R Textbook Companion for Business Statistics For Contemporary Decision Making by Ken $Black^1$

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Book Description

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R numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means an R code whose theory is explained in Section 2.3 of the book.

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Chapter 2

Charts and Graphs

R code Exa 2.1.a Class Midpoints

```
1 # Class midpoints.
3 Interest_rate <- c</pre>
      (7.29, 7.23, 7.11, 6.78, 7.47, 6.69, 6.77, 6.57, 6.80, 6.88, 6.98, 7.16,
                        7.30,7.24,7.16,7.03,6.90,7.16,7.40,7.05,7.28,7.31
4
5
                        7.03,7.17,6.78,7.08,7.12,7.31,7.40,6.35,6.96,7.29
6
                        6.96,7.02,7.13,6.84)
8 summary(Interest_rate)
10 low_val<- 6.30
11 high_val <-7.70
12 step_val <- 0.20
13 x_breaks <- seq(low_val,high_val,step_val)</pre>
14 \text{ x\_breaks}
15 x_mid <- seq(low_val+step_val/2, high_val-step_val/2,
      step_val)
16 \text{ x\_mid}
```

```
17  x <-cut(Interest_rate, breaks = x_breaks, right=FALSE)
18  x
19  y <-table(x)
20  y
21
22  df <- data.frame(y)
23  df
24
25  # Class Mid point :
26  df$midpoint <- x_mid
27  View(df)</pre>
```

R code Exa 2.1.b Relative Frequency

```
1 # Relative Frequency.
3 Interest_rate <- c</pre>
      (7.29, 7.23, 7.11, 6.78, 7.47, 6.69, 6.77, 6.57, 6.80, 6.88, 6.98, 7.16,
                        7.30,7.24,7.16,7.03,6.90,7.16,7.40,7.05,7.28,7.31
4
5
                        7.03,7.17,6.78,7.08,7.12,7.31,7.40,6.35,6.96,7.29
6
                        6.96,7.02,7.13,6.84)
7
8 summary(Interest_rate)
10 low_val<- 6.30
11 high_val <-7.70
12 step_val <- 0.20
13 x_breaks <- seq(low_val, high_val, step_val)
14 x_breaks
15 x_mid <- seq(low_val+step_val/2, high_val-step_val/2,
      step_val)
16 \text{ x_mid}
```

```
17 x <-cut (Interest_rate, breaks = x_breaks, right=FALSE)
18 x
19 y \leftarrow table(x)
20 y
21
22 df <- data.frame(y)
23 df
24
25 # Class Mid point :
26 	ext{ df} 	ext{midpoint } 	ext{<-} 	ext{x_mid}
27 df
28
29 # Relative Frequency:
30 rf <- df$Freq/sum(df$Freq)
31 rf
32 df$relative_frequency <- rf
33 View(df)
```

R code Exa 2.1.c Cumulative Frequency

```
12 step_val <- 0.20
13 x_breaks <- seq(low_val,high_val,step_val)</pre>
14 x_breaks
15 x_mid <- seq(low_val+step_val/2, high_val-step_val/2,
      step_val)
16 \text{ x_mid}
17 x <-cut (Interest_rate, breaks = x_breaks, right=FALSE)
18 x
19 y \leftarrow table(x)
20 y
21
22 df <- data.frame(y)
23 df
24
25 # Class Mid point :
26 df$midpoint <- x_mid
27 df
28
29 # Relative Frequency:
30 rf <- df$Freq/sum(df$Freq)
31 rf
32 df$relative_frequency <- rf
33 View(df)
34
35 # Cumulative Frequency:
36 c < - cumsum (df $Freq)
37 df$cumulative_frequency <- c
38 n <- sum(df$Freq)
39 crf <- c/n
40 df$cumul <- crf
41 df$pie <- round(360*rf,1)
42 \text{ View}(df)
```

R code Exa 2.2 Steam and leaf plot

R code Exa 2.3.a Bar Graph

R code Exa 2.3.b Bar Graph

```
1 # Pie Chart:
3 Inventary_shrinkage <- c("Employee theft","
      Shoplifting", "Administrative error", "Vendor fraud
      ")
5 Annual_amount <- c(17918.6, 15191.9,7617.6,2553.6)
7 data <- data.frame(Inventary_shrinkage, Annual_amount
9 Proportion <- data$Annual_amount/sum(data$Annual_
      amount)
10
11 Percent <- Proportion*100</pre>
12
13 data <- cbind(data, Proportion, Percent)</pre>
14
15 Degree <- data$Proportion*360
16
17 data <-cbind (data, Degree)
18
19 labls <- paste(data$Inventary_shrinkage,data$Percent
      ,sep = "
20
21 labls <- paste(labls, "%", sep="")
```

```
22
23 pie(data$Percent, labels = labls)
```

R code Exa 2.4 Scatter Plot

```
1 # Scatter Plot :
2 Residential <- c
      (169635, 155113, 149410, 175822, 162706, 134605, 195028, 231396, 234955,
3
                      266481, 267063, 263385, 252745, 228943, 197526, 232134, 24
4
                      251937, 281229, 280748, 297886, 315757)
6 Non_residential <- c
      (96497, 115372, 96407, 129275, 140569, 145054, 131289, 155261, 178925,
7
                          163740, 160363, 164191, 169173, 167896, 135389, 12092
                          139711, 153866, 166754, 177639, 175048)
8
10 home <- cbind(Residential, Non_residential)</pre>
11 View(home)
12
13 # Scatter plot :
14 plot(Residential, Non_residential, xlab="Residential"
      ,ylab="Non-Residential")
```

Chapter 3

Descriptive Statistics

R code Exa 3.1.a Mode

```
1 # Mode Example :
3 getmode <- function(v) {</pre>
     uniqv <- unique(v)</pre>
     uniqv[which.max(tabulate(match(v, uniqv)))]
6 }
8 Company <- c("Enterprise", "Hertz", "Natioanl/Alamo","
      Avis", "Dollar", "Budget", "Advantage",
                 "U-save", "Payless", "ACE", "Fox", "Rent-A-
9
                    Wreck", "Traingle")
10
11 Number_of_Cars_in_Service <- c
      (643000, 327000, 233000, 204000, 167000, 144000, 20000, 12000, 10000,
                                     9000,9000,7000,6000)
12
13
14 data1 <- data.frame(Company, Number_of_Cars_in_
      Service)
15
16 sort_data <- data1[order(-Number_of_Cars_in_Service
```

```
),]
17
18 result <- getmode(sort_data$Number_of_Cars_in_
      Service)
19 print(result)
   R code Exa 3.1.b Median
1 \# Median :
3 Company <- c("Enterprise", "Hertz", "Natioanl/Alamo","
      Avis", "Dollar", "Budget", "Advantage",
                 "U-save", "Payless", "ACE", "Fox", "Rent-A-
                    Wreck", "Traingle")
6 Number_of_Cars_in_Service <- c
      (643000, 327000, 233000, 204000, 167000, 144000, 20000, 12000, 10000,
7
                                 9000,9000,7000,6000)
  data1 <- data.frame(Company, Number_of_Cars_in_</pre>
      Service)
10
11 sort_data <- data1[order(-Number_of_Cars_in_Service</pre>
      ),]
12
13 median(sort_data$Number_of_Cars_in_Service)
   R code Exa 3.1.c Mean
1 # Mean Example :
```

```
3 Company <- c("Enterprise", "Hertz", "Natioanl/Alamo","
      Avis", "Dollar", "Budget", "Advantage",
                 "U-save", "Payless", "ACE", "Fox", "Rent-A-
4
                    Wreck", "Traingle")
6 Number_of_Cars_in_Service <- c
      (643000, 327000, 233000, 204000, 167000, 144000, 20000, 12000, 10000,
7
                                    9000,9000,7000,6000)
8
  data1 <- data.frame(Company, Number_of_Cars_in_</pre>
      Service)
10
11 sort_data <- data1[order(-Number_of_Cars_in_Service
      ),]
12
13 mean(sort_data$Number_of_Cars_in_Service)
```

R code Exa 3.2 Determine the 30th percentile of the following eight numbers

```
1 # Determine the 30th percentile of the following
    eight numbers :
2 data3 <- c(5,12,13,14,17,19,23,28)
3 N = 8
4 P = 30
5
6 # 30th percentile value is :
7 a <- quantile(data3,c(.30))
8 cat("30th percentile value is : ",a)</pre>
```

R code Exa 3.3 Quartiles

```
1 # Quartiles :
2
3 Category <- c("Automotive", "Personal Care", "
      Entertainment & Media",
                  "Food", "Drugs", "Electronics", "Soft
4
                     Drinks", "Retail", "Cleaners",
                  "Restaurants", "Computers", "Telephone",
5
                     "Financial",
                  "Beer Wine & Liquor", "Candy", "Toys")
6
7
8 Ad_spending <- c
      (22195, 19526, 9538, 7793, 7707, 4023, 3916, 3576, 3571, 3553, 3247, 2488,
9
                      2433,2050,1137,699)
10
11 advertise_age <- cbind(Category,Ad_spending)</pre>
12 View(advertise_age)
13
14 N = 16
15
16 \# Q1 = P25 is found by :
17 i = 25/100*N
18 i
19
20 \#Q3 = P75 is solved by :
21 i1 = 75/100*(N)
22 i1
23
24 \# Quantile:
25 quantile(Ad_spending)
```

R code Exa 3.5 Chebyshevs Theorem

```
1 # Chebyshev's Theorem : 2
```

```
3 \text{ avg\_age} = 28
4 \text{ sd} = 6
6 # Chebyshev's theorem states that at least (1-1)/k
       ^2 proportion of the values are within
7 \#(\text{mean}+k*sd). Because 80% of the values are within
       this range, let
8
9 \#1 - (1/k^2) = .80
10
11 k = sqrt(1/(1-0.80))
12 k
13
14 # now for :
15 \text{ mean} = 28
16 \text{ sd} = 6
17
18 # values are within
19 \text{ r1} = \text{mean} + \text{k} * \text{sd}
20 r1 #41.41
21 \text{ r2} = \text{mean} - \text{k} * \text{sd}
22 \text{ r2} \# 14.58
23
24 # Years of age or between 14.6 and 41.4 years old.
```

R code Exa 3.6.a Mean Absolute Deviation

```
1 # Mean absolute deviation :
2
3 x <- c(55,100,125,140,60)
4 n = 5
5
6 # a = abs(x - x_bar), where x_bar = sum(x)/n
7 a <- c(41,4,29,44,36)</pre>
```

```
9 x <- cbind(x,a)
10 View(x)
11
12 # MAD :
13 mean_dev <- sum(a)/n
14 mean_dev</pre>
```

R code Exa 3.6.b Variance and Standard deviation

```
1 # Variance and stanadard deviation :
3 \text{ x} < -c (55, 100, 125, 140, 60)
4 n = 5
6 \# a = abs(x - x_bar), where x_bar = sum(x)/n
7 a \leftarrow c(41,4,29,44,36)
9 \# b = (x - x_bar)^2
10 b <- c(1681,16,841,1936,1296)
11
12 y \leftarrow cbind(x,a,b)
13 View(y)
14
15 \# Variance :
16 var(x)
17
18 # standard deviation :
19 \text{ sd}(x)
```

