm(1 - alpha)
30 critical_value <- z_alpha
31
32 if(z_value >= critical_value)
33 {
     cat("Since z-value", z_value ,"is greater then or
34
        equal to", critical_value, "therefore we
        reject
```

```
the null hypothesis and accept the alternative hypothesis.")

36 } else{
37    cat("Since z-value", z_value ,"is less than", critical_value, "therefore we accept the null hypothesis.")

38 }
```

#### R code Exa 9.4a Calculating the Probability of Type Second Errors

```
1
                                            # Page no. :
                                                382 - 383
3 # Calculating the Probability of Type Second Errors
5 mu0 <- 120
6 alpha <- 0.05
7 z_value <- 1.645
8 n <- 36
9 sigma <- 12
10
11 xbar <- mu0 - z_value * (sigma / sqrt(n))
12
13 mu <- 112
14 z <- (xbar - mu) / (sigma / sqrt(n))
15
16 # Upper Tail Test
17
18 beta_value <- pnorm(z, lower.tail = F)</pre>
19
20 cat("The type 2nd error is", beta_value)
21
22
                                        # Page no. : 384
23
24 xbar <- 116.71
```

```
25  mu <- 115
26  sigma <- 12
27  n <- 36
28
29  z <- (xbar - mu) / (sigma / sqrt(n))
30
31  # Upper Tail Test
32
33  beta_value <- pnorm(z, lower.tail = F)
34
35  cat("The type 2nd error is", beta_value)</pre>
```

#### R code Exa 9.5a Determining the Sample Size

```
1
                                             # Page no. :
                                                 389
3 # Determining the Sample Size
5 alpha <- 0.05
6 beta <- 0.10
7 z_alpha \leftarrow 1.645
8 z_beta <- 1.28
9 mu0 <- 120
10 mua <- 115
11 sigma <- 12
12
13 n <- ((z_alpha + z_beta)**2) * (sigma)**2 / (mu0 -
     mua)**2
                # Sample Size
14 n <- ceiling(n)
15 cat ("Sampling Size is",n)
```

## Chapter 10

## Inference About Means and Proportions With Two Populations

R code Exa 10.1a Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 known

```
# Page no.:
410

2
3 # Inference about the Difference between the two
Population Means Sigma 1 and Sigma 2 known

4
5 sigma1 <- 9
6 sigma2 <- 10
7 sample_size1 <- 36
8 sample_size2 <- 49
9 sample_mean1 <- 40
10 sample_mean2 <- 35
11
12 point_estimate <- sample_mean1 - sample_mean2
13
14 z_value <- qnorm(0.975) # alpha/2 = 0.05/2 = 0.025
```

```
= 1- 0.025 = 0.975

15

16 standard_error <- sqrt((((sigma1)^2)/(sample_size1)) + (((sigma2)^2)/(sample_size2)))

17

18 IE1 <- point_estimate + z_value*standard_error
19 IE2 <- point_estimate - z_value*standard_error
20

21 cat("The interval estimation for the given information at 95% confidence level is ",IE2 ,"to "

22 , IE1)
```

R code Exa 10.1b Hypothesis Tests About Difference between two Means

```
1
                                        # Page no. : 410
                                            -412
3 # Hypothesis Tests About Difference between two
     Means
5 sigma1 <- 10
6 sigma2 <- 10
7 alpha <- 0.05
8 n1 <- 30
9 n2 <- 40
10 xbar1 <- 82
11 xbar2 <- 78
12 DO <- 0
13
14 z_value <- ((xbar1 - xbar2) - D0) / sqrt(((sigma1)**
     2/n1) + ((sigma2)**2/n2))
15
16 # P-value Approach
17
```

```
18 # Two Tail Test
19
20 pval <- 2 * pnorm(z_value, lower.tail = F)
21
22 if (pval <= alpha)
23 {
     cat("Since P-Value", pval, "is less than or equal to
24
         0.05 therefore we can reject Null Hypothesis")
25 } else {
     cat ("Since P-Value", pval, "is more than 0.05
26
        therefore we cannot reject Null Hypothesis")
27 }
28
29 # Critical Value Approach
30
                                    \# \text{ alpha/2} = 0.05/2 =
31 z_half_alpha \leftarrow qnorm(0.975)
      0.025 = 1 - 0.025 = 0.975
32 critical_value_1 <- -z_half_alpha
33 critical_value_2 <- z_half_alpha</pre>
34
  if(z_value >= critical_value_2 || z_value <=</pre>
      critical_value_1)
36 {
     cat ("Since Z-value", z_value, "does not lie in the
37
        range", critical_value_1, "to", critical_value_2,
38
         "therefore we can reject Null Hypothesis")
39 } else {
     cat ("Since Z-value", z_value, "lie in the range",
40
        critical_value_1, "to", critical_value_2,
         "therefore we cannot reject Null Hypothesis")
41
42 }
```

R code Exa 10.2a Inference about the Difference between the two Population Means Sigma 1 and Sigma 2 Unknown

```
1
                                            # Page no. :
                                               415 - 417
3 # Inference about the Difference between the two
      Population Means Sigma 1 and Sigma 2 Unknown
5 s1 <- 150
6 s2 <- 125
7 n1 <- 28
8 n2 <- 22
9 xbar1 <- 1025
10 xbar2 <- 910
11
12 point_estimate <- xbar1 - xbar2
13
14 numerator <-((((s1)**2 /n1) + ((s2)**2 /n2))**2)
15 denomenator \leftarrow ((1 /(n1 -1)) * (((s1)**2 / n1)**2))
     + ((1 /(n2 -1)) * (((s2)**2 / n2)**2))
16
17 df <- numerator / denomenator # Degree of Freedom
18
                              \# \text{ alpha/2} = 0.05/2 = 0.025
19 t_value <- qt(0.975, df)
      = 1 - 0.025 = 0.975
20
21 standard_error <- sqrt((((s1)^2)/(n1)) + (((s2)^2)/(
     n2)))
22
23 IE1 <- point_estimate + t_value*standard_error
24 IE2 <- point_estimate - t_value*standard_error
25
26 cat ("The interval estimation for the given
      information at 95\% confidence level is ",IE2,
       "to", IE1)
27
```

R code Exa 10.2b Hypothesis Tests About Difference between two Means

```
1
                                             # Page no. :
                                                  418 -
                                                419
2
3 # Hypothesis Tests About Difference between two
     Means
4
5 \times < -c(300, 280, 344, 385, 372, 360, 288, 321, 376,
     290, 301, 283)
  y <- c(274, 220, 308, 336, 198, 300, 315, 258, 318,
     310, 332, 263)
8 DF <- data.frame(x,y)</pre>
10 test <- t.test(DF$x, DF$y, paired = F, alternative =
      "greater")
11
  test
12
13 # Upper Tail Test
14
15 if (test$p.value <= 0.05) # 95% Confidence Level
16 {
17
     cat ("Since P-Value", test$p.value, "is less than or
        equal to 0.05 therefore we can reject
         Null Hypothesis")
18
19 } else {
20
     cat("Since P-Value", test$p.value, "is more than
        0.05 therefore we cannot reject Null Hypothesis
        ")
21 }
```

R code Exa 10.3a Inference About the Difference Between Two Population Means Matched samples

```
1
                                            # Page no. :
                                               424 - 425
3 # Inference About the Difference Between Two
      Population Means Matched samples
5 workers <-c(1,2,3,4,5,6)
6 method_1 \leftarrow c(6.0,5.0,7.0,6.2,6.0,6.4)
7 method_2 \leftarrow c(5.4,5.2,6.5,5.9,6.0,5.8)
8 diff <- method_1 - method_2</pre>
10 dataFrame <- data.frame(workers, method_1, method_2,
       diff)
11
12 test <- t.test(dataFrame$method_1, dataFrame$method_</pre>
      2, paired = T)
13 test
14
15 # Two Tail Test
16
17 if(test$p.value <= 0.05)
18 {
     cat ("Since P-Value", test$p.value, "is less than or
19
        equal to 0.05 therefore we can
         reject Null Hypothesis")
20
21 } else {
     cat("Since P-Value", test$p.value, "is more than
        0.05 therefore we cannot reject Null Hypothesis
        ")
23 }
24
25 # Interval Estimate
26
27 IE1 <- test$conf.int[1]
28 IE2 <- test$conf.int[2]
29
30 cat ("The interval estimation for the given
      information at 95% confidence level is ",IE1 ,"to
```

31 IE2)

R code Exa 10.4a Inference About the Difference Between Two Population Proportions

```
1
                                           # Page no. :
                                              431
3 # Inference About the Difference Between Two
      Population Proportions
5 n1 <- 250
6 n2 <- 300
7 x1 <- 35
8 \times 2 < -27
9 alpha <- 0.1
10
11 pbar1 <- x1 / n1
12 pbar2 <- x2 / n2
13
14 qbar1 <- 1 - pbar1
15 qbar2 <- 1 - pbar2
16
17 # Interval Estimation
18
19 diff_prop <- pbar1 - pbar2
20
21 z_half_alpha <- qnorm(0.95) \# alpha / 2 = 0.1 /
      2 = 0.05 = 0.95 \quad (1 - 0.05)
22
23 margin_of_error <- z_half_alpha * sqrt((pbar1 *</pre>
      qbar1)/n1 + (pbar2 * qbar2)/n2)
24
25 IE1 <- diff_prop + margin_of_error
```

 ${f R}$  code Exa 10.4b Hypothesis Tests About Difference between two Proportions

```
1
                                            # Page no. :
                                               432 - 433
3 # Hypothesis Tests About Difference between two
      Proportions
5 pbar1 <- 0.14
6 pbar2 <- 0.09
7 n1 <- 250
8 n2 <- 300
9 alpha <- 0.10 # Significance Level
10
11 pbar \leftarrow ((n1 * pbar1) + (n2 * pbar2)) / (n1 + n2)
     # Pooled Estrimator
12
13 z_value <- (pbar1 - pbar2) / sqrt((pbar*(1 - pbar))*
      ((1/n1)+(1/n2))
14
15 # Two Tail Test
16
17 pval <- 2 * pnorm(z_value, lower.tail = F)
18
19 if (pval <= alpha)
20 {
21
     cat ("Since P-Value", pval, "is less than or equal to
         0.10 therefore we can reject Null Hypothesis")
```

## Chapter 11

# Inferences About Population Variances

R code Exa 11.1a Inferences About Population Variance

```
1
                                                 # Page no. :
                                                      453
3 # Inferences About the Population Variance
5 n <- 20
6 variance <- 0.0025
7 df <- 19 # Degrees of Freedom
9 \text{ chisq}_1 \leftarrow \text{qchisq}(0.975, \text{df})
10 chisq_2 <- qchisq(0.025,df)</pre>
11
12 # Interval Estimation
13
14 IE1 <- sqrt((df * variance) / chisq_1)</pre>
15 IE2 <- sqrt((df * variance) / chisq_2)</pre>
16
17 cat ("Interval Estimation at 95% confidence interval
      for population standard deviation is", IE1,
```

#### R code Exa 11.1b Hypothesis Testing

```
1
                                            # Page no. :
                                               455 - 456
3 # Hypothesis Testing
5 n < -24
6 alpha <- 0.05 # Significance Level
7 \text{ sigma0\_sq} \leftarrow 4
8 variance <- 4.9
10 chisq_value <- ((n - 1) * variance) / sigma0_sq
11
12 df <- n - 1 # Degree of Freedom
13
14 # Upper Tail Test
15
16 # P-value Approach
17
18 pval <- pchisq(chisq_value, df, lower.tail = F)</pre>
19
20 if(pval <= alpha)
21 {
     cat("Since pval", pval, "is less than or equal to
22
        0.05 therefore we can reject Null Hypothesis")
23 } else{
     cat("Since pval", pval, "is greater than 0.05
        therefore we cannot reject Null Hypothesis")
25 }
26
27 # Critical Value Approach
28
```

```
29 chisqvalue <- qchisq(0.95,df) # Chi-square value
      for 0.95 (1 - 0.05)
30
31 if(chisq_value >= chisqvalue)
32 {
33
     cat("Since Chi-square value",chisq_value,"is
        greater than or equal to Chi-square value",
        chisqvalue,
         "therefore we will reject Null Hypothesis")
34
35 } else {
     cat ("Since Chi-square value", chisq_value, "is less
36
        than Chi-square value", chisqvalue,
37
         "therefore we cannot reject Null Hypothesis")
38 }
39
40
41
                                              # Page no. :
                                                  456 -
                                                 457
42
43 n <- 30
44 alpha <- 0.05 # Significance Level
45 \text{ sigma0\_sq} \leftarrow 100
46 variance <- 162
47
48 chisq_value \leftarrow ((n - 1) * variance) / sigma0_sq
49
50 df <- n - 1 # Degree of Freedom
51
52 # Two Tail Test
53
54 # P-value Approach
55
56 pval <- 2 * pchisq(chisq_value, df, lower.tail = F)
57
58 if(pval <= alpha)
59 {
     cat ("Since pval", pval, "is less than or equal to
60
```

