## Scilab Textbook Companion for Feedback Control of Dynamic Systems by G. F. Franklin, J. D. Powell and A. Emami-Naeini<sup>1</sup>

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# **Book Description**

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

**AP** Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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## Chapter 2

18

19 //step response to u=500;

## Dynamic Models

Scilab code Exa 2.1.b step response of Cruise control system

```
//Example 2.1
//(b) step response of Cruise control system

xdel(winsid())//close all graphics Windows
clear;
clc;

// Cruise control parameters
m=1000;
b=50;
u=500;

// Transfer function
s=%s; // or
s=poly(0, 's');
sys=syslin('c',(1/m)/(s+b/m))
```

```
20 t=0:0.5:100;
21 v=csim('step',t,u*sys);
22 plot2d(t,v,2)
23
24 //Title, labels and grid to the figure
25 exec .\fig_settings.sci; //custom script for setting figure properties
26 title('Responses of car velocity to a step in u',' fontsize',3)
27 xlabel('Time t (sec.)','fontsize',2)
28 ylabel('Amplitude','fontsize',2)
29
30 //
```

fig\_settings.sci

#### Scilab code Exa 2.5.b step response of pendulum

```
1 //Example 2.5
2 //(b) step response of pendulum
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7
8 //
```

```
9 //Pendulum parameters 10 m=0.5;
```

```
11 1=1;
12 g=9.81;
13
14 // Transfer function
15 \text{ s=}\%\text{s};
16 sys=syslin('c',(1/(m*l^2))/(s^2+g/l));
17
18 //step response to u=500;
19 t=0:0.02:10;
20 theta=csim('step',t,sys);
21 plot(t,theta*57.3);
22
23 //Title, labels and grid to the figure
24 exec .\fig_settings.sci; // custom script to set
      figure properties
25 title('Response of pendulum to a step input in the
      applied torque',...
26 'fontsize',3);
27 xlabel('Time t (sec.)', 'fontsize',2);
28 ylabel('Pendulum angle (degree)', 'fontsize', 2);
29
30 //
```

fig\_settings.sci

### Chapter 3

## Dynamic Responses

```
check Appendix AP 1 for dependency:
    fig_settings.sci
```

#### Scilab code Exa 3.4 Frequency response

14 sysH=syslin('c',1/(s+k))

15

```
16 //Frequency response for k=1
17 //Note that - magnitude plot semilog plot unlike log
     -log plot in the book.
18 bode (sysH, fmin, fmax)
19 title('Frequency response for k=1', 'fontsize',3)
20
21 //
\frac{22}{(b)} Response to u=\sin(10*t);
23 t=0:0.02:10;
24 \ u = \sin(10*t);
25 \text{ y=csim}(u,t,sysH);
26 figure, plot(t,y)
27
28 //Title, labels and grid to the figure
29 exec .\fig_settings.sci; // custom script for
      setting figure properties
30 title('Complete transient response', 'fontsize', 3)
31 xlabel('Time (sec.)', 'fontsize',2)
32 ylabel('Output', 'fontsize',2)
33
34 //phase lag
35 figure, plot(t,y)
36 plot(t,u,'r')
37 zoom_rect([9 -1 10 1])
38 exec .\fig_settings.sci; // custom script for
      setting figure properties
39 title('Phase lag between output and input', 'fontsize
      ',3)
40 xlabel('Time (sec.)', 'fontsize',2)
41 ylabel('Output, Input', 'fontsize',2)
42 h=legend('y(t)', 'u(t)')
43 h.legend_location = "in_upper_right"
44 h.fill_mode='off'
45
46 // time lag
47 \text{ w=find}(t>=9.4 \& t<=10);
```

```
48 \text{ T=t(w)};
49 Y = y(w);
50 \ U=u(w);
51 \text{ wu} = \text{find}(U == \text{max}(U))
52 \text{ wy=find}(Y==\max(Y))
53
54 //Responses
55 plot2d3(T(wy),Y(wy))
56 plot2d3(T(wu),U(wu))
57 delta_t=T(wu)-T(wy); //time lag sec.
58 xstring(9.64,-0.1,"\$\ delta t$",0,0)
59 xarrows([9.58;9.72], [0;0], 0.7, 1)
60 xarrows([9.72;9.58], [0;0], 0.7, 1)
61 t=get("hdl")
62 disp(abs(delta_t), "Time lag of output in sec. is")
63 disp(abs(delta_t)*10, "Phase lag of output in
      radians is")
64
65 //
```

Scilab code Exa 3.8 Partial fraction expansion for distinct real roots

```
1 //Example 3.8
2 //Partial fraction expansion for distinct real roots
.
3
4 clear;
5 clc;
6 //
```

```
7 // Partial fraction expansion for distinct real roots
8 // Transfer function
9 s = %s;
10 num = (s+2)*(s+4)
11 p1=s;
12 p2=(s+1);
13 p3=(s+3);
14 sys=syslin('c',num/(p1*p2*p3))
15 //
16 // Partial fraction expansion is: sys = r1/p1 + r2/p2
      + r3/p3
17 //residue calculation
18 r1=residu(num,p1,(p2*p3))
19 r2=residu(num,p2,(p1*p3))
20 \text{ r3}=\text{residu}(\text{num},\text{p3},(\text{p1}*\text{p2}))
21
22 disp([r1 r2 r3]', "Residues of the poles p1, p2 and
      p3 are")
23 disp([roots(p1), roots(p2), roots(p3)]', "Poles p1,
      p2 and p3 are at")
24 disp('k=[]')
25
26 //
```

#### Scilab code Exa 3.9 Final value theorem

```
1 //Example 3.9
2 //Computing final value (use of final value theorem)
```

```
3
4 clear;
5 clc;
6
7 //
9 //Computing final value (use of final value theorem)
10 // Output of the system
11 s=poly(0, 's');
12 \text{ num} = 3*(s+2);
13 den=s*(s^2+2*s+10);
14 Ys=syslin('c',num/den);
15
16
17 //final value theorem, \lim s \longrightarrow 0 in s*Y(s)
19 Y_final=horner(s*Ys,0)
20 disp(Y_final, "The final value of the output y is:")
21
22 //
```

#### Scilab code Exa 3.10 Incorrect use of final value theorem

```
8 s=poly(0,'s');
9 num=3;
10 den=s*(s-2);
11 Ys=syslin('c',num/den);
12
13 //final value theorem, lim s-->0 in s*Y(s)
14 Y_final=horner(s*Ys,0);
15 disp(Y_final,"The final value of the output y is:");
16 disp('The final value computed is incorrect as the system...
17 response is unbounded');
18 //
```

#### Scilab code Exa 3.11 DC gain of the system

```
1  //Example 3.11
2  //Computing DC gain of the system.
3
4  clear;
5  clc;
6  //
7  //Transfer Function
8  s=poly(0, 's');
9  num=3*(s+2);
10  den=(s^2+2*s+10);
11  Ys=syslin('c',num/den);
12
13  //The DC gain of the system Y(s) as s-->0 is
14  DC_Gain=horner(Ys,0)
```

```
15 disp(DC_Gain, "The DC gain of the system is:")
16 //
```

