### Scilab Textbook Companion for Signals And Systems by I. J. Nagrath, S. N. Sharan And R. Ranjan<sup>1</sup>

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# **Book Description**

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

**Eqn** Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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## Chapter 1

# Introduction to Signal and Systems

Scilab code Exa 1.6 Shifting Scaling Time Reversal

```
1 //shifting and scaling
\frac{2}{2} / \text{Ex} \ 1.6
3 clear all;
4 clc;
5 close;
6 t = 0:1/100:2;
7 	ext{ for } i = 1: length(t)
       if t(i)<1 then
          x(i) = (2)*t(i);
9
             else
10
             x(i) = 2;
11
12
        end
13 end
14 for i = length(t)+1:2*length(t)
15 x(i) = 0;
16 \text{ end}
17 t1=0:1/100:4.01;
18 figure
19 subplot (3,1,1), plot2d(t1,x)
```

```
20 a=gca();
21 t2=t1-1;
22 subplot(3,1,2),plot2d(t2,x)
23 xtitle('x(t+1)')
24 a.y_location='origin'
25 \ a = gca();
26 subplot(3,1,3),plot2d(t1/1.5,x)
27 xtitle('x(1.5t)')
28 figure
29 a=gca();
30 subplot(2,1,1),plot2d((t2/1.5),x)
31 xtitle('x(1.5t+1)')
32 a.y_location='origin'
33 \ a = gca();
34 t3 = -3:1/100:1.01;
35 subplot(2,1,2),plot2d(t3,x($:-1:1))
36 xtitle('x(-t+1)')
37 a.y_location = 'origin';
```

### Scilab code Exa 1.9 Check for Periodicity

```
1 //Ex 1.9
2 //Check For periodicity
3 clc;
4 //pi=22/7
5 k=1;
6 N=2*7*k/5;
7 z=2*N;
8 n=0:.1:z //Defining discrete time
```

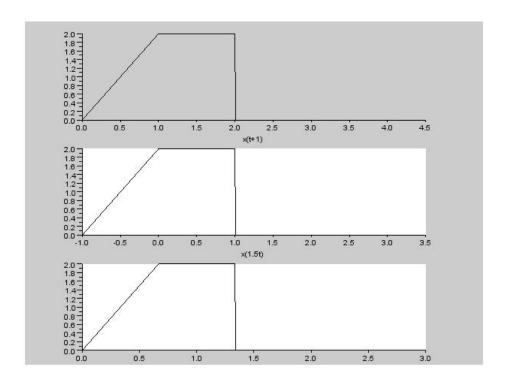


Figure 1.1: Shifting Scaling Time Reversal

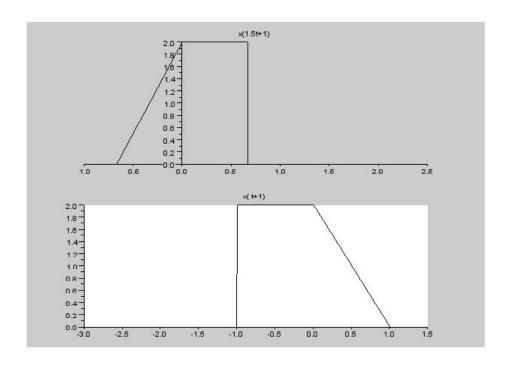


Figure 1.2: Shifting Scaling Time Reversal

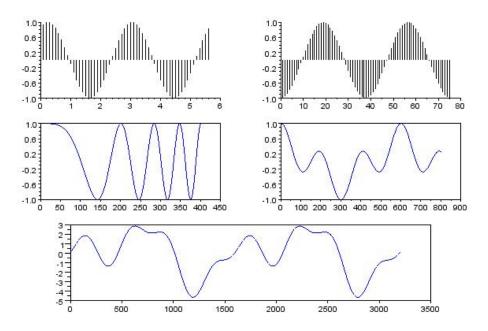


Figure 1.3: Check for Periodicity

```
9 x=sin((5*\%pi*n/7)+1); //sinusoid function
10 subplot(3,2,1), plot2d3(n,x) // ploting the sinusoid
      showing it as periodic 2pik=5piN/7
11 disp('the plot shows the above signal is periodic');
12
13 k=1;
14 N = 2 * \%pi * k * 6;
15 z=2*N;
16 n=0:1:z // Defining discrete time
17 x = \cos((n/6) - \%pi);
18 subplot(3,2,2), plot2d3(n,x); // the plot shows the
      above signal is periodic
  disp('the plot shows the above signal is periodic');
19
20
21 k = 1;
22 N = sqrt(2*k*2);
23 z = 2 * N;
24 n=0:1/100:z // Defining discrete time
25 x = \cos(((n.^2)*\%pi)/2);
```

```
26 subplot(3,2,3),plot(x);//the plot shows that the
      above signal is not periodic
27 disp ('the plot shows the above signal is not
      periodic');
28
29 k=1;
30 N = 2 * k;
31 z=2*N;
32 n=0:1/100:2*z //Defining discrete time
33 x = \cos(n*\%pi/3).*\cos(2*\%pi*n/3);
34 subplot (3,2,4), plot (x); // the plot shows that the
      above signal is periodic
35 disp('the plot shows the above signal is periodic');
36
37 k = 1;
38 N = 2 * k * 8;
39 z = 2 * N;
40 n=0:1/100:z //Defining discrete time
41 x=2*\cos(n*\%pi/4)+\sin((n*\%pi/2)-(\%pi/3))-2*\cos((n*\%pi/2))
      /8) + (\%pi/3));
42 subplot (3,1,3), plot (x); // the plot shows that the
      above signal is periodic
43 disp('the plot shows the above signal is periodic');
```

#### Scilab code Exa 1.11 Check for Periodicity

```
1 //Ex 1.11
2 //Check for peridicity
3 clc;
4 T=2*%pi/8;
5 z=2*T;
6 t=0:0.001:z
7 x=%i*exp(%i*8*t);
```