R code Exa 3.7 Mean Median Mode Variance and Standard deviation

```
1 \# Mean, Median, Mode, Variance, and Standard deviation :
```

```
3 \text{ class} \leftarrow c("10-under-15","15-under-20","20-under-25")
       30 - under - 30, "30 - under - 35, ,
                 "35-under-40", "40-under-45", "45-under-50"
                     )
5 \text{ freq } \leftarrow c(6,22,35,29,16,8,4,2)
 6 class <-data.frame(class,freq)</pre>
 7 class
9 # Mean of each intervals :
10 \ a < - mean(10:15)
11 b <-mean (15:20)
12 c < -mean(20:25)
13 d \leftarrow mean (25:30)
14 e < -mean (30:35)
15 f \leftarrow mean(35:40)
16 \text{ g} < -\text{mean} (40:45)
17 h \leftarrow mean (45:50)
18 Mean \leftarrow rbind(a,b,c,d,e,f,g,h)
19 Mean
20
21 # fM :
22 for(i in 1:8)
23 {
24
      fM <- freq * Mean
25 }
26 fM
27
28 \# \text{group mean}:
29 Group_mean <- sum(fM)/sum(freq)
30 Group_mean
31
32 \# \text{Mean} - \text{group mean}:
33 for(i in 1:8)
34 {
      Mean_grpmean <- Mean - Group_mean</pre>
35
36 }
37 Mean_grpmean
```

```
38
39 # Square of Mean_grpmean :
40 Mean_grpmean_sq <- Mean_grpmean^2
41 Mean_grpmean_sq
42
43 # freq * Mean_grpmean_sq :
44 freq_Mean_grpmean_sq <- freq * Mean_grpmean_sq
45 freq_Mean_grpmean_sq
46
47
48 var <- sum(freq_Mean_grpmean_sq)/(sum(freq)-1)
49 var
50 sd <- sqrt(var)
51 sd</pre>
```

Chapter 4

Probability

R code Exa 4.1 Addition Law

```
1 # Addition Law: P(F \text{ and } P) = P(F) + P(P) - P(F \text{ or } P)
3 Type_of_position <- c("Managerial", "Professional","
      Technical", "Clerical")
4 Sex_male \leftarrow c(8,31,52,9)
5 Sex_female \leftarrow c(3,13,17,22)
6 total_r \leftarrow c(11,44,69,31)
7 total_c <- c(" ",100,55,55)
8 Compny_HR_data <- cbind(Type_of_position, Sex_male,
      Sex_female,total_r)
9 Compny_HR_data <- rbind(Compny_HR_data, total_c)
10 View (Compny_HR_data)
12 # F denote the event of female and P denote the
      event of professional worker
13
14 # Probability of event of female :
15 Pb_F = sum(Sex_female)/sum(sum(Sex_female),sum(Sex_
      male))
16 \text{ Pb}_{\text{F}}
```

```
17
18 # Probability of event of professional worker :
19 Pb_P = sum(Sex_male[2],Sex_female[2])/sum(sum(Sex_female),sum(Sex_male))
20 Pb_P
21
22 # Probability of female or Professional worker :
23 Pb_F_P = Sex_female[2]/sum(sum(Sex_female),sum(Sex_male))
24 Pb_F_P
25
26 # probability that the employee is female or a professional worker :
27 Pb_F_a_P <- Pb_F + Pb_P - Pb_F_P
28 Pb_F_a_P</pre>
```

R code Exa 4.3 Special Law of Addition

```
1 # Special Law of Addition : P(T \text{ and } C) = P(T) + P
      (\mathbf{C})
3 Type_of_position <- c("Managerial", "Professional","
      Technical", "Clerical")
4 Sex_male \leftarrow c(8,31,52,9)
5 \text{ Sex\_female} \leftarrow c(3,13,17,22)
6 total_r \leftarrow c(11,44,69,31)
7 total_c <- c(" ",100,55,55)
8 Compny_HR_data <- cbind(Type_of_position, Sex_male,
      Sex_female,total_r)
9 Compny_HR_data <- rbind(Compny_HR_data, total_c)
10 View (Compny_HR_data)
11
12 # T denote technical, C denote clerical, and P
      denote professional.
13
```

```
14 # Probability of Technical position :
15 Pb_T = sum(Sex_male[3],Sex_female[3])/sum(sum(Sex_
      female),sum(Sex_male))
16 \text{ Pb}_{\mathtt{T}}
17
18 # Probability of Clerical position
19 Pb_C = sum(Sex_male[4],Sex_female[4])/sum(sum(Sex_
      female),sum(Sex_male))
20 Pb_C
21
22 # Probability of professional position :
23 Pb_P = sum(Sex_male[2],Sex_female[2])/sum(sum(Sex_
      female), sum (Sex_male))
24 Pb_P
25
26 # probability that a worker is either technical or
      clerical is :
27 \text{ Pb\_T\_C} = \text{Pb\_T} + \text{Pb\_C}
28 Pb_T_C
29
30 #
       probability that a worker is either professional
       or clerical is:
31 \text{ Pb_P_C} = \text{Pb_P} + \text{Pb_C}
32 Pb_P_C
```

R code Exa 4.5 Multiplication Law

```
1 # General Law of Multiplication : P (X or Y) = P(X)*
        P(Y|X) = P(Y)*P(X|Y)
2
3 Total_emp = 140
4 supervisor = 30
5 Married_emp = 80
6 Pb_S_M = .20 # P(S|M) i.e. married employees are supervisors
```

```
7
8 # probability that the employee is married:
9 Pb_M = Married_emp/Total_emp
10 Pb_M
11
12 # probability that the employee is married and is a supervisor:
13 Pb_M_s <- Pb_M * Pb_S_M
14 Pb_M_s
15
16 # 11.43% of the 140 employees are married and are supervisors</pre>
```

R code Exa 4.6 General Law of Multiplication

```
1 # General Law of Multiplication :
2
3 Industry_type <- c("Finance_A", "Manufacturing_B","
     Communication_C")
4 Northeast_D <- c(.12,.15,.14)
5 Southeast_E <- c(.05,.03,.09)
6 Midwest_F <-c(.04,.11,.06)
7 West_G <-c(.07,.06,.08)
8 total_r <- c(.28,.35,.37)</pre>
9 total_c <- c(" ",.41,.17,.21,.21,1.00)
10 Industry_type <- cbind(Industry_type, Northeast_D,
      Southeast_E, Midwest_F, West_G, total_r)
11 Industry_type <- rbind(Industry_type,total_c)</pre>
12 View(Industry_type)
13
14 # a.) P(Manufacturing_B and Southeast_E):
15 P_B_E \leftarrow total_r[2]*(Southeast_E[2]/total_r[2])
16 P_B_E
17
18 # b.) P(West_G and Finance_A) :
```

R code Exa 4.8 Special Law of Multiplication

```
1 # Special law of Mulyiplication : If X, Y are
      independent, P(X \text{ or } Y) = P(X) * P(Y)
2
4 T1 <- c("A", "B", "C")
5 D \leftarrow c(8,20,6)
6 E \leftarrow c(12,30,9)
7 total_r <- c(20,50,15)
8 total_c <- c(" ",34,51,85)
9 T1 <- cbind(T1,D,E,total_r)
10 T1 <- rbind(T1,total_c)</pre>
11 View(T1)
12
13 # Probability of B:
14 Pb_B = sum(D[2], E[2])/sum(total_r)
15 Pb_B
16
17 # Probability of D:
18 Pb_D = sum(D)/sum(total_r)
19 Pb_D
20
21 # Probability of B and D is:
22 \text{ Pb\_B\_D} = \text{Pb\_B} * \text{Pb\_D}
23 Pb_B_D
```

R code Exa 4.9 Conditional Probability

```
1 # Conditinal Probability : P(X|Y) = P(X \text{ or } Y)/P(Y)
       = (P(X) *P(Y|X))/P(Y)
  Industry_type <- c("Finance_A", "Manufacturing_B","</pre>
      Communication_C")
4 Northeast_D <- c(.12,.15,.14)
5 \text{ Southeast\_E} \leftarrow c(.05,.03,.09)
6 Midwest_F <-c(.04,.11,.06)
7 \text{ West\_G} \leftarrow c(.07,.06,.08)
8 total_r \leftarrow c(.28,.35,.37)
9 total_c <- c(" ",.41,.17,.21,.21,1.00)
10 Industry_type <- cbind(Industry_type, Northeast_D,</pre>
      Southeast_E, Midwest_F, West_G, total_r)
11 Industry_type <- rbind(Industry_type,total_c)</pre>
12 View(Industry_type)
13
14 #a.) P(Manufacturing_B | Midwest_F) = P(
      Manufacturing_B and Midwest_F)/P(Midwest_F)
15 Pb_B_F = Midwest_F[2]/sum(Midwest_F)
16 Pb_B_F
17
18 #b.) P(West_G | Communication_C) = P(West_G and
      Communication_C) /P(Communication_C)
  Pb_G_C = West_G[3] / sum(Northeast_D[3], Southeast_E
      [3], Midwest_F[3], West_G[3])
  Pb_G_C
20
21
22 #c.) P(Northeast_D | Midwest_F) = P(Northeast_D and
      Midwest_F)/P(Midwest_F)
23 \text{ Pb\_D\_F} = .00/\text{sum}(\text{Midwest\_F})
24 Pb_D_F
```

R code Exa 4.11 Independent Event

```
1 # Independent Event : P(X|Y) = P(X) and P(Y|X) = P(Y|X)
2
3 T1 <- c("A", "B", "C")
4 D < -c(8,20,6)
5 E \leftarrow c(12,30,9)
6 \text{ total\_r} \leftarrow c(20,50,15)
7 total_c <- c(" ",34,51,85)
8 T1 <- cbind(T1,D,E,total_r)</pre>
9 T1 <- rbind(T1, total_c)
10 View(T1)
11
12 # Check the ???rst cell in the matrix to ???nd
      whether P(A|D) = P(A)
13 Pb_A_D \leftarrow D[1]/sum(D) \# P(A|D)
14 \text{ Pb\_A\_D}
15
16 P_A <- sum(D[1],E[1])/sum(total_r)
17 P_A \# P(A)
```

R code Exa 4.12 Bayes Rule

```
1 # Bayes's Rule : P(Xi|Y) = P(Xi)*P(Y|Xi) / P(X1)*P(Y|X1)+P(X2)*P(Y|X2)+...+P(Xn)*P(Y|Xn)

2 
3 Event <- c("A","B","C")
4 Prior <- c(.60,.30,.10) # P(Ei)
5 Conditional <- c(.40,.50,.70) # P(x|Ei)
6 Joint <- c(.24,.15,.07) # P(X|Ei)
Ei)
```

```
7 Posterior <- c(.52,.33,.15) # P(X and Ei)/sum(P(X and Ei))
8
9 machine <- cbind(Event, Prior, Conditional, Joint, Posterior)
10 machine
11
12 # Revised Probabilities :
13 machine_A <- Prior[1]* Conditional[1]/sum(Joint)
14 machine_A
15
16 machine_B <- Prior[2]* Conditional[2]/sum(Joint)
17 machine_B
18
19 machine_C <- Prior[3]* Conditional[3]/sum(Joint)
20 machine_C</pre>
```

