Scilab Textbook Companion for Heat Transfer (In SI Units) by J. P. Holman¹

Created by
Shivam Singh
B.Tech
Chemical Engineering
IT BHU
College Teacher
Prakash Kotecha
Cross-Checked by

August 10, 2013

¹Funded by a grant from the National Mission on Education through ICT, http://spoken-tutorial.org/NMEICT-Intro. This Textbook Companion and Scilab codes written in it can be downloaded from the "Textbook Companion Project" section at the website http://scilab.in

Book Description

Title: Heat Transfer (In SI Units)

Author: J. P. Holman

Publisher: Tata McGraw - Hill Education, New Delhi

Edition: 9

Year: 2002

ISBN: 0-07-063451-3

Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

Contents

Lis	List of Scilab Codes		
1	Introduction	8	
2	Steady State Conduction One Dimension	13	
3	Steady State Conduction Multiple Dimension	28	
4	Unsteady State Conduction	47	
5	Principles of Convection	64	
6	Empirical and Practical Relations for Forced Convection Heat Transfer	80	
7	Natural Convection Systems	99	
8	Radiation Heat Transfer	116	
9	Condensation and Boiling Heat Transfer	158	
10	Heat Exchangers	164	
11	Mass Transfer	198	

List of Scilab Codes

Exa 1.1	conduction through copper plate
Exa 1.2	convection calculation
Exa 1.3	multimode heat transfer
Exa 1.4	heat source and convection
Exa 1.5	radiation heat transfer
Exa 1.6	total heat loss by convection and radiation
Exa 2.1	multilayer conduction
Exa 2.2	multilayer cylindrical system
Exa 2.3	heat transfer through a composite wall
Exa 2.4	overall heat transfer coefficient for a tube
Exa 2.5	critical insulation thickness
Exa 2.6	heat source with convection
Exa 2.7	influence of thermal conductivity on fin temperature
	profiles
Exa 2.8	straight aluminium fin
Exa 2.9	circumferential aluminium fin
Exa 2.10	rod with heat sources
Exa 2.11	influence of contact conductance on heat transfer 26
Exa 3.1	buried pipe
Exa 3.2	cubical furnace
Exa 3.3	buried disk
Exa 3.4	buried parallel disk
Exa 3.5	Nine node problem
Exa 3.6	Gauss seidal calculation
Exa 3.7	numerical formulation with heat generation 35
Exa 3.8	heat generation with non uniform nodal elements 38
Exa 3.11	use of variable mesh size
Exa 3.12	Three dimensional numerical formulation 44

Exa 4.1	steel ball cooling in air	17
Exa 4.2	Semi infinite solid with sudden change in surface condi-	
		18
Exa 4.3		19
Exa 4.4	-	50
Exa 4.5	sudden exposure of semi infinite solid slab to convection 5	51
Exa 4.6	•	53
Exa 4.7		54
Exa 4.8	9 · 1	56
Exa 4.9		57
Exa 4.10		59
Exa 4.12		31
Exa 5.1		64
Exa 5.2		35
Exa 5.3		66
Exa 5.4	· · · · · · · · · · · · · · · · · · ·	67
Exa 5.5		38
Exa 5.6	-	70
Exa 5.7		71
Exa 5.8		72
Exa 5.9	-	74
Exa 5.10	_	75
Exa 5.11		75
Exa 6.1	turbulent heat transfer in a tube	30
Exa 6.2	heating of water in laminar tube flow	31
Exa 6.3		33
Exa 6.4	heating of air with isothermal tube wall	35
Exa 6.5	heat transfer in a rough tube	36
Exa 6.6		38
Exa 6.7	airflow across isothermal cylinder	39
Exa 6.8		90
Exa 6.9		92
Exa 6.10	heating of air with in line tube bank	93
Exa 6.11		95
Exa 6.12	heating of liquid bismuth in tube	97
Exa 7.1		99
Exa 7.2	heat transfer from isothermal vertical plate 10)1
Exa 7.3	heat transfer from horizontal tube in water 10	12

Exa 7.4	heat transfer from fine wire in air	103
Exa 7.5	heated horizontal pipe in air	104
Exa 7.6	cube cooling in air	105
Exa 7.7	calculation with simplified relations	106
Exa 7.8	heat transfer across vertical air gap	108
Exa 7.9	heat transfer across horizontal air gap	109
Exa 7.10	heat transfer across water layer	110
Exa 7.11	reduction of convection in ar gap	111
Exa 7.12	heat transfer across evacuated space	113
Exa 7.13	combined free and forced convection with air	114
Exa 8.1	transmission and absorption in a gas plate	116
Exa 8.2	heat transfer between black surfaces	117
Exa 8.3	shape factor algebra for open ends of cylinder	118
Exa 8.4	shape factor algebra for truncated cone	119
Exa 8.5	shape factor algebra for cylindrical reflactor	121
Exa 8.6	hot plates enclosed by a room	122
Exa 8.7	surface in radiant balance	124
Exa 8.8	open hemisphere in large room	126
Exa 8.9	effective emissivity of finned surface	128
Exa 8.10	heat transfer reduction with parallel plate shield	129
Exa 8.11	open cylindrical shield in large room	130
Exa 8.12	network for gas radiation between parallel plates	132
Exa 8.13	cavity with transparent cover	134
Exa 8.14	Transmitting and reflecting system for furnace opening	134
Exa 8.15	numerical solution for enclosure	137
Exa 8.16	numerical solution for parallel plates	139
Exa 8.17	radiation from a hole with variable radiosity	142
Exa 8.18	heater with constant heat flux and surrounding shields	146
Exa 8.19	numerical solution for combined convection and radia-	
	tion non linear system	151
Exa 8.20	solar environment equilibrium temperatures	154
Exa 8.21	influence of convection on solar equilibrium temperature	155
Exa 8.23	temperature measurement error caused by radiation .	156
Exa 9.1	condensation on vertical plate	158
Exa 9.2	condensation on tube tank	159
Exa 9.3	boiling on brass plate	160
Exa 9.4	Flow boiling	161
Exa 9.5	water boiling in a pan	162

Exa 9.6	heat flux comparisons	163
Exa 10.1	overall heat transfer coefficient for pipe in air	164
Exa 10.2	overall heat transfer coefficient for pipe exposed to steam	166
Exa 10.3	influence of fouling factor	168
Exa 10.4	calculation of heat exchanger size from known temper-	
	atures	169
Exa 10.5	shell and tube heat exchanger	170
Exa 10.6	design of shell and tube heat exchanger	171
Exa 10.7	cross flow exchanger with one fluid mixed	173
Exa 10.8	effects of off design flow rates for exchanger in previous	
	example	174
Exa 10.9	off design calculation using E NTU method	176
Exa 10.10	off design calculation of exchanger in example 10 4	177
Exa 10.11	cross flow exchanger with both fluid unmixed	179
Exa 10.12	comparison of single or two exchanger options	181
Exa 10.13	shell and tube exchangeras air heater	184
Exa 10.14	ammonia condenser	185
Exa 10.15	crossflow exchanger as energy conservation device	186
Exa 10.16	heat transfer coefficient in compact exchanger	189
Exa 10.17	transient response of thermal energy storage system .	190
Exa 10.18	variable properties analysis of a duct heater	194
Exa 11.1	diffusion coefficient for co2	198
Exa 11.2	diffusion coefficient for co2	199
Exa 11.3	Wet bulb temperature	199
Exa 11.4	relative humidity of air stream	200
Exa 11.5	water evaporation rate	201

Chapter 1

Introduction

Scilab code Exa 1.1 conduction through copper plate

Scilab code Exa 1.2 convection calculation

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 1.2\n \n");
4 // convection calculation
5 // illustration1.2
6 // solution
8 Twall = 250; // [degree celsius] wall temperature
9 Tair = 20; // [degree celsius] air temperature
10 h = 25; // [W/square meter] heat transfer coefficient
11 1 = 75*10^{(-2)}; // [m] length of plate
12 b = 50*10^{(-2)}; // [m] width of plate
13 area = 1*b; //[square meter] area of plate
14 dt = 250-20; // [degree celsius]
15 // from newton's law of cooling
16 q = h*area*dt; // [W]
17 printf("rate of heat transfer is %f kW",q/1000);
```

Scilab code Exa 1.3 multimode heat transfer

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 1.3\n\n\n");
4 // multimode heat transfer
5 // illustration1.3
6 // solution
7
8 Qconv = 2156; // [W] from previous problem
9 Qrad = 300; // [W] given
10 dx = 0.02; // [m] plate thicknesss
11 l = 0.75; // [m] length of plate
12 w = 0.5; // [m] width of plate
13 k = 43; // [W/m] from table 1.1
14 area = l*w; // [square meter] area of plate
15 Qcond = Qconv+Qrad; // [W]
```

```
16 dt = Qcond*dx/(k*area);// [degree celsius]
        temperature difference
17 Ti = 250+dt;// inside temperature
18 printf("the inside plate temperature is therefore %f degree celsius",Ti);
```

Scilab code Exa 1.4 heat source and convection

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 1.4 \n\n");
4 // heat source and convection
5 // illustration1.4
6 // solution
8 d = 1*10^(-3); //[m] diameter of wire
9 1 = 10*10^{(-2)}; //[m] length of wire
10 Sarea = 22*d*1/7; // [square meter] surface area of
     wire
11 h = 5000; // [W/square meter] heat transfer
      coefficient
12 Twall = 114;// [degree celsius]
13 Twater = 100; // [degree celsius]
14 //total convection loss is given by equation (1-8)
15 Q = h*Sarea*(Twall-Twater); // [W]
16 printf("heat transfer is therefore %f W",Q);
17 printf(" this is equal to the electric power which
     must be applied");
```

Scilab code Exa 1.5 radiation heat transfer

```
1 clear;
2 clc;
```

Scilab code Exa 1.6 total heat loss by convection and radiation

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 1.6\n \n \);
4 // total heat loss by convection and radiation
5 // illustration1.6
6 // solution
8 d = 0.05; //[m] diameter of pipe
9 Twall = 50; // [degree celsius]
10 Tair = 20; // [degree celsius]
11 emi = 0.8; // emissivity
12 h = 6.5; // [W/square meter] heat transfer coefficient
       for free convection
13 Q1 = h*22*d*(Twall-Tair)/7; //[W/m] convection loss
      per unit length
14 sigma = 5.669*10^{(-8)}; // [W/square meter*k^{(4)}]
      universal constant
15 T1 = 273.15+Twall; // [k]
16 T2 = 273.15 + Tair; // [k]
```

Chapter 2

Steady State Conduction One Dimension

Scilab code Exa 2.1 multilayer conduction

```
1 clear;
3 printf("\t\t\Example Number 2.1\n\n");
4 // multilayer conduction
5 // illustration 2.1
6 // solution
8 dx1 = 0.1; // [m] thickness of layer of common brick
  k1 = 0.7; // [W/m degree celsius] heat transfer
     coefficient of common brick
10 dx2 = 0.0375; // [m] thickness of layer of gypsum
      plaster
11 k2 = 0.48; // [W/m degree celsius] heat transfer
     coefficient gypsum plaster
12 Rb = dx1/k1; // [square meter degree celsius /W]
     thermal resistance of brick
13 Rp = dx2/k2; // [square meter degree celsius /W]
     thermal resistance of gypsum plaster
14 R = Rb+Rp; // [square meter degree celsius /W]
```

```
thermal resistance without insulation

15 R1 = R/0.2; // [square meter degree celsius /W] with insulation

16 // heat loss with the rock-wool insulation is 20 percent

17 Rrw = R1-R; // [square meter degree celsius /W]

18 k3 = 0.065; // [W/m degree celsius] heat transfer coefficient

19 dx3 = Rrw*k3; // [m]

20 printf("length of thickness is %f cm added to reduce the heat loss(or gain) through wall by 80 percent", dx3*100);
```

Scilab code Exa 2.2 multilayer cylindrical system

```
1 clear;
2 \text{ clc};
3 printf("\t\tExample Number 2.2 \ln n);
4 // multilayer cylindrical system
5 // illustration 2.2
6 // solution
8 ID = 0.02; // [m] inner diameter of steel
9 OD = 0.04; //[m] outer diameter of steel
10 t = 0.03; //[m] thickness of asbestos insulation
11 // system is like three concentric cylinders
12 T1 = 600; // [degree celsius] inside wall temperature
13 T2 = 100; // [degree celsius] outside insulation
      temperature
14 Ks = 19; // [W/m degree celsius] heat transfer
      coefficient of steel
15 Ka = 0.2; // [W/m degree celsius] heat transfer
      coefficient of asbestos
16 // heat flow is given by per unit length
17 \ Q_1 = ((2*22*(T1-T2)/7)/((\log(OD/ID)/Ks)+(\log(0.1/OD)/Ks))
```

```
)/Ka)));// [W/m]

18 // above calculated heat flow is used to calculate
    the interface temperature

19 // between the outside wall and the insulation
20 Ta = Q_1*(log(0.1/OD)/(2*3.14*Ka))+T2;// [degree
    celsius] Ta is interface temperature
21 printf("heat flow is given by %f W/m",Q_1);
22 printf("\n the interface temperature is %f degree
    celsius ",Ta);
```

Scilab code Exa 2.3 heat transfer through a composite wall

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 2.3 \n\n");
4 // heat transfer through a composite wall
5 // illustration 2.3
6 // solution
8 // 1. heat transfer through studs for unit depth
9 1 = 0.0413; // [m] length of wood studs
10 b = 1.0; // [m] unit depth
11 A = l*b; // [square meter] area of studs for unit
     depth
12
  hi = 7.5; // [W/square meter per degree celsius]
      convectional heat transfer coefficient
13 ho = 15; // [W/square meter per degree celsius]
     convectional heat transfer coefficient
14 Kb = 0.69; // [W/m per degree celsius] heat transfer
     coefficient of brick
15 Kgi = 0.96; // [W/m per degree celsius] heat transfer
      coefficient of gypsum inner sheath
16 Ki = 0.04; // [W/m per degree celsius] heat transfer
      coefficient of insulation
17 Kws = 0.1; // [W/m per degree celsius] heat transfer
```

```
coefficient of wood stud
18 Kgo = 0.48; // [W/m per degree celsius] heat transfer
       coefficient of gypsum outer sheath
19 Rair = 1/(ho*A); // [degree celsius /W] convection
      resistance outside of brick
20 \text{ dx_b} = 0.08; // [m] \text{ thickness of brick}
21 \text{ dx_os} = 0.019; //[m] \text{ thickness of outer sheet}
22 \text{ dx_ws} = 0.0921; // [m] \text{ thickness of wood stud}
23 \text{ dx_is} = 0.019; // [m] \text{ thickness of inner sheet}
24 Rb = dx_b/(Kb*A); // [degree celsius /W] conduction
      resistance in brick
  Ros = dx_os/(Kgi*A); // [degree celsius /W]
      conduction resistance through outer sheet
26 Rws = dx_ws/(Kws*A);// [degree celsius /W]
      conduction resistance through wood stud
  Ris = dx_is/(Kgo*A);// [degree celsius /W]
      conduction resistance through inner sheet
  Ri = 1/(hi*A); // [degree celsius /W] convection
      resistance on inside
  Rt = Rair+Rb+Ros+Rws+Ris+Ri;// [degree celsius /W]
      total thermal resistance through the wood stud
      section
30 printf ("total thermal resistance through the wood
      stud section is %f degree celsius /W", Rt);
31 // 2. heat transfer through insulation section
32 A1 = 0.406-A; // [square meter] area of insulation
      section for unit depth
33 \text{ dx_ins} = 0.0921; // [m] \text{ thickness of insulation}
34 Rins = dx_ins/(Ki*A1);// [degree celsius /W]
      conduction resistance through insulation section
35 // five of the materials are same but resistance
      involve different area
36 // i.e. (40.6-4.13) cm instead of 4.13 cm
37 // so that each of the previous must be multiplied
      by a factor of (4.13/(40.6-4.13)) = 0.113
38 Rt_ins = (Rair+Rb+Ros+Ris+Ri)*0.113+Rins;// [degree
      celsius /W total resistance through insulation
```

section

```
39 printf("\n total thermal resistance through the
      insulation section is %f degree celsius /W',
     Rt_ins);
40 R_overall = 1/((1/Rt)+(1/Rt_ins)); // [degree celsius]
      W overall resistance for the section
41 // the value is related to overall heat transfer
      coefficient by
42 // Q = U*A*dt = dt/R_overall
43 // where A is area of total section
44 A<sub> = </sub> = 0.406; // [square meter] area of total section
45 U = 1/(R_{overall*A_{i}}); // [W/square meter degree]
      celsius] overall heat transfer coefficient
  // R value is somewhat different from thermal
46
      resistance and is given by
47 R_value = 1/U; // [degree celsius square meter/W] R
      value of system
48 printf("\n overall heat transfer coefficient is %f W
     /square meter per degree celsius",U);
49 printf("\n R value is %f square meter/W', R_value);
```

Scilab code Exa 2.4 overall heat transfer coefficient for a tube

```
12 L = 1.0; // [m] tube length
13 Ai = %pi*ID*L; // [square meter] inside crossectional
14 Ao = %pi*OD*L;// [square meter] outside
      crossectional area
15 k = 16; // [W/square meter per degree celsius]
     thermal conductivity of tube
16 Ri = 1/(hi*Ai); // [degree celsius /W] convection
      resistance inside tube
  Rt = \log(OD/ID)/(2*3.14*k*L); // [degree celsius /W]
     thermal resistance
18 Ro = 1/(ho*Ao); // [degree celsius /W] convection
      resistance outside tube
19 R_total = Ri+Rt+Ro; // [degree celsius /W] total
     thermal and convection resistance
20 Uo = 1/(Ao*R_total); // [W/square meter degree
      celsius] overall heat transfer coefficient
21 printf("overall heat transfer coefficient is %f W/
      square meter degree celsius", Uo);
22 Tw = 50; // [degree celsius] water temperature
23 Ta = 20; // [degree celsius] surrounding air
     temperature
24 dt = Tw-Ta; // [degree celsius] temperature
      difference
25 q = Uo*Ao*dt; // [W] heat transfer
26 printf("\n heat loss per unit length is %f W(for 1m
     length)",q);
```

Scilab code Exa 2.5 critical insulation thickness

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 2.5\n\n\n");
4 // critical insulation thickness
5 // illustration2.5
```

```
6 // solution
8 k = 0.17; // [W/m per degree celsius] heat transfer
      coefficient of asbestos
9 Tr = 20; // [degree celsius] temperature of room air
10 h = 3; // [W/square meter per degree celsius]
      convectional heat transfer coefficient
11 Tp = 200; // [degree celsius] temperature of pipe
12 d = 0.05; // [m] diameter of pipe
13 // from equation (2-18) we calculate r<sub>o</sub> as
14 r_o = k/h; // [m] critical radius of insulation
15 printf ("critical radius of insulation for asbestos
      is %f cm ",r_o*100);
16 Ri = d/2; // [m] inside radius of insulation
17 // heat transfer is calculated from equation (2-17)
18 \quad q_by_L = (2*3.14*(Tp-Tr))/(((log(r_o/Ri))/0.17)+(1/(
     h*r_o)));// [W/m] heat transfer per unit length
19 printf("\n heat loss when covered with critical
      radius of insulation is %f W/m",q_by_L);
20 // without insulation the convection from the outer
      surface of pipe is
21 \text{ q_by_L1} = h*2*3.14*Ri*(Tp-Tr); // [W/m] convection
     from outer surface without insulation
22 printf("\n heat loss without insulation is %f W/m",
      q_by_L1);
23 per_inc = ((q_by_L-q_by_L1)/q_by_L1)*100; //
      percentage increase in heat transfer
24 printf("\n so the addition of 3.17 of insulation
      actually increases the heat transfer by %f
      percent", per_inc);
```

Scilab code Exa 2.6 heat source with convection

```
1 clear;
2 clc;
```

```
3 printf("\t\t\tExample Number 2.6\n\n'");
4 // heat source with convection
5 // illustration 2.6
6 // solution
8 // all the power generated in the wire must be
      dissipated by convection to the liquid
9 // P = i^{(2)} *R = q = h*A*dt
10 L = 100; // [cm] length of the wire
11 k = 19; // [W/m per degree celsius] heat transfer
      coefficient of steel wire
12 A = \%pi*(0.15)^(2);// [square meter] crossectional
     area of wire
13 rho = 70*10^{(-6)}; // [micro ohm cm] resistivity of
     steel
14 R = rho*L/A;// [ohm] resistance of wire
15 i = 200; // [ampere] current in the wire
16 P = i^(2)*R; // [W] power generated in the wire
17 Tl = 110; // [degree celsius] liquid temperature
18 d = 0.003; // [m] diameter of wire
19 l = 1; // [m] length of wire
20 Tw = (P/(4000*3.14*d*1))+110; // [degree celsius]
      wire temperature
21 // heat generated per unit volume q_dot is
      calculated as
22 / P = q_dot*V = q_dot*3.14*r^(2)*l
23 r = d/2; // [m] radius of wire
24 q_dot = P/(\%pi*r^{(2)}*1); //[W/m^{(3)}]
25 // finally the center temperature of the wire is
      calculated from equation (2-26)
26 To = ((q_dot*(r^(2)))/(4*k))+Tw; // [degree celsius]
27 printf ("center temperature of the wire is %f degree
      celsius", To);
```

Scilab code Exa 2.7 influence of thermal conductivity on fin temperature profiles

```
1 clear;
2 clc;
3 printf("\t\tExample Number 2.7 \ln n);
4 // influence of thermal conductivity on fin
     temperature profiles
  // illustration 2.7
6 // solution
8 d = 0.02; // [m] diameter of rod
9 L = 0.1; // [m] length of rod
10 A = \%pi*d^(2)/4;// [square meter] crossectional area
       of rod
11 h = 25; // [W/square meter per degree celsius]
     convectional heat transfer coefficient
12 k_c = 385; // [W/m per degree celsius] heat transfer
      coefficient of copper
13 k_s = 17; // [W/m per degree celsius] heat transfer
      coefficient of steel
14 k_g = 0.8; // [W/m per degree celsius] heat transfer
      coefficient of glass
15 // calculating (h*P/(k*A)) and m and m*L for three
      different rod
16 P = \%pi*d; // [m] perimeter of rod
17 printf("Material\t(hP/kA)\t\tm\t\tmL");
18 printf("\ncopper\t\t\f\t\f\t\t\f\f\",(h*P/(k_c*A)),((h*
     P/(k_c*A)))^(1/2),((h*P/(k_c*A)))^(1/2)*L);
19 printf("\nstainless steel\t\%f\t\%f\t\%f\, (h*P/(k_s*A))
      ((h*P/(k_s*A)))^(1/2),((h*P/(k_s*A)))^(1/2)*L);
  printf("\nglass\t\t\%f\t\%f\t\%f\",(h*P/(k_g*A)),((h*P/(
20
     k_g*A)))^(1/2),((h*P/(k_g*A)))^(1/2)*L);
21 //
22 Lc = L+d/4; // [m] corrected length
23 // the parameters of interest for the heat flow and
      efficiency comparisons are now tabulated as
24 printf("\nthe parameters of interest for the heat
```

```
flow and efficiency comparisons are now tabulated
                  as");
25 printf("\nMaterial\tt(hPkA)\ttmLc");
26 printf("\ncopper\t\t\f\f\t\t\f\f\",(h*P*k_c*A),((h*P/(k_c
               *A)))^(1/2)*Lc);
27 printf("\nstainless steel\t\%f\t\t\%f",(h*P*k_s*A),((h
               *P/(k_s*A)))^(1/2)*Lc);
      printf("\nglass\t\t\f\f\t\t\f\f\",(h*P*k_g*A),((h*P/(k_g*
               A)))^(1/2)*Lc);
      // efficiency is calculated using equation (2-38) by
               using the above values of mLc
      // to compare the heat flows we could either
               calculate the values from equation (2-36) for a
               unit value of theta_o
31 printf("\nMaterial\t\tefficiency\tq relative to
               copper percentage");
32 printf("\ncopper\t\t\f\f\t\t\f\f\", tanh(((h*P/(k_c*A)))
                (1/2)*Lc)/(((h*P/(k_c*A)))^(1/2)*Lc),100);
33 printf("\nstainless steel\t\%f\t\t\%f", tanh(((h*P/(k_s
               *A)))^(1/2)*Lc)/(((h*P/(k_s*A)))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh))^(1/2)*Lc),((tanh
               (((h*P/(k_s*A)))^(1/2)*Lc)/(((h*P/(k_s*A)))^(1/2)
               *Lc))/(tanh(((h*P/(k_c*A)))^(1/2)*Lc)/(((h*P/(k_c*A)))^(1/2)*Lc))/(((h*P/(k_c*A)))^(1/2)*Lc)/(((h*P/(k_c*A)))^(1/2)*Lc)/(((h*P/(k_c*A)))^(1/2)*Lc)/(((h*P/(k_c*A)))^(((h*P/(k_c*A)))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^(((h*P/(k_c*A))))^((((h*P/(k_c*A))))^(((h*P/(k_c*A))))^((((h*P/(k_c*A))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A))))))^((((h*P/(k_c*A)))))^((((h*P/(k_c*A))))))))
               *A)))^(1/2)*Lc)))*100);
34 printf("\nglass\t\t\f\f\t\t\f\f\", tanh(((h*P/(k_g*A)))
               (1/2)*Lc)/(((h*P/(k_g*A)))^(1/2)*Lc),((tanh(((h*
               P/(k_g*A)))^(1/2)*Lc)/(((h*P/(k_g*A)))^(1/2)*Lc))
               /(tanh(((h*P/(k_c*A)))^(1/2)*Lc)/(((h*P/(k_c*A))))
               ^(1/2)*Lc)))*100);
     deff('[y]=f1(x)', 'y=exp(-((h*P/(k_c*A)))^(1/2)*x)
               /(1+\exp(-2*((h*P/(k_c*A)))^(1/2)*L))+\exp(((h*P/(
               k_c * A)))^(1/2) * x)/(1+exp(2*((h*P/(k_c*A)))^(1/2)*
               L))');
36 deff('[y]=f2(x)', 'y=exp(-((h*P/(k_s*A)))^(1/2)*x)
               /(1+\exp(-2*((h*P/(k_s*A)))^(1/2)*L))+\exp(((h*P/(
               k_s*A)))^(1/2)*x)/(1+exp(2*((h*P/(k_s*A)))^(1/2)*
               L))');
37 deff('[y]=f3(x)', 'y=exp(-((h*P/(k_g*A)))^(1/2)*x)
               /(1+\exp(-2*((h*P/(k_g*A)))^(1/2)*L))+\exp(((h*P/(
```

```
k_g*A)))^(1/2)*x)/(1+exp(2*((h*P/(k_g*A)))^(1/2)*
L))');

38     x=0:0.01:0.1;

39     plot(x,f1,x,f2,x,f3);
40     legend("copper, k = 385 W/m degree celsius","
          stainless steel k = 17 W/m degree celsius"," glass k = 0.8 W/m degree celsius");

41     xlabel("x,m");
42     ylabel("theta / theta_O");
43     xgrid();
```

Scilab code Exa 2.8 straight aluminium fin

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 2.8\n \n \);
4 // straight aluminium fin
5 // illustration 2.8
6 // solution
7
8 t = 0.003; // [m] thickness of fin
9 L = 0.075; // [m] length of fin
10 Tb = 300; // [degree celsius] base temperature
11 Tair = 50; // [degree celsius] ambient temperature
12 k = 200; // [W/m per degree celsius] heat transfer
      coefficient of aluminium fin
13 h = 10; // [W/square meter per degree celsius]
     convectional heat transfer coefficient
14 // We Will use the approximate method of solution by
       extending the fin
15 // With a fictitious length t/2
16 // using equation (2-36)
17 Lc = L+t/2; // [m] corrected length
18 z = 1; // [m] unit depth
19 p = (2*z+2*t); // [m] perimeter of fin
```

Scilab code Exa 2.9 circumferential aluminium fin

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 2.9\n \n \);
4 // circumferential aluminium fin
5 // illustration 2.9
6 // solution
8 t = 0.001; // [m] thickness of fin
9 L = 0.015; // [m] length of fin
10 Ts = 170; // [degree celsius] surface temperature
11 Tfluid = 25; // [degree celsius] fluid temperature
12 k = 200; // [W/m per degree celsius] heat transfer
     coefficient of aluminium fin
13 h = 130; // [W/square meter per degree celsius]
     convectional heat transfer coefficient
14 d = 0.025; // [m] tube diameter
15 Lc = L+t/2; // [m] corrected length
16 r1 = d/2; // [m] radius of tube
17 r2_c = r1+Lc;// [m] corrected radius
18 Am = t*(r2_c-r1); [square meter] profile area
19 c = r2_c/r1; // constant to determine efficiency of
      fin from curve
20 c1 = ((Lc)^{(1.5)})*((h/(k*Am))^{(0.5)}; // constant to
```

```
determine efficiency of fin from curve

// using c and c1 to determine the efficiency of the fin from figure (2-12)

// we get nf = 82 percent

// heat would be transferred if the entire fin were at the base temperature

// both sides of fin exchanging heat

// both sides of fin exchanging heat

// max = 2*%pi*(r2_c^(2)-r1^(2))*h*(Ts-Tfluid);// [W] maximum heat transfer

// q_act = 0.82*q_max;// [W] actual heat transfer

// printf("the actual heat transferred is %f W",q_act);
```

Scilab code Exa 2.10 rod with heat sources

```
1 clear:
   2 clc;
   3 printf("\t\t\Example Number 2.10\n\n'");
   4 // rod with heat sources
   5 // illustration 2.10
   6 // solution
   8 // q_dot is uniform heat source per unit volume
  9 // h is convection coefficient
10 // k is heat transfer coefficient
11 // A is area of crossection
12 // P is perimeter
13 // Tinf is environment temperature
14 // we first make an energy balance on the element of
                           the rod shown in figure (2-10)
15 // energy in left place + heat generated in element
                           = energy out right face + energy lost by
                        convection
16 // or
17 // -(k*A*dT_by_dx) + (q_dot*A*dx) = -(k*A(dT_by_dx) + (q_dot*A*dx)) =
                        d2T_by_dx^2 + dx^2 + h*P*dx*(T-Tinf)
```

```
18 // simlifying we have
19 // d2T_by_dx^2 - ((h*P)/(k*A))*(T_Tinf)+q_dot/k = 0
20 // replacing theta = (T-Tinf) and (square meter) =
      ((h*P)/(k*A))
21 // d2theta_by_dx2 -(square meter)*theta+q_dot/k = 0
22 // we can make a further substitution as theta =
      theta -(q_dot/(k*(square meter)))
23 // so that our differential equation becomes
\frac{24}{\sqrt{d2}} d2theta '_by_dx2 -(square meter)*theta '
25 // which has the general solution theta = C1*exp^(-
     m*x)+C2*exp^(m*x)
  // the two end temperatures are used to establish
      the boundary conditions:
  // theta ' = theta1 ' = T1-Tinf-q_dot/(k*(square meter))
      ) = C1+C2
  // theta ' = theta2 ' = T2-Tinf-q_dot/(k*(square meter))
      (-m*L)+C2*exp^(m*L)
29 // solving for the constants C1 and C2 gives
30 // (((theta1 *exp^(2*m*L)-theta2 *exp^(m*L))*exp^(-m))
      *x) + ((theta2 'exp^(m*L) - theta1 ') exp^(m*x)) / (exp^(m*x)) = (theta2 'exp^(m*L) - theta1 ') exp^(m*x)
      (2*m*L)-1)
31 printf("the expression for the temperature
      distribution in the rod is ");
32 printf("\n theta' = (((theta1'*exp^(2*m*L)-theta2'*
      \exp^{(m*L)} \exp^{(-m*x)} + ((theta2 \cdot exp^{(m*L)} - theta1)
      ') \exp (m*x) / (\exp (2*m*L) - 1)'');
33 printf("\n for an infinitely long heat generating
      fin with the left end maintained at T1, the
      temperature distribution becomes ");
34 printf("\n theta'/theta1 = \exp^(-m*x)");
```

Scilab code Exa 2.11 influence of contact conductance on heat transfer

```
1 clear;
2 clc;
```

```
3 printf("\t\t\tExample Number 2.11\n\n");
4 // influence of contact conductance on heat transfer
5 // illustration 2.11
6 // solution
8 d = 0.03; //[m] diameter of steel bar
9 1 = 0.1; //[m] length of steel bar
10 A = (\%pi*d^(2))/4; [square meter] crossectional
     area of bar
11 k = 16.3; // [W/square meter per degree celsius]
      thermal conductivity of tube
12 hc = 1893.93; // [W/square meter per degree celsius]
      contact coefficient
13 // the overall heat flow is subjected to three
     thermal resistances
14 // one conduction resistance for each bar
15 // contact resistance
16 Rth = 1/(k*A); // [degree celsius /W]
17 // from table (2-2) the contact resistance is
18 Rc = 1/(hc*A); // [degree celsius /W]
19 Rt = 2*Rth+Rc; // [degree celsius /W] total
      resistance
20 dt = 100; // [degree celsius] temperature difference
21 q = dt/Rt;// [W] overall heat flow
22 printf("overall heat flow is %f W",q);
23 // temperature drop across the contact is found by
      taking the ratio
24 // of the contact resistance to the total thermal
      resistance
25 \text{ dt_c} = (\text{Rc/(2*Rth)})*\text{dt}; // [\text{degree celsius}]
26 printf("\nthe temperature drop across the contact is
      %f degree celsius", dt_c);
```

Chapter 3

Steady State Conduction Multiple Dimension

Scilab code Exa 3.1 buried pipe

```
1 clear;
3 printf("\t\t\Example Number 3.1\n\n");
4 // buried pipe
5 // illustration 3.1
6 // solution
8 d = 0.15; // [m] diameter of pipe
9 r = d/2;// [m] radius of pipe
10 L = 4; // [m] length of pipe
11 Tp = 75; // [degree celsius] pipe wall temperature
12 Tes = 5; // [degree celsius] earth surface
     temperature
13 k = 0.8; // [W/m per degree celsius] thermal
     conductivity of earth
14 D = 0.20; // [m] depth of pipe inside earth
15 // We may calculate the shape factor for this
     situation using equation given in table 3-1
16 // since D < 3*r
```

```
17 S = (2*%pi*L)/acosh(D/r);// [m] shape factor
18 // the heat flow is calculated from
19 q = k*S*(Tp-Tes);// [W]
20 printf("heat lost by the pipe is %f W",q);
```

Scilab code Exa 3.2 cubical furnace

```
1 clear;
2 clc;
3 printf("\t\tExample Number 3.2 \ln n);
4 // cubical furnace
5 // illustration 3.2
6 // solution
8 a = 0.5; // [m] length of side of cubical furnace
9 Ti = 500; // [degree celsius] inside furnace
     temperature
10 To = 50; // [degree celsius] outside temperature
11 k = 1.04; // [W/m per degree celsius] thermal
     conductivity of fireclay brick
12 t = 0.10; // [m] wall thickness
13 A = a*a; // [square meter] area of one face
14 // we compute the total shape factor by adding the
     shape factors for the walls, edges and corners
15 Sw = A/t; // [m] shape factor for wall
16 Se = 0.54*a; // [m] shape factor for edges
17 Sc = 0.15*t; // [m] shape factor for corners
18 // there are six wall sections, twelve edges and
     eight corners, so the total shape factor S is
19 S = 6*Sw+12*Se+8*Sc; // [m]
20 // the heat flow is calculated as
21 q = k*S*(Ti-To); // [W]
22 printf("heat lost through the walls is %f kW",q
     /1000);
```