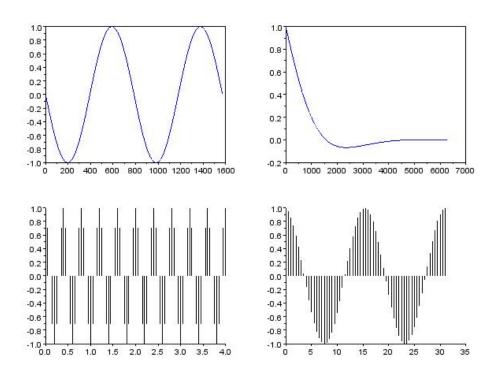


Figure 1.4: Check for Periodicity

```
8 subplot(2,2,1), plot(x); // the plot shows that the
      above signal is periodic
9
10 T=2*\%pi/(-1+\%i);
11 z=2*T;
12 disp('T cannot be complex so non periodic');
13 t=0:-0.001:z
14 x = \exp((-1 + \%i) * abs(t));
15 subplot(2,2,2), plot(x); //the plot shows that the
      above signal is not periodic
16
17 N=2*\%pi/\%pi;
18 z = 2 * N;
19 \quad n=0:0.05:z
20 x = exp(\%i*5*\%pi*n); //exp(i*(4*pi+pi)*n) = exp(i*pi*n)
21 subplot(2,2,3), plot2d3(n,x); //the plot shows that
      the above signal is periodic
22
23 k = 1;
24 N = 2 * \%pi * 5/2;
25 z = 2 * N;
26 n = 0:0.5:z
27 x = \exp((\%i * 2/5) * (n + (1/3)));
28 subplot(2,2,4), plot2d3(n,x); // the plot shows that
      the above signal is periodic
```

### Scilab code Exa 1.13 Check for Periodicity

```
1 //Ex 1.13
2 //Check for periodicity
3 clc;
4 T=2*%pi/6;
5 t=0:0.001:T*2
```

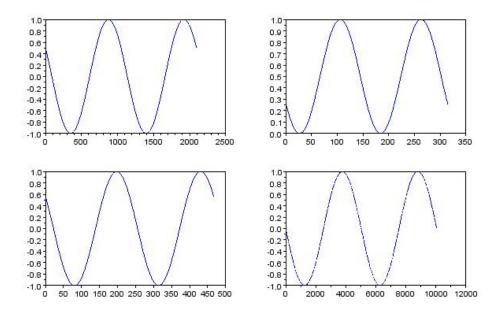


Figure 1.5: Check for Periodicity

```
6 x = \cos((6*t) + \%pi/3);
7 subplot(3,2,1),plot(x);
8 disp('the plot shows that the above signal is
      periodic');
9
10 T=2*\%pi/(\%i*\%pi);
11 t=0:0.001:T*2
12 x = \exp(\%i * (\%pi * abs(t-1))); //\exp(\%i * (\%pi * t-1)) = \exp(\%i *
      %pi*t)/exp(%i)
  //since the period is a complex no so non periodic
14 disp('T cannot be complex so non periodic T=2*%pi/(
      %i*%pi)');
15
16 / \text{pi} = 22/7
17 T=2*%pi/4;//calc the fundamental period
18 z=2*T;
19 t = 0:1/100:z
20 x=(\cos(2*t+\%pi/3))^2; //sinusoid function
21 subplot(3,2,2),plot(x)
```

```
22 disp('the plot shows that the above signal is
      periodic');
23
24 k = 1;
25 N=2*k*7/6;
26 z = 2 * N;
27 n=0:1/100:z
28 x = \cos((6*\%pi*n/7)+1);
29 subplot(3,2,3), plot(x); //the plot shows that the
      above signal is periodic
30 disp('the plot shows that the above signal is
      periodic');
31
32 k = 1;
33 N=2*\%pi*k*8;
34 z = 2 * N;
35 n=0:1/100:z
36 x = \sin((n/8) - \%pi);
37 subplot(3,2,4), plot(x); //the plot shows that the
      above signal is periodic
38 disp('the plot shows that the above signal is
      periodic');
39
40 k = 1;
41 N=2*k*12; //2*\cos(n*\%pi/4).*\cos(n*\%pi/3)=\cos(7*n*\%pi
      /12)-cos (n*%pi/12)
42 z = 2 * N;
43 \quad n=0:1/100:z
44 x=2*\cos(n*\%pi/4).*\cos(n*\%pi/3);
45 subplot(3,1,3), plot(x); //the plot shows that the
      above signal is periodic
46 disp('the plot shows the above signal is periodic');
```

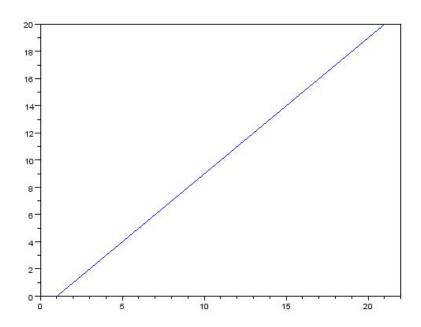


Figure 1.6: Integral of Unit step function

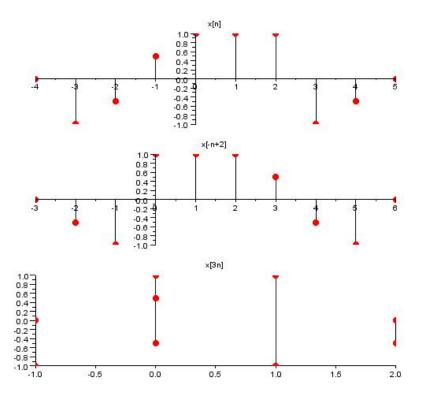


Figure 1.7: Shifting Time Reversal of discrete time signals

### Scilab code Exa 1.30 Integral of Unit step function

```
1 //Ex 1.30
2 //Integral of unit step function
3 clc;
4 x0=0;//lower bound
5 x1=0:20;//upper bound vector
6 X=integrate('1','x',x0,x1);
7 //integration of unt step seq
8 //resulting in ramp seq
9 plot(X)
```

### Scilab code Exa 1.37 Shifting Time Reversal of discrete time signals

```
1 //Ex 1.37
2 //shifting and scaling discrete signals
3 clear;
4 clc;
5 close;
6 t = -4:5;
7 x = [0 -1 -.5 .5 1 1 1 -1 -.5 0]
8 a=gca();
9 subplot(3,1,1),plot2d3(t,x)
10 subplot(3,1,1),plot(t,x,'r.')
11 xtitle('x[n]')
12 a.x_location='origin';
13 a.y_location='origin';
14
15 \text{ t1} = -5:4;
16 t2=t1+2;
17 a=gca();
18 subplot(3,1,2),plot2d3(t2,x($:-1:1))
19 subplot(3,1,2),plot(t2,x($:-1:1),'r.')
20 xtitle('x[-n+2]')
21
22 a = gca()
23 subplot(3,1,3),plot2d3(ceil(t/3),x)
24 subplot(3,1,3), plot(ceil(t/3),x,'r.')
25 xtitle('x[3n]')
26 a.x_location='origin';
27 a.y_location='origin';
```

