## Scilab Textbook Companion for Data Structures Using C And C++ by Y. Langsam, M. Augenstein And A. M. Tenenbaum<sup>1</sup>

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# **Book Description**

 ${\bf Title:}\ \, {\rm Data}\ \, {\rm Structures}\ \, {\rm Using}\ \, {\rm C}\ \, {\rm And}\ \, {\rm C}{\rm +}{\rm +}$ 

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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## Chapter 1

## Introduction To Data Structures

Scilab code Exa 1.1 To calcualte Average And Deviation

```
1 //Solved Example 1
2 //:To calcualte Average And Deviation
3 function[avg]=average(a)
     i=1;
     [j,k]=size(a);
5
     j = 0;
    for i=1:k
8
       j=j+a(i);
9
     end
10
     avg=j/k;
11
     dev=0;
     disp(avg, "Average =");
12
13
     disp("The deviations are:");
14
    for i=1:k
15
       dev=a(i)-avg;
16
       disp(dev);
17
     end
18 endfunction
19 // Calling routine
```

```
20 a=[3 223 212 343]
21 avg=average(a)
```

#### Scilab code Exa 1.1.4 Decimal form of given no represented variably

```
1 //Exercise1.1 Example.1.1.4
2 //To calculate
                     Decimal No. of a given Number
3 //Treating them as i) Normal binary nos(ii) Twos
      complemented iii)BCD:
  function[c]=twos1(a1)
     [j1,i1] = size(a1)
5
6
     i4 = 1
7
     c=-(a1(i4)*2^(i1-1));
8
     i1=i1-1;
     while(i1>=1)
9
10
       i4 = i4 + 1;
       c=c+a1(i4)*2^(i1-1);
11
12
        i1=i1-1;
13
     end
14
     disp(a1," Decimal form of the Twos Complement
        Number");
     disp(c," is");
15
  endfunction
16
17
   function[d]=binary_dec(a2)
     [j2,i2] = size(a2);
18
     k = modulo(i2,4);
19
20
     d=0;
21
     if(k==0)
22
       e=i2/4;
23
        i3 = 1
       while(i3<=i2)</pre>
24
25
          1=3
         m = 0
26
27
          while (1>=0)
28
            m=m+(a2(i3)*2^1);
```

```
29
            1=1-1;
30
            i3=i3+1;
31
         end
32
         if(m>9)
33
            d = -1;
34
            disp("Cannot be coded in this form")
35
          break;
36
         end
37
         if(m \le 9)
            d=d+m*10^(e-1)
38
39
            e=e-1;
40
         end
41
       end
42
     end
     disp(a2, "Decimal form of BCD number");
43
     disp(d,"is");
44
45 endfunction
46 // Given Example:
47 //(A)
48 p1 = [1 0 0 1 1 0 0 1];
49 p2=base2dec(['10011001'],2)
50 p2=twos1(p1)
51 p2=binary_dec(p1)
52 //(b)
53 p3 = [1 0 0 1];
54 p4=base2dec(['1001'],2)
55 p4=twos1(p3)
56 p4=binary_dec(p3)
57 //(C)
58 p5 = [0 0 0 1 0 0 0 1 0 0 0 1];
59 p6=base2dec(['000100010001'],2)
60 p6=twos1(p5)
61 p6=binary_dec(p5)
62 // (d)
63 p7=[0 1 1 1 0 1 1 1];
64 p8=base2dec(['01110111'],2)
65 p8 = twos1(p7)
66 p8=binary_dec(p7)
```

```
67 //(e)

68 p9=[0 1 0 1 0 1 0 1];

69 p10=base2dec(['010101010'],2)

70 p10=twos1(p9)

71 p10=binary_dec(p9)

72 //(F)

73 p11=[1 0 0 0 0 0 0 1 0 1 0 1];

74 p12=base2dec(['100000010101'],2)

75 p12=twos1(p11)

76 p12=binary_dec(p11)
```

### Scilab code Exa 1.1.5 Add Substract And Multiply binary numbers

```
1 //Exercise 1.1 example 1.1.5
2 //Add, Substract And Multiply binary numbers
3 function[a] = add(b,c)
     d=base2dec(b,2)
     e=base2dec(c,2)
5
6
     a=d+e
     a=dec2bin(a)
     disp(a, "Result of addition")
9 endfunction
10 function[a]=subtract(b,c)
     d=base2dec(b,2)
11
12
     e=base2dec(c,2)
     a=d-e
13
14
     a=dec2bin(a)
     disp(a, "Result of subtraction")
15
16 endfunction
17 function[a]=multiply(b,c)
     d=base2dec(b,2)
18
19
     e=base2dec(c,2)
20
     a=d*e
21
     a=dec2bin(a)
     disp(a, "Result of multiplication");
22
```

```
23 endfunction

24 // Calling Routine:

25 b="11001";

26 c="10011";

27 a=add(b,c)

28 a=subtract(b,c)

29 a=multiply(b,c)
```

### Scilab code Exa 1.1.7 TO Convert Binary To Ternary

```
1 // Exercise 1.1 Example 1.1.7
2 //TO Convert Binary To Ternary
3 function[t]=bin_ter(a)
4
     b=0
5
     b=base2dec(a,2);
6
     disp(b);
     [j,i]=size(a);
8
     t = [];
9
     while (b^{-}=0)
       m = modulo(b,3);
10
11
       t=[t(:,:) m];
12
       b=b/3;
       b=b-modulo(b,10);
13
14
15
     disp(t, "Ternary Equivalent");
16 endfunction
17 // Calling Routine:
18 a="100101101110"
19 disp(a, "input string is");
20 b=bin_ter(a)
```

Scilab code Exa 1.2 String Manipulations

```
1 //Solved Example 2
2 //: String Manipulations
3 funcprot(0)
4 function[1]=strlen(str)
     i=1;
6
     1 = 0;
7
    [j,k]=size(str)
     for i=1:k
8
9
       l=l+length(str(i));
10
     disp(1, "string length is");
11
12 endfunction
13 // Calling Routine:
14 str="Hello World";
15 l=strlen(str)
16 function[c]=strcat1(a,b)
     disp(strcat([a b]), "After concatination");
17
     c=strcat([a b]);
18
19 endfunction
20 // Calling Routine:
21 a="hello";
22 b="world";
23 c=strcat1(a,b);
```

### Scilab code Exa 1.2.1 Calculate Median And Mode Of an Array

```
1  // Exercise Example 1.2.1
2  // Calculates Median And Mode Of an Array
3  //(A)
4  function[y]=median1(a)
5    p=mtlb_sort(a);
6    [j,i]=size(a);
7    y=0
8    j=modulo(i,2);
9    if(j==0)
```

```
y=((a(i/2)+a(i/2+1))/2);
10
11
     end
     if(j==1)
12
        i=i/2;
13
14
        i=i-modulo(i,10);
15
        y=a(i+1);
16
     end
     disp(y, "median is");
17
18 endfunction
19 //(B)
20 function[z]=mode1(a)
21
     p=mtlb_sort(a);
22
     disp(p)
     q=1;
23
24
     r=1;
25
     i=1;
26
     [j,i1]=size(a);
27
     if(i1>1)
28
        for i=1:i1-1
          if (p(i)~=p(i+1))
29
30
          q = [q(:,:) i+1];
31
          r=[r(:,:) 1];
32
          else
33
            [c,d]=size(r);
34
            r(d)=r(d)+1;
35
          end
36
        end
        q1=mtlb_sort(r);
37
38
        [j,i1]=size(q1)
39
        if (q1(i1-1) == q1(i1))
40
          z = -1;
          disp("Mode does not exist");
41
42
          break;
43
          else
            c=q1(i1);
44
45
            k=1;
46
            while (r(k)^=c)
              k=k+1;
47
```

```
48
            end
            z=p(q(k));
49
50
          end
51
       end
52
       if (i1==1)
53
          z=a(1);
54
       end
       disp(z, "mode is");
55
56 endfunction
57 a=[223 12 233322 121]
58 y=median1(a);
59 z=mode1(a);
```

### Scilab code Exa 1.2.6 Finding the adress in a row major array

```
1 //Exercise1.2 Example 1.2.6
2 //Finding the adress in a row major array
3 function[] = add(m,n)
     printf("Adress is %d\n",m+n*20);
5 endfunction
7 //(a)
8 add(10,0);
9 //(b)
10 add(100,0);
11 //(c)
12 add(0,0);
13 //(d)
14 add(2,1);
15 // (e)
16 add(5,1);
17 // (f)
18 add(1,10);
19 // (g)
20 add(2,10);
```

```
21 //(h)

22 add(5,3);

23 //(i)

24 add(9,19);
```

Scilab code Exa 1.3 Writing name from structure and counting alphabets

```
1 //Solved Example 5:
2 //Writing a name from the given structure and
3 //counting the number of alphabets printed
4 function[1]=strlen(str)
     i=1;
6
     1 = 0;
7
     [j,k]=size(str)
     for i=1:k
9
       l=l+length(str(i));
10
     end
11 endfunction
12 function [count] = writename(name)
13
     printf("\n");
     printf("%s", name.first);
14
     printf("%c",' ');
15
     printf("%s", name.midinit);
16
     printf(" \setminus t");
17
     printf("%s", name.last);
18
     printf("\n");
19
20
21
     a=string(name.first);
22
     count=strlen(a);
     a=string(name.midinit);
23
     count=count+strlen(a);
24
     a=string(name.last);
25
     count=count+strlen(a);
26
     disp(count, "Count is:");
27
28 endfunction
```

#### Scilab code Exa 1.3.1 Implementing Complex Numbers by structure

```
1 //Exercise 1.3
2 //Example 1.3.1
3 //Implementing Complex Numbers by structure
4 function [] = complexmanu(x1, x2, x3, x4)
6
     com1=struct('real',x1,'complex',x2);
7
     com2=struct('real',x3,'complex',x4);
      //adding 2 numbers
8
      add=struct('real',x1+x3,'complex',x2+x4);
9
      disp(add.complex,"+ i",add.real,"Addition result
10
         is ");
      //Substract
11
12
      sub=struct('real',x1-x3,'complex',x2-x4);
13
      disp(sub.complex,"+ i", sub.real, "Substraction
         result is ");
14
      //Negating
      neg=struct('real',-x1,'complex',-x2);
15
      disp(neg.complex,"+ i",neg.real,"Negation result
16
         for the first is ");
      // Multiplication
17
      mul=struct('real',x1*x3-x2*x4,'complex',x2*x3+x4*
18
         x1);
       disp(mul.complex,"+ i",mul.real," Multiplication
19
          result is ");
20
    endfunction
21
    x1=3;
22
    x2=5;
23
    x3=5;
```

```
24 x4=6;
25 complexmanu(x1,x2,x3,x4);
```

Scilab code Exa 1.3.6 Adding Substracting and multiplying Rational Nos

```
1 //Exercise 1.3
2 //Example 1.3.6
3 //Adding, Subtracting and multiplying Rational
4 function[]=rational(x1,x2,x3,x4)
5 rational1=struct('numerator',x1,'denominator',x2);
6 disp(rational1);
7 rational2=struct('numerator',x3,'denominator',x4);
8 disp(rational2);
9 //Add
10 x5 = int32([x2 x4]);
11 x5 = 1cm(x5);
12 x6=x1*(x5/x2)+x3*(x5/x4);
13 rational3=struct('numerator',x6,'denominator',x5);
14 disp(rational3, "After addition");
15 //subtract
16 \quad x6=x1*(x5/x2)-x3*(x5/x4)
17 rational4=struct('numerator',x6,'denominator',x5);
18 disp(rational4, "After Subtraction");
19 // Multiply
20 x7 = x1 * x3;
21 \times 8 = \times 2 \times \times 4;
22 rational5=struct('numerator', x7, 'denominator', x8);
23 disp(rational5, "After multiplication");
24 endfunction
25 \times 1 = 43;
26 \times 2 = 32;
27 x3 = 233;
28 \times 4 = 33;
29 rational(x1,x2,x3,x4);
```

