Scilab Textbook Companion for Digital Signal Processing: A Computer Based Approach by S. K. Mitra¹

Created by
Sanjeev Irny
B.Tech
Instrumentation Engineering
Shri Gurugobind Singhji Institute of Engg. & Tech.
College Teacher
Dr. B. M. Patre
Cross-Checked by

November 3, 2014

¹Funded by a grant from the National Mission on Education through ICT, http://spoken-tutorial.org/NMEICT-Intro. This Textbook Companion and Scilab codes written in it can be downloaded from the "Textbook Companion Project" section at the website http://scilab.in

Book Description

Title: Digital Signal Processing: A Computer Based Approach

Author: S. K. Mitra

Publisher: Tata McGraw - Hill Education

Edition: 3

Year: 2008

ISBN: 978-0-07-066756-3

Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

Contents

Lis	List of Scilab Codes		
2	Discreet Time Signals and Systems	8	
3	Discreet TIme Fourier Transform	22	
4	Digital Processing of Continous TIme Systems	29	
5	Finite Length Discreet Transform	33	
6	z Transform	45	
7	LTI Discreet Time systems in the Transform Domain	61	
8	Digital Filter Structures	64	
9	IIR digital filter design	69	
10	FIR digital filter design	7 4	
11	DSP Algorithm implementation	80	
12	Analysis of Finite Wordlength Effects	83	
13	Multirate DIgital Signal Processing Findamentals	84	
14	Applications of Digital Signal Processing	87	

List of Scilab Codes

Exa 2.1	Ensemble Averaging
Exa 2.2	Basic operations
Exa 2.3	Unequal length sequence
Exa 2.5	Generating symmetric parts
Exa 2.6	Energy Signal
Exa 2.7	Power Signal
Exa 2.9	Square wave generation
Exa 2.16	Linearity of accumulator
Exa 2.20	Passive system
Exa 2.22	Impulse response of Accumulator
Exa 2.26	Convolution
Exa 2.27	Convolution
Exa 2.28	Convolution
Exa 2.29	Convolution
Exa 2.30	Convolution
Exa 2.31	Stabbility of causal system
Exa 2.32	Stability of Anti causal system
Exa 2.33	Stability of a system
Exa 2.46	Cross coreation computation
Exa 3.5	DTFT computation
Exa 3.6	DTFT computation
Exa 3.7	Plotting real and imaginary part
Exa 3.10	DTFT of finite length exponential sequence 25
Exa 3.12	Plotting DTFT of exponential sequence
Exa 3.13	DTFT computation
Exa 3.14	Energy of signal
Exa 3.15	Energy of exponential sequence
Exa 4.5	Passband and Stopband ripple computation 29

Exa 4.6	Order of Analog filter	29
Exa 4.7	Order of Analog Chebyshev Filter	30
Exa 4.8	Order of Analog Lowpass Elliptic Filter	31
Exa 4.16	Design of Analof Butterworth HP Filter	31
Exa 5.1	DFT computation	33
Exa 5.2	DFT of sinusoidal sequence	33
Exa 5.3	DFT computation	34
Exa 5.4	IDFT Computation	35
Exa 5.5	DFT computation	37
Exa 5.7	Cicular convolution computation	37
Exa 5.8	Cicular convolution computation	38
Exa 5.10	Generating symmetric parts	39
Exa 5.11	Cicular convolution computation	40
Exa 5.12	Linear Convolution using DFT	41
Exa 5.14	DFT computationusing single DFT	42
Exa 5.15	DFT computation using single DFT of shorter length .	42
Exa 6.1	z Transform of causal exponential sequence	45
Exa 6.2	z transform of anticausal sequence	45
Exa 6.3	z Transform	46
Exa 6.4	z Transform	46
Exa 6.5	Z transform of causal sequence	46
Exa 6.9	z Transform	47
Exa 6.10	Rational form of z Transform from its zero and pole	
	locations	47
Exa 6.11	Inverse z Transform	48
Exa 6.12	Inverse z Transform	48
Exa 6.13	Proper fraction of Rational z Transform	49
Exa 6.14	Inverse z Transform by partial fraction expansion	50
Exa 6.15	residue computation using coefficient matching approach	50
Exa 6.16	Inverse z Transform by power series expansion	51
Exa 6.17	Coefficients of rational form	52
Exa 6.18	Inverse z Transform using long division	52
Exa 6.19	Inverse z Transform using long division	53
Exa 6.20	Inverse z Transform	53
Exa 6.22	z Transform	53
Exa 6.23	z Transform	54
Exa 6.24	sum of sequences of non overlapping ROC	54
Exa 6.25	z Transform	55

Exa 6.26	z Transform
Exa 6.27	Inverse z Transform
Exa 6.28	Enlargement of ROC by pole zero cancellation 57
Exa 6.30	Convolution
Exa 6.31	Convolution
Exa 6.33	Transfer Function of Moving Average Filter 59
Exa 6.34	Transfer function determination
Exa 7.1	Bounded real function 61
Exa 7.2	Transfer function determination
Exa 7.6	FIR Transfer function
Exa 8.1	Analysis of Cascaded lattice digital filter structure 64
Exa 8.6	Factorization of FIR Transfer Function
Exa 8.7	Factorization of IIR Transfer Function 65
Exa 8.10	Cascaded lattice realization of IIR digital Transfer Func-
	tion
Exa 8.12	Gray Markel method of realization 66
Exa 8.18	Cascaded lattice realization
Exa 9.1	Computating ripple values
Exa 9.2	conversion of bandedged frequencies to Normalized dig-
	ital frequencies
Exa 9.3	Design of HP Digital Filter
Exa 9.6	Changing passband edge frequencies to LP IIR digital
	frequencies
Exa 9.7	Design of HP IIR Digital Filter from LP Digital Filter 72
Exa 9.12	Minimum order of Type 2 Chebyshev HP IIR digital
	filter
Exa 10.1	Kaiser formula
Exa 10.2	Bellenger formula
Exa 10.3	Hermann formula
Exa 10.4	Order Estimation
Exa 10.6	Filter length estimation for window based design 77
Exa 10.7	Order Estimation
Exa 10.8	Kaiser window
Exa 11.3	Reconstruction of Transfer function from Impulse re-
	sponse coefficients
Exa 11.11	Cascaded lattice Filter structure 81
Exa 12.3	Signal to Quantisation Noise Ratio
Exa 13.1	Up sampling operation

Exa 13.2	Down sampling operation	85
Exa 13.6	Decimator Computation complexity	85
Exa 14.1	Effect of DFT length	87
Exa 14.2	Effect of DFT length	88

Chapter 2

Discreet Time Signals and Systems

Scilab code Exa 2.1 Ensemble Averaging

```
1 //EXAMPLE 2.1
2 //Ensemble averaging
3 clear;
4 clc;
5 n = 1:50;
6 clf();
7 figure(0)
8 a=gca();
9 a.x_location="origin";
10 a.y_location="origin";
11
     for i =1:length(n)
12
          s(i)=2*n(i)*((0.9)^n(i));
          d(i)=(-0.1)^n(i); //arbitrary noise
13
             signal.
14
     end
15
16 M=length(n);
17
18
  for i = 1:M
```

Scilab code Exa 2.2 Basic operations

```
//EXAMPLE 2.2 , BASIC OPERATIONS.
clear;
clc;
c=[3.2 41 36 -9.5 0];
disp(c,'c=');
d=[1.7 -0.5 0 0.8 1];
disp(d,'d=');
w1=c.*d;
disp(w1,'The product of two input vectors is =');
w2=c+d;
disp(w2,'The addition of two input vectors is =');
w3=3.5*c;
disp(w3,'The scaling of first input vector is =');
```

Scilab code Exa 2.3 Unequal length sequence

```
1 //EXAMPLE 2.3, Basic ops on unequal length sequence
2 clear;
3 clc;
4 c=[3.2 41 36 -9.5 0];
```

```
5 \text{ disp(c,'c = ');}
6 g = [-21 1.5 3];
7 \text{ disp}(g, g' = g');
8 a=length(g);
9 b=length(c);
10 i = 0;
        while(i < b - a)</pre>
11
12
             g(b-i)=0;
13
             i=i+1;
14
        end
15 \text{ w4=g.*c};
16 disp(w4, 'The product of two sequences is =');
17 w5=c+g;
18 disp(w5, 'The addition of two sequences is =');
```

Scilab code Exa 2.5 Generating symmetric parts

```
1 //EXAMPLE 2.5, Conjugate-Antisymmetric & Conjugate-
     symmetric parts of Sequence
2 clc;
3 clear;
4 g = [0, 1+\%i*4, -2+\%i*3, 4-\%i*2, -5-\%i*6, -\%i*2, 3];
5 \text{ disp}(g, g' = g')
                         //Conjugate of g;
6 g1=conj(g);
7 disp(g1,conj(g));
8 a=length(g);
9 for i=1:a
10
       g2(1,i)=g1(a-i+1);
11 end
12
                        //Conjugate-Symmetric part
13 gcs = (g+g2)/2
14 disp(gcs, 'The Conjugate symmetric part is =');
15 gcas=(g-g2)/2; //Conjugate-Antisymmetric part
16 disp(gcas, 'The Conjugate antisymmetric part is =');
```

Scilab code Exa 2.6 Energy Signal

```
//EXAMPLE 2.6, Energy Signal
3 clear;
4 clc;
5 n = -5:5;
6 for i =1:length ( n )
    if(n(i)>=1)
    h(i)=1/n(i);
8
9
    else
10
    h(i)=0;
11
    end
12 end
13
14 Sum = 0;
15 N=1:10000;
16
     for i=1:length(N)
17
     h(i) = (1/N(i))^2;
18
     end
19
20 Energy = sum(h);
21
22
    if (Energy<%inf ) then</pre>
     disp ('Energy Signal');
23
     disp(Energy, 'Energy of signal = ');
24
     else
25
26
          (Energy/length(N)<%inf ) then
     disp ('Power Signal');
27
28
29
     else
     disp ('Niether Energy nor Power Signal');
30
31
     end
32
    end
```

Scilab code Exa 2.7 Power Signal

```
1 //EXAMPLE 2.7, Example of Power signal
2 clear;
3 clc;
4
5 \text{ Sum} = 0;
6 N=1:10000;
       for i=1:length(N)
8
        h1 = 3*((-1)^i);
9
        h=h1^2;
10
       end
11
12 Energy = sum(h);
         (Energy/(2*(length(N))+1)<%inf) then
13
     disp ('Power Signal');
14
     disp(Energy/2, 'Power Signal = ');
15
16
     else
17
     disp ('Not a Power Signal');
18
     end
```

Scilab code Exa 2.9 Square wave generation

```
1 //EXAMPLE 2.9, Generation of a Square wave sequence:
2 clc;
3 clear;
4 clf();
5 a=gca();
6 figure(0);
7 a.x_location="origin";
8 x=[0:1:80];
9 y1=sin(x*.05*%pi);
```

```
10  y2=sin(x*.15*%pi);
11  y3=sin(x*.25*%pi);
12  y4=y1+y2/3+y3/5;
13  plot2d3(x,y4,2)
14  plot(x,y4,'r.')
15  xtitle('Approximate Square wave','x','y4');
16  a.children.children.thickness=3;
```