Scilab code Exa 3.14 Partial fraction expansion for distinct real roots

```
1 //Example 3.14
2 // Partial fraction expansion for distinct real roots
3 clear;
4 clc;
5 //
6 // Transfer function
7 s = %s;
8 \text{ num}=2;
9 p1=(s+1);
10 p2=(s+2);
11 p3=(s+4);
12 sys=syslin('c',num/(p1*p2*p3))
13
14 // Partial fraction expansion is: sys = r1/p1 + r2/p2
      + r3/p3
15 //residue calculation
16 \text{ r1}=\text{residu}(\text{num},\text{p1},(\text{p2*p3}))
17 r2=residu(num, p2, (p1*p3))
18 r3 = residu(num, p3, (p1*p2))
19
20 disp([r1 r2 r3]'," Residues of the poles p1, p2 and
      p3 are")
21 disp([roots(p1), roots(p2), roots(p3)]', "Poles p1,
      p2 and p3 are at")
22 disp('k=[]')
23 //
```

#### Scilab code Exa 3.15 Cruise Control Transfer Function

```
1 //Example 3.15 Cruise Control Transfer Function.
2 // Coefficients of numerator and denominator of the
      transfer function
3
4 clear;
5 clc;
6 //
7 // Transfer function coefficients
8 \text{ num} = [0.001 0];
9 \text{ den} = [0 \ 0.05 \ 1];
10
11 // Transfer function
12 Ns=poly(num, 's', 'coeff');
13 Ds=poly(den,'s','coeff');
14 sys=syslin('c', Ns/Ds);
15
16 //gain (K) pole (P) and zeros (Z) of the system
17 temp=polfact(Ns);
18 Z=roots(Ns); //locations of zeros
19 P=roots(Ds); //locations of poles
20 K=temp(1); //first entry is always gain
21 disp(K, "Gain", P, "Poles", Z, "Zeros",)
22
23 //
```

check Appendix AP 1 for dependency:

#### Scilab code Exa 3.16 DC Motor Transfer Function

```
1 //Example 3.16 DC Motor Transfer Function.
3 xdel(winsid())//close all graphics Windows
4 clear;
5 clc;
6 //
7 // Coefficients of numerator and denominator of the
     transfer function
8 numb=[100];
9 denb=[0 101 10.1 1];
10
11 // Transfer function
12 Ns=poly(numb, 's', 'coeff');
13 Ds=poly(denb, 's', 'coeff');
14 sysb=syslin('c', Ns/Ds);
15
16 //gain (K) pole (P) and zeros (Z) of the system
17 temp=polfact(Ns);
18 Z=roots(Ns); //locations of zeros
19 P=roots(Ds); //locations of poles
20 K=temp(1); //first entry is always gain
21 disp(K, "Gain", P, "Poles", Z, "Zeros",)
22
23 //Transient response of DC Motor (consider velocity
     as output)
24 s = %s;
25 t=linspace(0,5,501);
y = csim('step',t,sysb*s)
27 plot(t,y)
```

#### Scilab code Exa 3.17 Transformations

```
1 //Example 3.17 Transformations
3 clear;
4 clc;
5 //
6 // Coefficients of numerator and denominator of the
      transfer function
7 \text{ numG} = [9 3];
8 denG=[25 6 1];
10 // Transfer function
11 Ns=poly(numG, 's', 'coeff');
12 Ds=poly(denG,'s','coeff');
13 sysG=syslin('c', Ns/Ds);
14
15 //gain (K) pole (P) and zeros (Z) of the system
16 temp=polfact(Ns);
17 Z=roots(Ns); //locations of zeros
18 P=roots(Ds); //locations of poles
19 K=temp(1); //first entry is always gain
```

```
20 disp(K, "Gain", P, "Poles", Z, "Zeros",)
21 //
```

Scilab code Exa 3.18 Satellite Transfer Function

```
1 //Example 3.18 Satellite Transfer Function
3 xdel(winsid())//close all graphics Windows
4 clear;
5 clc;
6 //
7 //(a)
8 //Given
9 d=1 //meters
10 I=5000 / Kg-meter^2
11
12 // Coefficients of numerator and denominator of the
     transfer function
13 // of satellite
14 numG=[d/I 0];
15 denG=[0 0 1];
16
17 // Transfer function
18 Ns=poly(numG, 's', 'coeff');
19 Ds=poly(denG,'s','coeff');
20 sysG=syslin('c', Ns/Ds);
21 t=0:0.01:10;
22 [i j]=size(t);
23
24 / /
```

```
25 //(b)
26 // Thrust input after 5 sec.
27 \quad u=zeros(1,j);
28 \text{ w=find}(t>=5 \& t<=5+0.1);
29 u(w) = 25;
30 plot(t,u);
31 exec .\fig_settings.sci; //custom script for setting
       figure properties
32 title ("Transient response of the satellite ...
    (a) Thrust input", 'fontsize', 3);
33
34 xlabel('Time t (sec.)', 'fontsize',2)
35 ylabel('Fc', 'fontsize', 2)
36
37 //Transient response of the satellite to the thrust
      input as a pulse
38 sysd=dscr(sysG,0.01); //sample data system model
39 \text{ y=flts}(u,sysd);
                            //impulse response
40 figure, plot(t,y*180/%pi);
41 exec .\fig_settings.sci; //custom script for setting
       figure properties
42 title ("Transient response of the satellite (double-
      pulse)...
    (b) satellite attitude", 'fontsize', 3);
43
44 xlabel('Time t (sec.)', 'fontsize',2)
45 ylabel('\$\theta(deg)\$', 'fontsize',2)
46 //
47 // Thrust input double-pulse.
48 \quad u=zeros(1,j);
49 \text{ w1} = \text{find}(t > = 5 \& t < = 5 + 0.1);
50 u(w1) = 25;
51 \text{ w2=find}(t>=6.1 \& t<=6.1+0.1);
52 u(w2) = -25;
53 figure,
54 plot(t,u);
55 exec .\fig_settings.sci; //custom script for setting
```

```
figure properties
56 title ("Transient response of the satellite (double-
      pulse)...
    (a) Thrust input", 'fontsize', 3);
57
58 xlabel('Time t (sec.)', 'fontsize',2)
59 ylabel('Fc', 'fontsize', 2)
60
61 //Transient response of the satellite to the thrust
      input as a pulse
62 sysd=dscr(sysG,0.01); //sample data system model
63 y=flts(u,sysd); //impulse response
64 figure, plot(t,y*180/%pi);
65 exec .\fig_settings.sci; //custom script for setting
       figure properties
66 title ("Transient response of the satellite (double-
      pulse)...
    (b) satellite attitude", 'fontsize', 3);
67
68 xlabel('Time t (sec.)', 'fontsize',2)
69 ylabel('\$ \land theta(deg)\$', 'fontsize', 2)
70
71 //
```

#### Scilab code Exa 3.21 Transfer function of a simple system

```
1 //Example 3.21
2 //Series, Parallel and Feedback connections of TF
         blocks
3 //to get effective TF.
```

```
7 //
8 //Transfer function block G1
9 num1 = [2];
10 den1=[1];
11 Ns=poly(num1, 's', 'coeff');
12 Ds=poly(den1, 's', 'coeff');
13 sysG1=syslin('c', Ns/Ds);
14
15 //Transfer function block G2
16 num2=[4];
17 den2=[0 1];
18 Ns = poly(num2, 's', 'coeff');
19 Ds=poly(den2, 's', 'coeff');
20 sysG2=syslin('c', Ns/Ds);
21
22 //Transfer function block G4
23 num4=[1];
24 \text{ den4} = [0 1];
25 Ns=poly(num4, 's', 'coeff');
26 Ds=poly(den4, 's', 'coeff');
27 sysG4=syslin('c',Ns/Ds);
28
29 //Transfer function block G6
30 \quad \text{num6} = [1];
31 \, \text{den6} = [1];
32 Ns = poly(num6, 's', 'coeff');
33 Ds=poly(den6, 's', 'coeff');
34 sysG6=syslin('c', Ns/Ds);
35
36 // Effective transfer function
37 // (+) operator for paralle connection,
38 // (*) operator for series connection
```