### Chapter 2

# Analysis of LTI continous time system

### Scilab code Exa 2.2 Convolution

```
1 / Ex 2.2
2 clc;
3 h = ones(1,10);
4 N2=0: length(h)-1;
5 a=0.5; //constant a>0
6 \text{ for } t=1:10
       x(t) = exp(-a*(t-1));
8 end
9 N1=0: length(x)-1;
10 y = convol(x,h) - 1;
11 N=0: length(x) + length(h) - 2;
12
13 subplot(3,1,1),plot2d(N2,h)
14 xtitle('Impulse Response', 't', 'h(t)');
15
16 subplot (3,1,2), plot2d(N1,x)
17 xtitle('Input Response', 't', 'x(t)');
```

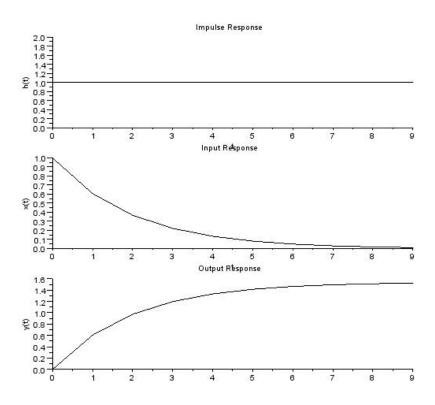


Figure 2.1: Convolution

```
18

19

20 subplot(3,1,3),plot2d(N(1:10),y(1:10))

21 xtitle('Output Response','t','y(t)');
```

Scilab code Exa 2.11.a Fourier transform of impulse function

```
//Fourier Transform of unit impulse
clc;
syms s t
X=symsum(1*%e^(-s*t),t,0,0);
```

Scilab code Exa 2.11.b Fourier transform of exponential function

```
1 clc;
2 A = 1;
3 \text{ Dt} = 0.005;
4 t=-4.5:Dt:4.5;
5 \text{ xt} = \exp(-A*abs(t));
6 Wmax=2*%pi*1;
7 \text{ K} = 4;
8 k=0:(K/1000):K;
9 W=k*Wmax/K;
10 XW=xt*exp(-sqrt(-1)*t'*W)*Dt;
11 XW = real (XW);
12 W=[-mtlb_fliplr(W),W(2:1001)];
13 XW=[mtlb_fliplr(XW), XW(2:1001)];
14 subplot(1,1,1)
15 subplot(2,1,1);
16 a=gca();
17 a.y_location="origin";
```

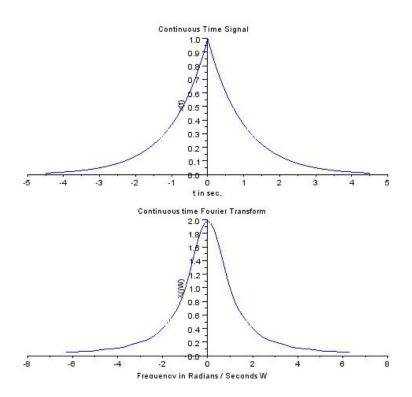


Figure 2.2: Fourier transform of exponential function

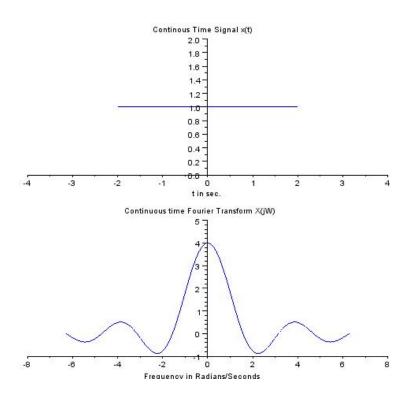


Figure 2.3: Fourier transform of Gate function

```
18 plot(t,xt);
19 xlabel('t in sec.');
20 ylabel('x(t)')
21 title('Continuous Time Signal')
22 subplot(2,1,2);
23 a=gca();
24 a.y_location="origin";
25 plot(W,XW);
26 xlabel('Frequency in Radians / Seconds W');
27 ylabel('X(jW)')
28 title('Continuous time Fourier Transform')
```

#### Scilab code Exa 2.12 Fourier transform of Gate function

```
1 //Ex 2.12
2 clc;
3 clear;
4 \quad A = 1;
5 Dt = 0.005;
6 T1 = 4;
7 t=-T1/2:Dt:T1/2;
8 for i=1:length(t)
9 xt(i)=A;
10 \text{ end}
11 Wmax=2*%pi*1;
12 K = 4;
13 k=0:(K/1000):K;
14 W=k*Wmax/K;
15 xt=xt';
16 XW=xt*exp(-sqrt(-1)*t'*W)*Dt;
17 XW_Mag=real(XW);
18 W=[-mtlb_fliplr(W),W(2:1001)];
19 XW_Mag=[mtlb_fliplr(XW_Mag), XW_Mag(2:1001)];
20 subplot(2,1,1);
21 a=gca();
22 a.data_bounds=[-4,0;4,2];
23 a.y_location="origin";
24 plot(t,xt);
25 xlabel('t in sec.');
26 title('Continous Time Signal x(t)');
27 subplot(2,1,2);
28 a=gca();
29 a.y_location="origin";
30 plot(W,XW_Mag);
31 xlabel('Frequency in Radians/Seconds');
32 title('Continuous time Fourier Transform X(jW)');
```

#### Scilab code Exa 2.14 Fourier transform one sided exponential function

```
1 //Ex 2.14
2 //Fourier Transform
3 clc;
4 clear;
5 A = 1;
6 Dt = 0.005;
7 t=0:Dt:10;
8 xt = exp(-A*t);
9 Wmax = 2 * \%pi * 1;
10 K = 4;
11 k=0:(K/1000):K;
12 W=k*Wmax/K;
13 XW=xt*exp(-sqrt(-1)*t'*W)*Dt;
14 XW_Mag=abs(XW);
15 W=[-mtlb_fliplr(W),W(2:1001)];
16 XW_Mag=[mtlb_fliplr(XW_Mag), XW_Mag(2:1001)];
17 [XW_Phase,db]=phasemag(XW);
18 XW_Phase=[-mtlb_fliplr(XW_Phase), XW_Phase(2:1001)];
19 figure
20 \quad a = gca();
21 a.y_location="origin";
22 plot(t,xt);
23 xlabel('t in sec.');
24 ylabel('x(t)');
25 title ('Continuous Time Signal');
26 figure
27 subplot(2,1,1);
28 \quad a = gca();
29 a.y_location="origin";
30 plot(W, XW_Mag);
31 xlabel('Frequency in Radians/Seconds>W');
32 ylabel('abs(X(jW))');
33 title('Magnitude Response (CTFT)');
34 subplot (2,1,2);
35 \quad a=gca();
36 a.y_location="origin";
```