```
0.05 therefore we can reject Null Hypothesis")
61 } else{
62   cat("Since pval", pval, "is greater than 0.05
        therefore we cannot reject Null Hypothesis")
63 }
```

#### R code Exa 11.2a Inferences About Two Population Variances

```
1
                                           # Page no. :
                                              462 - 464
3 # Inferences About Two Population Variances
5 alpha <- 0.10 # Significance Level
6 n1 <- 26
7 n2 <- 16
8 sv1 <- 48
9 sv2 <- 20
10
11 f_value <- (sv1) / (sv2)
12
13 df1 <- n1 - 1 # Degrees of Freedom 1
14 df2 \leftarrow n2 - 1 # Degrees of Freedom 2
15
16 # Two Tail Test
17
18 # P-value Approach
19
20 pval <- 2 * pf(f_value,df1,df2,lower.tail = F)
21
22 if(pval <= alpha)
23 {
     cat ("Since pval", pval, "is less than or equal to
        0.10 therefore we can reject Null Hypothesis")
25 } else{
```

```
cat ("Since pval", pval, "is greater than 0.10
26
        therefore we cannot reject Null Hypothesis")
27 }
28
29 # Critical Value Approach
30
31 half_alpha <- alpha / 2
32 fval <- qf(0.95,df1,df2) \# half_alpha = 0.05 = 1
       -0.05 = 0.95
33
34 if(f_value >= fval)
35 - \{
36
     cat("Since F value",f_value,"is greater than or
        equal to F value", fval,
         "therefore we will reject Null Hypothesis")
37
     cat ("Since F value", f_value, "is less than F value"
39
        ,fval,
         "therefore we cannot reject Null Hypothesis")
40
41 }
42
                                            # Page no. :
43
                                                464
44
45 alpha <- 0.05 # Significance Level
46 n1 <- 41
47 n2 <- 31
48 sv1 <- 120
49 sv2 <- 80
50
51 \text{ f_value} \leftarrow (\text{sv1}) / (\text{sv2})
52
53 df1 <- n1 - 1
                    # Degrees of Freedom 1
54 df2 <- n2 - 1 \# Degrees of Freedom 2
56 # Upper Tail Test
57
58 # P-value Approach
```

```
59
60 pval <- pf(f_value,df1,df2,lower.tail = F)
61
62 if (pval <= alpha)
63 {
64
     cat ("Since pval", pval, "is less than or equal to
        0.10 therefore we can reject Null Hypothesis")
65 } else{
     cat("Since pval", pval, "is greater than 0.10
66
        therefore we cannot reject Null Hypothesis")
67 }
68
69 # Critical Value Approach
70
71 fval <- qf (0.90, df1, df2) \# alpha = 0.05 = 1 - 2
     * 0.05 = 0.90
72
73 if(f_value >= fval)
74 {
     cat("Since F value",f_value,"is greater than or
75
        equal to F value", fval,
         "therefore we will reject Null Hypothesis")
76
77 } else {
     cat("Since F value",f_value,"is less than F value"
78
        ,fval,
        "therefore we cannot reject Null Hypothesis")
79
80 }
```

## Chapter 12

## Tests of Goodness of Fit and Independence

R code Exa 12.1a Goodness of Fit Test A Multinomial Population

```
1
                                               # Page no. :
                                                  474 - 476
3 # Goodness of Fit Test A Multinomial Population
5 category <- c("Company A", "Company B", "Company C")
6 prop \leftarrow c(0.30, 0.50, 0.20)
7 freq1 \leftarrow c(48, 98, 54)
8 \text{ freq2} \leftarrow c(60, 100, 40)
9 diff <- freq1 - freq2
10 \text{ sq\_diff} \leftarrow (\text{diff})**2
11 answer <- sq_diff / freq2
12 DF <- data.frame(category, prop, freq1, freq2, diff,
       sq_diff, answer)
13
14 total_observe_freq <- sum(DF$freq1)
15 chisq_value <- sum(DF$answer)
16
17 alpha <- 0.05
```

```
18 df <- nrow(DF) - 1 # Degrees of Freedom
19
20 # Upper Tail Test
21
22 # P-value Approach
23
24 pval <- pchisq(chisq_value, df, lower.tail = F)
25
26 if (pval <= alpha)
27 {
     cat("Since pval", pval, "is less than or equal to
28
        0.05 therefore we can reject Null Hypothesis")
29 } else{
     cat ("Since pval", pval, "is greater than 0.05
        therefore we cannot reject Null Hypothesis")
31 }
32
33 # Critical Value Approach
34
35 chisqValue \leftarrow qchisq(0.95,df) # 1 - alpha = 1 -
      0.05 = 0.95
36
37 if(chisq_value >= chisqValue)
38 {
     cat("Since Chi-square value",chisq_value,"is
39
        greater than or equal to Chi-square value",
        chisqValue,
         "therefore we will reject Null Hypothesis")
40
     cat ("Since Chi-square value", chisq_value, "is less
42
        than Chi-square value", chisqValue,
         "therefore we cannot reject Null Hypothesis")
43
44 }
```

R code Exa 12.2a Tests of Independence

```
# Page no. :
1
                                                 480 - 482
3 # Tests of Independence
5 gender <- c("Male", "Female")
6 light <-c(20,30)
7 regular \leftarrow c(40,30)
8 \text{ dark} \leftarrow c(20,10)
9 total <-c(80,70)
10
11 DF <- data.frame(gender, light, regular, dark, total
12
13 test <- chisq.test(DF[,2:4])
14 test
15
16 # Upper Tail Test
17
18 if(test$p.value <= 0.05)
19 {
     cat("Since pval",test$p.value,"is less than or
20
        equal to 0.05 therefore we can reject
         Null Hypothesis")
21
22 } else{
     cat("Since pval", test$p.value, "is greater than
23
        0.05 therefore we cannot reject Null
         Hypothesis")
24
25 }
```

R code Exa 12.3a Goodness of Fit Test Poisson Distribution

```
1 # Page no. :
488 - 490
```

```
3 # Goodness of Fit Test Poisson Distribution
5 \times (0,1,2,3,4,5,6,7,8,9)
6 observed_freq <- c(2,8,10,12,18,22,22,16,12,6)
7 y <- x * observed_freq
8 e < -2.72
9
10 mu <- sum(y) / sum(observed_freq)
11 fun_of_x \leftarrow round(((mu)**x) * (e)**(-mu) / factorial
      (x), 4) # Function of x
12
13 expected_freq <- round(sum(observed_freq)*fun_of_x,</pre>
14
15 diff <- observed_freq - expected_freq
17 sq_diff <- round((diff)**2,2)</pre>
18
19 answer <- round(sq_diff / expected_freq,2)</pre>
20
21 DF <- data.frame(x,observed_freq,expected_freq,diff,
      sq_diff, answer)
22
23 total_observe_freq <- sum(DF$observed_freq)
24 total_expexted_freq <- sum(DF$expected_freq)
25
26 chisq_value <- sum(DF$answer)
27
28 df <- nrow(DF) - 2 # Degrees of Freedom (k - p - 1)
       where k = 10, p = 1
29
30 alpha <- 0.05
31
32 # Upper Tail Test
33
34 # P-value Approach
35
36 pval <- pchisq(chisq_value, df, lower.tail = F)
```

#### R code Exa 12.3b Goodness of Fit Test Normal Distribution

```
1
                                             # Page no. :
                                                491 - 494
3 # Goodness of Fit Test Normal Distribution
4
5 data <- c
      (71,66,61,65,54,93,60,86,70,70,73,73,55,63,56,62,76,54,82,79,76,68
6
              61,61,64,65,62,90,69,76,79,77,54,64,74,65,65,61,56,63,80,5
8 xbar <- mean(data)</pre>
9 s <- sd(data)
10
11 cat ("Value of mean is", xbar)
12 cat ("Value of standard variance is",s)
13
14 percentage \leftarrow c(0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9)
15 z <- c()
```

16 test\_score <- c()

```
17
18 for (i in 1:length(percentage)) {
    z[i] <- round(qnorm(percentage[i]),2)</pre>
20
    test_score[i] <- round(xbar + (z[i] * round(s,2)),</pre>
       2)
21 }
22
23 DF <- data.frame(percentage, z, test_score)
24
25 interval \leftarrow c("Less than 55.10", "55.10 to 59.68", "
      59.68 to 63.01", "63.01 to 65.82",
                  "65.82 to 68.42", "68.42 to 71.02", "
26
                      71.02 to 73.83", "73.83 to 77.16",
                  "77.16 to 81.74", "81.74 and over")
27
28 observed_freq \leftarrow c(5,5,9,6,2,5,2,5,5,6)
29 expected_freq \leftarrow c(5,5,5,5,5,5,5,5,5,5)
30
31 diff <- observed_freq - expected_freq
32 \text{ sq\_diff} \leftarrow (\text{diff})**2
33
34 answer <- (sq_diff) / expected_freq
35
36 dataset <- data.frame(interval, observed_freq,
      expected_freq, diff, sq_diff, answer)
37
38 chisq <- sum(dataset$answer)
39
40 alpha <- 0.10 # Significance Level
41
42 df <- nrow(dataset) - 3 # Degrees of Freedom (k -
      p - 1 where k = 10, p = 2)
43
44 # Upper Tail Test
45
46 # P-value Approach
47
48 pval <- pchisq(chisq,df,lower.tail = F)
49
```

## Chapter 13

# Experimental Design and Analysis of Variance

R code Exa 13.1a Analysis of Variance and the Completely Randomized Design

```
14
15 variance1 <- sum((DF$method_A - mean1)**2) / (nrow(
     DF)-1)
               # Sample Variance 1
16 variance2 <- sum((DF$method_B - mean2)**2) / (nrow(
     DF)-1)
             # Sample Variance 2
17 variance3 <- sum((DF$method_C - mean3)**2) / (nrow(
     DF)-1) # Sample Variance 3
18
                             # Sample Standard Variance
19 sd1 <- sqrt(variance1)</pre>
20 sd2 <- sqrt(variance2)
                             # Sample Standard Variance
  sd3 <- sqrt(variance3) # Sample Standard Variance
21
     3
22
23 \text{ sample_mean} \leftarrow (\text{mean1} + \text{mean2} + \text{mean3}) / 3
      Overall Sample Mean
24
25 variance <- ((mean1 - sample_mean)**2 + (mean2 -
      sample_mean)**2 + (mean3 - sample_mean)**2) /
      (3 - 1)
26 # Sample Varince for Overall Sample Mean (3 -->
     Methods)
27
28 sigma_sq <- nrow(DF) * variance # Between-
      treatment Estimate of Sigma Square
29
30 estimate_sigma_sq <- (variance1 + variance2 +
      variance3) / 3 # Within-treatment Estimate of
     Sigma Square
31
32 ratio <- sigma_sq / estimate_sigma_sq
33
34 cat ("Ratio of Between-treatment Estimate of Sigma
      Square by Within-treatment Estimate
       of Sigma Square is", ratio)
35
```

R code Exa 13.2a Analysis of Variance and the Completely Randomized Design

```
\# Page no. : 518
1
2
3 # Analysis of Variance and the Completely Randomized
       Design
4
5 \text{ method\_A} \leftarrow c(58,64,55,66,67)
6 method_B \leftarrow c(58,69,71,64,68)
7 method_C \leftarrow c(48,57,59,47,49)
9 DF <- data.frame(method_A, method_B, method_C)
10
                    # Number of Treatments
11 k <- ncol(DF)
12 n <- nrow(DF)
                    # Number of Observations for each
      Treatment
13 N <- n * k
                 # Total Observations
14
15 df_numerator <- k - 1 # Degrees of Freedom for
      Numerator
16 df_denomenator <- N - k # Degrees of Freedom for
      Denomenator
17
18 alpha <- 0.05
19
20 \times (c(t(as.matrix(DF))))
21 f <- c("method_A", "method_B", "method_C")
22 tm \leftarrow gl(k, 1, n*k, factor(f))
23 result <- anova(lm(x \sim tm)) # Similar to aov(x \sim tm)
      tm)
24
25 result
26
```