Scilab code Exa 3.3 buried disk

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 3.3 \n\n\n");
4 // buried disk
5 // illustration3.3
6 // solution
8 d = 0.30; // [m] diameter of disk
9 r = d/2; // [m] radius of disk
10 Td = 95; // [degree celsius] disk temperature
11 Ts = 20; // [degree celsius] isothermal surface
     temperature
12 k = 2.1; // [W/m per degree celsius] thermal
     conductivity of medium
13 D = 1.0; // [m] depth of disk in a semi-infinite
     medium
14 // We have to calculate shape factor using relation
     given in table (3-1)
15 // We select the relation for the shape factor is
     for the case D/(2*r)>1
16 S = (4*\%pi*r)/((\%pi/2)-atan(r/(2*D)));//[m] shape
     factor
17 // heat lost by the disk is
18 q = k*S*(Td-Ts); // [W]
19 printf("heat lost by disk is %f W",q);
```

Scilab code Exa 3.4 buried parallel disk

```
1 clear;
2 clc;
```

```
3 printf("\t\tExample Number 3.4 \ln n);
4 // buried parallel disk
5 // illustration 3.4
6 // solution
8 d = 0.50; // [m] diameter of both disk
9 r = d/2; // [m] radius of disk
10 Td1 = 80;// [degree celsius] first disk temperature
11 Td2 = 20;// [degree celsius] second disk temperature
12 k = 2.3; // [W/m per degree celsius] thermal
     conductivity of medium
13 D = 1.5; // [m] separation of disk in a infinite
     medium
14 // We have to calculate shape factor using relation
     given in table (3-1)
15 // We select the relation for the shape factor is
     for the case D>5*r
16 S = (4*\%pi*r)/((\%pi/2)-atan(r/D));//[m] shape
     factor
17 q = k*S*(Td1-Td2); // [W]
18 printf("heat transfer between the disks is %f W",q);
```

Scilab code Exa 3.5 Nine node problem

```
10 dx = 1/3; // [m] length of small squares in x
      direction
11 dy = 1/3; // [m] length of small squares in y
      direction
12 y = h*dx/(k); // to use in equation (3-25) and (3-26)
13 // the nodal equation for nodes is following
14 / T2 + T4 - 4 * T1 = -600 \text{ FOR NODE } 1
15 / T3+T1+T5-4*T2 = -500 \text{ FOR NODE } 2
16 / 2*T2+T6-4.67*T3 = -567 \text{ FOR NODE } 3
17 // T5+T7+T1-4*T4 = -100 FOR NODE 4
18 / T6+T4+T8+T2-4*T5 = 0 FOR NODE 5
19 / 2*T5+T3+T9-4.67*T6 = -67 FOR NODE 6
20 / / 2*T4+T8-4.67*T7 = -167 FOR NODE 7
21 // 2*T5+T7+T9-4.67*T8 = -67 FOR NODE 8
22 / T6+T8-2.67*T9 = -67 \text{ FOR NODE } 9
23 A = \begin{bmatrix} -4 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & -4 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 2 & -4 & .67 \end{bmatrix}
       0 0 1 0 0 0;1 0 0 -4 1 0 1 0 0;0 1 0 1 -4 1 0 1
      0;0 0 1 0 2 -4.67 0 0 1;0 0 0 2 0 0 -4.67 1 0;0 0
       0\ 0\ 2\ 0\ 1\ -4.67\ 1; 0\ 0\ 0\ 0\ 1\ 0\ 1\ -2.67];
24 \text{ C} = [-600; -500; -567; -100; 0; -67; -167; -67; -67];
25 T = A^(-1)*C; // [degree celsius]
26 printf ("The nodal temperature of node 1 to 9 is
      shown below respectively");
27 disp(T);
28 // the heat flows at the boundaries are computed in
      two ways:
  // as conduction flows for the 100 and 500 degree
      celsius faces and
30 // as convection flows for the other two faces
31 // for the 500 degree face the heat flow into the
      face is q = sigma(k*dx*dT/dy)
  // where dt is temperature difference and dy is
      length of small squares in y direction
33 q = k*dx*[500-T(1)+500-T(2)+(500-T(3))/2]/dy;//[W/m]
34 // the heat flow out of the 100 degree face is
      sigma(k*dy*dT/dx)
35 \text{ q1} = k*dy*[T(1)-100+T(4)-100+(T(7)-100)/2]/dx; // [W/
```

```
\mathbf{m}
36 // the convection heat flow out the right face is
      given by the convection relation q = sigma(h*dy*(
     T-Tinf)
37 \text{ q2} = h*dy*[T(3)-100+T(6)-100+(T(9)-100)/2]; // [W/m]
38 // the convection heat flow out the bottom face is
      given by the convection relation q = sigma(h*dx*(
     T-Tinf)
39 \quad q3 = h*dx*[(100-100)/2+T(7)-100+T(8)-100+(T(9)-100)]
      /2];// [W/m]
40 // total heat flow out is
41 \text{ qt} = q1+q2+q3;
42 printf(" heat conducted into the top face is %f W/m"
      ,q);
43 printf("\n total heat flow out is \%f W/m",qt);
44 printf("\n this compares that heat flow into the
      system is equal to the heat flow out of the
      system ");
```

Scilab code Exa 3.6 Gauss seidal calculation

```
node, we obtain (qi = 0)
11 // Ti = (\operatorname{sum} \operatorname{Kj} * \operatorname{Tj}) / (\operatorname{sum} \operatorname{Kj})
                                      (b)
12 // because each node has four resistances connected
       to it and k is assumed constant,
13 // \text{ sum Kj} = 4*k
14 // and
15 // Ti = (1/4)*(sum Tj)
                                           (c)
16 // we are now making four nadal equations for
       iteration
17 // node 1 : T1 = (1/4)*(100+500+T2+T3)
18 // node 2 : T2 = (1/4)*(500+100+T1+T4)
19 // node 3 : T3 = (1/4)*(100+100+T1+T4)
20 // node 3 : T4 = (1/4)*(T3+T2+100+100)
21 // we now set up an iteration table as shown in
       output
22 A = [4 -1 -1 0; -1 4 0 -1; -1 0 4 -1; 0 -1 -1 4];
23 b = [600; 600; 200; 200];
24 x = [300; 300; 200; 200];
25 NumIters=6;
26 D = diag(A);
27 \quad A = A - diag(D);
28 \text{ for } i=1:4
29
        D(i)=1/D(i);
30 \text{ end}
31 n = length(x);
32 x = x(:);
33 y=zeros(n, NumIters);
34 for j=1:NumIters
35
        for k=1:n
36
             x(k) = (b(k) - A(k, :) *x) *D(k);
37
        end
        y(:,j)=x;
38
40 printf("the iteration table is shown as : \n\n");
41 disp(y);
42 printf("\n after five iterations the solution
```

```
converges and the final temperatures are \n");
43 disp(y(1,6), "T1=");
44 disp(y(2,6), "T2=");
45 disp(y(3,6), "T3=");
46 disp(y(4,6), "T4=");
```

Scilab code Exa 3.7 numerical formulation with heat generation

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 3.7 \ln n);
4 // numerical formulation with heat generation
5 // \text{Example } 3.7 \text{ (page no.} -99-100)
6 // solution
8 d = 4; // [mm] diameter of wire
9 Q = 500; // [MW/cubic meter] heat generation
10 Tos = 200; // [degree celsius] outside surface
      temperature of wire
11 k = 19; // [W/m degree celsius] thermal conductivity
12 // we shall make the calculations per unit length
13 \, dz = 1;
14 // because the system is one-dimensional, we take
15 \text{ dphai} = 2*\%pi;
16 \, dr = 0.5; // [mm]
17 // a summary of values for different nodes are
      following
18
19 // node 1.
20
21 \text{ rm1} = 0.25; // [mm]
22 Rmplus1 = (dr/2)/((rm1+dr/4)*dphai*dz*k);// [degree]
      celsius /W]
23 // Rmminus1 = infinity
24 dV1 = rm1*dr*dphai*dz;// [cubic micro meter]
```

```
25 \text{ q1} = Q*dV1; // [W]
26
27 // node 2.
28
29 \text{ rm2} = 0.75; // [mm]
30 Rmplus2 = (dr/2)/((rm2+dr/4)*dphai*dz*k); // [degree]
      celsius/W
31 // Rmminus2 = infinity
32 dV2 = rm2*dr*dphai*dz; // [cubic micro meter]
33 \ q2 = Q*dV2; // [W]
34
35 // node 3.
36
37 \text{ rm3} = 1.25; // [mm]
38 Rmplus3 = (dr/2)/((rm3+dr/4)*dphai*dz*k);// [degree]
      celsius/W
39 // Rmminus3 = infinity
40 dV3 = rm3*dr*dphai*dz;// [cubic micro meter]
41 \text{ q3} = Q*dV3; // |W|
42
43 // node 4.
44
45 \text{ rm}4 = 1.75; // [mm]
46 Rmplus4 = (dr/2)/((rm4+dr/4)*dphai*dz*k);// [degree]
      celsius/W
47 // Rmminus1 = infinity
48 dV4 = rm4*dr*dphai*dz;// [cubic micro meter]
49 \text{ q4} = Q*dV4; // [W]
50
51 // a summary of values of sum_one_by_Rij and Ti
      according to equation (3-32) is now given to be
      used in gauss seidal iteration scheme
52
53 // node 1
54
55 sum_one_by_Rij1 = (1/Rmplus1); // [degree celsius/W]
56 // the equations formed after putting values are
57 // T1 = 3.288 + T2
```

```
58
59 // node 2
60
61 sum_one_by_Rij2 = (1/Rmplus2);// [degree celsius/W]
62 // the equations formed after putting values are
63 // T2 = 3.289 + (1/3) *T1 + (2/3) *T3
64
65 // node 3
66
67 sum_one_by_Rij3 = (1/Rmplus3);// [degree celsius/W]
68 // the equations formed after putting values are
69 / T3 = 3.290 + 0.4 * T2 + 06 * T4
70
71 // \text{ node } 4
72
73 sum_one_by_Rij4 = (1/Rmplus4); // [degree celsius/W]
74 // the equations formed after putting values are
75 // T4 = 2.193+(2/7)*T3+142.857
76
77 // now we will solve these equations by iteration
78 A = [1 -1 0 0; -(1/3) 1 -(2/3) 0; 0 -0.4 1 -0.6; 0 0
      -(2/7) 1];
79 b = [3.288; 3.289; 3.290; 142.857+2.193];
80 x = [240; 230; 220; 210];
81 NumIters=13;
82 D = diag(A);
83 A=A-diag(D);
84 n = length(x);
85 x = x(:);
86 y=zeros(n, NumIters);
87 for j=1:NumIters
88
       for z=1:n
            x(z) = (b(z) - A(z, :) *x) *D(z);
89
90
       end
91
       y(:,j)=x;
92 end
93 printf("thirteen iterations are now tabulated :\n");
94 disp(y);
```

```
95 // the total heat loss from the wire may be
      calculated as the conduction through Rmplus at
      node 4. then
96 T4 = y(4,13); // [degree celsius]
97 q = (T4-Tos)/(Rmplus4); // [W/m]
98 // this must equal the heat generated in the wire,
      or
99 V = \text{%pi*}(d*10^{(-3)/2})^{(2)}; // [square meter]
100 q_exact = Q*10^{(6)}*V; // [W/m]
101 printf("\n the total heat loss from the wire by
      the conduction through Rmplus at node 4 is %f kW/
      m", q/1000);
102 printf("\n\n heat generated in the wire is %f kW/m",
      q_exact/1000);
103 printf("\n\n the difference between the two values
      results from the inaccuracy in determination of
      T4");
```

Scilab code Exa 3.8 heat generation with non uniform nodal elements

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 3.8\n\n\n");
4 // heat generation with non uniform nodal elements
5 // Example 3.8 (page no.-100-103)
6 // solution
7
8 k = 0.8; // [W/m degree celsius] thermal conductivity of glass
9 d = 0.003; // [m] thickness of layer of glass
10 x = 0.001; // [m] thickness of electric conducting strip
11 Tinf = 30; // [degree celsius] environment temperature
12 h = 100; // [W/square meter degree celsius]
```

```
13 q1 = 40; // [W] heat generated by strips
14 q2 = 20; // [W] heat generated by strips
15 // the nodal network for a typical section of the
      glass is shown in figure. In this example we have
       not chosen dx = dy.
16 // because of symmetry T1 = T7, T2 = T6, etc., and we
       only need to solve the temperatures of 16 nodes.
       we employ the resistance formulation. As shown,
       we have chosen
17 dx = 0.005; // [m]
18 dy = 0.001; // [m]
19 A = 0.005; // [square meter]
20 // various resistances may now be calculated:
21
\frac{22}{\sqrt{100}} for nodes \frac{1}{2}, \frac{3}{4}:
23 one_by_Rm_p1 = k*dy/(2*dx);
24 \text{ one\_by\_Rm\_m1} = \text{one\_by\_Rm\_p1};
25 \text{ one\_by\_Rn\_p1} = h*A;
26 one_by_Rn_m1 = k*dx/dy;
27
28 // for nodes 8,9,10,11,15,16,17,18:
29 one_by_Rm_p2 = k*dy/(dx);
30 one_by_Rm_m2 = one_by_Rm_p2;
31 one_by_Rn_m2 = k*dx/dy;
32 \text{ one\_by\_Rn\_p2} = \text{one\_by\_Rn\_m2};
33
34 // for nodes 22,23,24,25:
35 one_by_Rm_p3 = k*dy/(2*dx);
36 \text{ one\_by\_Rm\_m3} = \text{one\_by\_Rm\_p3};
37 \text{ one_by_Rn_p3} = k*dx/dy;
38 one_by_Rn_m3 = 0; // [insulated surface]
39
40 // from the above resistances we may calculate the
      sum_one_by_Rij as
41 // \text{ nodes} : 1, 2, 3, 4:
42 \text{ sum\_one\_by\_Rij1} = 4.66;
43 // nodes : 8,9,10,11,15,16,17,18:
44 \text{ sum\_one\_by\_Rij2} = 8.32;
```

```
45 // nodes : 22,23,24,25:
46 \text{ sum\_one\_by\_Rij3} = 4.16;
47 // the nodal equations are obtained from equation
            (3-31)
     // only node 4 has a heat generation term, Qi = 0
             for all other nodes.
49 // the equations are listed below
50 // for node 1 : T8*one_by_Rn_m1+T2*one_by_Rm_p1+30*
             one_bv_Rn_m1-sum_one_bv_Rij1*T1 = 0;
     // for node 4 : T5*one_by_Rm_p1+T3*one_by_Rm_m1+30*
             one_by_Rn_p1+T11*one_by_Rn_m1+Q-sum_one_by_Rij1*
      // similar equations are obtained and we solve it by
52
               matrix method
      53
54
                  0 0.08 -4.66 0.08 0 0 4 0 0 0 0 0 0 0 0;
55
                 0 0 0.16 -4.66 0 0 0 4 0 0 0 0 0 0 0;
56
                 4 0 0 0 -8.16 0.16 0 0 4 0 0 0 0 0 0;
57
58
                  0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0 0 0 0;
                 0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0 0 0 0;
59
                  0 0 0 4 0 0 0.32 -8.32 0 0 0 4 0 0 0 0;
60
                  0 0 0 0 4 0 0 0 -8.16 0.16 0 0 4 0 0 0;
61
                  0 0 0 0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0;
62
                  0 0 0 0 0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0;
63
64
                  0 0 0 0 0 0 4 0 0 0.32 -8.32 0 0 0 4;
65
                  0 0 0 0 0 0 0 4 0 0 0 -4.08 0.08 0 0;
                  0 0 0 0 0 0 0 0 4 0 0 0.08 -4.16 0.08 0;
66
                 0 0 0 0 0 0 0 0 0 4 0 0 0.08 -4.16 0.08;
67
                  68
70 \text{ T1} = Z^{(-1)} *C;
71 printf("Nodes
             (1,2,3,4,8,9,10,11,15,16,17,18,22,23,24,25)
             temperature at 20 W/m respectively");
72 disp(T1);
73 	ext{ Z1 } = [-4.58 	ext{ } 0.08 	ext{ } 0 	ext{ } 4 	ext{ } 0 	ext{ } 
                  74
```

```
0 0.08 -4.66 0.08 0 0 4 0 0 0 0 0 0 0 0;
75
76
       0 0 0.16 -4.66 0 0 0 4 0 0 0 0 0 0 0;
       4 0 0 0 -8.16 0.16 0 0 4 0 0 0 0 0 0;
77
       0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0 0 0 0;
78
79
       0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0 0 0 0;
80
       0 0 0 4 0 0 0.32 -8.32 0 0 0 4 0 0 0 0;
       0 0 0 0 4 0 0 0 -8.16 0.16 0 0 4 0 0 0;
81
       0 0 0 0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0 0;
82
       0 0 0 0 0 0 4 0 0 0.16 -8.32 0.16 0 0 4 0;
83
       0 0 0 0 0 0 0 4 0 0 0.32 -8.32 0 0 0 4;
84
       0 0 0 0 0 0 0 4 0 0 0 -4.08 0.08 0 0;
85
       0 0 0 0 0 0 0 0 4 0 0 0.08 -4.16 0.08 0;
86
87
       0 0 0 0 0 0 0 0 0 4 0 0 0.08 -4.16 0.08;
       88
90 	ext{ T2} = Z1^{(-1)}*C1;
91 printf("\n\n Nodes
     (1,2,3,4,8,9,10,11,15,16,17,18,22,23,24,25)
     temperature at 40 W/m respectively");
92 disp(T2);
93 // we know the numerical value that the convection
     should have
  // the convection losss at the top surface is given
     by
95 qc1 = 2*h*[(dx/2)*(T1(1)-Tinf)+dx*(T1(2)+T1(3)-2*
     Tinf)+(dx/2)*(T1(4)-Tinf)]; // [W] for <math>20W/m, the
     factor of 2 accounts for both sides of section
96 \text{ qc2} = 2*h*[(dx/2)*(T2(1)-Tinf)+dx*(T2(2)+T2(3)-2*
     Tinf)+(dx/2)*(T2(4)-Tinf)]; // [W] for <math>40W/m
97 printf("\n\n the convection loss at the top surface
     is given by (for 20 W/m heat generation) %f W',
     qc1);
98 printf("\n\n the convection loss at the top surface
     is given by (for 40 W/m heat generation) %f W',
     qc2);
```

Scilab code Exa 3.11 use of variable mesh size

```
1 clear;
2 clc;
3 printf("\t\tExample Number 3.11\n\n");
4 // use of variable mesh size
\frac{5}{\sqrt{2}} Example 3.11 (page no. -108-110)
6 // solution
  // using data given in figure example 3-11(page no
      -109
9 // nodes 5,6,8, and 9 are internal nodes with dx =
      dy and have nodal equations in the form of
      equation (3-24). Thus,
10 / 600 + T6 + T8 - 4 * T5 = 0
11 // 500 + T5 + T7 + T9 - 4 * T6 = 0
12 / 100 + T5 + T9 + T11 - 4 * T8 = 0
13 / T8 + T6 + T10 + T12 - 4 * T9 = 0
14 // For node 7 we can use a resistance formulation
      and obtain
  // (1/R_{-}7_{-}6) = k
15
16 / (1/R_7_{500} - degree) = k*(dx/6+dx/2)/(dy/3) = 2*k
17 // (1/R_{-}7_{-}10) = 2*k
18 // and we find
19 / 1000 + T6 + 2*T10 - 5*T7 = 0
20 // similar resistance are obtained for node 10
21 // (1/R_{-}10_{-}9) = k
22 / (1/R_{-}10_{-}7) = 2*k = (1/R_{-}10_{-}1)
23 // so that
24 // 2*T7+T9+2*T1-5*T10 = 0
25 // for node 1,
26 // (1/R_1_1_2) = k*(dy/6+dy/2)/(dx/3) = 2*k
27 / (1/R_1_3) = k*(dx/6+dx/2)/(dy) = 2*k/3
28 // (1/R_1_1_0) = 2*k
```

```
29 // and the nodal equation becomes
30 // 3*T12+3*T10+T3-7*T1 = 0
31 // for node 11,
32 / (1/R_11_100_degree) = (1/R_11_12) = k*(dy/6+dy/2)
      /(dx/3) = 2*k
  // (1/R_11_8) = k
33
34 / (1/R_11_13) = k*(dx/3)/dy = k/3
35 // and the nodal equation becomes
36 / 600 + 6*T12 + 3*T8 + T13 - 16*T11 = 0
37 // Similarly, the equation for node 12 is
38 // 3*T9+6*T11+6*T1+T14-16*T12 = 0
39 // for node 13,
40 // (1/R_13_100_degree) = k*(dy)/(dx/3) = 3*k = 1/
      R_{-}13_{-}14
  // (1/R_{-}13_{-}11) = (1/R_{-}13_{-}100) = k/3
41
42 // and we obtain
43 / 1000 + 9 * T14 + T11 - 20 * T13 = 0
44 // similarly for node 14,
45 / 100 + 9 * T13 + 9 * T3 + T12 - 20 * T14 = 0
46 // finally, from resistances already found, the
      nodal equation for node 3 is
  // 200+9*T14+2*T1-13*T3 = 0
47
48 // we choose to solve the set of equations by the
      gauss-seidel iteration technique
49 A=[1 -1 0 0 0 0 0 0 0 0 0 0 0;0 0 1 -1 0 0 0 0 0
      0 0 0 0;0 0 0 0 -4 1 0 1 0 0 0 0 0;0 0 0 0 1
      -4 1 0 1 0 0 0 0 0;0 0 0 0 1 0 0 -4 1 0 1 0 0 0;0
      0 0 0 0 1 0 1 -4 1 0 1 0 0;0 0 0 0 0 1 -5 0 0 2
      0 0 0 0;2 0 0 0 0 2 0 1 -5 0 0 0 0;-7 0 1 0 0 0
      0 0 0 3 0 3 0 0;0 0 0 0 0 0 0 3 0 0 -16 6 1 0;6
      0 0 0 0 0 0 3 0 6 -16 0 1;0 0 0 0 0 0 0 0 0 1
      0 -20 9;0 0 9 0 0 0 0 0 0 0 1 9 -20;2 0 -13 0
      0 0 0 0 0 0 0 0 0 9];
50 b
      = [0;0;-600;-500;-100;0;-1000;0;0;-600;0;-1000;-100;-200];
51 T = A^{(-1)}*b;
52 printf ("Nodal temperatures for node
```

```
(1,2,3,4,5,6,7,8,9,10,11,12,13,14) are
respectively as follows in degree celsius");
53 disp(T);
```

Scilab code Exa 3.12 Three dimensional numerical formulation

```
1 clear;
2 clc;
3 printf("\t\tExample Number 3.12\n\n");
4 // Three-dimensional numerical formulation
5 // Example 3.12 (page no.-110-113)
6 // solution
  Tinf = 10; // [degree celsius] environment
      temperature
9 h = 500; // [W/square meter degree celsius]
10 Ts = 100; // [degree celsius] four side temperature
11 k = 2; // [W/m degree celsius]
12 dx = 0.01; // [m]
13 dy = 0.01; // [m]
14 dz = 0.01; // [m]
15 // all of the interior nodes for Z-planes 2,3,4 have
       resistances of
16 A = dy*dz; // [square meter]
17 one_by_R = k*A/dx;
18 one_by_R_11_21 = one_by_R;
19 one_by_R_21_22 = one_by_R;
20 // the surface conduction resistances for surface Z-
      plane are
21 one_by_R_11_12 = k*A/dx;
20 \text{ one_by_R_11_14} = \text{one_by_R_11_12};
23 // the surface convection resistances are
24 one_by_R_11_inf = h*A;
25 // for surfaces nodes like 11 the sum_one_by_R_ij
      term in equation (3-32) becomes
```

```
26 \text{ sum\_one\_by\_R\_11\_j} = 4*one\_by\_R\_11\_12+one\_by\_R+
      one_by_R_11_inf;
27 // while, for interior nodes, we have
28 sum_one_by_R_21_j = 6*one_by_R;
29 // for the insulated black surface nodes
30 \text{ sum\_one\_by\_R\_51\_j} = 4*one\_by\_R\_11\_12+one\_by\_R;
31 // there are 30 nodes in total; 6 in each z-plane.
      we could write the equations for all of them but
      prefer to take advantage of the symmetry of the
      problem as indicated in figure. thus,
32 // T11 = T13 = T14 = T16 And T12 = T15, etc
33 // we may then write the surface nodal equations as
34 // T11 = [0.05 * Tinf + 0.02 * T21 + (0.01) * (100 + 100 + T14 + T12)]
      ) ] / 0.11
  // T12 = [0.05 * Tinf + 0.02 * T22 + (0.01) * (100 + T11 + T15 + T13)]
35
      ) | / 0.11
  // inserting
36
37 Tinf = 10; // [degree celsius]
38 // following the same procedure for the other z-
      planes we obtain
  // T21 = (200+T11+T31+T22)/5
39
40 / T22 = (100 + T12 + T32 + 2 * T21) / 5
41 / T31 = (200 + T21 + T41 + T32) / 5
42 / T32 = (100 + T22 + T42 + 2*T31) / 5
43 // T41 = (200+T31+T51+T42)/5
44 / T42 = (100 + T32 + T52 + 2 + T41) / 5
45 // T51 = (2+0.02*T41+0.01*T52)/0.05
46 // T52 = (1+0.02*T42+0.02*T51)/0.05
47 // Solving the 10 equations
48 \ Z = [-0.1 \ 0.01 \ 0.02 \ 0 \ 0 \ 0 \ 0 \ 0;
         0.02 -0.1 0 0.02 0 0 0 0 0;
49
50
         1 0 -5 1 1 0 0 0 0 0;
        0 1 2 -5 0 1 0 0 0 0;
51
52
        0 0 1 0 -5 1 1 0 0 0;
        0 0 0 1 2 -5 0 1 0 0;
53
        0 0 0 0 1 0 -5 1 1 0;
54
        0 0 0 0 0 1 2 -5 0 1;
55
        0 0 0 0 0 0 0.02 0 -0.05 0.01;
56
```

```
0\ 0\ 0\ 0\ 0\ 0\ 0\ 0.02\ 0.02\ -0.05];
57
58 \ C = [-2.5; -1.5; -200; -100; -200; -100; -200; -100; -2; -1];
59 T = Z^{(-1)} *C;
60 \text{ T11} = \text{T(1)};
61 \quad T12 = T(2);
62 	ext{ T21} = 	ext{T(3)};
63 \quad T22 = T(4);
64 \quad T31 = T(5);
65 \quad T32 = T(6);
66 \quad T41 = T(7);
67 	ext{ T42} = 	ext{ T(8)};
68 	 T51 = T(9);
69 	ext{ T52} = 	ext{T(10)};
70 printf("the following results for the temperature in
        each z-plane is ;");
71 printf("\n \t \t z-plane \t \t \n \de 1 \t \t \n \de 2");
72 printf("\n\t\t\t\t\t\t\t\tf\t\t\t\f\f\t\t\f\f\f\' 1,T11,T12);
73 printf("\n\t\t\t\t\t\t\tf\t\t\f\f\t\t\f\f\f\' 1,2,T21,T22);
74 printf("\n\t\t\t\t\t\t\tf\t\t\t\f\f\t\t\f\f\f\",3,T31,T32);
76 printf("\n\t\t\t\t\t\t\t\t\tf\t\t\t\f\f\t\t\f\f\f\' ,5,T51,T52);
77 \text{ val} = [1 2 3 4 5];
78 val1 = [T11 T21 T31 T41 T51];
79 \text{ val2} = [T12 \ T22 \ T32 \ T42 \ T52];
80 plot(val, val1, val, val2);
81 legend("T11","T22");
82 xgrid();
83 xlabel("z-plane");
84 ylabel("Temperature (degree celsius)");
```

Chapter 4

Unsteady State Conduction

Scilab code Exa 4.1 steel ball cooling in air

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 4.1\n\n");
4 // steel ball cooling in air
5 // illustration4.1
6 // solution
8 h = 10; // [W/square meter per degree celsius]
      convectional heat transfer coefficient
9 k = 35; // [W/m per degree celsius] heat transfer
     coefficient
10 c = 460; // [kJ/kg]
11 r = 0.05/2; // [m] diameter of ball
12 Tb = 450;// [degree celsius] ball temperature
13 Te = 100; // [degree celsius] environment temperature
14 A = 4*\%pi*r^{(2)};
15 V = 4*\%pi*r^{(3)}/3;
16 // We anticipate that the lumped capacity method
      will apply because of the low value of h and high
       value of k
17 // we check by using equation (4-6)
```

```
18 K = h*(V/A)/k;
19 // since the value of K is less than 0.1 so we will
      use equation (4-5)
20 T = 150; // [degree celsius] attained temperature by
      the ball
21 rho = 7800; // [kg/cubic meter] density of the ball
22 a = (h*A)/(rho*c*V);
23 t = log((T-Te)/(Tb-Te))/(-a); // [s] time required to
      attain the temperature of 150 degree celsius
24 printf("time required to attain the temperature of
      150 by degree celsius by the ball is %f h",t
      /3600);
```

Scilab code Exa 4.2 Semi infinite solid with sudden change in surface conditions

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 4.2\n \n");
4 // Semi-infinite solid with sudden change in surface
      conditions
5 // illustration4.2
6 // solution
8 k = 45; // [W/m per degree celsius] thermal
      conductivity of steel block
9 alpha = 1.4*10^(-5); // [square meter/s] constant
10 Tb = 35; // [degree celsius] block temperature
11 x = 0.025; // [m] depth at which temperature is
     calculated
12 t = 30; // [s] time after which temperature is to be
     calculated
13 // we can make use of the solutions for the semi-
      infinite solid given as equation (4-8) and (4-13a)
```

```
14 // for case A (by suddenly raising the surface
      temperature to 250 degree celsius)
15 To = 250; // [degree celsius]
16 T_x_t = To + (Tb - To) * (erf(x/(2*(alpha*t)^(1/2))));
17 printf("temperature at depth of 0.025 m after 30
      second for case 1 is %f degree celsius", T_x_t);
  // for the constant heat flux case B we make use of
18
      equation (4-13a)
19 // since qo/A is given
20 \text{ q_by_A} = 3.2*10^{(5)}; // [W/square meter]
21 T_x_t1 = Tb + (2*q_by_A*(alpha*t/%pi)^(1/2)*exp(-x^(2))
      /(4*alpha*t))/k)-(q_by_A*x*(1-erf(x/(2*(alpha*t)))/k)
      ^(1/2))))/k);// [degree celsius]
22 printf("\n temperature at depth of 0.025 m after 30
      second for case 2 is %f degree celsius", T_x_t1)
  // for the constant heat flux case the surface
      temperature after 30 s would be evaluated with x
      = 0 in equation (4-13a)
24 x = 0; // [m] at the surface
25 \text{ T_x_o} = \text{Tb+}(2*q_by_A*(alpha*t/\%pi)^(1/2)*exp(-x^(2))
      /(4*alpha*t))/k)-(q_by_A*x*(1-erf(x/(2*(alpha*t)))/k)
      ^(1/2))))/k);// [degree celsius]
26 printf("\n surface temperature after 30 second is %f
       degree celsius", T_x_o);
```

Scilab code Exa 4.3 pulsed energy at surface of semi infinite solid

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 4.3\n\n\n");
4 // pulsed energy at surface of semi-infinite solid
5 // illustration4.3
6 // solution
7
8 rho = 7800; // [kg/cubic meter] density of slab
```

```
9 c = 460; // [J/kg degree celsius] constant
10 alpha = 0.44*10^{(-5)}; // [square meter/s] constant
11 Ts = 40; // [degree celsius] initial temperature of
     of slab
12 x = 0.0; // [m] depth at which temperature is
      calculated
13 t = 2; // [s] time after which temperature is
     calculated
14 // this problem is a direct application of equation
     (4-13b)
15 // we have
16 Qo_by_A = 10^(7); // [J/square meter] heat flux
17 To = Ts+(Qo_by_A/(rho*c*(\%pi*alpha*t)^(1/2)))*exp(-x)
      ^(2)/(4*alpha*t));// [degree celsius] surface
     temperature at x = 0
18 printf("surface temperature at x = 0 and at t = 2
     second is %f degree celsius", To);
19 x = 0.002; // [m] depth at which temperature is
      calculated
20 T = Ts+(Qo_by_A/(rho*c*(\%pi*alpha*t)^(1/2)))*exp(-x)
     ^(2)/(4*alpha*t));// [degree celsius] temperature
       at depth x = 0.002
21 printf("\n temperature at depth 0.002 m and after 2
     second is %f degree celsius",T);
```

Scilab code Exa 4.4 heat removal from semi infinite solid

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 4.4\n\n\n");
4 // heat removal from semi-infinite solid
5 // illustration4.4
6 // solution
7
8 alpha = 8.4*10^(-5);// [square meter/s] constant
```

```
9 Ts = 200; // [degree celsius] initial temperature of
     of slab
10 x = 0.04; // [m] depth at which temperature is
     calculated
11 T_x_t = 120; // [degree celsius] temperature at depth
       0.04 \, \mathrm{m}
12 To = 70; // [degree celsius] surface temperature
      after lowering
13 k = 215; // [W/m degree celsius] heat transfer
      coefficient
14 // We first find the time required to attain the 120
      degree celsius temperature
15 // and then integrate equation (4-12) to find the
      total heat removed during this interval
16 t = (x/(erfinv(((T_x_t-T_0)/(T_s-T_0)))*2*sqrt(alpha)))
     ^(2);// s
17 printf ("time taken to attain the temperature of 120
      degree celsius %f s",t);
18 // the total heat removed at the surface is obtained
      by integrating equation (4-12):
19 // Qo_by_A = integrate('qo_by_A', 'dt', 0, t)
20 // or Qo_by_A = integrate('k*(To-Ts)/(sqrt(\%pi*alpha))
     *t))','dt',0,t)
21 Qo_by_A = integrate('k*(To-Ts)/(sqrt(\%pi*alpha*t))',
      't',0,t);
22 printf("\n the total heat removed from the surface
      is \%e J/square meter", Qo_by_A);
```

Scilab code Exa 4.5 sudden exposure of semi infinite solid slab to convection

```
1 clear; 2 clc; 3 printf("\t\t\tExample Number 4.5\n\n"); 4 // sudden exposure of semi-infinite solid slab to
```

```
convection
  5 // illustration4.5
  6 // solution
  8 alpha = 8.4*10^(-5); // [square meter/s] constant
  9 Ts = 200; // [degree celsius] initial temperature of
                of slab
10 Te = 70; // [degree celsius] environment temperature
11 k = 215; // [W/m degree celsius] heat transfer
                 coefficient of slab
12 h = 525; // [W/square meter degree celsius] heat
                 transfer coefficient
13 x = 0.04; // [m] depth at which temperature is
                 calculated
14 T_x_t = 120; // [degree celsius] temperature at depth
                    0.04 \, \mathrm{m}
15 // we can use equation (4-15) or figure (4-5) for
                 solution of this problem
16 // by using figure it is easier to calculate
                 involves iterative method to solve because time
                 appeares in both the variables
17 // h*sqrt(alpha*t)/k and x/(2*sqrt(alpha*t))
18 K = (T_x_t-T_s)/(T_e-T_s);
19 // we seek the values of t such that the above value
                    of K is equal to the value of K which comes out
                from graph
20 // we therfore try values of t and obtain other
                 readings
21 printf("The iteration are listed below\n");
22 // \text{ at t} = 1000 \text{ s}
23 t = 1000; // [s] time
24 A = h*sqrt(alpha*t)/k;
25 B = x/(2*sqrt(alpha*t));
26 printf(" t \setminus t \setminus th * sqrt(alpha * t) / k \setminus t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t) + t \times / (2 * sqrt(alpha * t
                 )) t (T_x_t-T_s)/(T_e-T_s)");
27 printf("\n \%f\t\t \%f\t\ \%f\t\t 0.41",t,A,B);
28 t = 3000; // [s] time
29 A = h*sqrt(alpha*t)/k;
```