Chapter 5

Discrete Distributions

R code Exa 5.1 Variance and standard deviation of a Discrete Distribution

```
1 # Variance and standard deviation of a Discrete
      Distribution:
3 Prize \leftarrow c(1000,100,20,10,4,2,1,0) # x
4 Probability <- c
      (.00002,.00063,.00400,.00601,.02403,.08877,.10479,.77175)
       \# P(x)
5
6 \# x * P(x) :
7 for(i in 1:8){
     x_Pb \leftarrow Prize*Probability # x * P(x)
9 }
10 print(x_Pb)
11
12 \# \text{sum Of } x * P(x) :
13 x_Pb_s \leftarrow sum(x_Pb)
14 x_Pb_s
15
16
17 \# (x - x_Pb_s)^2
18 for(j in 1:8){
```

```
19
     x_{mean} sq <- (Prize - x_{pb})^2
20 }
21 print(x_mean_sq)
22
23
24 \# (x - x_Pb_s)^2 * P(x) :
25 for(j in 1:8){
     x_mean_sq_Pb <- (Prize - x_Pb_s)^2 * Probability</pre>
26
27 }
28 print(x_mean_sq_Pb)
29
30 \# sum of (x - x_Pb_s)^2 * P(x) :
31 x_mean_sq_Pb_s <- sum(x_mean_sq_Pb)
32 \text{ x}_{mean}_{sq}Pb_{s}
33
34 Prize <- cbind(Prize, Probability, x_mean_sq, x_mean_sq
      _Pb)
35 View(Prize)
36
37 # Variance and Standard deviation :
38 var <- x_mean_sq_Pb_s</pre>
39 var
40 sd <- sqrt(var)
41 sd
```

R code Exa 5.2 Binomial Distribution

```
1 # Binomial Distribution : P(x) = nCx*p^x*q^n-x = n!/
    x!(n - x)! *p^x*q^n-x
2
3 p = .65
4 q = 1-p
5 n = 25
6 x = 19
7 x1 = 0:19
```

R code Exa 5.3 Binomial Distribution ex 2

```
1 # Binomial Disribution ex 2 :
2
3 p = .06
4 q = .94
5 n = 20
6
7 x <- c(0,1,2)
8 c<-choose(n,x)*(p^x) * (q^(n-x))
9 c
10 sum(c)</pre>
```

R code Exa 5.5 Using Binomial Table

```
1 # using Binomial Table :
2
3 n = 20
4 p = .10
5 q = 1-p
6
7 x <- c(0,1,2,3)</pre>
```

```
8 c<-choose(n,x)*(p^x) * (q^(n-x))
9 c
10
11 # Probability that fewer than four purchasers
        choose Oreos i.e. x<4 :
12 sum(c) # about 86.7% of the time fewer than four of
        the 20 will select Oreos</pre>
```

R code Exa 5.6 Mean and standard deviation in Binomial distribution

```
1 # Mean and standard deviation in Binomial
       distribution:
2 \# \text{mean} = n * p \text{ and } \text{sd} = \text{sqrt}(n*p*q)
3
4 n = 10
5 p < -c (.10, .20, .30, .40)
6 \, q = 1 - p
8 # mean <- n*p
9 for(p1 in 1:4){
     mean = n*p
10
11 }
12 print(mean)
13
14 pd <-pbinom (2, n, p)
15
16
17 p <-cbind (p, mean, pd)
18 p
```

R code Exa 5.7 Poissions formula

```
1 # Poission formula : P(x) = lamda^x *e^-lamda/x!
```

```
3 1 <- 3.2 # lamda
4 # x>7 customers/4 minutes
6 # through in build function of poission in r:
7 dpois(8, lambda = 3.2) \# x=8
9 \# x = 8 \text{ through formula}:
10 x = 8
11 pd_8 \leftarrow (1^x*exp(-1))/factorial(x)
12 pd_8
13
14 \# x = 9 \text{ through formula}:
15 x = 9
16 pd_9 \leftarrow (1^x*exp(-1))/factorial(x)
17 pd_9
18
19 \# x = 10 \text{ through formula}:
20 x = 10
21 pd_10 \leftarrow (1^x*exp(-1))/factorial(x)
22 pd_10
23
24 \# x = 11 \text{ through formula}:
25 \times 11
26 pd_11 \leftarrow (1^x*exp(-1))/factorial(x)
27 pd_11
28
29 \# x = 12 \text{ through formula}:
30 \times = 12
31 pd_12 \leftarrow (1^x*exp(-1))/factorial(x)
32 pd_12
33
34 \# x = 13 \text{ through formula}:
35 \times 13
36 \text{ pd}_13 \leftarrow (1^x*exp(-1))/factorial(x)
37 pd_13
38
39 # Poission distribution for x>=8
```

```
40 sum(pd_8,pd_9,pd_10,pd_11,pd_12,pd_13)
```

R code Exa 5.8 Poisson distribution Example

```
1 # Poisson distribution Example :
2 # Poission formula : P(x) = lamda^x*e^-lamda/x!
3
4 l=3.2
5 x = 10
6 pd <- dpois(x,l,log=FALSE)
7 pd
8
9 # probability of getting exactly 10 customers during an 8-minute interval
10 l1=6.4
11 x1 = 10
12 pd1 <- dpois(x1,l1,log=FALSE)
13 pd1</pre>
```

R code Exa 5.9 Using poissions table

```
1 # using poission table :
2
3 1 <- 1.6
4 x<- c(6,7,8,9)
5
6
7 # Poission probability for x>5 :
8 p<-dpois(x,1)
9 p
10 sum(p)</pre>
```

R code Exa 5.10 Probability Example

```
1 # Probability Example:
3 p = .0003
4 n = 10000
5 l \leftarrow n*p
6 1
7 \times (-c(7,8,9,10,11,12))
9 # Binomial probability for x>5:
10 b < -dbinom(x,n,p)
11 b
12 sum(b)
13
14
15 # Poission probability for x>5:
16 p < -dpois(x,1)
17 p
18 sum(p)
```

R code Exa 5.11 Hypergeometrics distribution

```
1 # Hypergeometric distribution : P(x) = ACx*(N-A)C(n-x)/NCn
2
3 # N = size of the population, n = sample size, A = number of successes in the population, x = number of successes in the sample; sampling is done without replacement
4
5 N = 18
```

```
6  n = 3
7  A = 12
8
9  # Using choose function :
10
11 1-((choose(A,0)*choose((N-A),n))/choose(N,n))
```

Chapter 6

Continuous Distributions

R code Exa 6.1 Uniform Distribution

```
1 # Probabilities in Uniform Distribution : P(x) = x^2 - x^2
      x1 / b-a  where: a \le x1 \le x2 \le b
3 b = 39
4 \ a = 27
6 f_x = 1/(b-a) \# f(x)
7 f_x
9 u <- (a+b)/2 #mean
10 u
11
12 sd <- (b-a)/sqrt(b-a) # standard deviation
13 sd
14
15 \# P(30 \le x \le 35) :
16 P = (35-30)/(39-27)
17 P
18
19 \# P(x < 30) :
20 \text{ P1} = (30-27)/(39-27)
```

$\bf R$ code Exa $\bf 6.2\,$ MEAN AND STANDARD DEVIATION OF A UNIFORM DISTRIBUTION

```
1 # MEAN AND STANDARD DEVIATION OF A UNIFORM
     DISTRIBUTION:
3 u = 691 \# mean
4 a = 200
5 b = 1182
6 \times 1 = 410
7 \times 2 = 825
8 sd <- (b-a)/sqrt(12) # standard deviation
9 sd
10
11 # height of distribution :
12 f_x = 1/(b-a) \# f(x)
13 f_x
14
15 # probability that a randomly selected person pays
     between $410 and $825 annually for automobile
      insurance in the US:
16 p_x = (x2-x1)/(b-a)
17 p_x
```

R code Exa 6.3 Normal Curve distribution

```
1 # Normal Curve distribution :
2
3 mean = 494
4 sd=100
5 x =700
```

```
6
7 # probability of x greater than 700 :
8 pnorm(x, mean, sd, lower.tail=FALSE)
```

R code Exa 6.4 PROBABILITY OF A UNIFORM DISTRIBUTION

```
1 # PROBABILITY OF A UNIFORM DISTRIBUTION
3 x = 550
4 \text{ mean} = 494
5 \text{ sd} = 100
6 lb = .2123 # probability of values between 550 and
      the mean
7 ub =.5000 # probability of values less than the
      mean
8
10 # using r function :
11 pnorm(x, mean, sd)
12
13 # Or using normal formula :
14 z = (x - mean)/sd
15 z
16
17 ub+lb # probability of values 550
```

R code Exa 6.5 Probability of Normal Curve DISTRIBUTION

```
1 # Probability of Normal Curve DISTRIBUTION :
2
3 x = 600
4 mean = 494
5 sd = 100
```

```
6 x1 = 300
7
8 a <- pnorm(x1, mean, sd, lower.tail=FALSE)
9 a
10 b <- pnorm(x, mean, sd, lower.tail=FALSE)
11 b
12
13 # probability of a value between 300 and 600 :
14 a - b</pre>
```

R code Exa 6.6 PROBABILITY OF A UNIFORM DISTRIBUTION

```
1 # PROBABILITY OF A UNIFORM DISTRIBUTION
2
3 x = 350
4 mean = 494
5 sd = 100
6 x1 = 450
7
8 a <- pnorm(x, mean, sd, lower.tail=FALSE)
9 a
10 b <- pnorm(x1, mean, sd, lower.tail=FALSE)
11 b
12
13 # probability of a value between 350 and 450 :
14 a-b</pre>
```

R code Exa 6.7 MEAN OF A UNIFORM DISTRIBUTION

```
1 # MEAN OF A UNIFORM DISTRIBUTION
2
3 x = 449
4 z = 1.11 # value taken from z table
```

```
5 sd = 36
6 # z = (x - mean)/sd
7
8 mean = x - (z*sd)
9 mean
```

R code Exa 6.8 Normal distribution using z value

```
1 # Normal distribution using z value :
2
3 mean = 3.58
4 z = -0.46 # value taken from z table
5 sd = 1.04
6 # z = (x - mean)/sd
7
8 x = (z*sd) + mean
9 x
10
11 # 67.72% of the daily average amount of solid waste per person weighs more than 3.10 pound.
```

R code Exa 6.9 Binomial distribution problem by using the normal distribution

```
9 mean
10
11 sd = sqrt(n*p*q)
12 sd
13
14 \# \text{test} : \text{mean} +/- 3 \text{sd}
15 test1 <- mean + 3*sd
16 test2 <- mean - 3*sd
17 test1
18 test2
19
20 # test : 2.65 to 17.35
21
22 \# z \text{ value at } x = 12.5
23 \times = 12.5
24 z = (x-mean)/sd
25 z
26
27 \# z \text{ value at } x = 12.5
28 x = 11.5
29 z = (x-mean)/sd
30 z
31
32 \text{ } \#z = 1.02 \text{ produces a probability of } .3461.
33 \# z = 0.61 produces a probability of .2291.
34
35 # The difference in areas yields the following
      answer:
36 0.3461 - .2291
```