39 // (/.) operator for feedback connection 40 sysG=(sysG1 + sysG2) \* sysG4 /. sysG6

5 clear;
6 clc;

```
41 disp(sysG, "The effective transfer function is")
42 //
     check Appendix AP 1 for dependency:
     fig_settings.sci
   Scilab code Exa 3.22 Response Versus Pole Locations Real Roots
1 //Example 3.22 Response Versus Pole Locations, Real
      Roots
3 xdel(winsid())//close all graphics Windows
4 clear;
5 clc;
6 //
7 //Transfer function
8 \text{ numH} = [1 2];
9 denH=[2 3 1];
10 Ns=poly(numH, 's', 'coeff');
11 Ds=poly(denH,'s','coeff');
12 sysH=syslin('c', Ns/Ds);
13
14 //Pole-zero locations
15 // Partial fraction method to see the effect of
      sperated poles
16 temp=polfact(Ds);
17 p1s=temp(2);
18 p2s=temp(3);
19
20 //residues at poles
```

21 r1=residu(Ns,p1s,p2s);

```
22 \quad r2 = residu(Ns, p2s, p1s);
23
24 // Note that -H1(s)+H2(s)=H(s)
25 H1s=syslin('c',r1/p1s);
26 H2s=syslin('c',r2/p2s);
27
\frac{1}{28} //impulse response of the \frac{1}{3} H1(s), H2(s) and H(s)
29 t = 0:0.02:10;
30 h1=csim('impuls',t,H1s);
31 h2=csim('impuls',t,H2s);
32 h=csim('impuls',t,sysH);
33 figure,
34 plot(t,h1,'r--',t,h2,'m-.', t, h, 'b')
35 plot(t,h2, 'm-.')
36 plot(t,h)
37
38 exec .\fig_settings.sci; //custom script for setting
       figure properties
39 title(['impulse response of the system and
      subsystems with ...
40
    independent poles.'; '(h1(t) is faster than h2(t))'
       ], 'fontsize', 3)
41 xlabel('Time t (sec.)', 'fontsize',2)
42 ylabel('h(t), h1(t), h2(t)', 'fontsize',2)
43 h=legend('h1(t) with pole at -2', 'h2(t) with pole at
       -1, ...
44 , 'h(t)=h1(t)+h2(t)'
45 h.legend_location = "in_upper_right"
46 h.fill_mode='off'
47 //
```

fig\_settings.sci

#### Scilab code Exa 3.23 Oscillatory Time Response

```
1 //Example 3.23 Oscillatory Time Response
3 xdel(winsid())//close all graphics Windows
4 clear;
5 clc;
6 //
7 //Transfer function of second order underdamped
      system
8 \text{ numH} = [1 2];
9 denH=[5 2 1];
10 Ns = poly(numH, 's', 'coeff');
11 Ds=poly(denH, 's', 'coeff');
12 sysH=syslin('c', Ns/Ds);
13
14 //damping factor (xi) and natural frequency (wn)
15 [wn xi] = damp(sysH);
16 wn=wn(1);
17 xi=xi(1);
18 sigma=xi*wn;
19 wd=wn*sqrt(1-xi^2);
20
21 //denominator in sigma-wn form H(s)=H1(s)+H2(s)
22 s = \%s;
23 p = (s + sigma)^2 + wd^2
24 temp=polfact(Ns);
25 \text{ k=temp}(1), zr=temp(2);
26 \text{ h1=(s+sigma)/p};
27 h2 = -((s+sigma) - temp(2))*wd/p;
28 H1s=syslin('c',k*h1);
29 H2s = syslin('c', k*h2/wd);
```

```
30
31 // responses with exponential envelope
32 Env=syslin('c',k/(s+sigma));
33 t=0:0.02:10;
34 //impulse response
35 ht=csim('impuls',t,sysH);
36 envt=csim('impuls',t,Env);
37 envt_neg=csim('impuls',t,-Env);
38
39 plot(t,ht)
40 plot(t, envt, 'r---')
41 plot(t, envt_neg, 'r---')
42 exec .\fig_settings.sci; //custom script for setting
       figure properties
43 title('Impulse response of the underdamped system','
      fontsize',3)
44 xlabel('Time t (sec.)', 'fontsize',2)
45 ylabel('h(t)', 'fontsize',2)
46 xset ("font",1,2)
47 xstring(1,0.75,"e^{-\sin a t}",0,0)
48 xstring(1,-0.85,"-e^{-\sin a t}",0,0)
49 //
```

fig\_settings.sci

Scilab code Exa 3.25 Aircraft Response

```
1 //Example 3.25 Aircraft Response
2 xdel(winsid())//close all graphics Windows
3 clear;
```

```
4 clc;
5 //
6 //(a) impulse response of aircraft
8 //Transfer function of aircraft
9 numG = [-6 \ 1];
10 denG=[0 13 4 1];
11 Ns=30*poly(numG, 's', 'coeff');
12 Ds=poly(denG, 's', 'coeff');
13 u=-1 //impulsive elevator input of 1 degree
14 sysG=syslin('c',u*Ns/Ds);
15
16 //impulse response
17 t=0:0.02:10;
18 gt=csim('impuls',t,sysG);
19 plot(t,gt)
20 exec .\fig_settings.sci; //custom script for setting
       figure properties
21 title ('Response of an airplanes altitude to an
      impulsive elevator input', 'fontsize', 3)
22 xlabel('Time (sec.)', 'fontsize',2)
23 ylabel('Altitude (ft)', 'fontsize',2)
24
25 //final value theorem, \lim s = >0 in s*G(s)
26 \text{ s=\%s};
27 gt_final=horner(s*sysG,0)
28 disp(gt_final,"The final value of the output
      altitude is:")
29
30 //(b) response specifications
31
32 //damping factor (xi) and natural frequency (wn)
33 [wn xi]=damp(sysG);
34 wn=wn(2);//natural frequency (wn)
```

```
35 xi=xi(2);//damping factor
36 disp(wn, xi, "Damping factor and natural frequency (
      rad)...
    of the response are:")
37
38
39 tr=1.8/wn; //rise time
40 disp(tr, "Rise time (sec) of the response is:")
41
42 sigma=xi*wn
43 ts=4.6/sigma; //settling time
44 disp(ts, "Settling time (sec) of the response is:")
45
46 Mp = exp(-xi*\%pi/sqrt(1-xi^2))
47 wd=wn*sqrt(1-xi^2);
48 \text{ tp=\%pi/wd};
49 disp(tp, Mp, "Overshoot and time of overshoot (sec)
    in the response are:")
50
51
52 //
```