```
30 B = x/(2*sqrt(alpha*t));
31 printf("\n %f\t\t %f \t %f \t\t 0.61",t,A,B);
32 t = 4000; // [s] time
33 A = h*sqrt(alpha*t)/k;
34 B = x/(2*sqrt(alpha*t));
35 printf("\n %f\t\t %f \t %f \t\t 0.68",t,A,B);
36 printf("\n consequently the time required is approximately 3000 second");
```

Scilab code Exa 4.6 aluminium plate suddenly exposed to convection

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 4.6\n\n'");
4 // aluminium plate suddenly exposed to convection
5 // illustration 4.6
6 // solution
8 alpha = 8.4*10^(-5); // [square meter/s] constant
9 Ts = 200; // [degree celsius] initial temperature of
     of plate
10 Te = 70; // [degree celsius] environment temperature
11 k = 215; // [W/m degree celsius] heat transfer
     coefficient of plate
12 h = 525; // [W/square meter degree celsius] heat
     transfer coefficient
13 x = 0.0125; // [m] depth at which temperature is
     calculated
14 t = 60; // [s] time after which plate temperature is
     calculated
15 L = 0.025; // [m] thickness of plate
16 theta_i = Ts-Te;// [degree celsius]
17 // then
18 Z = alpha*t/L^2;
19 X = k/(h*L);
```

```
20 \text{ x_by_L} = \text{x/L};
21 // from figure 4-7 (page no. -144-145)
22 theta_o_by_theta_i = 0.61;
23 theta_o = theta_o_by_theta_i*theta_i;// [degree
      celsius]
24 // from figure 4-10(page no. -149) at x/L = 0.5,
25 theta_by_theta_o = 0.98;
26 theta = theta_by_theta_o*theta_o; // [degree celsius]
27 T = Te+theta; // [degree celsius]
28 // we compute the energy lost by the slab by using
      Figure 4-14 (page no. -152). For this calculation
     we require the following properties of aluminium:
29 rho = 2700; // [kg/cubic meter]
30 C = 900; // [J/kg degree celsius]
31 // for figure 4-14(page no. -152) we need
32 V = h^2*alpha*t/(k^2);
33 B = h*L/k;
34 // from figure 4-14(page no. -152)
35 Q_by_Qo = 0.41;
36 // for unit area
37 Qo_by_A = rho*C*2*L*theta_i; // [J/square\ meter]
38 // so that the heat removed per unit surface area is
39 Q_by_A = Qo_by_A*Q_by_Qo; // [J/square meter]
40 printf("\n temperature at a depth of 1.25 cm from
      one of faces after 1 min of exposure of plate to
      the environment is %f degree celsius",T);
41 printf("\n\n energy removed per unit area from the
      plate in this time is %e J/square meter", Q_by_A);
```

Scilab code Exa 4.7 long cylinder suddenly exposed to convection

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 4.7(Page no.-154-155)\n\\n\n");
```

```
4 // long cylinder suddenly exposed to convection
5 // Example 4.7
6 // solution
8 d = 0.05; // [m] diameter of cylinder
9 Ti = 200; // [degree celsius] initial temperature of
      aluminium cylinder
10 Tinf = 70; // [degree celsius] temperature of
      environment
11 h = 525; // [W/square meter degree celsius] heat
      transfer coefficient
12 // we have
13 theta_i = Ti-Tinf; // [degree celsius]
14 alpha = 8.4*10^(-5); // [square meter/s]
15 ro = d/2; // [m]
16 t = 60; // [s]
17 k = 215; // [W/m degree celsius]
18 r = 0.0125; // [m]
19 rho = 2700; // [kg/cubic meter]
20 C = 900; // [J/kg degree celsius]
21 // we compute
22 Z = alpha*t/ro^2;
23 X = k/(h*ro);
24 \text{ r_by_ro} = \text{r/ro};
25 // from figure 4-8(page no. -146)
26 theta_o_by_theta_i = 0.38;
27 // and from figure 4-11(page no.-150) at r/ro = 0.5
28 \text{ theta_by\_theta_o} = 0.98;
29 // so that
30 theta_by_theta_i = theta_o_by_theta_i*
      theta_by_theta_o;
31 theta = theta_i*theta_by_theta_i;// [degree celsius]
32 T = Tinf+theta; // [degree celsius]
33 // to compute the heat lost, we determine
34 V = h^2*alpha*t/k^2;
35 B = h*ro/k;
36 // then from figure 4-15 (page no. -153)
37 Q_by_Qo = 0.65;
```

```
38  // for unit length
39  Qo_by_L = rho*C*%pi*ro^2*theta_i; // [J/m]
40  // and the actual heat lost per unit length is
41  Q_by_L = Qo_by_L*Q_by_Qo; // [J/m]
42  printf("temperature at a radius of 1.25 cm is %f
        degree celsius", T);
43  printf("\n\nheat lost per unit length 1 minute after
        the cylinder is exposed to the environment is %e
        J/m", Q_by_L);
```

Scilab code Exa 4.8 semi infinite cylinder suddenly exposed to convection

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 4.8 \n\n");
4 // semi-infinite cylinder suddenly exposed to
     convection
5 // illustration 4.8
  // solution
8 d = 0.05; // [m] diameter of aluminium cylinder
9 Ti = 200; // [degree celsius] initial temperature of
     of cylinder
10 Te = 70; // [degree celsius] environment temperature
11 k = 215; // [W/m degree celsius] heat transfer
      coefficient of plate
12 h = 525; // [W/square meter degree celsius]
     convection heat transfer coefficient
13 alpha = 8.4*10^(-5); // [square meter/s] constant
14 x = 0.10; // [m] distance at which temperature is
      calculated from end
15 t = 60; // [s] time after which temperature is
     measured
16 // so that the parameters for use with figure (4-5)
17 A = h*sqrt(alpha*t)/k;
```

```
18 B = x/(2*sqrt(alpha*t));
19 // from figure (4-5)
20 z = 1-0.036;
21 S_of_X = z;
22 // for the infinite cylinder we seek both the axis-
      and surface-temperature ratios.
23 // the parameters for use with fig (4-8) are
24 r_o = d/2; // [m] radius of aluminium cylinder
25 r = d/2; // [m] for surface temperature ratio
26 C = k/(h*r_o);
27 D = (alpha*t/r_o^{(2)});
28 \quad y = 0.38;
29 // this is the axis temperature ratio.
30 // to find the surface-temperature ratio, we enter
      figure (4-11), using
31 R = r/r_o;
32 u = 0.97;
33 // thus
34 \text{ w} = \text{y}; // \text{ at } \text{r} = 0
35 \text{ v} = \text{y*u}; // \text{ at } \text{r} = \text{r}_{-0}
36 C_of_O_axis = w; // at r = 0
37 \ C_of_O_r_o = v; // \ at \ r = r_o
38 // combining the solutions for the semi-infinite
      slab and infinite cylinder, we have
39 t = S_of_X*C_of_O_axis;
40 s = S_of_X*C_of_0_r_o;
41 // the corresponding temperatures are
42 \text{ T_axis} = \text{Te+t*(Ti-Te)};
43 \text{ T_r_o} = \text{Te+s*(Ti-Te)};
44 printf ("the temperature at the axis is %f degree
      celsius", T_axis);
45 printf("\n the temperature at the surface is %f
      degree celsius", T_r_o);
```

Scilab code Exa 4.9 finite length cylinder suddenly exposed to convection

```
1 clear;
2 clc;
3 printf("\t\tExample Number 4.9 \n\n");
4 // finite length cylinder suddenly exposed to
      convection
5 // illustration 4.9
6 // solution
8 d = 0.05; // [m] diameter of aluminium cylinder
9 Ti = 200; // [degree celsius] initial temperature of
      of cylinder
10 Te = 70; // [degree celsius] environment temperature
11 k = 215; // [W/m degree celsius] heat transfer
      coefficient of plate
12 h = 525; // [W/square meter degree celsius]
     convection heat transfer coefficient
13 alpha = 8.4*10^(-5); // [square meter/s] constant
14 x1 = 0.00625; // [m] distance at which temperature is
      calculated from end
15 t = 60; // [s] time after which temperature is
     measured
16 r = 0.0125; // [m] radius at which temperature is
     calculated
17 // to solve this problem we combine the solutions
     from heisler charts for an infinite cylinder and
     an infinite plate in accordance with the
      combination shown in fig (4-18f)
18 // for the infinite plate problem
19 L = 0.05; // [m]
20 // the x position is measured from the center of the
     plate so that
21 x = L - x1; // [m]
22 \quad A = k/(h*L);
23 B = (alpha*t/L^{(2)});
24 // from figures (4-17) and (4-10) respectively
25 thetha_o_by_i = 0.75;
26 \text{ thetha_by_i} = 0.95;
27 // so that
```

```
28 thetha_by_i_plate = thetha_o_by_i*thetha_by_i;
29 // for the cylinder
30 r_o = d/2; // [m] radius of the cylinder
31 R = r/r_o;
32 C = k/(h*r_o);
33 D = (alpha*t/r_o^(2));
34 // and from figures (4-8) and (4-11), respectively
35 thetha_o_by_i_cyl = 0.38;
36 \text{ thetha_by_o} = 0.98;
37 // so that
38 thetha_by_i_cyl = thetha_o_by_i_cyl*thetha_by_o;
39 // combibing the solutions for the plate and
      cylinder gives
40 thetha_by_i_short_cyl = thetha_by_i_plate*
     thetha_by_i_cyl;
41 // thus
42 T = Te+thetha_by_i_short_cyl*(Ti-Te);
43 printf("the temperature at a radial position of
      0.0125 m and a distance of 0.00625m from one end
     of cylinder 60 second after exposure to
     environment is %f degree celsius",T);
```

Scilab code Exa 4.10 heat loss for finite length cylinder

```
1 clear;
2 clc;
3 printf("\t\tExample Number 4.10\n\n\n");
4 // heat loss for finite-length cylinder
5 // illustration4.10
6 // solution
7
8 d = 0.05;// [m] diameter of aluminium cylinder
9 l = 0.1;// [m] length of aluminium cylinder
10 Ti = 200;// [degree celsius] initial temperature of of cylinder
```

```
11 Te = 70; // [degree celsius] environment temperature
12 k = 215; // [W/m degree celsius] heat transfer
      coefficient of plate
13 h = 525; // [W/square meter degree celsius]
      convection heat transfer coefficient
14 alpha = 8.4*10^(-5); // [square meter/s] constant
15 x1 = 0.00625; // [m] distance at which temperature is
       calculated from end
16 t = 60; // [s] time after which temperature is
     measured
17 r = 0.0125; // [m] radius at which temperature is
      calculated
18 // we first calculate the dimensionless heat-loss
      ratio for the infinite plate and infinite
      cylinder which make up the multidimensional body
19 // for the plate we have
20 L = 0.05; // [m]
21 \quad A = h*L/k;
22 B = h^{(2)}*alpha*t/k^{(2)};
23 // from figure (4-14), for the plate, we read
24 Q_by_Q_o_plate = 0.22;
25 // for the cylinder
26 \text{ r_o} = 0.025; // [m]
27 // so we calculate
28 C = h*r_o/k;
29 // and from figure (4-15) we have
30 \ Q_by_Q_o_cyl = 0.55;
31 // the two heat ratios may be inserted in equation
      (4-22) to give
32 \ Q_by_Q_o_tot = Q_by_Q_o_plate+Q_by_Q_o_cyl*(1-
     Q_by_Q_o_plate);
33 c = 896; // [J/kg degree celsius] specific heat of
      aluminium
34 rho = 2707; // [kg/cubic meter] density of aluminium
35 \ V = \%pi*r_o^(2)*l; // [cubic meter]
36 \text{ Qo = rho*c*V*(Ti-Te);}// [J]
37 Q = Qo*Q_by_Q_o_tot; // [J] the actual heat loss in
      the 1-minute
```

38 printf(" the actual heat loss in the 1-minute is %f kJ",Q/1000);

Scilab code Exa 4.12 implicit formulation

```
1 clear;
2 clc;
3 printf("\t\tExample Number 4.12\n\n");
4 // implicit formulation
\frac{5}{\sqrt{2}} Example 4.12 (page no. -173-174)
6 // solution
  // we are using the data of example 4.11 for this
      question
9 // we are inserting the value of Rij in equation
      (4-43) to write the nodal equations for the end
      of the first time increment, taking all T1^(p) =
      200 degree celsius
10 // we use underscore to designate the temperatures
      at the end of the time increment. for node 1
  // 0.05302*T1_{-} = 200/70.731+T2_{-}
      /70.731+40/84.833+0.01296*200
12 // for node 2
13 / 0.05302*T2_{-} = T1_{-}/70.731+T3_{-}
      /70.731+40/84.833+0.01296*200
14 // for node 3 and 4,
15 // 0.05302*T3_{-} = T2_{-}/70.731+T4_{-}
      /70.731+40/84.833+0.01296*200
16 // 0.02686 * T4_{-} = T3_{-}
      /70.731+40/2829+40/169.77+0.00648*200
17 // these equations can then be reduced to
18 // 0.05302*T1_{-}-0.01414*T2_{-} = 5.8911
19 // -0.01414*T1_+ + 0.05302*T2_- -0.01414*T3_ = 3.0635
20 // -0.01414*T2_+ +0.05302*T3_- -0.01414*T4_ = 3.0635
21 // -0.01414*T3_++0.02686*T4_ = 1.5457
```

```
22 // These equations can be solved by matrix method
Z = [0.05302 -0.01414 \ 0 \ 0; -0.01414 \ 0.05302 \ -0.01414]
      0;0 -0.01414 0.05302 -0.01414;0 0 -0.01414
      0.02686];
24 \ C = [5.8911; 3.0635; 3.0635; 1.5457];
25 T_{-} = Z^{(-1)}*C;
26 T1_ = T_(1); // [degree celsius]
27 T2_ = T_(2);// [degree celsius]
28 T3_ = T_(3); // [degree celsius]
29 T4_ = T_(4); // [degree celsius]
30 // we can now apply the backward-difference
      formulation a second time using the double
      underscore to designate the temperatures at the
      end of the second time increment:
31 / 0.05302 * T1_{--} = 200/70.731 + T2_{--}
      /70.731+40/84.833+0.01296*145.81
32 / 0.05302 * T2_{--} = T1_{--}/70.731 + T3_{--}
      /70.731+40/84.833+0.01296*130.12
33 // 0.05302*T3_{--} = T2_{--}/70.731+T4_{--}
      /70.731+40/84.833+0.01296*125.43
34 // 0.02686*T4_{--} = T3_{--}
      /70.731+40/2829+40/169.77+0.00648*123.56
35 // These equations can be solved by matrix method
36 \ X = [0.05302 -0.01414 \ 0 \ 0; -0.01414 \ 0.05302 \ -0.01414
      0;0 -0.01414 0.05302 -0.01414;0 0 -0.01414
      0.02686];
37 V = [5.1888; 2.1578; 2.0970; 1.0504];
38 T_{-} = X^{(-1)} *V;
39 T1_{-} = T_{-}(1); // [degree celsius]
40 T2_{-} = T_{-}(2); // [degree celsius]
41 T3_{-} = T_{-}(3); // [degree celsius]
42 \text{ T4}_{-} = \text{T}_{-}(4); // [degree celsius]
43 printf(" temperatures after time increment 1 are:");
44 printf("\n\t\T1'' == \%f",T1_);
45 printf("\n\t T2'' == \%f", T2_);
46 printf("\n\t\T3'' == \%f",T3_);
47 printf("\n\t T4'' == \%f", T4_);
48 printf("\n temperatures after time increment 2 are
```

```
:");
49 printf("\n\n\t\t T1''' == %f",T1__);
50 printf("\n\n\t\t T2''' == %f",T2__);
51 printf("\n\n\t\t T3''' == %f",T3__);
52 printf("\n\n\t\t T4'''' == %f",T4__);
```

Chapter 5

Principles of Convection

Scilab code Exa 5.1 water flow in a diffuser

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 5.1\n\n");
4 // water flow in a diffuser
5 // illustration 5.1
6 // solution
8 Tw = 20; // [degree celcius] water temperature
9 m_dot = 8; // [kg/s] water flow rate
10 d1 = 0.03; // [m] diameter at section 1
11 d2 = 0.07; // [m] diameter at section 2
12 A1 = \%pi*d1^(2)/4;// [square meter] cross-sectional
      area at section 1
13 A2 = \%pi*d2^(2)/4;// [square meter] cross-sectional
      area at section 2
14 gc = 1; // [m/s<sup>(2)</sup>] acceleration due to gravity
15 rho = 1000; // [kg/cubic meter] density of water at
      20 degree celcius
16 // we may calculate the velocities from the mass-
      continuity relation
17 u1 = m_dot/(rho*A1); // [m/s]
```

Scilab code Exa 5.2 isentropic expansion of air

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 5.2\n \n \);
4 // isentropic expansion of air
5 // illustration 5.2
6 // solution
8 Ta = 300+273.15; // [K] air temperature
9 Pa = 0.7; // [MPa] pressure of air
10 u2 = 300; // [m/s] final velocity
11 gc = 1; // [m/s^{(2)}] acceleration due to gravity
12 Y = 1.4; // gama value for air
13 Cp = 1005; // [J/kg degree celsius]
14 // the initial velocity is small and the process is
     adiabatic. in terms of temperature
15 T2 = Ta-u2^(2)/(2*gc*Cp);
16 printf("the static temperature is %f K",T2);
17 // we may calculate the pressure difference from the
      isentropic relation
18 p2 = Pa*((T2/Ta)^(Y/(Y-1)));
19 printf("\n static pressure is %f MPa",p2);
20 // the velocity of sound at condition 2 is
21 \ a2 = 20.045*T2^(1/2); // [m/s]
22 // so that the mach no. is
23 M2 = u2/a2;
24 printf("\n\n Mach number is \%f", M2);
```

Scilab code Exa 5.3 mass flow and boundary layer thickness

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 5.3 \n\n");
4 // mass flow and boundary-layer thickness
5 // illustration 5.3
6 // solution
8 Ta = 27+273.15; // [K] air temperature
9 Pa = 101325; // [Pa] pressure of air
10 u = 2; // [m/s] air velocity
11 x1 = 0.2; // [m] distance from the leading edge of
      plate
12 x2 = 0.4; // [m] distance from the leading edge of
      plate
13 R = 287; //
14 mu = 1.85*10^{(-5)}; // [kg/m s] viscosity of air
15 // the density of air is calculated from
16 rho = Pa/(R*Ta); // [kg/cubic meter]
17 // the reynolds number is calculated as
18 Re_x1 = rho*u*x1/mu;
19 Re_x2 = rho*u*x2/mu;
20 // the boundary layer thickness is calculated from
      equation (5-21)
21 \text{ del}_x1 = 4.64*x1/Re_x1^(1/2); // [m]
22 \text{ del}_x2 = 4.64*x2/Re_x2^(1/2); // [m]
23 // to calculate the mass flow which enters the
      boundary layer from the free stream between x =
      0.2 \text{ m} \text{ and } x = 0.4 \text{ m}
24 // we simply take the difference between the mass
      flow in the boundary layer at these two x
      positions.
25 // at any x position the mass flow in the boundary
```

Scilab code Exa 5.4 isothermal flat plate heated over entire length

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 5.4\n\n'");
4 // isothermal flat plate heated over entire length
5 // illustration 5.4
6 // solution
8 // total heat transfer over a certain length of the
     plate is desired, so we wish to calculate average
      heat transfer coefficients.
9 // for this purpose we use equations (5-44) and
     (5-45), evaluating the properties at the film
     temperature:
10 Tp = 60+273.15; // [K] plate temperature
11 Ta = 27+273.15; // [K] air temperature
12 Tf = (Tp+Ta)/2; // [K]
13 u = 2; // [m/s] air velocity
14 // from appendix A the properties are
15 v = 17.36*10^{(-6)}; // [square meter/s] kinematic
      viscosity
16 x1 = 0.2; // [m] distance from the leading edge of
     plate
17 x2 = 0.4; // [m] distance from the leading edge of
     plate
```

```
18 k = 0.02749; // [W/m K] heat transfer coefficient
19 Pr = 0.7; // prandtl number
20 Cp = 1006; // [J/kg K]
21 // at x = 0.2m
22 Re_x1 = u*x1/v; // reynolds number
23 Nu_x1 = 0.332*Re_x1^(1/2)*Pr^(1/3); // nusselt number
24 \text{ hx1} = \text{Nu_x1*k/x1;} // [\text{W/square meter K}]
25 // the average value of the heat transfer
      coefficient is twice this value, or
26 h_bar1 = 2*hx1; // [W/square meter K]
27 // the heat flow is
28 A1 = x1*1; // [square meter] area for unit depth
29 q1 = h_bar1*A1*(Tp-Ta); // [W]
30 // \text{ at } x = 0.4 \text{m}
31 Re_x2 = u*x2/v; // reynolds number
32 Nu_x2 = 0.332*Re_x2^(1/2)*Pr^(1/3);// nusselt number
33 hx2 = Nu_x2*k/x2; // [W/square meter K]
34 // the average value of the heat transfer
      coefficient is twice this value, or
35 h_bar2 = 2*hx2; // [W/square meter K]
36 // the heat flow is
37 A2 = x2*1; // [square meter] area for unit depth
38 \ q2 = h_bar2*A2*(Tp-Ta); // [W]
39 printf ("the heat transferred in first case of the
      plate is %f W',q1);
40 printf("\n\n and the heat transferred in second case
      of the plate is %f W',q2);
```

Scilab code Exa 5.5 flat plate with constant heat flux

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 5.5\n\n\n");
4 // flat plate with constant heat flux
5 // illustration 5.5
```

```
6 // solution
8 u = 5; // [m/s] air velocity
9 1 = 0.6; // [m] plate length
10 Ta = 27+273.15; // [K] temperature of airstream
11 // properties should be evaluated at the film
     temperature, but we do not know the plate
      temperature so for an initial calculation we take
      the properties at the free-stream conditions of
12 \ v = 15.69*10^{(-6)}; // [square meter/s] kinematic
      viscosity
13 k = 0.02624; // [W/m degree celsius] heat transfer
     coefficient
14 Pr = 0.7; // prandtl number
15 Re_l = 1*u/v; // reynolds number
16 P = 1000; // [W] power of heater
17 qw = P/1^(2); // [W/square meter] heat flux per unit
      area
18 // from equation (5-50) the average temperature
      difference is
  Tw_minus_Tinf_bar = qw*1/(0.6795*k*(Re_1)^(1/2)*(Pr)
      ^(1/3));// [degree celsius]
20 // now, we go back and evaluate properties at
21 Tf = (Tw_minus_Tinf_bar+Ta+Ta)/2;// [degree celsius]
22 // and obtain
23 \text{ v1} = 28.22*10^{(-6)}; // [square meter/s] kinematic
      viscosity
24 k1 = 0.035; // [W/m degree celsius] heat transfer
      coefficient
25 Pr1 = 0.687; // prandtl number
26 Re_11 = 1*u/v1; // reynolds number
27 \text{ Tw_minus_Tinf_bar1} = \text{qw*l/(0.6795*k1*(Re_11)^(1/2)*(}
     Pr1)^(1/3));// [degree celsius]
28 // at the end of the plate (x = 1 = 0.6m) the
      temperature difference is obtained from equation
      (5-48) and (5-50) with the constant of 0.453
29 Tw_minus_Tinf_x_equal_1 = Tw_minus_Tinf_bar1
      *0.6795/0.453; // [degree celsius]
```

Scilab code Exa 5.6 plate with unheated starting length

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 5.6\n\n'");
4 // plate with unheated starting length
5 // illustration 5.6
6 // solution
8 u = 20; // [m/s] air velocity
9 1 = 0.2; // [m] plate length as well as width (square
10 p = 101325; // [Pa] air pressure
11 Ta = 300; // [K] temperature of airstream
12 Tw = 350; // [K] temperature of last half of plate
13 // First we evaluate the air properties at the film
     temperature
14 Tf = (Tw+Ta)/2; // [K]
15 // and obtain
16 v = 18.23*10^{(-6)}; // [square meter/s] kinematic
     viscosity
17 k = 0.02814; // [W/m degree celsius] heat transfer
      coefficient
18 Pr = 0.7; // prandtl number
19 // at the trailing edge of the plate the reynolds
     number is
20 Re_1 = 1*u/v; // reynolds number
21 // or laminar flow over the length of the plate
22 // heating does not start until the last half of the
```

```
plate, or at position xo = 0.1m.
23 \text{ xo} = 0.1; // [m]
24 // the local heat transfer coefficient is given by
      equation (5-41)
25 // hx = 0.332*k*Pr^(1/3)*(u/v)^(1/2)*x^(-1/2)*[1-(xo)
     (x)^{(0.75)}^{(1)} (-1/3);
26 // the plate is 0.2 m wide so the heat transfer is
      obtained by integrating over the heated length xo
27 \text{ q} = 1*(Tw-Ta)*integrate('(0.332*k*Pr^(1/3)*(u/v))
      (1/2)*x^{(-1/2)}*[1-(xo/x)^{(0.75)}]^{(-1/3)}', 'x', xo
      ,1);
28 printf("the heat lost by the plate is \( \)f W', q);
29 // the average value of the heat transfer
      coefficient over the heated length is given by
30 h = q*(Tw-Ta)*(1-xo)*1; // [W/square meter degree
      celsius
31 printf("\n\n the average value of heat transfer
      coefficient over the heated length is given by \%f
      W/square meter degree celsius",h);
```

Scilab code Exa 5.7 oil flow over heated flat plate

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 5.7\n\n\n");
4 // oil flow over heated flat plate
5 // illustration5.7
6 // solution
7
8 u = 1.2; // [m/s] oil velocity
9 l = 0.2; // [m] plate length as well as width (square )
10 To = 20+273.15; // [K] temperature of engine oil
11 Tu = 60+273.15; // [K] uniform temperature of plate
```

```
12 // First we evaluate the film temperature
13 T = (To+Tu)/2; // [K]
14 // and obtain the properties of engine oil are
15 rho = 876; // [kg/cubic meter] density of oil
16 v = 0.00024; // [square meter/s] kinematic viscosity
17 k = 0.144; // [W/m degree celsius] heat transfer
      coefficient
18 Pr = 2870; // prandtl number
19 // at the trailing edge of the plate the reynolds
     number is
20 Re = 1*u/v; // reynolds number
21 // because the prandtl no. is so large we will
     employ equation (5-51) for the solution.
22 // we see that hx varies with x in the same fashion
      as in equation (5-44), i.e. hx is inversely
      proportional to the square root of x,
23 // so that we get the same solution as in equation
     (5-45) for the average heat transfer coefficient.
24 // evaluating equation (5-51) at x = 0.2m gives
25 \text{ Nux} = 0.3387*\text{Re}^{(1/2)*\text{Pr}^{(1/3)}/[1+(0.0468/\text{Pr})^{(2/3)}]}
     ]^{(1/4)};
26 hx = Nux*k/l;// [W/square meter degree celsius]
     heat transfer coefficient
  // the average value of the convection coefficient
28 h = 2*hx; // [W/square meter degree celsius]
29 // so that total heat transfer is
30 A = 1^{(2)}; // [square meter] area of the plate
31 \ q = h*A*(Tu-To); // [W]
32 printf("average value of the convection coefficient
      is %f W/square meter degree celsius",h);
33 printf("\n\n and the heat lost by the plate is %f W"
      ,q);
```

Scilab code Exa 5.8 drag force on a flat plate

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 5.8\n\n'");
4 // drag force on a flat plate
5 // illustration 5.8
6 // solution
8 // data is used from example 5.4
9 // we use equation (5-56) to compute the friction
      coefficient and then calculate the drag force.
10 // an average friction coefficient is desired, so
      \operatorname{st_bar} \operatorname{pr}^{(2/3)} = \operatorname{Cf_bar}/2
11 p = 101325; // [Pa] pressure of air
12 x = 0.4; // [m] drag force is computed on first 0.4 m
       of the plate
13 R = 287; //
14 Tf = 316.5; // [K]
15 u = 2; // [m/s] air velocity
16 Cp = 1006; // [J/kg K]
17 Pr = 0.7; // prandtl no.
18 rho = p/(R*Tf); // [kg/cubic meter] density at 316.5
19 h_bar = 8.698; // [W/square meter K] heat transfer
      coefficient
20 // for the 0.4m length
21 \text{ st\_bar} = h\_bar/(rho*Cp*u);
22 // then from equation (5-56)
23 Cf_bar = st_bar*Pr^(2/3)*2;
24 // the average shear stress at the wall is computed
      from equation (5-52)
25 tau_w_bar = Cf_bar*rho*u^(2)/2;// [N/square\ meter]
26 A = x*1; // [square meter] area per unit length
27 // the drag force is the product of this shear
      stress and the area,
28 D = tau_w_bar*A; // [N]
29 printf("Drag force exerted on the first 0.4 m of the
       plate is \%f mN", D*1000);
```

Scilab code Exa 5.9 turbulent heat transfer from isothermal flat plate

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 5.9\n\n");
4 // turbulent heat transfer from isothermal flat
      plate
  // illustration 5.9
6 // solution
8 p = 101325; // [Pa] pressure of air
9 R = 287; // []
10 Ta = 20+273.15; // [K] temperature of air
11 u = 35; // [m/s] air velocity
12 L = 0.75; // [m] length of plate
13 Tp = 60+273.15; // [K] plate temperature
14 // we evaluate properties at the film temperature
15 Tf = (Ta+Tp)/2; // [K]
16 rho = p/(R*Tf); // [kg/cubic meter]
17 mu = 1.906*10^{(-5)}; // [kg/m s] viscosity
18 k = 0.02723; // [W/m degree celsius]
19 Cp = 1007; // [J/kg K]
20 Pr = 0.7; // prandtl no.
21
  // the reynolds number is
22
   Rel = rho*u*L/mu;
23
   // and the boundary layer is turbulent because the
       reynolds number is greater than 5*10^{\circ}(5).
   // therefore, we use equation (5-85) to calculate
24
      the average heat transfer over the plate:
    Nul_bar = Pr^(1/3)*(0.037*Rel^(0.8)-871);
25
26
    A = L*1; // [square meter] area of plate per unit
27 h_bar = Nul_bar*k/L; // [W/square meter degree
      celsius]
```

```
28 q = h_bar*A*(Tp-Ta); // [W] heat transfer from plate
29 printf("heat transfer from plate is %f W',q);
```

Scilab code Exa 5.10 turbulent boundary layer thickness

```
1 clear;
2 clc;
3 printf("\t\tExample Number 5.10\n\n'");
4 // turbulent-boundary-layer thickness
5 // illustration 5.10
6 // solution
8 // we have to use the data from example 5.8 and 5.9
9 Rel = 1.553*10^6; // from previous example
10 L = 0.75; // [m] length of plate
11 // it is a simple matter to insert this value in
     equations (5-91) and (5-95) along with
12 x = L; // [m]
13 // turbulent-boundary-layer thickness are
14 // part a. from the leading edge of the plate
15 del_a = x*0.381*Rel^(-0.2); // [m]
16 // part b from the transition point at Recrit =
      5*10^{(5)}
17 del_b = x*0.381*Rel^(-0.2)-10256*Rel^(-1); // [m]
18 printf("turbulent-boundary-layer thickness at the
     end of the plate from the leading edge of the
      plate is \%f mm", del_a*1000);
19 printf("\n\n turbulent-boundary-layer thickness at
     the end of the plate from the transition point at
      Re_crit = 5*10^{(5)} is \%f mm', del_b*1000);
```

Scilab code Exa 5.11 high speed heat transfer for a flat plate

```
1 clear;
2 clc;
3 printf("\t\tExample Number 5.11\n\n");
4 // high speed heat transfer for a flat plate
5 / \text{Example } 5.11 \text{ (page no.} -257-259)
6 // solution
8 L = 0.7; // [m] length of flat plate
9 W = 1; // [m]  width of plate
10 // flow conditions are
11 M = 3;
12 p = 101325/20; // [Pa]
13 T = -40+273; // [degree celsius]
14 Tw = 35; // [degree celsius] temperature at which
      plate is maintained
15 \text{ Gamma} = 1.4;
16 \text{ g_c} = 1; // []
17 R = 287; // [] universal gas costant
18 // we have to consider laminar and turbulent
      portions of the boundary layer seperately
19 // the free-stream acoustic velocity is calculated
      from
20 a = sqrt(Gamma*g_c*R*T); // [m/s]
21 // so that free stream velocity is
22 u = M*a; // [m/s]
23 // the maximum reynolds number is estimated by
      making a computation based on properties
      evaluated at free stream conditions:
24 rho = p/(R*T); // [Kg/m^{(3)}]
25 mu = 1.434*10^(-5); // [Kg/m s]
26 \text{ Re}_L = \text{rho*u*L/mu};
27 // thus we conclude that both laminar and turbulent
      boundary layer heat transfer must be considered.
28 // we first determine the reference temperature for
      the two regimes and then evaluate properties at
      these temperatures.
29
30 // LAMINAR PORTION
```

```
31
32 \text{ T_o} = \text{T*}(1+((Gamma-1)/2)*M^(2)); // [K]
33 Pr = 0.7// prandtl number(assuming)
34 // we have
35 r = sqrt(Pr);
36 \text{ T_aw} = r*(T_o-T)+T; // [K]
37 // then the reference temperature from equation
      (5-124) is
38 T_{star} = T+0.5*(Tw-(T-273))+0.22*(T_{aw}-T); // [K]
39 // checking the prandtl number at this temperature
40 \text{ Pr\_star} = 0.697;
41 // so that the calculation is valid.because Pr_star
      and the value of Pr used to determine the
      recovery factor are almost same
42 // the other properties to be used in the laminar
      heat transfer analysis are
43 rho_star = p/(R*T_star); //[Kg/m^(3)]
44 mu_star = 2.07*10^(-5); // [Kg/m s]
45 \text{ k\_star} = 0.03; // [W/m degree celsius]
46 Cp_star = 1009; // [J/Kg degree celsius]
47
48 // TURBULENT PORTION
49
50 // Assuming
51 \text{ Pr} = 0.7;
52 r = Pr^{(1/3)};
53 T_aw1 = r*(T_o-T)+T; // [K]
54 // then the reference temperature from equation
      (5-124) is
55 \text{ T_star} = \text{T+0.5*}(\text{Tw-(T-273)}) + 0.22*(\text{T_aw-T}); // [K]
56 // checking the prandtl number at this temperature
57 \text{ Pr_star1} = 0.695;
58 // the agreement between Pr_star and the assumed
      value is sufficiently close.
59 // the other properties to be used in the turbulent
      heat transfer analysis are
60 rho_star1 = p/(R*T_star); //[Kg/m^{(3)}]
61 \text{ mu\_star1} = 2.09*10^(-5); // [Kg/m s]
```

```
62 k_star1 = 0.0302; // [W/m degree celsius]
63 Cp_star1 = 1009; // [J/Kg degree celsius]
64
65 // LAMINAR HEAT TRANSFER
66
67 // we assume
68 Re_star_crit = 5*10^{(5)};
69 x_c = Re_star_crit*mu_star/(rho_star*u);// [m]
70 Nu_bar = 0.664*(Re_star_crit)^(1/2)*(Pr_star)^(1/3);
71 h_bar = Nu_bar*k_star/x_c; // [W/m^(2)] degree celsius
      average heat transfer coefficient
72 // heat transfer is calculated as
73 A = x_c*1; // [m^{(2)}]
74 q = h_bar*A*(Tw-(T_aw-273)); // [W]
75
76 // TURBULENT HEAT TRANSFER
77
78 // to determine the turbulent heat transfer we must
      obtain an expression for the local heat transfer
      coefficient from
79 // St_x * Pr_s tar1^(2/3) = 0.0296 * Re_s tar_x^(-1/5)
80 // and then integrate from x = 0.222m to x = 0.7m to
       determine the total heat transfer
81 h_x = integrate('Pr_star1^(-2/3)*rho_star1*u*
      Cp_star1*0.0296*(rho_star1*u*x/mu_star1)^(-1/5)',
      'x',0.222,0.7);// [W/m^{(2)}] degree celsius]
82 // the average heat transfer coefficient in the
      turbulent region is determined from integral h_x
     dx divided by integral dx limit from 0.222 to 0.7
83 h_bar1 = h_x/(integrate('1', 'x', 0.222, 0.7)); //[W/m]
      ^(2) degree celsius]
84 // using this value we may calculate the heat
      transfer in the turbulent region of the flat
      plate:
85 A1 = (L-0.222); // [m^{(2)}]
86 q1 = h_bar1*A1*(Tw-(T_aw1-273)); // W
87
88 // the total amount of cooling required is the sum
```