#### Scilab code Exa 1.3.7 Checking Equality Of 2 Rational Numbers

```
1 // Exercise 1.3
2 //Example 1.3.7
3 // Checking Equality Of 2 Rational Numbers Without
      Reducing Them
4 function[]=rational_equal(x1,x2,x3,x4)
5 rational1=struct('numerator',x1,'denominator',x2);
6 disp(rational1);
7 rational2=struct('numerator',x3,'denominator',x4);
8 disp(rational2);
9 if (x1*x4==x2*x3)
     disp("Equal");
10
11
     break;
12 else
     disp("Not Equal");
13
14
     break;
15 end
16 endfunction
17 // Calling Routine:
18 \times 1 = 32;
19 x2=45;
20 \times 3 = 43;
21 \times 4 = 55;
22 rational_equal(x1,x2,x3,x4);
```

#### Scilab code Exa 1.4 Raising the salary of employee

```
for i=1:n
4
5
       if (employee(i)(1).year <= 2000)</pre>
         employee(i)(2) = employee(i)(2)*1.1;
6
7
       else
8
         employee(i)(2) = employee(i)(2)*1.05;
9
       end
10
     end
     employee1 = employee;
11
12
     disp("After Raising");
     for i=1:n
13
14
       printf("Employee no %d\n",i);
       disp(employee(i)(1));
15
16
       disp(employee(i)(2));
17
     end
18
19 endfunction
20 // Calling Routine:
21 datehired=struct('year',1993,'month',12);
22 employee1=list(datehired,14000);
23 datehired=struct('year',1998,'month',12);
24 employee2=list(datehired, 17000);
25 datehired=struct('year',2003,'month',12);
26 employee3=list(datehired, 25000);
27 datehired=struct('year',2002,'month',12);
28 employee4=list(datehired, 35000);
29 datehired=struct('year',2006,'month',12);
30 employee5=list(datehired, 13000);
31 employee=list(employee1,employee2,employee3,
      employee4,employee5);
32 employee=raise(employee,5)
```

Scilab code Exa 1.5 Reducing the given rational number

```
1 // Solved Example 7:2 // Reducing The Given Rational Number
```

```
3 funcprot(0)
4 function[y]=reduce(nm,dn)
5 rational1=struct('numerator',nm,'denominator',dn)
6 v = 0
7 if (rational1.numerator>rational1.denominator)
     a=rational1.numerator;
     b=rational1.denominator;
10 else
11
     a=rational1.denominator;
     b=rational1.numerator;
13 end
14 \text{ while}(b~=0)
15
    rem=modulo(a,b);
16
     a=b;
17
     b=rem;
18 \, \text{end}
19 y=struct('numerator',nm/a,'denominator',dn/a);
20 disp(y);
21 endfunction
22 \text{ nm} = 22;
23 \, dn = 44;
24 y=reduce(nm,dn)
```

#### Scilab code Exa 1.6 Equality check of 2 rational nos by reduction

```
//Solved Example 8:
//Checking for the equality of 2 rational numbers by reducing them
function[] = equal(x1,x2,x3,x4)
rational1 = struct('numerator',x1,'denominator',x2)
rational2 = struct('numerator',x3,'denominator',x4)
y=0
fi(rational1.numerator>rational1.denominator)
a = rational1.numerator;
b = rational1.denominator;
```

```
10 else
11
     a=rational1.denominator;
12
     b=rational1.numerator;
13 end
14 while(b~=0)
15
     rem=modulo(a,b);
16
     a=b;
     b=rem;
17
18 end
19 y=struct('numerator',x1/a,'denominator',x2/a);
20 y1 = 0
21 if (rational2.numerator>rational2.denominator)
     a=rational2.numerator;
23
     b=rational2.denominator;
24 else
25
     a=rational2.denominator;
26
     b=rational2.numerator;
27 end
28 \text{ while (b~=0)}
29
     rem=modulo(a,b);
30
     a=b;
31
     b=rem;
32 end
33 y1=struct('numerator',x3/a,'denominator',x4/a);
34 \text{ if } (y == y1)
     disp("Equal")
35
36
     break;
37 else
     disp("Not Equal")
39
     break;
40 \, \text{end}
41 endfunction
42 \times 1 = 5;
43 \times 2 = 7;
44 \times 3 = 35;
45 \times 4 = 49;
46 equal(x1,x2,x3,x4);
```

## Chapter 2

## **Stacks**

Scilab code Exa 2.1 To determine the syntacticaly valid string

```
1 //Solved Example 1
2 //To determine the syntacticaly valid string
3 function[1]=strlen(x)
     i=1;
5
     1=0;
     [j,k]=size(x)
    for i = 1 : k
8
       l=l+length(x(i));
9
     end
10 endfunction
11 function[]=stringvalid(str)
     str=string(str);
12
     stack=struct('a','0','top',0);
13
14
     11=strlen(str);
15
     valid=1;
16
     1=1;
17
     while(1<=11)</pre>
         if (str(1) == '('|str(1) == '['|str(1) == '{'}]
18
            if (stack.top==0)
19
20
              stack.a=str(1);
21
              stack.top=stack.top+1;
```

```
22
            else
               stack.a=[stack.a(:,:) str(1)];
23
24
               stack.top=stack.top+1;
25
            end
26
          end
          if (str(1) == ') '| str(1) == '] '| str(1) == '} ')
27
            if (stack.top==0)
28
29
               valid=0;
30
              break;
31
            else
32
             i=stack.a(stack.top);
33
             stack.top=stack.top-1;
34
             symb=str(1);
             if (((symb==')')&(i=='('))|((symb==')')&(i==
35
                 '['))|((symb=='}')&(i=='{')))
36
            else
37
              valid=0;
38
              break;
39
            end
40
          end
41
        end
42
          1=1+1;
43
        end
        if (stack.top~=0)
44
          valid=0;
45
46
        end
        if (valid==0)
47
          disp("Invalid String");
48
49
          disp("Valid String");
50
51
        end
     endfunction
52
     // Calling Routine:
53
54 stringvalid(['H' 'E' 'L' 'L' 'O'])
```

### Scilab code Exa 2.1.2 To determine the syntacticaly valid string

```
1 //Solved Example 1
2 //To determine the syntactically valid string
3 function[1]=strlen(x)
     i = 1:
     1 = 0;
5
     [j,k]=size(x)
6
7
     for i=1:k
       l=l+length(x(i));
8
9
     end
10 endfunction
11 function[] = stringvalid(str)
     str=string(str);
12
     stack=struct('a','0','top',0);
13
     11=strlen(str);
14
     valid=1;
15
     1=1;
16
17
     while (1<=11)
          if (str(1) == '('|str(1) == '['|str(1) == '{'}]
18
19
            if (stack.top==0)
20
              stack.a=str(1);
21
              stack.top=stack.top+1;
22
            else
              stack.a=[stack.a(:,:) str(1)];
23
24
              stack.top=stack.top+1;
25
            end
26
            disp(stack);
27
          if (str(l) == ') '|str(l) == '] '|str(l) == '} ')
28
            if (stack.top==0)
29
30
              valid=0;
31
              break;
32
            else
              i=stack.a(stack.top);
33
              b=stack.a(1);
34
              for i1=2:stack.top-1
35
                b=[b(:,:) stack.a(i1)]
36
```

```
37
                                                   end
38
                                                   stack.a=b;
39
                                               stack.top=stack.top-1;
40
                                              symb=str(1);
41
                                              disp(stack);
                                              if (((symb==')')&(i=='('))|((symb==')')&(i=')
42
                                                          ['))|((symb='}')&(i='{')))
43
                                           else
44
                                                  valid=0;
45
                                                  break;
46
                                           end
47
                                   end
48
                           end
49
                                   1=1+1;
50
                           end
51
                           if (stack.top~=0)
52
                                   valid=0;
53
                           end
54
                           if (valid==0)
                                   disp("Invalid String");
55
56
                           else
57
                                   disp("Valid String");
58
                           end
59
                   endfunction
                   //Calling Routine:
60
                   stringvalid(['(' 'A' '+' 'B' ')'])
61
                   62
                              'C', '-', 'D', ')', ']']
                   stringvalid(['(',',A',',+',',B',',')',',-',',{',',C',',+',','}
63
                            D^{(1)}, F^{(2)}, F
                   64
                             65
```

Scilab code Exa 2.2 Implementing Stack using union

```
1 //Solved Example 2:
2 //Implementing Stack using union:
3 function[stack]=sta_union(etype,a)
     stackelement=struct('etype',etype);
     [k,1]=size(a);
6 select stackelement.etype,
7 case 'int' then
     a=int32(a);
     stack=struct('top',1,'items',a);,
     case 'float' then
10
    a=double(a);
11
12
    stack=struct('top',1,'items',a);,
13
     case 'char' then
14
     a=string(a);
     stack=struct('top',1,'items',a);,
15
16 \text{ end}
17 disp(stack, "Stack is:");
18 endfunction
19 a=[32 12.34 232 32.322]
20 stack=sta_union('float',a)
21 stack=sta_union('int',a)
22 stack=sta_union('char',a)
```

#### Scilab code Exa 2.2.3 Check if string is of certain form

```
1 function[1]=strlen(x)
2    i=1;
3    l=0;
4    [j,k]=size(x)
5    for    i=1:k
6     l=l+length(x(i));
7    end
8    endfunction
9    function[]=str(st)
10    stack=struct('a',0,'top',0);
```

```
11
     st=string(st);
12
     1=1;
13
     11=strlen(st);
     symb=st(1);
14
15
     valid=1;
16
     while (1<11)
        while (symb \sim = 'C')
17
          if (stack.top==0)
18
19
               stack.a=st(1);
20
               stack.top=stack.top+1;
21
           else
22
               stack.a=[stack.a(:,:) st(1)];
23
               stack.top=stack.top+1;
24
           end
25
           1=1+1;
26
           symb=st(1);
27
         end
28
         i=st(l+1);
29
        if (stack.top==0)
30
            valid=0;
31
            break;
32
         else
           symb1=stack.a(stack.top);
33
34
           stack.top=stack.top-1;
           if(i~=symb1)
35
36
             valid=0;
37
             break;
38
           end
39
         end
40
        1=1+1;
41
        if (stack.top~=0)
42
43
          valid=0;
44
        end
        if (valid==0)
45
          disp("Not of the given format");
46
47
        else
          disp("String Of the Given Format");
48
```

```
49     end
50     endfunction
51     // Calling     Routine:
52     st=['A' 'A' 'B' 'A' 'C' 'A' 'B' 'A' 'A']
53     str(st)
54     st=['A' 'A' 'B' 'A' 'C' 'A' 'B' 'A']
55     str(st)
```