fig\_settings.sci

#### Scilab code Exa 3.29 Stability versus parameter range

```
1 //Example 3.29
2 //Stability versus parameter range
3
4 xdel(winsid())//close all graphics Windows
5 clear;
```

```
7 //
8 //Stability versus parameter range
10 numT = [-1]; //zeros
11 denT = [1 \ 0 \ -6]; //poles
12 Ns=poly(numT, 's', 'roots');
13 Ds=poly(denT, 's', 'roots');
14 Gfs=syslin('c', Ns/Ds); //forward transfer function
      block
15
16 num = [1];
17 \text{ den} = [1 \ 0];
18 Ns=poly(num, 's', 'coeff');
19 Ds=poly(den,'s','coeff');
20 Hs=syslin('c', Ns/Ds); //feedback transfer function
      block
21
22 //check the step responses with the forward path
      gain K=7.5, 13, 25
23 t=0:0.02:12;
24 i = 1;
25
26 \text{ for } K = [7.5, 13, 25]
27
       sysT = (K * Gfs) /. Hs;
28
       yt(i,:)=csim('step',t,sysT);
29
       i = i + 1;
30 end
31 //Step response
32 plot(t',yt')
33 exec .\fig_settings.sci; //custom script for setting
       figure properties
34 title ("Transient response for different values of K"
      , 'fontsize', 3);
35 xlabel('Time t (sec.)', 'fontsize',2)
36 ylabel('y(t)', 'fontsize', 2)
```

6 clc;

```
37 h=legend('K=7.5', 'K=13', 'K=25')  
38 h.legend_location = "in_upper_right"  
39 h.fill_mode='off'  
40 //
```

```
fig_settings.sci
```

Scilab code Exa 3.30 Stability versus two parameter ranges

```
1 //Example 3.30
 2 //Stability versus two parameter ranges
 3 xdel(winsid())//close all graphics Windows
4 clear;
5 clc;
 6 //
7 //Stability versus parameter ranges
9 num = \begin{bmatrix} 1 & 0 \end{bmatrix}; //zeros
10 den=[-1 -2]; // poles
11  Ns=poly(num, 's', 'coeff');
12  Ds=poly(den, 's', 'roots');
13 Gfs=syslin('c', Ns/Ds); //forward transfer function
       block
14
15 num = [1];
16 den=[1 0];
17 Ns = poly (num, 's', 'coeff');
18 Ds=poly(den, 's', 'coeff');
```

```
19 Hs=syslin('c', Ns/Ds); //feedback transfer function
      block
20
21 //check the step responses with the forward, path
      gain K=7.5, 13, 25
22 t=0:0.02:12;
23 i = 1;
24 num = [5 10;1 1;0 1];
25
26 \text{ for } i=1:3
27
       den = [0 \ 1];
28
       Ns=poly(num(i,:), 's', 'coeff');
29
       Ds=poly(den,'s','coeff');
       Gcs=syslin('c',Ns/Ds); //Controller transfer
30
          function block
       sysT = Gcs * Gfs /. Hs;
31
       yt(i,:)=csim('step',t,sysT);
32
33
       i=i+1;
34 end
35
36 //Transient response for different values of K and
      Ki
37 plot(t',yt')
38 exec .\fig_settings.sci; //custom script for setting
       figure properties
39 title ("Transient response for the system", 'fontsize'
      ,3);
40 xlabel('Time t (sec.)', 'fontsize',2)
41 ylabel('y(t)', 'fontsize', 2)
42 xset("font",1,1)
43 xstring(1.4,1.05, {}^{1}K=10, K_{I}=5);
44 xstring (3.3,0.8, '$K=1, K_I=1$');
45 xstring (5.5,0.35, {}^{1}K=1, K_{I}=0)
46 //
```

### Chapter 4

### Basic properties of feedback

Scilab code Exa 4.6 PID Control of DC Motor Speed

```
1 / \text{Example } 4.6
2 //PID Control of DC Motor Speed.
3
5 //NOTE THAT—
7 //The model as given in matlab program for this
      example in the book is
9 /\text{num} = \text{Ra} * s + \text{La} * s^2;
10 //den=Ke*ki + (Ra*Ke*Ke+Ke*kp)*s + (Ra*b+Ke*Ke+Ke*kd)
      )*s^2 + Jm*La*s^3;
11
12 //this does not match to the model of DC motor given
       on page 43.
13 //Also, if we assume this model, disturbance
      response given
14 //in figure 4.13 (a)
15 //is different from expected.
```

```
16 //For instance, with P control, output should
      asymptotically go to 0
17 //for disturbance step input, because numerator is s
      (Ra + La*s)
18 //and system is type 0 (no pole at origin).
19 //i.e. y (inf)=lim s->0 s*Y(s)= s*[s(Ra + La*s)/den
      |*1/s=0;
20
  //In following code, we have considered correct
21
      model of DC motor as
22 //given on page 43. Note that, this model must have
      been used
23 //by authors of the book for
24 //step reference tracking as it is correctly shown
      in figure 4.13 (b)
25
26 / /
27 xdel(winsid())//close all graphics Windows
28 clear;
29 clc;
30
31 //
32 // System parameters
33 Jm=0.0113; // N-m-s^2/rad
34 b=0.028; // N-m-s/rad
35 La=0.1; // henry
36 Ra=0.45; // ohms
37 Kt=0.067 // n-m/amp
38 Ke=0.067; // V-sec/amp
39
40 // Controller parameters
41 \text{ kp=3};
42 ki=15; // \sec^- -1
43 kd=0.3; // \sec c
```

```
44
45 // DC Motor Transfer function as given on page 43 of
       book (edition 5)
46 //G = Kt/[Jm*La s^2 + (Jm*Ra + La*b)s + (Ra*b + Kt*Ke)]
47 s = %s;
48 num = [Kt];
49 den=[(Ra*b + Kt*Ke) (Jm*Ra + La*b) Jm*La];
50 Ns = poly(num, 's', 'coeff');
51 Ds=poly(den,'s','coeff');
52 \text{ G=syslin}('c', Ns/Ds)
53
54 //PID controller, Gc=(kd s^2 + kp s + ki)/s
55 num=[ki kp kd;ki kp 0;0 kp 0]; //numerator
      parameters of controller)
                                       //(row wise for PID
56
                                           , PI and P)
57 \text{ den} = [0 \ 1];
                                    //denominator
      parameters of controller
58 Ds=poly(den, 's', 'coeff');
                                   //denominator
      polynomial of controller
59 t=0:0.005:10;
                                  // Simulation time
60 //
61 //Step disturbance response with P, PI and PID
      controller.
62
63 \text{ for } i=1:3
64 Ns=poly(num(i,:), 's', 'coeff');//numerator polynomial
       of controller
65 sysG=syslin('c', Ns/Ds);
66 \text{ sysD=G/. sysG};
67 v(i,:) = csim('step',t,sysD);
68 end
69 plot(t',v');
70 //Title, labels and grid to the figure
71 exec .\fig_settings.sci; //custom script to set the
      figure properties
```

```
72 title ('Responses of P, PI and PID control to step
      disturbance...
    input', 'fontsize',3)
73
74 xlabel('Time t (sec.)', 'fontsize',2)
75 ylabel ('Amplitude', 'fontsize', 2)
76 hl=legend(['PID', 'PI', 'P']);
77
78 //
79 // Reference step response
80
81 figure
82 \text{ for } i=1:3
83 Ns=poly(num(i,:), 's', 'coeff');
84 Gc=syslin('c', Ns/Ds);
85 // Step reference response with P, PI and PID
      controller.
86 sysR=G*Gc/(1+G*Gc);
87 v(i,:) = csim('step',t,sysR);
88 end
89 plot(t',v')
90 //Title, labels and grid to the figure
91 exec .\fig_settings.sci; //custom script to set the
      figure properties
92 title ('Responses of PID control to step reference
      input', 'fontsize',3)
93 xlabel('Time t (sec.)', 'fontsize',2)
94 ylabel('Amplitude', 'fontsize',2)
95 hl=legend(['PID', 'PI', 'P']);
96
97 //
```

```
check Appendix AP 1 for dependency: fig_settings.sci
```