```
of the heat transfers for the laminar and
    turbulent portions

89  Total_cooling = abs(q)+abs(q1);// [W]
90  printf("the total amount of cooling required is the
    sum of the heat transfers for the laminar and
    turbulent portions is %f W', Total_cooling);
```

Chapter 6

Empirical and Practical Relations for Forced Convection Heat Transfer

Scilab code Exa 6.1 turbulent heat transfer in a tube

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 6.1\n \n \);
4 // turbulent heat transfer in a tube
5 // illustration6.1
6 // solution
8 p = 2*101325; // [Pa] pressure of air
9 Ta = 200+273.15; // [K] temperature of air
10 d = 0.0254; // [m] diameter of tube
11 R = 287; // [] gas constant
12 u = 10; // [m/s] velocity of air
13 dT = 20; // [degree celsius] temperature difference
     between wall and air
14 // we first calculate the reynolds number to
     determine if the flow is laminar or turbulent,
     and then select the appropriate empirical
```

```
correlation to calculate the heat transfer
15 // the properties of air at a bulk temperature of
      473 K are
16 rho = p/(R*Ta); // [kg/cubic meter] density of gas
17 mu = 2.57*10^{(-5)}; // [kg/m s] viscosity
18 k = 0.0386; // [W/m degree celsius]
19 Cp = 1025; // [J/kg K]
20 \text{ Pr} = 0.681; // \text{ prandtl no}.
21 Re_d = rho*u*d/mu; // reynolds number
22 disp(Re_d, "reynolds number is");
23 disp("so that the flow is turbulent");
24 // we therefore use equation (6-4a) to calculate the
       heat transfer coefficient
25 \text{ Nu_d} = 0.023*\text{Re_d^(0.8)*Pr^(0.4)}; // \text{ nusselt no.}
26 h = Nu_d*k/d; // [W/m^2 degree celsius] heat transfer
       coefficient
27 // the heat transfer per unit length is then
28 \text{ q_by_L} = h*\%pi*d*(dT); // [W/m]
29 L = 3; // [m]
30 // we can now make an energy balance to calculate
      the increase in bulk temperature in a 3 m length
      of tube:
31 // q = m_{dot}*Cp*dT_b = L*(q_byL)
32 m_dot = rho*u*%pi*d^(2)/4; // [kg/s] gas flow rate
33 // so that we insert the numerical values in the
      energy balance to obtain
34 \text{ dT_b} = L*q_by_L/(m_dot*Cp); // [degree celsius]
35 printf("\n heat transfer per unit length is %f W/m",
      q_by_L);
36 printf("\n\n bulk temperature increase over the
      length of 3 m on tube is %f degree celsius ",dT_b
      );
```

Scilab code Exa 6.2 heating of water in laminar tube flow

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.2 \ln n");
4 // heating of water in laminar tube flow
5 // illustration6.2
6 // solution
8 Tw = 60; // [degree celsius] temperature of water
9 d = 0.0254; // [m] diameter of tube
10 R = 287; // [] gas constant
11 u = 0.02; // [m/s] velocity of water
12 Tw = 80; // [degree celsius] temperature of wall
13 L = 3; // [m] length of the tube
14 // we first calculate the reynolds number at the
     inlet bulk temperature to determine the flow
     regime
15 // the properties of water at temperature of 333.15
      K are
16 rho = 985; // [kg/cubic meter] density of gas
17 mu = 4.71*10^(-4); // [kg/m s] viscosity
18 k = 0.651; // [W/m degree celsius]
19 Cp = 4.18*10^3; // [J/kg K]
20 \text{ Pr} = 3.02; // \text{ prandtl no.}
21 Re_d = rho*u*d/mu;// reynolds number
22 disp(Re_d, "reynolds number is");
23 disp("so that the flow is laminar");
24 // so the flow is laminar, calculating the
      additional parameter, we have
25 B = Re_d*Pr*d/L ;
26 // since the value of B is greater than 10, so
      equation (6-10) is applicable.
27 // firstly making the calculation on the basis of 60
       degree celsius, determine the exit bulk
     temperature
28 // the energy balance becomes q = h*pi*d*L(Tw-(Tb1+
     Tb2)/2) = m_dot*Cp*(Tb2-Tb1) say equation a
29 // at the wall temperature of 80 degree celsius
30 mu_w = 3.55*10^(-4); // [kg/m s]
```

```
31 // from equation (6-10)
32 \text{ Nu_d} = 1.86*(B)^(1/3)*(mu/mu_w)^(0.14);
33 h = k*Nu_d/d;
34 // the mass flow rate is
35 m_dot = rho*%pi*d^(2)*u/4; // [kg/s]
36 // inserting the values in equation a
37 Tb1 = 60; // [degree celsius]
38 deff('[y] = f(Tb2)', 'y = (h*\%pi*d*L*(Tw-(Tb1+Tb2)/2)
      -m_{dot}*Cp*(Tb2-Tb1))')
39 \text{ Tb2} = \text{fsolve}(1,f);
40 Tb_mean = (Tb1+Tb2)/2; // [degree celsius]
41 // we obtain the properties at Tb_mean
42 rho1 = 982; // [kg/m^{\circ}(3)] density of gas
43 mu1 = 4.36*10^(-4); // [kg/m s] viscosity
44 k1 = 0.656; // [W/m degree celsius]
45 Cp1 = 4.185*10^3; // [J/kg K]
46 Pr1 = 2.78; // prandtl no.
47 \text{ Re_d1} = \text{Re_d*mu/mu1};
48 C = Re_d1*Pr1*d/L;
49 \text{ Nu_d1} = 1.86*(C)^(1/3)*(mu1/mu_w)^(0.14);
50 h = k1*Nu_d1/d;
51 // we insert this value of h back into equation a to
       get
52 deff('[y] = f(Tb2)', 'y = (h*\%pi*d*L*(Tw-(Tb1+Tb2)/2)
      -m_{dot}*Cp*(Tb2-Tb1))')
53 \text{ Tb2} = \text{fsolve}(1,f);
54 printf("\n the exit water temperature is %f degree
      celsius", Tb2);
```

Scilab code Exa 6.3 heating of air in laminar tube flow for constant heat flux

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.3\n\n\n");
```

```
4 // heating of air in laminar tube flow for constant
      heat flux
5 // illustration6.3
6 // solution
8 p = 101325; // [Pa] pressure of air
9 Ta = 27; // [degree celsius] temperature of air
10 d = 0.005; // [m] diameter of tube
11 R = 287; // [] gas constant
12 u = 3; // [m/s] velocity of air
13 L = 0.1; // [m] length of tube
14 Tb = 77; // [degree celsius] exit bulk temperature
15 // we first must evaluate the flow regime and do so
      by taking properties at the average bulk
      temperature
16 Tb_bar = (Ta+Tb)/2; // [degree celsius]
17 v = 18.22*10^(-6); // [square meter/s] kinematic
      viscosity
18 k = 0.02814; // [W/m degree celsius]
19 Cp = 1006; // [J/kg K]
20 \text{ Pr} = 0.703; // \text{ prandtl no}.
21 Re_d = u*d/v; // reynolds number
22 disp(Re_d, "reynolds number is");
23 disp("so that the flow is laminar");
24 // so that the flow is laminar
25 //the tube length is short, so we expect a thermal
      entrance effect and shall consult figure (6-5)
26 // the inverse Graetz number is computed as
27 Gz_inverse = L/(Re_d*Pr*d);
28 // therefore, for qw = constant, we obtain the
      nusselt number at exit from figure (6-5) as
29 \text{ Nu} = 4.7;
30 // the total heat transfer is obtained in terms of
      the overall energy balance
31 // at entrance
32 rho = 1.1774; // [kg/cubic meter] density
33 // \text{ mass flow is}
34 \text{ m\_dot} = \text{rho*\%pi*d^(2)*u/4;} // [kg/s]
```

Scilab code Exa 6.4 heating of air with isothermal tube wall

```
1 clear;
2 clc;
3 printf("\t\tExample Number 6.4 \ln n);
4 // heating of air with isothermal tube wall
5 // illustration 6.4
6 // solution
8 p = 101325; // [Pa] pressure of air
9 Ta = 27; // [degree celsius] temperature of air
10 d = 0.005; // [m] diameter of tube
11 R = 287; // [] gas constant
12 u = 3; // [m/s] velocity of air
13 L = 0.1; // [m] length of tube
14 Tb = 77; // [degree celsius] exit bulk temperature
15 // we first must evaluate the flow regime and do so
     by taking properties at the average bulk
     temperature
```

```
16 Tb_bar = (Ta+Tb)/2;// [degree celsius]
17 \ v = 18.22*10^{(-6)}; // [square meter/s] kinematic
      viscosity
18 k = 0.02814; // [W/m \text{ degree celsius}]
19 Cp = 1006; // [J/kg K]
20 \text{ Pr} = 0.703; // \text{ prandtl no}.
21 Re_d = u*d/v; // reynolds number
22 disp(Re_d, "reynolds number is");
23 disp("so that the flow is laminar");
24 // so that the flow is laminar
25 // now we determine Nu_d-bar for Tw = constant. for
      Gz_{inverse} = 0.0346 we read
26 \text{ Nu_d} = 5.15;
27 // we thus calculate the average heat transfer
      coefficient as
28 h_bar = Nu_d*k/d;// [W/square meter degree celsius]
29 // we base the heat transfer on a mean bulk
      temperature of Tb_bar, so that
30 Tw = 3.49/(h_bar*\%pi*d*L)+Tb_bar;// [degree celsius]
31 printf("\n exit wall temperature is %f degree
      celsius", Tw);
```

Scilab code Exa 6.5 heat transfer in a rough tube

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.5\n\n\n");
4 // heat transfer in a rough tube
5 // illustration6.5
6 // solution
7
8 Tw = 90;// [degree celsius] temperature of tube wall
9 d = 0.02;// [m] diameter of tube
10 u = 3;// [m/s] velocity of air
11 Tw_i = 40;// [degree celsius] entering water
```

```
temperature
12 Tw_f = 60; // [degree celsius] leaving water
      temperature
13 Cp = 4.174*10^3; // [J/kg K]
14 Tb_bar = (Tw_i+Tw_f)/2; // [degree celsius]
15 // we first calculate the heat transfer from q =
      m_{dot}*Cp*dTb
16 q = 989*3*\%pi*0.01^(2)*4174*(Tw_f-Tw_i); // W
17 // for the rough tube condition, we may employ the
      Petukhov relation, equation (6-7) The mean film
      temperaturee is
18 Tf = (Tw+Tb_bar)/2; // [degree celsius]
19 // and the fluid properties are
20 rho = 978; // [kg/cubic meter] density of gas
21 mu = 4.0*10^(-4); // [kg/m s] viscosity
22 k = 0.664; // [W/m degree celsius]
23 Pr = 2.54; // prandtl no.
24 // also
25 mu_b = 5.55*10^(-4); // [kg/m s] viscosity
26 \text{ mu_w} = 2.81*10^{(-4)}; // [kg/m s] viscosity
27 // the reynolds number is thus
28 \text{ Re_d} = \text{rho*u*d/mu};
29 // consulting figure (6-14), we find the friction
      factor as
30 	 f_f = 0.0218;
31 // because Tw>Tb, we take
32 n = 0.11;
33 // and obtain
34 \text{ Nu_d} = ((f_f*Re_d*2.54)/((1.07+12.7*(f_f/8)^(0.5)))
      *(2.54^{(2/3)-1)}*8))*(mu_b/mu_w)^(n);
35 h = Nu_d*k/d;// [W/square meter degree celsius]
36 // the tube length is obtained from energy balance
37 L = q/(h*\%pi*d*(Tw-Tb_bar)); // [m]
38 printf ("the length of tube necessary to accomplish
      the heating is %f m",L);
```

Scilab code Exa 6.6 turbulent heat transfer in a short tube

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 6.6 \n\n\n");
4 // turbulent heat transfer in a short tube
5 // illustration6.6
6 // solution
8 p = 101325; // [Pa] pressure of air
9 Ta = 300; // [K] temperature of air
10 d = 0.02; // [m] diameter of tube
11 u = 40; // [m/s] velocity of air
12 L = 0.1; // [m] length of tube
13 dT = 5; // [degree celsius] rise in temperature
14 // we first must evaluate the air properties at 300
     K
15 v = 15.69*10^{(-6)}; // [square meter/s] kinematic
      viscosity
16 k = 0.02624; // [W/m degree celsius]
17 Cp = 1006; // [J/kg K]
18 Pr = 0.70; // prandtl no.
19 rho = 1.18; // [kg/cubic meter]
20 Re_d = u*d/v; // reynolds number
21 disp(Re_d, "reynolds number is ");
22 disp("so the flow is turbulent");
23 // consulting figure (6-6) for this value of Re<sub>-</sub>d
     and L/d = 5 we find
24 \text{ Nu}_x_by_Nu_inf = 1.15;
25 // or the heat transfer coefficient is about 15
      percent higher that it would be for thermally
      developed flow.
26 // we calculate heat-transfer for developed flow
      using
```

```
27 \text{ Nu_d} = 0.023*\text{Re_d^(0.8)*Pr^(0.4)};
28 // and
29 h = k*Nu_d/d; // [W/square meter degree celsius]
30 // increasing this value by 15 percent
31 h = 1.15*h; // [W/square meter degree celsius]
32 // the mass flow is
33 Ac = \%pi*d^(2)/4;// [square meter]
34 \text{ m\_dot} = \text{rho*u*Ac;} // [\text{kg/s}]
35 // so the total heat transfer is
36 A = \%pi*d*L; // [square meter]
37 \text{ q_by_A} = \text{m_dot*Cp*dT/A;} // [W/square meter]
38 printf("\n the constant heat flux that must be
      applied at the tube surface to result in an air
      temperature rise of 5 degree celsius is %f W/
      square meter", q_by_A);
39 Tb_bar = (Ta+(Ta+dT))/2; // [K]
40 Tw_bar = Tb_bar+q_by_A/h; // [K]
41 printf("\n average wall temperature is %f K",
      Tw_bar);
```

Scilab code Exa 6.7 airflow across isothermal cylinder

```
1 clear;
2 clc;
3 printf("\t\tExample Number 6.7\n\n\n");
4 // airflow across isothermal cylinder
5 // illustration6.7
6 // solution
7
8 p = 101325; // [Pa] pressure of air
9 Ta = 35+273.15; // [K] temperature of air
10 d = 0.05; // [m] diameter of tube
11 R = 287; // [] gas constant
12 u = 50; // [m/s] velocity of air
13 Tc = 150+273.15; // [degree celsius] cylinder
```

```
temperature
14 // we first find the reynolds number and then find
      the applicable constants from table (6-2) for use
      with equation (6-17)
15 // the properties of air are evaluated at the film
      temperature:
16 Tf = (Ta+Tc)/2;//[K]
17 rho_f = p/(R*Tf); // [kg/cubic meter]
18 mu_f = 2.14*10^(-5); // [kg/m s]
19 k_f = 0.0312; // [W/m degree celsius]
20 Pr_f = 0.695;// prandtl number
21 Re_f = rho_f*u*d/mu_f;// reynolds number
22 // from table (6-2) table
23 C = 0.0266;
24 n = 0.805;
25 // so from equation (6-17)
26 h = C*(Re_f)^(n)*(Pr_f)^(1/3)*k_f/d; // [W/square]
     meter degree celsius | heat transfer coefficient
27 // the heat transfer per unit length is
28 \text{ q_by_L} = h*\%pi*d*(Tc-Ta); // [W/m]
29 printf ("heat loss per unit length of cylinder is %f
     W/m", q_by_L);
```

Scilab code Exa 6.8 heat transfer from electrically heated

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.8\n\n\n");
4 // heat transfer from electrically heated
5 // illustration6.8
6 // solution
7
8 p = 101325; // [Pa] pressure of air
9 Tw = 25+273.15; // [K] temperature of air
10 d = 3.94*10^(-5); // [m] diameter of wire
```

```
11 R = 287; // [] gas constant
12 u = 50; // [m/s] velocity of air perpendicular to the
                    air
13 Tr = 50+273.15; // [degree celsius] rise in surface
                 temperature
14 // we first obtain the properties at the film
                 temperature:
15 Tf = (Tw+Tr)/2; // [K]
16 \text{ v_f} = 16.7*10^{(-6)}; // [square meter/s]
17 k = 0.02704; // [W/m degree celsius]
18 Pr_f = 0.706; // prandtl number
19 Re_d = u*d/v_f; // reynolds number
20 // the Peclet number is
21 Pe = Re_d*Pr_f;
22 // and we find that equations (6-17), (6-21), or
                 (6-19) apply.
23 // let us make the calculation with both the
                 simplest expression, (6-17), and the most complex
                  (6-21), and compare results.
24 // using equation (6-17) with
25 C = 0.683;
26 n = 0.466;
27 // we have
28 \text{ Nu_d} = 0.683*\text{Re_d^(n)}*\text{Pr_f^(1/3)};
29 // the value of heat transfer coefficient is
30 h = Nu_d*k/d; // [W/square meter degree celsius]
31 // the heat transfer per unit length is then
32 \, q_by_L = \%pi*d*h*(Tr-Tw); // [W/m]
33 // using equation (6-21), we calculate the nusselt
                 no as
34 \text{ Nu_d1} = 0.3 + ((0.62 * \text{Re_d^(1/2}) * \text{Pr_f^(1/3)}) / ((1 + (0.4 / \text{mag})) + (0.62 * \text{Re_d^(1/2})) + (0.64 / \text{mag}) / (0.64 / \text{mag}
                 Pr_f)^(2/3)^(1/4)*((1+(Re_d/282000)^(5/8))
                 ^{(4/5))};
35 h1 = Nu_d1*k/d; // [W/square meter degree celsius]
37 \text{ q_by_L1} = h1*\%pi*d*(Tr-Tw); // [W/m]
38 printf("heat lost per unit length by the wire is %f
                W/m", q_by_L1);
```

Scilab code Exa 6.9 heat transfer from sphere

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.9 \n\n");
4 // heat transfer from sphere
5 // illustration 6.9
6 // solution
8 p = 101325; // [Pa] pressure of air
9 Ta = 27+273.15; // [K] temperature of air
10 d = 0.012; // [m] diameter of sphere
11 u = 4; // [m/s] velocity of air
12 Ts = 77+273.15; // [degree celsius] surface
     temperature of sphere
13 // consulting equation (6-30) we find that the
     reynolds number is evaluated at the free-stream
     temperature.
14 // we therefore need the following properties at Ta
     = 300.15 K
15 v = 15.69*10^(-6); // [square meter/s]
16 k = 0.02624; // [W/m degree celsius]
17 Pr = 0.708; // prandtl number
18 mu_inf = 1.8462*10^{-5}; // [kg/m s]
19 // at Ts = 350K
20 mu_w = 2.075*10^{(-5)}; // [kg/m s]
21 Re_d = u*d/v; // reynolds number
22 // from equation (6-30),
23 Nu_bar = 2+((0.4)*(Re_d)^(1/2)+0.06*(Re_d)^(2/3))*(
     Pr^(0.4))*((mu_inf/mu_w)^(1/4));
24 // and
25 h_bar = Nu_bar*k/d;// [W/square meter degree celsius
      heat transfer coefficient
26 // the heat transfer is then
```

Scilab code Exa 6.10 heating of air with in line tube bank

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.10\n\n\n");
4 // heating of air with in-line tube bank
5 // Example 6.10(page number-300-302)
6 // solution
7
8 p = 101325; // [Pa] pressure of air
9 Ta = 10+273.15; // [K] temperature of air
10 d = 0.0254; // [m] diameter of tubes
11 Sp = 0.0381; // [m] spacing between tubes in normal and parallel direction
12 Sn = Sp;
13 R = 287; // [] universal gas constant
14 u = 7; // [m/s] velocity of air
15 Ts = 65+273.15; // [K] surface temperature of tubes
```

```
16 // the constants for use with equation (6-17) may be
       obtained from table 6-4 (page no. -298), using
17 Sp_by_d = Sp/d;
18 \text{ Sn_by_d} = \text{Sn/d};
19 // so that
20 C = 0.278;
21 n = 0.620;
22 // the properties of air are evaluated at the film
      temperature, which at entrance to the tube bank
      is
23 Tf = (Ta+Ts)/2; // [K]
24 rho_f = p/(R*Tf); // [kg/cubic meter]
25 \text{ mu_f} = 1.894*10^(-5); // [kg/m s]
26 \text{ k_f} = 0.027; // [W/m \text{ degree celsius}]
27 Pr_f = 0.706; // prandtl number
28 Cp = 1007; // [J/Kg degree celsius]
29 // the maximum velocity is therefore
30 u_max = u*Sn/(Sn-d); // [m/s]
31 // the reynolds number is computed by using the
     maximum velocity
32 \text{ Re} = \text{rho}_f * u_max*d/mu_f;
33 // the heat transfer coefficient is calculated by
      using equation (6-17)
34 h = C*Re^{(n)*Pr_f^{(1/3)*k_f/d}} / W/square meter
      degree celsius
35 // multiplying by 0.92 from table 6-5 (page no. -298)
       to correct for only five tube rows gives
36 h = 0.92*h; // [W/square meter degree celsius]
37 // the total surface area for heat transfer,
      considering unit length of tubes is
38 N = 15*5; // ttal no. of tubes
39 A = N*\%pi*d*1; // [square meter/m]
40 // befre calculating the heat transfer, we must
      recognize that the air temperature increases as
      the air flows thrugh the tube bank.
41 // therefore, this must be taken into account when
      u \sin g = h*A*(Ts-Ta)
42 // as a good approximatin, we can use an arithmetic
```

```
average value of Tinf and write for the energy
     balance
43 // say the equation A is q = h*A*(Ts-(Tinf1+
     Tinf2)/2) = m_dot*Cp*(Tinf2-Tinf1)
44 // where now the subscripts 1 and 2 designate
      entrance and exit to the tube bank.
45 // the mass flow to the entrance to the 15 tubes is
46 rho_inf = p/(R*Ta); // [Kg/m^{(3)}]
47 m_dot=rho_inf*u*15*Sn; // [kg/s]
48 // so that equation A becomes after inserting the
      values and solving
49 Tinf1 = Ta; // [K]
50 deff('[y] = f1(Tinf2)', 'y = (h*A*(Ts-(Tinf1+Tinf2))'
     /2)-m_dot*Cp*(Tinf2-Tinf1))')
51 Tinf2=fsolve(1,f1);
52 // the heat transfer is then obtained from the right
       side of equation A
53 q = m_dot*Cp*(Tinf2-Ta); // [W/m]
54 printf ("the exit air temperature is %f degree
      celsius", Tinf2-273);
55 printf("\n\n heat transfer per unit length for the
     tube bank is \%f \text{ kW/m}, q/1000);
```

Scilab code Exa 6.11 alternate calculation method

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 6.11\n\n\n");
4 // alternate calculation method
5 // example 6.10 (page no.-302)
6 // solution
7
8 // data for this example is taken from previous example (6-10)
9 // properties for use in equation (6-34) are
```

```
evaluated at free-atream conditions of 10 degree
      celsius
10 v = 14.2*10^(-6); // [square meter/s]
11 k = 0.0249; // [W/m degree celsius]
12 Pr = 0.712; // prandtl number
13 Pr_w = 0.70; // prandtl number
14 u = 7; // [m/s] velocity of air
15 Sp = 0.0381; // [m] spacing between normal and
      parallel direction to the flow
16 Sn = 0.0381; // spacing between normal and parallel
      direction to the flow
17 d = 0.0254; // [m] diameter of tube
18 //maximum velocity is
19 u_max = u*(Sn/(Sn-d)); // [m/s]
20 // the reynolds number is
21 Re_d_max = u_max*d/v;
22 // so that the constants for equation (6-34) are
23 \quad C = 0.27;
24 n = 0.63;
25 // inserting values we obtain
26 h = C*Re_d_max^(n)*(Pr/Pr_w)^(1/4)*k/d; // [W/square]
     meter degree celsius | heat transfer coefficient
27 // multiplying by 0.92 from table 6-7 (page no. -300)
      to correct for only five tube rows gives
28 h = 0.92*h; // [W/square meter degree celsius]
29 printf ("the value of heat transfer coefficient is %f
      W/square meter degree celsius",h);
30 h_in = 163.46432; // [W/square meter degree celsius]
     from previous example
31 printf("\n\n the value of heat transfer coefficient
     for previous problem is %f W/square meter degree
      celsius", h_in);
32 P = (h-h_in)*100/h_in;
33 printf("\n\n percentage increase in value of h is %f
     ",P);
```

Scilab code Exa 6.12 heating of liquid bismuth in tube

```
1 clear;
   2 clc;
   3 printf("\t\tExample Number 6.12\n\n");
   4 // heating of liquid bismuth in tube
   \frac{5}{\sqrt{2}} = \frac{11}{\sqrt{2}} = \frac
   6 // solution
   8 m_dot = 4.5; // [Kg/s] flow rate of bismuth
   9 d = 0.05; // [m] diameter of steel tube
10 Ti = 415; // [degree celsius] initial temperature of
                       bismuth
          Tf = 440; // [degree celsius] final temperature of
11
                        bismuth
12 // because a constant heat flux is maintained, we
                       may use equation 6-47 to calculate the heat
                        transfer coefficient.
13 // the properties of bismuth are evaluated at the
                        average bulk temperature of
14 Ta = (Ti+Tf)/2; // [degree celsius]
15 mu = 1.34*10^{(-3)}; // [Kg/m s] viscosity
16 Cp = 149; // [J/Kg degree celsius] heat
17 k = 15.6; // [W/m degree celsius]
18 Pr = 0.013; // prandtl number
19 // the total transfer is calculated from
20 q = m_dot*Cp*(Tf-Ti); // [W]
21 // we calculate reynolds and peclet number as
22 G = m_dot/(\pi v^*d^2)/4);
23 \text{ Re_d} = d*G/mu;
24 \text{ Pe} = \text{Re}_d * \text{Pr};
25 // the heat transfer coefficient is calculated from
                        equation 6-47
26 \text{ Nu_d} = 4.82+0.0185*Pe^(0.827);
```

Chapter 7

Natural Convection Systems

Scilab code Exa 7.1 constant heat flux from vertical plate

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 7.1\n\n");
4 // constant heat flux from vertical plate
5 // \text{Example } 7.1 \text{ (page no.} -330 - 331)
6 // solution
8 q_w = 800; // [W/square meter] radiant energy flux
9 H = 3.5; // [m] height of metal plate surface
10 W = 2; // [m] width of metal plate
11 Ta = 30; // [degree celsius] surrounding air
      temperature
12 // we treat this problem as one with constant heat
      flux on the surface since we do not know the
      surface temperature, we must make an estimate for
      determining Tf and the air properties.
13 // an approximate value of h for free convection
     problems is
14 h = 10; // [W/square meter degree celsius]
15 dT = q_w/h; // [degree celsius]
16 // then
```

```
17 Tf = (dT/2)+Ta; // [degree celsius] approximately
18 // at Tf the properties of air are
19 v = 2.005*10^{(-5)}; // [square meter/s]
20 k = 0.0295; // [W/m degree celsius]
21 Pr = 0.7; // prandtl number
22 Beta = 1/(Tf+273); //[K^{(-1)}]
23 // from equation (7-30), with
24 x = 3.5; // [m]
25 g = 9.8; // [square meter/s] acceleration due to
      gravity
26 \text{ Gr}_x = (g*Beta*q_w*x^(4))/(k*v^(2));
27 // we may therefore use equation (7-32) to evaluate
     h_x
28 h_x = (k*0.17*(Gr_x*Pr)^(1/4))/x; // [W/square meter]
      degree celsius]
  // in the turbulent heat transfer governed by
      equation (7-32), we note that
30 // Nu_x = h*x/k ~ (Gr_x)^(1/4) ~ x
31 // or h_x doest noy vary with x, and we may take
      this as the average value, the value of h
32 h = 5.41; // [W/square meter degree celsius]
33 // is less than the approximate value we used to
      estimate Tf, recalculating dT, we obtain
34 dT1 = q_w/h_x; // [degree celsius]
35 // our new film temperature would be
36 Tf1 = Ta+dT1/2; // [degree celsius]
37 // at Tf the properties of air are
38 v1 = 2.354*10^(-5); // [square meter/s]
39 k1 = 0.0320; // [W/m degree celsius]
40 Pr1 = 0.695; // prandtl number
41 Beta1 = 1/(Tf1+273); //[K^{(-1)}]
42 // then
43 Gr_x1 = (g*Beta1*q_w*x^(4))/(k1*v1^(2));
44 // and h<sub>x</sub> is calculated from
45 \text{ h_x1} = (k1*0.17*(Gr_x1*Pr1)^(1/4))/x; // |W/square
      meter degree celsius]
46 // our new temperature difference is calculated as
dT2 = q_w/h_x1; // [degree celsius]
```

```
48 // the average wall temperature is therefore
49 T_w_avg = dT2+Ta; // [degree celsius]
50 printf("the average wall temperature is therefore %f degree celsius", T_w_avg);
```

Scilab code Exa 7.2 heat transfer from isothermal vertical plate

```
1 clear;
2 clc;
3 printf("\t\tExample Number 7.2\n\n");
4 // heat transfer from isothermal vertical plate
5 // \text{Example } 7.2 \text{ (page no.} -332)
6 // solution
8 H = 4; // [m] height of vertical plate
9 Tp = 60;// [degree celsius] plate temperature
10 Ta = 10; // [degree celsius] atmospheric temperature
11 // we first determine the film temperature as
12 Tf = (Tp+Ta)/2; // [degree celsius]
13 // the properties of interest are thus
14 v = 16.5*10^{(-6)}; // [square meter/s]
15 k = 0.02685; // [W/m degree celsius]
16 Pr = 0.7; // prandtl number
17 Beta = 1/(Tf+273); //[K^{\hat{}}(-1)]
18 g = 9.8; // [square meter/s] acceleration due to
      gravity
19 // and
20 Gr_into_Pr = (g*Beta*(Tp-Ta)*H^(3)*Pr)/(v^(2));
21 // we then may use equation (7-29) to obtain
22 \text{ Nu\_bar\_root} = 0.825 + (0.387 * (Gr\_into\_Pr)^(1/6))
      /(1+(0.492/Pr)^(9/16))^(8/27);
23 \text{ Nu\_bar} = (\text{Nu\_bar\_root})^{(2)};
24 // the heat transfer coefficient is
25 h_bar = Nu_bar*k/H;// [W/square meter degree celsius
```

```
26  // the heat transfer is
27  A = H*10; // [square meter] for 10 m wide plate
28  q = h_bar*A*(Tp-Ta); // [W]
29  // as an alternative, we could employ the simpler
    relation
30  Nu = 0.1*(Gr_into_Pr)^(1/3);
31  printf("heat transfer if the plate is 10 m wide is
    %f W",q);
```

Scilab code Exa 7.3 heat transfer from horizontal tube in water

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.3\n\n'");
4 // heat transfer from horizontal tube in water
5 // \text{Example } 7.3 \text{ (page no.} -333)
6 // solution
8 d = 0.02; // [m] diameter of heater
9 Ts = 38; // [degree celsius] surface temperature of
      heater
10 Tw = 27; // [degree celsius] water temperature
11 // the film temperature is
12 Tf = (Ts+Tw)/2; // [degree celsius]
13 // from appendix A the properties of water are
14 k = 0.630; // [W/m degree celsius] thermal
      conductivity
15 // and the following term is particularly useful in
      obtaining the product GrPr product when it is
      multiplied by d^{(3)}*DT
16 // g*Beta*rho^{(2)}*Cp/(mu*k) = 2.48*10^{(10)} [1/m^{(3)}]
     degree celsius]
17 K = 2.48*10^(10); // [1/m^(3)] degree celsius
18 Gr_into_Pr = K*(Ts-Tw)*d^(3);
19 // using table 7-1 (page number -328), we get
```

Scilab code Exa 7.4 heat transfer from fine wire in air

```
1 clear;
2 clc;
3 printf("\t\tExample Number 7.4 \ln n);
4 // heat transfer from fine wire in air
5 // Example 7.4 (page no. -333-334)
6 // solution
8 d = 0.00002; // [m] diameter of wire
9 L = 0.5; // [m] length of wire whose temperature is
     maintained
10 Ts = 54; // [degree celsius] surface temperature of
      wire
11 Pa = 101325; // [Pa] pressure of air
12 Ta = 0; // [degree celsius] temperature of air
13 // we first determine the film temperature as
14 Tf = (Ts+Ta)/2; // [degree celsius]
15 // the properties of interest are thus
16 \ v = 15.69*10^{(-6)}; // [square meter/s]
17 k = 0.02624; // [W/m \text{ degree celsius}]
18 Pr = 0.708; // prandtl number
19 Beta = 1/(Tf+273); //[K^{(-1)}]
20 g = 9.8; // [square meter/s] acceleration due to
```

```
gravity
21 // and
22 Gr_into_Pr = (g*Beta*(Ts-Ta)*d^(3)*Pr)/(v^(2));
23 // from table 7-1 we find
24 C = 0.675;
25 m = 0.058;
26 // so that
27 Nu_bar = C*(Gr_into_Pr)^(m);
28 h_bar = Nu_bar*k/d;// [W/square meter degree celsius]
29 // the heat required is
30 A = %pi*d*L;// [square meter] surface area of wire
31 q = h_bar*A*(Ts-Ta);// [W]
32 printf("electric power necessary to maintain the the wire temperature if the length is 0.5 m is %f W",q);
```

Scilab code Exa 7.5 heated horizontal pipe in air

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.5\n\n\n");
4 // heated horizontal pipe in air
5 // Example 7.5 (page no.-334-335)
6 // solution
7
8 d = 0.3048; // [m] diameter of pipe
9 Ts = 250; // [degree celsius] surface temperature of pipe
10 Ta = 15; // [degree celsius] temperature of air
11 // we first determine the Grashof-prandtl number product and then select the appropriate constants from table 7-1(page no.-328) for use with equation (7-25)
12 // the properties of air are evaluated at the film
```