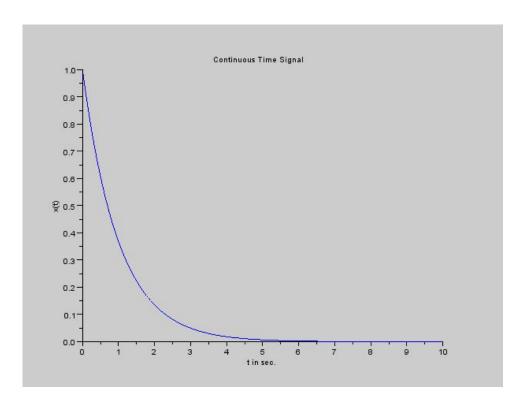


Figure 2.4: Fourier transform one sided exponential function

```
37 a.x_location="origin";
38 plot(W,XW_Phase*%pi/180);
39 xlabel('Frequency in Radians/Seconds');
40 ylabel('<X(jW)')
41 title('Phase Response (CTFT) in Radians');</pre>
```

Scilab code Exa 2.20.a Laplace transform of unit impulse

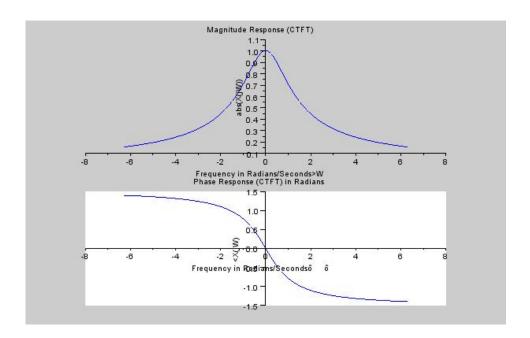


Figure 2.5: Fourier transform one sided exponential function

```
1 //laplace of unit impulse
2 clc;
3 syms s;
4 X=symsum(1*%e^(-s*t),t,0,0);
```

### Scilab code Exa 2.23 Laplace Transform

```
1 syms a t;
2 x=exp(-a*t);
3 y=diff(x,t)
4 X=laplace(y);
```

Scilab code Exa 2.26.a Inv Laplace

```
1 syms s;
2 x=ilaplace((s^2+2*s+1)/(s*(s+2)*(s+1)));
3 disp (x);
```

### Scilab code Exa 2.26.b Inv Laplace

```
1 syms s;
2 x=ilaplace((2*s+3)/((s^2+4*s+5)*(s+1)));
3 disp (x);
```

### Scilab code Exa 2.26.c Inv Laplace

```
1 syms s;
2 x=ilaplace(1/((s^2)*(s+1)));
3 disp (x);
```

### Scilab code Exa 2.28 Laplace Transform

```
1 clc;
2 syms s;
3 X=5/((s+2)*(s-3));
4 x=ilaplace(X);
```

Scilab code Exa 2.33 Plot the spectrum

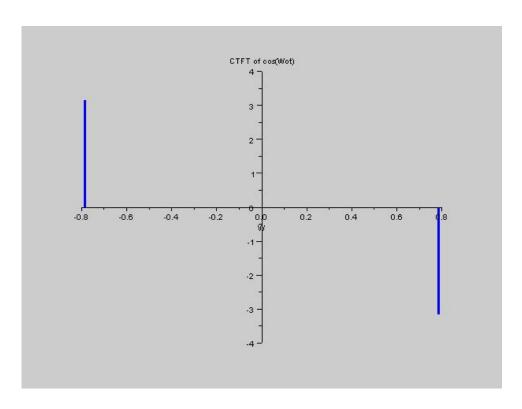


Figure 2.6: Plot the spectrum

```
1 / Ex 2.33
2 clc;
3 clear;
4 T1=2;
5 T=4*T1;
6 Wo=2*\%pi/T;
7 W = [-Wo, 0, Wo];
8 ak=(2*%pi*Wo*T1/%pi)/sqrt(-1);
9 \text{ XW=} [-ak, 0, ak];
10 ak1 = -(2*\%pi*Wo*T1/\%pi);
11 XW1 = [-ak1, 0, ak1];
12 figure
13 a=gca();
14 a.y_location="origin";
15 a.x_location="origin";
16 plot2d3('gnn',W,XW1,2);
17 poly1=a.children(1).children(1);
18 poly1.thickness=3;
19 xlabel('W');
20 title('CTFT of cos(Wot)');
```

### Scilab code Exa 2.39 Convolution of two signals

```
1 //Ex 2.39
2 clc;
3 clear;
4 A=1;
5 Dt=0.005;
6 T1=1;
7 t=-T1:Dt:T1;
8 for i=1:length(t)
9 xt(i)=A;
10 end
```

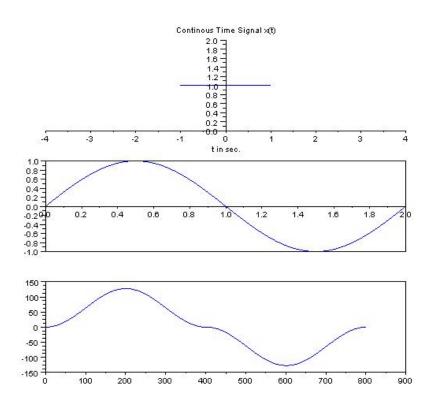


Figure 2.7: Convolution of two signals

```
11 xt=xt';
12 t1=0:0.005:2;
13 for j=1:length(t1)
    x1(j)=sin(%pi*t1(j));
14
15 end
16 subplot(3,1,1);
17 a=gca();
18 a.data_bounds=[-4,0;4,2];
19 a.y_location="origin";
20 plot(t,xt);
21 xlabel('t in sec.');
22 title('Continous Time Signal x(t)');
23 subplot(3,1,2);
24 a=gca();
25 plot(t1,x1);
26 y = convol(x1,xt);
27 subplot(3,1,3);
28 a.y_location="origin";
29 a.x_location="origin";
30 plot(y);
```