```
27 # Upper Tail Test
28
29 # Critical Value Approach
30
31 fval \leftarrow qf(0.95, df_numerator, df_denomenator) # 1
      - \text{ alpha} = 1 - 0.05 = 0.95
32 fval <- round(fval, 2)
33
34 fvalue <- result $ 'F value '[1]
36 if(fvalue >= fval)
37 - \{
38
     cat ("Since F value", fvalue, "is greater than or
        equal to F value", fval,
         "therefore we will reject Null Hypothesis")
39
     cat ("Since fvalue value", fvalue, "is less than
41
        fvalue value", fval,
         "therefore we cannot reject Null Hypothesis")
42
43 }
44
45 # P-value Approach
46
47 pval <- pf(fvalue, df_numerator, df_denomenator, lower.</pre>
      tail = F)
48
49 if(pval <= alpha)
50 {
     cat ("Since pval", pval, "is less than or equal to
51
        0.05 therefore we can reject Null Hypothesis")
52 } else{
53
     cat ("Since pval", pval, "is greater than 0.05
        therefore we cannot reject Null Hypothesis")
54 }
```

#### R code Exa 13.3a Multiple Comparison Procedures Fishers LSD

```
# Page no. : 525
1
                                               -526
3 # Multiple Comparison Procedures : Fisher's LSD
5 \text{ method\_A} \leftarrow c(58,64,55,66,67)
6 \text{ method\_B} \leftarrow c(58,69,71,64,68)
7 method_C \leftarrow c(48,57,59,47,49)
9 DF <- data.frame(method_A,method_B,method_C)
10
                    # Number of Treatments
11 k \leftarrow ncol(DF)
                    # Number of Observations for each
12 n <- nrow(DF)
      Treatment
13 N <- n * k
                 # Total Observations
14
15 x <- c(t(as.matrix(DF)))</pre>
16 f <- c ("method_A", "method_B", "method_C")
17 tm <- gl(k, 1, n*k, factor(f))
18 result \leftarrow anova(lm(x ~ tm)) # Similar to aov(x ~
      tm)
19
20 # Approach - 1
21
22 # Fisher's LSD Procedure for Method A and Method B
23
24 t_value1 <- (mean(DF$method_A) - mean(DF$method_B))
      / sqrt(result$'Mean Sq'[2] * ((1 / n)
25
```

```
26
27 t_value1 <- round(t_value1, 2)
28
29 df <- N - k # Degrees of Freedom
30
31 # Two Tail Test
32
33 # P-value Approach
34
35 alpha <- 0.05
36
37 pval <- 2 * pt(t_value1, df, lower.tail = T)
39 if(pval <= alpha)
40 {
     cat ("Since pval", pval, "is less than or equal to
41
        0.05 therefore we can reject Null Hypothesis")
42 } else{
     \mathtt{cat} ("Since pval", pval, "is greater than 0.05
43
        therefore we cannot reject Null Hypothesis")
44 }
45
46 tval \leftarrow qt (0.975, df) # alpha/2 = 0.05 / 2 =
      0.025 = (1 - 0.025) = 0.975
47 tval <- round(tval, 3)
48
49 LSD <- tval * sqrt(result $`Mean Sq'[2] * ((1 / n) +
      (1 / n))
50 LSD <- round(LSD, 2)
51
52 \# Approach - 2
54 # Fisher's LSD Procedure for Method A and Method C
55
56 diff_A_C <- mean(DF$method_A) - mean(DF$method_C)
```

```
57
58 if(diff_A_C > LSD)
59 {
     cat ("Since the value of difference", diff_A_C," is
60
        greater than LSD", LSD, "therefore we will reject
         Null Hypothesis")
61
62 } else{
     cat ("Since the value of difference", diff_A_C," is
63
        less than LSD", LSD, "therefore we cannot reject
         Null Hypothesis")
64
65 }
66
67 # Fisher's LSD Procedure for Method B and Method C
68
69 diff_B_C <- mean(DF$method_B) - mean(DF$method_C)
70
71 if(diff_B_C > LSD)
72 {
     cat ("Since the value of difference", diff_B_C," is
73
        greater than LSD", LSD, "therefore we will reject
74
         Null Hypothesis")
75 } else{
     cat ("Since the value of difference", diff_B_C," is
76
        less than LSD", LSD, "therefore we cannot reject
77
         Null Hypothesis")
78 }
```

#### R code Exa 13.4a Randomized Block Design

```
# Page no.:
534

2
3 # Randomized Block Design
4
5 blocks <- c("Controller 1", "Controller 2", "
```

```
Controller 3", "Controller 4", "Controller 5", "
      Controller 6")
6 system_A <- c(15, 14, 10, 13, 16, 13)
7 system_B <- c(15, 14, 11, 12, 13, 13)
8 system_C <- c(18, 14, 15, 17, 16, 13)
10 DF <- data.frame(blocks, system_A, system_B, system_
      C)
11
12 k <- ncol(DF) - 1 # Number of Treatments (blocks
      is not the treatement)
13 b <- nrow(DF) # Number of blocks
14 N <- k * b
               # Total sample Size
15
16 x \leftarrow c(t(as.matrix(DF[,-1])))
17 f <- c("system_A", "system_B", "system_C")
18 tm <- gl(k, 1, N, factor(f))
19 blk \leftarrow gl(b, k, N)
20 result \leftarrow anova(lm(x ~ tm + blk)) # Similar to aov
      (x - tm)
21
22 result
23
24 f_value <- result\(^F\) value \(^[1]\)
25
26 # Upper Tail Test
27
28 # P-value Approach
29
30 pval <- result$'Pr(>F)'[1]
31
32 \text{ if (pval } \leq 0.05)
33 {
     cat ("Since pval", pval, "is less than or equal to
34
        0.05 therefore we can reject Null Hypothesis")
35 } else{
     cat ("Since pval", pval, "is greater than 0.05
        therefore we cannot reject Null Hypothesis")
```

# R code Exa 13.5a Factorial Design

```
# Page no. : 542
1
2
3 # Factorial Experiment
5 program <- c("Three-hour review", "Three-hour review
      ", "One-day program", "One-day program", "10-week
       course",
                 "10-week course")
7 business \leftarrow c(500, 580, 460, 540, 560, 600)
8 engineering \leftarrow c(540, 460, 560, 620, 600, 580)
9 \text{ arts\_and\_science} \leftarrow c(480, 400, 420, 480, 480, 410)
10
11 DF <- data.frame(program, business, engineering,
      arts_and_science)
12
            # Number of levels in Factor A (Unique
13 a <- 3
      Programs)
14 b <- 3
            # Number of levels in Factor B (Columns
      Except program)
15 r <- 2
            # Number of Replications (Each Program has
      2 Replications)
16 N <- a * b * r # Total Observations
17
18 x \leftarrow c(t(as.matrix(DF[,-1])))
19 f1 <- c("Three-hour review", "One-day program", "10-
      week course")
20 f2 <- c("business", "engineering", "arts and science
      ")
21 \text{ tm} 2 \leftarrow gl(a, 1, N, factor(f1))
22 tm1 \leftarrow gl(b, r * a, N, factor(f2))
23 result \leftarrow anova(lm(x ~ tm1 * tm2))
                                          # Similar to
```

```
aov(x * tm)
24
25 result
26
27 alpha <- 0.05
28
29 # Upper Tail Test
30
31 pval1 <- result\(^\text{'Pr(>F)'[1]}\)
32 pval2 <- result$'Pr(>F)'[2]
33 pval3 <- result$'Pr(>F)'[3]
34
35 if (pval1 <= alpha)
36 {
     cat ("Since pval", pval1, "is less than or equal to
37
        0.05 therefore we can reject Null Hypothesis
          for Undergraduation.")
38
39 } else{
     cat ("Since pval", pval1, "is greater than 0.05
40
        therefore we cannot reject Null Hypothesis
         for Undergraduation.")
41
42 }
43
44 \text{ if}(pval2 \ll alpha)
45 {
     cat ("Since pval", pval2, "is less than or equal to
46
        0.05 therefore we can reject Null Hypothesis
          for programs.")
47
48 } else{
     cat ("Since pval", pval2, "is greater than 0.05
49
        therefore we cannot reject Null Hypothesis
50
          for programs.")
51 }
52
53 if (pval3 <= alpha)
54 {
     cat ("Since pval", pval3, "is less than or equal to
55
        0.05 therefore we can reject Null Hypothesis
```

```
56     for interaction.")
57     } else{
58     cat("Since pval",pval3,"is greater than 0.05
          therefore we cannot reject Null Hypothesis
59          for interaction.")
60     }
```

# Chapter 14

# Simple Linear Regression

R code Exa 14.1a Least Squares Method

```
1
                                          # Page no. : 565
                                             -566
3 # Least Squares Method
5 restaurant \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 student_population \leftarrow c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
      (58,105,88,118,117,137,157,169,149,202)
9 DF <- data.frame(restaurant, student_population,
      quartely_sales)
10
11 # Install Library if not installed
12
13 # install.packages("ggplot2")
14
15 # Import Library
16
17 library(ggplot2)
18
```

```
19 ggplot(DF,aes(student_population, quartely_sales)) +
       geom_point() +
     labs(title = "Scatter Plot between Student
20
        Population and Quartely Sales", x = "Student
21
          Population (1000s)", y = "Quartely Sales ($
             1000s)")
22
                                      # Page no. : 567 -
23
                                          569
24
25 regressor <- lm(quartely_sales ~ student_population,
      data = DF)
26 res <- summary(regressor)
27
28 res
29
30 b1 <- res$coefficients[[2]]
31
32 b0 <- res$coefficients[[1]]
33
34 cat ("Estimated Regression Equation is y_cap =",b0,"+
     ",b1,"x")
35
36 ggplot(DF,aes(student_population, quartely_sales)) +
       geom_point() +
     geom_smooth(method='lm', se = F) + labs(title = "
37
        Scatter Plot between Student Population
38 and Quartely Sales", x = "Student Population (1000s)"
     , y = "Quartely Sales (\$1000s)")
```

## R code Exa 14.2a Coefficient of Determination

```
1 # Page no. : 576-580
```

```
3 # Coefficient of Determination
5 restaurant \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 student_population \leftarrow c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
      (58, 105, 88, 118, 117, 137, 157, 169, 149, 202)
8
9 DF <- data.frame(restaurant, student_population,
      quartely_sales)
10
11 regressor <- lm(quartely_sales ~ student_population,
       data = DF)
12 res <- summary(regressor)</pre>
13
14 table <- anova(regressor)</pre>
15
16 SSE <- table $'Sum Sq'[2] # Sum of Squares due to
      Error
17
18 cat ("Value of SSE is", SSE)
19
20 SSR <- table $'Sum Sq'[1] # Sum of Squares due to
      Regression
21
22 cat("Value of SSR is", SSR)
23
                       # Total Sum of Squares
24 SST <- SSE + SSR
25
26 cat ("Value of SST is", SST)
27
28 r_sq <- res$r.squared # Coefficient of
      Determination
29
30 corrcoeff <- sqrt(r_sq) # Correlation Coefficient
31
32 cat ("Value of Coefficient of Determination is", r_sq)
33 cat ("Value of correlation Coefficient is", corrcoeff)
```

# R code Exa 14.3a Test of Significance

```
1
                                             # Page no. :
                                                485 - 489
3 # Test of Significance
5 restaurant \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 \text{ student\_population} \leftarrow c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
      (58, 105, 88, 118, 117, 137, 157, 169, 149, 202)
8
9 DF <- data.frame(restaurant, student_population,
      quartely_sales)
10
11 regressor <- lm(quartely_sales ~ student_population,
       data = DF)
12 res <- summary(regressor)</pre>
13
14 standard_error_MSE <- res$sigma
15
16 cat("Value of square root of MSE is", standard_error_
      MSE)
17
18 b1 <- res$coefficients[2]
19
20 tval <- res$coefficients[6]
21
22
23 # T Test
24
25 # Two Tail Test
26
27 # P-value Approach
```

```
28
29 pval <- round(res$coefficients[8],3)
30
31 \text{ if (pval } >= 0.01)
32 {
33
     cat ("Since pval", pval, "is greater than or equal to
         0.01 therefore we cannot reject the Null
        Hypothesis")
34 } else{
     cat ("Since pval", pval, "is less than 0.01 therefore
         we can reject the Null Hypothesis")
36
37 }
38
39 # F Test
40
41 test <- anova (regressor)
42
43 fval <- test\( 'F \) value '
44
45 pval \leftarrow round(test^{\circ}(Pr(>F)'[1],3) # P value is
      extremely small ie negligible to 0
46
47 \text{ if (pval } >= 0.01)
48 {
     cat ("Since pval", pval, "is greater than or equal to
49
         0.01 therefore we cannot reject the Null
        Hypothesis")
50 } else{
     cat ("Since pval", pval, "is less than 0.01 therefore
         we can reject the Null Hypothesis")
52
53 }
54
55 # Confidence Interval
56
57 confidence <- confint(regressor, "student_population
      ", level = 0.99)
```

R code Exa 14.4a Using the Estimated Regression Equation for Estimation and Prediction