### Scilab code Exa 4.7 Discrete Equivalent

```
1 //Example 4.7
2 // Discrete Equivalent.
3 //
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
8 // Transfer function
9 s = %s;
10 num = [1 11];
11 den = [1 \ 3]
12 Us=poly(num, 's', 'coeff');
13 Es=poly(den,'s','coeff');
14 Ds=syslin('c', Us/Es);
15 sysc=tf2ss(Ds)
16
17 // Discretize the system using sampling time Ts=1 and
       Bilinear Transform
18 Ts=1;
19 sysd=cls2dls(sysc,Ts);
20
21 // Pulse transfer function
22 Dd=ss2tf(sysd)
```

```
23 disp(Dd, "Dd=")
24 disp("Note that, multiply numerator and denomintor
      each by 7...
    will give the result as in book.")
25
26 //
     check Appendix AP 1 for dependency:
     fig_settings.sci
   Scilab code Exa 4.8 Equivalent discrete controller for DC motor speed
   control
1 / Example 4.8
2 // Equivalent discrete controller for DC motor speed
      control.
3 //
4 //NOTE THAT— The system response (continuous) to
      sampled control
5 //input depends on
6 //the sampling time set for continuous signal in
      SIMULATION.
7 //In this example we consider sampling period of
      0.009 \, \mathrm{sec}
8 //to represent continuous time signal.
10
11 xdel(winsid())//close all graphics Windows
12 clear;
13 clc;
```

```
14 //
```

```
15 // Continuous time system and controller
16 // System transfer function
17 \text{ s=}\%\text{s};
18 num = [45 \ 0];
19 den=[45 14 1]
20 Nms=poly(num, 's', 'coeff');
21 Dns=poly(den, 's', 'coeff');
22 Gp=syslin('c', Nms/Dns); //system transfer function
23
24 // Controller
25
26 numDa=[6 1];
27 \text{ denDa} = [0 \ 1]
28 Nms=poly(numDa,'s','coeff');
29 Dns=poly(denDa, 's', 'coeff');
30 sysD=syslin('c',1.4*Nms/Dns); //controller transfer
      function
31
32 //Closed loop responses
33
34 \text{ num} = [1 \ 0];
35 \text{ den} = [1 \ 0];
36 Nms=poly(num, 's', 'coeff');
37 Dns=poly(den, 's', 'coeff');
38 H=syslin('c', Nms/Dns)
39
40 \text{ sysDa=Gp*sysD/.H};
41
42 //step response and control input
43 t=0:0.009:5;
44 yt=csim('step',t,sysDa); //step response
45 figure(0)
46 plot2d(t,yt,1)
47 Gu=sysD/(1+Gp*sysD);
48 ut=csim('step',t,Gu); //control input
```

```
50 plot2d(t,ut,1)
51 //
52
53 sys=tf2ss(Gp); //state space model of the system
54 con=tf2ss(sysD); //controller state space model
55
56 // discrete-time time system and controller
57
58 // Discretize the system and control with sampling
     time Ts=0.07
59 // using Bilinear Transform
60 \text{ Ts} = 0.07;
61 sysDd=cls2dls(sys,Ts); // discrete-time system state
       space model
62 conDd=cls2dls(con,Ts); // discrete-time controller
      state space model
63
64 //Pulse transfer function of system
65 Gpz=ss2tf(sysDd);
66 //Pulse transfer function of controller
67 Gcz=ss2tf(conDd);
68 //Closed loop response
69 \text{ Gz=Gpz*Gcz/(1+Gpz*Gcz)}
70 //Control input pulse transfer function
71 Guz=Gcz/(1+Gpz*Gcz)
72 \quad T=0:Ts:5;
73 r = ones(1, length(T));
74 yd=flts(r,Gz);.....//Discrete respnse to
      discrete input
75 ud=flts(r,Guz);
                              // Discrete Control input
76 //continuous response for digital input
77 t=0:0.009:5;
78 k=0;
79
80 for i=1:length(yd)
```

49 figure (1)

```
81
        for j=1:8
82
           if (k+j)>length(t) then
83
              break
84
              else
85
              YD(1,k+j)=yd(i);
86
           end
87
           end
88
        k=k+j;
89 end
90
91 yt = csim(1 - YD, t, Gp*sysD);
92 scf(0)
93 plot2d(t,yt,5);
94 scf(1)
95 plot2d2(T,ud,5);
96 //
97 // Discretize the system and control with sampling
      time Ts=0.035
98 // using Bilinear Transform
99 Ts = 0.035;
100 sysDd=cls2dls(sys,Ts); // discrete-time system state
        space model
101 conDd=cls2dls(con,Ts); // discrete-time controller
       state space model
102
103 Gpz=ss2tf(sysDd); //Pulse transfer function of
      system
104 Gcz=ss2tf(conDd); //Pulse transfer function of
       controller
105
106 //Closed loop response
107 \text{ Gz=Gpz*Gcz/(1+Gpz*Gcz)}
108 //Control input pulse transfer function
109 \text{ Guz=Gcz/(1+Gpz*Gcz)}
110 T=0:Ts:5;
111 r = ones (1, length(T));
```

```
112 yd=flts(r,Gz);.....//Discrete respnse to
       discrete input
113 ud=flts(r,Guz);
                               //Discrete Control input
114 t=0:0.009:5;
115 k=0;
116
117 for i=1:length(yd)
        for j=1:4
118
           if (k+j)>length(t) then
119
120
              break
121
              else
              YD(1,k+j)=yd(i);
122
123
           end
124
           end
125
        k=k+j;
126 end
127
128 yt = csim(1 - YD, t, Gp*sysD);
129 scf(0)
130 plot2d(t,yt,2);
131 scf(1)
132 plot2d2(T, ud, 2);
133
134 scf(0)
135 //Title, labels and grid to the figure
136 exec .\fig_settings.sci; //custom script to set the
       figure properties
137 title ('Comparision plots of Speed-control system
       with continuous...
     and discrete controllers', 'fontsize', 3)
138
139 xlabel('Time t (sec.)', 'fontsize',2)
140 hl=legend(['Continuous time', 'Discrete-time, Ts=0.07
        s '...
141 , 'Discrete-time, Ts=0.035 \text{ s'}],4);
143 //Title, labels and grid to the figure
144 exec .\fig_settings.sci; //custom script to set the
       figure properties
```

### Chapter 5

## The Root Locus Design method

```
check Appendix AP 1 for dependency:
    fig_settings.sci
```

Scilab code Exa 5.1 Root locus of a Motor Position Control

```
1 //Example 5.1
2 //Root locus of a Motor Position Control.
3
4 xdel(winsid())//close all graphics Windows 5 clear;
6 clc;
7
8 //
```

```
9
10 //System transfer function and its root locus
11
12 s=poly(0,'s');
13 Ls=1/(s*(s+1));
14
15 //Title, labels and grid to the figure
```

```
fig_settings.sci
```