### Chapter 3

# Analysis of LTI Discrete time system

Scilab code Exa 3.1 Convolution sum method

```
1 clc;
2 //k=2;
3 r=1;
4 k=0:1:2;
5 h=0.5^(k);
6 l1=convol(h,r);
7 disp(l1);
8 //k=3;
9 r=1;
10 k=0:1:3;
11 h=0.5^(k);
12 l2=convol(h,r);
13 disp(l2);
```

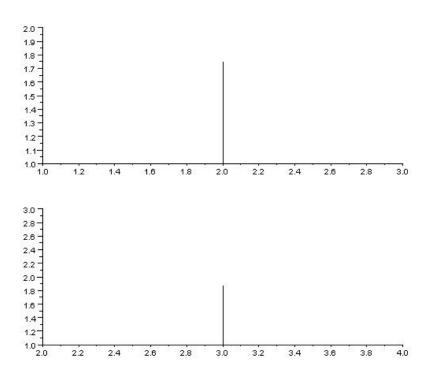


Figure 3.1: Graphical Convolution

### Scilab code Exa 3.2 Graphical Convolution

```
1 clc;
2 / k = 2;
3 r=1;
4 k=0:1:2;
5 h=0.5^{(k)};
6 \quad 11 = convol(h,r);
7 s1 = sum(11);
8 disp(s1);
9 n=2;
10 subplot(2,1,1),plot2d3(n,s1);
11 / k = 3;
12 r=1;
13 k=0:1:3;
14 h=0.5^(k);
15 12=convol(h,r);
16 \text{ s2=sum}(12);
17 disp(s2);
18 m=3;
19 subplot(2,1,2),plot2d3(m,s2);
```

### Scilab code Exa 3.17.b Z Transform

```
1 //Ex 3.17b
2 clc;
3 syms z n;
4 x=1;
5 X=symsum(x*z^(-n),n,0,%inf);
6 disp(X);
```

Scilab code Exa 3.17.c Z Transform

```
1 //Ex 3.17c
2 clc;
3 syms z n B k;
4 x=exp(B*k);
5 X=symsum(x*z^(-n),n,0,%inf);
6 disp(X);
```

### Scilab code Exa 3.17a Z Transform

```
1 //Ex 3.17a
2 clc;
3 syms z n;
4 x=1;
5 X=symsum(x*z^(-n),n,0,0);
6 disp(X);
```

### Scilab code Exa 3.19 Final Value Theorem

```
1 //Ex 3.19
2 clc;
3 syms z;
4 c=(z-1)/(1+0.5*z^(-1))+(z^(-1)*(z-1))/((1+0.5*z^(-1)));
5 l=limit(c,z,1);
6 disp(1);
```

### Scilab code Exa 3.21 Inverse Ztransform

```
1 //Ex 3.21
2 clc;
```

```
3 z=%z;
4 x=ldiv(z^2,(z^3)-(1.7*(z^2))+0.8*z+0.1,3);
5 dims=1;
6 xo=[0];
7 y=cat(dims,xo,x);
8 //degree of Num polynomial And Den Polynomial must be same
9 // else Zeros are padded accordingly on the basis of Std Eq.
10 disp(y);
```

### Scilab code Exa 3.22 Z inverse

```
1 //Ex 2.22a
2 clc;
3 z=%z;
4 x=ldiv(z,z-0.4,4);
5 disp(x);
```

# Discrete Fourier Transform And Fast Fourier Transform

### Scilab code Exa 4.4 DFT computation

### Scilab code Exa 4.5 DFT computation

```
1 clc;
2 clear;
3 N1=8;
4 n=-N1:N1;
5 for i=1:length(n)
6     x(i)=1;
7 end
```

```
8 X = fft(x,-1);
```

### Scilab code Exa 4.6 DFT computation

```
1 clc;
2 clear;
3 Wo=2*%pi/3;
4 n=-8:8;
5 for i=1:length(n)
6     x(i)=cos(Wo*n(i));
7 end
8 X=fft(x,-1);
```

## Scilab code Exa 4.9 DFT computation

```
1 clc;
2 clear;
3 a=0.5;
4 b=0.25;
5 n = -10:10;
6 for i=1:length(n)
       if n(i)<0 then
7
8
            x(i)=0;
            h(i)=0;
9
10
       else
11
            x(i)=b^n(i);
            h(i)=a^n(i);
12
13
       end
14 end
15 y = convol(x,h);
16 \text{ n1} = -20:20;
17 plot2d3(n1,y)
```

### Scilab code Exa 4.28 Circular convolution

```
1 //Ex 4.28
2 clc;
3 f1=[2,1,2,1];
4 f2=[1,2,3,4];
5 F1=fft(f1,-1);
6 F2=fft(f2,-1);
7 F=F1.*F2;
8 f=fft(F,1);
```

### Scilab code Exa 4.29 Record Length

```
1 //Ex 4.29
2 clc;
3 fm=500;
4 fs=2*fm;
5 T=1/fs;
6 df=10;
7 N=2*fm/df;
8 rl=N*T;
9 disp(rl, 'Record Length');
10 sl=0.05;
11 zp=rl-sl;
12 disp(zp, 'Zero padding required');
```

Scilab code Exa 4.31 Sampling rate and DFT size

```
1 / Ex 4.31
```

```
2 clc;
3 fm=10*10^3;
4 df=100;
5 N=2*fm/df;
6 l=log2(N);
7 l1=ceil(l);
8 N1=2^l1;
9 fs=N1*df;
10 disp(fs, 'Required Sampling Freq');
```

### Scilab code Exa 4.32 DFT computation

```
1 //Ex 4.32
2 clc;
3 clear;
4 f=[0 1 1 1 0 0];
5 F=fft(f,-1);
```

# Sampling

Scilab code Exa 5.1 Minimum Sampling Frequency

```
1 //Ex 5.1
2 clc;
3 fmax=30;
4 fmin=20;
5 BW=fmax-fmin;
6 disp(BW, 'Bandwidth (kHz)');
7 mFs=2*BW;
8 disp(mFs, 'Minimum Sampling Frequency (kHz)');
```

Scilab code Exa 5.2.a Minimum Sampling Interval

```
1 //Ex 5.2a
2 clc;
3 syms T;
4 disp('x(t)=1+cos(20%pi*t)');
5 w=20*%pi;
6 f=w/(2*%pi);
7 T=1/(2*f);
8 disp(T, 'minimum sampling interval');
```