```
1
                                      # Page no. : 595 -
                                          597
3 # Using the Estimated Regression Equation for
      Estimation and Prediction
5 restaurant \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 student_population \leftarrow c(2,6,8,8,12,16,20,20,22,26)
7 quartely_sales <- c
      (58,105,88,118,117,137,157,169,149,202)
8
9 DF <- data.frame(restaurant, student_population,
      quartely_sales)
10
11 regressor <- lm(quartely_sales ~ student_population,</pre>
       data = DF)
12 res <- summary(regressor)</pre>
13
14 pred <- predict(regressor, data.frame(student_
      population=10), interval="confidence")
15
16 PE <- pred[1]
17 IE1 <- pred[2]
18 IE2 <- pred[3]
19
20 cat ("Point estimate is", PE)
```

```
21 cat("Confidence Interval is ",IE1, "to", IE2)
22
23 pred2 <- predict(regressor, data.frame(student_ population=10), interval="predict")
24
25 IE1 <- pred2[2]
26 IE2 <- pred2[3]
27
28 cat("Prediction Confidence Interval is ",IE1, "to", IE2)</pre>
```

### R code Exa 14.5a Residual Analysis Validating Model Assumptions

```
# Page no. : 605
1
                                             -609
3 # Residual Analysis : Validating Model Assumptions
5 \times (2,6,8,8,12,16,20,20,22,26)
                                        # Student
      Population
6 y <- c (58,105,88,118,117,137,157,169,149,202)
                                                     #
  estimated_sales \leftarrow 60 + (5 * x)
                                      # Regression
      Equation = 60 + 5 x
10 residuals <- y - estimated_sales</pre>
11
12 DF <- data.frame(x, y, estimated_sales, residuals)
13
14 # Install Library if not installed
16 # install.packages("ggplot2")
17
18 # Import Library
```

```
19
20 library(ggplot2)
21
22 ggplot(DF,aes(x, residuals)) + geom_point() + geom_
     hline(yintercept = 0, linetype=2) +
23 labs(title = "Residual Plot", x = "X", y = "Residual
     ")
24
  ggplot(DF,aes(estimated_sales, residuals)) + geom_
25
     point() + geom_hline(yintercept = 0,
           linetype=2) + labs(title = "Plot between
26
              Estimated Sales and Residuals", x =
27
                                 "Estimated Sales", y =
                                    "Residual")
```

#### R code Exa 14.5b Standardized Residuals

```
1
                                        # Page no. : 610 -
                                           612
2
3 # Standardized Residuals
5 i \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 x <- c(2,6,8,8,12,16,20,20,22,26) # Student
      Population
7 n <- 10
8 s <- 13.829 # Standard error
9 y \leftarrow c (58,105,88,118,117,137,157,169,149,202)
      Sales
10
11 estimated_sales \leftarrow 60 + (5 * x)
                                         # Regression
      Equation = 60 + 5 x
12
13 x_{deviation} \leftarrow x - mean(x)
14
```

```
15 \text{ x\_deviation\_sq} \leftarrow (\text{x\_deviation})**2
16
17 z <- round(x_deviation_sq / sum(x_deviation_sq),4)
18
19 h \leftarrow round ((1 / n) + z, 4)
20
                                         # Standard
21 \text{ s_i} \leftarrow \text{round}(\text{s} * \text{sqrt}(1 - \text{h}), 4)
      Deviation for Residual i
22
23 residuals <- y - estimated_sales
24
25 standard_residuals <- round((residuals) / (s_i), 4)
26
27 DF <- data.frame(x, y, estimated_sales, x_deviation,
       x_deviation_sq, z, h, s_i, residuals, standard_
      residuals)
28
29 # Install Library if not installed
30
31 # install.packages("ggplot2")
32
33 # Import Library
34
35 library(ggplot2)
36
37 ggplot(DF,aes(x, standard_residuals)) + geom_point()
       + geom_hline(yintercept = 0, linetype=2) +
      labs(title = "Scatter Plot between x and
38
         Standard Residuals", x = "X",
            y = "Standard Residuals")
39
40
41 normal_scores <- round(qqnorm(1:10)$x, 2)
42 standard_residuals <- sort(standard_residuals,
      decreasing = F)
43
44 table <- data.frame(normal_scores, standard_
      residuals)
45
```

# R code Exa 14.6a Detecting Outliers

```
# Page no. : 615

# Page no. : 615

# Detecting Outliers

x <- c(1,1,2,3,3,3,4,4,5,6)

y <- c(45,55,50,75,40,45,30,35,25,15)

But by the state of the state
```

### R code Exa 14.6b Detecting Influential Observations

```
# Page no.:
617 - 618

## Detecting Influential Observations

x <- c(10, 10, 15, 20, 20, 25, 70)

y <- c(135, 130, 120, 115, 120, 110, 100)
</pre>
```

```
8 DF <- data.frame(x, y)</pre>
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF, aes(x, y)) + geom_point() + labs(title =
     "Scatter Plot between x and y", x = "X",
                                                 y = "Y")
19
20
21 point <- x[7] # From Scatter Plot
23 h <- (1 / nrow(DF)) + (((point - mean(DF$x))**2) / (
     sum((DF\$x - mean(DF\$x))**2)))
24
25 cat ("Leverage at point 7 is", h)
```

# Chapter 15

# Multiple Regression

R code Exa 15.1a Least Squares Method

```
1
                                          # Page no. :
                                              646 - 647
3 # Least Squares Method
5 driving_assignment \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 x <- c(100,50,100,100,50,80,75,65,90,90) # Miles
      Traveled
7 y \leftarrow c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1)
      Travel Time (hours)
9 DF <- data.frame(driving_assignment, x ,y)
10
11 # Install Library if not installed
12
13 # install.packages("ggpolt2")
14
15 # Import Library
16
17 library(ggplot2)
18
```

```
19 ggplot(DF,aes(x, y)) + geom_point() +labs(title = "
      Scatter Plot between Miles Traveled
     and Travel Time", x = "Miles Traveled", y = "
20
        Travel Time in Hours")
21
22
                                        # Page no. : 647
                                           -648
23
24 model \leftarrow lm(y \sim x, data = DF)
25 summ <- summary(model)
26 summ
27
28 b0 <- model$coefficients[1]
29 b1 <- model$coefficients[2]
30
31 cat ("Linear Regression Equation is y_cap =",b0,"+",
      b1,"x1")
32
33 # F Test
34
35 fval <- summ$fstatistic[1]
36
37 # Upper Tail Test
38
39 # P-value Approach
40
41 alpha <- 0.05
42
43 pval <- summ$coefficients[8] # P-value
44
45 if (pval >= alpha)
46 {
47
     cat ("Since pval", pval, "is greater than or equal to
         0.01 therefore we cannot reject the Null
        Hypothesis")
48 } else{
     cat ("Since pval", pval, "is less than 0.05 therefore
         we can reject the Null Hypothesis")
```

```
50
51 }
```

#### R code Exa 15.2a Two Independent Variables

```
# Page no. : 648
1
                                               -649
3 # Two Independent Variables
5 driving_assignment \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 \times 1 < c(100,50,100,100,50,80,75,65,90,90) # Miles
      Traveled
  x2 \leftarrow c(4,3,4,2,2,2,3,4,3,2) # Number of
      Deliveries
  y \leftarrow c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1)
      Travel Time (hours)
10 DF <- data.frame(driving_assignment, x1, x2, y)
11
12 model \leftarrow lm(y \sim x1 + x2, data = DF)
13 summary (model)
14
15 b0 <- model$coefficients[1]
16 b1 <- model$coefficients[2]
17 b2 <- model$coefficients[3]
18
19 cat ("Multiple Regression Equation is y_cap =",b0,"+"
      , b1 , "x1 +", b2 , "x2")
```

R code Exa 15.3a Multiple Coefficient of Determination

```
1
                                            # Page no. :
                                                654 - 655
3 # Multiple Coefficient of Determination
5 driving_assignment \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 \times 1 \leftarrow c(100,50,100,100,50,80,75,65,90,90)
      Traveled
7 \times 2 \leftarrow c(4,3,4,2,2,2,3,4,3,2) \# Number of
      Deliveries
8 y \leftarrow c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1)
      Travel Time (hours)
9
10 DF <- data.frame(driving_assignment, x1, x2, y)
11
12 model \leftarrow lm(y \sim x1 + x2, data = DF)
13 summ <- summary(model)</pre>
14
15 mean_y <- mean(DF$y)
                          # Mean of Travel time
16
17 predicted_travel_time <- round(predict(model), 2)</pre>
18
19 DF <- cbind(DF, predicted_travel_time)</pre>
20
21 SSR <- sum((DF$predicted_travel_time - mean_y)**2)</pre>
        # Sum of Squares due to Regression
22
23 cat ("Value of SSR is", SSR)
25 SSE <- sum((DF$y - DF$predicted_travel_time)**2)
       Sum of Squares due to Error
26
27 cat ("Value of SSE", SSE)
28
                        # Total Sum of Squares
29 SST <- SSR + SSE
30
31 cat("Value of SST", SST)
32
```

## R code Exa 15.4a Testing of significance

```
1
                                              # Page no. :
                                                 660 - 662
3 # Testing for Significance
5 driving_assignment \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 \times 1 < c(100,50,100,100,50,80,75,65,90,90) # Miles
      Traveled
7 \times 2 \leftarrow c(4,3,4,2,2,2,3,4,3,2) \# Number of
      Deliveries
  y \leftarrow c(9.3,4.8,8.9,6.5,4.2,6.2,7.4,6.0,7.6,6.1)
      Travel Time (hours)
10 DF <- data.frame(driving_assignment, x1, x2, y)
11
12 model \leftarrow lm(y \sim x1 + x2, data = DF)
13 summ <- summary(model)</pre>
14
15 SSR <- 21.6252
                     # Sum of Squares due to Regression
16
17 SSE <- 2.2952
                      # Sum of Squares due to Error
```

```
18
19 n <- nrow(DF) # Total Observations
20
21 p <- 2 # Number of Independent Variables
22
23 MSR <- SSR / p # Mean Square due to Regression
24
25 cat ("Value of MSR is", MSR)
26
27 MSE <- SSE / (n - p - 1) # Mean Square due to
     Error
28
29 # F Test
30
31 fval <- summ$fstatistic[1]
32
33 alpha <- 0.01
34
35 # Upper Tail Test
36
37 # P-value Approach
38
39 pval <- summ$coefficients[11]
40
41 if (pval >= alpha)
42 {
43
     cat ("Since pval", pval, "is greater than or equal to
         0.01 therefore we cannot reject the Null
        Hypothesis")
44 } else{
     cat ("Since pval", pval, "is less than 0.01 therefore
         we can reject the Null Hypothesis")
46
47 }
48
49 s <- summ$sigma # Standard Error of the Estimate
51 cat ("Value of Standard Error of the Estimate is",s)
```

```
52
53 coeff <- as.data.frame(summ$coefficients)
54
55 b1 <- coeff$Estimate[2]
56 b2 <- coeff $Estimate [3]
57
58 s1 <- coeff$'Std. Error'[2]
                                   # Standard Error of
      the x1 (Miles Traveled)
59 s2 <- coeff$'Std. Error'[3]
                                    # Standard Error of
      the x2 (Number of Deliveries)
60
61 df <- n - p - 1 # Degrees of Freedom
62
63 # T Test
64
65 \text{ tval1} \leftarrow \text{round}(b1 / s1, 3)
66 \text{ tval2} \leftarrow \text{round}(b2 / s2, 3)
67
68 # Upper Tail Test
69
70 # P-value Approach
71
72 pval1 <- round(pt(tval1, df, lower.tail = F),5)
73 pval2 <- round(pt(tval2, df, lower.tail = F),5)
74
75
76 if(pval1 >= alpha && pval2 >= alpha)
77 {
     cat ("Since pval1", pval1, "and pval2", pval2, "is
78
        greater than or equal to 0.01 therefore we
        cannot reject the
79
          Null Hypothesis")
80 } else{
     cat("Since pval1", pval1, "and pval2", pval2, "is less
81
         than 0.01 therefore we can reject the Null
        Hypothesis")
82
83 }
```

### R code Exa 15.5a Categorical Independent Variables

```
1
                                            # Page no. :
                                               668 - 671
3 # Categorical Independent Variables
5 service <- c(1:10)
6 month \leftarrow c(2,6,8,3,2,7,9,8,4,6)
7 repair <- c("electrical", "mechanical", "electrical", "
      mechanical", "electrical", "electrical",
                "mechanical", "mechanical", "electrical", "
8
                   electrical")
9 time \leftarrow c(2.9, 3.0, 4.8, 1.8, 2.9, 4.9, 4.2, 4.8,
      4.4, 4.5
10
11 DF <- data.frame(service, month, repair, time)
12
13 # With one Independent variable
14
15 regressor \leftarrow lm(time ~ month, data = DF)
16 res <- summary(regressor)</pre>
17
18 \text{ res}
19
20 b0 <- res$coefficients[1]
21 b1 <- res$coefficients[2]
22
23 cat ("Equation is y = ", b0 ,"+",b1,"x1")
24
25 # With Categorical Variable
26
27 DF$repair <- factor(DF$repair,
                         levels = c('electrical', '
28
```