11

Scilab code Exa 5.2 Root locus with respect to a plant open loop pole

```
//Example 5.2
//Root locus with respect to a plant open loop pole.

xdel(winsid())//close all graphics Windows

clear;

clc;

//System transfer function and its root locus
s=poly(0,'s');
Gs=s/(s*s+1);
```

fig\_settings.sci

Scilab code Exa 5.3 Root locus for satellite attitude control with PD control

```
1 //Example 5.3
2 //Root locus for satellite attitude control with PD
        control.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7
8 //
```

9 //System transfer function and its root locus 10

```
11     s=poly(0, 's');
12     sysS=(s+1)/(s^2);
13     evans(sysS,100)
14
15     //Title, labels and grid to the figure
16     exec .\fig_settings.sci; // custom script for setting figure properties
17     title(['Root locus for', '$L(s)=G(s)=(s+1)/s^2$'],' fontsize',3)
18     zoom_rect([-6 -3 2 3])
19     h=legend('');
20     h.visible = "off"
21
22  //
```

fig\_settings.sci

Scilab code Exa 5.4 Root locus for satellite attitude control with modified PD control or Lead compensator

```
1 //Example 5.4
2 //Root locus for satellite attitude control with modified
3 //PD control or Lead compensator.
4 
5 xdel(winsid())//close all graphics Windows clear;
7 clc;
8
```

```
9 //
```

```
10 //System transfer function and its root locus
11
12 s=poly(0, 's');
13 sysL=(s+1)/(s^2*(s+12));
14 evans (sysL, 100)
15
16 //Title, labels and grid to the figure
17 exec .\fig_settings.sci; // custom script for
      setting figure properties
18 title(['Root locus for', '$L(s)=(s+1)/s^2(s+12)$'],'
      fontsize',3)
19 zoom_rect([-6 -3 2 3])
20 h=legend(',');
21 \text{ h.visible} = "off"
22
23 //
```

fig\_settings.sci

Scilab code Exa 5.5 Root locus for satellite control with Lead compensator

```
5 clear;
6 clc;
7
8 //
9 //System transfer function and its root locus
10
11 s=poly(0, 's');
12 sysL=(s+1)/(s^2*(s+4));
13 evans (sysL)
14
15 //Title, labels and grid to the figure
16 exec .\fig_settings.sci; // custom script for
      setting figure properties
17 title(['Root locus for', \$L(s)=(s+1)/s^2(s+4)\$'],'
      fontsize',3)
18 zoom_rect([-6 -3 2 3])
19 h=legend('');
20 \text{ h.visible} = "off"
21
22 //
```

```
fig_settings.sci
```

Scilab code  $\mathbf{Exa}$  5.6 Root locus for satellite attitude control with a Transition value for the pole

```
1 //Example 5.6
2 //Root locus for satellite attitude control with a
```

```
3 //Transition value for the pole.
5 xdel(winsid())//close all graphics Windows
6 clear;
7 clc;
8
9 //
10 //System transfer function and its root locus
11
12 \text{ s=poly}(0, 's');
13 sysL=(s+1)/(s^2*(s+9));
14 evans (sysL)
15
16 // Title, labels and grid to the figure
17 exec .\fig_settings.sci; // custom script for
      setting figure properties
18 title(['Root locus for', '$L(s)=(s+1)/(s^2(s+9))$'],
      'fontsize',3)
19 zoom_rect([-6 -3 2 3])
20 h=legend(',');
21 \text{ h.visible} = "off"
22
23 //
```

fig\_settings.sci

Scilab code Exa 5.7 Root locus for satellite control with a Collocated Flexibility

```
1 / \text{Example } 5.7
2 //Root locus for satellite control with a Collocated
       Flexibility.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 \text{ clc};
7
8 //
9 //System transfer function with controller.
10
11 s=poly(0, 's');
12 NumD = (s+1);
13 DenD = (s+12);
14 D=NumD/DenD;
15
16 NumG = (s+0.1)^2+36
17 DenG=s^2*((s+0.1)^2+(6.6)^2)
18
19 G=NumG/DenG;
20
21 \quad \text{NumL} = \text{NumD} * \text{NumG};
22 DenL=DenD*DenG;
23
24 L=NumL/DenL;
25
26 zr=roots(NumL);
27 pl=roots(DenL);
28
29 //
30 //Angle of departure.
31 //Find angle of departure from pole at phi1= -0.1 +
       6.6 i
32 //(real poles don't have angle of departure,
```

```
33 //they move along real axis only)
34 //psi1 = angle [(Departing pole) - (zero at - 0.1 + 6.6i)]
35 [Mpsi1, psi1] = polar(pl(2)-zr(1))
36 psi1=real(psi1)*180/%pi;
                                        //angle in degree
37
38 //psi2 = angle [(Departing pole) - (zero at - 0.1 - 6.6i)]
      ) ]
39 [Mpsi2, psi2] = polar(pl(2)-zr(2))
40 psi2=real(psi2)*180/%pi;
                                        //angle in degree
41
42 // psi3 = angle [(Departing pole) - (zero at - 1)]
43 [Mpsi3, psi3] = polar(pl(2)-zr(3))
44 psi3=real(psi3)*180/%pi;
                                        //angle in degree
45
46 //phi2=angle [(Departing pole) - (pole at 0)]
47 [Mphi2, phi2] = polar(pl(2)-pl(4))
48 phi2=real(phi2)*180/%pi;
                                        //angle in degree
49
50 //phi3 is same as phi2, as pole is repeated at 0.
51 phi3=phi2;
52
53 //phi4=angle [(Departing pole)-(pole at - 0.1 - 6.6 i
     ) ]
54 \text{ [Mphi4, phi4]} = polar(pl(2)-pl(3))
55 phi4=real(phi4)*180/%pi;
                                        //angle in degree
56
57 //phi5=angle [(Departing pole) - (pole at - 12)]
58 \text{ [Mphi5, phi5]} = polar(pl(2)-pl(1))
59 phi5=real(phi5)*180/%pi;
                                        //angle in degree
60
61 //Therefore angle of departure phi1 at -0.1 + 6.6i
      is
  //phi1 = 180 + sum(angle to zeros) - sum(angle to
      poles)
63
64 phi1 = 180 + sum(psi1+psi2+psi3) - sum(phi2+phi3+
     phi4+phi5)
```

```
65
66 //angle contributions in figure
67 figure (0)
68 plzr(L)
69 xset ('font size', 1.5)
70 xarrows([real(pl(1));real(pl(2))],[imag(pl(1));imag(
      p1(2))],0,2)
71 \text{ xarc}(-13,1,2,2,0,phi5*64)
72 xstring (-11, 0.05, "\$ \ phi_5\$")
73
74
75 xarrows([real(zr(3));real(pl(2))],[imag(zr(3));imag(
      p1(2))],0,4)
76 xarc(-2,1,2,2,0,psi3*64)
77 xstring(-0.7,1,"\$ \setminus psi_3\$")
78
79 xarrows([real(pl(4)); real(pl(2))],[imag(pl(4)); imag(
      p1(2))],0,5)
80 xarc(-1,1,2,2,0,phi2*64)
81 xstring (0.8,0.5, "\$\phi_2,\,\phi_3\$")
82
83
84 xarrows([real(pl(3)); real(pl(2))],[imag(pl(3)); imag(
      p1(2))],0,3)
85 \text{ xarc}(-1, -6.6, 2, 2, 0, phi4*64)
86 xstring(0.8, -7, "\$\phi_4\$")
87
88 xarrows([real(zr(2));real(pl(2))],[imag(zr(2));imag(
      p1(2))],0,6)
89 \text{ xarc}(-1, -5, 2, 2, 0, psi2*64)
90 xstring (0.8, -5.5, "\$ \setminus psi_2\$")
91
92 xarrows([real(zr(1));real(pl(2))],[imag(zr(1));imag(
      pl(2))],0,24)
93 xstring (0.3, 5.5, "\$ \setminus psi_1 \$")
94 xstring (0.3, 6.5, "\$ \ phi_1 \$")
95
96 exec .\fig_settings.sci; //custom script for setting
```

```
figure properties
97 title(['Figure for computing a departure angle for'
    `$L(s) = \frac{s+1}{s+12} \frac{(s+0.1)^2+6^2}{s^2[(s+0.1)^2+6^2]}
98
       +0.1)^2+6.6^2] $ '],...
99 'fontsize',3)
100 zoom_rect([-15 -8 5 8])
101 h=legend(',');
102 \text{ h.visible} = "off"
103
104 //
105 //Root locus system transfer function with
       controller.
106 figure (1)
107 \text{ evans}(L)
108 // Title, labels and grid to the figure
109 exec .\fig_settings.sci; //custom script for setting
        figure properties
110 title(['Root locus for', 'L(s) = \frac{s+1}{s+12} \frac{s}{rac}
       \{(s+0.1)^2+6^2\}...
111 \{s^2[(s+0.1)^2+6.6^2]\} ; ], 'fontsize',3)
112 zoom_rect([-15 -8 5 8])
113 h=legend(',');
114 h.visible = "off"
115
116 //
```

```
check Appendix AP 1 for dependency:
```

```
fig_settings.sci
```