## Scilab code Exa 2.3 Implementing Push And Pop Functions

```
1 //Solved Example 3:
2 //Implementing Push And Pop Functions:
3 function[y,sta1]=empty(sta)
4
     y = 0;
5
     sta1=0;
     if (sta.top==0)
6
7
       y = 0;
8
     else
9
       y=1;
10
     end
11
     sta1=sta
12 endfunction
13
14 function[sta] = push(stac, ele)
     sta=0;
15
     if (empty(stac) == 0)
16
17
       stac.a=ele;
18
       stac.top=stac.top+1;
19
     else
       stac.a=[stac.a(:,:) ele]
20
       stac.top=stac.top+1;
21
22
     end
23
     disp(stac);
24
     sta=stac;
25 endfunction
```

```
26
27
  function[ele,sta]=pop(stack)
     ele='-1';
28
     if (empty(stack) == 0)
29
30
       disp("Stack Underflow");
31
       break:
32
     else
       ele=stack.a(stack.top);
33
       stack.top=stack.top-1;
34
       if (stack.top~=0)
35
         b=stack.a(1);
36
37
       for i2=2:stack.top
38
         b=[b(:,:) stack.a(i2)];
39
       end
40
       stack.a=b;
41
       stack.a='0';
42
43
     end
44
     end
45
     disp(stack);
     sta=stack;
46
47 endfunction
48 global stack
49 // Calling Routine:
50 stack=struct('a',0,'top',0);
51 stack=push(stack,4);
52 stack=push(stack,55);
53 stack=push(stack,199);
54 stack=push(stack,363);
55 [ele,stack]=pop(stack);
56 disp(stack, "After the above operations stack is:");
```

Scilab code Exa 2.4 Convering an infix expression to a Postfix Express

```
1 //Solved Example 5:
```

```
2 // Convering an infix expression to a Postfix
      Expression:
  function[sta] = push(stac, ele)
4
     sta=0;
5
     if (stac.top==0)
6
       stac.a=ele;
7
       stac.top=stac.top+1;
8
     else
9
       stac.a=[stac.a(:,:) ele]
10
       stac.top=stac.top+1;
11
     end
12
     disp(stac);
13
     sta=stac;
14 endfunction
15
16 function[ele,sta]=pop(stack)
     ele='-1';
17
     if (stack.top==0)
18
19
       disp("Stack Underflow");
20
       break:
21
     else
22
       ele=stack.a(stack.top);
       stack.top=stack.top-1;
23
24
       if (stack.top~=0)
25
          b=stack.a(1);
26
       for i2=2:stack.top
27
          b=[b(:,:) stack.a(i2)];
28
       end
29
       stack.a=b;
30
     else
31
       stack.a='0';
32
     end
33
     end
     sta=stack;
34
35 endfunction
36 function[1]=strlen(x)
37
     i=1;
38
     1 = 0;
```

```
[j,k]=size(x)
39
40
     for i = 1 : k
        1=1+length(x(i));
41
42
     end
43 endfunction
   function[p]=pre(s1,s2)
45
         i1=0;
        select s1,
46
        case '+' then i1=5;
47
       case '-' then i1=5;
48
        case '*' then i1=9;
49
       case '/' then i1=9;
50
51
        end
52
        i2=0;
53
        select s2,
       case '+' then i2=5;
54
55
        case '-' then i2=5;
56
        case '*' then i2=9;
57
        case '/' then i2=9;
58
        end
59
       p=0;
60
       p=i1-i2;
        if(s1=='(')
61
62
          p = -1;
63
        end
        if (s2== '('&s1~=')')
64
65
          p = -1;
66
        end
67
        if (s1~='('&s2==')')
68
          p=1;
69
        end
70
71
     endfunction
72 function[a2]=intopo(a1,n)
     stack=struct('a',0,'top',0);
73
74
     11=1;
75
     12=strlen(a1(1))
76
     for i=2:n
```

```
77
        12=12+strlen(a1(i))
78
      end
79
      a2=list();
      while(11<=12)</pre>
80
81
        symb=a1(11);
82
        if(isalphanum(string(a1(11))))
           a2=list(a2, symb);
83
        else
84
           while(stack.top~=0&(pre(stack.a(stack.top),
85
              symb) >= 0)
86
             [topsymb,stack]=pop(stack);
87
             if (topsymb == ') '| topsymb == '(')
88
               a2 = a2;
             else
89
90
               a2=list(a2,topsymb);
91
92
           end
93
           if (stack.top==0|symb~=')')
94
             stack=push(stack,symb);
95
           else
96
             [ele,stack]=pop(stack);
97
           end
98
        end
99
        11=11+1;
100
      end
      while(stack.top~=0)
101
102
         [topsymb,stack]=pop(stack);
        if (topsymb== ') '|topsymb== '(')
103
104
           a2=a2;
105
        else
106
           a2=list(a2,topsymb);
107
        end
108
      end
      disp(a2);
109
110 endfunction
111 // Calling Routine:
112 a1=['(' '2' '+' '3' ')' '*' '(' '5' '-' '4' ')']
113 a2=intopo(a1,11)
```

## Chapter 3

## Recursion

### Scilab code Exa 3.1 Multiplication of 2 numbers

```
// Multiplication of 2 numbers
funcprot(0)
function[val]=mul(a,b)

if(b==1)
val=a;
else
val=a+mul(a,b-1);
end
endfunction
// Calling Routine:
1 a=4;
b=3;
val=mul(4,3)
printf("Product of %d and %d is %d",a,b,val);
```

#### Scilab code Exa 3.2 Factorial of a number

```
1 //Function To Caluculate factorial of a given number
```

```
2 function[value]=fact(a)
     value = -1;
3
4
     if(a<0|a>170)
       disp("Invalid valu.");
6
       break;
     else
       if (a==1 | a==0)
8
         value=1;
9
10
       else
         value=a*fact(a-1);
11
12
       end
13
     end
14 endfunction
15 // Calling Routine:
16 \ a=5;
17 val=fact(a);
18 printf("%d factorial is %d",a,val);
```

## Scilab code Exa 3.3 Fibbonacci series

```
1 function[fib]=fibbo(n)
2
     fib=-1;
3
     if(n<0)
       disp("Invalid Entry");
4
      if (n<=1)
6
7
        fib=n;
9
        fib=fibbo(n-1)+fibbo(n-2);
10
      end
11
    end
12 endfunction
13
14 function[1]=fibbon(n)
15
     x=0;
```

```
16  l=(fibbo(0));
17  for x=1:n-1
18  l=[l(:,:),fibbo(x)];
19  end
20  disp(l);
21  endfunction
22  // Calling Routine:
23  n=5;
24  l=fibbon(n)
```

### Scilab code Exa 3.4 Binary Search

```
1 function[b]=bsear(a,1,u,n)
2
     if(1>u)
3
       b = -1;
4
     else
       mid = int32((1+u)/2);
5
       if (n==a(mid))
6
7
          b=n;
8
       else
9
          if(n>a(mid))
             mid = int32((1+u)/2);
10
            b=bsear(a,mid+1,u,n);
11
12
          else
13
             mid = int32((1+u)/2);
            b=bsear(a,l,mid-1,n);
14
15
          end
16
       end
17
     end
18 endfunction
19
20 function[b]=bsearc(a,1,u,n)
21
     b=bsear(a,1,u,n);
22
     if(b==-1)
       disp("The element is not there");
23
```

```
24    end
25    if(b==n)
26        disp("The element is there");
27    end
28    endfunction
29    // Calling Routine:
30    a=[12 122 3233 12121] // Must be sorted:
31    b=bsearc(a,1,4,12)
```

#### Scilab code Exa 3.5 Tower Of Hanoi

```
1 function[] = towe(n, from, to, aux)
2
     if (n==1);
       disp(to,"to ",from,"Move peg 1 from");
3
4
       towe(n-1, from, aux, to);
5
       disp(to, "to", from, "from", n, "Move Peg");
6
       towe (n-1, aux, to, from);
     end
9 endfunction
10
11 function[] = tower(from, to, aux)
12
     n=input("Enter n");
13
     towe(n,from,to,aux);
14 endfunction
15 // Calling Routine:
16 n=3//Number of disks
17 towe(n,'a','b','c')
```

#### Scilab code Exa 3.6 Prefix To Postfix Conversion

```
1 funcprot(0)
2 function[y]=find1(g)
```

```
3
      length1=strlen(g);
4
      if (length1==0)
 5
        y = 0;
 6
      else
        if(isalphanum(g(1)))
 7
8
           y=1;
9
        else
10
           if (length1<2)</pre>
11
             y = 0;
12
           else
              s=strsplit(g,1);
13
14
              s=s(2);
15
              m=find1(s);
              if (m==0|length1==m)
16
17
                 y = 0;
18
              else
19
                  e=strsplit(g,m+1);
20
                  e=e(2);
21
                  n=find1(e);
22
                  if(n==0)
23
                     y=0;
24
                  else
25
                     y=m+n+1;
                  \quad \text{end} \quad
26
27
                end
28
             end
29
           end
30
        end
31
      endfunction
      function[1] = strlen(x)
32
33
      i=1;
34
      1=0;
      [j,k]=size(x)
35
36
      for
           i=1:k
        l=l+length(x(i));
37
38
      end
39 endfunction
40 function[po]=pr2po(pr)
```

```
41
     length1=strlen(pr);
     if (length1==1)
42
       if(isalphanum(pr))
43
         po(1)=pr(1);
44
45
       else
46
          disp("Invalid string\n");
47
       end
48
     else
49
       s=strsplit(pr,1);
       g=s(2);
50
       m=find1(g);
51
52
       s=strsplit(pr,m+1);
53
       g1=s(2);
       n=find1(g1);
54
       f=strsplit(pr,1);
55
56
       c=f(1);
       if ((c~='+'&c~='-'&c~='/'&c~='*')|m==0|n==0|m+n
57
          +1~=length1)
          printf("Invalid string\n");
58
       else
59
60
          s=strsplit(pr,1);
         s=strsplit(s(2),m);
61
62
          opnd1=s(1);
63
          s=strsplit(pr,m+1);
          opnd2=s(2);
64
65
          post1=pr2po(opnd1);
66
          post2=pr2po(opnd2);
          post=[post1(:,:) post2(:,:)]
67
          f=strsplit(pr,1);
68
          c=f(1);
69
70
          post3=[post(:,:) c];
71
         po=post3;
72
         end
73
      end
74
    endfunction
75
    // Calling Routine:
76
    s1="+-*abcd";//no spaces between
77
```

```
78    po=pr2po(s1);
79    disp(po,"postfix is");
80    s1="+-*/+-*/abcdefghi"
81    po=pr2po(s1);
82    disp(po,"postfix is");
```

### Scilab code Exa 3.7 Simulating Factorial By Non recursion

```
1
2 function[]=simu_fact(n);
3 a=1;
4 while(n>0)
5 a=a*n;
6 n=n-1;
7 end
8 disp(a,"Factorial is ");
9 endfunction
10 //Calling Routine:
11 a=9
12 simu_fact(a)
```