R code Exa 6.10 Binomial distribution by using the normal distribution

```
3 p = .37
4 n = 100
 5 q = 1 - p
6 \text{ mean1} = n*p
7 mean1
8 \text{ sd} = \text{sqrt}(n*p*q)
9 \text{ sd}
10
11 # range :
12 u = mean +3*(sd)
13 u
14 \ 1 = mean - 3*(sd)
15 l
16
17 x = 26.5
18 z = (x - mean) / sd
19 z
20
21 \#  tail of the distribution :
22 .5000 - .4850
23
24 \times 1 < -c(26:20)
25 b < -dbinom(x1,n,p)
26 b
27 sum(b)
```

R code Exa 6.11 Exponential Distribution

```
6 mean = 1/1
7 mean
8 x0 = .75
9
10 # P(x>=x0) :
11 P <- exp(-1*x0)
12 P
13
14 # for x0 = 0.75, Probability < x0 :
15 Prob = 1-P
16 Prob</pre>
```

Chapter 7

Sampling and Sampling Distributions

${f R}$ code ${f Exa}$ 7.1 ${f Z}$ formula for sample means

```
1 # Z formula for sample means : z = (sample_mean -
      average)/(standard_dev/sqrt(sample_size))
2
3 \text{ mean} = 448
4 \text{ sd} = 21/\text{sqrt}(49)
5 n = 49 \# sample size
6 \# sample mean : 441 <= x_bar <= 446
7 \text{ samplemean_l} = 441
8 \text{ samplemean}_u = 446
9
10 a <-pnorm(samplemean_l, mean, sd, lower.tail=FALSE)
12 b <-pnorm(samplemean_u, mean, sd, lower.tail=FALSE)
13 b
14
15
16 # probability of a value being between z = -2.33
      and -0.67 is :
17 \text{ prob} = a - b
```

R code Exa 7.2 Z formula for Sample mean of a finite population

R code Exa 7.3 Z formula for Sample Proportion

```
6  n = 80
7  q = 1-p
8
9  sd = sqrt(p*q/n)
10
11 # P(sample_prop >= .15) :
12  pnorm(sample_prop,p,sd,lower.tail=FALSE)
```

Chapter 8

Statistical Inference Estimation for Single Populations

R code Exa 8.1 Confidence interval to Estimate Population mean

```
1 # Confidence interval to Estimate Population mean :
2 # pop_mean +/- z*(sd/sqrt(n))
3
4 n = 44
5 sample_mean = 10.455
6 sd = 7.7
7 z = 1.645
8
9 pop_mean_1 = sample_mean - (z*(sd/sqrt(n)))
10 pop_mean_1
11
12 pop_mean_2 = sample_mean + (z*(sd/sqrt(n)))
13 pop_mean_2
```

R code Exa 8.2 Confidence interval to Estimate Population mean using Finite Correction

```
1 # Confidence interval to Estimate Population mean
      using finite correction:
2 \# (pop\_mean) +/- (z*(sd/sqrt(n))*sqrt(N-n/N-1))
3
4 n = 50
5 N = 800
6 \text{ sample_mean} = 34.30
7 \text{ sd} = 8
8 z = 2.33
10 pop_mean_1 = sample_mean - (z*(sd/sqrt(n))*sqrt((N-n))
      )/(N-1))
11 pop_mean_1
12
13 pop_mean_2 = sample_mean + (z*(sd/sqrt(n))*sqrt((N-n
     )/(N-1))
14 pop_mean_2
```

R code Exa 8.3 Confidence Interval to Estimate population mean Population standard deviation unknown and population normally distributed

```
# Confidence Interval to Estimate population mean :
    Population standard devition unknown and
    population normally distributed

# pop_mean +/- t*(sd/sqrt(n)) , df = n-1

a <- c(3,1,3,2,5,1,2,1,4,2,1,3,1,1)

n = 14

df = n-1

t = 3.012

sd = 1.29

sample_mean = 2.14

pop_mean_1 = sample_mean - (t*(sd/sqrt(n)))

pop_mean_1

pop_mean_1</pre>
```

```
13 pop_mean_2 = sample_mean + (t*(sd/sqrt(n)))
14 pop_mean_2
```

R code Exa 8.4 Confidence Interval to estimate Population Proportion

```
# Confidence Interval to estimate Population
        Proportion :
2 # p = samp_prop +/- (z*sqrt(samp_prop*q/sample size)
3
4 samp_prop = 0.51
5 q = 1-samp_prop
6 z = 1.75
7 n = 210 # sample size
8
9 p_1 = samp_prop - (z*sqrt(samp_prop*q/n))
10 p_1
11
12 p_2 = samp_prop + (z*sqrt(samp_prop*q/n))
13 p_2
```

R code Exa 8.5 Confidence Interval to estimate Population Proportion

```
1 # Confidence Interval to estimate Population
    Proportion :
2 # p = samp_prop +/- (z*sqrt(samp_prop*q/sample size)
3
4 samp_prop = 34/212 # sample size =212 and no. of
    jeans = 34
5 q = 1-samp_prop
6 z = 1.645
7 n = 212 # sample size
8
9 p_1 = samp_prop - (z*sqrt(samp_prop*q/n))
```

R code Exa 8.6 Confidence to estimate the Population Variance

```
2 # Confidence to estimate the Population Variance :
3 \# \text{var} = ((n-1)*s^2)/(X(a/2))^2 \text{ or } ((n-1)*s^2)/(X(1-a))
      (2))<sup>2</sup>, df = n-1
4
5 s = 1.12
6 n = 25
7 	 df = n-1
9 = qchisq(0.975, df=24)
10 a
11 b = qchisq(.025, df=24)
12 b
13
14 \text{ var}_1 = ((n-1)*s^2)/a
15 var_1
16
17 \text{ var}_2 = ((n-1)*s^2)/b
18 var_2
```

R code Exa 8.7 Sample Size when Estimating Population mean

```
1 # Sample Size when Estimating Population mean :
2 # n = (z*sd/E)^2
3
4 E = 1 # error in estimating
```

```
5 z = 1.96
6 sd = 5
7
8 n = (z*sd/E)^2
9 n
```

R code Exa 8.8 Sample size when estimating population proportion

```
1 # Sample size when estimating population proportion
    :
2 # n = z^2*p*q/E^2
3
4 E = .03
5 p = .40
6 z = 2.33
7 q = 1-p
8
9 n = z^2*p*q/E^2
10 n
```

Chapter 9

Statistical Inference Hypothesis Testing for Single Populations

R code Exa 9.1 Test Hypothesis about population mean

```
1 # Formula to test Hypoyhesis about population mean
2 \# z = sample\_mean - pop\_mean/(sd/sqrt(n))
4 \text{ pop}_{mean} = 4.30
5 \text{ sample_mean} = 4.156
6 \text{ sd} = .574
7 n = 32
8 a = .05 \# alpha value
10 # Calcultaed value of test statistic :
11 z1 = (sample_mean - pop_mean)/(sd/sqrt(n))
12 z1
13
14 \# Critical Z value associated with alpha = 0.05 :
15 z = qnorm(.05,lower.tail=TRUE)
16 z
17
18 # critical sample mean :
```

```
19 sample_mean_c = (z * (sd/sqrt(n))) + pop_mean
20 sample_mean_c
```

R code Exa 9.2 t test for population mean

```
1 # t test for population mean:
2 \# t = (sample\_mean - pop\_mean) / (sd/sqrt(n)), df =
      n-1
3
4 \text{ pop}_{mean} = 471
5 \text{ sample_mean} = 498.78
6 \text{ sd} = 46.94
7 n = 23
8 \text{ alpha} = 0.05
9 	 df = n-1
10
11 \# t-distribution function to calculate critical t-
      value using alpha and df:
12 qt(alpha, df, lower.tail = FALSE, log.p = FALSE)
13
14 # Observed t valueusing sample mean and standard
      deviation:
15 t = (sample_mean - pop_mean) / (sd/sqrt(n))
16 t
17
18 # The observed t value of 2.84 is greater than the
      table t value of 1.717,
19 # so the business researcher rejects the null
      hypothesis.
```

R code Exa 9.3 z test of a population proportion

```
1 # z test of a population proportion :
```

```
2 # z = sample_prop - population_prop/sqrt(population_
      prop*q/n)
3
4 n = 550
5 x = 115
6 \text{ sample_prop} = 115/550
7 \text{ population}_{prop} = .17
8 q = 1- population_prop
10 \# \text{test statistic value of z}:
11 z1 = (sample_prop - population_prop)/sqrt((
      population_prop*q)/n)
12 z1
13
14 # critical value of z :
15 z = qnorm(.05,lower.tail=FALSE)
16 z
17
18 # critical sample proportion :
19 sample_prop_c = z * sqrt(population_prop*q/n) +
      population_prop
20 sample_prop_c
```

R code Exa 9.4 Test Hypothesis about a population variance

```
1 # Test Hypothesis about a population variance: 2 # X^2 = (n-1)*s^2/var, df = n-1
3 
4 var = 25
5 n = 16
6 s_sq = 28.0625 # sample variance
7 df = n-1
8 
9 # Two tailed test and alpha = .10 it will be divided by 2:
```

```
10 \ a < - .10/2
11
12 # we have two critical values of chi square :
13
14 # 1st chi-sq value is a :
15 \text{ qchisq}(a, df=15)
16
17 \# 2nd chi-sq is 1-a :
18 \text{ qchisq}(1-a, df=15)
19
20 # The decision rule is to reject the null hypothesis
                               if the observed value
21 # of the test statistic is less than 7.26093 or
                            greater than 24.9958.
22
23 X_sq = ((n-1)*s_sq)/var
24 \quad X_sq
25
26 # This observed chi-square value is in the
                            nonrejection region because
27 \# \text{chi}_{sq}(.05) = 7.26 < \text{chi}_{sq}(\text{observed}) = 16.83 < \text{chi}_{sq}(.05) = 16.83 < \text{chi}_
                           sq(.95) = 24.9958.
28 # The company fails to reject the null hypothesis.
                           The population variance
29 # of overtime hours per week is 25.
```

R code Exa 9.5 Z value for Type II error

```
7
8 z = (sample_mean_c - pop_mean_1)/(sd/sqrt(n))
9 z
```

R code Exa 9.6 Z value for Type II error

```
1 # Z value for Type II error
3 z_c = 1.96
4 p = .40
5 q = 1 - p
6 n = 250
7 \# z_c = (p_c-p)/sqrt(p*q/n)
8 p_c = z_c * sqrt((p*q)/n) + p
9 p_c
10 p_c1 = z_c * sqrt((p*q)/n) - p
11 p_c1
12
13 # z value on taking p_c = .46 and p = .36:
14 p_c = .46
15 p = .36
16 z_c = (p_c-p)/sqrt(p*q/n)
17 z_c
18
19 \# z value on taking p_c = .34 and p = .36 :
20 p_c = .34
21 p = .36
z_c = (p_c-p)/sqrt(p*q/n)
23 z_c
24
25 # The area associated with z = 3.29 is .4995.
      Combining this value with the .2454 obtained from
      the left side of the distribution in graph (b)
      yields the total probability of committing a Type
       II error:
```