```
mechanical'),
                          labels = c(1, 0)
29
30
31 regressor \leftarrow lm(time ~ month + repair, data = DF)
32 res <- summary(regressor)</pre>
33
34 \text{ res}
35
36 b0 <- res$coefficients[1]
37 b1 <- res$coefficients[2]
38 b2 <- res$coefficients[3]
39
40 # For Electrical Repair
41
42 \text{ bterm} \leftarrow b0 + b2 * 1
43
44 cat ("Equation for electrical is y = ", bterm ,"+",
      b1,"x1")
45
46 # For Mechanical Repair
47
48 \text{ bterm2} \leftarrow b0 + b2 * 0
49
50 cat ("Equation for mechanical is y = ", bterm2,"+",
      b1,"x1")
```

### R code Exa 15.6a Residual Analysis

```
# Page no.:
676 - 679

Residual Analysis

miles <- c(100, 50, 100, 100, 50, 80, 75, 65, 90, 90)</pre>
```

```
6 deliveries \leftarrow c(4, 3, 4, 2, 2, 2, 3, 4, 3, 2)
7 time \leftarrow c(9.3, 4.8, 8.9, 6.5, 4.2, 6.2, 7.4, 6.0,
      7.6, 6.1)
9 DF <- data.frame(miles, deliveries, time)
10
11 regressor <- lm(time ~ miles + deliveries, data = DF
12 res <- summary(regressor)</pre>
14 predict <- predict(regressor)</pre>
15 residuals <- DF$time - predict
16 std_residuals <- rstandard(regressor)</pre>
17
18 DF <- cbind(DF, predict, residuals, std_residuals)</pre>
19
20 View(DF)
21
22 # Install Library if not installed
23
24 # install.packages("ggplot2")
25
26 # Import Library
27
28 library(ggplot2)
29
30 ggplot(DF,aes(predict, std_residuals)) + geom_point
      () + geom_hline(yintercept = 0,
         linetype=2) + labs(title = "Plot between
31
            predicted values and standardizes residuals
            ", x =
                                          "Prediction", y
32
                                             Standardization
                                              Residual")
33
34
35 leverage <- hatvalues(regressor)
```

```
36 cook_dist <- cooks.distance(regressor)
37
38 DF <- cbind(DF, leverage, cook_dist)
39
40 View(DF)
```

# R code Exa 15.6b Influential Observations

```
# Page no. :
1
                                                679 - 680
3 # Influential Observations
5 \times (-c(1, 1, 2, 3, 4, 4, 5, 15))
6 \text{ y} \leftarrow c(18, 21, 22, 21, 23, 24, 26, 39)
8 DF <- data.frame(x, y)</pre>
10 regressor \leftarrow lm(y ~x, data = DF)
11 res <- summary(regressor)</pre>
12
13 lev <- hatvalues(regressor)</pre>
14 DF <- cbind(DF, lev)
15
16 View(DF)
17
18
19 # Install Library if not installed
20
21 # install.packages("ggplot2")
22
23 # Import Library
24
25 library(ggplot2)
26
```

```
27 ggplot(DF,aes(x, y)) + geom_point() + geom_smooth(
      method = "lm", se = F) +
     labs(title = "Plot between x and y", x = "X", y =
28
        "Y")
29
30
31 cat("Equation is y = ",res$coefficients[1],"+",res$
      coefficients[2], "x1")
32
33
34 # Removing Influential Observation
35
36 \times (-c(1, 1, 2, 3, 4, 4, 5))
37 \text{ y} \leftarrow c(18, 21, 22, 21, 23, 24, 26)
38
39 DF <- data.frame(x, y)
40
41 regressor \leftarrow lm(y ~x, data = DF)
42 res <- summary(regressor)
43
44 cat("Equation is y = ",res$coefficients[1],"+",res$
      coefficients[2], "x1")
```

#### R code Exa 15.7a Logistic Regression

```
# Page no.:
684 - 686

Logistic Regression

customer <- c(1,2,3,4,5,6,7,8,9,10)

spending <- c
(2.291,3.215,2.135,3.924,2.528,2.473,2.384,7.076,1.182,3.345)

card <- c(1,1,1,0,1,0,0,0,1,0)
```

```
8 coupon <- c(0,0,0,0,0,1,0,0,1,0)
9
10 DF <- data.frame(customer, spending, card, coupon)
11
12 regressor <- glm(coupon ~ spending + card, data = DF
          )
13 summary(regressor)
14
15 # Book answer is different</pre>
```

# Chapter 16

# Regression Analysis Model Building

R code Exa 16.1a General Linear Model

```
16 library (ggplot2)
17
18 ggplot(DF, aes(x,y)) + geom_point() + labs(title = "
      Scatter Plot between Months
19
     Employed and Scales sold", x = "Months Employed",
        y = "Scales Sold")
20
21 model \leftarrow lm(y \sim x, data = DF)
  summary(model)
22
23
24 b1 <- model$coefficients[1]
25 b2 <- model$coefficients[2]
26
27 cat ("Regression Equation is sales =",b1,"+",b2,"
     months")
28 \# Book Answer is sales = 111 + 2.38 months
      is wrongly used in book)
29
30 predicted_scales_sold <- predict(model)
31
32 DF <- cbind(DF, predicted_scales_sold)
33
34 # Standard Residuals
35
36 standard_residuals <- rstandard(model)
37
38 DF <- cbind(DF, standard_residuals)
39
40 ggplot(DF,aes(predicted_scales_sold, standard_
     residuals)) + geom_point() +
     geom_hline(yintercept = 0, linetype=2) +
41
42 labs(title = "Scatter Plot between Predicted scales
      sold and Standard Residuals",
        x = "Predicted scales sold", y = "Standard
43
           Residuals")
44
                                           # Page no. :
45
                                              716 - 717
```

```
46
47 	 x2 < - x**2
48
49 DF2 \leftarrow data.frame(x,x2,y)
50
51 model2 \leftarrow lm(y \sim x + x2, data = DF2)
52 summary (model2)
53
54 b1 <- model2$coefficients[1]
55 b2 <- model2$coefficients[2]
56 b3 <- model2$coefficients[3]
57
58 cat ("Regression Equation is sales =",b1,"+",b2,"
     months", "+", b3, "monthsq")
59 \# Book Answer is sales = 45.3 + 6.34 months - 0.0345
       monthsq (Data is wrongly used in book)
60
61 predicted_scales_sold2 <- predict(model2)</pre>
62
63 DF2 <- cbind(DF2, predicted_scales_sold2)
64
65 # Standard Residuals
66
67 standard_residuals2 <- rstandard(model2)
68
69 DF2 <- cbind(DF2, standard_residuals2)
70
71 ggplot(DF2,aes(predicted_scales_sold2, standard_
      residuals2)) + geom_point() +
     geom_hline(yintercept = 0, linetype=2) +
72
     labs(title = "Scatter Plot between Predicted
73
        scales sold and Standard Residuals",
          x = "Predicted scales sold", y = "Standard
74
             Residuals")
```

#### R code Exa 16.1b Interaction

```
# Page no. : 718
1
                                             -721
3 # Interaction
5 price \leftarrow c(2.00, 2.50, 3.00, 2.00, 2.50, 3.00, 2.00,
       2.50, 3.00, 2.00, 2.50, 3.00,
               2.00, 2.50, 3.00, 2.00, 2.50, 3.00, 2.00,
6
                   2.50, 3.00, 2.00, 2.50, 3.00)
   advertising \leftarrow c(50, 50, 50, 50, 50, 50, 50, 50, 50,
       50, 50, 50, 100, 100, 100, 100, 100,
                     100, 100, 100, 100, 100, 100, 100)
  sales \leftarrow c(478, 373, 335, 473, 358, 329, 456, 360,
      322, 437, 365, 342, 810, 653, 345, 832, 641,
10
               372, 800, 620, 390, 790, 670, 393)
11
12 DF <- data.frame(price, advertising, sales)
13
14 # Install Library if not install
15
16 # install.packages("dplyr")
17
18 # Import Library
19
20 library(dplyr)
21
22 DF %>% group_by(price,advertising) %>% summarize(
      Average=mean(sales))
23
  model <- lm(sales ~ price + advertising + (price *</pre>
      advertising), data = DF)
25 res <- summary(model)
26
27 b0 <- res$coefficients[1]
28 b1 <- res$coefficients[2]
29 b2 <- res$coefficients[3]
```

```
30 b3 <- res$coefficients[4]
31
32 cat("Equation is sales = ", b0, "+", b1, "Price +", b2, "AdvExp +", b3, "PriAdv")
```

R code Exa 16.1c Transformations Involving the Dependent Variables

```
1
                                        # Page no. : 721
                                            -724
3 # Transformations Involving the Dependent Variables
5 x <- c
      (2289,2113,2180,2448,2026,2702,2657,2106,3226,3213,3607,2888)
        # Weight
6 y <- c
      (28.7,29.2,34.2,27.9,33.3,26.4,23.9,30.5,18.1,19.5,14.3,20.9)
        # Miles Per Gallon
8 DF <- data.frame(x,y)</pre>
10 # Install Library if not install
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF, aes(x,y)) + geom_point() + labs(title = "
      Scatter Plot between Weight and Miles
                                                Per
19
                                                   Gallon
                                                   ", x =
```

```
", y =
                                                     Miles
                                                     Per
                                                     Gallon
                                                     ")
20
21 \mod \text{c} - \ln(y \text{ x, data} = DF)
22 summary (model)
23
24 b1 <- model$coefficients[1]
25 b2 <- model$coefficients[2]
26
27 cat ("Regression Equation is sales =",b1,"+",b2,"
      months")
28
29 # Prediction
30
31 predicted_miles_per_gallon <- predict(model)</pre>
32
33 DF <- cbind(DF, predicted_miles_per_gallon)
34
35 # Standard Residuals
36
37 standard_residuals <- rstandard(model)</pre>
38
39 DF <- cbind(DF, standard_residuals)</pre>
40
41
   ggplot(DF,aes(predicted_miles_per_gallon, standard_
      residuals)) + geom_point() +
     geom_hline(yintercept = 0, linetype=2) +
43
     labs(title = "Scatter Plot between Predicted Miles
44
         per Gallon and Standard Residuals",
            x = "Predicted Miles per Gallon", y = "
45
               Standard Residuals")
46
```

Weight

```
47 # Log Transformation
48
49 \# \log_{x} < - \log(x)
\log_y < \log(y)
51
52 DF2 <- data.frame(x, log_y)
53
54 options(scipen = 999)
                            # To display not in
      scientific notation
55 \mod \text{c} - \ln(\log_y \text{ x, data} = DF2)
56 summary (model)
57
58 b1 <- model$coefficients[1]
59 b2 <- model$coefficients[2]
60
61 cat ("Regression Equation is sales =",b1,"+",b2,"
      months")
62
63 # Prediction
64
65 predicted_miles_per_gallon <- predict(model)
66
67 DF2 <- cbind(DF2, predicted_miles_per_gallon)
68
69 # Standard Residuals
70
71 standard_residuals <- rstandard(model)
72
73 DF2 <- cbind(DF2, standard_residuals)
74
75
76 ggplot(DF2,aes(predicted_miles_per_gallon, standard_
      residuals)) + geom_point() +
     geom_hline(yintercept = 0, linetype=2) + labs(
77
        title = "Scatter Plot between Log
78 Transformation of Predicted Miles per Gallon and
      Standard Residuals",
          x = "Predicted Miles per Gallon", y = "
79
```

#### R code Exa 16.2a Analysis of a Large Problem

```
# Page no. : 736
1
                                             -738
3 # Analysis of a Large Problem
5 Sales <- c(3669.88, 3473.95, 2295.10, 4675.56,
      6125.96, 2134.94, 5031.66, 3367.45, 6519.45,
              4876.37, 2468.27, 2533.31, 2408.11,
6
                 2337.38, 4586.95, 2729.24, 3289.40,
                 2800.78,
              3264.20, 3453.62, 1741.45, 2035.75,
                 1578.00, 4167.44, 2799.97)
  Time \leftarrow c(43.10, 108.13, 13.82, 186.18, 161.79,
      8.94, 365.04, 220.32, 127.64, 105.69, 57.72,
      23.58,
             13.82, 13.82, 86.99, 165.85, 116.26,
9
                42.28, 52.84, 165.04, 10.57, 13.82,
                8.13, 58.44,
10
             21.14)
11 Poten <- c(74065.1, 58117.3, 21118.5, 68521.3,
      57805.1, 37806.9, 50935.3, 35602.1, 46176.8,
      42053.2,
               36829.7, 33612.7, 21412.8, 20416.9,
12
                 36272.0, 23093.3, 26878.6, 39572.0,
                 51866.1, 58749.8,
              23990.8, 25694.9, 23736.3, 34314.3,
13
                 22809.5)
   AdvExp \leftarrow c(4582.9, 5539.8, 2950.4, 2243.1, 7747.1,
      402.4, 3140.6, 2086.2, 8846.2, 5673.1, 2761.8,
               1991.8, 1971.5, 1737.4, 10694.2, 8618.6,
15
                   7747.9, 4565.8, 6022.7, 3721.1,
```