```
temperature:
13 Tf = (Ts+Ta)/2; // [degree celsius]
14 // the properties of interest are thus
15 v = 26.54*10^{(-6)}; // [square meter/s]
16 k = 0.03406; // [W/m degree celsius]
17 Pr = 0.687; // prandtl number
18 Beta = 1/(Tf+273); //[K^{(-1)}]
19 g = 9.8; // [square meter/s] acceleration due to
      gravity
20 Gr_d_into_Pr = g*Beta*(Ts-Ta)*d^(3)*Pr/(v^(2));
21 // from table 7-1
22 C = 0.53;
23 \text{ m} = 1/4;
24 \text{ Nu_d} = C*(Gr_d_into_Pr)^(m);
25 h = Nu_d*k/d; // [W/square meter degree celsius]
26 // the heat transfer per unit length is then
      calculated from
27 \text{ q_by_L = } h*\%pi*d*(Ts-Ta); // [W/m]
28 printf ("free-convection heat loss per unit length is
       \%f kW/m",q_by_L/1000);
```

Scilab code Exa 7.6 cube cooling in air

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.6\n\n\n");
4 // cube cooling in air
5 // Example 7.6 (page no.-336)
6 // solution
7
8 L = 0.2; // [m] side length of cube
9 Ts = 60; // [degree celsius] surface temperature of cube
10 Ta = 10; // [degree celsius] air temperature
11 // this is an irregular solid so we use the
```

```
information in the last entry of table 7-1 (page
     no.-328) in the absence of a specific correlation
       for this
                   geometry.
12 // the properties were evaluated as
13 v = 17.47*10^(-6); // [square meter/s]
14 k = 0.02685; // [W/m degree celsius]
15 Pr = 0.70; // prandtl number
16 Beta = 3.25*10^{(-3)}; // [K^{(-1)}]
17 g = 9.8; // [square meter/s] acceleration due to
     gravity
18 // the characteristic length is the distance a
     particle travels in the boundary layer, which is
     L/2 along the bottom plus L along the side plus L
     /2 on the top or
19 Gr_{into_Pr} = (g*Beta*(Ts-Ta)*(2*L)^(3)*Pr)/(v^(2));
20 // from the last entry in table 7-1 we find
21 C = 0.52;
22 n = 1/4;
23 // so that
24 Nu = C*(Gr_into_Pr)^(n);
25 h_bar = Nu*k/(2*L);// [W/square meter degree celsius
26 // the cube has six sides so the area is
27 A = 6*L^{(2)}; // [square meter]
28 // the heat required is
29 q = h_bar*A*(Ts-Ta); // [W]
30 printf("heat transfer is %f W',q);
```

Scilab code Exa 7.7 calculation with simplified relations

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.7\n\n\n");
4 // calculation with simplified relations
5 // Example 7.7 (page no.-338-339)
```

```
6 // solution
8 // this example is calculation of heat transfer with
       simplified relations for example (7.5) so we use
       the data of example 7.5
10 d = 0.3048; // [m] diameter of pipe
11 Ts = 250; // [degree celsius] surface temperature of
     pipe
12 Ta = 15; // [degree celsius] temperature of air
13 // we first determine the Grashof-prandtl number
     product and then select the appropriate constants
      from table 7-1 (page no. -328) for use with
                   equation (7-25)
14 // the properties of air are evaluated at the film
     temperature:
15 Tf = (Ts+Ta)/2; // [degree celsius]
16 // the properties of interest are thus
17 v = 26.54*10^{(-6)}; // [square meter/s]
18 k = 0.03406; // [W/m degree celsius]
19 Pr = 0.687; // prandtl number
20 Beta = 1/(Tf+273); //[K^{(-1)}]
21 g = 9.8; // [square meter/s] acceleration due to
     gravity
22 // in example (7.5) we found that a rather large
     pipe with a substantial temperature difference
     between the surface and air still had a GrPr
     product of 1.57*10^{(8)} < 10^{(9)}, so laminar
     equation is selected from table 7-2 (page no. -339)
     . the heat transfer coefficient is given by
23 h = 1.32*((Ts-Ta)/d)^(1/4); // [W/square meter degree]
      celsius
24 // the heat transfer is then
25 \text{ q_by_L} = h*\%pi*d*(Ts-Ta); // [W/m]
26 printf("heat transfer is %f kW/m",q_by_L/1000);
```

Scilab code Exa 7.8 heat transfer across vertical air gap

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 7.8\n\n");
4 // heat transfer across vertical air gap
5 / \text{Example } 7.8 \text{ (page no.} -345)
6 // solution
8 L = 0.5; // [m] side length vertical square plate
9 d = 0.015; // [m] distance between plates
10 p = 101325; // [Pa] pressure of air
11 R = 287; // [] universal gas constant
12 T1 = 100; // [degree celsius] temperature of first
      plate
13 T2 = 40; // [degree celsius] temperature of second
14 E = 0.2; // emissivity of both surfaces
15 // the properties of air is evaluated at the mean
      temperature
16 Tf = (T1+T2)/2; // [degree celsius]
17 rho = p/(R*(Tf+273)); // [Kg/m^(3)] density
18 k = 0.0295; // [W/m degree celsius]
19 Pr = 0.70; // prandtl number
20 Beta = 1/(Tf+273); //[K^{(-1)}]
21 mu = 2.043*10^{(-5)}; // [Kg/m s] viscosity
22 g = 9.8; // [square meter/s] acceleration due to
      gravity
23 // the Grashof-prandtl number product is now
      calculated as
24 \text{ Gr_into_Pr} = (g*rho^(2)*Beta*(T1-T2)*(d)^(3)*Pr)/(mu)
      ^(2));
25 // we may now use equation (7-64) to calculate the
      effective thermal conductivity, with
```

```
26 L = 0.5; // [m]
27 \text{ del} = 0.015; // [m]
28 // and the constants taken from table 7-3 (page no
      .-344):
29 Ke_by_K = 0.197*(Gr_into_Pr)^(1/4)*(L/del)^(-1/9);
30 // the heat transfer may now be calculated with
      equation (7-54). the area is
31 A = L^{(2)}; // [square meter]
32 q = Ke_by_K*k*A*(T1-T2)/del; // [W]
33 // the radiation flux is calculated with equation
       (7-67), taking
34 \text{ T1} = 373; // [K]
35 T2 = 313; // [K]
36 E1 = E;
37 E2 = E;
38 sigma = 5.669*10^(-8); // [W/square meter K^(4)]
39 \text{ q_A} = \text{sigma*}(T1^(4)-T2^(4))/((1/E1)+(1/E2)-1); // W/
      square meter]
40 \text{ q\_rad} = A*q\_A; // [W]
41 printf ("free-convection heat transfer across the air
       space is %f W',q);
42 printf("\n\nradiation heat transfer across the air
      space is %f W",q_rad);
```

Scilab code Exa 7.9 heat transfer across horizontal air gap

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.9\n\n");
4 // heat transfer across horizontal air gap
5 // Example 7.9 (page no.-346)
6 // solution
7
8 a = 0.2;// [m] side length of plate
9 d = 0.01;// [m] seperation between two plates
```

```
10 p = 101325; // [Pa] pressure of air
11 R = 287; // [] universal gas constant
12 T1 = 100; // [degree celsius] temperature of first
      plate
13 T2 = 40; // [degree celsius] temperature of second
      plate
14 // the properties are the same as given in example
      (7.8)
15 Tf = (T1+T2)/2; // [degree celsius]
16 rho = p/(R*(Tf+273)); // [Kg/m^{3}] density
17 k = 0.0295; // [W/m degree celsius]
18 Pr = 0.70; // prandtl number
19 Beta = 1/(Tf+273); //[K^{(-1)}]
20 mu = 2.043*10^{(-5)}; // [Kg/m s] viscosity
21 g = 9.8; // [square meter/s] acceleration due to
      gravity
22 // the GrPr product is evaluated on the basis of the
      separating distance, so we have
23 Gr_{into_Pr} = (g*rho^{(2)}*Beta*(T1-T2)*(d)^{(3)}*Pr)/(mu
      ^(2));
24 // consulting table 7-3(page no. -344) we find
25 C = 0.059;
26 n = 0.4;
27 \text{ m} = 0;
28 Ke_by_K = C*(Gr_into_Pr)^(n)*(a/d)^(m);
29 A = a^(2); // [square meter] area of plate
30 q = Ke_by_K*k*A*(T1-T2)/d; // |W|
31 printf ("heat transfer across the air space is %f W",
     q);
```

Scilab code Exa 7.10 heat transfer across water layer

```
1 clear; 2 clc; 3 printf("\t \t \t Example Number 7.10\n \n \);
```

```
4 // heat transfer across water layer
5 / \text{Example } 7.10 \text{ (page no.} -346 - 347)
6 // solution
8 L = 0.5; // [m] length of square plate
9 d = 0.01; // [m] separation between square plates
10 T1 = 100; // [degree F] temperature of lower plate
11 T2 = 80; // [degree F] temperature of upper plate
12 // we evaluate properties at mean temperature of 90
      degree F and obtain, for water
13 k = 0.623; // [W/m degree celsus]
14 // and the following term is particularly useful in
      obtaining the product GrPr
15 / g*Beta*rho^(2)*Cp/(mu*k) = 2.48*10^(10) [1/m^(3)]
      degree celsius]
16 // the Grashof-prandtl number product is now
      evaluated using the plate spacing of 0.01 m as
      the characterstic dimension
17 K = 2.48*10^(10); // [1/m^(3)] degree celsius
18 Gr_{into_Pr} = K*(T1-T2)*(5/9)*d^(3);
19 // now, using equation 7-64 and consulting table
      7-3(page no. -344) we obtain
20 C = 0.13;
21 \quad n = 0.3;
22 \text{ m} = 0;
23 // therefore, equation (7-64) becomes
24 Ke_by_K = C*Gr_into_Pr^(n);
25 // the effective thermal conductivity is thus
26 ke = k*Ke_by_K; // [W/m degree celsius]
27 // and the heat transfer is
28 A = L^(2); // [square meter] area of plate
29 q = ke*A*(T1-T2)*(5/9)/d;//W
30 printf("heat lost by the lower plate is %f W",q);
```

Scilab code Exa 7.11 reduction of convection in ar gap

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 7.11 \n \n");
4 // reduction of convection in ar gap
5 // \text{ Example } 7.11 \text{ (page no.} -347)
6 // solution
8 Tm = 300; // [K] mean temperature of air
9 dT = 20; // [degree celsius] temperature difference
10 R = 287; // [] universal gas constant
11 g = 9.81; // [m/s^(2)] acceleration due to gravity
12 p_atm = 101325; // [Pa] atmospheric pressure
13 // consulting table 7-13 (page no. -344), we find that
       for gases, a value Grdel_into_Pr <2000 is
      necessary to reduce the system to one of pure
      conduction.
14 // at 300 K the properties of air are
15 k = 0.02624; // [W/m degree celsius]
16 Pr = 0.7; // prandtl no.
17 mu = 1.846*10^{(-5)}; // [Kg/m s]
18 Beta = 1/300;
19 // we have
20 \text{ Grdel\_into\_Pr} = 2000;
21
22 // Part A for spacing of 1cm
23
24 del = 0.01; // [m] spacing between plate
25 p = sqrt((Grdel_into_Pr*((R*Tm)^(2))*mu^(2))/(g*Beta)
      *dT*del^(3)*Pr));// [Pa]
26 // or vacuum
27 \text{ vacuum} = p_atm-p; // [Pa]
28 printf ("vacuum necessary for glass spacings of 1 cm
      is %f Pa", vacuum);
29
30 // Part B for spacing of 2cm
31
32 \text{ del1} = 0.02; // [m] \text{ spacing between plate}
33 p1 = sqrt(Grdel_into_Pr*(R*Tm)^(2)*mu^(2)/(g*Beta*dT)
```

Scilab code Exa 7.12 heat transfer across evacuated space

```
1 clear;
2 clc;
3 printf("\t\tExample Number 7.12\n\n");
4 // heat transfer across evacuated space
5 / \text{Example } 7.12 \text{ (page no.} -351 - 352)
6 // solution
8 E = 0.06; // emmissity of polished aluminium plate
9 d = 0.025; // [m] separation between plates
10 p = 101325*10^{(-6)}; // [Pa] pressure of air between
      plates
11 T1 = 100; // [degree celsius] temperature of plate 1
12 T2 = 30; // [degree celsius] temperature of plate 2
13 // we first calculate the mean free path to
      determine if low-density effects to be important.
14 // evaluating properties at the mean air temperature
       of 65 degree celsius, we have
15 lambda = (2.27*10^{-5})*((T1+T2)/2+273))/(p);//[m]
16 // since the plate spacing is only 2.5 cm, we should
       expect low-density effects to be important.
17 // evaluating properties at the mean temperature of
     65 degree celsius, we have
18 k = 0.0291; // [W/m degree celsius]
19 Gamma = 1.40;
20 \text{ Pr} = 0.7;
21 alpha = 0.9; // from table 7-4(page no. -350)
22 // combining equations (7-75) with the central
```

```
temperature gradient relation gives
23 // inserting the appropriate properties gives
24 deff('y = f(dT)', 'y = dT - ((2-alpha)/alpha) * (2*Gamma)
     /(Gamma+1))*(lambda/Pr)*((T1-T2-2*dT)/d)');
25 	ext{ dT = fsolve}(1,f);
26 // the conduction heat transfer is thus
27 \text{ q_by_A} = k*((T1-T2-2*dT)/d); // [W/square meter]
28 printf ("conduction heat transfer through the air gap
       is %f W/square meter", q_by_A);
29 // at normal atmospheric pressure the conduction
     would be
30 q_by_A1 = k*((T1-T2)/d); // [W/square meter]
31 // the radiation heat transfer is calculated with
      equation (8-42), taking E1=E2=0.06 for polished
     aluminium:
32 \text{ sigma} = 5.669*10^{(-8)}; //
33 q_by_A_rad = sigma*(((T1+273)^(4)-(T2+273)^(4))/((2/4))
     E)-1));// [W/square meter]
34 printf("\n thus, at the low density condition the
      radiation heat transfer is almost %f times as
     large as the conduction", q_by_A_rad/q_by_A);
```

Scilab code Exa 7.13 combined free and forced convection with air

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 7.13\n\n\n");
4 // combined free and forced convection with air
5 // Example 7.12 (page no.-353-355)
6 // solution
7
8 p = 101325;// [Pa] pressure of air
9 Ta = 27;// [degree celsius] temperature of air
10 d = 0.025;// [m] diameter of tube
11 u = 0.3;// [m/s] velocity of air
```

```
12 Tw = 140; // [degree celcius] temperature of tube
      wall
13 L = 0.4; // [m] length of tube
14 R = 287; // [] universal gas constant
15 // the properties of air are evaluated at the film
      temperature:
16 Tf = (Tw+Ta)/2; // [degree celcius]
17 // the properties of interest are thus
18 kf = 0.0305; // [W/m degree celcius]
19 Pr = 0.695; // prandtl number
20 Beta = 1/(Tf+273); //[K^{(-1)}]
21 g = 9.8; // [square meter/s] acceleration due to
      gravity
22 \text{ mu_f} = 2.102*10^{(-5)}; // [Kg/m s]
23 mu_w = 2.337*10^(-5); // [Kg/m s]
24 rho_f = p/(R*(Tf+273)); // [Kg/cubic meter]
25 // let us take the bulk temperature as 27 degree
      celsius for evaluating mu_b; then
26 \text{ mu_b} = 1.8462*10^(-5); // [Kg/m s]
27 // the significant parameters are calculated as
28 \text{ Re_f} = \text{rho_f*u*d/mu_f};
29 Gr = rho_f^{(2)}*g*Beta*(Tw-Ta)*d^{(3)}/mu_f^{(2)};
30 Z = Gr*Pr*d/L; // constant
31 // according to figure (7-14) (page no. -354), the
      mixed convection flow regime is encountered. thus
       we must use equation (7-77).
32 // The graetz number is calculated as
33 \text{ Gz} = \text{Re}_f * \text{Pr} * d/L;
34 // and the numerical calculation for equation (7-77)
      becomes
35 Nu = 1.75*(mu_b/mu_w)^(0.14)*[Gz+0.012*(Gz*Gr^(1/3))
      (4/3)](1/3);
36 // the average heat transfer coefficient is
      calculated as
37 h_bar = Nu*kf/d;// [W/square meter degree celsius]
38 printf ("heat transfer coefficient is %f W/square
      meter degree celsius",h_bar);
```

Chapter 8

Radiation Heat Transfer

Scilab code Exa 8.1 transmission and absorption in a gas plate

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 8.1\n\n");
4 // transmission and absorption in a gas plate
5 // Example 8.1  (page no. -381)
6 // solution
8 T = 2000+273; // [K] furnace temperature
9 L = 0.3;// [m] side length of glass plate
10 t1 = 0.5; // transmissivity of glass between lambda1
      to lambda2
11 lambda1 = 0.2; // [micro m]
12 lambda2 = 3.5; // [micro m]
13 E1 = 0.3; // emissivity of glass upto lambda2
14 E2 = 0.9; // emissivity of glass above lambda2
15 t2 = 0; // transmissivity of glass except in the
      range of lambda1 to lambda2
16 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
17 A = L^(2); // [square meter] area of glass plate
18 // calculating constants to use table 8-1(page no
     .-379-380)
```

```
19 K1 = lambda1*T; // [micro m K]
20 K2 = lambda2*T; // [micro m K]
21 // from table 8-1
22 \quad Eb_0_lam1_by_sigmaT4 = 0;
23 \text{ Eb}_0=1 \text{am}_2=\text{by}_sigmaT4 = 0.85443;
24 Eb = sigma*T^(4); // [W/square meter]
25 // total incident radiation is
26 // for 0.2 micro m to 3.5 micro m
27 TIR = Eb*(Eb_0_lam2_by_sigmaT4-Eb_0_lam1_by_sigmaT4)
      *A; // [W]
28 TRT = t1*TIR; // [W]
29 RA1 = E1*TIR; // [W] for 0 < lambda < 3.5 micro m
30 RA2 = E2*(1-Eb_0_lam2_by_sigmaT4)*Eb*A;//[W]
      3.5 micro m < lambda < infinity
31 TRA = RA1+RA2; // [W]
32 printf("total energy absorbed in the glass is %f kW"
      ,TRA/1000);
33 printf("\n total energy transmitted by the glass
      is %f kW", TRT/1000);
```

Scilab code Exa 8.2 heat transfer between black surfaces

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.2\n\n\n");
4 // heat transfer between black surfaces
5 // Example 8.2 (page no.-389-390)
6 // solution
7
8 L = 1; // [m] length of black plate
9 W = 0.5; // [m] width of black plate
10 T1 = 1000+273; // [K] first plate temperature
11 T2 = 500+273; // [K] second plate temperature
12 sigma = 5.669*10^(-8); // [W/square meter K^(4)]
13 // the ratios for use with figure 8-12(page no.-386)
```

```
are
14 Y_by_D = W/W;
15 X_by_D = L/W;
16 // so that
17 F12 = 0.285; // radiation shape factor
18 // the heat transfer is calculated from
19 q = sigma*L*W*F12*(T1^(4)-T2^(4));
20 printf("net radiant heat exchange between the two plates is %f kW",q/1000);
```

Scilab code Exa 8.3 shape factor algebra for open ends of cylinder

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.3\n\n'");
4 // shape-factor algebra for open ends of cylinder
5 // \text{Example } 8.3 \text{ (page no.} -395)
6 // solution
8 d1 = 0.1; // [m] diameter of first cylinder
9 d2 = 0.2; // [m] diameter of second cylinder
10 L = 0.2; // [m] length of cylinder
11 // we use the nomenclature of figure 8-15(page no
      (-388) for this problem and designate the open
      ends as surfaces 3 and 4.
12 // we have
13 L_by_r2 = L/(d2/2);
14 r1_by_r2 = 0.5;
15 // so from figure 8-15 or table 8-2(page no. -389) we
       obtain
16 	ext{ F21 = 0.4126};
17 F22 = 0.3286;
18 // using the reciprocity relation (equation 8-18) we
       have
19 F12 = (d2/d1)*F21;
```

```
20 // for surface 2 we have F12+F22+F23+F24 = 1.0
21 // and from symmetry F23 = F24 so that
22 	ext{ F23} = (1-F21-F22)/2;
23 	ext{ F24} = 	ext{F23};
24 // using reciprocity again,
25 A2 = \%pi*d2*L; // [m<sup>2</sup>]
26 \text{ A3} = \text{\%pi*(d2^2-d1^2)/4;// [m^2]}
27 F32 = A2*F23/A3;
28 // we observe that F11 = F33 = F44 = 0 and for
       surface 3 \text{ F}31+\text{F}32+\text{F}34 = 1.0
29 // so, if F31 can be determined, we can calculate
      the desired quantity F34. for surface 1 F12+F13+
      F14 = 1.0
30 // and from symmetry F13 = F14 so that
31 \text{ F13} = (1-\text{F12})/2;
32 \text{ F14} = \text{F13};
33 // using reciprocity gives
34 A1 = \%pi*d1*L;// [square meter]
35 \text{ F31} = (A1/A3)*F13;
36 // then
37 \text{ F34} = 1 - \text{F31} - \text{F32};
38 printf("shape factor between the open ends of the
       cylinder is %f ",F34);
```

Scilab code Exa 8.4 shape factor algebra for truncated cone

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.4\n\n\n");
4 // shape-factor algebra for truncated cone
5 // Example 8.4 (page no.-396)
6 // solution
7
8 d1 = 0.1; // [m] diameter of top of cone
9 d2 = 0.2; // [m] diameter of bottom of cone
```

```
10 L = 0.1; // [m] height of cone
11 // we employ figure 8-16 (page no. -390) for solution
                of this problem and take the nomenclature as
                shown, designating the top as surface 2,
12 // the bottom as surface 1, and the side as surface
                3. thus the desired quantities are F23 and F33.
                we have
13 Z = L/(d2/2);
14 Y = (d1/2)/L;
15 // thus from figure 8-16 (page no. -390)
16 \text{ F12} = 0.12;
17 // from reciprcity (equatin 8-18)
18 A1 = \%pi*d2^(2)/4;// [square meter]
19 A2 = %pi*d1^(2)/4;// [square meter]
20 \text{ F21} = \text{A1*F12/A2};
21 / and
22 	ext{ F22 = 0};
23 // so that
24 F23 = 1-F21;
25 // for surface 3 F31+F32+F33 = 1, so we must find
                F31 and F32 in order to evaluate F33. since F11 =
                   0 we have
26 	ext{ F13} = 1 - F12;
27 // and from reciprocity
28 A3 = \pi(d1+d2)/2 = (d1/2-d2/2)^2 = \pi(d1/2-d2/2)^2 = \pi(d1/2-d
             // [square meter]
29 // so from above equation
30 \text{ F31} = \text{A1*F13/A3};
31 // a similar procedure is applies with surface 2 so
                that
32 F32 = A2*F23/A3;
33 // finally from above equation
34 	ext{ F33} = 1-F32-F31;
35 printf("shape factor between the top surface and the
                   side is %f ",F23);
36 printf("\nshape factor between the side and itself
                is %f ",F33);
```

Scilab code Exa 8.5 shape factor algebra for cylindrical reflactor

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 8.5 \n\n");
4 // shape-factor algebra for cylindrical reflactor
5 // Example 8.5 (page no. -397 - 398)
6 // solution
8 d = 0.6; // [m] diameter of long half-circular
      cylinder
9 L = 0.2; // [m] length of square rod
10 // we have given figure example 8-5(page no. -397)
     for solution of this problem and take the
      nomenclature as shown,
11 // from symmetry we have
12 F21 = 0.5;
13 \text{ F23} = \text{F21};
14 // in general, F11+F12+F13 = 1. to aid in the
      analysis we create the fictious surface 4 shown
     in figure example 8-5 as dashed line.
15 // for this surface
16 \text{ F41} = 1.0;
17 // now, all radiation leaving surface 1 will arrive
      either at 2 or at 3. likewise, this radiation will
       arrive at the imaginary surface 4, so that F41 =
      F12+F13 say eqn a
18 // from reciprocity
19 A1 = \%pi*d/2;// [square meter]
20 A4 = L+2*sqrt(0.1^(2)+L^(2)); [square meter]
21 A2 = 4*L; // [square meter]
22 // so that
23 F14 = A4*F41/A1; // say eqn b
24 // we also have from reciprocity
```

```
25 F12 = A2*F21/A1; // say eqn c
26 // combining a,b,c, gives
27 F13 = F14-F12;
28 // finally
29 F11 = 1-F12-F13;
30 printf("value of F12 is %f ",F12);
31 printf("\nvalue of F13 is %f ",F13);
32 printf("\nvalue of F11 is %f ",F11);
```

Scilab code Exa 8.6 hot plates enclosed by a room

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.6\n\n'");
4 // hot plates enclosed by a room
5 // \text{Example } 8.6 \text{ (page no.} -402-404)
6 // solution
8 \text{ w} = 0.5; // [m] \text{ width of plate}
9 L = 1; // [m] length of plate
10 t = 0.5; // [m] separation between two plates
11 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
12 // this is a three-body problem, the two plates and
      the room, so the radiation network is shown in
      figure (8-27) page no. -401.
13 // from the data of the problem
14 T1 = 1000+273; // [K] temperature of first plate
15 T2 = 500+273; // [K] temperature of second plate
16 T3 = 27+273; // [K] temperature of walls of plates
17 A1 = w*L; // [square meter] area of plate
18 A2 = A1; // [square meter] area of plate
19 E1 = 0.2; // emissivity of plate 1
20 E2 = 0.5; // emissivity of plate 2
21 // because the area of the room A3 is very large,
      the resistance (1-E3)/(E3*A3) may be taken as
```

```
zero and we obtain Eb3 = J3.
22 // the shape factor F12 was given in example 8-2:
23 	ext{ F12} = 0.285;
24 \text{ F21} = \text{F12};
25 \text{ F13} = 1 - \text{F12};
26 	ext{ F23} = 1 - F21;
27 // the resistance in the network are calculated as
28 R1 = (1-E1)/(E1*A1);
29 R2 = (1-E2)/(E2*A2);
30 R3 = 1/(A1*F12);
31 R4 = 1/(A1*F13);
32 R5 = 1/(A2*F23);
33 // taking the resistance (1-E3)/(E3*A3) as zero, we
      have the network (as shown in figure example 8-6)
      page no. -403).
34 // to calculate the heat flows at each surface we
      must determine the radiosities J1 and J2. the
      network is solved by setting the sum of the heat
      currents entering nodes J1 and J2 to zero
35
36 // node J1:
37 / (Eb1-J1)/R1+(J2-J1)/R3+(Eb3-J1)/R4 = 0
                                   (a)
38
39 // node J2:
40 / (J1-J2)/R3+(Eb3-J2)/R5+(Eb2-J2)/R2 = 0
                                   (b)
41
42 // now
43 Eb1 = sigma*T1^(4); // [W/square meter]
44 Eb2 = sigma*T2^(4); // [W/square meter]
45 Eb3 = sigma*T3^(4); // [W/square meter]
46 J3 = Eb3; // [W/square meter]
47 // inserting the values of Eb1, Eb2, and Eb3 into
      equations (a) and (b), we have two equations and
      two unknowns J1 and J2 that may be solved
      simultaneously to give
48 // on simplifying we get J1 = (J2-R3*[(Eb3-J2)/R5+(
```

```
Eb2-J2)/R2])
49 // putting this value in equation (a) and solve for
50 deff('[y] = f3(J2)', 'y = (Eb1-(J2-R3*[(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R5+(Eb3-J2)/R
                    Eb2-J2)/R2))/R1+(J2-(J2-R3*[(Eb3-J2)/R5+(Eb2-J2)
                    (R2)) /R3+(Eb3-(J2-R3*[(Eb3-J2)/R5+(Eb2-J2)/R2])
                    /R4');
51 J2 = fsolve(1,f3); // [W/square meter]
52 	ext{ J1 = (J2-R3*[(Eb3-J2)/R5+(Eb2-J2)/R2]);// [W/square]}
                    meter]
53 // the total heat lost by plate 1 is
54 \text{ q1} = (Eb1-J1)/[(1-E1)/(E1*A1)]; // W
55 // and the heat lost by plate 2 is
56 \text{ q2} = (Eb2-J2)/[(1-E2)/(E2*A2)]; // [W]
57 // the total heat received by the room is
58 \quad q3 = [(J1-J3)/(1/(A1*F13))]+[(J2-J3)/(1/(A2*F23))];
                    // [W]
       printf("the net heat transfer for plate 1 is %f kW",
                    q1/1000)
60 printf("\n\n the net heat transfer for plate 2 is %f
                      kW", q2/1000)
61 printf("\n the net heat transfer to the room
                    %f kW, q3/1000)
```

Scilab code Exa 8.7 surface in radiant balance

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.7\n\n\n");
4 // surface in radiant balance
5 // Example 8.7 (page no.-404-405)
6 // solution
7
8 w = 0.5;// [m] width of plate
9 L = 0.5;// [m] length of plate
```

```
10 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
11 // from the data of the problem
12 T1 = 1000; // [K] temperature of first surface
13 T2 = 27+273; // [K] temperature of room
14 A1 = w*L;// [square meter] area of rectangle
15 A2 = A1; // [square meter] area of rectangle
16 E1 = 0.6; // emissivity of surface 1
17 // although this problems involves two surfaces
      which exchange heat and one which is insulated or
       re-radiating, equation (8-41) may not be used
      for the calculation because one of the heat-
      exchanging surfaces (the room) is not convex. The
      radiation network is shown in figure example 8-7(
      page no. -404) where surface 3 is the room and
      surface 2 is the insulated surface, note that J3
      = Eb3 because the room is large and (1-E3)/(E3*A3)
      approaches zero. Because surface 2 is insulated
      it has zero heat transfer and J2 = Eb2. J2 "
      floats" in the network and is determined from the
       overall radiant balance.
18 // from figure 8-14(page no. -387) the shape factors
      are
19 	ext{ F12} = 0.2;
20 \text{ F21} = \text{F12};
21 // because
22 \text{ F11} = 0;
23 	ext{ F22 = 0};
24 \text{ F13} = 1 - \text{F12};
25 	ext{ F23} = 	ext{F13};
26 // the resistances are
27 R1 = (1-E1)/(E1*A1);
28 R2 = 1/(A1*F13);
29 R3 = 1/(A2*F23);
30 \text{ R4} = 1/(\text{A1}*\text{F12});
31 // we also have
32 Eb1 = sigma*T1^(4); // [W/square meter]
33 Eb3 = sigma*T2^(4); // [W/square meter]
34 	ext{ J3 = Eb3;} // 	ext{ [W/square meter]}
```

```
35 // the overall circuit is a series parallel
      arrangement and the heat transfer is
36 \text{ R_equiv} = \text{R1} + (1/[(1/\text{R2}) + 1/(\text{R3} + \text{R4})]);
37 q = (Eb1-Eb3)/R_equiv; // [W]
38 // this heat transfer can also be written as q = (
      Eb1-J1)/((1-E1)/(E1*A1))
39 // inserting the values
40 J1 = Eb1-q*((1-E1)/(E1*A1)); // [W/square\ meter]
41 // the value of J2 is determined from proportioning
      the resistances between J1 and J3, so that
42 // (J1-J2)/R4 = (J1-J3)/(R4+R2)
43 J2 = J1-((J1-J3)/(R4+R2))*R4;// [W/square\ meter]
44 Eb2 = J2; // [W/square meter]
45 // finally, we obtain the temperature of the
      insulated surface as
46 T2 = (Eb2/sigma)^(1/4); // [K]
47 printf ("temperature of the insulated surface is %f K
      ",T2);
48 printf("\n\n heat lost by the surface at 1000K is %f
      kW", q/1000);
```

Scilab code Exa 8.8 open hemisphere in large room

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.8\n\n\n");
4 // open hemisphere in large room
5 // Example 8.8 (page no.-406-408)
6 // solution
7
8 d = 0.3; // [m] diameter of hemisphere
9 T1 = 500+273; // [degree celsius] temperature of hemisphere
10 T2 = 30+273; // [degree celsius] temperature of enclosure
```

```
11 E = 0.4; // surface emissivity of hemisphere
12 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
      constant
13 // the object is completely surrounded by a large
      enclosure but the inside surface of the sphere is
       not convex.
14 // in the given figure example 8-8 (page no. -407) we
      take the inside of the sphere as surface 1 and
      the enclosure as surface 2.
15 // we also create an imaginary surface 3 covering
      the opening.
16 // then the heat transfer is given by
17 Eb1 = sigma*T1^(4); // [W/square meter]
18 Eb2 = sigma*T2^(4); // [W/square meter]
19 A1 = 2*\%pi*(d/2)^(2); // [square meter] area of
      surface 1
20 // calculating the surface resistance
21 R1 = (1-E)/(E*A1);
22 // since A2 tends to 0 so R2 also tends to 0
23 R2 = 0;
24 // now at this point we recognize that all of the
      radiation leaving surface 1 which will eventually
       arrive at enclosure 2 will also hit the
      imaginary surface 3(F12 = F13), we also
      recognize that A1*F13 = A3*F31. but
25 	ext{ F31 = 1.0};
26 \text{ A3} = \%pi*(d/2)^(2); // [square meter]
27 \text{ F13} = (A3/A1)*F31;
28 \text{ F12} = \text{F13};
29 // then calculating space resistance
30 \text{ R3} = 1/(\text{A1}*\text{F12});
31 // we can claculate heat transfer by inserting the
      quantities in equation (8-40):
32 q = (Eb1-Eb2)/(R1+R2+R3); // [W]
33 printf("net radiant exchange is %f W",q);
```

Scilab code Exa 8.9 effective emissivity of finned surface

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 8.9\n\n");
4 // effective emissivity of finned surface
5 // \text{Example } 8.9 \text{ (page no.} -409-410)
6 // solution
8 // for unit depth in the z-dimension we have
9 A1 = 10; // [square meter]
10 A2 = 5;// [square meter]
11 A3 = 60; // [square meter]
12 // the apparent emissivity of the open cavity area
      A1 is given by equation (8-47) as
13 // Ea1 = E*A3/[A1+E*(A3-A1)]
14 // for constant surface emissivity the emitted
      energy from the total area A1+A2 is
15 // e1 = Ea1*A1+E*A2*Eb
16 // and the energy emitted per unit area for that
      total area is
17 // e_t = [(Ea1*A1+E*A2)/(A1+A2)]*Eb
18 // the coefficient of Eb is the effective emissivity
      , E_eff of the combination of the surface and
      open cavity. inserting
19 // above equations gives the following values
20
21 // \text{ for } E = 0.2
22
23 E = 0.2;
24 \text{ Ea1} = \text{E*A3/[A1+E*(A3-A1)]};
25 \text{ E_eff} = [(Ea1*A1+E*A2)/(A1+A2)];
26 printf ("For emissivity of 0.2 the value of effective
       emissivity is %f ",E_eff);
```

```
27
28 // \text{ for E} = 0.5
29
30 E = 0.5;
31 \text{ Ea1} = \text{E*A3/[A1+E*(A3-A1)]};
32 \text{ E_eff} = [(Ea1*A1+E*A2)/(A1+A2)];
33 printf("\n For emissivity of 0.5 the value of
       effective emissivity is %f ",E_eff);
34
35 // \text{ for E} = 0.8
36
37 E = 0.8;
38 \text{ Ea1} = \text{E*A3/[A1+E*(A3-A1)]};
39 E_{eff} = [(Ea1*A1+E*A2)/(A1+A2)];
40 printf("\n For emissivity of 0.8 the value of
       effective emissivity is %f ",E_eff);
```

Scilab code Exa 8.10 heat transfer reduction with parallel plate shield

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.10\n\n\n");
4 // heat transfer reduction with parallel plate shield
5 // Example 8.10 (page no.-413)
6 // solution
7
8 E1 = 0.3; // emissivity of first plane
9 E2 = 0.8; // emissivity of second plane
10 E3 = 0.04; // emissivity of shield
11 sigma = 5.669*10^(-8); // [W/square meter K^(4)]
12 // the heat transfer without the shield is given by
13 // q_by_A = sigma*(T1^4-T2^4)/((1/E1)+(1/E2)-1) = 0.279*sigma*(T1^4-T2^4)
14 // where T1 is temperature of first plane and T2 is
```

```
temperature of second plane

// the radiation network for the problem with the shield in place is shown in figure (8-32) (page no.-410).