# Chapter 4

# Queues and linked list

Scilab code Exa 4.1 Implementing Singly Connected Linked List

```
1 //SINGLY CONNECTED LINKED LIST:
2 function[link2] = append(ele, link1)
    link2=list
       if (link1(1)(1).add==0)
4
      link1(1)(1).data=ele;
6
      link1(1)(1).add=1;
      link1(1)(1).nexadd=0;
8
      link2(1)=link1(1)(1);
9
      if (link1(1)(1).nexadd==0)
10
11
        lin2=link1(1)(1);
12
        lin2.data=ele;
        lin2.add=link1(1)(1).add+1;
13
14
        link1(1)(1).nexadd=lin2.add;
        lin2.nexadd=0;
15
16
        link2(1)=link1(1)(1);
17
        link2(2)=lin2;
18
      else
19
        lin2=link1(1)(1);
```

```
20
         i=1;
21
         while(link1(i)(1).nexadd~=0)
22
           i=i+1;
23
         end
24
         j=i;
         lin2.data=ele;
25
26
         lin2.add=link1(i).add+1;
         lin2.nexadd=0;
27
28
         link1(i).nexadd=lin2.add;
29
         link2(1)=link1(1)(1);
30
         i=2;
31
         while (link1(i).nexadd~=lin2.add)
32
           link2(i)=(link1(i));
33
           i=i+1;
34
         end
         link2(i)=link1(i);
35
         link2(i+1)=lin2;
36
37
       end
38
     end
39 endfunction
40 function[link2] = add(ele, pos, link1);
41
      link2=list
         ;
      i=1;
42
43
      while(i<=pos)</pre>
        if (link1(i).nexadd==0)
44
45
          break;
46
        else
47
          i=i+1;
48
        end
49
      end
      if(link1(i).nexadd~=0)
50
51
        i=i-1;
         lin2.data=ele;
52
         lin2.add=i;
53
         j=i;
54
         while(link1(j).nexadd~=0)
55
```

```
link1(j).add=link1(j).add+1;
56
            link1(j).nexadd=link1(j).nexadd+1;
57
58
            j = j + 1;
59
          end
60
          link1(j).add=link1(j).add+1;
61
          lin2.nexadd=link1(i).add;
          link1(i-1).nexadd=lin2.add;
62
63
          k=1;
64
          while(k<i)</pre>
             link2(k)=link1(k);
65
66
             k=k+1;
67
68
           link2(k)=lin2;
69
           k=k+1;
           link2(k)=link1(k-1);
70
           k=k+1
71
72
           1=k-1;
73
           while(k~=j)
74
             link2(k)=link1(l);
75
             k=k+1;
76
             1=1+1;
77
           end
           link2(j)=link1(j-1);;
78
79
           link2(j+1)=link1(j);
80
         else
           if (i == pos&i~=1)
81
82
             k=1;
83
             lin2.data=ele;
84
             lin2.add=link1(i-1).add+1;
             link1(i).add=link1(i).add+1;
85
             lin2.nexadd=link1(i).add;
86
87
             k=1;
88
             while(k<pos)</pre>
               link2(k)=link1(k);
89
90
               k=k+1;
             end
91
92
             link2(k)=lin2;
93
             link2(k+1)=link1(k)
```

```
94
           end
           if (i == pos&i == 1)
95
             link2=append(ele,link1);
96
97
             return link2;
98
           end
99
         end
100 endfunction
101 function[link2] = delete1(pos, link1)
102
      link2=list
         103
     i=1;
104
      while(i<=pos)</pre>
        if((link1(i).nexadd==0))
105
106
          break;
107
        else
108
          i=i+1;
109
        end
110
      end
      if (link1(i).nexadd~=0)
111
112
        i=i-1;
113
        j=1;
        if (i == 1)
114
115
          j=1;
          while(link1(j).nexadd~=0)
116
117
            link2(j)=link1(j);
118
            j=j+1;
119
          end
120
          link2(j)=link1(j);
121
        else
122
        link1(i-1).nexadd=link1(i+1).add;
123
        while(link1(j).nexadd~=link1(i+1).add)
124
          link2(j)=link1(j);
125
          j = j + 1;
126
        end
127
        if(j~=i-1)
128
          link2(j)=link1(j);
129
          link2(j+1)=link1(j+1);
```

```
130
          k=i+1;
131
          1=2;
132
        else
           link2(j)=link1(j);
133
134
          k=i+1;
135
          1=1;
136
        end
        while(link1(k).nexadd~=0)
137
           link2(j+1)=link1(k);
138
139
          k=k+1;
140
           1 = 1 + 1;
141
142
        link2(j+1)=link1(k);
143
      end
144
      else
        if(i==pos)
145
146
           j=1;
147
           link1(i-1).nexadd=0;
148
           while (j \le i - 1)
             link2(j)=link1(j);
149
150
             j=j+1;
151
           end
152
        end
153
      end
154 endfunction
155
156
157
158 // Calling Routine:
159 link1=struct('data',0,'add',0,'nexadd',0);//Creates
       empty list
160 link1=append(4,link1)
161 link1=append(6,link1)
162 link1=add(7,2,link1)
163 link1=append(8,link1)
164 link1=delete1(4,link1)
165 disp(link1,"The linked list after the above
       modifications is:");
```

### Scilab code Exa 4.2 Implementing Queue Operarions

```
1 //Queue Operations
2 function[q2]=push(ele,q1)
     if (q1.rear==q1.front)
4
       q1.a=ele;
5
       q1.rear=q1.rear+1;
6
     else
       q1.a=[q1.a(:,:) ele];
       q1.rear=q1.rear+1;
8
9
     end
10
     q2=q1;
11 endfunction
12 function[ele,q2]=pop(q1)
13
     ele=-1;
14
     q2=0;
     if (q1.rear == q1.front)
15
       disp("Queue Underflow");
16
17
       return;
18
     else
19
       ele=q1.a(q1.rear-q1.front);
20
       q1.front=q1.front+1;
21
       i=1;
22
       a=q1.a(1);
       for i=2:(q1.rear-q1.front)
23
24
         a=[a(:,:) q1.a(i)];
25
       end
26
       q1.a=a;
27
     end
28
     q2=q1;
29 endfunction
30 // Calling Routine:
31 q1=struct('a',0,'rear',0,'front',0)
32 q1=push(3,q1)
```

```
33  q1=push(22,q1);
34  q1=push(21,q1);
35  disp(q1,"Queue after insertion");
36  [ele,q1]=pop(q1)
37  disp(ele,"poped element");
38  disp(q1,"Queue after poping");
39  [ele,q1]=pop(q1);
40  [ele,q1]=pop(q1);
41  [ele,q1]=pop(q1);//Underflow Condition
```

#### Scilab code Exa 4.3 Implementing Circular Linked List

```
1 //CIRCULAR LINKED LIST
2 function[link2] = append(ele, link1)
    link2=list
       if (link1(1)(1).add==0)
4
      link1(1)(1).data=ele;
5
      link1(1)(1).add=1;
6
7
      link1(1)(1).nexadd=1;
8
      link2(1)=link1(1)(1);
9
      else
10
      if (link1(1)(1).nexadd==link1(1)(1).add)
        lin2=link1(1)(1);
11
12
        lin2.data=ele;
        lin2.add=link1(1)(1).add+1;
13
        link1(1)(1).nexadd=lin2.add;
14
15
        lin2.nexadd=link1(1)(1).add;
        link2(1)=link1(1)(1);
16
        link2(2)=lin2;
17
18
      else
        lin2=link1(1)(1);
19
20
21
        while(link1(i)(1).nexadd~=link1(1)(1).add)
```

```
22
           i=i+1;
23
         end
24
         j=i;
25
         lin2.data=ele;
26
         lin2.add=link1(i).add+1;
27
         lin2.nexadd=link1(1)(1).add;
28
         link1(i).nexadd=lin2.add;
         link2(1)=link1(1)(1);
29
30
         while(link1(i).nexadd~=lin2.add)
31
32
           link2(i)=(link1(i));
33
           i=i+1;
34
         end
         link2(i)=link1(i);
35
         link2(i+1)=lin2;
36
37
       end
38
     end
39 endfunction
40 function[link2] = add(ele, pos, link1);
41
      link2=list
         42
      i=1;
      while(i<=pos)</pre>
43
        if (link1(i).nexadd==link1(1)(1).add)
44
45
          break;
46
        else
47
          i=i+1;
48
        end
49
      end
      if (link1(i).nexadd~=link1(1)(1).add)
50
51
        i=i-1;
52
         lin2.data=ele;
53
         lin2.add=i;
54
         while(link1(j).nexadd~=link1(1)(1).add)
55
           link1(j).add=link1(j).add+1;
56
           link1(j).nexadd=link1(j).nexadd+1;
57
```

```
58
            j=j+1;
59
          end
          link1(j).add=link1(j).add+1;
60
          lin2.nexadd=link1(i).add;
61
62
          link1(i-1).nexadd=lin2.add;
63
          k=1;
          while(k<i)</pre>
64
             link2(k)=link1(k);
65
             k=k+1;
66
67
           end
68
           link2(k)=lin2;
69
           k=k+1;
70
           link2(k)=link1(k-1);
71
           k=k+1
72
           l = k - 1;
           while(k~=j)
73
74
             link2(k)=link1(l);
75
             k=k+1;
76
             1=1+1;
77
           end
           link2(j)=link1(j-1);;
78
79
           link2(j+1)=link1(j);
80
         else
           if(i==pos)
81
82
             k=1;
83
             lin2.data=ele;
             lin2.add=link1(i-1).add+1;
84
             link1(i).add=link1(i).add+1;
85
86
             lin2.nexadd=link1(i).add;
             link1(i).nexadd=link1(1)(1).add;
87
88
             k=1;
             while(k<pos)</pre>
89
90
                link2(k)=link1(k);
               k=k+1;
91
92
93
             link2(k)=lin2;
94
             link2(k+1)=link1(k)
95
           end
```

```
96
        end
97
98 endfunction
99 function[link2] = delete1(pos,link1)
100
     link2=list
        101
     i=1;
102
     j=1;
103
     while(i<pos)</pre>
104
        if ((link1(j).nexadd==link1(1)(1).add))
105
          j=1;
106
          i=i+1;
107
       else
108
          i=i+1;
109
          j=j+1;
110
       end
111
112
     if(link1(j).nexadd~=link1(1)(1).add)
       k=1;
113
114
       if(j==1)
115
         k=2;
          while(link1(k).nexadd~=link1(1)(1).add)
116
117
            link2(k-1)=link1(k);
118
           k=k+1;
119
          end
120
          link2(k-1)=link1(k);
          link2(k-1).nexadd=link2(1).add;
121
122
       else
          lin2=link1(j);
123
          link1(j-1).nexadd=link1(j+1).add;
124
125
126
          while(link1(k).nexadd~=link1(j+1).add)
            link2(k)=link1(k);
127
128
           k=k+1;
129
          end
130
          link2(k)=link1(k);
         k=k+2;
131
```

```
while(link1(k).nexadd~=link1(1)(1).add)
132
133
            link2(k-1)=link1(k);
134
            k=k+1;
135
          end
136
          link2(k-1)=link1(k);
137
        end
138
      else
        link1(j-1).nexadd=link1(1)(1).add;
139
140
        while(link1(l).nexadd~=link1(1)(1).add)
141
142
          link2(1)=link1(1);
143
          1=1+1;
144
        end
145
        link2(1)=link1(1);
146
      end
147 endfunction
148 // Calling Routine:
149 link1=struct('data',0,'add',0,'nexadd',0);
150 link1=append(4,link1);//This will actualy create a
       list and 4 as start
151 link1=append(6,link1);
152 link1=add(10,2,link1);
153 link1=delete1(4,link1);//As the list is circular the
        4'th element refers to actualy the 1'st one
154 disp(link1, "After the above manuplations the list is
      ");
```