```
861.0, 3571.5,
                2845.5, 5060.1, 3552.0)
16
   Share \leftarrow c(2.51, 5.51, 10.91, 8.27, 9.15, 0.15,
17
      8.54, 7.07, 12.54, 8.85, 5.38, 5.43, 8.48, 7.80,
               10.34, 5.15, 6.64, 5.45, 6.31, 6.35,
18
                  7.37, 8.39, 5.15, 12.88, 9.14)
   Change \leftarrow c(0.34, 0.15, -0.72, 0.17, 0.50, 0.15,
      0.55, -0.49, 1.24, 0.31, 0.37, -0.65, 0.64, 1.01,
                0.11, 0.04, 0.68, 0.66, -0.10, -0.03,
20
                   -1.63, -0.43, 0.04, 0.22, -0.74)
21 Accounts \leftarrow c(74.86, 107.32, 96.75, 195.12, 180.44,
      104.88, 256.10, 126.83, 203.25, 119.51, 116.26,
22
                  142.28, 89.43, 84.55, 119.51,80.49,
                     136.58, 78.86, 136.58, 138.21,
                     75.61, 102.44,
23
                  76.42, 136.58, 88.62)
24 Work <- c(15.05, 19.97, 17.34, 13.40, 17.64, 16.22,
      18.80, 19.86, 17.42, 21.41, 16.32, 14.51,
              19.35, 20.02, 15.26, 15.87, 7.81, 16.00,
25
                 17.44, 17.98, 20.99, 21.66, 21.46,
                 24.78,
              24.96)
26
27 Rating \leftarrow c(4.9, 5.1, 2.9, 3.4, 4.6, 4.5, 4.6, 2.3,
      4.9, 2.8, 3.1, 4.2, 4.3, 4.2, 5.5, 3.6, 3.4,
                4.2, 3.6, 3.1, 1.6, 3.4, 2.7, 2.8, 3.9)
28
29
30 DF <- data.frame(Sales, Time, Poten, AdvExp, Share,
      Change, Accounts, Work, Rating)
31 View(DF)
32
33 library(corrplot)
34
35 matrix <- round(cor(DF), 3)
36 matrix
37
  regressor <- lm(Sales ~ Time + Poten + AdvExp +
      Share + Change + Accounts + Work + Rating,
39
                    data = DF)
```

```
40 summary (regressor)
41
  cat("Equation is Sales = ",regressor$coefficients
42
      [1],"+",regressor$coefficients[2],"Time +",
43
       regressor$coefficients[3], "Poten +", regressor$
          coefficients[4], "AdvExp +", regressor$
          coefficients [5],
       "Share +", regressor $ coefficients [6], "Change +",
44
          regressor$coefficients[7], "Accounts +",
       regressor$coefficients[8], "Work +", regressor$
45
          coefficients[8], "Rating")
46
47 # Book Answer is different
48
  regressor2 <- lm(Sales ~ Poten + AdvExp + Share,
      data = DF)
  summary(regressor2)
50
51
  cat("Equation is Sales = ",regressor2$coefficients
52
      [1],"+",regressor2$coefficients[3],"Poten +",
       regressor2$coefficients[4], "AdvExp +", regressor2
53
          $coefficients[5],
       "Share")
54
55
56 # Book Answer is different
```

R code Exa 16.3a Multiple Regression Approach to Experimental Design

```
# Page no.: 745 -
747

2

3 # Multiple Regression Approach to Experimental
Design

4

5 A <- c(58,64,55,66,67)
```

```
6 B \leftarrow c(58,69,71,64,68)
7 \quad C \leftarrow c(48,57,59,47,49)
9 DF <- data.frame(A,B,C)
10
11 newA <- c(1,1,1,1,1,0,0,0,0,0,0,0,0,0,0)
12 newB \leftarrow c(0,0,0,0,0,1,1,1,1,1,0,0,0,0,0)
13 y <- c(58,64,55,66,67,58,69,71,64,68,48,57,59,47,49)
14
15 DF2 <- data.frame(newA, newB, y)
16
17 regressor <- lm(y ~ newA + newB, data = DF2)
18 summary(regressor)
19
20 cat("Equation is y = ",regressor$coefficients[1],"+"
      ,regressor$coefficients[2],"A+",
       regressor$coefficients[3],"B")
21
```

### Chapter 17

### **Index Numbers**

R code Exa 17.1a Price Relatives

```
1
                                          # Page no. : 765
3 # Price Relatives
5 year <- c
      (1990, 1991, 1992, 1993, 1994, 1995, 1996, 1997, 1998, 1999, 2000, 2001, 2002
7 price_per_gallon <- c(1.30,
      1.10,1.09,1.07,1.08,1.11,1.22,1.20,1.03,1.14,1.48,1.42,1.34,1.56,
9 DF <- data.frame(year,price_per_gallon)</pre>
10
11 base_year <- 1990
12 base_year_price <- DF$price_per_gallon[DF$year ==
      base_year]
13
14 price_relative <- round(((DF$price_per_gallon) / (</pre>
      base_year_price)) * 100, 2)
15
```

```
16 DF <- cbind(DF, price_relative)
17
18 View(DF)</pre>
```

#### R code Exa 17.2a Aggregate Price Indexes

```
1
                                           # Page no. :
                                              766
2
3 # Aggregate Price Indexes
5 item <- c("Gallon of gasoline", "Quart of oil", "Tire"
      "," Insurance policy,
6 year_1990 \leftarrow c(1.30,2.10,130.00,820.00)
7 year_2008 <- c(3.25,8.00,140.00,1030.00)
8 quantity \leftarrow c(1000, 15, 2, 1)
10 DF <- data.frame(item, year_1990, year_2008, quantity)
11
12 base_year <- 1990
13
14 sum_of_1990_items <- sum(DF$year_1990)
15
16 sum_of_2008_items <- sum(DF$year_2008)
17
18 aggregate_index_2008 <- (sum_of_2008_items / sum_of_
      1990_items) * 100
19
20 cat ("The unweighted aggregate index for year 2008 is
      ",aggregate_index_2008)
21
22
23 sum_of_1990_items <- sum(DF$year_1990 * DF$quantity)
         # Weighted Sum
24
```

R code Exa 17.3a Computing an Aggregate Price Index from Price Relatives

```
# Page no. : 769
1
                                          -770
3 # Computing an Aggregate Price Index from Price
      Relatives
5 item <- c("Gallon of gasoline", "Quart of oil", "Tire"
      ", Insurance policy,
6 year_1990 <- c(1.30,2.10,130.00,820.00)
7 year_2008 <- c(3.25,8.00,140.00,1030.00)
8 quantity \leftarrow c(1000,15,2,1)
10 DF <- data.frame(item, year_1990, year_2008, quantity)
11
12 base_year <- 1990
13
14 price_relative <- (DF$year_2008 / DF$year_1990) *
      100
15
16 weight <- DF$year_1990 * DF$quantity
17
18 weight_price_relative <- price_relative * weight
19
```

```
20 DF <- cbind(DF, price_relative, weight, weight_price
    _relative)
21
22 aggregate_2008 <- sum(DF$weight_price_relative) /
    sum(DF$weight)
23
24 cat("Aggregate Price Index for year 2008 is",
    aggregate_2008)</pre>
```

#### R code Exa 17.4a Deflating a Series by Price Indexes

```
1
                                           # Page no. :
                                              774
3 # Deflating a Series by Price Indexes
5 year <- c(2004,2005,2006,2007,2008)
6 hourly_wage <- c(15.69,16.12,16.76,17.45,18.07)
7 CPI \leftarrow c(188.9,195.3,201.6,207.3,215.3)
9 DF <- data.frame(year, hourly_wage, CPI)
10
11 # Install Library if not installed
12
13 # install.packages("ggplot2")
14
15 # Import Library
16
17 library(ggplot2)
18
19 ggplot(DF, aes(year, hourly_wage)) + geom_line() +
     geom_point() +
20
    labs(title = "Year V/S Hourly Wage Graph", x = "
       Year", y = "Hourly Wage")
21
```

## Chapter 18

# Time Series Analysis and Forecasting

R code Exa 18.1a Time Series Patterns

```
point() + ylim(c(0,25)) + labs(title =

"Week V/S Sales Time Series
Plot", x = "Weeks", y = "
Sales")
```

#### R code Exa 18.1b Time Series Patterns Eg2

```
1
                                        # Page no. : 787
                                            -788
3 # Time Series Patterns Eg-2
5 week <- c
      (1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22)
6 sales <- c
      (17,21,19,23,18,16,20,18,22,20,15,22,31,34,31,33,28,32,30,29,34,3
8 DF <- data.frame(week, sales)</pre>
10 # Install Library if not installed
12 # install.packages("gpplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF,aes(week,sales)) + geom_line() + geom_
     point() + ylim(c(0,40)) +
19 labs(title = "Week V/S Sales Time Series Plot", x =
     "Weeks", y = "Sales")
```

#### R code Exa 18.1c Time Series Patterns Eg3

```
1
                                           # Page no. :
                                               788 - 789
3 # Time Series Patterns Eg-3
5 year \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 sales <- c
      (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)
8 DF <- data.frame(year, sales)</pre>
10 # Install Library if not installed
11
12 # install.packages("gpplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18
  ggplot(DF,aes(year,sales)) + geom_line() + geom_
      point() + ylim(c(20,34)) +
    labs(title = "Years V/S Sales Time Series Plot", x
19
       = "Years", y = "Sales")
```

#### R code Exa 18.1d Time Series Patterns Eg4

```
# Page no. : 789
- 790
```

```
3 # Time Series Patterns Eg-4
5 year \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 revenue <- c
      (23.1,21.3,27.4,34.6,33.8,43.2,59.5,64.4,74.2,99.3)
7
8 DF <- data.frame(year, revenue)
10 # Install Library if not installed
11
12 # install.packages("gpplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
18 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
     point() + ylim(c(0,120)) +
    labs(title = "Years V/S Revenue Time Series Plot",
19
      x = "Years", y = "Revenue")
```

#### R code Exa 18.1e Time Series Patterns Eg5

```
Quarters
8 sales <- c(125, 153, 106, 88, 118, 161, 133, 102,
      138, 144, 113, 80, 109, 137, 125, 109, 130, 165,
              128, 96)
9
10
11 DF <- data.frame(year_quart, sales)</pre>
12
13 # Install Library if not installed
14
15 # install.packages("gpplot2")
16
17 # Import Library
18
19 library(ggplot2)
20
  ggplot(DF,aes(year_quart,sales, group = 1)) + geom_
21
      line() + geom_point() + ylim(c(0,180)) +
     labs(title = "Years/quart V/S Sales Time Series
22
        Plot", x = "Year/Quarter", y = "Sales")
```

#### R code Exa 18.1f Time Series Patterns Eg6

```
# Page no.:

791 - 792

# Time Series Patterns Eg-6

year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
"Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",

"Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
"Y4 Q2", "Y4 Q3", "Y4 Q4")

# Years and Quarters

sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
```

#### R code Exa 18.2a Forecast Accuracy

```
1
                                              # Page no. :
                                                 793 - 795
3 # Forecast Accuracy
5 week \leftarrow c(1,2,3,4,5,6,7,8,9,10,11,12)
6 sales \leftarrow c(17,21,19,23,18,16,20,18,22,20,15,22)
7 forcast <- c(NA, 17, 21, 19, 23, 18, 16, 20, 18, 22, 20, 15)
9 DF <- data.frame(week, sales, forcast)
10
11 forcast_error <- DF$sales - DF$forcast</pre>
12
13 absolute_forecast_error <- abs(forcast_error)</pre>
14
15 square_absolute_forcast_error <- absolute_forecast_</pre>
      error**2
16
```

```
17 percent_error <- round((forcast_error / DF$sales) *
      100, 2)
18
19 absolute_percent_error <- abs(percent_error)</pre>
20
21 DF <- cbind(DF, forcast_error, absolute_forecast_error</pre>
      ,square_absolute_forcast_error,
22
               percent_error, absolute_percent_error)
23
24 View(DF)
25
26 total_forcast_error <- sum(DF$forcast_error, na.rm =
27
28 total_absolute_forcast_error <- sum(DF$absolute_</pre>
      forecast_error, na.rm = T)
29
30 total_sq_abs_error <- sum(DF$square_absolute_forcast
     \_error, na.rm = T)
31
32 total_percent_error <- sum(DF$percent_error, na.rm =
       T)
33
34 total_absolute_percent_error <- sum(DF$absolute_
     percent_error, na.rm = T)
35
36 # Native Value
37
38 MAE <- round(total_absolute_forcast_error / (nrow(DF
     )-1), 2)
                 # Not including 1st row
39 # Mean Absolute Error
40
41 MSE <- round(total_sq_abs_error / (nrow(DF)-1), 2)
       # Not including 1st row
42 # Mean Square Error
43
44 MAPE <- round(total_absolute_percent_error / (nrow(
     DF)-1), 2) \# Not including 1st row
```