// the resistances are

R1 = (1-E1)/E1;
R2 = (1-E2)/E2;
R3 = (1-E3)/E3;
// the total resistance with the shield is
R = R1+R2+R3;
// and the heat transfer is
// q_by_A = sigma*(T1^4-T2^4)/R = 0.01902*sigma*(T1^4-T2^4)

rintf("so the heat tranfer is reduced by %f percent ",((0.279-0.01902)/0.279)*100);
```

Scilab code Exa 8.11 open cylindrical shield in large room

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.11\n\n");
4 // open cylindrical shield in large room
5 // Example 8.11 (page no.-413-415)
6 // solution
8 // two concentric cylinders of example (8.3) have
9 T1 = 1000; // [K]
10 E1 = 0.8;
11 E2 = 0.2;
12 T3 = 300; // [K] room temperature
13 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
14 // please refer to figure example 8-11(page no. -413)
      for radiation network
15 // the room is designed as surface 3 and J3 = Eb3,
      because the room is very large, (i.e. its surface
```

```
is very small)
16 // in this problem we must consider the inside and
      outside of surface 2 and thus have subscripts i
      and o to designate the respective quantities.
17 // the shape factor can be obtained from example 8-3
       as
18 	ext{ F12} = 0.8253;
19 	ext{ F13} = 0.1747;
20 \text{ F23i} = 0.2588;
21 	ext{ F23o} = 1.0;
22 // also
23 A1 = \%pi*0.1*0.2; // [square meter] area of first
      cylinder
24 A2 = \%pi*0.2*0.2; // [square meter] area of second
      cylinder
25 Eb1 = sigma*T1^4; // [W/square meter]
26 Eb3 = sigma*T3^4; // [W/square meter]
27 // the resistances may be calculated as
28 R1 = (1-E1)/(E1*A1);
29 R2 = (1-E2)/(E2*A2);
30 R3 = 1/(A1*F12);
31 R4 = 1/(A2*F23i);
32 R5 = 1/(A2*F23o);
33 R6 = 1/(A1*F13);
34 // the network could be solved as a series-parallel
      circuit to obtain the heat transfer, butwe will
      need the radiosities anyway, so we setup three
      nodal equations to solve for J1, J2i, and J2o.
  // we sum the currents into each node and set them
      equal to zero:
36
37 / \text{node J1: } (Eb1-J1)/R1+(Eb3-J3)/R6+(J2i-J1)/R3 = 0
38 // node J2i: (J1-J2i)/R3+(Eb3-J2i)/R4+(J2o-J2i)/(2*
     R2) = 0
39 // \text{ node } J2o: (Eb3-J2o)/R5+(J2i-J2o)/(2*R2) = 0
40 // these equations can be solved by matrix method
      and the solution is
41 J1 = 49732; // [W/square meter]
```

Scilab code Exa 8.12 network for gas radiation between parallel plates

```
clear;
clc;
printf("\t\t\tExample Number 8.12\n\n\n");
// network for gas radiation between parallel plates
// Example 8.12 (page no.-422-423)
// solution

T1 = 800;// [K] temperature of first plate
E1 = 0.3;// emissivity
T2 = 400;// [K] temperature of second plate
E2 = 0.7;// emissivity
Eg = 0.2;// emissivity
Eg = 0.2;// emissivity of gray gas
degree = 0.8;// transmissivity of gray gas
sigma = 5.669*10^(-8);// [W/square meter K^(4)]
// the network shown in figure 8-39(page no.-419)
```

```
applies to this problem. all the shape factors
      are unity for large planes and the various
      resistors can be computed on a unit area basis as
16 \text{ F12} = 1;
17 \text{ F1g} = 1;
18 \text{ F2g} = \text{F1g};
19 R1 = (1-E1)/E1;
20 R2 = (1-E2)/E2;
21 R3 = 1/(F12*(1-Eg));
22 R4 = 1/(F1g*Eg);
23 R5 = 1/(F2g*Eg);
24 Eb1 = sigma*T1^(4); // [W/square meter]
25 Eb2 = sigma*T2^(4); // [W/square meter]
26 // the equivalent resistance of the center "triangle
      "is
27 R = 1/[(1/R3)+(1/(R4+R5))];
28 // the total heat transfer is then
29 q_by_A = (Eb1-Eb2)/(R1+R2+R); // [W/square meter]
30 // if there were no gas present the heat transfer
      would be given by equation (8-42):
31 \text{ q_by_A1} = (Eb1-Eb2)/[(1/E1)+(1/E2)-1]; // [W/square]
      meter
32
  // the radiosities may be computed from q_by_A = (
     Eb1-J1)*(E1/(1-E1)) = (J2-Eb2)*(E2/(1-E2))
33 J1 = Eb1-q_by_A*((1-E1)/E1); // [W/square meter]
34 	ext{ J2 = Eb2+q_by_A*((1-E2)/E2); // [W/square meter]}
35 // for the network Ebg is just the mean of these
      values
36 Ebg = (J1+J2)/2; // [W/square meter]
37 // so that the temperature of the gas is
38 Tg = (Ebg/sigma)^{(1/4)}; // [K]
39 printf("the heat-transfer rate between the two
      planes is %f W/square meter",q_by_A);
40 printf("\n\n the temperature of the gas is \%f K", Tg)
41 printf("\n the ratio of heat-transfer with
      presence of gas to without presence of gas is %f"
      ,q_by_A/q_by_A1);
```

Scilab code Exa 8.13 cavity with transparent cover

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.13\n\n");
4 // cavity with transparent cover
5 // \text{Example } 8.13 \text{ (page no.} -433-434)
6 // solution
8 E1 = 0.5; // emissivity of rectangular cavity
9 t2 = 0.5; // transmissivity
10 rho2 = 0.1; // reflectivity
11 E2 = 0.4; // emissivity
12 // from example 8-9 we have
13 // per unit depth in the z direction we have
14 \quad A1 = 25 + 25 + 10;
15 \quad A2 = 10;
16 // we may evaluate K from equation (8-96a)
17 K = E1/(t2+(E2/2));
18 // the value of Ea is then computed from equation
      (8-96) as
19 Ea = (t2+(E2/2))*K/[(A2/A1)*(1-E1)+K];
20 printf ("apparent emissivity of covered opening is %f
      ",Ea);
21 // if there were no cover present, the value of Ea
      would be given by equation (8-47) as
22 Ea1 = E1*A1/[A2+E1*(A1-A2)];
23 printf("\n\n if there were no cover present, the
      value of Ea(apparent emissivity) would be %f", Ea1
      );
```

Scilab code Exa 8.14 Transmitting and reflecting system for furnace opening

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.14\n\n");
4 // Transmitting and reflecting system for furnace
      opening
  // Example 8.14 (page no. -434-435)
  // solution
8 T1 = 1000+273; // [K] temperature of furnace
9 lambda = 4.0; // [micro meter]
10 // for 0 < lambda < 4 micro meter
11 t1 = 0.9;
12 E1 = 0.1;
13 \text{ rho1} = 0;
14 //for 4 micro meter < lambda < infinity
15 	 t2 = 0;
16 E2 = 0.8;
17 \text{ rho2} = 0.2;
18 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
19 T3 = 30+273; // [K] room temperature
20 // the diagram of this problem is shown in figure
      example 8-14 (page no. -434). because the room is
      large it may be treated as a blackbody also.
21 // we shall analyze the problem by calculating the
      heat transfer for each wavelength band and then
      adding them together to obtain the total. the
      network for each band is a modification of figure
       8-57 (page no. -430), as shown here for black
      furnace and room. we shall make the calculation
      for unit area; then
22 A1 = 1.0; // [square meter]
23 A2 = 1.0; // [square meter]
24 A3 = 1.0; // [square meter]
25 	ext{ F12} = 1.0;
26 \text{ F13} = 1.0;
```

```
27 \text{ F32} = 1.0;
28 // the total emissive powers are
29 Eb1 = sigma*T1^(4); // [W/square meter]
30 Eb3 = sigma*T3^(4); // [W/square meter]
31 // to determine the fraction of radiation in each
      wavelength band, we calculate
32 lamba_into_T1 = lambda*T1; // [micro meter K]
33 lamba_into_T3 = lambda*T3; // [micro meter K]
34 // consulting table 8-1(page no. -379-380), we find
35 Eb1_0_to_4 = 0.6450*Eb1; // [W/square meter]
36 \text{ Eb3\_0\_to\_4} = 0.00235*Eb3; // [W/square meter]
37 Eb1_4_to_inf = (1-0.6450)*Eb1; // [W/square meter]
38 Eb3_4_to_inf = (1-0.00235)*Eb3; // [W/square meter]
39 // we now apply these numbers to the network for the
       two wavelengths bands, with unit areas.
40
41 // 0 < lambda < 4 micro meter band:
42 R1 = 1/(F13*t1);
43 R2 = 1/(F32*(1-t1));
44 R3 = 1/(F12*(1-t1));
45 \text{ R4} = \text{rho1/(E1*(1-t1))};
46 // the net heat transfer from the network is then
47 R_{equiv_1} = 1/(1/R1+1/(R2+R3+R4));
48 q1 = (Eb1_0_to_4-Eb3_0_to_4)/R_equiv_1; // [W/square]
      meter]
49
50 // 4 \text{ micro meter} < \text{lambda} < \text{infinity band}:
51 R2 = 1/(F32*(1-t2));
52 R3 = 1/(F12*(1-t2));
53 R4 = rho2/(E2*(1-t2));
54 // the net heat transfer from the network is then
55 // R1 is infinity
56 R_{equiv_2} = R2+R3+R4*2;
57 	ext{ q2} = (Eb1_4_to_inf-Eb3_4_to_inf)/R_equiv_2; // [W/s]
      square meter
58
59 // the total heat loss is then
60 \text{ q\_total} = \text{q1+q2;} // [W/\text{square meter}]
```

Scilab code Exa 8.15 numerical solution for enclosure

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.15\n\n");
4 // numerical solution for enclosure
5 // \text{Example } 8.15 \text{ (page no.} -440)
6 // solution
8 // the geometry of example 8-5 is used
9 d = 0.6; // [m] diameter of long half-circular
      cylinder
10 L = 0.2; // [m] length of square rod
11 E2 = 0.5;
12 T2 = 1000; // [K] temperature of body 2
13 T3 = 300; // [K] temperature of body 3
14 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
15 // for unit length we have:
16 Eb2 = sigma*T2^(4); // [W/square meter]
17 \text{ Eb3} = \text{sigma}*T3^{(4)};
18 A1 = 4*L;// [square meter]
19 A2 = \%pi*d/2;// [square meter/meter]
20 // we will use the numerical formulation. we find
      from example 8-5, using the nomenclature of the
      figure
```

```
21 	ext{ F11} = 0.314;
22 	ext{ F12} = 0.425;
23 \text{ F13} = 0.261;
24 	ext{ F21 = 0.5};
25 \text{ F22} = 0;
26 	ext{ F23} = 0.5;
27 // F31, F32 tends to zero so
28 	ext{ F33} = 1;
29 // we now write the equations.
30 // surface 1 is insulated so we use equation (8-107a)
31 // J1*(1-F11)-F12*J2-F13*J3 = 0
32 // surface 2 is constant temperature so we use
      equation (8-106a):
33 // J2*(1-F22*(1-E2))-(1-E2)*[F21*J1+F23*J3] = E2*Eb2
34 // because surface 3 is so large
35 J3 = Eb3; // [W/square meter]
36 // rearranging the equation gives
37 // J1*(1-F11)-J2*F12 = F13*J3
38 // J1*(-1)*(1-E2)*F21+J2*(1-F22*(1-E2)) = E2*Eb2+(1-F22*(1-E2))
      E2)*(F23*J3)
39 // solving the above two equations using matrix
40 \quad X = [(1-F11) -F12; (-1)*(1-E2)*F21 (1-F22*(1-E2))];
41 \quad Y = [F13*J3; E2*Eb2+(1-E2)*(F23*J3)];
42 \quad J = X^{(-1)} *Y;
43 J1 = J(1); // [W/square\ meter]
44 J2 = J(2); // [W/square meter]
45 // the heat transfer is thus
46 \text{ q} = (Eb2-J2)/((1-E2)/(E2*A1)); // [W/m] length
47 // because surface 1 is insulated
48 Eb1 = J1; // [W/square meter]
49 // we could calculate the temperature as
50 \text{ T1} = (Eb1/sigma)^(1/4); // [K]
51 printf ("heat lost to the large room per unit length
      of surface 2 is %f W/m",q);
52 printf("\n\n temperature of the insulated surface is
       %f K",T1);
```

Scilab code Exa 8.16 numerical solution for parallel plates

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.16\n\n'");
4 // numerical solution for parallel plates
5 // Example 8.16 (page no.-440-443)
6 // solution
8 T1 = 1000; // [K]
9 T2 = 400; // [K]
10 \text{ E1} = 0.8; //
11 E2 = 0.5; //
12 // consulting figure 8-12, we obtain
13 \text{ F12} = 0.2;
14 F21 = 0.2;
15 \text{ F11} = 0;
16 \text{ F22} = 0;
17 \text{ F13} = 0.8;
18 F23 = 0.8;
19 A1 = 1;// [square meter]
20 A2 = 1;// [square meter]
21 // surface 3 is the surrounding or insulated surface
      . For part A(the plates are surrounded by a large
       room at 300K)
22 \text{ T3} = 300; // [K]
23 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
24 Eb1 = sigma*T1^(4); // [W/square meter]
25 Eb2 = sigma*T2^(4); // [W/square meter]
26 Eb3 = sigma*T3^(4); // [W/square meter]
27 // because A3 tends to infinity, F31 and F32 must
      approach zero since A1*F13 = A3*F31 and A2*F23 =
      A3*F32. the nodal equations are written in the
      form of equations (8-107):
```

```
28 // surface 1
                       J1-(1-E1)*(F11*J1+F12*J2+F13*J3)
     = E1*Eb1
29 // surface 2
                       J2-(1-E2)*(F21*J1+F22*J2+F23*J3)
     = E2*Eb2
30 // surface 3
                       J3-(1-E3)*(F31*J1+F32*J2+F33*J3)
     = E3*Eb3
31
32 // because F31 and F32 approach zero, F33 must be
      1.0.
33 \text{ F33} = 1;
34 // inserting the various numerical values for the
      various terms and solving the third equation we
35 // the third equation as: J3*E3 = E3*Eb3 so we get
      the value of J3 as
36 J3 = Eb3; // [W/square meter]
37 // finally the equations are written in compact form
       after getting the value of J3 we solve for J2
      and J1 by matrix method
38 \ Z = [1-(1-E1)*F11 - (1-E1)*F12; -(1-E2)*F21 1-(1-E2)*
     F22];
39 \ C = [E1*Eb1+(1-E1)*F13*J3;E2*Eb2+(1-E2)*F23*J3];
40 J = Z^{(-1)} *C;
41 J1 = J(1); // [W/square meter]
42 J2 = J(2); // [W/square meter]
43 // the heat transfers are obtained from equation
      (8-104):
44 \text{ q1} = A1*E1*(Eb1-J1)/(1-E1); // [W]
45 \text{ q2} = A2*E2*(Eb2-J2)/(1-E2); // [W]
46 // the net heat absorbed by the room is algebric sum
       of q1 and q2
47 \text{ q3\_absorbed} = \text{q1+q2;}// [W]
48 printf("\t \subset ASE(A)");
49 printf("\n\n the heat transfers are \n\t q1 = \%f
      kW", q1/1000);
50 printf("\n\t\tq1 = %f kW",q2/1000)
51 printf("\n\n the net heat absorbed by the room in
      part (a) is \%f kW", q3_absorbed/1000);
```

```
52
53 // for part(b), A3 for the enclosing wall is 4.0
      square meter
54
55 \quad A3 = 4; // \quad [square meter]
56 // and we set
57 J3 = Eb3; // [W/square meter], because surface 3 is
      insulated.
58 // from reciprocity we have
59 F31 = A1*F13/A3;
60 \text{ F32} = \text{A2*F23/A3};
61 // then, we have
62 	ext{ F33} = 1 - 	ext{F31} - 	ext{F32};
63 // the set of equations are same with J3 = Eb3
64 // surface 1
                       J1-(1-E1)*(F11*J1+F12*J2+F13*J3)
     = E1*Eb1
  // surface 2
                       J2-(1-E2)*(F21*J1+F22*J2+F23*J3)
     = E2*Eb2
                       J3-(1-E3)*(F31*J1+F32*J2+F33*J3)
  // surface 3
     = E3*J3
67 // the third equation of set can be written as
68 // J3(1-E3) - (1-E3) * (F31*J1+F32*J2+F33*J3) = 0
69 // so that (1-E3) term drops out, and we obtain
      three equation in three variable which can be
      solved by matrix method
70 \ Z = [1-(1-E1)*F11 - (1-E1)*F12 - (1-E1)*F13; - (1-E2)*
      F21 1-(1-E2)*F22 -(1-E2)*F23;-F31 -F32 1-F33];
71 C = [E1*Eb1; E2*Eb2; 0];
72 J = Z^{(-1)} *C;
73 J1n = J(1); // [W/square meter]
74 J2n = J(2); // [W/square meter]
75 J3n = J(3); // [W/square meter]
76 // the heat transfers are
77 q1n = A1*E1*(Eb1-J1n)/(1-E1);//
78 \text{ q2n} = A2*E2*(Eb2-J2n)/(1-E2); // W
79 // of course these heat transfers should be equal in
       magnitude with opposite sign because the
      insulated wall exchanges no heat.
```

Scilab code Exa 8.17 radiation from a hole with variable radiosity

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.17 \ln n);
4 // radiation from a hole with variable radiosity
5 // \text{Example } 8.17 \text{ (page no.} -443-446)
6 // solution
8 T1 = 1273; // [K]
9 	ext{ T5} = 293; // [K]
10 E1 = 0.6;
11 // all the shape factors can be obtained with the
      aid of figure 8-13 (page no. -387) and the
      imaginary disk surfaces 6 and 7. we have
12 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
13 Eb1 = sigma*T1^(4); // [W/square meter]
14 Eb2 = Eb1; // [W/square meter]
15 Eb3 = Eb2; // [W/square meter]
16 Eb4 = Eb3;// [W/square meter]
17 Eb5 = sigma*T5^(4); // [W/square meter]
18 E2 = E1;
19 E3 = E2;
20 \text{ E4} = \text{E3};
21 	 E5 = 1.0;
```

```
22 r = 0.01; // [m]
23 A1 = \%pi*r^(2); // [square m]
24 \text{ A5} = \text{A1}; // [square m]
25 A6 = A1; // [square m]
26 \text{ A7} = \text{A1}; // [\text{square m}]
27 \text{ A2} = \%pi*2*r*0.01; // [square m]
28 A3 = A2; // [square m]
29 A4 = A2; // [square m]
30 \text{ F11} = 0;
31 	ext{ F55} = 0;
32 \text{ F16} = 0.37;
33 	ext{ F17} = 0.175;
34 \text{ F15} = 0.1;
35 \text{ F12} = 1 - \text{F16};
36 	ext{ F54} = 	ext{F12};
37 \text{ F13} = \text{F16} - \text{F17};
38 	ext{ F53} = 	ext{F13};
39 \text{ F14} = \text{F17} - \text{F15};
40 	ext{ F52} = 	ext{F14};
41 \text{ F21} = \text{F16}*\text{A1/A2};
42 \text{ F26} = \text{F21};
43 \text{ F45} = \text{F21};
44 \text{ F36} = \text{F45};
45 \text{ F37} = \text{F36};
46 	ext{ F22} = 1 - F21 - F26;
47 \text{ F33} = \text{F22};
48 	ext{ F44} = 	ext{F22};
49 \text{ F31} = \text{F13*A1/A3};
50 \text{ F32} = \text{F36-F31};
51 \text{ F34} = \text{F32};
52 \text{ F43} = \text{F34};
53 F23 = F34;
54 	ext{ F27} = 	ext{F26} - 	ext{F23};
55 \text{ F46} = \text{F27};
56 \text{ F41} = \text{F14} \times \text{A1/A4};
57 	ext{ F25} = 	ext{F41};
58 	ext{ F42} = 	ext{F46-F41};
59 	ext{ F24} = 	ext{F42};
```

```
60 // the equations for the radiosities are now written
                in the form of equation 8-106, noting that
61 	ext{ F11 = 0};
62 	ext{ J5} = 	ext{Eb5}; // 	ext{ [W/square meter]}
63 // J1 = (1-E1)*(F12*J2+F13*J3+F14*J4+F15*Eb5)+E1*
              Eb1
                J2 = [(1-E2)*(F21*J1+F23*J3+F24*J4+F25*Eb5)+E2*
64 //
              Eb2/(1-F22*(1-E2))
      // J3 = [(1-E3)*(F31*J1+F32*J2+F34*J4+F35*Eb5)+E3*
              Eb3/(1-F33*(1-E3))
              J4 = [(1-E2)*(F41*J1+F42*J2+F43*J3+F45*Eb5)+E4*
              Eb4/(1-F44*(1-E4))
      // we have 4 equations with 4 variables which can be
                 solved by matrix method
68 \ Z = [1 \ -(1-E1)*F12 \ -(1-E1)*F13 \ -(1-E1)*F14; -F21*(1-E1)*F14; -F21*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E1)*F14*(1-E
              E2)/(1-F22*(1-E2)) 1 -F23*(1-E2)/(1-F22*(1-E2)) -
              F24*(1-E2)/(1-F22*(1-E2));-F31*(1-E3)/(1-F33*(1-
              E3)) -F32*(1-E3)/(1-F33*(1-E3)) 1 -F34*(1-E3)/(1-E3)
              F33*(1-E3));-F41*(1-E4)/(1-F44*(1-E4)) -F42*(1-E4
              )/(1-F44*(1-E4)) -F43*(1-E4)/(1-F44*(1-E4)) 1];
69 \ C = [E1*Eb1+(1-E1)*F15*Eb5; (E2*Eb2+F25*Eb5*(1-E2))
              /(1-F22*(1-E2));104859;(E4*Eb4+F45*Eb5*(1-E4))
              /(1-F44*(1-E4));
70 J = Z^{(-1)} *C;
71 J1 = J(1); // [W/square\ meter]
72 J2 = J(2); // [W/square\ meter]
73 J3 = J(3); // W/square meter
74 	ext{ J4 = J(4); // [W/square meter]}
75 // the heat transfer can be calculated from equation
              (8-104):
76 \text{ q1} = \text{E1}*\text{A1}*(\text{Eb1}-\text{J1})/(1-\text{E1}); //
                                                                                   W
77 q2 = E2*A2*(Eb2-J2)/(1-E2);/
                                                                                    [W]
78 	ext{ q3} = E3*A3*(Eb3-J3)/(1-E3);//
                                                                                   [W]
79 q4 = E4*A4*(Eb4-J4)/(1-E4);//
                                                                                   [W]
80 // THE TOTAL HEAT TRANSFER
81 q = q1+q2+q3+q4; // [W]
82 printf("the heat transfer rate is %f W",q);
83 // It is of interest to compare this heat transfer
```

```
with the value we would obtain by assuming
      uniform radiosity on the hot surface. we would
      then have a two-body problem with
84 A1 = \%pi+3*(2*\%pi);// [square cm]
85 A5 = \%pi*10^(-4);// [square cm]
86 	ext{ F51} = 1.0;
87 E1 = 0.6;
88 E5 = 1.0;
89 // the heat transfer is then calculated from
      equation (8-43), with appropriate change of
      nomenclature:
90 q_new = (Eb1-Eb5)*A5/((1/E5)+(A5/A1)*((1/E1)-1));/
91 printf("\n\nthus the assumption of uniform radiosity
       gives a heat transfer that is %f percent below
      the value obtained by breaking the hot surface
      into four parts for the calculations", (q-q_new)
      *100/q);
92 // let us now consider the case where surface 1 is
       still radiating at 1000 degree celsius
93 E = 0.6;
94 // the nodal equations for J1 is the same as before
      but now the equations for J2, J3, and J4 must be
      written in the form of equation (8-107). when that
       is done and the numerical values are inserted,
      we obtain
95 // J1 = 0.252*J2+0.078*J3+0.03*J4+89341
96 // J2 = 0.5*J1+0.3452*J3+0.09524*J4+24.869
97 // J3 = 0.1548*J1+0.3452*J2+0.3452*J4+64.66
98 //
      J4 = 0.05952*J1+0.0952*J2+0.3452*J3+208.9
99 // when these equations are solved, we obtain
100 J1 = 1.1532*10^{(5)}; // [W/square meter]
101 J2 = 0.81019*10^{(5)}; // [W/square meter]
102 J3 = 0.57885*10^{(5)}; // [W/square meter]
103 J4 = 0.34767*10^{(5)}; // [W/square meter]
104 // the heat transfer at surface 1 is
105 A1 = %pi*10^(-4);// [square cm]
106 \text{ A5} = \% \text{pi} * 10^{(-4)}; // [square cm]
```

Scilab code Exa 8.18 heater with constant heat flux and surrounding shields

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.18\n\n");
4 // heater with constant heat flux and surrounding
      shields
\frac{5}{\sqrt{8}} Example 8.18 (page no. -446-449)
6 // solution
8 sigma = 5.669*10^{(-8)}; // [W/square meter K^(4)]
9 T6 = 293; // [K] temperature of room
10 E1 = 0.8;
11 E2 = 0.4:
12 E3 = 0.4;
13 \quad E4 = 0.4;
14 E5 = 0.4;
15 // in reality, surfaces 2,3,4, and 5 have two
      surfaces each; an inside and an outside surface.
      we thus have nine surfaces plus the room, so a 10
       body problem is involved. of course, from
```

```
symmetry we can see that T2 = T4 and T3 = T5.
16 // we designate the large room as surface 6 and it
        behaves as E6 = 1.0.
17 // the shape factors of the inside surfaces are
        obtained from figure 8-12 and 8-14:
18 \text{ F16} = 0.285;
19 \text{ F61} = \text{F16};
20 	ext{ F13} = 0.24;
21 	ext{ F15} = 0.24;
22 	ext{ F31} = 0.24;
23 	ext{ F51} = 0.24;
24 \text{ F12} = 0.115;
25 \text{ F14} = 0.115;
26 	ext{ F24} = 0.068;
27 	ext{ F42} = 0.068;
28 	ext{ F35} = 0.285;
29 	ext{ F53} = 0.285;
30 \text{ F32} = 0.115;
31 	ext{ F52} = 0.115;
32 \text{ F34} = 0.115;
33 	ext{ F25} = 0.23;
34 	ext{ F23} = 0.23;
35 	ext{ F45} = 0.23;
36 	ext{ F43} = 0.23;
37 	ext{ F21} = 0.23;
38 	ext{ F41 = 0.23;}
39 	ext{ F26} = 0.23;
40 \text{ F46} = 0.23;
41 \text{ F11} = 0;
42 \text{ F22} = 0;
43 \text{ F33} = 0;
44 	ext{ F44} = 0;
45 	ext{ F55} = 0;
46 // for the outside surfaces,
47 	ext{ } F_26 = 1;
48 \text{ F}_36 = 1;
49 \quad F_46 = 1;
50 F_56 = 1;
```

```
51 // Where the underscore indicate the outside
      surfaces.
52 // for the room
53 Eb6 = sigma*T6^(4); // [W/square meter]
54 // for surface 1 with constant heat flux, we use
      equation (8-108a) and write
  // J1 - (F12 * J2 + F13 * J3 + F14 * J4 + F15 * J5 + F16 * J6) =
      1.0*10^{(5)}
                                 GIVEN
                                                     (a)
56 // because of the radiant balance condition we have
57 / (J2-Eb2)*E2*A2/(1-E2) = (Eb2-J_2)*E2*A2/(1-E2)
58 // and
               Eb2 = (J2+J_{-}2)/2
      (b)
59 // Where underscore indicates the outside radiosity.
       a similar relation applies for surfaces 3,4, and
       5. thus we can use equation (8-106a) for inside
      surface 2
60 // J2 - (1-E2) * (F21*J1+F23*J3+F24*J4+F25*J5+F26*J6) =
      E2*(J2+J_2)/2
                                             (c)
61 // and for outside surface 2
62 // J_2 - (1-E_2) * (F_2 6 * J 6) = E_2 * (J_2 + J_2) / 2
      d)
63 // Equations like (c) and (d) are written for
      surfaces 3,4, and 5 also, and with the shape
      factors and emmissivities inserted the following
      set of equations is obtained
64 // J1 - 0.115*J2 - 0.24*J3 - 0.115*J4 - 0.24*J5 =
      1.0012*10^{(5)}
  // -0.138*J1+0.8*J2-0.2*J_2-0.138*J3-0.0408*J4
      -0.138*J5 = 57.66
66 / 0.2*J2 - 0.8*J_2 = -250.68
67 // -0.144*J1 -0.069*J2 +0.8*J3 -0.2*J_3 -0.069*J4 -0.05*
      J5 = 60.16
68 // 0.2*J3 - 0.8*J_3 = -250.68
```

```
5
69 // -0.138*J1-0.0408*J2-0.138*J3+0.8*J4-0.2*J_4
      -0.138*J5 = 57.66
70 // 0.2 * J4 - 0.8 * J_4 = -250.68
  // -0.144*J1-0.069*J2-0.057*J3-0.069*J4+0.8*J5-0.2*
      J_{-}5 = 60.16
  // 0.2*J5-0.8*J_5 = -250.68
      9
  // We thus have nine equations and nine unknowns,
      which may be solved by matrix method
74 \ Z = [1 \ -0.115 \ -0.24 \ -0.115 \ -0.24 \ 0 \ 0 \ 0; -0.138 \ 0.8]
      -0.138 -0.0408 -0.138 -0.2 0 0 0;0 0.2 0 0 0 -0.8
       0 0 0; -0.144 -0.069 0.8 -0.069 -0.05 0 -0.2 0
      0;0 0 0.2 0 0 0 -0.8 0 0; -0.138 -0.0408 -0.138
      0.8 -0.138 0 0 -0.2 0;0 0 0 0.2 0 0 0 -0.8
      0; -0.144 -0.069 -0.057 -0.069 0.8 0 0 0 -0.2; 0 0
      0 0 0.2 0 0 0 -0.8];
75 C = [1.0012*10^{5})
      ;57.66;-250.68;60.16;-250.68;57.66;-250.68;60.16;-250.68];
76 J = Z^{(-1)}*C;
77 J1 = J(1); // [W/square\ meter]
78 J2 = J(2); // [W/square meter]
79 J3 = J(3); // W/square meter
80 J4 = J(4); // [W/square meter]
81 J5 = J(5); // [W/square meter]
82 J_2 = J(6); // [W/square meter]
83 J_3 = J(7); // [W/square meter]
84 \ J_4 = J(8); // [W/square meter]
85 \ J_5 = J(9); // [W/square meter]
86 // the temperatures are thus computed from equation
87 Eb2 = (J2+J_2)/2; // [W/square meter]
88 T2 = (Eb2/sigma)^{(1/4)}; // [K]
89 T4 = T2; // [K]
```

```
90 Eb3 = (J3+J_3)/2; // [W/square\ meter]
91 T3 = (Eb3/sigma)^{(1/4)}; // [K]
92 	ext{ T5} = 	ext{ T3}; // [K]
93 // for surface 1 we observed that
94 \ q = 1*10^{(5)}; // [W/square meter]
95 Eb1 = q*(1-E1)/E1+J1; // [W/square meter]
96 // and
97 T1 = (Eb1/sigma)^{(1/4)}; // [K]
98 printf ("temperature of all surfaces are following")
99 printf("\n\t T1 = \%f K", T1);
100 printf("\n\t T2 = \%f K", T2);
101 printf("\n\t T3 = \%f K", T3);
102 printf("\n\t T4 = \%f K", T4);
103 printf("\n\n\t T5 = \%f K", T5);
104
105 // surfaces 2,3,4, and 5 as one surface
106 // we now go back and take surfaces 2,3,4, and 5 as
       one surface, which we choose to call surface 7.
       the shape factors are then
107 \text{ F16} = 0.285;
108 \text{ F61} = 0.285;
109 \text{ F17} = 1-0.285;
110 \quad A1 = 2.0;
111 \quad A7 = 6.0;
112 // THUS
113 	ext{ F71} = A1*F17/A7;
114 	ext{ F77} = 1-2*F71;
115 	ext{ F76} = 	ext{F71};
116 \quad F_{76} = 1.0;
117 // then for surface 1 we use equation (8-109a) to
       obtain
118 // J1 - (F17*J7+F16*J6) = 1.0*10^{(5)}
119 // using Eb7 = (J7+J_{-}7)/2, we have for the inside of
        surface 7
120 // J7*[1-F77*(1-E7)]-(1-E7)*(F71*J1+F76*J6) = (J7+
       J_{-7})*E7/2
121 // while for the outside we have
```

```
122 // J_7 - (1-E7) *F_76 *J6 = (J7+J_7) *E7/2
123 // when the numerical values are inserted, we obtain
       the set of three equations:
124 // J1 - 0.715 J7 = 1.0012 * 10^{(5)}
125 // -0.143*J1+0.486*J7-0.2*J_7 = 59.74
126 // 0.2*J7 - 0.8*J_7 = -250.68
127 // Solving above three equations by matrix method
128 \ Z = [1 \ -0.715 \ 0; -0.143 \ 0.486 \ -0.2; 0 \ 0.2 \ -0.8];
129 \ C = [1.0012*10^{(5)}; 59.74; -250.68];
130 J = Z^{(-1)}*C;
131 J1 = J(1); // [W/square meter]
132 J7 = J(2); // [W/square meter]
133 J_7 = J(3); // [W/square meter]
134 // the temperatures are thus computed as before
135 Eb7 = (J7+J_7)/2; // [W/square\ meter]
136 T7 = (Eb7/sigma)^(1/4); // [K]
137 Eb1 = q*(1-E1)/E1+J1; // [W/square meter]
138 T11 = (Eb1/sigma)^(1/4); // [K]
139 printf("\n from second method T1 = %f K", T11);
140 printf("\n so there is a difference of \%f K
      between the two methods", T11-T1);
```

Scilab code Exa 8.19 numerical solution for combined convection and radiation non linear system

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.19\n\n\n");
4 // numerical solution for combined convection and radiation(non-linear system)
5 // Example 8.19 (page no.-449-452)
6 // solution
7
8 1 = 0.5;// [m] length of plate
9 b = 0.5;// [m] breadth of plate
```

```
10 T1 = 1300; // [K] temperature of plate
11 Tinf = 300; // [K] temperature of surrounding
12 T4 = Tinf;// [degree celsius]
13 h = 50; // [W/square meter] convection heat transfer
      coefficient
14 E1 = 0.8;
15 E2 = 0.3;
16 E3 = 0.3;
17 // using figures 8-12(page no. -386) and 8-14(page no
      (1.387), we can evaluate the shape factors as
18 \text{ F12} = 0.2;
19 	ext{ F13} = 0.2;
20 \text{ F23} = 0.2;
21 	ext{ F32} = 0.2;
22 	ext{ F14} = 1-0.2-0.2;
23 F24_L = 1;
24 \text{ F34}_R = 1;
25 	ext{ F21 = F12};
26 	ext{ F31} = 	ext{F12};
27 F24_R = 0.6;
28 F34_L = 0.6;
29 	ext{ F11 = 0};
30 \text{ F22} = 0;
31 \text{ F33} = 0;
32 // J2R = J3L
33 // J2L = J3R
                       From symmetry
34 sigma = 5.669*10^(-8); // [W/square meter K^(4)]
35 Eb4 = sigma*T4^(4); // [W/square meter]
36 Eb1 = sigma*T1^(4); // [W/square meter]
37 	ext{ J4 = Eb4;} // 	ext{ [W/square meter]}
38 // we now use equation (8-107) to obtain a relation
      for J1:
39 // J1 = (1-E1) * [F12*J2R+F13*J3L+F14*J4]+E1*Eb1
40 // but J2R = J3L and F12 = F13 so that
41 // J1 = (1-E1) * [2*F13*J2R+F14*J4]+E1*Eb1
                                                   (a)
42 // we use equation (8-108) for the overall energy
      balance on surface 2:
```