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Chapter 10

Statistical Inferences About Two Populations

R code Exa 10.1 Z formula for the difference in Two Sample Means

```
1 # z formula for the difference in two sample means :
z \# z = (samp_mean_1 - samp_mean_2) - (pop_mean_1 - pop_mean_1)
      2)/sqrt((sd1^2/n1)+(sd2^2/n2))
3
4 \quad \mathtt{samp} \underline{\mathtt{mean}} \underline{\mathtt{1}} = 3352
5 \text{ samp}_{mean}_2 = 5727
6 \text{ sd1} = 1100
7 \text{ sd2} = 1700
8 n1 = 87
9 n2 = 76
10
11 # Observed value of Z :
12 z1 = ((samp_mean_1-samp_mean_2)-(0))/sqrt((sd1^2/n1))
       +(sd2^2/n2)
13 z1
14
15 # Critical value of Z :
16 z = qnorm(.001, mean = 0, sd = 1, lower.tail = TRUE,
        log.p = FALSE)
```

```
17 z
18
19 # sample critical :
20 \text{ s_c} = (0) - (z*sqrt((sd1^2/n1) + (sd2^2/n2)))
21 s_c
22
23 # The difference in sample means would need to be at
       least 704.23
24 # to reject the null hypothesis.
25
26~\# The actual sample difference in this problem :
27 \text{ s_c} = \text{samp_mean_1-samp_mean_2}
28 s_c # which is considerably larger than the critical
       value of difference
29
30 #
     Thus, with the critical value method also, the
      null hypothesis is rejected.
```

R code Exa 10.2 Confidence Interval to estimate difference in two population means

R code Exa 10.3 t formula to test the difference in means assuming the standard deviations are equal

```
1 # t formula to test the difference in means assuming
                           sd1, sd2 are equal:
   2 \#t = (samp_mean_1-samp_mean_2)-(pop_mean_1-pop_mean_1)
                        2)/(sqrt((s1^2(n1-1))+(s2^2(n2-1))/n1+n2-2))*sqrt
                        ((1/n1)+(1/n2))
   4 n1 = 46
   5 n2 = 26
   6 \text{ samp}_{mean}_1 = 5.42
   7 \text{ samp}_{mean}_2 = 5.04
   8 \text{ s1} = .58
  9 \text{ s2} = .49
10 \quad df = n1+n2-2
11
12 # Critical t value :
13 qt(.005, df, lower.tail = FALSE, log.p = FALSE)
14
15 # Observed t value :
16 \ t = ((samp_mean_1 - samp_mean_2) - 0) / (sqrt(((s1^2*(n1)) - 0) / (sqrt))) / (sqrt)) / (sqrt) /
                        -1))+(s2^2*(n2-1)))/(n1+n2-2))*sqrt((1/n1)+(1/n2)
                        ))
17 t
18
19 # Because the observed value of is greater than the
                        critical table value of the decision is to reject
20 # the null hypothesis
```

 $\bf R$ code Exa $\bf 10.4$ CONFIDENCE INTERVAL TO ESTIMATE difference in means ASSUMING THE POPULATION VARIANCES ARE UNKNOWN AND EQUAL

```
1 # CONFIDENCE INTERVAL TO ESTIMATE difference in
      means ASSUMING THE POPULATION VARIANCES ARE
     UNKNOWN AND EQUAL:
2 n1 = 13
3 n2 = 15
4 \text{ samp}_{mean}_1 = 4.35
5 \text{ samp}_{mean}_2 = 6.84
6 	 s1 = 1.20
7 	 s2 = 1.42
9 \text{ alpha} = .025
10 \, df = 26
11
12 t = qt(alpha, df, lower.tail = FALSE, log.p = FALSE)
13 t
14
15 \# p_m_diff = pop_mean_1-pop_mean_2
16 s_diff = samp_mean_1-samp_mean_2
17 b = sqrt(((s1^2*(n1-1))+(s2^2*(n2-1)))/(n1+n2-2))
18 c = sqrt((1/n1)+(1/n2))
19
20
21 p_m_diff_1 = s_diff - (t*b*c)
22 p_m_diff_1
23
24 p_m_diff_2 = s_diff + (t*b*c)
25 p_m_diff_2
```

R code Exa 10.5 t formula to test the Difference in Two Dependent Population

```
1 # t formula to test the Difference in Two Dependent
      Population:
2 \# t = (\text{mean\_samp\_diff} - D) / (\text{sd/sqrt}(n))
3 \# df = n-1
4 \# D = \text{mean\_pop\_diff}, \text{ sd} = \text{sd\_samp\_diff}, \text{ n} = \text{num\_of\_}
      pairs, d= samp_diff_pair
5
7 Individual \leftarrow c(1,2,3,4,5,6,7)
8 Before \leftarrow c(32,11,21,17,30,38,14)
9 After <- c(39,15,35,13,41,39,22)
10 \, n = 7
11
12 for(i in 1:7){
13
     d = Before - After
14 }
15 print(d)
16 Individual <- cbind(Individual, Before, After, d)
17 Individual
18
19 mean_samp_diff = sum(d)/n
20 mean_samp_diff
21 	 d1 = sum(d)/7
22
23 sd = sqrt((sum((d-mean_samp_diff)^2))/(n-1))
24 \text{ sd}
25
26 \, \mathbf{D} = \mathbf{0}
27 t = (mean\_samp\_diff - D)/(sd/sqrt(n))
28 t
29
      Because the observed value of -2.54 is less than
30 #
      the critical, table value of -1.943 and the
31 # p-value (0.022) is less than alpha (.05), the
      decision is to reject the null hypothesis.
```

R code Exa 10.6 Z formula to test the difference in Population Proportion

```
1 # Z formula to test the difference in Population
      Proportion:
2 \# z = ((p1_c - p2_c) - (p1-p2)) / sqrt((p_c*q_c)*((1/p)))
     n1)+(1/n2))
3 \# p_c = ((n1*p1_c) + (n2*p2_c))/(n1+n2)
4 \# q_c = 1 - p_c
5
6 n1 = 100
7 n2 = 95
8 p1_c = .24
9 p2_c = .41
10
11 p_c = ((n1*p1_c)+(n2*p2_c))/(n1+n2)
12 p_c
13 \ q_c = 1 - p_c
14 q_c
15 \# p1 - p2 = 0
16
17 z = ((p1_c - p2_c) - (0)) / sqrt((p_c*q_c) * ((1)))
     /n1) + (1/n2) ) )
18 z
19
     If a one-tailed test had been used, zc would have
      been z.01 = 2.33,
21 \# \text{ and the null hypothesis would have been rejected.}
      If alpha had been .05,
22 \# zc would have been z. 025 =, and the null
      hypothesis would have been rejected.
```

R code Exa 10.7 F test for two Population Variance

```
1 # F test for two Population Variance :
2 \# F = s1^2/s2^2
3 \# df_num = v1 = n1-1 \text{ and } df_deno = v2 = n2-1
5 # from given table we computed :
6 s1_sq = 5961428.6
7 \text{ s2\_sq} = 737142.9
8 n1 = 7
9 n2 = 8
10
11 # critical F-value :
12 qf(.01, df1=n1-1, df2=n2-1, lower.tail = FALSE, log.
      p = FALSE)
13
14 # Obseved F- value :
15 F = s1_sq/s2_sq
16 F
17
18 \# Because the observed value of F = 8.09 is greater
      than the table
19 \# critical F value of 7.19, the decision is to
      reject the null hypothesis.
```

Chapter 11

Analysis of Variance and Design of Experiments

R code Exa 11.1 One Way ANOVA

```
1 # One Way ANOVA SSE, SSc, SST values :
2 \# SSC = sum(nj*(xj_b-x_b)^2)
3 \# SSE = sum(sum((xij-xj_b)^2))
4 \# SST = sum(sum((xij-x_b)^2))
6 \text{ a} \leftarrow c(29,27,30,27,28)
7 b \leftarrow c(32,33,31,34,30)
8 c < c(25,24,24,25,26)
9 df <- data.frame(a,b,c)
10 df
11
12 r = c(t(as.matrix(df))) \# response data
14 f = c("a", "b", "c") # treatment levels
15 k = 3
                              # number of treatment
     levels
16 \, n = 5
17
18 tm = gl(k, 1, n*k, factor(f)) # matching
```

```
treatments

19 tm

20

21 av = aov(r ~ tm)

22 av

23 summary(av)
```

R code Exa 11.2 TUKEYs HSD Test

```
1 # TUKEYs HSD Test : HSD = q*sqrt(MSE/n) # q =
       critical value
3 \text{ a} \leftarrow c(2.46, 2.41, 2.43, 2.47, 2.46)
4 b \leftarrow c(2.38,2.34,2.31,2.40,2.32)
5 c < c(2.51, 2.48, 2.46, 2.49, 2.44)
6 d \leftarrow c(2.49,2.47,2.48,2.46,2.44)
7 e \leftarrow c(2.56,2.57,2.53,2.55,2.55)
8 df <- data.frame(a,b,c,d,e)</pre>
9 df
10
11
12 r = c(t(as.matrix(df))) \# response data
13 r
14 f = c("a", "b", "c", "d", "e") # treatment levels
15 k = 5
                                 # number of treatment
      levels
16 n = 5
17
18 tm = gl(k, 1, n*k, factor(f)) # matching
      treatments
19 tm
20
21 \text{ av} = \text{aov}(\text{r} \text{ tm})
23 b <- summary(av)
```

```
24 b
25
26 # From above anova analysis we get MSE value:
27 MSE = 0.000618
28 q = 5.29
29 n = 5
30 HSD = q*sqrt(MSE/n)
31 HSD
```

R code Exa 11.3 Randomized Block Design

```
1 # Formula for computing Randomized Block Design for
      SSE, SSC, SSR, SST
2 \# SSC = n*sum((xj_b-x_b)^2)
3 \# SSR = C*sum((xi_b-x_b)^2)
4 \# SSE = sum(sum((xij-xj_b-xi_b+x_b)^2))
5 \# SST = sum(sum((xij-x_b)^2))
7 a \leftarrow c(3.47,3.43,3.44,3.46,3.46,3.44)
8 b \leftarrow c(3.40,3.41,3.41,3.45,3.40,3.43)
9 \quad c \leftarrow c(3.38, 3.42, 3.43, 3.40, 3.39, 3.42)
10 d \leftarrow c(3.32,3.35,3.36,3.30,3.39,3.39)
11 e \leftarrow c(3.50,3.44,3.45,3.45,3.48,3.49)
12 df <- data.frame(a,b,c,d,e)
13 df
14
15
16 r = c(t(as.matrix(df))) \# response data
17 r
18 f = c("a", "b", "c", "d", "e")
                                    # treatment levels
19 k = 5
                               # number of treatment
      levels
20 \, \text{n} = 6
21
22 blk = gl(n, k, k*n)
                                      # blocking factor
```