```
45 # Mean Absolute Percent Error
46
47 cat ("Value of MAE is", MAE)
48 cat ("Value of MSE is", MSE)
49 cat("Value of MAPE is", MAPE)
50
51 # Average of Past Values
52
53 forcast2 <- c(NA
      ,17.00,19.00,19.00,20.00,19.60,19.00,19.14,19.00,19.33,19.40,19.0
54
55 DF2 <- data.frame(week, sales, forcast2)
56
57 forcast_error2 <- DF2$sales - DF2$forcast2
58
59 absolute_forecast_error2 <- abs(forcast_error2)
60
61 square_absolute_forcast_error2 <- absolute_forecast_
      error2**2
62
63 percent_error2 <- round((forcast_error2 / DF2$sales)
       * 100, 2)
64
65 absolute_percent_error2 <- abs(percent_error2)
66
67 DF2 <- cbind(DF2, forcast_error2, absolute_forecast_
      error2, square_absolute_forcast_error2,
68
               percent_error2, absolute_percent_error2)
69
70 View(DF2)
71
72 total_forcast_error2 <- sum(DF2$forcast_error2, na.</p>
      rm = T)
73
74 total_absolute_forcast_error2 <- sum(DF2$absolute_
      forecast_error2, na.rm = T)
75
```

```
76 total_sq_abs_error2 <- sum(DF2$square_absolute_
      forcast_error2, na.rm = T)
77
78 total_percent_error2 <- sum(DF2$percent_error2, na.
     rm = T)
79
80 total_absolute_percent_error2 <- sum(DF2$absolute_
     percent_error2, na.rm = T)
81
82 MAE2 <- round(total_absolute_forcast_error2 / (nrow(
     DF2)-1), 2)
                   # Not including 1st row
83 # Mean Absolute Error
84
85 MSE2 <- round(total_sq_abs_error2 / (nrow(DF2)-1),
         # Not including 1st row
86 # Mean Square Error
87
88 MAPE2 <- round(total_absolute_percent_error2 / (nrow
      (DF2)-1), 2)
                   # Not including 1st row
89 # Mean Absolute Percent Error
90
91 cat ("Value of MAE is", MAE2)
92 cat ("Value of MSE is", MSE2)
93 cat("Value of MAPE is", MAPE2)
```

#### R code Exa 18.3a Moving Averages

```
9 DF <- data.frame(week, sales, forcast)
10
11 forcast_error <- DF$sales - DF$forcast
12
13 absolute_forecast_error <- abs(forcast_error)</pre>
14
15 square_absolute_forcast_error <- absolute_forecast_</pre>
      error**2
16
17 percent_error <- round((forcast_error / DF$sales) *
      100, 2)
18
19 absolute_percent_error <- abs(percent_error)</pre>
20
21 DF <- cbind(DF, forcast_error, absolute_forecast_error</pre>
      ,square_absolute_forcast_error,
22
                percent_error, absolute_percent_error)
23
24 View(DF)
25
26 # Install Library if not installed
27
28 # install.packages("ggplot2")
29
30 # Import Library
31
32 library(ggplot2)
33
34 ggplot(DF, aes(week)) + geom_line(aes(y = forcast),
      color = "red") +
     geom_line(aes(y = sales), color = "blue") + geom_
35
        point(aes(y = forcast)) +
36
     geom_point(aes(y = sales))+
     ylim(c(0,25)) +
37
     labs(title = "Week V/S Sales Time Series Plot", x
38
        = "Week", y = "Sales")
```

#### R code Exa 18.3b Exponential Smoothing

```
1
                                         # Page no. : 802
                                             -803
3 # Exponential Smoothing
5 week \leftarrow c(1,2,3,4,5,6,7,8,9,10,11,12)
6 sales \leftarrow c(17,21,19,23,18,16,20,18,22,20,15,22)
7 forcast <- c(NA,17.00,17.80, 18.04, 19.03, 18.83,
      18.26, 18.61, 18.49, 19.19, 19.35, 18.48)
8 forcast_error <- sales - forcast</pre>
9 forcast_error_sq <- (forcast_error)**2
10
11 DF <- data.frame(week, sales, forcast, forcast_error
      , forcast_error_sq)
12
13 View(DF)
14
15 # Install Library if not installed
16
17 # install.packages("ggplot2")
18
19 # Import Library
20
21 library(ggplot2)
22
23
    ggplot(DF,aes(week)) + geom_line(aes(y = forcast),
       color = "red") +
      geom_line(aes(y = sales), color = "blue") + geom_
24
         point(aes(y = forcast)) +
      geom_point(aes(y = sales))+
25
26
       ylim(c(0,25)) +
27
     labs(title = "Week V/S Sales Time Series Plot", x
```

```
= "Week", y = "Sales")
```

#### R code Exa 18.4a Trend Projection

```
1
                                          # Page no. :
                                             807 - 808
3 # Trend Projection
5 year \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 sales <- c
      (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)
8 DF <- data.frame(year, sales)</pre>
10 # Install Library if not installed
11
12 # install.packages("ggplot2")
13
14 # Import Library
15
16 library(ggplot2)
17
  ggplot(DF,aes(year,sales)) + geom_line() + geom_
18
     point() + ylim(c(20,34)) +
    labs(title = "Years V/S Sales Time Series Plot", x
19
      = "Years", y = "Sales")
20
21 ggplot(DF,aes(year,sales)) + geom_line() + geom_
     point() + ylim(c(20,34)) +
     geom\_smooth(method = "lm", se = F) +
22
    labs(title = "Years V/S Sales Time Series and
23
       Linear Function Plot", x = "Years", y = "Sales")
```

#### R code Exa 18.4b Trend Projection Part2

```
1
                                     # Page no. : 809 -
                                        812
3 \# \text{Trend Projection Part} - 2
5 year \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 sales <- c
      (21.6,22.9,25.5,21.9,23.9,27.5,31.5,29.7,28.6,31.4)
7 forcast <- c
      (21.5,22.6,23.7,24.8,25.9,27.0,28.1,29.2,30.3,31.4)
9 DF <- data.frame(year, sales, forcast)
10
11 regressor <- lm(sales ~ year, data = DF)
12
13 cat ("Linear Trend Equation is T =", regressor$
      coefficients[1],"+",regressor$coefficients[2],"t"
      )
14
15 res <- anova (regressor)
16
17 cat("MSE is ",res$'Sum Sq'[2]/10)
18
19 cat("MSE is ",res$'Mean Sq'[2])
20
21 regressor
22 res
23
24 # Install Library if not installed
25
```

#### R code Exa 18.4c Nonlinear Trend Regression

```
1
                                       # Page no. : 814 -
                                           816
3 # Nonlinear Trend Regression
5 year \leftarrow c(1,2,3,4,5,6,7,8,9,10)
6 revenue <- c
      (23.1,21.3,27.4,34.6,33.8,43.2,59.5,64.4,74.2,99.3)
7 year_sq <- year**2
9 DF <- data.frame(year, revenue, year_sq)
10
11 # Install Library if not installed
12
13 # install.packages("gpplot2")
14
15 # Import Library
16
17 library(ggplot2)
18
```

```
19 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
     point() + ylim(c(0,120)) +
     labs(title = "Years V/S Revenue Time Series Plot",
20
        x = "Year", y = "Revenue")
21
22 regressor <- lm(revenue ~ year + year_sq, data = DF)
23 summary (regressor)
24 anova (regressor)
25
26 ggplot(DF,aes(year,revenue)) + geom_line() + geom_
     point() + ylim(c(0,120)) + geom_smooth(method =
27
                                                              lm
                                                              se
                                                              F
                                                              )
28
     labs(title = "Years V/S Revenue Time Series Plot",
        x = "Year", y = "Revenue")
```

#### R code Exa 18.5a Seasonality Without Trend

```
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
      "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
                    "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
6
                       "Y4 Q2", "Y4 Q3", "Y4 Q4", "Y5 Q1
                      ", "Y5 Q2",
                    "Y5 Q3", "Y5 Q4") # Years and
7
                       Quarters
  sales <- c(125, 153, 106, 88, 118, 161, 133, 102,
      138, 144, 113, 80, 109, 137, 125, 109, 130, 165,
9
               128, 96)
10
11 DF <- data.frame(year_quart, sales)</pre>
12
13 # Install Library if not installed
14
15 # install.packages("gpplot2")
16
17 # Import Library
18
19 library(ggplot2)
20
21 ggplot(DF,aes(year_quart,sales, group = 1)) + geom_
      line() + geom_point() + vlim(c(0,180)) +
     labs(title = "Years/quart V/S Sales Time Series
22
        Plot", x = "Year/Quarter", y = "Sales")
23
24
25 q1 \leftarrow c(1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0)
26 	 q2 \leftarrow c(0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0)
27 q3 \leftarrow c(0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0)
28
29 DF <- cbind(DF,q1,q2,q3)
30
31 regressor \leftarrow lm(sales ~ q1 + q2 + q3, data = DF)
32 summary (regressor)
33
34 b0 <- regressor$coefficients[1]
35 b1 <- regressor$coefficients[2]
```

#### R code Exa 18.5b Seasonality and Trend

```
1
                                       # Page no. : 823 -
                                           824
3 # Seasonality and Trend
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
     "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
                   "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
6
                      "Y4 Q2", "Y4 Q3", "Y4 Q4")
7 # Years and Quarters
8 sales \leftarrow c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
      6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
10 DF <- data.frame(year_quart, sales)</pre>
11
12 # Install Library if not installed
13
14 # install.packages("gpplot2")
15
16 # Import Library
17
18 library(ggplot2)
19
20 ggplot(DF,aes(year_quart,sales, group = 1)) + geom_
      line() + geom_point() + ylim(c(0.0,9.0)) +
21
     labs(title = "Years/quart V/S Sales Time Series
        Plot", x = "Year/Quarter", y = "Sales")
```

```
22
23 q1 \leftarrow c(1,0,0,0,1,0,0,0,1,0,0,0,1,0,0,0)
24 q2 \leftarrow c(0,1,0,0,0,1,0,0,0,1,0,0,0,1,0,0)
25 q3 \leftarrow c(0,0,1,0,0,0,1,0,0,0,1,0,0,0,1,0)
26 \text{ period} < - c(1:16)
27
28 DF <- cbind(DF,q1,q2,q3,period)
29
30 regressor <- lm(sales ~ q1 + q2 + q3 + period, data
      = DF)
31 summary (regressor)
32
33 b0 <- regressor$coefficients[1]
34 b1 <- regressor$coefficients[2]
35 b2 <- regressor$coefficients[3]
36 b3 <- regressor$coefficients[4]
37 b4 <- regressor$coefficients[5]
38
39 cat ("Equation is sales = ", b0,"+", b1," Qtr1 +", b2,"
      Qtr2 +",b3,"Qtr3 +",b4,"t")
```

#### R code Exa 18.6a Time Series Decomposition

```
# Page no.:
832 - 833

# Time Series Decomposition

year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
"Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",

"Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
"Y4 Q2", "Y4 Q3", "Y4 Q4")

# Page no.:
832 - 833

# Time Series Decomposition

4

5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
"Y2 Q1", "Y2 Q4", "Y3 Q1",
"Y4 Q2", "Y4 Q3", "Y4 Q4")

# Years and Quarters

8 sales <- c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4)
```

```
9 moving_avg <- c(NA
      ,5.350,5.600,5.875,6.075,6.300,6.350,6.450,6.625,6.725,6.800,6.87
10
                    7.15, NA, NA)
11 centered_avg <- c(NA,NA</pre>
      ,5.475,5.738,5.975,6.188,6.325,6.400,6.538,6.675,6.763,6.838,6.938
12
                      NA, NA)
13
14 DF <- data.frame(year_quart, sales,moving_avg,
      centered_avg)
15
16 # Install Library if not installed
17
18 # install.packages("gpplot2")
19
20 # Import Library
21
22 library(ggplot2)
23
24 ggplot(DF,aes(year_quart, group = 1)) + geom_line(
     aes(y = sales),color = "red") +
25
     geom_point(aes(y = sales)) + geom_line(aes(y =
        centered_avg),color = "blue") +
     geom_point(aes(y = centered_avg))+
26
27
     ylim(c(0.0,9.0)) +
     labs(title = "Years/quart V/S Sales Time Series
28
        Plot", x = "Year/Quarter", y = "Sales")
```

R code Exa 18.6b Deseasonalizing the Time Series