```
43 // 2*h*(Tinf-T2) = E2*(Eb2-J2R)/(1-E2)+E2*(Eb2-J2L)
      /(1-E2)
44 // 2*h*(Tinf-T2) = E2*(2*Eb2-J2R-J2L)/(1-E2)
                                           (b)
45 // equation (8-105) is used for surface J2R.
46 // J2R = (1-E2)*(F21*J1+F23*J3L+F24_R*J4)+E2*Eb2
47 // \text{But J2R} = \text{J3L so that}
48 // J2R = [(1-E2)*(F21*J1+F24_R*J4)+E2*Eb2]/(1-(1-E2))
      *F23)
                                     (c)
49 // for surface J2L the equation is
50 // J2L = (1-E2)*(F24_L*J4)+E2*Eb2
                                                        (d)
51 // we now have four equations with four unknowns, J1
      J_{2R}, J_{2L}, E_{b2}, \text{ with } T_{2} = (E_{b2}/sigma) (1/4).
   // however equation (b) is nonlinear in Eb so we
      must use a special procedure to solve the set.
  for T2 = 300:0.1:400
53
       Z = [1 - (1-E1)*2*F13 \ 0 \ 0; 0 - E2/(1-E2) - E2/(1-E2)
           2*E2/(1-E2);(1-E2)*F21/(1-(1-E2)*F23) -1 0
          E2/(1-(1-E2)*F23);0 0 1 -E2];
       C = [E1*Eb1; 2*h*(Tinf-T2); -F24_R/(1-(1-E2)*F23)]
55
          ;(1-E2)*F24_L];
       S = Z^{(-1)}*C;
56
57
       Eb2_E = S(4);
       Eb2_T = sigma*T2^(4);
58
       dEb2 = Eb2_E - Eb2_T;
59
60
       if (dEb2>0 & dEb2<5) then
            J1 = S(1); // [W/square meter]
61
            J2R = S(2); // [W/square meter]
62
            J2L = S(3); // [W/square meter]
63
            Eb2 = S(4); // [W/square meter]
64
65
            T2new = T2; // [K]
66
       end
67 end
68 // the total heat flux lost by surface 1 is
69 q1_by_A1 = h*(T1-Tinf)+(Eb1-J1)*E1/(1-E1); // W/
      square meter]
70 // for a 0.5 by 0.5 m surface the heat lost is thus
```

```
71 q1 = q1_by_A1*l*b; // [W]
72 printf("\n\n the heat lost by plate is %f W',q1);
```

Scilab code Exa 8.20 solar environment equilibrium temperatures

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.20\n\n");
4 // solar-environment equilibrium temperatures
\frac{5}{\sqrt{2}} Example 8.20 (page no. -454)
6 // solution
8 \ q_by_A_sun = 700; // [W/m^(2)] \ solar \ flux
9 T_surr = 25+273; // [K] surrounding temperature
10 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
11 // at radiation equilibrium the netenergy absorbed
      from sun must equal the long-wavelength radiation
       exchange with the surroundings, or
  // (q_by_A_sun)*alpha_sun = alpha_low_temp*sigma*(T
      ^4-T_surr^4
                            (a)
13
14 // case (a) for white paint
15
16 // for white paint we obtain from table 8-4
17 	 alpha_sun = 0.12;
18 alpha_low_temp = 0.9;
19 // so that equation (a) becomes
20 T = [(q_by_A_sun)*alpha_sun/(alpha_low_temp*sigma)+
      T_{surr}^{(4)}]^{(1/4)}; // [K]
21 printf("radiation equilibrium temperature for the
      plate exposed to solar flux if the surface is
      coated with white paint is %f degree celsius",T
      -273);
22
23 // case (b) for flat black lacquer we obtain
```

Scilab code Exa 8.21 influence of convection on solar equilibrium temperature

```
1 clear;
2 clc;
3 printf("\t\tExample Number 8.21\n\n");
4 // influence of convection on solar equilibrium
      temperature
5 // \text{Example } 8.21 \text{ (page no.} -455)
6 // solution
8 T_surr = 25+273; // [K] surrounding temperature
9 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
10 h = 10; // [W/square meter] heat transfer coefficient
11 // in this case the solar energy absorbed must equal
       the sum of the radiation and convection
      transfers to the surroundings
12 // (q_by_A_sun)*alpha_sun = alpha_low_temp*sigma*(T)
      ^4 - T_surr^4) + h*(T - T_surr)
                                          (a)
13 q_by_A_sun = 700; // [W/m^(2)] solar flux
14
15 // for the white paint, using the same surface
      properties as in example 8-20 gives
16
```

```
17 	 alpha_sun = 0.12;
18 alpha_low_temp = 0.9;
19 // so that equation (a) becomes
20 deff('[y] = f(T)', 'y = (q_by_A_sun)*alpha_sun -
      alpha_low_temp*sigma*(T^4-T_surr^4)-h*(T-T_surr)
     );
21 T = fsolve(1,f);
22 printf ("the radiation-convection equillibrium
      temperatures for case (a) is %f degree celsius",T
      -273);
23
24 //for flat black lacquer we obtain
25
26 \text{ alpha_sun} = 0.96;
27 alpha_low_temp = 0.95;
28 // so that equation (a) becomes
29 deff('[y] = f2(T1)', 'y = (q_by_A_sun)*alpha_sun -
      alpha_low_temp*sigma*(T1^4-T_surr^4)-h*(T1-T_surr
      ) ');
30 \text{ T1} = fsolve(1,f2);
31 printf("\n\n the radiation-convection equillibrium]
      temperatures for case (b) is %f degree celsius",
     T1-273);
32 printf("\n\n where case (a)
                                    surface is coated
      with white paint");
33 printf("\n
                      case (b)
                                    surface is coated
      with flat black lacquer");
```

Scilab code Exa 8.23 temperature measurement error caused by radiation

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 8.23\n\n");
4 // temperature measurement error caused by radiation
5 // Example 8.23 (page no.-460)
```

Chapter 9

Condensation and Boiling Heat Transfer

Scilab code Exa 9.1 condensation on vertical plate

```
1 clear;
3 printf("\t \t \t Example Number 9.1\n \n \);
4 // condensation on vertical plate
5 // Example 9.1 (page no. -492)
6 // solution
8 // we have to check the reynolds no. to that film is
      laminar or turbulent
9 Tf = (100+98)/2; // [degree celsius]
10 Tw = 98; // [degree celsius]
11 RHOf=960; // [kg/cubic meter]
12 MUf = 2.82*10^(-4); // [kg/m s]
13 Kf=0.68; // [W/m degree celsius]
14 g=9.81; // [m/s^{(2)}]
15 L=0.3; // [m]
16 // RHOf(RHOf–RHOv)~RHOf^(2)
17 // let us assume laminar film condensate
18 Tsat=100; // [degree celsius]
```

```
19 Tg=100; // [degree celsius]
20 Hfg=2255*10^{(3)}; // [J/kg]
21 hbar=0.943*((RHOf^(2)*g*Hfg*Kf<math>^(3)/(L*MUf*(Tg-Tw)))
      ^(0.25));// [W/square meter degree celsius]
22 h=hbar; // [W/square meter degree celsius]
23 // checking reynolds no. with equation (9-17)
24 Ref=4*h*L*(Tsat-Tw)/(Hfg*MUf);
25 printf ("value of reynolds no. is \%f \n\ so the
     laminar assumption was correct ", Ref);
26 // the heat transfer is now calculated from
27 A=0.3*0.3; // [square meter]
28 q=hbar*A*(Tsat-Tw); // [W]
29 mdot=q/Hfg; // [kg/h]
30 printf("\n the heat transfer is %f w",q);
31 mdot=mdot*3600; // [kg/h]
32 printf("\n total mass flow condensate is \%f kg/h",
     mdot):
```

Scilab code Exa 9.2 condensation on tube tank

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 9.2\n\n\n");
4 // condensation on tube tank
5 // Example 9.2(page no.-493)
6 // solution
7
8 // the condensate properties are obtained from previous example
9 // replacing L by n*d
10 Tw=98;// [degree celsius]
11 RHOf=960;// [kg/cubic meter]
12 MUf=2.82*10^(-4);// [kg/m s]
13 Kf=0.68;// [W/m degree celsius]
14 g=9.81;// [m/s^(2)]
```

```
15 Tsat=100; // [degree celsius]
16 Tg=100; // [degree celsius]
17 Hfg=2255*10^{(3)};//[J/kg]
18 d=0.0127; // [m]
19 n = 10;
20 hbar=0.725*((RHOf^(2)*g*Hfg*Kf^(3)/(n*d*MUf*(Tg-Tw))
      )^(0.25));// [W/square meter degree celsius]
21 // total surface area is
22 n = 100;
23 Al=n*22*d/7; // [square meter]
24 printf("total surface area is %f square meter/m", Al)
25 // so the heat transfer is
26 Ql=hbar*Al*(Tg-Tw); // [W]
27 printf("\n\n heat transfer is %f kW/m",Q1/1000);
28 // total mass flow of condensate is then
29 mdotl=Ql/Hfg; // [kg/h]
30 mdotl=mdotl*3600; // [kg/h]
31 printf("\n\n total mass flow of condensate is %f kg/
     h", mdotl);
```

Scilab code Exa 9.3 boiling on brass plate

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 9.3\n\n\n");
4 // boiling on brass plate
5 // Example 9.3(page no.-501-502)
6 // solution
7
8 Qawater_platinum=946.1; // [kw/square meter] from figure (9-8) heat flux for water platinum combination
9 Tw=117; // [degree celsius]
10 Tsat=100; // [degree celsius]
```

```
// from table (9-2)
Csfwater_platinum=0.013; // for water platinum
Csfwater_brass=0.006; // for water brass
deff('y = G(Qawater_brass)', 'y = (((Qawater_brass) /((Qawater_platinum)))-((Csfwater_platinum/Csfwater_brass)^(3)))');
Qawater_brass = fsolve(0,G);
printf("heat transfer for water brass system is %f W/square meter", Qawater_brass);
```

Scilab code Exa 9.4 Flow boiling

```
1 clear;
2 clc;
3 printf("\t \t \t Example Number 9.4\n \n \);
4 // Flow boiling
5 // \text{Example } 9.4 \text{ (page no.} -506)
6 // solution
8 p = 5*101325/10^{(6)}; // [MPa] pressure of water
9 d = 0.0254; // [m] diameter of tube
10 Tw = 10; // [degree celsius]
11 // for calculation we use equation (9-45), noting
      that
12 dT = 10; // [degree celsius]
13 // the heat transfer coefficient is calculated as
14 h = 2.54*Tw^{(3)}*exp(p/1.551); [W/square meter
      degree celsius
15 // the surface area for a 1-m length of tube is
16 L = 1; // [m]
17 A = \%pi*d*L;// [square meter]
18 // so the heat transfer is
19 q = h*A*dT; // [W/m]
20 printf ("the heat transfer in a 1.0 m length of tube
      is \%f W/m",q);
```

Scilab code Exa 9.5 water boiling in a pan

```
1 clear;
2 clc;
3 printf("\t\tExample Number 9.5 \n\n");
4 // water boiling in a pan
5 // \text{Example } 9.5 \text{ (page no.} -506 - 507)
6 // solution
8 p = 101325/10<sup>(6)</sup>;// [MPa] pressure of water
9 	ext{ dT_x = 8;// [degree celsius]}
10 p1 = 0.17; // [MPa] given operating pressure
11 // we will use the simplified relation of table
     9-13 (page no. -506) for the estimates we do not
     know the value of g_by_A and so must choose one
      of the two relation for a horizontal surface from
       the table
12 // we anticipate nucleate boiling, so choose
13 h = 5.56*dT_x^(3); // [W/square meter degree celsius]
14 // and the heat flux is
15 q_by_A = h*dT_x; // [W/square meter]
16 // for operation as a pressure cooker we obtain the
      value of h from equation (9-44)
17 hp = h*(p1/p)^(0.4); // [W/square meter degree
      celsius]
18 // the corresponding heat flux is
19 q_by_A1 = hp*dT_x; // [W/square meter]
20 printf("heat flux obtained is %f kW/square meter",
      q_by_A/1000);
21 per_inc = 100*(q_by_A1-q_by_A)/q_by_A;
22 printf("\n\n if the pan operates as a pressure
      cooker at 0.17 MPa the increase in heat flux is
     %f percent", per_inc);
```

Scilab code Exa 9.6 heat flux comparisons

```
1 clear;
2 clc;
3 printf("\t\t\Example Number 9.6\n\n'");
4 // heat-flux comparisons
5 // \text{Example } 9.6 \text{ (page no.} -509)
6 // solution
8 Tw = 200; // [degree celsius] water temperature
9 L = 0.08; // [m] length of solid copper bar
10 dT = 100; // [degree celsius] temperature
      differential in copper bar
11 //using the data of table 9-4(page no. -508)
12 // the heat flux per unit area is expressed as
     q_by_A = -k*del_T/dx
13 // from table A-2(page no.-) the thermal
      conductivity of copper is
14 k = 374; // [W/m degree celsius]
15 q_by_A = -k*(-dT)/L; // [W/square meter]
16 // from table 9-4(page no.-508) the typical axial
     heat flux for a water heat flux for a water heat
      pipe is
17 q_by_A_axial = 0.67; // [kW/csquare meter]
18 q_by_A = q_by_A/(1000*10^(4)); // [kW/csquare meter]
19 printf("thus the heat transfers more than %f times
      the heat of a pure copper rod with a substantial
      temperature gradient.",q_by_A_axial/q_by_A);
```

Chapter 10

Heat Exchangers

Scilab code Exa 10.1 overall heat transfer coefficient for pipe in air

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.1\n\n");
4 // overall heat transfer coefficient for pipe in air
5 // \text{Example } 10.1 \text{ (page no.} -520 - 522)
6 // solution
8 Tw = 98; // [degree celsius] temperature of hot water
9 k_p = 54; // [W/m degree celsius] heat transfer
      coefficient of pipe
10 Ta = 20; // [degree celsius] atmospheric air
      temperature
11 u = 0.25; // [m/s] water velocity
12 // from appendix A the dimensions of 2-in schedule
     40 pipe are
13 ID = 0.0525; // [m]
14 OD = 0.06033; // [m]
15 // the properties of water at 98 degree celsius are
16 rho = 960; // [kg/cubic meter]
17 mu = 2.82*10^(-4); // [kg/m s]
18 k_w = 0.68; // [W/m degree celsius]
```

```
19 Pr = 1.76; // prandtl number
20 // the reynolds number is
21 Re = rho*u*ID/mu;
22 // and since turbulent flow is encountered, we may
      use equation (6-4):
23 Nu = 0.023*Re^{(0.8)*Pr^{(0.4)}};
24 hi = Nu*k_w/ID; // [W/square meter degree celsius]
25 // for unit length of pipe the thermal resistance of
      the steel is
26 \text{ Rs} = \frac{\log(0D/ID)}{(2*\%pi*k_p)};
27 // again, on a unit length basis the thermal
     resistance on the inside is
28 Ai = %pi*ID; // [square meter]
29 Ri = 1/(hi*Ai);
30 Ao = \%pi*OD; // [square meter]
31 // the thermal resistance for outer surface is as
      yet unknown but is written, for unit lengths, is
      Ro = 1/(ho*Ao)
                                    (a)
  // from table 7-2(page no. -339), for laminar flow,
      the simplified relation for ho is
33 // ho = 1.32*(dT/d)^(1/4) = 1.32*((To-Ta)/OD)^(1/4)
      (b)
34 // where To is the unknown outside pipe surface
      temperature, we designate the inner pipe surface
      as Ti and the water temperature as Tw; then the
      energy balance requires
35 / (Tw-Ti)/Ri = (Ti-To)/Rs = (To-Ta)/Ro
      (c)
36 // combining equations (a) and (b) gives
37 // (To-Ta)/Ro = \%pi*OD*1.32*(To-Ta)^(5/4)/OD^(1/4)
38 // this relation may be introduced into equation (c)
      to yield two equations with the two unknowns Ti
     and To:
39
40 // (Tw-Ti)/Ri = (Ti-To)/Rs
41 // (Ti-To)/Rs = \%pi*OD*1.32*(To-Ta)^(5/4)/OD^(1/4)
```

```
(2)
42 // this is a non-linear equation which can be solved
43 for Ti = 50:0.001:100
       Q = ((Ti-(Ti-(Tw-Ti)*(Rs/Ri)))/Rs)-(%pi*OD)
44
          *1.32*((Ti-(Tw-Ti)*(Rs/Ri))-Ta)^(5/4)/OD
          ^(1/4));
       if Q>0 & Q<6 then
45
           Tinew = Ti;
46
47
       else
48
           Ti = Ti;
49
       end
50 end
51 Ti = Tinew;// [degree celsius]
52 To = (Ti-(Tw-Ti)*(Rs/Ri)); // [Degree celsius]
53 // as a result, the outside heat transfer
      coefficient and thermal resistance are
54 ho = 1.32*((To-Ta)/OD)^(1/4);//[W/square meter]
      degree celsius]
55 \text{ Ro} = 1/(0D*7.91*\%pi); //
56 // the overall heat transfer coefficient based on
      the outer area is written in terms of these
      resistances as
57 Uo = 1/(Ao*(Ri+Ro+Rs)); // [W/area degree celsius]
58 // in this calculation we used the outside area for
      1.0 m length as Ao
59 // so
60 Uo = Uo; // [W/square meter degree celsius]
61 printf("overall heat transfer coefficient is %f W/
      square meter degree celsius", Vo);
```

Scilab code Exa 10.2 overall heat transfer coefficient for pipe exposed to steam

```
1 clear;
```

```
2 clc;
3 printf("\t\t\Example Number 10.2 \ln n");
4 // overall heat transfer coefficient for pipe
      exposed to steam
5 / \text{Example } 10.2 \text{ (page no.} -523 - 524)
6 // solution
8 p = 101325; // [Pa] pressure of steam
9 Tg = 100; // [degree celsius] temperature of steam
10 // we have already determined the inside convection
      heat-transfer coefficient in example (10.1) as
11 hi = 1961; // [W/square meter]
12 // the water film properties are
13 rho = 960; // [kg/cubic meter] density
14 mu_f = 2.82*10^(-4); // [kg/m s]
15 kf = 0.68; // [W/m degree celsius]
16 hfg = 2255*10^{(3)}; // [J/kg]
17 g = 9.8; // [m/s^(2)] acceleration due to gravity
18 d = 0.06033; // [m] diameter of the pipe
19 // the convection coefficient for condensation on
      the outside of the pipe is obtained by using
      equation (9-12)
20 // h_o = 0.725*[(rho^(2)*g*hfg*kf^(3))/(mu_f*d*(Tg-
     To)) | ^ (1/4)
                                                (a)
21 Ao = \%pi*d;// [square meter] outside area
22 // outside thermal resistance per unit length is
23 // R_o = 1/(h_o * A_o)
      (b)
24 // the energy balance requires
25 // [Tg-To]/R_o = [To-Ti]/R_s = [Ti-Tw]/R_i
      (c)
26 // from example 10.1 we have
27 \text{ Ri} = 3.092*10^{(-3)};
28 \text{ Rs} = 4.097*10^{-4};
29 Tw = 98; // [degree celsius]
30 // equation (b) and (c) may be combined to give
```

```
31 / (Tg-To)^(3/4)/3403 = (To-Ti)/Rs
                                                                                                                                                                          (1)
32 // (To-Ti)/Rs = (Ti-Tw)/Ri
                                                                                                                                            (2)
33 // this is a non-linear equation which can be solved
                      as
34 for Ti = 98.1:0.01:99.75
35
                      P = ((Tg - (Ti + Rs * (Ti - Tw) / Ri))^{(3/4)}) * 3403 - (((Ti + Tw) / Ri))^{(3/4)}) * ((Ti + Tw) / Ri)) * ((Ti + Tw) / Ri))
                               Rs*(Ti-Tw)/Ri)-Ti)/Rs);
36
                       if P > (-10) \& P < 0 then
37
                                    Tinew = Ti;
38
                       else
39
                                    Ti = Ti;
40
                       end
41
42 end
43 Ti = Tinew; // [degree celsius]
44 To = (Ti+Rs*(Ti-Tw)/Ri);//[degree celsius]
45 // the exterior heat-transfer coefficient and
                   thermal resistance then become
46 ho = 0.725*[(rho^{(2)}*g*hfg*kf^{(3)})/(mu_f*d*(Tg-To))]
                  ]^(1/4);// [W/square meter degree celsius]
47 Ro = 1/(ho*Ao);
       // based on unit length of pipe, the overall heat
                   transfer coefficient is
49 Uo = 1/(Ao*(Ri+Ro+Rs)); // [W/area degree celsius]
50 // since Ao and the R's were per unit length
51 // so
52 Uo = Uo; // [W/square meter degree celsius]
53 printf ("overall heat transfer coefficient is %f W/
                   square meter degree celsius", Uo);
```

Scilab code Exa 10.3 influence of fouling factor

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.3\n\n\n");
```

```
4  // influence of fouling factor
5  // Example 10.2 (page no.-524-525)
6  // solution
7
8  // the fouling factor influences the heat transfer coefficient on the inside of the pipe. we have
9  Rf = 0.0002;
10  // using
11  h_clean = 1961; // [W/square meter degree celsius]
12  // we obtain
13  hi = 1/[Rf+(1/h_clean)]; // [W/square meter degree celsius]
14  printf("the percent reduction because of fouling factor is %f",(h_clean-hi)*100/h_clean);
```

Scilab code Exa 10.4 calculation of heat exchanger size from known temperatures

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.4 \ln n");
4 // calculation of heat exchanger size from known
      temperatures
5 // \text{Example } 10.4 \text{ (page no.} -532-533)
6 // solution
8 \text{ m\_dot} = 68; // [kg/min] \text{ water flow rate}
9 U = 320; // [W/square meter degree celsius] overall
      heat transfer coefficient
10 T1 = 35; // [degree celsius] initial temperature
11 T2 = 75; // [degree celsius] final temperature
12 Toe = 110; // [degree celsius] oil entering
      temperature
13 Tol = 75; // [degree celsius] oil leaving temperature
14 Cw = 4180; // [J/kg degree celsius] water specific
```

```
heat capacity

// the total heat transfer is determined from the energy absorbed by the water:

q = m_dot*Cw*(T2-T1); // [J/min]

q = q/60; // [W]

// since all the fluid temperatures are known, the LMTD can be calculated by using the temperature scheme in figure 10-7b(page no.-530)

dT_m = ((Toe-Tol)-(T2-T1))/log((Toe-Tol)/(T2-T1)); // [degree celsius]

// then, since q = U*A*dT_m

A = q/(U*dT_m); // [square meter] area of heat—exchanger

printf("area of heat—exchanger is %f square meter", A);
```

Scilab code Exa 10.5 shell and tube heat exchanger

```
clear;
clc;
printf("\t\t\tExample Number 10.5\n\n\n");

// shell-and-tube heat exchanger
// Example 10.5 (page no.-533-534)

// solution

// to solve this problem, we determine a correction factor from figure 10-8 to be used with the LMTD calculated on the basis of counterflow exchanger.

// the parameters according to the nomenclature of figure 10-8(page no.-532) are

T1 = 35; // [degree celsius]
T2 = 75; // [degree celsius]

t1 = 110; // [degree celsius]

t2 = 75; // [degree celsius]

t3 t2 = 75; // [degree celsius]

t4 P = (t2-t1)/(T1-t1);
```

```
15 R = (T1-T2)/(t2-t1);
16 // so the correction factor is
17 F = 0.81; // from figure 10-10(page no.-534)
18 // and the heat transfer is q = U*A*F*dT_m
19 // so that. from example 10-4 we have
20 U = 320; // [W/square meter degree celsius] overall
    heat transfer coefficient
21 q = 189493.33; // [W]
22 dT_m = 37.44; // [degree celsius]
23 A = q/(U*F*dT_m); // [square meter]
24 printf("area required for this exchanger is %f
    square meter", A)
```

Scilab code Exa 10.6 design of shell and tube heat exchanger

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.6 \ln n");
4 // design of shell-and-tube heat exchanger
5 // Example 10.5 (page no.-534-536)
6 // solution
8 \text{ m\_dot\_c} = 3.8; // [kg/s] \text{ water flow rate}
9 Ti = 38; // [degree celsius] initial temperature of
      water
10 Tf = 55; // [degree celsius] final temperature of
      water
11 m_{dot_h} = 1.9; // [kg/s] water flow rate entering the
       exchanger
12 Te = 93; // [degree celsius] entering water
      temperature
13 U = 1419; // [W/square meter degree celsius] overall
     heat transfer coefficient
14 d = 0.019; // [m] diameter of tube
15 v_{avg} = 0.366; // [m/s] average water velocity in
```

```
exchanger
16 Cc = 4180; // [] specific heat of water
17 Ch = Cc; // [] specific heat
18 rho = 1000; // [kg/cubic meter] density of water
19 // we first assume one tube pass and check to see if
      it satisfies the conditions of this problem. the
      exit temperature of the hot water is calculated
     from
20 dTh = m_dot_c*Cc*(Tf-Ti)/(m_dot_h*Ch); // [degree]
      celsius
21 Th_exit = Te-dTh;// [degree celsius]
22 // the total required heat transfer is obtained for
     the cold fluid is
23 q = m_dot_c*Cc*(Tf-Ti); // [W]
24 // for a counterflow exchanger, with the required
     temperature
25 \quad LMTD = ((Te-Tf)-(Th_exit-Ti))/log((Te-Tf)/(Th_exit-Ti))
     Ti));// [degree celsius]
26 dTm = LMTD;// [degree celsius]
27 A = q/(U*dTm); // [square meter]
28 // using the average water velocity in the tubes and
      the flow rate, we calculate the total area with
29 A1 = m_dot_c/(rho*v_avg); // [square meter]
30 // this area is the product of number of tubes and
     the flow area per tube:
31 n = A1*4/(\%pi*d^2); // no. of tubes
32 n = ceil(n); // rounding of value of n because no. of
      pipe is an integer value
33 // the surface area per tube per meter of length is
34 S = %pi*d; // [square meter/tube meter]
35 // we recall that the total surface area required
     for a one tube pass exchanger was calculated
     above .
36 // we may thus compute the length of tube for this
     type of exchanger from
37 L = A/(S*n); // [m]
38 // this length is greater than the allowable 2.438 m
      , so we must use more than one tube pass. when we
```

```
increase the number of passes, we
      correspondingly increase the total surface area
      required because of the reduction in LMTD caused
     by the correction factor F.
39 // we next try two tube passes. from figure 10-8(
     page no. -532)
40 F = 0.88;
41 A_total = q/(U*F*dTm); // [square meter]
42 // the number of tubes per pass is still 37 because
     of the velocity requirement. for the two pass
     exchanger the total surface area is now related
     to the length by
43 L1 = A_{total}/(2*S*n); // [m]
44 // this length is within the 2.438 m requirement, so
      the final design choice is
45 printf("number of tubes per pass = \%f",n);
46 printf("\n\n number of passes = 2");
47 printf("\n\n length of tube per pass = \%f m",L1);
```

Scilab code Exa 10.7 cross flow exchanger with one fluid mixed

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.7\n\n\n");
4 // cross flow exchanger with one fluid mixed
5 // Example 10.7 (page no.-537)
6 // solution
7
8 m_dot = 5.2; // [kg/s] mass flow rate
9 T1 = 130; // [degree celsius] temperature of entering steam
10 T2 = 110; // [degree celsius] temperature of leaving steam
11 t1 = 15; // [degree celsius] temperature of entering oil
```

```
12 t2 = 85; // [degree celsius] temperature of leaving
13 c_oil = 1900; // [J/kg degree celsius] heat capacity
      of oil
14 c_steam = 1860; // [J/kg degree celsius] heat
      capacity of steam
15 U = 275; // [W/square meter degree celsius] overall
     heat transfer coefficient
16 //the total heat transfer may be obtained from an
      energy balance on the steam
17 q = m_dot*c_steam*(T1-T2); // [W]
18 // we can solve for the area from equation (10-13).
     the value of dT_m is calculated as if the
      exchanger were counterflow double pipe, thus
19 dT_m = ((T1-t2)-(T2-t1))/log((T1-t2)/(T2-t1)); // [
      degree celsius
20 // t1,t2 is representing the unmixed fluid(oil) and
     T1, T2 is representing the mixed fluid (steam) so
      that:
21 // we calculate
22 R = (T1-T2)/(t2-t1);
23 P = (t2-t1)/(T1-t1);
24 // consulting figure 10-11(page no. -534) we find
25 F = 0.97;
26 // so the area is calculated from
27 A = q/(U*F*dT_m); // [square meter]
28 printf ("surface area of heat exchanger is %f square
     meter", A);
```

Scilab code Exa 10.8 effects of off design flow rates for exchanger in previous example

```
1 clear; 2 clc; 3 printf("\t\t\tExample Number 10.8\n\n");
```

```
4 // effects of off-design flow rates for exchanger in
      example 10-7
5 // \text{Example } 10.8 \text{ (page no.} -537-538)
6 // solution
8 // we did not calculate the oil flow in example 10-7
      but can do so now from
9 q = 193; // [kW]
10 c_oil = 1.9; // [J/kg degree celsius] heat capacity
11 t1 = 15; // [degree celsius] temperature of entering
12 t2 = 85; // [degree celsius] temperature of leaving
      o i l
13 m_{dot_o} = q/(c_{oil}*(t2-t1)); // [kg/s]
14 // the new flow rate will be half this value
15 m_{dot_o} = m_{dot_o/2}; // [kg/s]
16 // we are assuming the inlet temperatures remain the
      same at 130 degree celsius for the steam and 15
      degree celsius for the oil.
17 // the new relation for the heat transfer is q =
      m_{dot_o} * c_{oil} * (Teo - 15) = m_{dot_s} * cp * (130 - Tes)
                             (a)
18 // but the exit temperatures, Teo and Tes are
     unknown. furthermore, dT_m is unknown without
      these temperatures, as are the values of R and P
     from figure 10-11 (page no. -535). this means we
     must use an iterative procedure to solve for the
      exit temperatures using equation (a) and
     A*F*dT_m
                         (b)
19 // the general procedure is to assume values of the
      exit temperatures until the q's agree between
      equations (a) and (b).
20 printf ("the objective of this example is to show
      that an iterative procedure is required when the
      inlet and outlet temperatures are not known or
      easily calculated");
21 printf("\n\n there is no need to go through this
```

iteration because it can be avoided by using the techniques described in section 10-6");

Scilab code Exa 10.9 off design calculation using E NTU method

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.9 \ n \ n");
4 // off-design calculation using E-NTU method
5 / \text{Example } 10.9 \text{ (page no.} -542 - 544)
6 // solution
8 \text{ m\_dot\_o} = 0.725; // [kg/s] \text{ oil flow rate}
9 \text{ m\_dot\_s} = 5.2; // [kg/s] \text{ steam flow rate}
10 t1 = 15; // [degree celsius] temperature of entering
      oil
11 T1 = 130; // [degree celsius] temperature of entering
12 c_oil = 1900; // [J/kg degree celsius] heat capacity
      of oil
13 c_steam = 1860; // [J/kg degree celsius] heat
      capacity of steam
14 // for the steam
15 Cs = m_dot_s*c_steam; // [W/degree celsius]
16 // for the oil
17 Co = m_dot_o*c_oil; // [W/degree celsius]
18 // so the oil is minium fluid. we thus have
19 C_min_by_C_max = Co/Cs;
20 U = 275; // [W/square meter degree celsius] overall
      heat transfer coefficient
21 A = 10.83; // [square meter] surface area of heat
      exchanger
22 NTU = U*A/Co;
23 // we choose to use the table and note that Co(
      minimum) is unmixed and Cs(maximum) is mixed so
```

```
that the first relation in the table 10-3 (page no
      .-543)
             applies.
24 // we therfore calculate E(effectiveness) as
25 E = (1/C_min_by_C_max)*\{1-exp(-C_min_by_C_max*(1-exp_max))\}
      (-NTU)))};
26 // if we were using figure 10-14 (page no. -544) we
      would have to evaluate
27 C_mixed_by_C_unmixed = Cs/Co;
28 // and would still determine
29 E = 0.8; // approximately
30 // now, using the effectiveness we can determine the
       temperature difference of the minimum fluid (oil
31 dT_o = E*(T1-t1); // [degree celsius]
32 // so that heat transfer is
33 q = m_{dot_o*c_oil*(dT_o);//[W]}
34 \text{ q\_initial} = 193440; // [W] \text{ heat transfer when oil}
      flow rate is 100 %
35 printf ("we find a reduction in the oil flow rate of
      50 % causes a reduction in heat transfer of only
       \%f \%\%, (q_initial-q)*100/q_initial);
```

Scilab code Exa 10.10 off design calculation of exchanger in example 10 4

```
10 T2 = 75; // [degree celsius] final temperature
11 Toe = 110; // [degree celsius] oil entering
      temperature
12 Tol = 75; // [degree celsius] oil leaving temperature
13 Cc = 4180; // [J/kg degree celsius] water specific
      heat capacity
14 Ch = 1900; // [J/kg degree celsius] heat capacity of
      oil
15 U = 320; // [W/square meter degree celsius] overall
     heat transfer coefficient
16 A = 15.814568; // [square meter] area of heat
      exchanger (from example 10-4)
17 // the flow rate of oil is calculated from the
      energy balance for the original problem:
18 m_{dot_h} = m_{dot_c*Cc*(T2-T1)/(Ch*(Toe-Tol)); // [kg/
19 // the capacity rates for the new conditions are
      calculated as
20 C_h = m_dot_h*Ch/60; // [W/degree celsius]
21 C_c = m_dot_c*Cc/60; // [W/degree celsius]
22 // so that the water (cold fluid) is the minimum
      fluid, and
23 C_min_by_C_max = C_c/C_h;
24 \text{ NTU_max} = \text{U*A/C_c};
25 // from figure 10-13 (page no. -542) or table 10-3 (
      page no. -543) the effectiveness is
26 E = 0.744;
27 // and because the cold fluid is the minimum, we can
28 \text{ dT\_cold} = \text{E*(Toe-T1);} // [degree celsius]
29 // and the exit water temperature is
30 Tw_exit = T1+dT_cold; // [degree celsius]
31 // the total heat transfer under the new flow
      conditions is calculated
32 \text{ m\_dot\_c} = 40; // [kg/min]
33 q = m_dot_c*Cc*dT_cold/60; // [W]
34 printf ("exit water temperature is %f degree celcius"
      ,Tw_exit);
```

35 printf(" \n the total heat transfer under the new flow conditions is %f kW",q/1000);

Scilab code Exa 10.11 cross flow exchanger with both fluid unmixed

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.11\n\n");
4 // cross-flow exchanger with both fluid unmixed
5 / \text{Example } 10.11 \text{ (page no.} -547 - 549)
6 // solution
8 pa = 101325; // [Pa] pressure of air
9 Ti = 15.55; // [degree celsius] initial temperature
10 Tf = 29.44; // [degree celsius] final temperature of
11 Thw = 82.22; // [degree celsius] hot water
      temperature
12 U = 227; // [W/square meter degree celsius] overall
     heat transfer coefficient
13 S = 9.29; // [square meter] total surface area of
     heat exchanger
14 R = 287; // [] universal gas constant
15 Cc = 1006; // [J/kg degree celsius] specific heat of
      air
16 Ch = 4180; // [J/kg degree celsius] specific heat of
17 // the heat transfer is calculated from the energy
     balance on the air. first, the inlet air density
18 rho = pa/(R*(Ti+273.15)); // [kg/cubic meter]
19 // so the mass flow of air (the cold fluid) is
20 mdot_c = 2.36*rho; // [kg/s]
21 // the heat transfer is then
```

```
22 q = mdot_c*Cc*(Tf-Ti); // [W]
23 // from the statement of the problem we do not know
      whether the air or water is the minimum fluid. a
      trial and error procedur must be used with figure
        10-15 (page no. -545) or table 10-3 (page no. -543)
24 // we assume that the air is the minimum fluid and
      then check out our assumption. then
25 Cmin = mdot_c*Cc; // [W/degree celsius]
26 \text{ NTU_max} = \text{U*S/Cmin};
27 // and the effectiveness based on the air as the
     minimum fluid is
28 E = (Tf-Ti)/(Thw-Ti);
29 // entering figure 10-15, we are unable to match
      these quantities with the curves. this require
      that the hot fluid be the minimum. we must
      therefore assume values for the water flow rate
      until we are able to match the performance as
      given by figure 10-15 or table 10-3, we first
      note that
30 Cmax = mdot_c*Cc; // [W/degree celsius]
                                                        (a)
31 // NTU_max = U*S/Cmin;
                                                         (b
32 // E = dT_h/(Thw-Ti)
                                                        (c)
33 // dT_h = q/Cmin
                                                        (d)
34
35 // now we assume different values for Cmin abd
      calculate different-different values for NTU_max,
       dT_h, and E
36
37 // for
38 \text{ Cmin_by\_Cmax1} = 0.5;
39 Cmin1 = Cmin_by_Cmax1*Cmax;// [W/degree celsius]
40 \text{ NTU_max1} = \text{U*S/Cmin1};
dT_h1 = q/Cmin1; // [degree celsius]
42 E1_c1 = dT_h1/(Thw-Ti); // calculated
43 \text{ E1\_t1} = 0.65; // \text{ from table}
44
```

```
45 // for
46 \text{ Cmin_by\_Cmax2} = 0.25;
47 Cmin2 = Cmin_by_Cmax2*Cmax;// [W/degree celsius]
48 \text{ NTU_max2} = \text{U*S/Cmin2};
49 dT_h2 = q/Cmin2;// [degree celsius]
50 \text{ E1\_c2} = dT\_h2/(Thw-Ti); // calculated
51 E1_t2 = 0.89; // from table
52
53 // for
54 \text{ Cmin_by\_Cmax3} = 0.22;
55 Cmin3 = Cmin_by_Cmax3*Cmax; // [W/degree celsius]
56 \text{ NTU_max3} = \text{U*S/Cmin3};
57 \text{ dT_h3} = \text{q/Cmin3;}// [\text{degree celsius}]
58 E1_c3 = dT_h3/(Thw-Ti); // calculated
59 E1_t3 = 0.92; // from table
60
61 // we estimate the water-flow rate as about
62 Cmin = 660; // [W/degree celsius]
63 \text{ mdot_h} = \text{Cmin/Ch}; // [kg/s]
64 // the exit water temperature is accordingly
65 Tw_exit = Thw-q/Cmin; // [degree celsius]
66 printf ("the exit water temperature is %f degree
      celsius", Tw_exit);
67 printf("\n\n the heat transfer is %f kW",q/1000);
```