Scilab code Exa 4.4 Implementing Doubly connected Linked List

```
link1(1)(1).data=ele;
5
6
       link1(1)(1).add=1;
       link1(1)(1).nexadd=0;
8
       link1(1)(1).prevadd=0;
9
       link2(1)=link1(1)(1);
10
       else
       if (link1(1)(1).nexadd==0)
11
         lin2=link1(1)(1);
12
13
         lin2.data=ele;
         lin2.add=link1(1)(1).add+1;
14
15
         link1(1)(1).nexadd=lin2.add;
         lin2.nexadd=0;
16
17
         lin2.prevadd=link1(1)(1).add;
         link2(1)=link1(1)(1);
18
         link2(2)=lin2;
19
20
       else
         lin2=link1(1)(1);
21
22
         i=1;
23
         while(link1(i)(1).nexadd~=0)
24
            i=i+1;
25
         end
         j=i;
26
27
         lin2.data=ele;
         lin2.add=link1(i).add+1;
28
         lin2.nexadd=0;
29
30
         link1(i).nexadd=lin2.add;
31
         lin2.prevadd=link1(i).add;
         link2(1)=link1(1)(1);
32
33
         i=2;
         while(link1(i).nexadd~=lin2.add)
34
            link2(i)=(link1(i));
35
36
           i=i+1;
37
         end
         link2(i)=link1(i);
38
         link2(i+1)=lin2;
39
40
       end
41
     end
42 endfunction
```

```
43 function[link2] = add(ele,pos,link1);
      link2=list
         45
      i=1;
46
      while(i<=pos)</pre>
        if (link1(i).nexadd==0)
47
48
          break;
49
        else
50
          i=i+1;
51
        end
52
53
      if (link1(i).nexadd~=0)
54
        i=i-1;
55
         lin2.data=ele;
         lin2.add=i;
56
57
         j=i;
         while(link1(j).nexadd~=0)
58
           link1(j).prevadd=link1(j).prevadd+1;
59
           link1(j).add=link1(j).add+1;
60
61
           link1(j).nexadd=link1(j).nexadd+1;
62
           j = j + 1;
63
         end
         link1(j).prevadd=link1(j).prevadd+1;
64
         link1(j).add=link1(j).add+1;
65
66
         lin2.nexadd=link1(i).add;
67
         link1(i).prevadd=lin2.add;
         lin2.prevadd=link1(i-1).add;
68
         link1(i-1).nexadd=lin2.add;
69
70
         k=1;
71
         while(k<i)
72
            link2(k)=link1(k);
73
            k=k+1;
74
          end
75
          link2(k)=lin2;
76
          k=k+1;
77
          link2(k)=link1(k-1);
          k=k+1
78
```

```
79
           1 = k - 1;
           while(k~=j)
80
             link2(k)=link1(l);
81
82
             k=k+1;
83
             1=1+1;
84
           link2(j)=link1(j-1);;
85
           link2(j+1)=link1(j);
86
87
         else
           if(i==pos)
88
89
             k=1;
90
             lin2.data=ele;
91
             lin2.add=link1(i-1).add+1;
92
             link1(i).add=link1(i).add+1;
93
             lin2.nexadd=link1(i).add;
             link1(i).prevadd=lin2.add;
94
             lin2.prevadd=link1(i-1).add;
95
96
             k=1;
97
             while(k<pos)</pre>
               link2(k)=link1(k);
98
99
               k=k+1;
100
             end
             link2(k)=lin2;
101
             link2(k+1)=link1(k)
102
103
           end
104
         end
105
106 endfunction
107 function[link2] = delete1(pos, link1)
108
      link2=list
        i=1;
109
      while(i<=pos)</pre>
110
        if ((link1(i).nexadd==0))
111
112
          break;
113
        else
114
          i=i+1;
```

```
115
         end
116
      end
      if (link1(i).nexadd~=0)
117
118
        i=i-1;
119
        j=1;
120
        if (i == 1)
121
           j=1;
122
           while(link1(j).nexadd~=0)
             link2(j)=link1(j);
123
124
             j = j + 1;
125
           end
126
           link2(j)=link1(j);
127
           link1(i-1).nexadd=link1(i+1).add;
128
129
           link1(i+1).prevadd=link1(i-1).add;
        while(link1(j).nexadd~=link1(i+1).add)
130
131
           link2(j)=link1(j);
132
           j=j+1;
133
        end
         if (j~=i-1)
134
135
           link2(j)=link1(j);
136
           link2(j+1)=link1(j+1);
137
           k=i+1;
138
           1 = 2;
139
        else
           link2(j)=link1(j);
140
141
           k=i+1;
142
           1=1;
143
        end
144
         while(link1(k).nexadd~=0)
           link2(j+1)=link1(k);
145
146
           k=k+1;
147
           1 = 1 + 1;
148
        link2(j+1)=link1(k);
149
150
      end
151
      else
        if(i==pos)
152
```

```
153
          j=1;
154
          link1(i-1).nexadd=0;
          while (j \le i - 1)
155
             link2(j)=link1(j);
156
157
             j = j + 1;
158
          end
159
        end
160
      end
161 endfunction
162 // Calling Routine:
163 link1=struct('data',0,'add',0,'nexadd',0);
164 link1=append(4,link1);
165 link1=append(6,link1);
166 link1=add(10,2,link1);
167 link1=delete1(3,link1);
168 disp(link1, "After the above manuplations the list is
       ");
```

Scilab code Exa 4.5 Implementing Stack using circular Linked list

```
1 //STACK USING CIRCULAR LINKED LIST
2 funcprot(0)
3 function[link2] = append(ele, link1)
    link2=list
      if (link1(1)(1).add==0)
5
6
      link1(1)(1).data=ele;
7
      link1(1)(1).add=1;
      link1(1)(1).nexadd=1;
8
      link2(1)=link1(1)(1);
9
10
      if (link1(1)(1).nexadd==link1(1)(1).add)
11
12
       lin2=link1(1)(1);
13
       lin2.data=ele;
```

```
14
         lin2.add=link1(1)(1).add+1;
         link1(1)(1).nexadd=lin2.add;
15
         lin2.nexadd=link1(1)(1).add;
16
17
         link2(1)=link1(1)(1);
18
         link2(2)=lin2;
19
       else
20
         lin2=link1(1)(1);
21
         i=1;
22
         while(link1(i)(1).nexadd~=link1(1)(1).add)
23
           i=i+1;
24
         end
25
         j=i;
26
         lin2.data=ele;
         lin2.add=link1(i).add+1;
27
         lin2.nexadd=link1(1)(1).add;
28
         link1(i).nexadd=lin2.add;
29
         link2(1)=link1(1)(1);
30
31
         i=2;
32
         while(link1(i).nexadd~=lin2.add)
           link2(i)=(link1(i));
33
34
           i=i+1;
35
         end
         link2(i)=link1(i);
36
37
         link2(i+1)=lin2;
38
       end
39
     end
40 endfunction
41 function[link2] = add(ele, pos, link1);
      link2=list
         ;
      i=1;
43
44
      while(i<=pos)</pre>
        if (link1(i).nexadd==link1(1)(1).add)
45
46
          break;
        else
47
48
          i=i+1;
49
        end
```

```
50
      end
51
      if (link1(i).nexadd~=link1(1)(1).add)
         i=i-1;
52
53
          lin2.data=ele;
54
          lin2.add=i;
55
          j=i;
          while(link1(j).nexadd~=link1(1)(1).add)
56
            link1(j).add=link1(j).add+1;
57
            link1(j).nexadd=link1(j).nexadd+1;
58
            j = j + 1;
59
60
          end
61
          link1(j).add=link1(j).add+1;
62
          lin2.nexadd=link1(i).add;
          link1(i-1).nexadd=lin2.add;
63
64
          k=1;
          while(k<i)</pre>
65
             link2(k)=link1(k);
66
67
             k=k+1;
68
           end
69
           link2(k)=lin2;
70
           k=k+1;
           link2(k)=link1(k-1);
71
72
           k=k+1
73
           1=k-1;
74
           while (k~=j)
             link2(k)=link1(l);
75
76
             k=k+1;
77
             1=1+1;
78
           link2(j)=link1(j-1);;
79
           link2(j+1)=link1(j);
80
81
         else
82
           if(i==pos)
83
             k=1;
             lin2.data=ele;
84
             lin2.add=link1(i-1).add+1;
85
             link1(i).add=link1.add+1;
86
             lin2.nexadd=link1(i).add;
87
```

```
link1(i).nexadd=link1(1)(1).add;
88
89
             k=1;
             while(k<pos)</pre>
90
               link2(k)=link1(k);
91
92
               k=k+1;
93
             end
94
             link2(k)=lin2;
             link2(k+1)=link1(k)
95
96
           end
97
         end
98
99 endfunction
100 function[link2] = delete1(pos,link1)
101
     link2=list
        102
     i=1;
103
     if (link1(1)(1).add==0)
104
       disp("Invalid");
     else
105
106
        if (link1(1)(1).nexadd==link1(1)(1).add)
107
          link1(1)(1).add=0;
         link1(1)(1).nexadd=0;
108
109
          link1(1)(1).data=0;
          link2(1)=link1(1)(1);
110
111
       else
112
     while(i<=pos)</pre>
       if ((link1(i).nexadd==link1(1)(1).add))
113
114
          break;
115
       else
116
         i=i+1;
117
       end
118
     end
     if (link1(i).nexadd~=link1(1)(1).add)
119
120
       i=i-1;
121
       j=1;
       if (i==1)
122
123
         j=1;
```

```
124
           while(link1(j).nexadd~=link1(1)(1).add)
             link2(j)=link1(j);
125
126
             j=j+1;
127
           end
128
           link2(j)=link1(j);
129
         link1(i-1).nexadd=link1(i+1).add;
130
         while(link1(j).nexadd~=link1(i+1).add)
131
           link2(j)=link1(j);
132
133
           j = j + 1;
134
        end
135
        if (j~=i-1)
           link2(j)=link1(j);
136
           link2(j+1)=link1(j+1);
137
138
           k=i+1;
139
           1 = 2;
140
        else
141
           link2(j)=link1(j);
142
           k=i+1;
           1=1;
143
144
        end
         while(link1(k).nexadd~=link1(1)(1).add)
145
           link2(j+1)=link1(k);
146
147
           k=k+1;
           1 = 1 + 1;
148
149
        end
         link2(j+1)=link1(k);
150
151
      end
152
      else
         if(i==pos)
153
154
           j=1;
           link1(i-1).nexadd=link1(1)(1).add;
155
           while (j \le i - 1)
156
             link2(j)=link1(j);
157
158
             j=j+1;
159
           end
160
        end
161
      end
```

```
162 end
163 end
164
165 endfunction
166 function[sta]=push(ele, stack)
167
      if (stack.top==0)
168
        stack.a=ele;
        stack.top=stack.top+1;
169
        sta=stack;
170
171
      else
172
        i=1;
173
        link1=struct('data',0,'add',0,'nexadd',0);
174
        while(i<=stack.top)</pre>
          link1=append(stack.a(i),link1);
175
176
          i=i+1;
177
        end
        link1=append(ele,link1);
178
179
        stack.top=stack.top+1;
        a=[stack.a(:,:) link1(stack.top).data];
180
181
        stack.a=a;
182
        sta=stack;
183
      end
184 endfunction
185 function[ele,sta]=pop(stack)
      ele=-1;
186
187
      sta=0;
      if (stack.top==0)
188
        disp("Stack Underflow");
189
190
        return;
191 else
192
        link1=struct('data',0,'add',0,'nexadd',0);
193
194
        while(i <= stack.top)</pre>
          link1=append(stack.a(i),link1);
195
          i=i+1;
196
        end
197
198
        ele=link1(stack.top).data;
199
        link1=delete1(stack.top,link1);
```

```
200
        stack.top=stack.top-1;
201
        i=2;
202
        a=link1(1)(1).data
        while(i<=stack.top)</pre>
203
204
          a=[a(:,:) link1(i).data];
205
          i=i+1;
206
        end
207
        stack.a=a;
208
        sta=stack;
209
210 endfunction
211 function[stack] = empty()
      stack=struct('a',0,'top',0);
212
213 endfunction
214 // Calling Routine:
215 stack=empty()//Create an empty stack
216 stack=push(4,stack);
217 stack=push(55, stack);
218 stack=push(199, stack);
219 stack=push(363, stack);
220 [ele, stack] = pop(stack);
221 disp(stack, "After the above operations stack is:");
```