```
# Page no. : 835 -
836

2
3 # Deseasonalizing the Time Series
```

```
4
5 year_quart <- c("Y1 Q1", "Y1 Q2", "Y1 Q3", "Y1 Q4",
     "Y2 Q1", "Y2 Q2", "Y2 Q3", "Y2 Q4", "Y3 Q1",
                    "Y3 Q2", "Y3 Q3", "Y3 Q4", "Y4 Q1",
6
                       "Y4 Q2", "Y4 Q3", "Y4 Q4")
7 # Years and Quarters
8 \text{ period} < - c(1:16)
9 sales \leftarrow c(4.8, 4.1, 6.0, 6.5, 5.8, 5.2, 6.8, 7.4,
      6.0, 5.6, 7.5, 7.8, 6.3, 5.9, 8.0, 8.4
10 index <- c
      (0.93,0.84,1.09,1.14,0.93,0.84,1.09,1.14,0.93,0.84,1.09,1.14,0.93
11 deseasonalized_sales <- c
      (5.16,4.88,5.50,5.70,6.24,6.19,6.24,6.49,6.45,6.67,6.88,6.84,6.77
                              7.02, 7.34, 7.37)
12
13
14 DF <- data.frame(year_quart, period, sales, index,
      deseasonalized_sales)
15
16 # Install Library if not installed
17
18 # install.packages("gpplot2")
19
20 # Import Library
21
22 library(ggplot2)
23
24 ggplot(DF,aes(year_quart,deseasonalized_sales, group
       = 1)) + geom_line() + geom_point() +
     ylim(c(0.0,9.0)) +
25
     labs(title = "Years/quart V/S Deseasonalized Sales
26
         Time Series Plot", x = "Year/Quarter",
          y = "Deseasonalized Sales")
27
28
29 regressor <- lm(deseasonalized_sales ~ period, data
      = DF)
30 summary (regressor)
```

## Chapter 19

### Non Parametric Tests

#### R code Exa 19.1a Rank Correlation

```
# Page no. : 887
1
                                               - 889
3 # Rank Correlation
5 sales_person <- c('A', 'B', 'C', 'D', 'E', 'F', 'G', 'H', 'I
      ', 'J')
6 \times < -c(2,4,7,1,6,3,10,9,8,5) \# Ranking of
      Potential
7 y \leftarrow c (400,360,300,295,280,350,200,260,220,385)
     Two Years Sales
8 z \leftarrow c(1,3,5,6,7,4,10,8,9,2) # Ranking According
      to y
10 DF <- data.frame(sales_person,x,y,z)</pre>
11
12 d <- DF$x - DF$z
13 d_sq < d**2
14
15 DF <- cbind(DF,d,d_sq)
16
```

```
17 total_d_sq <- sum(DF$d_sq)
18
19 n <- nrow(DF)
20
21 \text{ r_s} \leftarrow 1 - ((6 * \text{total_d_sq})/(n * (n**2 + 1)))
      Spearman Rank-Correlation Coefficient
22
23 mean_rs <- 0
24
25 sigma_rs <- sqrt(1 / (n - 1))
26
27 z_val <- (r_s - mean_rs) / sigma_rs
28
29 alpha <- 0.05
30
31 # Two Tail Test
32
33 # P-value Approach
34
35 \text{ pval} \leftarrow 2 * \text{pnorm}(z_val, lower.tail} = F)
36
37 \text{ if (pval >= alpha)}
38 {
     cat ("Since pval", pval, "is greater than or equal to
39
          0.05 therefore we cannot reject the Null
         Hypothesis")
40 } else{
     cat ("Since pval", pval, "is less than 0.05 therefore
          we can reject the Null Hypothesis")
42 }
```

 ${f R}$  code  ${f Exa}$  19.2a Sign Test

```
# Page no. : 858
- 861
```

```
3 # Sign Test
5 store \leftarrow c(56, 19, 36, 128, 12, 63, 39, 84, 102, 44)
6 sales \leftarrow c(485, 562, 415, 860, 426, 474, 662, 380,
      515, 721)
7
8 DF <- data.frame(store, sales)
10 \text{ median} < -450
11 sign <- c()
12
13 for (i in 1:nrow(DF)) {
     if(DF$sales[i] >= median)
14
15
        sign[i] = "+"
16
     }else
17
18
       sign[i] <- "-"
19
20
     }
21 }
22
23 DF <- cbind(DF, sign)
24 View(DF)
25
26 positive <- table(DF$sign)[[2]]
27 \text{ n} \leftarrow \text{nrow}(DF)
28
29 test <- binom.test(positive, n)
30 test
31
32 if (test$p.value >= 0.05)
33 {
     cat ("We cannot reject null hypothesis")
34
35 } else
36 {
    cat("We can reject null hypothesis")
38 }
```

```
39
40
41 N <- 60
               # "+ sign
42 n1 <- 22
              # "- sign
43 n2 <- 38
44 \text{ med} < -236000
45
46 \text{ mean} < -0.50 * N
47 \text{ sd} \leftarrow \text{sqrt}(0.25 * N)
48
49 CF <- 22.5
                   # Correction Factor
50
51 p <- pnorm(CF, mean = mean, sd = sd)
52
53 \text{ if (p >= 0.05)}
54 {
     cat ("We cannot reject null hypothesis")
55
56 } else
57 {
     cat ("We can reject null hypothesis")
58
59 }
```

#### R code Exa 19.3a Wilcoxon Signed Rank Test

```
9 DF <- data.frame(worker, A, B)
10
11 \text{ options}(\text{warn} = -1)
12
13 test <- wilcox.test(DF$A, DF$B, paired = T)
14 test
15
16 \text{ if}(\text{test\$p.value} >= 0.05)
17 {
     cat ("We cannot reject null hypothesis")
18
19 } else
20 {
21
     cat ("We can reject null hypothesis")
22 }
```

#### R code Exa 19.4a Mann Whitney Wilcoxon Test

```
# Page no. : 873 -
875

2
3 # Mann - Whitney - Wilcoxon - Test
4
5 college <- c(1:4)
6 m1 <- c(15,3,23,8)
7
8 high <- c(1:5)
9 m2 <- c(18,20,32,9,25)
10
11 test <- wilcox.test(m1, m2, correct = F)
12 test
13
14 if(test$p.value >= 0.05)
15 {
16 cat("We cannot reject null hypothesis")
17 } else
```

```
18 {
19    cat("We can reject null hypothesis")
20 }
```

#### R code Exa 19.4b Mann Whitney Wilcoxon Test Eg2

```
1
                                                # Page no. :
                                                     876 - 878
3 # Mann - Whitney - Wilcoxon - Test Eg - 2
5 \ \text{account1} < - \ c(1:12)
6 account2 <- c(1:10)
8 balance1 <- c(1095, 955, 1200, 1195, 925, 950, 805,
      945, 875, 1055, 1025, 975)
9 balance2 <- c(885, 850, 915, 950, 800, 750, 865,
      1000, 1050, 935)
10
11 test <- wilcox.test(balance1, balance2, correct = F)</pre>
12 test
13
14 \text{ if}(\text{test}p.\text{value} >= 0.05)
15 {
     cat ("We cannot reject null hypothesis")
16
17 } else
18 {
     cat("We can reject null hypothesis")
19
20 }
```

R code Exa 19.5a Kruskal Wallis Test

```
1
                                            # Page no. : 883 -
                                                 884
3 # Kruskal – Wallis Test
5 A \leftarrow c(25, 70, 60, 85, 95, 90, 80)
6 B \leftarrow c(60, 20, 30, 15, 40, 35)
7 \text{ C} \leftarrow c(50, 70, 60, 80, 90, 70, 75)
9 x <- list(A,B,C)
10
11 test <- kruskal.test(x)</pre>
12 test
13
14 \text{ if}(\text{test\$p.value} >= 0.05)
     cat("We cannot reject null hypothesis")
16
17 } else
18 {
     cat("We can reject null hypothesis")
19
20 }
```

### Chapter 20

### Statistical Process Control

R code Exa 20.1a Sample Mean Chart Process Mean and SD Unknown

```
1
                                       # Page no. : 913 -
                                            919
3 # Sample Mean Chart: Process Mean and SD Unknown
5 \text{ ol} \leftarrow c(3.5056, 3.4882, 3.4897, 3.5153, 3.5059,
      3.4977, 3.4910, 3.4991, 3.5099, 3.4880, 3.4881,
           3.5043, 3.5043, 3.5004, 3.4846, 3.5145,
6
              3.5004, 3.4959, 3.4878, 3.4969)
  o2 \leftarrow c(3.5086, 3.5085, 3.4898, 3.5120, 3.5113,
      3.4961, 3.4913, 3.4853, 3.5162, 3.5015, 3.4887,
           3.4867, 3.4769, 3.5030, 3.4938, 3.4832,
              3.5042, 3.4823, 3.4864, 3.5144)
  o3 \leftarrow c(3.5144, 3.4884, 3.4995, 3.4989, 3.5011,
      3.5050, 3.4976, 3.4830, 3.5228, 3.5094, 3.5141,
           3.4946, 3.4944, 3.5082, 3.5065, 3.5188,
10
              3.4954, 3.4964, 3.4960, 3.5053)
  04 \leftarrow c(3.5009, 3.5250, 3.5130, 3.4900, 3.4773,
      3.5014, 3.4831, 3.5083, 3.4958, 3.5102, 3.5175,
           3.5018, 3.5014, 3.5045, 3.5089, 3.4935,
12
              3.5020, 3.5082, 3.5070, 3.4985)
```

```
13 \text{ o5} \leftarrow c(3.5030, 3.5031, 3.4969, 3.4837, 3.4801,
      3.5060, 3.5044, 3.5094, 3.5004, 3.5146, 3.4863,
           3.4784, 3.4904, 3.5234, 3.5011, 3.4989,
14
              3.4889, 3.4871, 3.4984, 3.4885)
15
16 DF <- data.frame(o1, o2, o3, o4, o5)
17
18 sample_mean <- rowMeans(DF)</pre>
19 sample_range <- c(0.0135, 0.0368, 0.0233, 0.0316,
      0.0340, 0.0099, 0.0213, 0.0264, 0.0270, 0.0266,
                      0.0312, 0.0259, 0.0274, 0.0230,
20
                         0.0243, 0.0356, 0.0153, 0.0259,
                          0.0206, 0.0259)
21
22 DF <- cbind(DF, sample_mean, sample_range)</pre>
23 View(DF)
24
25 AR <- mean(DF$sample_range) # Average Range
26 OM <- mean(DF$sample_mean) # Overall Mean
27 n <- 5 # Sample Observations
28 d2 <- 2.362
29 A2 < -3 / (d2 * sqrt(n))
30
31 UCL <- OM + (A2 * AR) # Upper Control Limit
                           # Lower Control Limit
32 LCL <- OM - (A2 * AR)
33
34 cat("UCL is ", UCL)
35 cat("LCL is", LCL)
36
37 library (qicharts2)
38
39 qic(DF\sample_mean, xlab = "Sample Number", ylab = "
      Sample Mean", title = "Sample Mean Chart")
40
41 d3 <- 0.864
42
43 D1 \leftarrow 1 + (3 * (d3 / d2))
44 D2 \leftarrow 1 - (3 * (d3 / d2))
```

```
45
46 UCL2 <- AR * D1
47 LCL2 <- AR * D2
48
49 cat("UCL is ", UCL2)
50 cat("LCL is", LCL2)
                         # Book answer is different
51
52 qic(DF\sample_range, xlab = "Sample Number", ylab =
      "Sample Range", title = "R Chart")
53
54 p <- 0.03
55 n <- 200
56
57 sigma <- sqrt((p * (1 - p)) / n)
58
59 UCL3 <- p + 3 * sigma
60 LCL3 <- p - 3 * sigma
61
62 cat("UCL is ", UCL3)
63 cat("LCL is", LCL3)
64
65 # Data for P chart is not available in Book
66
67 UCL4 \leftarrow n * p + 3 * sqrt(n * p * (1 - p))
68 LCL4 \leftarrow n * p - 3 * sqrt(n * p * (1 - p))
69
70 cat("UCL is ", UCL4)
71 cat("LCL is", LCL4)
```

## Chapter 21

## **Decision Analysis**

#### R code Exa 21.1a Problem Formulation

```
1
                                         # Page no. :
                                            940 - 941
3 # Problem Formulation
5 decision <- factor(c("Small Complex, d1", "Medium
     Complex, d2", "Large Complex, d3"))
6 demand1 <- c(8, 14, 20)
7 demand2 <-c(7, 5, -9)
9 DF <- data.frame(decision, demand1, demand2)
10
11 # Install Library if not install
12
13 install.packages("rpart")
14 install.packages("rpart.plot")
15
16 # Import Library
17
18 library(rpart)
19 library(rpart.plot)
```