Scilab code Exa 10.12 comparison of single or two exchanger options

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.12\n\n\n");
4 // comparison of single - or two-exchanger options
5 // Example 10.12 (page no.-549-551)
6 // solution
7
8 mdot_c = 1.25; // [kg/s] water flow rate
```

```
9 Ti = 35; // [degree celsius] initial temperature of
     water
10 Tf = 80; // [degree celsius] final temperature of
     water
11 Toi = 150; // [degree celsius] initial temperature of
       oil
12 Tof = 85; // [degree celsius] final temperature of
      oil
13 U = 850; // [W/square meter degree celsius] overall
     heat transfer coefficient
14 Cp_water = 4180;// [] specific heat of water
15 Cp_oil = 2000; // [J/kg degree celsius]
16 // we calculate the surface area required for both
      alternatives and then compare costs. for the one
     large exchanger
17 q = mdot_c*Cp_water*(Tf-Ti); // [W]
18 mdot_c_into_Cp_water = mdot_c*Cp_water; // [W/degree]
      celsius
19 mdot_h_into_Cp_oil = q/(Toi-Tof);// [W/degree
      celsius
20 Cmin = mdot_h_into_Cp_oil; // [W/degree celsius]
21 Cmax = mdot_c_into_Cp_water; // [W/degree celsius]
22 // so that oil is the minimum fluid:
23 Eh = (Toi-Tof)/(Toi-Ti);
24 Cmin_by_Cmax = Cmin/Cmax;
25 // from figure 10-13 (page no. -542),
26 \text{ NTU_max} = 1.09;
27 A = NTU_max*Cmin/U; // [square meter]
28 // we now wish to calculate the surface—area
     requirement for the two small exchanger because U
     *A and Cmin are the same for each exchanger.
29 // this requires that the effectiveness be the same
     for each exchanger, thus,
30 // E1 = (Toi-Toe_1)/(Toi-Ti) = E2 = (Toi-Toe_2)/(Toi
     -Tw2)
     (a)
31 // where the nomenclature for the temperatures is
     indicated in the sketch. because the oil flow is
```

```
the same in each exchanger and the average exit
      oil temperature must be 85 degree celsius, we may
       write
32 / (Toe_1 + Toe_2)/2 = 85
  // an energy balance on the second heat exchanger
      gives
34 // \text{mdot\_c\_into\_Cp\_water} * (\text{Tf-Tw2}) =
      m dot_h into_C p_oil*(Toi-Toe_2)/2
                                          (c)
35 // we now have three equations (a),(b), and (c)
      which may be solved for the three unknowns Toe_1,
       Toe_2, and Tw2.
36 // eliminating Tw2, and Toe_1 from equation (a) by
      the help of equation (b) and (c)
37 deff('[y] = H(Toe_2)', 'y = (Toi-(170-Toe_2))/(Toi-Tie_2)
      - (Toi-Toe_2)/(Toi-(Tf-(mdot_h_into_Cp_oil*(Toi)
      -\text{Toe}_2)/(mdot_c_into_Cp_water*2)))));
38 Toe_2 = fsolve(1,H);// [degree celsius]
39 Toe_1 = (170-Toe_2);// [degree celsius]
40 \text{ Tw2} = (\text{Tf-(mdot\_h\_into\_Cp\_oil*(Toi-Toe\_2)/(}
      mdot_c_into_Cp_water*2)));// [degree celsius]
41 // the effectiveness can then be calculated as
42 E1 = (Toi-Toe_1)/(Toi-Ti);
43 E2 = E1;
44 // from figure 10-13 (page no. -542), we obtain
45 \text{ NTU_max} = 1.16;
46 // so that
47 A1 = NTU_max*Cmin/(U*2); // [square meter]
48 printf ("we have find that %f square meter of area is
       required for each of small exchangers, or a
      total of %f square meter", A1,2*A1);
49 printf("\n\n the area required in the one larger
      exchanger is %f square meter", A);
50 printf("\n\n the cost per unit area is greater so
      that the most economical choice would be the
      single larger exchanger ");
```

Scilab code Exa 10.13 shell and tube exchangeras air heater

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.13 \setminus n \setminus n");
4 // shell and tube exchangeras air heater
5 / \text{Example } 10.13 \text{ (page no.} -551 - 552)
6 // solution
8 To = 100; // [degree celsius] temperature of hot oil
9 m_{dot_a} = 2; // [kg/s] flow rate of air
10 T1 = 20; // [degree celsius] initial temperature of
      air
11 T2 = 80; // [degree celsius] final temperature of air
12 Cp_o = 2100; // [J/kg degree celsius] specific heat
      of the oil
13 Cp_a = 1009; // [J/kg degree celsius] specific heat
      of the air
14 m_{dot_o} = 3; // [kg/s] flow rate of oil
15 U = 200; // [W/square meter] overall heat transfer
      coefficient
16 // the basic energy balance is m_dot_o*Cp_o*(To-Toe)
      = m_{dot_a} * Cp_a * (T2-T1)
17 Toe = To-m_dot_a*Cp_a*(T2-T1)/(m_dot_o*Cp_o); //
      degree celsius
18 // we have
19 m_dot_h_into_Ch = m_dot_o*Cp_o; // [W/degree celsius]
20 m_dot_c_into_Cc = m_dot_a*Cp_a; // [W/degree celsius]
21 // so the air is minimum fluid
22 C = m_dot_c_into_Cc/m_dot_h_into_Ch;
23 // the effectiveness is
24 E = (T2-T1)/(To-T1);
25 // now we may use either figure 10-16 (page no. -546)
      or the analytical relation from table 10-4 (page
```

Scilab code Exa 10.14 ammonia condenser

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.14\n\n");
4 // ammonia condenser
5 // \text{Example } 10.14 \text{ (page no.} -552 - 553)
6 // solution
8 Ta = 50; // [degree celsius] temperature of entering
     ammonia vapour
  Tw1 = 20; // [degree celsius] temperature of entering
       water
10 q = 200; // [kW] total heat transfer required
11 U = 1; // [kW/square meter degree celsius] overall
     heat transfer coefficient
12 Tw2 = 40; // [degree celsius] temperature of exiting
      water
13 Cw = 4.18; // [kJ/kg degree celsius] specific heat of
       water
14 // the mass flow can be calculated from the heat
      transfer with
15 m_{dot_w} = q/(Cw*(Tw2-Tw1)); // [kg/s]
16 // because this is the condenser the water is the
     minimum fluid and
17 C_min = m_dot_w*Cw; // [kW/degree celsius]
```

```
18 // the value of NTU is obtained from the last entry
      of table 10-4 (page no. -543), with
19 E = 0.6; // effectiveness
20 \quad NTU = -\log(1-E);
21 // so that area is calculated as
22 A = C_{min*NTU/U;} [square meter]
23 // when the flow rate is reduced in half the new
      value of NTU is
24 NTU1 = U*A/(C_min/2);
25 // and the effectiveness is computed from the last
      entry of table 10-3 (page no. -543):
26 \quad E1 = 1 - \exp(-NTU1);
27 // the new water temperature difference is computed
      as
28 dT_w = E1*(Ta-Tw1); // [degree celsius]
29 // so that the heat transfer is
30 \text{ q1} = C_min*dT_w/2; // [kW]
31 printf("the area to achieve a heat exchanger
      effectiveness of 60%% with an exit water
      temperature of 40 degree celsius is %f square
     meter", A);
32 printf("\n by reducing the flow rate we have
     lowered the heat transfer by %d percent", (q-q1)
      *100/q);
```

Scilab code Exa 10.15 crossflow exchanger as energy conservation device

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 10.15\n\n\n");
4 // crossflow exchanger as energy conservation device
5 // Example 10.15 (page no.-553-555)
6 // solution
7
8 q = 210000;// [W] heat to be removed from
```

```
atmospheric air
9 m_{dot_h} = 1200/60; // [kg/s] hot air flow rate
10 m_dot_c = m_dot_h; // [kg/s] cold air flow rate
11 Ta1 = 25; // [degree celsius] atmospheric air
     temperature
12 Ta2 = 0; // [degree celsius] temperature of air
     entering from out-door conditions
13 U = 30; // [W/m degree celsius] overall heat transfer
      coefficient
14 Cp = 1005; // [J/kg degree celsius] specific heat of
      air
15
16 //*************calculation 1. the design value for
      the area of the heat exchanger *********//
17
18 // the hot and cold fluids have the same flow rate
19 // and
20 Ch = m_dot_h*Cp; // [W/degree celsius]
21 Cc = m_dot_c*Cp; // [W/degree cslsius]
22 Cmin_by_Cmax = 1; // for use in table 10-3 (page no
     -543
23 // the energy balance gives q = Ch*dT_h = Cc*dT_c
24 // and
25 dT_h = q/Ch; // [degree celsius]
26 dT_c = q/Cc;// [degree celsius]
27 // the heat exchanger effectiveness is
28 E = dT_h/(Ta1-Ta2);
29 // consulting table 10-3 (page no. -543) for a cross
     flow exchanger with both fluids unmixed, and
     inserting the value
30 \ C = 1;
31 // \text{ we have}
32 deff('[y] = f(N)', 'y = E-1+\exp(N^{(0.22)}*(\exp(-N))
     (0.78))-1));
33 N = fsolve(1,f);
34 // solving above to get the value of NTU
35 // area is
36 A = N*Ch/U; // [square meter]
```

```
37 printf("the design value for the area of heat
      exchanger is %f square meter", A);
38
39 //************calculation 2. the percent reduction
     in heat transfer rate if the flow rate is reduced
      by 50% while keeping the inlet temperatures and
        value of U constant **********//
40
41 // we now examine the effect of reducing the flow
     rate by half, while keeping the inlet
      temperatures and value of U the same.
42 // note that the flow rate of both fluids is reduced
      because they are physically the same fluid. this
      means that the value of Cmin_by_Cmax will remain
      the same at a value of 1.0.
43 // the new value of Cmin is
44 Cmin = Cc/2; // [W/degree celsius]
45 // so that NTU is
46 N = U*A/Cmin;
47 // equation (b) may be used for the calculation of
      effectiveness
48 E = 1 - \exp(N^{(0.22)} * (\exp(-N^{(0.78)}) - 1));
49 // the temperature difference for each fluid is then
50 dT = E*(Ta1-Ta2); // [degree celsius]
51 // the resulting heat transfer is then
52 \text{ q_dot} = \text{m_dot_c*Cp*dT/2;} // [W]
53 printf("\n\nthe percent reduction in heat transfer
      rate if the flow rate is reduced by 50%% is %f "
      ,(q-q_dot)*100/q);
54
55 //***********calculation 3. the percent reduction
     in heat transfer rate if the flow rate is reduced
      by 50\% and the value of U varies as mass flow to
         the 0.8 power, with the same inlet temperature
       conditions
56
57 // finally, we examine the effect of reducing the
     flow rate by 50 percent coupled with reduction in
```

```
overall heat-transfer coefficient under the
      assumption that U varies as m_dot^(0.8) or,
      correspondingly, as Cmin<sup>(0.8)</sup>
58 // still keeping the area constant, we would find
      that NTU varies as N = U*A/Cmin ~ C^{(0.8)}*C^{(-1)}
      = C^{(-0.2)}
59 // our new value of N under these conditions would
      be
60 \text{ N1} = 0.8*(\text{Cmin/Cc})^{(-0.2)};
61 // inserting this value in equation (b) above for
      the effectiveness
62 E1 = 1 - \exp(N1^{(0.22)} * (\exp(-N1^{(0.78)}) - 1));
63 // the corresponding temperature difference in each
      fluid is
64 dT = E1*(Ta1-Ta2); // [degree celsius]
65 // the heat transfer is calculated as
66 \text{ q1} = \text{Cmin}*\text{dT}; // [W]
67 printf("\n\n the percent reduction in heat transfer
      is \%f ",(q-q1)*100/q);
```

Scilab code Exa 10.16 heat transfer coefficient in compact exchanger

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.16\n\n\n");
4 // heat-transfer coefficient in compact exchanger
5 // Example 10.16 (page no.-556-557)
6 // solution
7
8 p = 101325; // [Pa] pressure of air
9 T = 300; // [K] temperature of entering air
10 u = 15; // [m/s] velocity of air
11 // we obtain the air properties from table A-5(page no.-607)
12 rho = 1.1774; // [kg/cubic meter] density of air
```

```
13 Cp = 1005.7; // [J/kg degree celsius] specific heat
      of air
14 mu = 1.983*10^{(-5)}; // [kg/m s] viscosity of air
15 Pr = 0.708; // prandtl number
16 // from figure 10-19(page no.-557) we have
17 \text{ Ac_by_A} = 0.697;
18 \text{ sigma} = Ac_by_A;
19 Dh = 3.597*10^{(-3)}; // [m]
20 // the mass velocity is thus
21 G = rho*u/sigma; // [kg/square meter s]
22 // and the reynolds number is
23 Re = Dh*G/mu;
24 // from figure 10-19 (page no. -557) we can read
25 \text{ St_into_Pr_exp_2_by_3} = 0.0036;
26 // and the heat transfer coefficient is
27 h = St_into_Pr_exp_2_by_3*G*Cp*(Pr)^(-2/3); // [W/]
      square meter degree celsius]
28 printf ("heat-transfer coefficient is %f W/square
      meter degree celsius",h);
```

Scilab code Exa 10.17 transient response of thermal energy storage system

```
11 // properties of the rock are:
12 rho_r = 1281.4; // [kg/cubic meter]
13 Cr = 0.880; // [kJ/kg degree celsius]
14 kr = 0.87; // [W/m degree celsius]
15 Ti = 5; // [degree celsius] initial temperature of
      rock bed
16 Ta = 40; // [degree celsius] air temperature
17 Tinf = Ta; // [degree celsius]
18 p = 101.325; // [kPa] pressure of air
19 Ts = 5; // [degree celsius] surrounding temperature
20 v1 = 0.3; // [m/s] inlet velocity 1
21 v2 = 0.9; // [m/s] inlet velocity 2
22 Cpa = 1.004; // [kJ/kg degree celsius]
23 R = 0.287; // [kJ/kg K] universal gas constant
24 // it can be seen that the axial energy conduction
      is small compared to the mass energy transport.
25 // for a 35 degree celsius temperature difference
     over a 0.6 length
26 \, dx = 1/5; // [m]
27 \text{ q\_cond} = \text{kr*A*(Ta-Ti)/dx;} // [W]
                                                        ( a
28 // the density of air at 40 degree celsius
29 rho_a = p/(R*(Ta+273));// [kg/cubic meter]
                                            (b)
30 // and the mass flow rate at 0.3 m/s is
31 mdot_a = rho_a*A*v1; // [kg/s]
      (c)
32 // the corresponding energy transport for a
     temperature difference of 35 degree celsius is
33 q = mdot_a*Cpa*(Ta-Ti); // [kW]
34 // and this is much larger than the value in
      equation (a).
35 // we now write an energy balance for one of the
      axial nodes as
```

```
36 // energy transported in - energy transported out -
      energy lost to surroundings = rate of energy
      accumulation of node
37 // \text{ or } \text{mdot}_a * \text{Cpa} * (\text{Tm}_o^(t) - \text{Tm}^(t)) - (\text{Tm}^(t) - \text{Tinf}) * P
      *dx/Rinf = rho_r*Cr*dVr*(Tm^(t+1)-Tm^(t))/dt
                               (e)
38 // where the exit temperature from node m is assumed
       to be the rock temperatre of that node(Tm^{\hat{}}(t)).
      equation (e) may be solved to give
39 / Tm^{(t+1)} = F*mdot_a*Cpa*Tm_o^{(t)} + [1-F*(mdot_a*
      Cpa-P*dx/Rinf) ]*Tm^(t) + F*P*dx*Tinf/Rinf
                               (f)
40 // where
41 //
                 F = dt/(rho_r*Cr*dVr)
42 // here P is perimeter and dx is the increment.
43 P = 4*1.5; // [m]
44 // the stability requirement is such that the
      coefficient on the Tm<sup>(t)</sup> terms cannot be
      negative. using dx = 0.6m, we find that the
      maximum value of
45 \, dx = 0.6; // [m]
46 \text{ Fmax} = 6.4495*10^{(-4)};
47 // which yields a maximum time increment of
48 \text{ tmax} = 0.54176; // [h]
49 // with a velocity of 0.9 m/s the maximum time
      increment for stability is
50 \text{ tmax_v2} = 0.1922; // [h]
51 // for the calculations we select the following
      values of dt with the resultant values of F:
52
53 // \text{ for v1}
54 \text{ dt1} = 0.2; // [h]
55 	ext{ F1} = 2.38095*10^{(-4)};
56 // for v2
57 \text{ dt2} = 0.1; // [h]
58 	ext{ F2} = 1.190476*10^{-4};
59
60 // with the appropriate properties and these values
```

```
inserted into equation (f) there results
61 // for v1
62 // \text{Tm}^{(t+1)} = \text{F1}*\text{mdot}_a*\text{Cpa}*\text{Tm}_o^{(t)} + [1-\text{F1}*(\text{mdot}_a)]
                   *Cpa+P*dx/Rinf) ]*Tm^(t) + F1*P*dx*Tinf/Rinf
                                                                                  (g)
63 // for v2
64 // \text{Tm}(t+1) = \text{F2}*\text{mdot}_a*\text{Cpa}*\text{Tm}_o(t) + [1-\text{F2}*(\text{mdot}_a)]
                   *Cpa+P*dx/Rinf)]*Tm^(t) + F2*P*dx*Tinf/Rinf
                                                                                 (h)
65
       // the energy storage relative to 5 degree celsius
                  can then be calculated from
67 E_t = 0;
68 i = 1;
69 \text{ T1} = 40;
70 \text{ T2} = 5;
71 \quad T3 = 5;
72 \quad T4 = 5;
73 	 T5 = 5;
74
                      for i = 1:100
                      T2 = (F2*mdot_a*Cpa*1000*T1 + [1-F2*(mdot_a*Cpa)]
75
                                *1000-P*dx/Rinf)]*T2 + F2*P*dx*Tinf/Rinf);
                       T3 = (F2*mdot_a*Cpa*1000*T2 + [1-F2*(mdot_a*Cpa)]
76
                                *1000-P*dx/Rinf)]*T3 + F2*P*dx*Tinf/Rinf);
                       T4 = (F2*mdot_a*Cpa*1000*T3 + [1-F2*(mdot_a*Cpa)]
77
                                *1000-P*dx/Rinf)]*T4 + F2*P*dx*Tinf/Rinf);
                       T5 = (F2*mdot_a*Cpa*1000*T4 + [1-F2*(mdot_a*Cpa)]
78
                                *1000-P*dx/Rinf)]*T5 + F2*P*dx*Tinf/Rinf);
79
                       Temp(i,:) = [T1 T2 T3 T4 T5];
                       E_t = (dt1/F1)*[(T1-5)+(T2-5)+(T3-5)+(T4-5)+(T5-5)+(T4-5)+(T5-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5)+(T4-5
80
                                -5)];
                       val(i) = i;
81
                       val1(i) = E_t;
82
83
                       end
84
85 E_t = 0;
86 i = 1;
87 \text{ T1} = 40;
```

```
88 T2 = 5;
89 \quad T3 = 5;
90 	ext{ T4 = 5};
91 	 T5 = 5;
92
        for i = 1:100
        T2 = (F1*mdot_a*Cpa*1000*T1 + [1-F1*(mdot_a*Cpa)]
93
           *1000-P*dx/Rinf)]*T2 + F1*P*dx*Tinf/Rinf);
        T3 = (F1*mdot_a*Cpa*1000*T2 + [1-F1*(mdot_a*Cpa)]
94
           *1000-P*dx/Rinf)]*T3 + F1*P*dx*Tinf/Rinf);
        T4 = (F1*mdot_a*Cpa*1000*T3 + [1-F1*(mdot_a*Cpa)]
95
           *1000-P*dx/Rinf)]*T4 + F1*P*dx*Tinf/Rinf);
        T5 = (F1*mdot_a*Cpa*1000*T4 + [1-F1*(mdot_a*Cpa*1000*T4)]
96
           *1000-P*dx/Rinf)]*T5 + F1*P*dx*Tinf/Rinf);
        Temp(i,:) = [T1 T2 T3 T4 T5];
97
        E_t = (dt1/F1)*[(T1-5)+(T2-5)+(T3-5)+(T4-5)+(T5-5)]
98
           -5)];
        val2(i) = i;
99
100
        val3(i) = E_t;
101
        end
102 plot(val, val1, val2, val3);
103 legend("v = 0.3 \text{m/s}","v = 0.9 \text{m/s}");
104 xlabel("time(h)");
105 ylabel("E(t) kJ");
106 printf("the result of the calculations are shown in
       the accompanying figure");
```

Scilab code Exa 10.18 variable properties analysis of a duct heater

```
1 clear;
2 clc;
3 printf("\t\tExample Number 10.18\n\n\n");
4 // variable-properties analysis of a duct heater
5 // Example 10.18 (page no.-562-564)
6 // solution
7
```

```
8 d = 0.3; // [m] diameter of duct
9 Tma = 700; // [K] temperature of hot air
10 E = 0.6; // emissivity of outside duct surface
11 Tinf = 20+273; // [K] room temperature
12 // air properties at 700 K
13 rho = 0.5030; // [kg/cubic meter] density of air
14 mu = 3.332*10^(-5); // [kg/m s] viscosity of air
15 k = 0.05230; // [W/m degree celsius] heat transfer
      coefficient
16 Pr = 0.684; // prandtl no. of air
17 A = \%pi*d^(2)/4;// [square meter] area of duct
18 sigma = 5.669*10^{(-8)}; // [W/square meter K<sup>(4)</sup>]
19 P = \%pi*d; // [m]
20 Cp = 1083.5; // [J/kg degree celsius]
21 // this is a problem where a numerical solution must
       be employed.
22 // we choose a typical section of the duct with
      length dx and perimeter P as shown inn figure
      example 10-18A (page no. -562) and make the energy
      balances.
23 // we assume that resistance of the duct wall is
      negligible.
24 // inside the duct the energy balance is
25 // \text{mdot}_a * \text{Cp} * \text{Tma} = \text{hi} * \text{P} * \text{dx} * (\text{Tma-Tmw}) + \text{mdot}_a * \text{Cp} *
      Tm_po_a
                               (a)
26 // where hi is the convection heat transfer
      coefficient on the inside which may be calculated
       from (the flow is turbulent)
27 // \text{Nu} = \text{hi}*d/k = 0.023*Re_d^(0.8)*Pr^(0.3)
                                    (b)
28 // with the properties evaluated at the bulk
      temperature of air (Tma). the energy balance for
      the heat flow through the wall is
29 // qconv_i = qconv_o + qrad_o
30 // or, by using convection coefficients and
      radiation terms per unit area,
31 // hi*(Tma-Tmw) = hc*(Tmw-Tinf)+sigma*E*(Tmw^(4)-
      Tinf^{(4)}
                               (c)
```

```
32 // where the outside convection coefficient can be
       calculated from the free convection relation
33 // hc = 0.27*((Tmw-Tinf)/d)^(1/4)
                                                    (d)
34 // inserting this relation in equation (c) gives
35 // hi*(Tma-Tmw) = 0.27*(Tmw-Tinf)^(5/4)/d^(1/4)+
      \operatorname{sigma} *E * (\operatorname{Tmw}^{(4)} - \operatorname{Tinf}^{(4)})
                                                        (e)
36 // equation (a) may be solved for Tm_po_a to give
37 // \text{Tm_po_a} = (1 - \text{hi} * P * \text{dx} / (\text{mdot_a} * \text{Cp})) \text{-m} * \text{Tma} + (\text{hi} * P * \text{ma})
      dx/(mdot_a*Cp))_m*Tmw
38
39 // for
40 x = 180;
41 mdot_a = [0.14 \ 0.45 \ 0.68]; // [kg/s]
42 \text{ for i} = 1:3
43
44 v = mdot_a(i)/(A*rho); // [m/s]
45 \text{ Re_d} = d*v*rho/mu;
46 hi = k*0.023*Re_d^(0.8)*Pr^(0.3)/d; | W/square
       meter degree celsius]
47
48
49 \quad for \quad dx = 1:1:179
        for Tmw = 295:1:715
50
             Z = (hi/dx)*(Tma-Tmw)-0.27*(Tmw-Tinf)^(5/4)/
51
                d^(1/4)-sigma*E*(Tmw^(4)-Tinf^(4));
             if (Z>0 & Z<40) then
52
                  Tmw_new = Tmw;
53
54
             end
55
        end
56
        for Tm_po_a = 275:1:715
57
             X = Tm_po_a - (1 - (hi/dx) *P*dx/(mdot_a(i) *Cp)) *
                Tmw_new + ((hi/dx)*P*dx/(mdot_a(i)*Cp))*
                Tmw_new;
58
             if (X>0 & X<5) then
                  Tm_po_a_new = Tm_po_a;
59
60
             end
61
        end
```

```
62
       q_by_A = (hi/dx)*(Tma-Tmw_new); // [W/square]
          meter]
       val1(dx,i) = q_by_A;
63
       val(dx) = dx;
64
       val2(dx,i) = Tmw_new;
65
66
       val3(dx,i) = Tm_po_a_new;
67 end
68 end
69 scf(1);
70 plot(val, val1(:,1), val, val1(:,2), val, val1(:,3));
71 legend("mdot_a = 0.14", "mdot_a = 0.45", "mdot_a = 0.68");
72 xlabel("Duct Length x,m");
73 ylabel("Local Heat Flux q / A,W / m^2");
74 xgrid();
75 title("Heat Flux");
76
77 scf(2);
78 plot(val, val2(:,1), val, val2(:,2), val, val2(:,3));
79 legend("Tw=0.14", "Tw=0.45", "Tw=0.68");
80 xlabel("Duct Length x,m");
81 ylabel("Local Wall Temperature Tw K");
82 xgrid();
83 title("Temperature Profile");
84
85 scf(3);
86 plot(val, val3(:,1), val, val3(:,2), val, val3(:,3));
87 legend("Ta=0.14", "Ta=0.45", "Ta=0.68");
88 xlabel("Duct Length x,m");
89 ylabel("Local Air Temperature Ta K");
90 xgrid();
91 title("Temperature Profile");
92 printf("plots are shown as :");
```

Chapter 11

Mass Transfer

Scilab code Exa 11.1 diffusion coefficient for co2

```
1 clear;
2 clc;
3 printf("\t\tExample Number 11.1\n\n");
4 // diffusion coefficient for co2
5 // Example 11.1(page no.-583)
6 // solution
8 T = 25+273.15; // [K] temperature of air
9 Vco2 = 34.0; // molecular volume of co2
10 Vair = 29.0; // molecular volume of air
11 Mco2 = 44; // molecular weight of <math>co2
12 Mair = 28.9; // molecular weight of air
13 P = 1.01325*10^{(5)}; // [Pa] atmospheric pressure
14 // using equation (11-2)
15 D = 435.7*T^(1.5)*(((1/Mco2)+(1/Mair))^(1/2))/(P*(
     Vco2^(1/3) + Vair^(1/3))^(2);
16 printf ("value of diffusion coefficient for co2 in
      air is %f square centimeter/s",D);
```

Scilab code Exa 11.2 diffusion coefficient for co2

```
1 clear;
2 clc;
3 printf("\t\tExample Number 11.2\n\n");
4 // diffusion coefficient for co2
5 // Example 11.2(page no.-586-587)
6 // solution
8 T = 25+273.15; // [K] temperature of air
9 p = 1.01325*10^(5);// [Pa] atmospheric pressure
10 pw1 = 3166.7618901; // [Pa] partial pressure at the
     bottom of test tube
11 pw2 = 0; // [Pa] partial pressure at the top of test
     tube
12 pa1 = p-pw1;//[Pa]
13 pa2 = p-pw2; // [Pa]
14 D = .256*10^(-4); // [square meter/s] diffusion
      coefficient
15 Mw = 18; // [g] molecular weight of water
16 A = 22*((5*10^{(-3)})^{(2)})/7; // [square meter] area of
       test tube
17 R = 8314; // [J/mol K] gas constant
18 // using equation (11-16)
19 mw = (D*p*Mw*A/(R*T*0.15))*log(pa2/pa1); // mass flow
20 printf(" mass flow rate is \%e \text{ kg/s}", mw);
```

Scilab code Exa 11.3 Wet bulb temperature

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 11.3\n\n\n");
4 // Wet-bulb temperature
5 // Example 11.3(page no.-590-591)
```

```
6 // solution
8 Pg = 2107; // [Pa] from steam table at 18.3 degree
      celcius
9 \text{ Pw} = \text{Pg}*18; // [Pa]
10 Rw = 8315; // [J/mol K] gas constant
11 Tw = 273.15+18.3; // [K]
12 RHOw = Pw/(Rw*Tw); // [kg/cubic meter]
13 Cw = RHOw; // [kg/cubic meter]
14 RHOinf = 0; // since the free stream is dry air
15 Cinf = 0;
16 P = 1.01325*10^{(5)}; // [Pa]
17 R = 287; // [ J /kg
18 T = Tw; // [K]
19 RHO = P/(R*T); // [kg/cubic meter]
20 Cp = 1004; // [J/kg degree celsius]
21 Le = 0.845;
22 Hfg = 2.456*10^{(6)}; // [J/kg]
23 // now using equation (11-31)
24 Tinf = (((Cw-Cinf)*Hfg)/(RHO*Cp*(Le^(2/3))))+Tw;//
      K
25 Tin = Tinf-273.15; // [degree celsius]
26 printf ("temperature of dry air is %f degree celsius"
      , Tin);
27 printf("\n\n these calculations are now recalculated
       the density at the arithmetic-average
      temperature between wall and free-stream
      conditions");
28 printf("\n\n with this adjustments these results are
      RHO = 1.143 \text{ kg/m}^{\circ}(3) and Tinf = 55.8 \text{ degree}
      celcius");
```

Scilab code Exa 11.4 relative humidity of air stream

```
1 clear;
```

```
2 clc;
3 printf("\t\tExample Number 11.4 \ln n");
4 // relative humidity of air stream
5 // Example 11.4(page no.-591)
6 // solution
8 // these data were taken from previous example
9 Rho = 1.212; // [kg/cubic meter]
10 Cp = 1004; // [J/kg]
11 Le = 0.845;
12 Tw = 18.3; // [degree celsius]
13 Tinf = 32.2; // [degree celsius]
14 Rhow = 0.015666; // [kg/cubic meter]
15 Cw = Rhow; // [kg/cubic meter]
16 Hfg = 2.456*10^{(6)}; // [J/kg]
17 // \text{ we use eqn } 11-31
18 Cinf = Cw-(Rho*Cp*Le^(2/3)*(Tinf-Tw)/Hfg);//[kg/
      cubic meter]
19 Rhoinf = Cinf; // [kg/cubic meter]
20 Rhog = 0.0342; // [kg/cubic meter]
21 \text{ RH} = (Rhoinf/Rhog)*100;
22 printf (" relative humidity is therefore %f
      percentage", RH);
```

Scilab code Exa 11.5 water evaporation rate

```
1 clear;
2 clc;
3 printf("\t\t\tExample Number 11.5\n\n\n");
4 // water evaporation rate
5 // Example 11.5(page no.-593-594)
6 // solution
7
8 Ta = 38+273; // [K] temperature of atmospheric air
9 RH = 0.30; // relative humidity
```

```
10 u = 10; // [mi/h] mean wind speed
11 R = 0.287; // universal gas constant
12 Dw = 0.256*10^(-4); // [square meter/s] from table A
      -8 (page no. -610)
13 rho_w = 1000; // [kg/cubic meter]
14 // for this calculation we can make use of equation
     (11-36). from thermodynamic steam tables
15 p_g = 6.545; // [kPa] at 38 degree celsius
16 p_s = p_g; // [kPa]
17 p_w = RH*p_s; // [kPa]
18 p_s = 1.933; // [in Hg]
19 p_w = 0.580; // [in Hg]
20 // also
21 u_bar = u*24; // [mi/day]
22 // equation (11-36) yields, with the application of
      the 0.7 factor
23 E_{1p} = 0.7*(0.37+0.0041*u_bar)*(p_s-p_w)^(0.88); // [
      in/day|
24 \text{ E_lp} = \text{E_lp*2.54/100; // [m/day]}
25 // noting that standard pan has the diameter of 1.2m
      , we can use the figure to calculate the mass
      evaporation rate per unit area as
26 m_dot_w_by_A = E_lp*rho_w/24; // [kg/h \text{ square meter}]
27 // as a matter of interest, we might calculate the
      molecular-diffusion rate of water vapour from
      equation (11-35), taking z1 as the 1.5m dimension
      above the standard pan.
28 	 z1 = 1.5; // [m]
29 // since
                rho = p/(R*T)
30 // equation (11-35) can be written as
31 m_dot_w_by_A1 = 0.622*Dw*p_g*3600/(R*Ta*z1); // [kg/h]
       square meter]
32 printf ("evaporation rate on the land under these
      conditions is %e kg/h square meter, m_dot_w_by_A1
     );
```