#### Scilab code Exa 5.8 Root locus for noncollocated case

```
1 //Example 5.8
2 //Root locus for noncollocated case.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7
8 //
9 //System transfer function with controller
10
11 s=poly(0, 's');
12 NumD = (s+1);
13 DenD = (s+12);
14 sysD=NumD/DenD;
15
16 NumG=1
17 DenG=s^2*((s+0.1)^2+(6.6)^2)
18
19 sysG=NumG/DenG;
20
21 NumL=NumD*NumG;
22 DenL=DenD*DenG;
23
24 sysL=NumL/DenL;
25
26 zr=roots(NumL);
27 pl=roots(DenL);
28
29 //
```

```
30 //Angle of departure.
31 //Find angle of departure from pole at phi1= -0.1 +
       6.6 i
32 //(real poles don't have angle of departure,
33 //they move along real axis only)
34
35 //psi1=angle [(Departing pole) - (zero at - 1]
36 \quad [Mpsi1, psi1] = polar(pl(2)-zr(1))
37 psi1=real(psi1)*180/%pi;
                                         //angle in degree
38
39 //phi2=angle [(Departing pole) - (pole at 0)]
40 [Mphi2, phi2] = polar(pl(2)-pl(4))
41 phi2=real(phi2)*180/%pi;
                                         //angle in degree
42
43 //phi3 is same as phi2, as pole is repeated at 0.
44 phi3=phi2;
45
  //phi4=angle [(Departing pole)-(pole at - 0.1 - 6.6 i
46
      ) ]
47 [Mphi4, phi4] = polar(pl(2)-pl(3))
48 phi4=real(phi4)*180/%pi;
                                         //angle in degree
49
50 //phi5=angle [(Departing pole) - (pole at - 12)]
51 \text{ [Mphi5, phi5]} = polar(pl(2)-pl(1))
52 phi5=real(phi5)*180/%pi;
                                         //angle in degree
53
54 //Therefore angle of departure phi1 at -0.1 + 6.6i
  //phi1 = 180 + sum(angle to zeros) - sum(angle to
      poles)
56
57 \text{ phi1} = 180 + \text{sum}(\text{psi1}) - \text{sum}(\text{phi2+phi3+phi4+phi5})
58
59 //angle contributions in figure
60 \text{ figure}(0)
61 plzr(sysL)
62 xset('font size',1.5)
```

```
63 xarrows([real(pl(1)); real(pl(2))],[imag(pl(1)); imag(
      pl(2))],0,2)
64 xarrows([real(pl(1)); -10],[0;0],0,2)
65 \text{ xarc}(-13,1,2,2,0,phi5*64)
66 xstring (-11, 0.05, "\$ \ phi_5\$")
67
68 xarrows([real(zr(1)); real(pl(2))],[imag(zr(1)); imag(
      pl(2))],0,6)
69 xarrows([real(zr(1)); -0.3],[0;0],0,6)
70 \text{ xarc}(-2,1,2,2,0,psi1*64)
71 xstring(-0.7,1,"\$\psi_1\$")
72
73 xarrows([real(pl(4));real(pl(2))],[imag(pl(4));imag(
      pl(2))],0,5)
74 xarrows([real(pl(4)); 1],[0;0],0,5)
75 xarc(-1,1,2,2,0,phi2*64)
76 xstring (0.8, 0.5, "\$ \ phi_2, \ , \ phi_3\$")
77
78 xarrows([real(pl(3));real(pl(2))],[imag(pl(3));imag(
      pl(2))],0,17)
79 xarrows([real(pl(3)); 2],[imag(pl(3));imag(pl(3))
      ], 0, 17)
80 xarc(-1.1,-5.6,2,2,0,phi4*64)
81 xstring (0.8, -5.5, "\$ \ phi_4\$")
82
83 xstring (0.3, 6.5, "\$ \ \text{phi}_1\$")
84
85 exec .\fig_settings.sci; //custom script for setting
       figure properties
86 title(['Figure to compute a departure angle for',...
87 \operatorname{L}(s) = \operatorname{frac}\{s+1\}\{s+12\} \operatorname{frac}\{1\}\{s^2[(s+0.1)]\}
       ^2+6.6^2] \ \ '],...
88 'fontsize',3)
89 zoom_rect([-15 -8 5 8])
90 h=legend('');
91 \text{ h.visible} = "off"
92
93 //
```