Scilab code Exa 2.16 Linearity of accumulator

```
1 //EXAMPLE 2.16,
2 clear;
3 clc;
4 //Given input sequence = \begin{bmatrix} 3 & 4 & 5 \end{bmatrix}
5 x = [0 3 4 5 0];
6 disp([3 4 5], 'Input sequence = ')
7 //determining median filter
8 // first sequence
9 \text{ for } k=2:4
10
            x(k)>x(k-1) & x(k+1)>x(k-1) & x(k+1)>x(k)
              y(k-1)=x(k);
11
12
         else
              x(k-1)>x(k+1) & x(k)>x(k+1) & x(k)>x(k-1)
13
14
              y(k-1)=x(k-1);
15
        end
16 end
17 disp(y', 'The Median Filter of the given input is =')
```

Scilab code Exa 2.20 Passive system

```
1 //EXAMPLE 2.20, Passive or lossless system. 2 clear;
```

```
3 clc;
4 a=input("any value of a less than or equal to one")
5 n = -10:1:10;
6
   x=n;
7
   y=a*n;
    S=0;
    for i=1:length(n)
9
        S=S+y^2;
10
11
    end
12
13
    if a<1 then
        disp('the system is passive')
14
15
    else
16
17
        a==1
        disp('the system is lossless')
18
19
20
    end
```

Scilab code Exa 2.22 Impulse response of Accumulator

```
//EXAMPLE 2.22, impulse response of accumulator

clear;
clc;
d=[1];
t=-1:.01:1;
h=0;
clf();
figure(0);
a=gca();
a.x_location="origin";

for i=1:length(t)
if t(i)<0</pre>
```

```
15
         h=0;
16
       else
17
           h=d;
           plot2d3(i-101,h)
18
19
            plot(i-101,h,'.r')
20
            xtitle('Impulse Response of accumulator', 't'
               , 'Y');
            a.children.children.thickness=1;
21
22
            a.children.children.foreground=2;
23
       end
24 end
25 disp(h, 'The impulse response of Accumulator is =')
```

Scilab code Exa 2.26 Convolution

```
1 //EXAMPLE 2.26, convolution of x & h
2 x=[-2 0 1 -1 3];
3 disp(x,'x = ');
4 h=[1 2 0 -1];
5 disp(h,'h = ');
6 n=0:7;
7 y=convol(x,h);
8 disp(y,'The convolution of the two inputs is :')
```

Scilab code Exa 2.27 Convolution

```
7 clf();
8 figure(0);
9 a=gca();
10 a.x_location="origin";
11 x = c^n;
12 subplot(2,2,1);
13 plot2d3(n,x,2);
14 plot(n,x,'.r');
15 xtitle('', 'n', 'x');
16 h = b^n;
17 subplot(2,2,2);
18 plot2d3(n,h,2)
19 plot(n,h,'.r')
20 xtitle('', 'n', 'h');
21 N = 0:.5:10;
22 y = convol (x , h);
23 subplot (2,2,3);
24 plot2d3(N,y,2)
25 plot(N,y,'.r')
26 xtitle('convol(x,h)', 'n', 'y');
27 disp(y, 'Convolution of the two exponential sequences
       is = ')
```

Scilab code Exa 2.28 Convolution

```
1 //EXAMPLE 2.28, graphical representation of
        convolution of x & h.
2 clear;
3 clc;
4 x=[-2 0 1 -1 3];
5 disp(x, 'x');
6 h=[1 2 0 -1];
7 disp(h, 'h');
8 n=0:7;
9 y=convol(x,h);
```

```
disp(y,'convolution = ');
clf();
figure(0);
a=gca();
a.x_location="origin";
a.y_location="origin";
plot2d3(n,y)
plot(n,y,'r.')
xtitle('convolution','n','Y');
a.children.children.thickness=2;
a.children.children.foreground=2;
```

Scilab code Exa 2.29 Convolution

```
1 //Example 2.29, Convolution using Tabular method.
2 clear;
3 clc;
4 x = [-2 \ 0 \ 1 \ -1 \ 3];
5 h = [1 2 0 -1];
6 q=length(x);
7 w=length(h);
8 z=q+w-1;
9 y0=0;
10 for i=1:z;
       y(i) = 0;
11
12
       for k=1:i;
13
            if k>q
14
                 x(k) = 0;
15
            else
                 if (i-k+1)>w
16
                     h(i-k+1)=0;
17
18
                 else
                  y(i) = y(i) + x(k)*h(i-k+1);
19
20
                 end
21
            end
```

```
22 end
23 end
24 disp(y', 'The Convolution of the two sequences is =')
```

Scilab code Exa 2.30 Convolution

```
1 //EXAMPLE 2.30
2 //Convolution of two sided sequences
3 clear;
4 clc;
5 g = [3 -2 4]; // originating at n = -1
6 h=[4 \ 2 \ -1];//originating at n=0
7 q=length(g);
8 \text{ w=length(h)};
9 z = q + w - 1;
10 y0=0;
11 for i=1:z;
        y(i) = 0;
12
        for k=1:i;
13
14
            if k>q
15
                 g(k)=0;
16
            else
17
                 if (i-k+1)>w
18
                      h(i-k+1)=0;
19
                 else
20
                  y(i) = y(i) + g(k)*h(i-k+1);
21
                 end
22
            end
23
        end
24 end
25 \quad n = -1 : z - 2;
26 disp(y, 'The Convolution of the two sequences is =')
27 clf();
28 a=gca();
29 figure(0);
```

```
30 a.x_location="origin";

31 plot2d3(n,y,2);

32 plot(n,y,'r.');

33 xtitle('convolution','n','y');
```

Scilab code Exa 2.31 Stabbility of causal system

```
1 //EXAMPLE 2.31, Stability for causal system.
2 //h[i]=impulse response of LTI system.
3 clear;
4 clc;
5 n = -5:0.001:5;
6 a=0.6;
8 for i=1:length(n)
9
       if (n(i)<0)
10
            h(i)=0;
11
       else
            h(i) = abs(a^n(i));
12
13
14
       end
15 end
16 S = sum(h);
17 if(S<%inf)
18
       disp('BIBO stable system');
19 else
       disp('BIBO unstable system');
20
21
22 \text{ end}
```

Scilab code Exa 2.32 Stability of Anti causal system

```
1 //EXAMPLE2.32 Stability for anti-Causal system.
```

```
2 //h[i]=impulse response of LTI system.
3 clear;
4 clc;
5 n = -5:1/1000:5;
6 a=5;
7 for i=1:length(n)
       if (n(i)>-1)
           h(i) = 0;
9
10
       else
           h(i)=a^n(i);
11
12
           S = sum(h);
13
       end
14 end
15
16 if(S<%inf)
17
       disp('BIBO stable system');
18 else
19
       disp('BIBO unstable system');
20
21 end
```

Scilab code Exa 2.33 Stability of a system

```
//EXAMPLE 2.33 , stability of finite impulse response
.
//h[i]=impulse response of LTI system.
clear;
clc;
n= -5:1/100:5;
a= input('value of a');
N1=input('lower limit');
N2=input('upper limit');
for i=1:length(a)
if (n(i)<N1 & n(i)>N2)
h(i)=0;
```

```
12
      else
13
         h(i)=a^n(i);
         S=sum(h);
14
15
      end
16 \text{ end}
17
18 if(S<%inf)
      19
        N1, N2! = \% inf
20 else
      disp('BIBO unstable system');
21
22
23 end
```

Scilab code Exa 2.46 Cross coreation computation

```
//EXAMPLE 2.46, Cross corelation Computation.
// Given two finite length sequence.x[n],y[n]:
clear;
clc;
x=[1 3 -2 1 2 -1 4 4 2];
disp(x,'x');
y=[2 -1 4 1 -2 3];
disp(y,'y');
//Cross corelation rxy[n]:
rxy=convol(x,mtlb_fliplr(y));
disp(rxy,'The Cross-Corelation Operation of the Inputs is =')
```

Chapter 3

Discreet TIme Fourier Transform

Scilab code Exa 3.5 DTFT computation

```
1 //EXAMPLE 3.5
2 //DTFT of unit sample sequence
3 clc;
4 clear;
5 / a = 0.5;
6 n=0:9;
7 x = [1, zeros(1,9)];
8 \operatorname{disp}(x, x[n] = ')
10 \text{ K} = 4;
11 k = 0:4/1000:4;
12 \ W = k*2*\%pi/K;
13 X = (x) * exp(%i*n'*W);
14 \operatorname{disp}(X, 'DTFT, x[n] \longrightarrow ')
15 \text{ X}_{mag}
           = abs(X);
16 X_phase = phasemag(X); //no phase exists
17
18 figure(0);
19 plot2d3(mtlb_fliplr(W), X_mag);
```

```
20 xtitle('Magnitude plot', 'W --->', 'X_mag --->');
21 figure(1);
22 plot2d3(mtlb_fliplr(W), X_phase);
23 xtitle(' zero phase plot', 'W --->', 'X_phase --->');
```

Scilab code Exa 3.6 DTFT computation

```
1 //EXAMPLE 3.6
2 //Determine DTFT of sequence
3 //PROGRAM REQUIRES MAXIMA SCILAB TOOLBOX
4
5 clc;
6 clear;
7 //Symbolic calculation
8 Syms n w a ;
9 x1=(a^n)*exp(-\%i*n*w);
10 X1=nusum(x1,n,0,%inf);
11 disp(X1, 'DFT, X = ');
12
13 // Given:
14 a=0.5;
15 n=0:9;
16 //x[n]=a^n*u[n]
17 \text{ for } i = 0:9
18
       x(i+1) = a^i;
19 end
20 //The DTFT of the sequence
21 \text{ K} = 4;
22 k = 0:4/1000:4;
23 W = k*6*\%pi/K;
24 X = (x')*exp(%i*n'*W);
25 \quad X_mag = abs(X);
26 [X_phase,db] = phasemag(X);
27
28 clf();
```

Scilab code Exa 3.7 Plotting real and imaginary part

```
1 //EXAMPLE 3.12
2 //x[n] = ((-1)^n) *(a^n) *u[n] \dots given a = 0.5;
3
4 clc;
5 clear;
6
7 a=0.5;
8 n=0:9;
9 \text{ for } i = 0:9
       x(i+1) = (a*exp(-%i*%pi))^i;
10
11 end
12
13 //The DTFT of the sequence
14 K = 4;
15 k = 0:4/1000:4;
16 \ W = k*6*\%pi/K;
17 X = (x')*exp(%i*n'*W);
18 \, X_{mag}
          = abs(X);
19 X_phase = phasemag(X);
20
21 //PLOTTING GRAPHS FOR THE INTERVAL OF 0 TO 6*%pi
22 clf();
```

```
23 a=gca();
24 figure(0);
25 plot2d3(mtlb_fliplr(W), X_mag);
26 xtitle('Magnitude response', 'W', 'Amplitude');
27 figure(1);
28 plot2d3(mtlb_fliplr(W), X_phase);
29 xtitle('Phase response', 'W', 'X_phase, degrees');
```