### Scilab code Exa 5.2.b Minimum Sampling Interval

```
1  //Ex 5.2b
2  clc;
3  disp('x(t)=(1/2%pi*t)[sin(31%pi*t)-sin(29%pi*t)]');
4  w1=31*%pi;
5  f1=w1/(2*%pi);
6  w2=29*%pi;
7  f2=w2/(2*%pi);
8  if f1<f2 then
9    T=1/(2*f2);
10 else
11    T=1/(2*f1);
12 end
13 disp(T, 'minimum sampling interval');</pre>
```

### Scilab code Exa 5.6 Continuous time Frequency

```
1 //Ex 5.6
2 clc;
3 ws=1000*%pi;
4 w=ws/2;
5 disp(w,'Cont. time Frequency w ( rad/seconed )');
```

### Scilab code Exa 5.9 Aliasing

```
1 //Ex 5.9
2 clc;
3 disp('x(t)=cos(200%pi*t+theta)');
```

```
4 w=200*%pi;
5 f=w/(2*%pi);
6 nyquist_rate=2*f;
7 disp(nyquist_rate,'Minimum sampling frequency to avoid aliasing is');
```

### Scilab code Exa 5.12 Find the frequency

```
1 omega=%pi/4;
2 T=10^(-3)
3 w=omega/T;
4 disp(w)
```

### Scilab code Exa 5.14 Sampling period

```
1 [N,kerA]=linsolve(5*%pi/9,-2*%pi);
2 N1=floor(N);
3 disp(N1);
```

## Transformed Networks

Scilab code Exa 6.1 Current flowing in a network

```
1 //Ex 6.1
2 clc;
3 syms s;
4 v=10;
5 R=4;
6 L=2;
7 C=0.125;
8 V=laplace(v);
9 I=V/(R+L*s+(1/(C*s)));
10 i=ilaplace(I);
11 disp(i, 'i(t)=');
```

Scilab code Exa 6.2 voltage across inductor

```
1 //Ex 6.2
2 clc;
3 syms s;
4 i=4;
```

```
5 R=13/4;
6 L=1;
7 C=1/13;
8 I=laplace(i)+1;
9 Y=1/R+s/13+1/s;
10 V=I/Y;
11 v=ilaplace(V);
12 disp(v,'v(t)=');
```

### Scilab code Exa 6.3 voltage across capacitor

```
1 //Ex 6.3
2 clc;
3 syms s;
4 i=5;
5 R=2;
6 L=1;
7 C=1/2;
8 Z=((R+L*s)*(1/(C*s)))/((R+L*s)+(1/(C*s)));
9 V=Z*i;
10 v=ilaplace(V);
11 disp(v,'v(t)=');
```

### Scilab code Exa 6.9 Bode Plot

```
1 //Ex 6.9
2 //Obtain the Bode plot
3 clc;
4 s=poly(0,'s');
5 H=syslin('c',8*(1+.1*s)/(s*(1+.5*s)*(1+.6*s/50+(s/50)^2)));
```

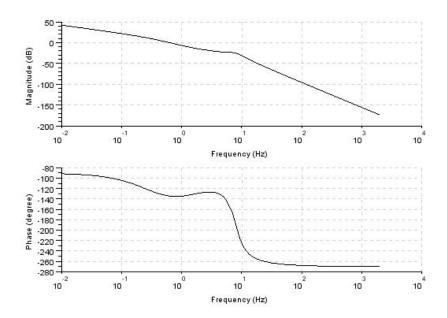


Figure 6.1: Bode Plot

```
6 bode(H,0.01,2000);
```

### Scilab code Exa 6.10 Bode Plot

```
1 //Ex 6.10
2 //Obtain the Bode plot
3 clc;
4 H=syslin('c',10*(1+%s/2)/(%s*(1+%s/.1)*(1+%s/.5)*(1+%s/10)));
5 bode(H,0.01,100);
```

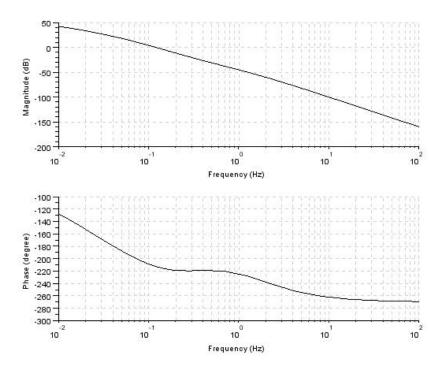


Figure 6.2: Bode Plot

# State Space Analysis

### Scilab code Exa 7.1 State Space Representation

```
1 clc;
2 close
3 clear;
4 s=%s;
5 tf=syslin('c',((s+3)/(s^3+5*s^2+8*s+3)));
6 ss=tf2ss(tf);
7 disp(ss)
```

### Scilab code Exa 7.2 State Space Representation

```
1 clc;
2 close
3 clear;
4 s=%s;
5 tf=syslin('c',((s+3)/((s+2)^2*(s+1))));
6 ss=tf2ss(tf);
7 disp(ss)
```

# Stability Analysis of LTI Systems

### Scilab code Exa 8.1.a check for HURWITZ

```
1
        clc;
2
        // Define the polynomial
       s=poly(0,"s");
3
       p=10+9*s+4*s^2+s^3;
4
5
        [C] = coeff(p);
6
        11=length(C);
7
       x = 0;
8
        for i1=1:11
            r1=C(1,i1);
9
            r1=real(a1);
10
11
            if r1>0 then
12
                 x = x + 1;
13
            end
14
        end
        if(x==11) then
15
            [S]=roots(p);
16
            disp(S,"Roots=");
17
            l=length(S);
18
19
            c=0;
```

```
20
            for i=1:1
                a=S(i,1);
21
22
                r=real(a);
                if r<0 then
23
24
                     c=c+1;
25
                end
26
            end
            if(c==1) then
27
                printf("Polynomial is Hurwitz");
28
29
            else
                printf("Polynomial is non-Hurwitz");
30
31
            end
32
       else
            printf("Polynomial is non-Hurwitz");
33
34
       end
```