#### Scilab code Exa 4.6 Implementing Priority Queue Using Lists

```
9
       link2(1)=link1(1)(1);
10
     else
       if (link1(1)(1).nexadd==link1(1)(1).add)
11
          if (ele>=link1(1)(1).data)
12
13
            t=ele;
14
            p=link1(1)(1).data;
15
          else
            t=link1(1)(1).data;
16
17
            p=ele;
18
19
          link1(1)(1).data=t;
20
          lin2=link1(1)(1);
21
          lin2.data=p;
22
          lin2.add=2;
23
          lin2.nexadd=link1(1)(1).add;
          link1(1)(1).nexadd=lin2.add;
24
25
          link2(1)=link1(1)(1);
26
          link2(2)=lin2;
27
       else
28
          i=1;
29
          a = [];
30
          while(link1(i).nexadd~=link1(1)(1).add)
            a=[a(:,:) link1(i).data];
31
32
            i=i+1;
33
34
          a=[a(:,:) link1(i).data];
35
          a=gsort(a);
36
          j=1;
37
          while(j<=i)</pre>
            link1(j).data=a(j);
38
39
            j = j + 1;
40
          end
41
          k=1:
          while(link1(k).data>=ele)
42
            if (link1(k).nexadd==link1(1)(1).add)
43
44
              break;
45
            else
              link2(k)=link1(k);
46
```

```
47
              k=k+1;
48
            end
49
          end
           if (link1(k).nexadd~=link1(1)(1).add)
50
51
             lin2=link1(k);
52
             lin2.data=ele;
53
             lin2.add=link1(k).add;
54
             j=k;
             y=link1(1)(1).add;
55
             while(link1(k).nexadd~=y)
56
               link1(k).add=link1(k).add+1;
57
58
               link1(k).nexadd=link1(k).nexadd+1;
59
               k=k+1;
60
             end
             link1(k).add=link1(k).add+1;
61
62
             lin2.nexadd=link1(j).add;
             link2(j)=lin2;
63
64
             j=j+1;
             while (j \le k+1)
65
               link2(j)=link1(j-1);
66
67
               j=j+1;
             end
68
69
           else
             lin2=link1(k);
70
             lin2.data=ele;
71
72
             lin2.nexadd=link1(1)(1).add;
73
             lin2.add=link1(k).add+1;
             link1(k).nexadd=lin2.add;
74
             j=1;
75
             while(j<=k)</pre>
76
               link2(j)=link1(j);
77
78
               j = j + 1;
79
             end
             link2(j)=lin2;
80
81
82
         end
83
      end
    endfunction
84
```

```
function[ele,link2] = extract_min(link1);
85
86
      link2=list
         87
      i=1;
      ele=-1;
88
      if (link1(1)(1).add==0)
89
        disp("Underflow");
90
        return;
91
92
      else
         if (link1(1)(1).nexadd==link1(1)(1).add)
93
          link1(1)(1).add=0;
94
95
          link1(1)(1).nexadd=0;
96
          ele=link1(1)(1).data;
97
          link1(1)(1).data=0;
          link2(1)=link1(1)(1);
98
99
        else
100
          i=1;
          while(link1(i).nexadd~=link1(1)(1).add)
101
102
            link2(i)=link1(i);
103
            i=i+1;
104
          end
105
          ele=link1(i).data;
          link2(i-1).nexadd=link2(1).add;
106
107
         end
108
      end
109
    endfunction
    // Calling Routine:
110
    link1=struct('data',0,'add',0,'nexadd',0);
111
112
    link1=insert_pri(3,link1);
    link1=insert_pri(4,link1);
113
114
    link1=insert_pri(22,link1);
115
    link1=insert_pri(21,link1);
    link1=insert_pri(11,link1);
116
    disp(link1, "List After Insertions");
117
    [ele,link1] = extract_min(link1)
118
119
    disp(ele, "Element after the min extraction");
```

# Chapter 5

## Trees

Scilab code Exa 5.1 Implementing Binary Tree

```
2 funcprot(0);
3 function[tree]=maketree(x)
     tree=zeros(30,1);
     for i=1:30
5
        tree(i) = -1;
6
     tree(1)=x;
9
     tree(2) = -2;
10 endfunction
11 function[tree1] = setleft(tree, tre, x)
     tree1=[];
12
13
     i=1;
     while(tree(i)~=-2)
14
15
       if(tree(i) == tre)
16
          j=i;
17
        end
18
        i = i + 1;
19
     end
20
     if(i>2*j)
       tree(2*j)=x;
21
```

```
22
     else
23
        tree(2*j)=x;
       tree(2*j+1)=-2;
24
       for l=i:2*j-1
25
26
          tree(i)=-1;
27
        end
28
     end
29
     tree1=tree;
30 endfunction
31 function[tree1] = setright(tree, tre, x)
32
     tree1=[];
33
     i=1;
34
     while(tree(i)~=-2)
        if(tree(i) == tre)
35
36
          j=i;
37
        end
38
        i=i+1;
39
     end
40
     if(i>2*j+1)
       tree(2*j+1)=x;
41
42
     else
43
        tree(2*j+1)=x;
       tree(2*j+2)=-2;
44
45
        for l=i:2*j
          tree(i) = -1;
46
47
        end
48
     end
49
     tree1=tree;
50 endfunction
51 function[x]=isleft(tree,tre)
52
     i=1;
     x=0;
53
     while(tree(i)~=-2)
54
       if(tree(i)==tre)
55
56
          j=i;
        end
57
        i=i+1;
58
59
     end
```

```
60
     if(i>=2*j)
        if ((tree(2*j)~=-1) | (tree(2*j)~=-2))
61
62
          x=1;
63
          return 1;
64
        else
65
          return 0;
66
        end
67
     else
68
        x = 0;
69
        return x;
70
     end
71 endfunction
72 function[x]=isright(tree,tre)
73
     i=1;
74
     x = 0;
     while(tree(i)~=-2)
75
        if(tree(i) == tre)
76
77
          j=i;
78
        end
79
        i=i+1;
80
     end
     if(i>=2*j+1)
81
        if ((tree(2*j+1)~=-1)|(tree(2*j+1)~=-2))
82
83
          x=1;
84
          return 1;
85
        else
86
          return 0;
87
        end
     else
88
89
        x = 0;
90
        return x;
91
     end
92 endfunction
93 // Calling Routine:
94 tree=maketree(3);
95 disp(tree, "Tree made");
96 tree=setleft(tree,3,1);
97 disp(tree, "After setting 1 to left of 3");
```

```
98 tree=setright(tree,3,2);
99 disp(tree,"After setting 2 to right of 3");
100 tree=setright(tree,2,4);
101 tree=setleft(tree,2,5);
102 tree=setright(tree,1,6);
103 tree=setright(tree,5,8);
104 disp(tree,"After above operations:");
105 x=isright(tree,3);
106 disp(x,"Checking for the right son of 3 yes if 1 else no");
107 x=isleft(tree,2);
108 disp(x,"Check for left son of 2");
```

### Scilab code Exa 5.2 Tree Trversal Techniques

```
1 funcprot(0);
2 function[tree] = maketree(x)
     tree=zeros(30,1);
3
     for i=1:30
4
       tree(i) = -1;
5
     end
     tree(1)=x;
     tree(2) = -2;
8
9 endfunction
10 function[tree1] = setleft(tree, tre, x)
     tree1=[];
11
12
     i=1;
     while(tree(i)~=-2)
13
14
       if (tree(i) == tre)
15
          j=i;
16
       end
17
       i=i+1;
18
     end
19
     if(i>2*j)
       tree(2*j)=x;
20
```

```
21
     else
22
        tree(2*j)=x;
       tree(2*j+1)=-2;
23
       for l=i:2*j-1
24
25
          tree(i)=-1;
26
        end
27
     end
28
     tree1=tree;
29 endfunction
30 function[tree1] = setright(tree, tre, x)
31
     tree1=[];
32
     i=1;
33
     while(tree(i)~=-2)
        if(tree(i) == tre)
34
35
          j=i;
36
        end
37
        i=i+1;
38
     end
39
     if(i>2*j+1)
       tree(2*j+1)=x;
40
41
     else
42
        tree(2*j+1)=x;
       tree(2*j+2)=-2;
43
44
        for l=i:2*j
          tree(i) = -1;
45
46
        end
47
     end
48
     tree1=tree;
49 endfunction
50 function[x]=isleft(tree, tre)
     i=1;
51
     x=0;
52
     while(tree(i)~=-2)
53
       if(tree(i)==tre)
54
55
          j=i;
       end
56
57
        i=i+1;
58
     end
```

```
59
     if(i>=2*j)
        if ((tree(2*j)~=-1)|(tree(2*j)~=-2))
60
61
          x=1;
62
          return 1;
63
        else
64
          return 0;
65
        end
66
      else
67
        x = 0;
68
        return x;
69
      end
70 endfunction
71 function[x]=isright(tree,tre)
72
     i=1;
73
     x = 0;
     while(tree(i)~=-2)
74
        if(tree(i) == tre)
75
76
          j=i;
77
        end
78
        i=i+1;
79
     end
80
      if(i>=2*j+1)
        if ((tree(2*j+1)~=-1)|(tree(2*j+1)~=-2))
81
82
          x=1;
83
          return 1;
84
        else
85
          return 0;
86
        end
87
     else
88
        x = 0;
89
        return x;
90
      end
91 endfunction
92 funcprot(0);
93 function[]=inorder(tree,p)
     if(tree(p) == -1 | tree(p) == -2)
94
95
        return;
96
     else
```

```
97
        inorder(tree,2*p);
        printf("%d\t", tree(p));
98
        inorder(tree,2*p+1);
99
100
      end
101 endfunction
102 function[]=preorder(tree,p)
      if(tree(p) == -1 | tree(p) == -2)
103
104
        return:
105
      else
106
        printf("%d\t", tree(p));
107
        preorder(tree,2*p);
108
        preorder(tree,2*p+1);
109
      end
110 endfunction
111 function[]=postorder(tree,p)
      if(tree(p) == -1 | tree(p) == -2)
112
        return;
113
114
      else
        postorder(tree,2*p);
115
        postorder(tree,2*p+1);
116
117
        printf("%d\t", tree(p));
118
      end
119 endfunction
120 // Calling Routine:
121 tree=maketree(3);
122 tree=setleft(tree,3,1);
123 tree=setright(tree,3,2);
124 tree=setleft(tree,2,4);
125 tree=setright(tree,2,5);
126 disp("Inorder traversal");
127 inorder(tree,1);
128 disp("Preorder traversal");
129 preorder (tree,1);
130 disp("Postorder traversal");
131 postorder(tree,1);
```