Scilab code Exa 3.10 DTFT of finite length exponential sequence

```
//EXAMPLE 3.10
// DTFT of a sequence
clc;
clear;
syms a n M w;
x=a^n;
X=nusum(x*(exp(-%i*w*n)),n,0,M-1)
disp(limit(X),'The DTFT of the given sequence, X = ')
```

Scilab code Exa 3.12 Plotting DTFT of exponential sequence

```
1 //EXAMPLE 3.12
2 //x[n]=((-1)^n)*(a^n)*u[n].....given a=0.5;
3
4 clc;
5 clear;
6
7 a=0.5;
8 n=0:9;
9 for i = 0:9
10     x(i+1) = (a*exp(-%i*%pi))^i;
11 end
```

```
12
13 //The DTFT of the sequence
14 \text{ K} = 4;
15 k = 0:4/1000:4;
16 \ W = k*6*\%pi/K;
17 X = (x')*exp(%i*n'*W);
18 X_mag = abs(X);
19 X_phase = phasemag(X);
20
21 //PLOTTING GRAPHS FOR THE INTERVAL OF 0 TO 6*%pi
22 clf();
23 a=gca();
24 figure(0);
25 plot2d3(mtlb_fliplr(W), X_mag);
26 xtitle('Magnitude response', 'W', 'Amplitude');
27 figure (1);
28 plot2d3(mtlb_fliplr(W), X_phase);
29 xtitle('Phase response', 'W', 'X_phase, degrees');
```

Scilab code Exa 3.13 DTFT computation

```
1 //EXAMPLE 3.13
2
3 clc;
4 clear;
5 a=0.5;
6 n=0:9;
7 for i = 0:9
8     x(i+1) = a^i;
9 end
10 //The DTFT of the sequence
11 K = 4;
12 k = 0:4/1000:4;
13 W = k*6*%pi/K;
14 X1 = (x')*exp(%i*n'*W);
```

Scilab code Exa 3.14 Energy of signal

```
1 //EXAMPLE 3.14
2 //ENERGY OF LP DISCREET TIME SIGNAL
3 //PROGRAM REQUIRES MAXIMA SCILAB TOOLBOX
4 clc;
5 clear;
6 syms n wc w;
7 wc = input("the value of wc (less than %pi)=");
8 n = -5:0.05:5;
10 for i =0:length (n)
       hlp(i+1) = (wc/\%pi)*sinc((wc*i)/\%pi);
12
      E(i+1) = (abs(hlp(i+1)))^2;
13 end
14
15 Energy = sum(E);
16 if (Energy < %inf ) then
17
    disp ('The filter is Energy Signal');
18
     else
```

```
if (Energy/length(N)<%inf ) then
disp ('Power Signal');
else
disp ('Niether Energy nor Power Signal');
end
end
disp(Energy, 'the energy is = ');</pre>
```

Scilab code Exa 3.15 Energy of exponential sequence

```
1 //EXAMPLE 3.15
2 //ENERGY OF A SIGNAL x[n]=a^n*u[n]
3 clc;
4 clear;
5 a=0.5;
6 n=0:0.1:9.9;
7 //x[n]=a^n*u[n]
8 for i = 0:length(n)
9     x(i+1) = a^i;
10     E=(abs(x))^2;
11 end
12 Energy=sum(E);
13 disp(Energy, 'Energy of the signal = ');
```

Chapter 4

Digital Processing of Continous TIme Systems

Scilab code Exa 4.5 Passband and Stopband ripple computation

```
//EXAMPLE 4.5
//determine ripple values in db;
clc
clear;
ap = 0.01//Peak passband ripple in dB
as = 70//min. stopband attenuation in dB
dp = 1-10^-(ap/20);
ds = 10^-(as/20);
disp(dp,'dp = ');
disp(ds,'ds = ');
```

Scilab code Exa 4.6 Order of Analog filter

```
1 //EXAMPLE 4.6
2 //Order of LP filter
3 clc;
```

```
4 clear;
5 ap = 1 //Peak passband ripple in dB
6 as = 40 //min. stopband attenuation in dB
7 wp = 1000 //Hz
8 ws = 5000 //Hz
9 k = wp/ws;
10 disp(1/k, '1/k = ');
11 k1 = 1/(sqrt((10^(0.1* as)-1)/(10^(0.1*ap)-1)));
12 disp(1/k1, '1/k1 = ');
13 N=ceil(log10(sqrt((10^(0.1* as)-1)/(10^(0.1*ap)-1))) /log10(1/k));
14 disp(N, 'order of the filter is :');
```

Scilab code Exa 4.7 Order of Analog Chebyshev Filter

```
1 //EXAMPLE 4.7
2 //Determine the order of Analog Chebyshev LP filter.
3 clc;
4 clear;
5 \text{ ap} = 1 //dB
6 \text{ as} = 40 \text{ }//\text{dB}
7 \text{ wp} = 1000 //Hz
8 \text{ ws} = 5000 //Hz
9 k = wp/ws;
10 disp(1/k, '1/k = ');
11 k1 = 1/(sqrt(((10^{(0.1* as))-1})/((10^{(0.1*ap))-1)));
12 disp(1/k1, '1/k1 = ');
13 N = a\cosh(1/k1)/a\cosh(1/k);
14 disp(N, 'N = ');
15 disp('Since order of the filter is always an integer
16 disp(ceil(N), 'Order of the filter is, N = ');
```

Scilab code Exa 4.8 Order of Analog Lowpass Elliptic Filter

```
1 //EXAMPLE 4.8
2 //Determine the order of Analog Elliptic LP filter.
3 clc;
4 clear;
5 \text{ ap} = 1 //dB
6 \text{ as} = 40 //dB
7 \text{ Fp} = 1000 //Hz
8 \text{ Fs} = 5000 //Hz
9 \text{ wp} = \text{Fp*2*%pi;}
10 ws = Fs*2*\%pi;
11
12
13 k1 = 1/(sqrt((10^{(0.1* as)-1)}/(10^{(0.1*ap)-1)));
14 disp(1/k1, '1/k1 = ');
15 k = wp/ws;
16 	 k2 = sqrt(1 - (k*k));
17 disp(k2,"k2 = ");
18 po = (1 - sqrt(k2))/(2*(1 + sqrt(k2)));
19 \operatorname{disp}(po, po = ');
20 p = po +2*po^5 + 15*po^9 + 150*po^13;
21 \text{ disp}(p, p = ');
22 N = (2*log10(4/k1))/log10(1/p);
23 disp(N, 'N = ');
24 disp('Since order of the filter is always an integer
25 disp(ceil(N), 'Order of the filter is, N = ');
```

Scilab code Exa 4.16 Design of Analof Butterworth HP Filter

```
1 //EXAMPLE 4.16
2 //Design analog butterworth High pass filter
3 clc;
4 clear;
```

```
5 \text{ wp} = 4000;
6 \text{ ws} = 1000;
 7 \text{ ap} = 0.1;
8 \text{ as} = 40;
9
10 Ap=1; // assumption
11 As=(2*\%pi*wp)*Ap/(2*\%pi*ws);
12
13 N=ceil(log10(sqrt((10^(0.1* as)-1)/(10^(0.1*ap)-1)))
       /log10(As/Ap));
14 disp(N, 'order of the filter is:');
15
16 Ac = As/((10^{(0.1*as)-1)^{(1/(N*2))}};
17 disp(Ac, 'cutoff frequency = ')
18
19 // [hs, pole, zero, gain] = analpf(N, 'butt', Ac);
20
21 \text{ s=\%s};
22 \text{ hs}=1/((s + 1)*(s^2 + 0.61803*s + 1)*(s^2 + 1.61803*s)
        + 1));
23 Hs=horner(hs,s/Ac);
24 \text{ H1} = \text{numer}(\text{Hs})/0.0976514;
25 \text{ H2} = \frac{\text{denom}(Hs)}{0.0976514};
26 disp(H1/H2, 'the low pass transfer function is, HLP(s)
        = ');
27 Hs=horner(hs,Ac/s);
28 \text{ H1} = \text{numer}(\text{Hs});
29 \text{ H2} = \text{denom}(\text{Hs});
30 disp(H1/H2, 'the High pass transfer function is, HHP(s
       ) = ');
```

Chapter 5

Finite Length Discreet Transform

Scilab code Exa 5.1 DFT computation

```
//EXAMPLE 5.1
//DETERMINE DFT OF GIVEN SEQUENCE
clc;
clear;
N = input("length of sequence = ");
x = [1,zeros(1,N-1)];
disp(x,'The sequence is,x = ');
X = dft(x,0);
disp(X,'DFT of the sequence is X = ');
m = input("value of some intemediate (mth) point = ");
y = [zeros(1,m-1),1,zeros(1,N-m)];
y = dft(y,0);
disp(Y,'DFT of the sequence is Y = ');
```

Scilab code Exa 5.2 DFT of sinusoidal sequence

```
1 //EXAMPLE 5.2
2 //DFT of sinusoidal sequence
3 clc;
4 clear;
6 N = input (" input value of N ");
                 input r value ");
7 r = input("
8 n = 0:N-1;
9 x = \cos(2*\%pi*r*n/N)
10 \quad X = \mathbf{dft}(x, -1)
11 //X exisits only at n=\{r, N-r\} where X = N/2
12 clf();
13 a=gca();
14 a.x_location = "origin";
15 a.y_location = 'origin';
16 plot2d3(n,X,2);
17 a.thickness=1;
18 plot(n, X, 'r.');
19
20 xtitle('DFT', 'K -->', 'X[K] -->');
21 X = disp(X, 'DFT \text{ of } x \longrightarrow ');
```

Scilab code Exa 5.3 DFT computation

```
//EXAMPLE 5.3
//DETERMINE DFT OF GIVEN SEQUENCE

clc;
clear;
N = input("length of sequence, N = ");
M = input("M point DFT = ");
if M > N

x = [ones(1,N),zeros(1,M-N)];
disp(x,'the sequence is :');
for n=0:M-1
```

```
12
            for k=0:M-1
13
                 W(n+1,k+1) = \exp(-(\%i*2*\%pi*k/M)*n);
14
            end
15
       end
16
       X = W * x';
       disp(X, 'DFT is, X = ');
17
18 else
       disp('invalid computation');
19
20 end
21
22
23 \quad n=0:M-1;
24 clf();
25 figure (0)
26 \ a = gca();
27 plot2d3(n,x,2) // plotting the sequence
28 plot(n,x,'r.');
29 a.x_location = 'origin';
30 a.y_location = 'origin';
31 \text{ poly1} = a . children (1) . children (1) ;
32 \text{ poly1.thickness} = 2.5;
33 xtitle('original sequence', 'n', 'x[n]');
34
35 figure (1)
36 \ a = gca();
37 plot2d3(n,abs(X),2) // plotting absolute value of
      DFT of sequence
38 plot(n,abs(X),'r.');
39 a.x_location = 'origin';
40 a.y_location = 'origin';
41 \text{ poly1} = a \cdot \text{children} (1) \cdot \text{children} (1) ;
42 poly1.thickness = 2.5;
43 xtitle('magnitude plot', 'M', 'Absolute value');
```