R code Exa 11.4 Two Way ANOVA

```
1 #
        Two-Way ANOVA:
 3 Types_of_warehouses <- c("GM", "GM", "GM", "GM", "GM", "GM", "
        GM", "GM", "GM", "GM",
                                              "Com", "Com", "Com", "Com", "
 4
                                                  \operatorname{Com} , "\operatorname{Com} , "\operatorname{Com} , "\operatorname{Com} , "\operatorname{Com} , "
                                                  Com",
                                              "BS", "BS", "BS", "BS", "BS", "
 5
                                                  BS", "BS", "BS", "BS",
                                              " \operatorname{CS}", " \operatorname{CS}", " \operatorname{CS}", " \operatorname{CS}", " \operatorname{CS}", "
 6
                                                  CS", " CS", " CS", " CS", "
                                                  CS")
 7
 8
    Training_sessions <- c("A", "A", "A", "B", "B", "B", "C", "
        C", "C", "A", "A", "A",
                                          "B" , "B" , "B" , "C" , "C" , "C" , "A" , "
10
                                              A", "A", "B", "B", "B",
                                          ^{"}C" , ^{"}C" , ^{"}C" , ^{"}A" , ^{"}A" , ^{"}A" , ^{"}B" , ^{"}
11
                                              B", "B", "C", "C", "C")
12
13 Values \leftarrow c(3,4.5,4,2,2.5,2,2.5,
```

```
1,1.5,5,4.5,4,1,3,2.5,0,1.5,2,2.5,3,3.5,1,3, 1.5,

3.5,3.5, 4,2,2,3,5, 4.5,2.5,4, 4.5, 5)

16 df <- data.frame(Types_of_warehouses,Training_sessions,Values)

17 df

18

19 av <- aov(Values~as.factor(Types_of_warehouses)*as.factor(Training_sessions),data= df)

20 av

21 summary(av)
```

Simple Regression Analysis and Correlation

R code Exa 12.1 Slope of Regression line

R code Exa 12.2 Residual Analysis

```
1 # Residual Analysis :
```

```
3 Hospitals \leftarrow c(1,2,3,4,5,6,7,8,9,10,11,12)
4 \times (-c(23,29,29,35,42,46,50,54,64,66,76,78)
5 y <- c
      (69,95,102,118,126,125,138,178,156,184,176,225)
6 for(i in 1:12){
    x_sq <- x*x
8 }
9 print(x_sq)
10
11 for(i in 1:12){
12 xy <- x*y
13 }
14 print(xy)
15
16 \times 1 \leftarrow cbind(x,y,x_sq,xy)
17
18 n = 12
19
20 b1 = ((sum(x*y)) - ((sum(x)*sum(y))/n))/((sum(x^2)) - (
      sum(x)^2/n)
21 b1
22
23 b0 = (sum(y)/n)-b1*(sum(x)/n)
24 b0
25
26 \# y_c = 30.91 + 2.23 * x
27 \quad y_c = b0 + b1*x
28 y_c
29 \times 1 \leftarrow cbind(x1,y_c)
30
31 Residual <- y-y_c
32 Residual
33
34 x1 <- cbind(x1, Residual)
35 \text{ View}(x1)
36
37 sum (Residual)
```

R code Exa 12.3 Standard Error of Estimation

```
1 # Standard Error of Estimation : Se = sqrt(SSE/(n-2))
2 \# SSE = sum((y-y_c)^2)
4 Hospitals \leftarrow c(1,2,3,4,5,6,7,8,9,10,11,12)
5 \times (23,29,29,35,42,46,50,54,64,66,76,78)
6 y <- c
      (69,95,102,118,126,125,138,178,156,184,176,225)
7 for(i in 1:12){
8
     x_sq \leftarrow x*x
9 }
10 print(x_sq)
11
12 for(i in 1:12){
13
     xy < - x*y
14 }
15 print(xy)
16
17 x1 \leftarrow cbind(x,y,x_sq,xy)
18
19 n = 12
20
21 b1 = ((sum(x*y))-((sum(x)*sum(y))/n))/((sum(x^2))-(
      sum(x)^2/n)
22 b1
23
24 b0 = (sum(y)/n)-b1*(sum(x)/n)
25 b0
26
27 \# y_c = 30.91 + 2.23 * x
```

```
28 \quad y_c = b0 + b1*x
29 y_c
30 \times 1 \leftarrow cbind(x1,y_c)
31
32 Residual <- y-y_c
33 Residual
34
35 x1 <- cbind(x1, Residual)
36
37 for(i in 1:12){
     Residual_sq = Residual^2
38
39 }
40 print(Residual_sq)
41
42 x1 <- cbind(x1, Residual_sq)
43 \text{ View}(x1)
44
45 SSE = sum(Residual_sq)
46 SSE
47
48 Se = sqrt(SSE/(n-2))
49 Se
```

R code Exa 12.4 Coeficient of Determination

```
9 }
10 print(x_sq)
11
12 for(i in 1:12){
13
     xy < - x*y
14 }
15 print(xy)
16
17 x1 \leftarrow cbind(x,y,x_sq,xy)
18
19 n = 12
20
21 b1 = ((sum(x*y))-((sum(x)*sum(y))/n))/((sum(x^2))-(
      sum(x)^2/n)
22 b1
23
24 b0 = (sum(y)/n)-b1*(sum(x)/n)
25 b0
26
27 \# y_c = 30.91 + 2.23 * x
28 \text{ y}_{c} = b0 + b1*x
29 y_c
30 \times 1 \leftarrow cbind(x1,y_c)
31
32 Residual <- y-y_c
33 Residual
34
35 x1 <- cbind(x1, Residual)
36
37 for(i in 1:12){
38
     Residual_sq = Residual^2
39 }
40 print(Residual_sq)
41
42 x1 <- cbind(x1, Residual_sq)
43 View(x1)
44
45 SSE = sum(Residual_sq)
```

```
46 SSE

47

48 SS_yy = sum(y^2)-(sum(y)^2/n)

49 SS_yy

50

51 r_sq = 1-(SSE/SS_yy)

52 r_sq

53

54 # Or r_sq = (b1^2 * SS_xx)/SS_yy
```

R code Exa 12.5 t test for slope

```
1 # t test for slope :
3 no_of_beds \leftarrow c(23,29,29,35,42,46,50,54,64,66,76,78)
4 FTEs <- c
      (69,95,102,118,126,125,138,178,156,184,176,225)
5 Hospitals <-data.frame(no_of_beds,FTEs)</pre>
6 Hospitals
7
8 # critical t value :
9 \text{ qchisq}(.01, df = 10)
10
11 # least squares equation of the regression line is:
12 a <- lm( FTEs ~ no_of_beds, data=Hospitals)
                         \# v_c = 30.91 + 2.23 * x
13 a
14 b <- summary(a)
15 b
16
17 # observed t value :
18 b$coefficients[6]
```

R code Exa 12.6 CONFIDENCE INTERVAL TO ESTIMATE THE SINGAL VALUE FOR A GIVEN VALUE OF ${\bf x}$

```
1 # CONFIDENCE INTERVAL TO ESTIMATE E (yx) FOR A GIVEN
      VALUE OF x :
2 \# y_c +/- t*Se*sqrt((1/n)+((x0-x_b)^2)/SS_xx)
3 \# SS_x = sum(x^2) - (sum(x)^2/n)
5 \text{ no\_of\_beds} \leftarrow c(23,29,29,35,42,46,50,54,64,66,76,78)
6 FTEs <- c
      (69,95,102,118,126,125,138,178,156,184,176,225)
7 Hospitals <-data.frame (no_of_beds,FTEs)
8 Hospitals
9
10 a <- lm( FTEs ~ no_of_beds, data=Hospitals)
12
13 data = data.frame(no_of_beds=40)
14 data
15
16 predict(a, data, interval="confidence")
17
18 predict(a, data, interval="predict")
```

R code Exa 12.7 Regression Analysis Example

```
8
9 library("ggplot2")
10 ggplot(df, aes(x=Month, y=Sales)) + geom_point(size =1)
11
12 # Regression Analysis: Sales versus Month
13 a <- lm(Sales~Month_number, data= df)
14 a
15 summary(a)
16
17 # y_cap = 32,628.2 - 86.21*x :
18 x =10
19 y_cap = 32628.2 - 86.21*x
20 y_cap</pre>
```

Multiple Regression Analysis

R code Exa 13.1 Multiple Regression Model

R code Exa 13.2 Multiple Regression Analysis Model

```
12 s <-summary(a)
13 s
14 anova(a)
15
16 pred <- predict(a)
17 resd <- s$residuals
18 data <- data.frame(pred,resd)
19 View(data)</pre>
```

Building Multiple Regression Models

R code Exa 14.1 Model Transformation

```
1 # Model Transformation : y = B0*x_B1 + E
3 \text{ y_cost} \leftarrow c(1.2, 9.0, 4.5, 3.2, 13.0, 0.6, 1.8, 2.7)
4 \text{ x\_weight} \leftarrow c
       (450,20200,9060,3500,75600,175,800,2100)
5 y_cost <- data.frame(y_cost,x_weight)</pre>
6 y_cost
8 \# \log y = \log_B B0 + B1 * \log x + E
9 \log_x y \leftarrow \log_10(y_cost)
10 \log_x xy
11
12 a <-lm(y_cost~x_weight,data=log_xy)</pre>
13 a
14 b <-summary(a)
15 b
16
17 b0 <- b$coefficients[1]
18 b0
```

```
19 b1 <- b$coefficients[2]
20 b1
21
22 logy_c = b0 + b1 * (sum(log_xy$x_weight)/8)
23 logy_c
24
25 # antilog = 2.9644
26 # y = (.055857)*x^.49606
```

Time Series Forecasting and Index Numbers

R code Exa 15.1.a Moving average

```
1 # Moving average :
3 Month <- c("January", "February", "March", "April", "May
     ", "June", "July", "August", "September", "October", "
      November", "December")
4 Shipments <- c
      (1056, 1345, 1381, 1191, 1259, 1361, 1110, 1334, 1416, 1282, 1341, 1382)
5 Month <- cbind (Month, Shipments)
6 Month
8 # The ???rst moving average is
9 first_four_Month_Moving_Average = sum(Shipments[1],
      Shipments [2], Shipments [3], Shipments [4])/4
10 first_four_Month_Moving_Average
11 Second_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [2], Shipments [3], Shipments [4])/4
12 Second_four_Month_Moving_Average
13 Third_four_Month_Moving_Average = sum(Shipments[5],
```

```
Shipments [6], Shipments [3], Shipments [4])/4
14 Third_four_Month_Moving_Average
15 fourth_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [6], Shipments [7], Shipments [4])/4
16 fourth_four_Month_Moving_Average
17 fifth_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [6], Shipments [7], Shipments [8])/4
18 fifth_four_Month_Moving_Average
19 sixth_four_Month_Moving_Average = sum(Shipments[9],
      Shipments [6], Shipments [7], Shipments [8])/4
20 sixth_four_Month_Moving_Average
21 seventh_four_Month_Moving_Average = sum(Shipments
      [9], Shipments [10], Shipments [7], Shipments [8])/4
22 seventh_four_Month_Moving_Average
23 eight_four_Month_Moving_Average = sum(Shipments[9],
      Shipments [10], Shipments [11], Shipments [8])/4
24 eight_four_Month_Moving_Average
25
26 \, a =
27 b =
29 d =
30 Average = rbind(a,b,c,d,first_four_Month_Moving_
      Average, Second_four_Month_Moving_Average, Third_
      four_Month_Moving_Average,
31
             fourth_four_Month_Moving_Average,fifth_
                four_Month_Moving_Average, sixth_four_
                Month_Moving_Average,
32
             seventh_four_Month_Moving_Average,eight_
                four_Month_Moving_Average)
33 Average
```