Scilab code Exa 5.3 Implementing And traversing a Binary Search Tree

```
1 funcprot(0);
2 function[tree] = maketree(x)
     tree=zeros(1,30);
3
4
     for i = 1:30
        tree(i) = -1;
6
     end
     tree(1)=x;
     tree(2) = -2;
9 endfunction
10 function[tree1] = setleft(tree, tre, x)
11
     tree1=[];
12
     i=1;
     while(tree(i)~=-2)
13
        if(tree(i)==tre)
14
15
          j=i;
16
        \quad \text{end} \quad
17
        i=i+1;
18
     end
     if(i>2*j)
19
20
        tree(2*j)=x;
21
     else
       tree(2*j)=x;
22
23
        tree(2*j+1)=-2;
       for l=i:2*j-1
24
          tree(i)=-1;
25
26
        end
27
     end
     tree1=tree;
29 endfunction
30 function[tree1] = setright(tree, tre, x)
31
     tree1=[];
32
     i=1;
```

```
33
     while(tree(i)~=-2)
        if (tree(i) == tre)
34
          j=i;
35
36
        end
37
        i=i+1;
38
     end
     if(i>2*j+1)
39
40
        tree(2*j+1)=x;
41
     else
42
       tree(2*j+1)=x;
        tree(2*j+2)=-2;
43
44
        for l=i:2*j
45
          tree(i)=-1;
        end
46
47
     end
48
     tree1=tree;
49 endfunction
50 function[x]=isleft(tree,tre)
51
     i=1;
52
     x = 0;
53
     while(tree(i)~=-2)
        if(tree(i) == tre)
54
55
          j=i;
56
        end
57
        i=i+1;
58
     end
     if(i>=2*j)
59
        if ((tree(2*j)~=-1)|(tree(2*j)~=-2))
60
61
          x=1;
62
          return 1;
63
        else
          return 0;
64
65
        end
66
     else
        x = 0;
67
68
        return x;
69
     end
70 endfunction
```

```
71 function[x]=isright(tree,tre)
72
      i=1;
73
      x=0;
      while(tree(i)~=-2)
74
75
        if (tree(i) == tre)
76
           j=i;
77
        end
78
        i=i+1;
79
      end
80
      if(i>=2*j+1)
        if((tree(2*j+1)~=-1)|(tree(2*j+1)~=-2))
81
82
           x=1;
83
           return 1;
84
        else
85
           return 0;
86
        end
87
      else
        x = 0;
88
89
        return x;
90
      end
91 endfunction
92 funcprot(0);
93 function[]=inorder(tree,p)
      if(tree(p) == -1 | tree(p) == -2)
94
95
        return;
96
      else
        inorder(tree,2*p);
97
        disp(tree(p)," ");
98
99
        inorder(tree,2*p+1);
100
      end
101 endfunction
102 function[]=preorder(tree,p)
      if(tree(p) == -1 | tree(p) == -2)
103
104
        return;
105
      else
        disp(tree(p)," ");
106
107
        preorder(tree,2*p);
108
        preorder(tree,2*p+1);
```

```
109
      end
110 endfunction
111 function[]=postorder(tree,p)
      if(tree(p) == -1 | tree(p) == -2)
112
113
         return;
114
      else
         postorder(tree,2*p);
115
         postorder(tree,2*p+1);
116
         disp(tree(p)," ");
117
118
      end
119 endfunction
120 function[tree1]=binary(tree,x)
121
      while (tree (p) =-1&tree (p) =-2)
122
123
         q=p;
124
         if(tree(p)>x)
125
           p=2*p;
126
         else
127
           p=2*p+1;
128
         end
129
      end
130
      i=1;
      while(tree(i)~=-2)
131
132
         i=i+1;
133
      end
      if(tree(q)>x)
134
         if(i==2*q)
135
           tree(2*q)=x;
136
137
           tree(2*q+1)=-2
138
         else
           if(i<2*q)</pre>
139
140
              tree(i)=-1;
              tree(2*q+1)=-2;
141
142
              tree(2*q)=x;
143
           end
144
         \quad \text{end} \quad
145
146
      else
```

```
if(i==2*q+1)
147
          tree(2*q+1)=x;
148
          tree(2*q+2)=-2;
149
150
        else
151
          if(i<2*q+1)
152
            tree(i)=-1;
            tree (2*q+1)=x;
153
            tree(2*q+2)=-2;
154
155
          end
156
        end
157
158
      end
159
      tree1=tree;
160 endfunction
161 // Calling Routine:
162 tree=maketree(3);
163 tree=binary(tree,1);
164 tree=binary(tree,2);
165 tree=binary(tree,4);
166 tree=binary(tree,5);
167 disp(tree, "Binary tree thus obtaine by inserting
       1,2,4 and5 in tree rooted 3 is:");
```

### Scilab code Exa 5.4 Checking the duplicate number using BST

```
1 function[tree1]=binary(tree,x)
2
     while (tree(p)^{-}=-1\&tree(p)^{-}=-2)
3
4
        q=p;
5
        if(tree(p)>x)
6
          p=2*p;
7
        else
8
          p=2*p+1;
9
        end
10
     end
```

```
11
     if(tree(q)>x)
        if(tree(2*q)==-2)
12
          tree(2*q)=x;
13
          tree(2*q+1)=-2;
14
15
        else
          tree(2*q)=x;
16
17
        end
18
     else
        if(tree(2*q+1) == -2)
19
          tree (2*q+1)=x;
20
          tree(2*q+2)=-2;
21
22
23
          tree (2*q+1)=x;
24
        end
25
     end
26
     tree1=tree;
27 endfunction
28 funcprot(0);
29 function[tree]=maketree(x)
     tree=zeros (40,1);
30
31
     for i = 1:40
32
        tree(i) = -1;
33
     end
34
     tree(1)=x;
35
     tree (2) = -2;
36 endfunction
37 function[]=duplicate1(a,n)
     tree=maketree(a(1));
38
39
     q=1;
40
     p=1;
41
     i=2;
     x=a(i)
42
43
     while(i<n)
        while (tree (p) =x\&tree(q)=-1\&tree(q)=-2)
44
45
          p=q;
          if(tree(p)<x)</pre>
46
47
            q=2*p;
48
          else
```

```
49
            q=2*p+1;
50
         end
       end
51
       if(tree(p) == x)
52
         disp(x," Duplicate ");
53
54
         tree=binary(tree,x);
55
56
       end
57
       i=i+1;
58
       x=a(i);
59
     end
     while(tree(p)~=x&tree(q)~=-1&tree(q)~=-2)
60
61
62
         if(tree(p) < x)
63
            q=2*p;
64
         else
65
            q=2*p+1;
66
         end
67
       end
       if(tree(p)==x)
68
         disp(x," Duplicate ");
69
70
       else
71
          tree=binary(tree,x);
72
       end
73 endfunction
74 // Calling Adress:
75 a=[22 11 33 22 211 334]
76 duplicate1(a,6)
77 a=[21 11 33 22 22 334]
78 duplicate1(a,6)
```

# Chapter 6

# Sorting

### Scilab code Exa 6.1 Bubble Sort

```
1 function[a1]=bubble(a,n)
     i=1;
3
     j=1;
     temp=0;
     for i=1:n-1
      for j=1:n-i
6
         if(a(j)>a(j+1))
8
            temp=a(j);
            a(j)=a(j+1);
9
10
            a(j+1) = temp;
11
12
         j=j+1;
13
       end
14
       i=i+1;
15
     end
16
     disp(a1, "Sorted array is:");
17
18 endfunction
19 // Calling Routine:
20 a=[23 21 232 121 2324 1222433 1212]
21 disp(a, "Given Array");
```

## Scilab code Exa 6.2 Quick Sort

```
1 function[a1] = quick(a);
     a=gsort(a);//IN BUILT QUICK SORT FUNCTION
     n=length(a);
3
     a1=[];
4
5
    for i=1:n
       a1=[a1(:,:) a(n+1-i)];
6
7
     disp(a1, "Sorted array is:");
9 endfunction
10 // Calling Routine:
11 a=[23 21 232 121 2324 1222433 1212]
12 disp(a, "Given Array");
13 a1=quick(a)
```

### Scilab code Exa 6.3 Selection Sort

```
1 function[a1] = selection(a,n)
2
     i=n;
     while (i \ge 1)
3
4
        large=a(1);
        indx=1;
5
       for j=1:i
6
          if(a(j)>large)
7
8
            large=a(j);
9
            indx=j;
10
          end
        end
11
12
        a(indx)=a(i);
13
        a(i)=large;
```

```
14    i=i-1;
15    end
16    a1=a;
17    disp(a1, "Sorted array is:");
18    endfunction
19    // Calling Routine:
20    a=[23 21 232 121 2324 1222433 1212]
21    disp(a, "Given Array");
22    a1=selection(a,7)
```

#### Scilab code Exa 6.4 Insertion Sort

```
1 function[a1]=insertion(a,n)
2
     for k=1:n
       y=a(k);
3
4
       i=k;
5
       while(i>=1)
6
          if (y < a(i))</pre>
7
            a(i+1)=a(i);
8
            a(i)=y;
9
          end
10
          i=i-1;
11
       end
12
     end
13
     a1=a;
     disp(a1, "Sorted array is:");
14
15 endfunction
16 // Calling Routine:
17 a=[23 21 232 121 2324 1222433 1212]
18 disp(a, "Given Array");
19 a1=insertion(a,7)
```

Scilab code Exa 6.5 Shell sort

```
function[a1] = shell(a,n,incr,nic)
2
     for i=1:nic
3
       span=incr(i);
       for j=span+1:n
4
5
          y=a(j);
6
          k=j-span;
          while (k \ge 1 \& y \le a(k))
7
              a(k+span)=a(k);
8
9
            k=k-span;
10
          end
11
          a(k+span)=y;
12
       end
13
     end
14
     a1=a;
     disp(a1, "Sorted array is:");
15
16 endfunction
17 // Calling Routine:
18 a=[23 21 232 121 2324 1222433 1212]
19 disp(a, "Given Array");
20 incr=[5 \ 3 \ 1]/must always end with 1
21 a1=shell(a,7,incr,3)
```

## Scilab code Exa 6.6 Merge Sort

```
function[a1] = mergesort(a,p,r)
2
     if(p<r)</pre>
3
        q=int((p+r)/2);
4
        a=mergesort(a,p,q);
        a=mergesort(a,q+1,r);
5
6
        a=merge(a,p,q,r);
7
     else
8
        a1=a;
9
        return;
10
     end
11
     a1=a;
```

```
12 endfunction
13 function[a1]=merge(a,p,q,r)
     n1=q-p+1;
14
15
     n2=r-q;
16
     left=zeros(n1+1);
17
     right=zeros(n2+1);
18
     for i=1:n1
19
       left(i)=a(p+i-1);
20
     end
     for i1=1:n2
21
22
         right(i1) = a(q+i1);
23
24
     left(n1+1)=999999999;
25
     right(n2+1)=999999999;
26
     i=1;
27
     j=1;
28
     k=p;
29
     for k=p:r
30
       if (left(i) <= right(j))</pre>
         a(k)=left(i);
31
32
         i=i+1;
33
       else
34
         a(k)=right(j);
         j=j+1;
35
36
       end
37
     end
38
     a1=a;
39 endfunction
40 // Calling Routine:
41 a=[23 21 232 121 26324 1222433 14212]
42 disp(a, "Given Array");
43 a1=mergesort(a,1,7)
44 disp(a1, "Sorted array is:");
45 a=[232 11212 3443 23221 123424 32334 12212 2443 232]
46 disp(a, "Given Array");
47 a1=mergesort(a,1,9);
48 disp(a1, "Sorted Array");
```

## Scilab code Exa 6.7 Binary Tree Sort

```
1 function[tree1] = binary(tree,x)
     p=1;
     while (tree (p) =-1&tree(p)=-2)
3
4
       q=p;
5
       if(tree(p)>x)
6
         p=2*p;
7
       else
8
         p=2*p+1;
9
       end
10
     end
11
     if(tree(q)>x)
          tree(2*q)=x;
12
13
     else
          tree (2*q+1)=x;
14
15
     end
16
     tree1=tree;
17 endfunction
18 funcprot(0);
19 function[tree] = maketree(x)
     tree=zeros(100,1);
20
     for i=1:100
21
       tree(i) = -1;
22
23
     end
24
     tree(1)=x;
     tree(2) = -2;
25
26 endfunction
27 function[]=inorder(tree,p)
     if(tree(p) == -1 | tree(p) == -2)
29
       return;
     else
30
        inorder(tree,2*p);
31
       printf("%d\t", tree(p));
32
```

```
inorder(tree,2*p+1);
33
34
     end
35 endfunction
36 function[]=binsort(a,n)
37
     a1=maketree(a(1))
     for i=2:n
38
       a1=binary(a1,a(i));
39
40
    end
     disp("Sorted array is:");
41
     inorder(a1,1);
43 endfunction
44 // Calling Routine:
45 a=[23 21 232 121 2324 1222433 1212]
46 disp(a, "Given Array");
47 a1=binsort(a,7)
```