Scilab code Exa 5.4 IDFT Computation

```
1 //EXAMPLE 5.4
2 //DETERMINE IDFT OF GIVEN SEQUENCE
3 clc;
4 clear;
5 K = input(" value of K
                                ");
6 disp('input M > K');
7 M = input("
                 value of M
                                ");
8 k1 = 0:K-1;
9 V1 = k1./K; //DFT
10 k=0:M-1;
11
12 N = length(V1);
13 V = [V1, zeros(1, M-N)];
14 v = dft(V,1); //IDFT
15
16 clf();
17 subplot (1,2,1)
18
19 a = gca();
20 plot2d3(k,real(v),2);
21 plot(k,real(v), 'r.');
22 a.x_location = 'origin';
23 a.y_location = 'origin';
24 \text{ poly1} = a . children (1) . children (1) ;
25 poly1.thickness = 2;
26 xtitle('real part', 'N', 'v');
27
28 subplot (1,2,2)
29 \ a = gca();
30 plot2d3(k,imag(v),2)
31 plot(k,imag(v),'r.');
32 a.x_location = 'origin';
33 a.y_location = 'origin';
34 \text{ poly1} = a . children (1) . children (1) ;
35 poly1.thickness = 2;
36 xtitle('imaginary part', 'N', 'v');
37 v = disp(v);
```

Scilab code Exa 5.5 DFT computation

```
1 //EXAMPLE 5.5
2 //DFT computation
3 clc;
4 clear;
6 N = 16 ;
7 r = 3 ;
8 n = 0:N-1;
9 x = \cos(2*\%pi*r*n/N)
10 X = fft(x,-1)/DFT of the sequence
11 clf();
12 \ a = gca();
13 plot2d3(n,X,2);
14 plot(n, X, 'r.')
15 a.x_location = 'origin';
16 a.y_location = 'origin';
17 poly1 = a . children (1) . children (1) ;
18 poly1.thickness = 3;
20 X = disp(real(X), 'X = ');
```

Scilab code Exa 5.7 Cicular convolution computation

```
1  //EXAMPLE 5.7
2  // Circular convolution
3  clear;
4  clc;
5  g = [1 2 0 1];
6  disp(g,'g[n] = ');
7  h = [2 2 1 1];
```

```
8 \text{ disp}(h, h[n] = ');
9 G = fft(g,-1);
10 H = fft(h, -1);
11 Y = G.*H;
12 yc = fft(Y,1);
13 \text{ n1} = 0: length(yc) - 1;
14 \text{ yl} = \text{convol}(g,h);
15 \text{ n2} = 0: length(yl)-1;
16
17 clf();
18 subplot (2,1,1)
19 a = gca();
20 plot2d3(n1,yc,2);
21 plot(n1,yc,'r.');
22 a.x_location = 'origin';
23 a.y_location = 'origin';
24 \text{ poly1} = a \cdot \text{children} (1) \cdot \text{children} (1) ;
25 poly1.thickness = 3;
26 xtitle('circular convolution', 'n', 'yc');
27
28 subplot (2,1,2)
29 \ a = gca();
30 plot2d3(n2,y1,2);
31 plot(n2,y1, 'r.');
32 a.x_location = 'origin';
33 a.y_location = 'origin';
34 \text{ poly1} = a . children (1) . children (1) ;
35 poly1.thickness = 3;
36 xtitle('linear convolution', 'n', 'yl');
37
38 disp(real(yc), "circular convolution, yc = ");
39 disp(yl, "linear convolution, yl = ");
```

Scilab code Exa 5.8 Cicular convolution computation

```
1 //EXAMPLE 5.8
2 // Cicular convolution
3 clc;
4 clear;
5 g = [1 2 0 1];
6 disp(g, g[n] = ');
7 h = [2 2 1 1];
8 \text{ disp(h,'h[n] = ');}
9 G = fft(g,-1);
10 H = fft(h, -1);
11 Y = G.*H;
12 yc = fft(Y,1);//IDFT of Y
13 disp(yc, "circular convolution, yc = ")
14 n = 0:3;
15 clf();
16 figure(0);
17 \ a = gca();
18 plot2d3(n,yc,2);
19 plot(n,yc,'r.');
20 a.x_location = 'origin';
21 a.y_location = 'origin';
22 \text{ poly1} = a . children (1) . children (1) ;
23 poly1.thickness = 3;
24 xtitle('Circular convolution', 'n', 'yc');
```

Scilab code Exa 5.10 Generating symmetric parts

```
1  //EXAMPLE 5_10
2  //conjugate symmetric & anti-symmetric parts of complex sequence
3  clear;
4  clc;
5  un=[1+%i*4,-2+%i*3,4-%i*2,-5-%i*6];
6  disp(un, 'u[n] = ');
7  u1=conj(un);
```

Scilab code Exa 5.11 Cicular convolution computation

```
1 //EXAMPLE 5.11
2 // Circular convolution using DFT
3 clc;
4 clear;
5 g = [1 2 0 1];
6 disp(g, g[n] = ');
7 h = [2 2 1 1];
8 disp(h, 'h[n] = ');
9 M = 4;
10 for n=0:M-1
11
            for k=0:M-1
12
                 W(n+1,k+1) = \exp(-(\%i*2*\%pi*k/M)*n);
13
             end
14
        end
15
       G = W*g';
       H = W*h';
16
17 \operatorname{disp}(G, 'DFT \text{ is }, G = ');
18 disp(H, 'DFT is, H = ');
19
20 Y = G . * H;
21 y=(1/4)*conj(W)*(Y);
```

Scilab code Exa 5.12 Linear Convolution using DFT

```
1 //EXAMPLE 5.12
2 //Linear convolution using Circular convolution
3 clc;
4 clear;
5 g = [1 2 0 1];
6 disp(g, g[n] = ');
7 h = [2 2 1 1];
8 \text{ disp(h,'h[n] = ');}
10 //linea convolution length = 4+4-1 = 7
11 //appending the two signals with zeros
12 g = [g, zeros(1,3)]
13 h = [h, zeros(1,3)]
14 G = fft(g, -1);
15 H = fft(h,-1);
16 Y = G.*H; //element wise multiplication
17 y = fft(Y,1); //IDFT
18
19 // Plotting linear convolution
20 n = 0:6;
21 figure(0);
22 clf();
23 \ a = gca();
24 a.x_location = 'origin';
25 a.y_location = 'origin';
26 plot2d3(n,y,2);
27 plot(n,y,'r.');
28 \text{ poly1} = a \cdot \text{children} (1) \cdot \text{children} (1) ;
29 poly1.thickness = 2;
30 xtitle('Linear convolution', 'n', 'y');
31 disp(y," linear convolution , y = ");
```

Scilab code Exa 5.14 DFT computationusing single DFT

```
1 //EXAMPLE 5.14
2 //DFT of two real sequences using one DFT
3 clear;
4 clc;
5 g = [1 2 0 1];
6 disp(g, 'g[n] = ');
7 h = [2 2 1 1];
8 disp(h, 'h[n] = ');
9 x = g + \%i.*h;
10 disp(x, 'x[n] = ');
11 X = fft(x,-1);
12 disp(X, 'The DFT, X[k] = ');
13 X1 = conj(X);
14 disp(X1, 'X*[k] = ');
15
16 for i=0:3;
       a(i+1) = pmodulo(-i,4);
17
18
       X2(i+1) = X1(a(i+1)+1);
19 end
20
21 X3 = conj(X2');
22 disp(X3, X*[<4-k>4] = ');
23 disp(0.5*(X + X3), 'G[k] = ');
24 disp((X - X3)/(2*\%i), 'H[k] = ');
```

Scilab code Exa 5.15 DFT computationusing single DFT of shorter length

```
3
4 clc;
5 clear;
6 v = [1 2 2 2 0 1 1 1];
7 \operatorname{disp}(v, '\operatorname{Length} - 8 \text{ real sequence } v[n] = ')
8 for i=1:4
        g(i)=v(2*i-1);
9
        h(i) = v(2*i);
10
11 end
12 G = fft(g,-1);
13 H = fft(h,-1);
14 M=length(v);
15 // for n=0:M-1
16
             for k=0:M-1
17
                  W(1,k+1) = \exp(-(\%i*2*\%pi*k/M)*1);
18
             end
19 / \text{end}
20 G = [G(1) G(2) G(3) G(4) G(1) G(2) G(3) G(4)];
21 H = [H(1) H(2) H(3) H(4) H(1) H(2) H(3) H(4)];
22 V = G + W.*H;
23 disp(V, 'DFt,V[k] = ');
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40 // for k = 0:3
```

```
\begin{array}{lll} 41 & // & V1(k+1) = G(k+1) + (\exp(-2*\%pi*\%i*k/8))*H(k+1) \\ & ; \\ 42 & //end \\ 43 & \\ 44 & //for & k = 4:7 \\ 45 & // & V2(k) = G(k-3) + (\exp(-2*\%pi*\%i*k/8))*H(k-3); \\ 46 & //end \\ 47 & //disp([V1,zeros(1,3)]+V2) \\ \end{array}
```

Chapter 6

z Transform

Scilab code Exa 6.1 z Transform of causal exponential sequence

```
1 //EXAMPLE 6.1
2 //Z-Transform of causal sequence
3 clc;
4 clear;
5 syms n a z;
6 x = a^n;
7 X = nusum(x*(1/z)^n,n,0,%inf);
8 limit(X);
9 disp(' X = ',X);
10 disp(' ROC = |z|>|a| ')
```

Scilab code Exa 6.2 z transform of anticausal sequence

```
1
2 clc;
3 clear;
4 syms n a z;
5 x = a^n;
```

```
6 X = nusum(-x*(1/z)^n,n,-%inf,-1);
7 limit(X);
8 disp(' X = ',X);
9 disp(' ROC = |z|<|a| ')</pre>
```

Scilab code Exa 6.3 z Transform

```
1  //EXAMPLE 6.3
2  //Z-Transform
3  clc;
4  clear;
5  syms n a z M N;
6  x = a^n;
7  X = nusum(x*(1/z)^n,n,M,N-1);
8  limit(X);
9  disp(X,' X = ');
```

Scilab code Exa 6.4 z Transform

```
1  //EXAMPLE 6.4
2  //Z-Transform
3  clc;
4  clear;
5  syms n z;
6  x = (-0.6)^n;
7  X = nusum(x*((1/z)^n),n,0,%inf);
8  limit(X);
9  disp(X,' X = ');
```