#### Scilab code Exa 8.1.b check for HURWITZ

```
1
       clc;
2
        // Define the polynomial
       s=poly(0,"s");
3
       p=30+4*s+s^2+s^3;
4
       [C] = coeff(p);
5
       11=length(C);
6
7
       x = 0;
       for i1=1:11
8
9
            a1=C(1,i1);
            r1=real(a1);
10
11
            if r1>0
12
                 x=x+1;
13
            end
14
       end
       if(x==11) then
15
16
            [S]=roots(p);
            disp(S,"Roots=");
17
```

```
l=length(S);
18
19
            c=0;
            for i=1:1
20
                a=S(i,1);
21
22
                r=real(a);
23
                 if r < 0 then
24
                     c=c+1;
25
                 end
26
            end
27
            if(c==1) then
                 printf("Polynomial is Hurwitz");
28
29
                printf("Polynomial is non-Hurwitz");
30
31
            end
32
       else
            printf("Polynomial is non-Hurwitz");
33
34
       end
```

### Scilab code Exa 8.2 checking stability

```
1
       clc;
       // Define the polynomial
2
       s=poly(0,"s");
3
       p=5+3*s+2*s^2+2*s^3+s^4+s^5;
4
       // Calculate the routh of above polynomial
5
       r=routh_t(p);
6
7
       A = r(:,1);
8
       c = 0;
9
       x=0;
       for i=1:6
10
            x=A(i,1);
11
            if x <> 0
12
13
                 c=c+1;
14
                 end
15
       end
```

```
if(c>=1) then
printf("system is unstable");
else
printf("system is stable");
end
```

### Scilab code Exa 8.3 checking stability

```
1
       clc;
2
       // Define the polynomial
3
       s=poly(0,"s");
       p=2+2*s+5*s^2+4*s^3+4*s^4+2*s^5+s^6;
4
5
       // Calculate the routh of above polynomial
6
       r=routh_t(p);
       S=roots(p);
       disp(r, "Routh array=");
8
9
       disp(S,"Roots=");
10
       A = r(:,1);
       c=0;
11
12
       x = 0;
13
       for i=1:6
            x = A(i, 1);
14
15
            if x < 0
16
                 c=c+1;
17
            end
18
        end
19
       if(c>=1) then
            printf("system is unstable");
20
21
       else
            l=length(S);
22
23
            c=0;
24
            for i=1:1
25
                a=S(i,1);
26
                r=real(a);
27
                 if r<0 then
```

```
28
                     c=c+1;
29
                 end
30
            end
            if c==0 then
31
               printf("system is stable");
32
33
            else
                 printf("system is unstable");
34
35
            end
36
37
       end
```

### Scilab code Exa 8.4 checking stability

```
1
       clc;
2
       // Define the polynomial
       s=poly(0,"s");
3
       p=1+2*s+5*s^2+5*s^3+2*s^4;
4
       // Calculate the routh of above polynomial
5
       r=routh_t(p);
6
7
       disp(r, "Routh array=");
8
       A = r(:,1);
       c=0;
9
10
       x1 = 0;
11
       eps=0;
       for i=1:5
12
13
            x1=A(i,1);
14
            if x1<0
15
                c=c+1;
16
            end
17
       end
       if(c>=1) then
18
            printf("system is unstable");
19
20
       else
            printf("system is stable");
21
22
       end
```

```
x = roots(p);
```

23

### Scilab code Exa 8.5 checking stability

```
1
       clc;
2
       // Define the polynomial
       s=poly(0,"s");
3
       p=36+12*s+12*s^2+3*s^3+s^4;
4
       // Calculate the routh of above polynomial
5
       r=routh_t(p);
6
       disp(r, "Routh array=");
7
       A = r(:,1);
8
9
       c=0;
10
       x = 0;
       for i=1:5
11
12
            x=A(i,1);
13
            if x < 0
14
                 c=c+1;
15
                 end
16
       end
       if(c>=1) then
17
            printf("system is unstable");
18
19
            printf("system is stable");
20
21
       end
22
       x = roots(p);
```

### Scilab code Exa 8.9 checking stability

```
1 clc;
2 // Define the polynomial
3 z=poly(0,"z");
4 p=5+3*z+2*z^2+2*z^3+z^4+z^5;
```

```
5 // Calculate the routh of above polynomial
6 r=routh_t(p);
```

### Scilab code Exa 8.11 Stability of discrete time system

```
1 clc;
2 // Define the polynomial
3 //z = poly(0, 'z');
4 //z^3 - 0.3*z^2 + .1*z - .1
5 / Put z = (1+r)/(1-r);
6 // Bilinear transformation
7 s=poly(0, 's');
8 p=.7+2.9*s+2.9*s^2+1.7*s^3;
9 // Calculate the routh of above polynomial
10 r=routh_t(p);
11 disp(r, "Routh array=");
12 A=r(:,1);
       c=0;
13
14
       x = 0;
15
       for i=1:3
16
            x = A(i, 1);
17
            if x < 0
18
                c=c+1;
19
            end
20
       end
       if(c>=1) then
21
            printf("system is unstable");
22
23
       else
24
            l=length(S);
            c=0;
25
            for i=1:1
26
                a=S(i,1);
27
28
                r=real(a);
29
                if r<0 then
30
                     c=c+1;
```

```
31
                end
32
           end
           if c==0 then
33
              printf("system is stable");
34
35
               printf("system is unstable");
36
           end
37
38
39
       end
```

# Analog and Digital Filter Design

### Scilab code Exa 9.1 BPF

```
1 / Ex 9.1
2 //Band pass Filter Design
3 / a
4 clc;
5 w1=10*10^3;
6 w2=15*10^3;
7 wot=sqrt(w1*w2);
8 wbt=w2-w1;
9 s = %s;
10 w = poly(0, 'w');
11 wt=poly(0,'wt');
12 wx = (wt^2 - wot^2) / (wbt*wt);
13 disp(w);
14 / b
15 / \text{Let } n=2
16 \text{ hb2=1/(s^2+sqrt(2)*s+1)};
17 hb21=horner(hb2,(%i*w));
18 disp(hb21);
19 hb22=horner(hb21,wx);
```

```
20 disp(hb22);
```

### Scilab code Exa 9.2 Band Stop Filter

```
1 / Ex 9.2
2 //Band Stop Filter Design
3 / a
4 clc;
5 \text{ w1} = 1200;
6 \text{ w2=2000};
7 s = %s;
8 \text{ w=poly}(0, 'w');
9 St=poly(0,'St');
10 wc=1; //For normalised Prototype
11 wd1t=poly(0,'wd1t');
12 \text{ wt1} = 2500;
13 wx1 = (wt1*(w2-w1)*wd1t)/(-wt1^2+w2*w1);
14 \text{ wt} 2 = 400;
15 wx2=(wt2*(w2-w1)*wd1t)/(-wt2^2+w2*w1);
16 disp(w);
17 wx=wx1; // required attenuation to less
            // \text{ than } -3 dB \text{ for } wx > -0.5195 wd1t
18
19 wd1t=wc/0.5195;
20 / b
21 // Let n=4
22 hb2=1/((s^2+.7654*s+1).*(s^2+1.8478*s+1));
23 hb21=horner(hb2,(%i*w));
24 disp(hb21);
25 hb22=horner(hb21,wx);
26 disp(hb22);
27 hb23=horner(hb22,-%i*St);
28 disp(hb23);
```