# Chapter 7

# Searching

## Scilab code Exa 7.1 Sequential Search

```
1 function[] = search(a,n,ele)
2
     i=1;
3
     j=0;
     for i=1:n
       if(a(i) == ele)
         printf("Found %d AT %d\n",ele,i);
         j=1;
8
       end
9
     end
     if(j==0)
10
       disp("%d NOT FOUND", ele);
11
12
     end
13 endfunction
14 // Calling Routine:
15 a=[2 33 22 121 23 233 222]
16 disp(a, "Given array");
17 search(a,7,23)
```

Scilab code Exa 7.2 Sorted sequential search

```
1 function[] = sortedsearch(a,n,ele)
     if(a(1)>ele|a(n)<ele)</pre>
3
       disp("NOT IN THE LIST");
4
     else
5
       i=1;
6
       j=0;
7
       for i=1:n
          if(a(i) == ele)
8
9
            printf("FOUND %d AT %d",ele,i);
10
          else
11
12
            if(a(i)>ele)
13
              break;
14
            end
15
          end
16
       end
17
       if(j==0)
          disp("%d NOT FOUND", ele);
18
19
       end
20
     end
21 endfunction
22 // Calling Routine:
23 a=[2 22 23 33 121 222 233]//a should be sorted
24 disp(a, "Given array");
25 search(a,7,23)
```

## Scilab code Exa 7.3 Binary Search

```
break;
9
       else
         if(a(mid)>i)
10
11
          h=mid-1;
12
         else
13
           l=mid+1;
14
         end
15
       end
16
     end
17 endfunction
18 // Calling Routine:
19 a=[2 22 23 33 121 222 233]//a should be sorted
20 disp(a, "Given array");
21 search(a,7,23)
```

# Chapter 8

# Graphs

## Scilab code Exa 8.1 Simple Graph Functions

```
1 //Simple Graph Functions
2 function[]=graph();
3
     i=1, j=1;
     adj=zeros (10000);
     for i=1:n
6
     for j=1:n
8
         adj((i-1)*n+j)=temp;
9
10
       end
11
     end
12
     for i=1:n
13
       for j=1:n
14
         if ((adj((i-1)*n+j))==1)
           printf("Vertex %d is connected to vertex %d\
15
              n",i,j);
16
         end
17
       end
18
     end
19
20 endfunction
```

Scilab code Exa 8.2 Finding The Number Of Paths From One Vertex-ToOther

```
1 // Finding The Number Of Paths From One Vertex To
      Another Of A Given Length
2
3
   function[b] = path(k,n,adj,i,j)
     b=0;
4
     if(k==1)
5
       b=adj((i-1)*n+j);
6
7
     else
8
       for c=1:n
9
         if(adj((i-1)*n+c)==1)
           b=b+path(k-1,n,adj,c,j);
10
11
12
       end
13
     end
14
       printf("Number of paths from vertex %d to %d of
          length %d are %d",i,j,k,b);
15
     return b;
16
  endfunction
17
  // Calling Routine:
18 n=3;
19 adj=[0 1 1 0 0 1 0 0 0]
20 b=path(1,n,adj,1,3)
```

Scilab code Exa 8.3 Finding The Number Of Simple Paths From One Point

1 // Finding The Number Of Simple Paths From One Point To Another In A Given Graph

```
2 funcprot(0)
3 function[]=sim_path(n,adj,i,j);
5
     m=1;
6
     for m=1:n
       l=l+path(m,n,adj,i,j);
8
     end
     printf ("There are %d simple paths from %d to %d
9
        in the given graph\n",1,i,j);
10 endfunction
  function[b] = path(k, n, adj, i, j)
12
     b=0;
13
     if(k==1)
       b=adj((i-1)*n+j);
14
15
     else
16
       for c=1:n
         if(adj((i-1)*n+c)==1)
17
           b=b+path(k-1,n,adj,c,j);
18
19
         end
20
       end
21
     end
22
     return b;
23 endfunction
24 n=3;
25 adj=[0 1 1 0 0 1 0 0 0];
26 b=sim_path(n,adj,1,3)
```

### Scilab code Exa 8.4 Finding Transitive Closure

```
//Finnding Transitive Closure
funcprot(0)
function[path]=Tranclose(adj,n);
i=1,j=1;
path=zeros(n*n,1);
path=tranclose(adj,n);
```

```
printf("Transitive Closure Of Given Graph is:\n");
  7
                    for i=1:n
  8
  9
                             printf("For Vertex %d\n",i);
10
                             for j=1:n
                                     printf(" %d %d is %d n",i,j,path((i-1)*n+j));
11
12
                             end
13
                    end
14
15 endfunction
16 function[path]=tranclose(adj,n)
17
                    adjprod=zeros(n*n,1);
18
                    k=1;
19
                    newprod=zeros(n*n,1);
20
                    for i=1:n
21
                             for j=1:n
22
                                     path((i-1)*n+j)=adj((i-1)*n+j);
23
                                     adjprod((i-1)*n+j)= path((i-1)*n+j);
24
                             end
25
                    end
26
                    for i=1:n
27
                             newprod=prod1(adjprod,adj,n);
28
                             for j=1:n
29
                                     for k=1:n
                                             path((j-1)*n+k)=path((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k)|newprod((j-1)*n+k
30
                                                         -1)*n+k);
31
                                     end
32
                             end
33
                             for j=1:n
34
                                     for k=1:n
                                              adjprod((j-1)*n+k)=newprod((j-1)*n+k);
35
36
                                     end
37
                             end
38
                    end
39 endfunction
40 function[c]=prod1(a,b,n)
                    for i=1:n
41
42
                             for j=1:n
                                     val=0
43
```

```
44
         for k=1:n
45
           val=val | (a((i-1)*n+k)&b((k-1)*n+j));
46
         c((i-1)*n+j)=val;
47
48
       end
49
     end
50 endfunction
51 // Calling Routine:
52 n=3;
53 adj=[0 1 0 0 0 1 0 0 0]
54 path=Tranclose(adj,n)
```

## Scilab code Exa 8.5 Warshalls Algorithm

```
1 //Warshall's Algorithm
2 funcprot(0)
3 function[path]=transclose(adj,n)
     for i = 1 : n
4
       for j=1:n
5
         path((i-1)*n+j)=adj((i-1)*n+j);
6
7
       end
8
     end
9
     for k=1:n
10
       for i=1:n
11
         if(path((i-1)*n+k)==1)
12
           for j=1:n
13
              path((i-1)*n+j)=path((i-1)*n+j)|path((k-1)
                 *n+j);
14
           end
15
         end
16
       end
17
     printf("Transitive closure for the given graph is
18
        :\n");
19
     for i=1:n
```

## Scilab code Exa 8.6 Depth First Search Traversal

```
1 //Depth First Search Traversal
2 funcprot(0)
3 function[]=Dfs(adj,n);
     i=1, j=1;
     colour=[];
5
     for i=1:n
6
     for j=1:n
         colour=[colour(:,:) 0];
9
       end
10
     end
     disp("The DFS traversal is");
11
12 dfs(adj,colour,1,n);
13 endfunction
14 function[] = dfs(adj,colour,r,n)
     colour(r)=1;
15
     disp(r," ");
16
     for i=1:n
17
       if (adj((r-1)*n+i)&(colour(i)==0))
18
         dfs(adj,colour,i,n);
19
20
       end
21
     end
22
     colour(r)=2;
```

```
23 endfunction

24 // Calling Routine:

25 n=4;

26 adj=[0 1 1 0 0 0 0 1 0 0 0 1 0 0 0]

27 Dfs(adj,n)
```

## Scilab code Exa 8.7 BFS Traversal

```
1 ///BFS Traversal
2 funcprot(0)
3 function[q2]=push(ele,q1)
     if (q1.rear == q1.front)
5
       q1.a=ele;
6
       q1.rear=q1.rear+1;
       q1.a=[q1.a(:,:) ele];
8
9
       q1.rear=q1.rear+1;
10
     end
11
     q2=q1;
12 endfunction
13 function[ele,q2]=pop(q1)
14
     ele=-1;
15
     q2 = 0;
     if (q1.rear == q1.front)
16
17
            return;
18
     else
19
       ele=q1.a(q1.rear-q1.front);
20
       q1.front=q1.front+1;
21
       i=1;
22
       a=q1.a(1);
       for i=2:(q1.rear-q1.front)
23
         a=[a(:,:) q1.a(i)];
24
25
       end
26
       q1.a=a;
27
     end
```

```
28
     q2 = q1;
29 endfunction
30
31 function[]=Bfs(adj,n);
32
     i=1, j=1;
33
     colour=[];
34
     for i=1:n
     for j=1:n
35
          colour=[colour(:,:) 0];
36
37
38
     end
39
     disp("The BFS Traversal is");
40 bfs(adj,colour,1,n);
41 endfunction
42 function [] = bfs(adj,colour,s,n)
     colour(s)=1;
43
     q=struct('rear',0,'front',0,'a',0);
44
     q=push(s,q);
45
     while((q.rear)-(q.front)>0)
46
       [u,q]=pop(q);
47
       disp(u," ");
48
       for i=1:n
49
          if (adj((u-1)*n+i)&(colour(i)==0))
50
            colour(i)=1;
51
            q=push(i,q);
52
53
          end
54
       end
       colour(u)=2;
55
56
57 endfunction
58 // Calling Routine:
59 n = 4;
60 adj=[0 1 1 0 0 0 0 1 0 0 0 1 0 0 0]
61 Bfs(adj,n)
```

## Scilab code Exa 8.8 Dijkstras Algorithm

```
1 // Dijkstras Algorithm
2 funcprot(0)
3 function[l]=short(adj,w,i1,j1,n)
     for i=1:n
5
        for j=1:n
          if(w((i-1)*n+j)==0)
6
            w((i-1)*n+j)=9999;
7
8
9
        end
10
     end
11
12
     distance=[];
     perm = [];
13
     for i=1:n
14
15
        distance=[distance(:,:) 99999];
16
        perm = [perm(:,:) 0];
17
     end
18
     perm(i1)=1;
19
     distance(i1)=0;
20
     current=i1;
     while(current~=j1)
21
22
        smalldist=9999;
        dc=distance(current);
23
        for i=1:n
24
          if (perm(i) == 0)
25
            newdist=dc+w((current-1)*n+i);
26
27
            if (newdist < distance(i))</pre>
28
               distance(i)=newdist;
29
            if (distance(i) < smalldist)</pre>
30
31
               smalldist=distance(i);
32
              k=i;
33
            end
34
          end
35
        end
        current=k;
36
```

```
37     perm(current)=1;
38     end
39     l=distance(j1);
40     printf("The shortest path between %d and %d is %d
        ",i1,j1,1);
41     endfunction
42     // Calling Routine:
43     n=3;
44     adj=[0 1 1 0 0 1 0 0 0]//Adjacency List
45     w=[0 12 22 0 0 9 0 0 0]//weight list fill 0 for no
          edge
46     short(adj,w,1,3,n);
```