Scilab code Exa 6.5 Z transform of causal sequence

```
1 //EXAMPLE 6.9
2 //Z-Transform of causal sequence
3 clc;
4 clear;
5 //z=%z;
6 syms n a z M N;
7 x = a^n;
8 X = nusum(x*(1/z)^n,n,-M,N);
9 limit(X);
10 disp(X,' X = ');
```

Scilab code Exa 6.9 z Transform

```
1 //EXAMPLE 6.9
2 // Determination of ROC
3 clc;
4 clear;
5 z=%z;
6 a=2*z^4+16*z^3+44*z^2+56*z+32;
7 b=3*z^4+3*z^3-15*z^2+18*z-12;
8 [h1,g1]=factors(a);
9 [h2,g2]=factors(b);
10 disp(h1,'h1 = ');
11 disp(h2,'h2 = ');
12 c=a/b;
13 disp(c,'function is = ');
14 plzr(c);
```

Scilab code Exa 6.10 Rational form of z Transform from its zero and pole locations

```
1 //EXAMPLE 6.10
2 //Z-transform from pole-zero locations
```

```
3 clc;
4 clear;
5 z=%z;
6 //using the pole & zero locations provided
7 num=(z-0.21)*(z-3.14)*(z-(-0.3+%i*0.5))*(z-(-0.3-%i*0.5));
8 den=(z+0.45)*(z-0.67)*(z-(0.81+%i*0.72))*(z-(0.81-%i*0.72));
9 k=2.2;
10 Gz=(num/den);
11 disp(k*Gz, 'Gz = ');
```

Scilab code Exa 6.11 Inverse z Transform

```
//EXAMPLE 6.11
//Inverse Z-transform
clc;
clear;
syms n z1;
z = %z;
num = z; //given |z|>1;
den = (z-1)^2;
//Power series expansion
z = ldiv(num, den, 20);
disp(x, 'x = ');
disp('x = n*u[n]');
```

Scilab code Exa 6.12 Inverse z Transform

```
1 //EXAMPLE 6.12
2 //Inverse Z-transform
```

Scilab code Exa 6.13 Proper fraction of Rational z Transform

```
1 //EXAMPLE 6.13
2 //Determining proper fraction
3 clc;
4 clear;
5 z = \%z;
6 \text{ num} = 2*z^3 + 0.8*z^2 + 0.5*z + 0.3;
7 den = (z^3 + 0.8*z^2 + 0.2*z);
8 func = num/den;
9 disp(func, 'the polynomial function is H = ')
10
     if degree(num)>=degree(den)
11
12
               disp('An improper fraction');
13
         else disp('A proper fraction');
14
     end
15
16 disp('decomposing the fraction we get .....');
17
18 H1 = func - (-3.5*z + 1.5)/z;
19 disp(H1, 'H1 = ');
```

Scilab code Exa 6.14 Inverse z Transform by partial fraction expansion

```
1 //EXAMPLE 6.14
2 //Inverse Z-transform
3 clear;
4 clc;
5 z = \%z;
6 num=z*(z+2);
7 den=(z-0.2)*(z+0.6);
8 H=num/den;
9 elts=factors(den);
10 disp(elts);
11 //solving Partial Fractions, we get:
12 Hz = 2.75/(1-(0.2)/z) - 1.75/(1+(0.6)/z);
13 disp(Hz);
14 // \operatorname{disp} (h = 2.75 * (0.2^n) - 1.75 * (0.6^n) * u(n));
15 h1= ldiv(2.75*z,(z-(0.2)),10)
16 disp(h1/2.75, 'h1 = ');
17 h1= ldiv(1.75*z,(z+(0.6)),10)
18 disp(h1/1.75, 'h2 = ');
19 disp('the inverse z-transform is:')
20 disp('h = 2.75*(0.2^n)*u(n) - 1.75*(-0.6^n)*u(n)')
```

Scilab code Exa 6.15 residue computation using coefficient matching approach

```
1 //EXAMPLE 6.15
2 //solving for coefficients;
3 clear;
4 clc;
5 z = %z;
```

```
6 num=z*(z+2);
7 den=(z-0.2)*(z+0.6);
8 H=num/den;
9 disp('the factors are :');
10 elts=factors(den);
11 disp(elts);
12 //coeff are:
13 disp('The coefficients are p1,p2:');
14 p1 = horner((z+2)/(z+0.6),0.2);
15 disp(p1,'p1 = ');
16 p2 = horner((z+2)/(z-0.2),-0.6);
17 disp(p2,'p2 = ');
```

Scilab code Exa 6.16 Inverse z Transform by power series expansion

```
1 //EXAMPLE 6.16
2 // Partial fraction expansion
3
4 clc;
5 clear;
6 z = \%z;
7 num = z^3;
8 \text{ den} = 18*z^3 + 3*z^2 - 4*z - 1;
9 elts=factors(den);
10 disp(elts, 'the factors are :');
11 func = num/den;
12 //the partial fraction gives:
13 p1 = horner((1/(1+0.33333333/z)^2), 0.5);
14 disp(p1, 'p1 = ');
15 p2 = horner(1/((1-0.5/z)), -0.3333333);
16 \text{ disp(p2,'p2} = ');
17 p3 = horner(0.6/((1-0.5/z)), -0.3333333);
18 disp(p3, p3 = ');
19 disp('partial fraction gives: ');
20 disp(p1*z/elts(1), 'h1 = ');
```

```
21 disp(p3*z/elts(3), 'h2 = ');
22 disp(p2*z^2/(elts(2)*elts(2)), 'h3 = ');
```

Scilab code Exa 6.17 Coefficients of rational form

```
//EXAMPLE 6.16
//Coefficients of Rational form

clc;
clear;
z=%z;
num = 18*z^3;
den = 18*z^3 + 3*z^2 - 4*z - 1;
disp(coeff(num)/18, 'the Numerator polynomial coefficients are:');
disp(coeff(den)/18, 'the denominator polynomial coefficients are:');
```

Scilab code Exa 6.18 Inverse z Transform using long division

```
//EXAMPLE 6.18
//Inverse Z-transform using power series expansion
clc;
clear;
z=%z;
Xnum=z;
Xden=(z-1)^2;
xn=ldiv(Xnum,Xden,15);
disp(xn,'The function is = ');
disp(' Thus, xn = n*u(n)');
```

Scilab code Exa 6.19 Inverse z Transform using long division

```
1 //EXAMPLE 6.19
2 //Inverse Z-transform using Long division method
3 clc;
4 clear;
5 z=%z;
6 Hnum=z^2 + 2*z;
7 Hden=z^2 + 0.4*z -0.12;
8 hn=ldiv(Hnum, Hden, 20);
9 disp(hn, 'The function is, hn = ');
```

Scilab code Exa 6.20 Inverse z Transform

```
1 //EXAMPLE 6.20
2 //Inverse Z-transform using power series expansion
3 clc;
4 clear;
5 z=%z;
6 Hnum=z^2 + 2*z;
7 Hden=z^2 + 0.4*z -0.12;
8 hn=ldiv(Hnum, Hden, 20);
9 disp(hn, 'The impulse response is, hn = ');
```

Scilab code Exa 6.22 z Transform

```
//Example 6.22
//MAXIMA SCILAB TOOLBOX REQUIRED FOR THIS PROGRAM
//Z transform of r n.cos(wo n)
clc;
clear;
syms r wo n z;
x1 = (r^n)*exp(%i*wo*n);
```

```
8 X1 = nusum(x1*(z^-n),n,0,%inf);
9 x2 =(r^n)*exp(-%i*wo*n);
10 X2 = nusum(x2*(z^-n),n,0,%inf);
11 X =(X1+X2)/2;
12 disp(X,'X(z)=');
13 disp('ROC : |z|>r');
```

Scilab code Exa 6.23 z Transform

Scilab code Exa 6.24 sum of sequences of non overlapping ROC

```
1 //Example 6.24

2 //MAXIMA SCILAB TOOLBOX REQUIRED FOR THIS PROGRAM

3 //Z transform of v(n) = (a)^(n)*u(n) - (b)^(n)*u(-n -1)

4 clc;

5 clear;

6 disp('assuming |b| > a');
```

```
7 syms a n;
8 x1 = a^n;
9 X1 = nusum(x1,n,0,%inf);
10 x1 = b^n;
11 X1 = nusum(x2,n,-%inf,-1);
12 Vz = X1 + X2;
13 disp(Vz, 'The Z-transform is = ');
14 disp('ROC = |a|<|z|<|b|');</pre>
```

Scilab code Exa 6.25 z Transform

Scilab code Exa 6.26 z Transform

```
1    // Example 6.26
2    //MAXIMA SCILAB TOOLBOX
3    //Z transform of (n+1)*a^n*u(n)
4
5 clear;
```

```
6 clc;
7 syms a n z;
8 x1 =(a)^n;
9 X1 = symsum(x1*(z^(-n)),n,0,%inf);
10 X2 = -z*(diff (X,z,1));
11 X = X1 + X2;
12 disp (X, 'Z transform of(n+1)*a^n*u(n) is X = ');
```

Scilab code Exa 6.27 Inverse z Transform

```
1 // Example 6.27
2 //inverse Z-transform of z^3/(z-0.5)*(z+1/3)^2;
4 clear;
5 clc;
6 z = \%z;
7 Gnum = z^3;
8 Gden = (z-0.5)*(z+1/3)^2;
9 G = Gnum/Gden;
10 g1=ldiv (Gnum, Gden, 10);
11 elts=factors(Gden);
12
13 //the partial fraction gives:
14 p1 = horner((1/(1+0.33333333/z)^2), 0.5);
15 disp(p1, 'p1 = ');
16 p2 = horner(1/((1-0.5/z)), -0.3333333);
17 disp(p2, p2 = ');
18 p3 = horner(0.6/((1-0.5/z)), -0.3333333);
19 disp(p3, p3 = ')
20 disp('partial fraction gives: ');
21 disp(p1*z/elts(1), 'h1 = ');
22 disp(p3*z/elts(3), 'h2 = ');
23 disp(p2*z^2/(elts(2)*elts(2)), 'h3 = ');
24 disp('gn = 0.36*(0.5) n + 0.24*(-1/3) n + 0.4*(n+1)
     *(-1/3)^n
```

```
25 disp(g1, 'the first 10 samples of g[n] = ');
```

Scilab code Exa 6.28 Enlargement of ROC by pole zero cancellation

```
1 // Example 6.28
2 // Enlargement of ROC by pole-zero cancellation
3 clc;
4 clear;
5 z=%z;
6 Gz = (2 + 1.2*(1/z))/(1 - 0.2*(1/z))
7 disp(Gz, 'Gz = ');
8 disp('ROC = |z|>0.2');
9 Hz = 3/(1 + 0.6*(1/z));
10 disp(Hz, 'Hz = ');
11 disp('ROC = |z|>0.6');
12 Xz = Gz*Hz;
13 disp(Xz, 'Xz = ');
14 disp('ROC = |z|>0.2');
```