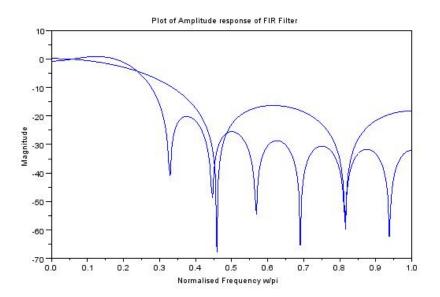


Figure 9.1: FIR Filter

### Scilab code Exa 9.3 FIR Filter

```
1  //Ex 9.3
2  //FIR Filter
3  close;
4  clc;
5  //Fourier series method
6  //for N=5
7  N=5;
8  U=3;
9  for n=-2+U:1:2+U
10  if n==3
11  hd(n)=0.25;
12  else
13  hd(n)=sin(%pi*(n-U)/4)/(%pi*(n-U));
```

```
14 end
15 end
16 [hzm ,fr] = frmag (hd ,256) ;
17 \text{ hzm\_dB} = 20* \frac{\log 10}{\log 10} \text{ (hzm)./ } \max \text{ (hzm);}
18 plot (2*fr , hzm_dB )
19
20 // for N=15
21 N = 15;
22 U=8;
23 for n = -7 + U : 1 : 7 + U
24
        if n==8
25
              hd(n) = 0.25;
26
         else
              hd(n) = sin(\%pi*(n-U)/4)/(\%pi*(n-U));
27
28
         end
29 end
30 [hzm, fr] = frmag (hd, 256);
31 \text{ hzm\_dB} = 20* \frac{\log 10}{\log 10} \text{ (hzm)./ } \max \text{ (hzm);}
32 plot (2*fr , hzm_dB )
33 xlabel('Normalised Frequency w/pi')
34 ylabel('Magnitude')
35 title('Plot of Amplitude response of FIR Filter')
```

#### Scilab code Exa 9.5 Low Pass Filter

```
1 //Ex 9.5
2 clc;
3 N=21;
4 U=11;
5 for n=-10+U:1:10+U
6 if n==11
7 hd(n)=0.25;
8 else
```

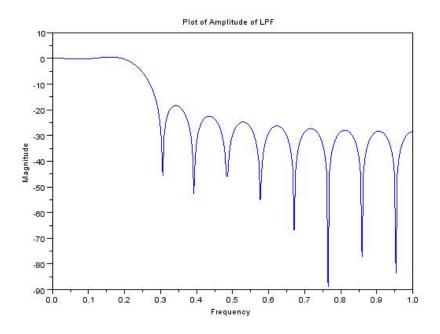


Figure 9.2: Low Pass Filter

```
9 hd(n)=(sin(%pi*(n-U)/4))/(%pi*(n-U));
10 end
11 end
12 [hzm ,fr ]= frmag (hd ,256);
13 hzm_dB = 20* log10 (hzm)./ max ( hzm );
14 plot (2*fr , hzm_dB );
15 xlabel ('Frequency');
16 ylabel ('Magnitude');
17 title('Plot of Amplitude of LPF')
```

### Scilab code Exa 9.7 2nd order Digital Butterworth Filter

```
1 //Ex 9.7
2 clc;
3 s=%s;
4 T=10^(-4);
5 wdc=2*%pi*10^3;
6 wac=2/T*tan(wdc*T/2);
7 HS=1/(s^2+sqrt(2)*s+1)//Transfer Function for N=1
8 HS1=horner(HS,s/wac);
9 disp(HS1,'Normalized Transfer Function, H(s) =');
10 z=%z;
11 HZ=horner(HS1,(2/T)*(z-1)/(z+1));
12 disp(HZ,'H(z) =');
```

# MATLAB Tools for Analysis of Signals and systems

Scilab code Exa 10.1 Solving Linear Equation

```
1 clc;
2 A=[2 1; 1 2]
3 B=[1; 0]
4 A=inv(A);
5 X=A*B;
```

Scilab code Exa 10.3 Find the step and impulse responce

```
1 clc;
2 s=poly(0,'s');
3 x=syslin('c',%s/(%s+2));
```

Scilab code Exa 10.9 Find the impulse responce

```
1 //Ex 10.9
2 //Impulse response
3 num=[1 3];
4 den=[1 3 2];
5 n=0:1:20;
6 x=[1 zeros(1,20)];
7 y=filter(num,den,x);
8 plot(n,y);
```

### Scilab code Exa 10.12 Find convolution and plot the result

```
1 //Ex 1012
2 // Convolution of two sequences
3 / [1 1 1 1 1]
4 / [1 \ 2 \ 3]
5 clc;
6 n1=0:1:4;
7 n2=0:1:2;
8 \quad x = [1 \quad 1 \quad 1 \quad 1 \quad 1]
9 h = [1 2 3]
10 y = convol(x,h);
11 l=length(y);
12 n3=0:1:1-1;
13 figure
14 title('Sequence x')
15 plot2d3(n1,x);
16 figure
17 title('Seequence h')
18 plot2d3(n2,h);
19 figure
20 title('Sequence y')
21 plot2d3(n3,y);
```

## Scilab code Exa $10.13\,$ Find the step response

```
1 //Ex 1013
2 //Convolution of two sequences
3 //To plot the step response
4 //[.25 .25 .25 .25]
5 / [.25 -.25 .25 -.25]
6 clc;
7 n1=0:1:8;
8 n2=0:1:8;
9 h1=[0 0 0 .25 .25 .25 .25 0 0]
10 h2=[0 0 0 .25 -.25 .25 -.25 0 0]
11 y = convol(h1, h2);
12 l=length(y);
13 n3=0:1:1-1;
14 figure
15 title('Sequence h1')
16 plot2d3(n1,h1);
17 figure
18 title('Seequence h2')
19 plot2d3(n2,h2);
20 figure
21 title('Sequence y')
22 plot2d3(n3,y);
```