R code Exa 15.1.b Moving average

1 # Error in Moving Average :

```
2 # Moving average :
3
4 Month <- c("January", "February", "March", "April", "May
      ", "June", "July", "August", "September", "October", "
      November", "December")
5 Shipments <- c
      (1056, 1345, 1381, 1191, 1259, 1361, 1110, 1334, 1416, 1282, 1341, 1382)
6 Month <- cbind (Month, Shipments)
7 Month
8
9 # The ???rst moving average is
10 first_four_Month_Moving_Average = sum(Shipments[1],
      Shipments [2], Shipments [3], Shipments [4])/4
11 first_four_Month_Moving_Average
12 Second_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [2], Shipments [3], Shipments [4])/4
13 Second_four_Month_Moving_Average
14 Third_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [6], Shipments [3], Shipments [4])/4
15 Third_four_Month_Moving_Average
16 fourth_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [6], Shipments [7], Shipments [4])/4
17 fourth_four_Month_Moving_Average
18 fifth_four_Month_Moving_Average = sum(Shipments[5],
      Shipments [6], Shipments [7], Shipments [8])/4
19 fifth_four_Month_Moving_Average
20 sixth_four_Month_Moving_Average = sum(Shipments[9],
      Shipments [6], Shipments [7], Shipments [8])/4
21 sixth_four_Month_Moving_Average
22 seventh_four_Month_Moving_Average = sum(Shipments
      [9], Shipments [10], Shipments [7], Shipments [8])/4
23 seventh_four_Month_Moving_Average
24 eight_four_Month_Moving_Average = sum(Shipments[9],
      Shipments [10], Shipments [11], Shipments [8])/4
25 eight_four_Month_Moving_Average
26
27 \ a = " "
```

```
28 b= ""
29 c = " "
30 \, d = " "
31 Average = rbind(a,b,c,d,first_four_Month_Moving_
     Average, Second_four_Month_Moving_Average, Third_
     four_Month_Moving_Average,
                   fourth_four_Month_Moving_Average,
32
                      fifth_four_Month_Moving_Average,
                      sixth_four_Month_Moving_Average,
33
                    seventh_four_Month_Moving_Average,
                      eight_four_Month_Moving_Average)
34 Average
35
36 \ a = " "
37 b= " "
38 c = ""
39 \, d = " "
40 Error_May = Shipments[5]-first_four_Month_Moving_
     Average
41 Error_June = Shipments[6]-Second_four_Month_Moving_
     Average
42 Error_July = Shipments[7]-Third_four_Month_Moving_
     Average
43 Error_Aug = Shipments[8]-fourth_four_Month_Moving_
     Average
44 Error_sep = Shipments[9]-fifth_four_Month_Moving_
     Average
45 Error_oct = Shipments[10]-sixth_four_Month_Moving_
     Average
46 Error_nov = Shipments[11]-seventh_four_Month_Moving_
     Average
  Error_dec = Shipments[12] - eight_four_Month_Moving_
47
     Average
48 Error <- rbind(a,b,c,d,Error_May,Error_June,Error_
     July, Error_Aug, Error_sep, Error_oct, Error_nov,
     Error_dec)
49 Error
50 Month <- cbind (Month, Average, Error)
```

R code Exa 15.2 Weighted Moving Average

```
1 # Weighted MOving Average : 3*l + 3*p + 3*b_p/6
3 Month <- c("January", "February", "March", "April", "May
     ", "June", "July", "August", "September", "October", "
     November", "December")
4 Shipments <- c
      (1056, 1345, 1381, 1191, 1259, 1361, 1110, 1334, 1416, 1282, 1341, 1382)
5 Month <- data.frame(Month, Shipments)
6 Month
7 weights1 <-c(4,2,1,1)
9 # install.packages("stats")
10 library(stats)
11
12 f_weight_may <- weighted.mean(Shipments[4:1],
     weights1)
13 f_weight_june <- weighted.mean(Shipments[5:2],
     weights1)
14 f_weight_july <- weighted.mean(Shipments[6:3],
     weights1)
15 f_weight_aug <- weighted.mean(Shipments[7:4],
     weights1)
16 f_weight_sep <- weighted.mean(Shipments[8:5],
     weights1)
17 f_weight_oct <- weighted.mean(Shipments[9:6],
     weights1)
18 f_weight_nov <- weighted.mean(Shipments[10:7],
     weights1)
19 f_weight_dec <- weighted.mean(Shipments[11:8],
     weights1)
```

R code Exa 15.3 EXPONENTIAL SMOOTHING

```
1 # EXPONENTIAL SMOOTHING :
2 \text{ Year } \leftarrow c(1:16)
3 Total_units <- c
      (1193,1014,1200,1288,1457,1354,1477,1474,1617,1641,1569,
                     1603,1705,1848,1956,2068)
4
5 data <- data.frame(Year, Total_units)</pre>
6 data
8 library(ggplot2)
9 ggplot(data=data, aes(x=data$Year, y=data$Total_
     units, group=1)) +
     geom_line(linetype = "dashed")+
10
11
     geom_point()
12
13 # using exponential smoothing function i.e. ses():
14 # install.package("forecast")
15 library(forecast)
```

```
16 # Forecast and error values for alpha = 0.2:
17 f_a <- ses(Total_units, h = 8, alpha = 0.2, initial
      = "simple")[["fitted"]]
18 error_a \leftarrow ses(Total_units, h = 8, alpha = 0.2,
       initial = "simple")[["residuals"]]
19
20 # Forecast and error values for alpha = 0.2:
21 	ext{ f_b } \leftarrow 	ext{ses}(	ext{Total\_units}, 	ext{ h = 8, alpha = 0.5, initial}
      = "simple")[["fitted"]]
22 error_b \leftarrow ses(Total_units, h = 8, alpha = 0.5,
       initial = "simple")[["residuals"]]
23
24 \# Forecast and error values for alpha = 0.2:
25 \text{ f_c} \leftarrow \text{ses(Total\_units, h = 8, alpha = 0.8, initial)}
      = "simple")[["fitted"]]
26 \text{ error}_{c} \leftarrow \text{ses}(\text{Total}_{units}, h = 8, alpha = 0.8,
       initial = "simple")[["residuals"]]
27
28 f_data <- data.frame(data,f_a,error_a,f_b,error_b,f_</pre>
       c, error_c)
29 View(f_data)
30
31 # MAD and MSE values of alpha = 0.2, 0.5, 0.8:
32 \text{ MAD}_a \leftarrow \text{sum}(abs(error_a))/15
33 MSE_a \leftarrow sum(abs(error_a^2))/15
34
35 \text{ MAD_b} \leftarrow \text{sum}(abs(error_b))/15
36 \text{ MSE\_b} \leftarrow \text{sum}(abs(error\_b^2))/15
37
38 MAD_c \leftarrow sum(abs(error_c))/15
39 MSE_c \leftarrow sum(abs(error_c^2))/15
40
41 val <- rbind(MAD_a, MSE_a, MAD_b, MSE_b, MAD_c, MSE_c)
42 val
```

R code Exa 15.4 Regression Trend Analysis Using Quadratic Models

```
1 # Regression Trend Analysis Using Quadratic Models
3 Year <- c(1991:2007)
4 Labour_force <- c
      (117.72,118.49,120.26,123.06,124.90,126.71,129.56,131.46,133.49,1
5 Year_sq <- Year^2</pre>
6 Year <- data.frame(Year, Labour_force, Year_sq)</pre>
7 Year
8 a <-lm(Labour_force~Year, data=Year)</pre>
9 a
10 anova(a)
11 ggplot(data = Year, aes(x=Year, y=Labour_force))+geom_
      point()+geom_smooth(method = "lm")
12
13 b <-lm(Labour_force~.,data=Year)</pre>
14 b
15 anova(b)
16 ggplot(data = Year, aes(x=Year_sq,y=Labour_force))+
      geom_point()+geom_smooth(method = "lm")
```

${f R}$ code Exa 15.5 LASPEYRES PRICE INDEX and PAASCHE PRICE INDEX

```
1 # LASPEYRES PRICE INDEX and PAASCHE PRICE INDEX :
2 year <- c(2008,2009)
3 p.Syrings <- c(6.70,6.95)
4 q.Syrings <- c(150,135)
5 p.Cotton <- c(1.35,1.45)
6 q.Cotton <- c(60,65)
7 p.Patient <- c(5.10,6.25)
8 q.Patient <- c(8,12)
9 p.ChildrenTylenol <- c(4.50,4.95)</pre>
```

```
10 q.ChildrenTylenol <- c(25,30)
11 p.Computerpaper <- c(11.95,13.20)
12 q.Computerpaper \leftarrow c(6,8)
13 p. Thermometer <-c(7.90, 9.00)
14 q. Thermometer \leftarrow c(4,2)
15
16 data <- data.frame(year,p.Syrings,q.Syrings,p.Cotton
      ,q.Cotton,p.Patient,q.Patient,
                       p.ChildrenTylenol,q.
17
                          ChildrenTylenol,p.
                          Computerpaper, q. Computerpaper,
                       p. Thermometer, q. Thermometer)
18
19 data
20
21 # Unweighted Aggregate Index for 2009 :
22 p_2009 <- sum(p.Syrings[2],p.Cotton[2],p.Patient[2],
      p.ChildrenTylenol[2],p.Computerpaper[2],
23
            p. Thermometer [2])
24 p_2008 <- sum(p.Syrings[1],p.Cotton[1],p.Patient[1],
      p.ChildrenTylenol[1],p.Computerpaper[1],
25
                  p. Thermometer [1])
26 I = (p_2009/p_2008)*100
27 I
28
29 # Laspeyres Price Indices
30 # install.packages("micEcon")
31 # install.packages("micEconIndex")
32 library (micEconIndex)
33 library (micEcon)
34 a <- priceIndex(c("p.Syrings","p.Cotton","p.Patient"
      ,"p. Children Tylenol", "p. Computerpaper",
                 "p. Thermometer"), c("q. Syrings", "q.
35
                    Cotton", "q. Patient", "q.
                    Children Tylenol"
                                       "q. Computerpaper","
36
                                          q. Thermometer")
                                          ,1,data)
37 a
```

```
38 \quad I_2009_Laspeyres \leftarrow a[2]*100
39 I_2009_Laspeyres
40
41 # Paasche Price Indices
42 b <- priceIndex(c("p.Syrings","p.Cotton","p.Patient"
      ", "p. Children Tylenol", "p. Computerpaper",
                 "p. Thermometer"), c("q.Syrings", "q.
43
                    Cotton", "q. Patient", "q.
                    Children Tylenol",
                                        "q. Computerpaper","
44
                                           q. Thermometer")
                                           ,1,data,"Paasche
45 b
46 I_2009_Passache <- b[2]*100
47 I_2009_Passache
```