Scilab code Exa 6.30 Convolution

```
H(n+1) = h(n+1)*z^{(-n)};
12
13 end
14 disp(X', 'X = ');
15 disp(H', 'H = ');
16
17 for i=1:5
18
        U(i) = 0;
         for j=1:5
19
20
              U(i) = U(i) + X(i) * H(j);
21
         end
22 \text{ end}
23 \quad Y = 0;
24 for i=1:5;
25
         Y = Y + U(i);
26 \, \text{end}
27 \text{ disp}(Y, 'Y = ');
28
29 disp('y = [-2 \ -4 \ 1 \ 3 \ 1 \ 5 \ 1 \ -3]')
```

Scilab code Exa 6.31 Convolution

```
14
15 \text{ for } n=0:2
16
         H(n+1) = h(n+1)*(z^-n);
17 \text{ end}
18 disp(H', 'H = ');
19
20
21 for i=1:3
22
         U(i) = 0;
23
         for j=1:3
24
              U(i) = U(i) + X(i) * H(j);
25
         end
26 \text{ end}
27 \quad Y = 0;
28 for i=1:3;
        Y = Y + U(i);
29
30 \text{ end}
31 disp(Y, 'Y = ');
32
33 disp('y = [12 -2 9 10 -4]');
```

Scilab code Exa 6.33 Transfer Function of Moving Average Filter

```
//EXAMPLE 6.33
//Transfer function of moving average filter
clear;
clc;
syms n z M;
x=z^(-n);
H1=nusum(x,n,0,M-1);
H=H1/M;
disp(H,'Transfer function, Hz = ');
```

Scilab code Exa 6.34 Transfer function determination

```
1 //EXAMPLE 6.34
2 //y[n] = x[n-1] - 1.2 * x[n-2] + x[n-3] + 1.3 * y[n-1]
      -1.04*y[n-2] + 0.222*y[n-3]
3 //Transfer function determination
5 clc;
6 clear;
7 z=\%z;
8 disp('Given the difference equation taking
      ztransform on both sides: ')
9 \text{ Yz} = \text{z}^2 -1.2*\text{z} +1;
10 Xz = z^3 -1.3*z^2 + 1.04*z -0.222;
11 Hz = Yz/Xz;
12 disp(Hz, 'The transfer function is = ')
13 elts = factors(Xz);
14 disp(elts, 'factors of Xz are = ')
15 plzr(Hz);
```

Chapter 7

LTI Discreet Time systems in the Transform Domain

Scilab code Exa 7.1 Bounded real function

```
1 //EXAMPLE 7.1
2 //PROGRAM REQUIRES MAXIMA SCILAB TOOLBOX
4 clc;
5 clear;
6 syms K a z w;
8 hzden = (1-a*(z^-1)); //0 < |a| < 1;
9 \text{ Hz} = \text{K/hzden};
10 \operatorname{disp}('|H(e^(jw))|^2 = K^2/((1+a)^2 - 2*\cos(w)');
11 // considering a>0
12 disp('(at w = \%pi),K^2/(1+a)^2 < |H|^2 < K^2/(1-a)
      ^{2}, (at w = 0);
13 //considering a<0
14 disp(' (at w = 0),K^2/(1+a)^2 < |H|^2 < K^2/(1-a)
      ^{2}, (at w = \%pi)');
15 disp('if K = +/-(1-a), observe....');
16 \operatorname{disp}('|H(e^{(jw)})| \le 1 Hence a Bounded real
      function.');
```

```
17 //w=0:%pi;

18 //[a,b]=freq(hznum,hzden,w);

19 disp(abs(Hz))
```

Scilab code Exa 7.2 Transfer function determination

```
1 //EXAMPLE 7.2
2 //|H(e^{(jw)})|^2 = 4*((1.09 + 0.6*cosw)*(1.16-0.8*)
      \cos w) / ((1.04 - 0.2 * \cos w) * (1.25 + \cos w))
\frac{3}{\sqrt{\text{REPLACING}}} \cos w = (z + z(^-1))/2
4 clc;
5 clear;
6 z = \%z;
7 H1=4*((1.09 + (0.3)*(z+1/z))*(1.16 - (0.4)*(z+1/z)))
8 H2=((1.04 - (0.2)*(z+1/z))*(1.25 + (0.5)*(z+1/z)));
9 \text{ H=H1/H2};
10 disp(H, 'The transfer function is, H = ')
11 elts1=factors(numer(H));
12 disp(elts1, 'The factors of numerator are :');
13 elts2=factors(denom(H));
14 disp(elts2, 'The factors of denominator are :');
15 disp('The Four posible stable transfer function with
       same square magnitude function are :');
16 h1=2*((1+(0.3)/z)*(1-(0.4)/z))/((1-(0.2)/z)
      *(1+(0.5)/z));
17 disp(h1, 'stable transfer function, h1 = ');
18 h2=2*((1+(0.3)/z)*((0.4)-(1)/z))/((1-(0.2)/z)
      *(1+(0.5)/z));
19 disp(h2, 'stable transfer function, h2s = ');
20 h3=2*(((0.3)+1/z)*((1)-(0.4)/z))/((1-(0.2)/z)
      *(1+(0.5)/z));
21 disp(h3, 'stable transfer function, h3 = ');
22 \quad h4=2*(((0.3)+1/z)*((0.4)-(1)/z))/((1-(0.2)/z)
      *(1+(0.5)/z));
```

Scilab code Exa 7.6 FIR Transfer function

```
1 //EXAMPLE 7.6
2 //FIR Trasnfer functions with different Phase.
3 clc;
4 clear;
5 z = \%z;
6 W = 0:(1/400):1;
7 z = \exp(\%i*2*\%pi*W);
8 \text{ for } i=1:401
       H1z(i) = -1 + 2/z(i) - 3/(z(i)^2) + 6/(z(i)^3)
          -3/(z(i)^4) +2/(z(i)^5) -1/z(i)^(6);
11 H1z_phase = phasemag(H1z);
12
13 clf();
14 figure(0);
15 plot2d(W/(2*%pi), H1z_phase, 1);
16 xtitle('phase response', W/(2*\%pi)', 'H2z_phase in
      degrees');
17
18 for i=1:401
       H2z(i) = +1 - 2/z(i) + 3/(z(i)^2) - 6/(z(i)^3) +
          3/(z(i)^4) - 2/(z(i)^5) + 1/z(i)^(6);
20 end
21 H2z_phase = phasemag(H2z);
22
23 plot2d(W/(2*%pi), H2z_phase, 2);
24 xtitle ('phase response', W/(2*\%pi)', 'H2z_phase in
      degrees');
```

Chapter 8

Digital Filter Structures

Scilab code Exa 8.1 Analysis of Cascaded lattice digital filter structure

```
//EXAMPLE 8.1
//MAXIMA SCILAB TOOLBOX REQUIRED FOR THIS EXAMPLE
//Digital filter structure
clear;
clc;
syms W1 W2 W3 X Y a d B y E z;
//Equations obtained are as follows:
W1 = X - a*W3/z;
W2 = W1 - d*W2/z;
W3 = W2/z + E*W2;
Y = B*W1 +y*W3/z;
Hz = (B + (B*d+y*E)/z + y/(z^2))/(1 + (d+a*E)/z + a/(z^2))
disp(Hz, 'Hz = ');
```

Scilab code Exa 8.6 Factorization of FIR Transfer Function

```
1 //Example 8.6
2 //Factorization of FIR Transfer Function
3 clear;
4 clc;
5 z=%z;
6 Hz=50.4+28.02/z+13.89/z^2+7.42/z^3+6.09/z^4+3/z^5+1/z^6;
7 disp(factors(numer(Hz)), 'The Factors of the FIR Transfer Function are = ');
```

Scilab code Exa 8.7 Factorization of IIR Transfer Function

```
1 / Example 8.7
2 // Factorization of IIR Transfer Function
3 clear;
4 clc;
5 z = \%z;
6 //Numerator of the transfer function
7 Numz = 6+17.1/z+33.05/z^2+24.72/z^3+19.908/z^4-5.292/z
      ^5+18.144/z^6;
8 //Denominator of the transfer function
9 Denz=1+2.2/z+2.56/z^2+1.372/z^3+0.118/z^4-0.332/z
      ^5-0.168/z^6;
10 Fn=factors(numer(Numz));
11 disp (Fn, 'Factors of the numerator of the Transfer
      Function = ');
12 Fd=factors(numer(Denz));
13 disp (Fd, 'Factors of the denominator of the Transfer
     Function = ');
```

Scilab code Exa 8.10 Cascaded lattice realization of IIR digital Transfer Function

```
1 //Example 8.10
2 //Cascaded lattice realization of IIR Transfer
      Function
3 clear:
4 clc;
5 z = \%z;
6 P3z = -0.2 + 0.18/z + 0.4/(z^2) + 1/(z^3);
7 D3z= 1 + 0.4/z + 0.18/(z^2) - 0.2/(z^3);
8 \quad A3z = P3z/D3z;
9 p1=coeff(numer(P3z));
10 p=mtlb_fliplr(p1);
11 disp(mtlb_fliplr(p), 'The coefficients ofnumerator
      are = ');
12 d1 = coeff(numer(D3z-1));
13 d=mtlb_fliplr(d1)
14 disp((d), 'The coefficients of numerator are = ');
15 d1_1dash = (d(1) - d(3) * d(2)) / (1 - d(3) * d(3));
16 disp(d1_1dash, "d1_1dash = ");
17 d2_1dash = (d(2)-d(3)*d(1))/(1-d(3)*d(3));
18 disp(d2\_1dash,"d2\_1dash");
19 d1_2dash=(d1_1dash)/(1+d2_1dash);
20 disp(d1_2dash, "d1_2dash = ");
21 A1z=(d1_2dash + 1/z)/(1 + d1_2dash/z);
22 \text{ disp}(A1z, 'A1z = ');
23 \text{ A2z} = (d2_1dash + d1_1dash*1/z + 1/z^2)/(1 + d1_1dash/
      z - d2_1dash/z^2;
24 \text{ disp}(A2z, 'A2z = ');
```

Scilab code Exa 8.12 Gray Markel method of realization

```
1 //Example 8.12
2 //Gray Markel method of Realisation
3 clear;
4 clc;
5 z=%z;
```

```
6 P3z = 0 + 0.44/z + 0.362/(z^2) + 0.02/(z^3);
7 D3z= 0.4/z + 0.18/(z^2) - .2/(z^3);
8 \text{ Hz}=P3z/D3z;
9 p1=coeff(numer(P3z));
10 p=mtlb_fliplr(p1)
11 disp(mtlb_fliplr(p), 'The coefficients ofnumerator
      are = ');
12 d1=coeff(numer(D3z));
13 d=mtlb_fliplr(d1)
14 disp(mtlb_fliplr(d), 'The coefficients ofnumerator
      are = ');
15 d1_1dash = (d(1)-d(3)*d(2))/(1-d(3)*d(3));
16 \operatorname{disp}(d1\_1\operatorname{dash}, "d1\_1\operatorname{dash} = ");
17 d2_1dash = (d(2) - d(3) * d(1)) / (1 - d(3) * d(3));
18 disp(d2\_1dash,"d2\_1dash");
19 d1_2dash = (d1_1dash)/(1+d2_1dash);
20 disp(d1_2dash, "d1_2dash = ");
21 \text{ a1=p(3)};
22 \text{ disp}(p(3), 'a1 = ');
23 \quad a2=p(2)-a1*d(1);
24 disp(p(2)-a1*d(1), 'a2 = ');
25 a3=p(1)-a1*d(2)-a2*d1_1dash;
26 \text{ disp}(p(1)-a1*d(2)-a2*d1_1dash, 'a3 = ');
27 \text{ disp}(0-a1*d(3)-a3*d1_2dash-a2*d2_1dash, 'a4 = ');
```

Scilab code Exa 8.18 Cascaded lattice realization

```
1  //Example 8.18
2  //Cascaded lattice realization of Power-symmetric
    FIR Transfer Function
3  clear;
4  clc;
5  z=%z;
6
7  H5z=(1 + 0.3/z + 0.2/z^2 - 0.376/z^3 - 0.06/z^4 +
```

```
0.2/z^5);

8 disp(H5z,'FIR filter = ');

9 G5=horner(H5z,-1/z);

10 G5z=G5/z^5;

11 disp(G5z,'FIR filter = ');

12 k5=0.2;

13 H3z=(1/(1+k5^2))*(H5z - k5*G5z);

14 disp(H3z,'Synthesis eqn,H3z = ');

15 G3z=(1/(1+k5^2))*(k5*H5z + G5z);

16 disp(G3z,'Synthesis eqn,G3z = ');

17 k=coeff(numer(G3z));

18 disp(k(4),'k3 = ');

19 disp(k(2),'k1 = ');
```

Chapter 9

IIR digital filter design

Scilab code Exa 9.1 Computating ripple values

```
//EXAMPLE 9.1
//pass band & stop band ripple
clc;
clear;
ap=0.1;//peak passband ripple in dB
as=35;//min. stopband attenuation in dB

//calculation of peak ripple values
dp=1-10^-(ap/20);
disp(dp, 'dp = ');
ds=10^-(as/20);
disp(ds, 'ds = ');
```

Scilab code Exa 9.2 conversion of bandedged frequencies to Normalized digital frequencies

```
1 //EXAMPLE 9.2
2 //analog passband & stopband frequencies(in KHz) :
```

```
3 clc;
4 clear;
5 ap=7;
6 as=3;
7 //Sampling frequency (in KHz):
8 FT=25;
9 //digital frequencies:
10 wp=2*%pi*ap/FT;
11 disp(wp, 'wp = ');
12 ws=2*%pi*as/FT;
13 disp(ws, 'ws = ');
```

Scilab code Exa 9.3 Design of HP Digital Filter

```
1 / Example 9.3
 2 //Design of HP IIR filter
3 clc;
4 clear;
5 \text{ Fp} = 700 / / \text{Hz}
6 \text{ Fs} = 500 / / \text{Hz}
 7 \text{ ap=1//dB}
8 \text{ as} = 32 / / dB
9 \text{ FT} = 2000 / / \text{Hz}
10 //normalized angular edge frequencies in rad/sec
11 wp=2*%pi*Fp/FT;
12 \text{ ws}=2*\%\text{pi}*\text{Fs/FT};
13 //prewarp the digital edge frequencies
14 Ap1=tan(wp/2);
15 As1=tan(ws/2);
16
17 Ap=1; // assuming
18 As=(2*\%pi*Ap1)*Ap/(2*\%pi*As1);
19 \text{ disp}(As, 'As = ')
20 //Order 'N' of the filter
21 k = Ap/As;
```

```
22 disp(1/k, '1/k = ');
23 k1 = 1/(sqrt(((10^(0.1* as))-1)/((10^(0.1*ap))-1)));
24 disp(1/k1, '1/k1 = ');
25 N = ceil(acosh(1/k1)/acosh(1/k));
26 \text{ disp}(N, N = ');
27 disp(N, 'Order of the filter is, N = ');
28
29 = sqrt(10^{(0.1*ap)-1});
30 \text{ u=1/e} + \text{sqrt}(1+(1/(e*e)));
31 a=Ap*(u^(1/N) - u^(-1/N))/2;
32 b=Ap*(u^(1/N) + u^(-1/N))/2;
33
34 \text{ for } i=1:N
35
        phi(i) = %pi/2 + (2*i -1)*(%pi)/(2*N);
36
        p(i)=a*cos(phi(i)) + %i*b*sin(phi(i));
37 end
38 \text{ s=}\%\text{s};
39 z = \%z;
40 \text{ H1=1};
41 // Numerator of H(s)
42 \text{ for } i=1:N
        H1=H1*(s + p(i))
43
44 end
45 // Denominator of H(s)
46 H2=horner(H1,0);
47 //Transfer function
48 \text{ H}=\text{H}2/\text{H}1;
49 \text{ disp}(H, 'H = ')
50 // Bilnear Transformation, s = ((z-1/(z+1));
51 Hz=horner(H,(z-1)/(z+1));
52 disp(Hz, 'The digital HP filter is Hz = ');
```

Scilab code Exa 9.6 Changing passband edge frequencies to LP IIR digital frequencies

Scilab code Exa 9.7 Design of HP IIR Digital Filter from LP Digital Filter

```
1 //EXAMPLE 9.7
2 //LP TO HP Transformation
3
4 clc;
5 clear;
6 z = \%z;
7 Glz=(0.0662272*(1+1/z)^3)/((1-0.2593284/z)
      *(1-0.6762858/z+0.3917468/(z^2)));
8 wc=0.25*%pi;//Oringinal passband edge
9 Wc=0.55*%pi;//Required passband edge
10 1 = -\cos((wc + Wc)/2)/\cos((wc - Wc)/2);
11 disp(1, 'lambda = ');
12
13 w = 0:0.001:1;
14 Ghz=horner(Glz, -((z + 1)/(1 + 1*z))); //LP TO HP
      Transformation formula
15 den=factors(denom(Ghz));
```

```
16 disp(Ghz, 'The transfer function is Gdz = ');
17 disp(den, 'the facors of the denominator are = ');
```

Scilab code Exa 9.12 Minimum order of Type 2 Chebyshev HP IIR digital filter

```
1 //EXAMPLE 9.12
2 //Minimum order of type-2 Chebyshev highpass digital
        filter
3 clc;
4 clear;
5 \text{ ap} = 1 //dB
6 \text{ as} = 40 \text{ }//\text{dB}
7 \text{ Fp} = 1000 //Hz
8 \text{ Fs} = 600 \text{ }/\text{Hz}
9 Wp = Fp*2*\%pi;
10 Ws = Fs*2*\%pi;
11
12 F = 4000 //Hz
13 T=1/F;
14
15 Ap = (2/T) * (tan(Wp*T/2))
16 As = (2/T) * (tan(Ws*T/2))
17
18
19 k = Ap/As;
20 disp(1/k, '1/k = ');
21 	 k1 = 1/(sqrt(((10^(0.1* as))-1)/((10^(0.1*ap))-1)));
22 disp(1/k1, '1/k1 = ');
23 N = acosh(1/k1)/acosh(k); //order of the filter
24 \text{ disp}(N, 'N = ');
25 disp('Since order of the filter is always an integer
      , ');
26 disp(ceil(N), 'Order of the filter is, N = ');
```

FIR digital filter design

Scilab code Exa 10.1 Kaiser formula

```
1 //Example 10.01
2 //Order estimation using Kaiser's formula
3 clear;
4 clc;
5 Fp=1800; //Passband edge freq. in Hz
6 Fs=2000; //stopband edge freq. in Hz
7 ap=0.1; //peak passband ripple in dB
8 as=35; //min. stopband attenuation in dB
9 FT=12000; // Sampling freq. in Hz
10
11 //calculation of peak ripple values
12 dp=1-10^-(ap/20);
13 disp(dp, 'dp = ');
14 ds=10^-(as/20);
15 \operatorname{disp}(\operatorname{ds}, '\operatorname{ds} = ');
16
17 //Order of the FIR filter
18 N = (-(20*log10(sqrt(ds*dp))) - 13)/((14.6)*(Fs-Fp)/FT
      );
19 disp(ceil(N), 'Order of the filter is N = ')
```

Scilab code Exa 10.2 Bellenger formula

```
1 //Example 10.01
2 // Order estimation using Bellanger's formula
3 clear;
4 clc;
5 Fp=1800; //Passband edge freq. in Hz
6 Fs=2000; //stopband edge freq. in Hz
7 ap=0.1;//peak passband ripple in dB
8 as=35; //min. stopband attenuation in dB
9 FT=12000; //Sampling freq. in Hz
10
11 //calculation of peak ripple values
12 dp=1-10^-(ap/20);
13 disp(dp, 'dp = ');
14 ds=10^-(as/20);
15 \operatorname{disp}(\operatorname{ds}, \operatorname{ds} = \cdot);
16
17 //Order of the FIR filter
18 N = ((-2*log10(10*ds*dp)) / ((3)*(Fs-Fp)/FT)) -1;
19 disp(ceil(N), 'Order of the filter is N = ')
```

Scilab code Exa 10.3 Hermann formula

```
//Example 10.03
//Order estimation using Hermann's formula
clear;
clc;
Fp=1800;//Passband edge freq. in Hz
Fs=2000;//stopband edge freq. in Hz
ap=0.1;//peak passband ripple in dB
as=35;//min. stopband attenuation in dB
```

```
9 FT=12000; //Sampling freq. in Hz
10
11 //calculation of peak ripple values
12 dp=1-10^-(ap/20);
13 disp(dp, 'dp = ');
14 \, ds=10^-(as/20);
15 \text{ disp}(ds, 'ds = ');
16
17 \quad a1 = 0.005309;
18 \quad a2 = 0.07114;
19 a3 = -0.4761;
20 \quad a4 = 0.00266;
21 \quad a5=0.5941;
22 \quad a6 = 0.4278;
23 D_{infi}=((a1*(log10(dp)^2) + a2*log10(dp) + a3)*log10
      (ds))-(a4*(log10(dp))^2 + a5*(log10(dp)) + a6);
24 disp(D_infi, D_infi = ');
25 b1=11.01217;
26 b2=0.51244;
27 F=b1 + b2*((log10(dp))-(log10(ds)));
28 \text{ disp}(F, 'F = ');
29
30 //Order of the FIR filter
31 N=(D_{infi}-F*((Fs-Fp)/FT)^2)/((Fs-Fp)/FT);
32 disp(ceil(N), Order of the filter is N = ')
```