Analysis of Categorical Data

R code Exa 16.1 CHI SQUARE GOODNESS OF FIT TEST

```
1 # CHI-SQUARE GOODNESS OF-FIT TEST : X_sq = sum((fo-
      fe)^2/fe)
2 \# df = k-1-c
3 Month <- c("January", "February", "March", "April", "May
      ", "June", "July", "August", "September", "October", "
      November", "December")
4 fo <- c
      (1610, 1585, 1649, 1590, 1540, 1397, 1410, 1350, 1495, 1564, 1602, 1655)
6 \# critical value of chi-square when alpha is <math>0.01 :
7 qchisq(.99, df=11)
8
10 fe <- sum(fo)/12
11 for(i in 1:12){
12
     X = (fo-fe)^2/fe
13 }
14 print(X)
15
16 # Observed chi-square value :
```

R code Exa 16.2 Test data is whether in Poisson distributed

```
1 # Test data is whether in Poisson distributed :
2
3 no_of_arrival \leftarrow c(0,1,2,3,4,5)
4 obs_freq \leftarrow c(7,18,25,17,12,5)
5
6 \# \text{chi square value when alpha} = 0.05:
7 qchisq(.95,4)
9 for(i in 1:6){
     arr_obs <- no_of_arrival*obs_freq</pre>
10
11 }
12 print(arr_obs)
14 l = sum(arr_obs)/sum(obs_freq)
15 1 # lambda
16
17 # Expected probability using lamba and no_of_arrival
18 exp_pb <- c(.1003,.2306,.2652,.2033,.1169,.0837)
19
```

```
for(i in 0:5){
    exp_freq = sum(obs_freq)*exp_pb

print(exp_freq)

no_of_arrival <- cbind(no_of_arrival, obs_freq, arr_
    obs, exp_pb, exp_freq)

no_of_arrival

for(i in 0:5){
    X = (obs_freq-exp_freq)^2/exp_freq
}

print(X)

sum(X)</pre>
```

R code Exa 16.3 CHI SQUARE GOODNESS OF FIT TEST example 2

```
1 # CHI SQUARE GOODNESS OF FIT TEST example 2 :
2 p <- c("Milk","non-Milk")</pre>
3 fo <-c(115,435)
4 fe <-c(93.5,456.5)
6 # critical value of chi-square :
7 qchisq(.95, df=1)
9 X_1 = (fo[1] - fe[1])^2/fe[1]
10 X_1
11
12 X_2 = (fo[2]-fe[2])^2/fe[2]
13 X<sub>2</sub>
14
15 # Observed value of chi-square :
16 \ X_sq = X_1 + X_2
17 X_sq
18
```

R code Exa 16.4 CHI SQUARE TEST OF INDEPENDENCE

```
1 # CHI-SQUARE TEST OF INDEPENDENCE :
3 Age = matrix(c(26,95,18,41,40,20,24,13,32),nrow=3,
     ncol=3, byrow = TRUE)
4 dimnames (Age) = list(c("21-34","35-55",">55"), c("
     Coffee_tea ", "Soft_Drink", "Other"))
5 Age
7 # chi-square expected value when alpha = .01:
8 \text{ qchisq}(.99, df=4)
9
10 # The degrees of freedom are (3-1)(3-1)=4, and
      the critical value is 13.2767.
11 # The decision rule is to reject the null hypothesis
      if the observed value of chisquare
12 \# is greater than 13.2767.
13
14
15 # chi-square observed value :
16 # installed.pacakges("stats")
17 library(stats)
18 chisq.test(Age)
19
20 # The observed value of chi-square, 59.41, is
      greater than the critical value, 13.2767,
21 # so the null hypothesis is rejected.
```

Nonparametric Statistics

R code Exa 17.1 Mann Whitney U test

```
Mann-Whitney U test:
3 Total_emp_comp <- c
     (18.75, 19.80, 20.10, 20.75, 21.64, 21.90, 22.36, 22.96, 23.45, 23.88, 24.1)
4 Rank <- c(1,2,3,4,5,6,7,8,9,10,11,12,13,14,15)
\mathrm{E"} , "E" , "E" , "E" , "E" )
6 Total_emp_comp <- data.frame(Total_emp_comp,Rank,</pre>
     Group)
  Total_emp_comp
9 \text{ W1} = 1+2+3+4+6+7+8
10 W1
11 \quad W2 = 5+9+10+11+12+13+14+15
12 W2
13 U1 = (7)*(8) + ((7)*(8))/2 - W1
14 U1
15 U2 = (7)*(8) + ((8)*(9))/2 - W2
16 U2
17
```

```
18 # Using Wilcox test :
19 wilcox.test(Total_emp_comp ~ Group, data = Total_emp_comp, exact = FALSE)
20
21 #Because U2 is the smaller value of U, we use U=3 as the test statistic for Table A.13.
22 # Because it is the smallest size, let n1=7; n2=8.
23
24 # Because the p-value is less than a = .05, the null hypothesis is rejected.
```

R code Exa 17.2 LARGE SAMPLE FORMULAS MANN WHITNEY U TEST

```
1 #LARGE-SAMPLE FORMULAS MANN-WHITNEY U TEST :
 3 Value <- c
         (2.25, 2.70, 2.75, 2.97, 2.97, 3.10, 3.15, 3.29, 3.50, 3.60, 3.61, 3.65, 3.68
                     4.01,4.05,4.10,4.10,4.25,4.29,4.53,4.75,4.80,4.80,4.98,5.
 4
 5 Rank <- c
         (1,2,3,4.5,4.5,6,7,8,9,10,11,12,13,14,15,16,17,18.5,18.5,20,21,22
 V', 'R', 'V', 'R', 'R',
                     ^{\prime}\mathrm{V}^{\prime} , ^{\prime}\mathrm{V}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{V}^{\prime} , ^{\prime}\mathrm{V}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{R}^{\prime} , ^{\prime}\mathrm{R}^{\prime} ,
 7
                         R', 'R', 'R', 'R', 'R')
 8 Value <- data.frame(Value, Rank, Group)
9 Value
10
             1 + 3 + 4.5 + 4.5 + 6 + 7 + 8 + 10 + 11 + 13 +
          16 + 17 + 21 + 22
12 W1
13
```

```
14 \ U = (14)*(16) + ((14)*(15))/2 - W1
15 U
16
17 U_u = ((14)*(16))/2
18 U_u
19
20 \text{ sd_u} = \text{sqrt}(((14)*(16)*(31))/12)
21 \text{ sd}_u
22
23 # observed value
24 z = (U-U_u)/sd_u
25 z
26
27 \# Wilcox test :
28 wilcox.test(Value ~ Group, data = Value, exact =
      FALSE)
```

R code Exa 17.3 WILCOXON MATCHED PAIRS SIGNED RANK TEST

```
11 # test statistic z value :
12 qnorm(.99,lower.tail = FALSE)
13
14 # T positive and negative using wilcox test function
15 wilcox.test(Worker$Before, Worker$After, paired=TRUE
16 wilcox.test(Worker$d, Worker$Rank, paired=TRUE)
17
18 # T positive and negative using formula:
19 T_p < 3.5+3.5+3.5
20 T_p
21 T_n \leftarrow 19 + 17 + 9 + 9 + 9 + 14.5 + 9 + 14.5 + 17 +
      17 + 9 + 3.5 + 3.5 + 12.5 + 3.5 + 12.5
22 \quad T_n
23
24 \quad T_{min} = \min(T_p, T_n)
25 \text{ T_min}
26
27 n = 19
28 T_{mean} = (n*(n+1))/4
29 T_{mean}
30
31 T_{sd} = sqrt((n*(n+1)*(2*n+1))/24)
32 T_sd
33
34 # observed z value :
35 z = (T_{min} - T_{mean})/T_{sd}
36 z
37
38 # The observed z value (-3.41) is in the rejection
      region, so the analyst rejects the null
      hypothesis.
39 # The productivity is signi????cantly greater after
      the implementation of quality control
40 # at this company.
```

R code Exa 17.4 KRUSKAL WALLIS TEST

```
1 # KRUSKAL–WALLIS TEST
3 Group_native \leftarrow c(8,5,7,11,9,6)
4 Group_water <- c(10,12,11,9,13,12)
5 Group_fertilizer <- c(11,14,10,16,17,12)
6 Group_water_fertilizer <- c(18,20,16,15,14,22)
7 Group <-data.frame(Group_native, Group_water, Group_
      fertilizer, Group_water_fertilizer)
8 Group
9
10 \# alpha = .01, critical value :
11 qchisq(.99,df=3)
12
13 native <- Group $Group_native
14 water <- Group $Group_water
15 fertilizer <- Group $Group _fertilizer
16 water_fertilizer <- Group $Group_water_fertilizer
17 x1<-c(native, water, fertilizer, water_fertilizer)
18 x1
19 g <- factor (rep (1:4, c(6,6,6,6)),
20
              labels = c("native",
                          "water",
21
22
                          "fertilizer",
                          "water_fertilizer"))
23
24 kruskal.test(x1, g)
25
26
     The observed K value is 16.77 and the critical is
27 #
       11.3449.
28 # Because the observed value is greater than the
      table value, the null hypothesis
29 # is rejected. There is a signi???cant difference in
```

R code Exa 17.5 FRIEDMAN TEST

```
1 # FRIEDMAN TEST :
3 Brand <- matrix(c</pre>
     2,3,4,5,1,2,4,5,3,1,3,5,4,2,1),
4
5
             nrow=10, ncol=5, byrow = TRUE
6 Brand
8 \# Chi-square value, alpha =0.01:
9 \text{ qchisq}(.99, df=4)
10
11 # observed value :
12 friedman.test(Brand)
13
14 # Because the observed value of = 3.68 is not
     greater than the critical value, 13.2767,
15 # the researchers fail to reject the null hypothesis
```

R code Exa 17.6 SPEARMANS RANK CORRELATION

```
5 Crude_rank \leftarrow c(3,1,2,4,5,6,8,9,7)
6 Gasoline_rank <-c(1,2.5,4,2.5,5,6,8,9,7)
7 d < c(2,-1.5,-2,1.5,0,0,0,0,0)
8 d_sq \leftarrow c(4,2.25,4,2.25,0,0,0,0,0)
9 oil <- data.frame(Crude_oil,Gasoline,Crude_rank,
      Gasoline_rank,d,d_sq)
10 oil
11 d_sq_sum <- sum(d_sq)
12 d_sq_sum
13
14 # Using cor.test:
15 # install.packages("stats")
16 library(stats)
17 cor.test(oil$Crude_oil, oil$Gasoline, method = "
      spearman")
18
19 # using formula :
20 \, \text{n} = 9
21 r_s \leftarrow 1 - ((6*d_sq_sum)/(n*(n^2-1)))
22 \text{ r}_{\text{s}}
23
24
25 # A high positive correlation is computed between
      the price of a barrel of
26 # West Texas intermediate crude and a gallon of
      regular unleaded gasoline.
```