Scilab code Exa 10.4 Order Estimation

```
//Example 10.04
//Kaiser's formula for bandpass filter
clear;
fcl;
Fp1=300;//Passband edge freq. in Hz
Fs1=350;//stopband edge freq. in Hz
Fp2=1000;//Passband edge freq. in Hz
```

```
8 Fs2=1100; //stopband edge freq. in Hz
9
10 dp=0.004; // passband ripple in dB
11 ds=0.01; //stopband ripple in dB
12 FT=10000; // Sampling freq. in Hz
13
14 // Since (Fp1-Fs1) < (Fs2-Fp2), bandwith used is (Fp1-Fs1)
15
16 // Order of the FIR filter
17 N=(-(20*log10(sqrt(ds*dp))) - 13)/((14.6)*(Fs1-Fp1)/FT);
18 disp(ceil(N), 'Order of the filter is N = ')</pre>
```

Scilab code Exa 10.6 Filter length estimation for window based design

```
1 //EXAMPLE 10.6
2 //Filter length for window -based design
3 clear;
4 clc;
5 wp=0.3*\%pi;//rad/sec
6 ws=0.5*\%pi;//rad/sec
7 as=40; //dB
9 wc=(wp+ws)/2;//cutoff frequency
10 Bw=ws-wp;
11 disp(Bw, 'Normalized transition bandwidth is = ')
12 //Hann window
13 M1 = 3.11 * \%pi/Bw;
14 disp(M1, 'Value of M = ')
15 //Hamming window
16 M2=3.32*\%pi/Bw;
17 disp(M2, 'Value of M = ')
18 //Blackman window
19 M3=5.56*\%pi/Bw;
```

Scilab code Exa 10.7 Order Estimation

```
//EXAMPLE 10.6
//Order estimation using Dolph-Cebyshev window
clear;
clc;
wp=0.3*%pi;//rad/sec
ws=0.5*%pi;//rad/sec
as=40;//dB

wc=(wp+ws)/2;//cutoff frequency
Bw=ws-wp;
disp(Bw,'Normalized transition bandwidth is = ')
//Order of the filter
N = ((2.056*as) - 16.4)/(2.285*Bw);
disp(ceil(N),'Order of the filter, N = ')
```

Scilab code Exa 10.8 Kaiser window

```
//EXAMPLE 10.8
//Design of LP FIR filter using Kaiser window
clear;
clc;
wp=0.3*%pi;//rad/sec
ws=0.5*%pi;//rad/sec
as=40;//dB
wc=(wp+ws)/2;//cutoff frequency
Bw=ws-wp;
disp(Bw,'Normalized transition bandwidth is = ')
```

```
12 ds=10^(-as/20);
13 B = (0.5842*(as-21)^0.4) + 0.07886*(as-21);
14
15 N = ceil((as - 8)/(2.285*Bw));
16 \operatorname{disp}(N, 'Order \ of \ the \ filter, N = ');
17 M = (N-1) *0.5;
18 disp(M, 'M = ');
19 w=window('kr',N,6);//Kaiser window
20 i = -M : 1 : M;
21
22
       hn = (wc/\%pi)*sinc(wc*i'/(\%pi));
23
       h=hn*w;
24
25 clf();
26 n=0:0.001:1;
27 [H,fr] = frmag(w,1001);
28
29 plot2d(2*fr,log10(H./max(H)),style=color('blue'))
30 set(gca(), 'grid', [1 1]*color('gray'))
31 \ a = gca \ () ;
32 xlabel ('w/\%pi');
33 ylabel ('Magnitude in dB');
34 title ('Gain Response of Kaiser Window');
```

DSP Algorithm implementation

Scilab code Exa 11.3 Reconstruction of Transfer function from Impulse response coefficients

```
1 // example 11.3
2 // Reconstruction of Transfer function from Impulse
      response coeff.
3 clear;
4 clc;
5 z = \%z;
6 numz = 2+6/z+3/(z^2);
7 denz=(1+1/z+2/z^2);
8 disp(numz/denz, 'Hz = ');
9 d=coeff(numer(denz));
10 disp(d, 'coefficients of the denominator are = ')
11 h1=ldiv(numer(numz), numer(denz),5);
12 disp(h1', 'The first five coeffcients are of H(z) = '
     );
13 for i=1:3
14
       for j=1:3
15
           if i >= j
                h(i,j)=h1(i-j+1)
16
17
           else
                h(i,j)=0;
18
```

```
19         end
20         end
21         end
22         disp(h, 'h = ');
23         disp((h'*d')', 'coefficients of the numerator are = ');
```

Scilab code Exa 11.11 Cascaded lattice Filter structure

```
1 //Example 11.11
2 //Simulation of IIR cascaded lattice filter
      structure
3 clear;
4 clc;
5 z = \%z;
6 P3z = 0 + 0.44/z + 0.362/(z^2) + 0.02/(z^3);
7 D3z= 1 + 0.4/z + 0.18/(z^2) - 0.2/(z^3);
8 \text{ Hz}=P3z/D3z;
9 p1=coeff(numer(P3z));
10 p=mtlb_fliplr(p1)
11 disp(mtlb_fliplr(p), 'The coefficients ofnumerator
      are = ');
12 d1=coeff(numer(D3z-1));
13 d=mtlb_fliplr(d1)
14 disp(mtlb_fliplr(d), 'The coefficients ofnumerator
      are = ');
15 d1_1dash = (d(1)-d(3)*d(2))/(1-d(3)*d(3));
16 \operatorname{disp}(d1\_1\operatorname{dash}, "d1\_1\operatorname{dash} = ");
17 d2_1dash = (d(2) - d(3) * d(1)) / (1 - d(3) * d(3));
18 disp(d2\_1dash,"d2\_1dash");
19 d1_2dash=(d1_1dash)/(1+d2_1dash);
20 disp(d1_2dash, "d1_2dash = ");
21 	 a1=p(3);
22 \text{ disp}(p(3), 'a1 = ');
23 \quad a2=p(2)-a1*d(1);
```

```
24 disp(p(2)-a1*d(1), 'a2 = ');

25 a3=p(1)-a1*d(2)-a2*d1_1dash;

26 disp(p(1)-a1*d(2)-a2*d1_1dash, 'a3 = ');

27 disp(0-a1*d(3)-a3*d1_2dash-a2*d2_1dash, 'a4 = ');
```

Analysis of Finite Wordlength Effects

Scilab code Exa 12.3 Signal to Quantisation Noise Ratio

```
1 //Example 12.3
2 //Signal-to-quantization Noise ratio
3 clear;
4 clc;
5 b=[7 9 11 13 15];//Given values of b
6 K=[4 6 8];//Given values of K
7 for i=1:5
8     for j=1:3
9         SNR(j,i)=6.02*b(i)+16.81-20*log10(K(j));
10     end
11 end
11 end
12 disp(SNR, 'SNR,A/D = ');
```

Multirate DIgital Signal Processing Findamentals

Scilab code Exa 13.1 Up sampling operation

```
1 //Example 13.1
2 //Upsampling Operation
3 clear;
4 clc;
5 clf();
6 a=gca();
7 figure(0);
8 n = [0:0.1:4.9];
9 a.x_location="origin";
10 x = sin(\%pi*n);
11 plot2d3(n,x,2);
12 xtitle('The sine wave', 'n', 'sin(x)');
13 plot(n,x,'r.');
14 //Up sampling
15 //Up sampling value - user input
16 figure(1);
17 L=input(" The up sampling value ");
18
19 a.x_location="origin";
```

```
20  x1=sin(%pi*n/L);
21  plot2d3(n,x1,5);
22  plot(n,x1,'r.');
23  xtitle('The sine wave','n','sin(x/L)');
```

Scilab code Exa 13.2 Down sampling operation

```
1 //Example 13.2
2 //Downsampling Operation
3 clear;
4 clc;
5 clf();
6 a=gca();
7 figure(0);
8 n = [0:0.1:4.9];
9 a.x_location="origin";
10 x=sin(\%pi*n);
11 plot2d3(n,x,2);
12 xtitle('The sine wave', 'n', 'sin(x)');
13 plot(n,x,'r.');
14 //Down sampling
15 //Down sampling - user input
16 figure(1);
17 M=input(" The down sampling factor
                                         ");
18 a.x_location="origin";
19 x1 = sin(\%pi*n*M);
20 plot2d3(n,x1,1);
21 plot(n,x1,'r.');
22 xtitle('The sine wave', 'n', 'sin(x*M)');
```

Scilab code Exa 13.6 Decimator Computation complexity

```
1 //Example 13.6
```

```
//Decimator computational complexity
clear;
clc;
//no. of multiplications/sec =Rm
FT = input("Sampling Frequency");
N = input("The order of the FIR Hz");
Rm1 = N*FT;
disp(Rm1, 'Rm, FIR = ');
//M = factor of Down sampler
M = input("The Down Sampling factor ");
disp(Rm1/M, 'Rm, FIR-DEC = ');
K = input("The order of the IIR Hz");
Rm2 = (2*K + 1)*FT;
disp(Rm2, 'Rm, IIR = ');
disp((K*FT + ((K+1)*FT/M)), 'Rm, IIR-DEC = ');
```

Applications of Digital Signal Processing

Scilab code Exa 14.1 Effect of DFT length

```
1 //Example 14.1
2 //EFFECT OF DFT LENGTH ON SPECTRAL ANALYSIS
3 clear;
4 clc;
5 N = 16;
6 n = 0: N-1;
7 f1=0.22;
8 f2=0.34;
10 R = input("R point DFT(R E [16, 128]) = ");
     Input f1 = 64
11 if R \gg N
       x=0.5*(sin(2*\%pi*f1*n')) + sin(sin(2*\%pi*f2*n'))
12
       x=[x', zeros(1, R-length(n))];
13
14
       disp(x,'the sequence is :');
15
       for n=0:R-1
16
           for k=0:R-1
17
                W(n+1,k+1) = \exp(-(\%i*2*\%pi*k/R)*n);
```

```
18
            end
19
       end
       X = W * x';
20
       disp(X, 'DFT is, X = ')
21
22 else
23
       disp('invalid computation');
24 end
25 \text{ m} = 0: R-1;
26 clf();
27 figure (0)
28 \ a = gca();
29 plot2d3(m,abs(X),2) // plotting DFT of sequence
30 plot(m, abs(X), 'r.')
31 a.x_location = 'origin';
32 a.y_location = 'origin';
33 \text{ poly1} = a . children (1) . children (1) ;
34 poly1.thickness = 2.5;
35 xtitle('original sequence', 'n', 'x[n]');
```

Scilab code Exa 14.2 Effect of DFT length

```
14
        disp(x,'the sequence is :');
        for n=0:R-1
15
            for k=0:R-1
16
                 W(n+1,k+1) = \exp(-(%i*2*\%pi*k/R)*n);
17
18
            end
19
        end
        X = W * x';
20
        disp(X, 'DFT is, X = ')
21
22 //plotting DFT of sequence
23 \text{ m} = 0 : R - 1;
24 clf();
25 figure (0)
26 \ a = gca();
27 plot2d3(m,abs(X),2)
28 plot(m,abs(X),'r.')
29 a.x_location = 'origin';
30 a.y_location = 'origin';
31 \text{ poly1} = a \cdot \text{children} (1) \cdot \text{children} (1) ;
32 poly1.thickness = 2.5;
33 xtitle('original sequence', 'n', 'x[n]');
```