fig\_settings.sci

Scilab code Exa 5.9 Root locus for the system having complex multiple roots

```
1 //Example 5.9
2 //Root locus for the system having complex multiple
    roots.
3
4 xdel(winsid())//close all graphics Windows
```

```
5 clear;
6 clc;
7 //
8 //System transfer function
10 s = poly(0, 's');
11
12 NumL=1;
13 DenL=s*(s+2)*[(s+1)^2+4];
15 L=NumL/DenL;
16
17 zr=roots(NumL);
18 pl=roots(DenL);
19
20 //
21 //Angle of departure.
22 //Find angle of departure from pole at phil= -1 + 2
23 //(real poles don't have angle of departure,
24 // they move along real axis only)
25
26 //phi2=angle [(Departing pole) - (pole at 0)]
27 [Mphi1, phi1] = polar(pl(1)-pl(4))
28 phi1=real(phi1)*180/%pi;
                                         //angle in degree
29
30 // \text{phi2} = \text{angle} [(\text{Departing pole}) - (\text{pole at } -2)]
31 \text{ [Mphi2, phi2]} = polar(pl(1)-pl(3))
32 phi2=real(phi2)*180/%pi;
                                         //angle in degree
33
34 //phi2=angle[(Departing pole)-(pole at -1 - 2i)]
35 \text{ [Mphi4, phi4]} = polar(pl(1)-pl(2))
36 phi4=real(phi4)*180/%pi;
                                         //angle in degree
37
```

```
38 //Therefore angle of departure phi1 at -1 + 2i is
39 //phi3 = 180 + sum(angle to zeros) - sum(angle to
      poles)
40
41 phi3 = 180 - sum(phi1+phi2+phi4)
42
43 //angle contributions in figure
44 figure (0)
45 plzr(L)
46 xset('font size',1.5)
47 xarrows([real(pl(4)); real(pl(1))],[imag(pl(4)); imag(
      pl(1))],0,2)
48 xarrows([real(pl(4)); 1],[0;0],0,2)
49 xarc(-0.5,0.5,1,1,0,phi1*64)
50 \text{ xstring}(0.5, 0.25, "\$ \ \text{phi}_1\$")
51
52 xarrows([real(pl(3));real(pl(1))],[imag(pl(3));imag(
      pl(1))],0,5)
53 xarrows([real(pl(3)); -1.3],[0;0],0,5)
54 \text{ xarc}(-2.5, 0.5, 1, 1, 0, phi2*64)
55 xstring(-1.5, 0.25, "\$ \ phi_2\$")
56
57 xarrows([real(pl(2)); real(pl(1))],[imag(pl(2)); imag(
      pl(1))],0,17)
58 xarrows([real(pl(2)); -0.3],[-2;-2],0,17)
59 xarc(-1.5,-1.5,1,1,0,phi4*64)
60 xstring (-0.5, -1.7, "\$ \ \text{phi}_4\$")
61
62 xstring(-0.8,2,"$\phi_1$")
63
64 exec .\fig_settings.sci; //custom script for setting
       figure properties
65 title(['Figure to computing a departure angle for'
66 '$L(s)=\frac{1}{s(s+2)[(s+1)^2+4]}$'], 'fontsize',3)
67 \text{ zoom\_rect}([-4 -3 4 3])
68 h=legend('');
69 h.visible = "off"
```

```
70 //
```

```
//Root locus of system transfer function with
    controller
figure(1)
sevans(L)
// Title, labels and grid to the figure
sexec .\fig_settings.sci; // custom script for
    setting figure properties
title(['Root locus for', '$L(s)=\frac{1}{s(s+2)[(s+1)^2+4]}$']...
, 'fontsize',3)
soom_rect([-4 -3 4 3])
h=legend('');
h.visible = "off"
```

fig\_settings.sci

Scilab code Exa 5.10 Design using Lead compensator

```
1 //Example 5.10
2 //Design using Lead compensator.
3
4 xdel(winsid())//close all graphics Windows 5 clear;
6 clc;
```

```
7 //
```

```
8 //System transfer function and its root locus
10 s = poly(0, 's');
11
12 NumG=1;
13 DenG=s*(s+1);
14 NumD=(s+2);
15 DenD = (s+10);
16
17 G=NumG/DenG;
18 D=NumD/DenD;
19
20 L=G*D; //open loop transfer function
21
22 figure (0)
23 evans(L)
24 sgrid(0.5,7,6);
25
26 xstring(-2,4,"Damping=0.5",0,0)
27 \text{ xstring}(-7,4,\text{"w}=7\text{"},0,0)
28 //Title, labels and grid to the figure
29 exec .\fig_settings.sci; // custom script for
      setting figure properties
30 title('Root locus for lead design', 'fontsize',3)
31 zoom_rect([-14 -8 4 8])
32 h=legend(',');
33 h.visible = "off"
34 //
35 // Unit step response
36 //closed loop system
37 \text{ K} = 70;
38 \text{ sysc=K*L/(1+K*L)};
39 sysc=syslin('c', sysc);
```

```
40 t=linspace(0,10,1000);
41 y=csim('step',t,sysc);
42 figure(1)
43 plot(t,y);
44 title('Step response for the system with lead
      compensator', 'fontsize',3)
45 xlabel('Time (sec)', 'fontsize',2)
46 ylabel('Amplitude', 'fontsize', 2)
47 set(gca(), "grid", [0.3 0.3])
48 zoom_rect([0 0 1.8 1.4])
49 exec .\fig_settings.sci;
50
51 scf(0)
52 pl=roots(DenG*DenD+K*NumG*NumD)
                                          //closed loop
      poles at K=70;
                                         //closed loop
53 plot(real(pl), imag(pl), 'ro')
      pole-locations at K=70;
54 \text{ xstring}(-5.8, 6, "K=70", 0, 0)
55 //
```

fig\_settings.sci

Scilab code Exa 5.11 A second Lead compensation Design

```
1 //Example 5.11
2 //A second Lead compensation Design.
3
4 xdel(winsid())//close all graphics Windows
```

```
6 clc;
7 //
  //System transfer function and its root locus
9
10 s=poly(0, 's');
11
12 NumG=1;
13 DenG=s*(s+1);
14 NumD = (s+5.4);
15 DenD = (s+20);
16
17 Gs=NumG/DenG;
18 Ds=NumD/DenD;
19
               //open loop transfer function
20 \text{ Ls=Gs*Ds};
21
22 zr=roots(NumD*NumG); //open loop system zeros
23 pl=roots(DenD*DenG); //open loop system poles
24 pd=-3.5+3.5*sqrt(3)*%i; //desired pole
25
26 //Construction for placing a specific point on the
      root locus.
27 figure (0)
28 plzr(Ls)
29 plot(real(pd), imag(pd), 'ro')
30 xarrows([real(pl(1)); real(pd)],[imag(pl(1)); imag(pd)
      ],0,2)
31 xarrows([real(pl(2)); real(pd)], [imag(pl(2)); imag(pd)
      ],0,2)
32 xarrows([real(pl(3)); real(pd)], [imag(pl(3)); imag(pd)
      ],0,2)
33 xarrows([real(zr);real(pd)],[imag(zr);imag(pd)],0,6)
34 xarrows([real(zr);-3],[0;0],0,6)
35 xarc(-6.4,1,2,2,0,72.6*64)
36 xset ('font size', 1.5);
```

5 clear;

```
37 xstring(-4.7,0.5,"$\psi$")
38 exec .\fig_settings.sci; //custom script for setting
       figure properties
39 title ('Construction for placing a specific point on
      the root locus',...
40 'fontsize',3)
41 h=legend('');
42 h.visible = "off"
43 //
44 //Root locus of system transfer function with
      controller
45 figure(1)
46 evans(Ls)
47 sgrid(0.5,7,6)
48 //Title, labels and grid to the figure
49 exec .\fig_settings.sci; //custom script for setting
       figure properties
50 title(['Root locus for', 'L(s) = \frac{s+5.4}{s(s+1)}
      (s+20) \ \ \ ' \ \ , ...
51 'fontsize', 3)
52 zoom_rect([-20 -8 5 8])
53 h=legend('');
54 \text{ h.visible} = "off"
55 //
56 // Unit step response
57 //closed loop system
58
59 K=127; // from root locus gain is computed
60 \text{ sysc=K*Ls/(1+K*Ls)}
61 sysc=syslin('c', sysc);
62 t=linspace(0,10,1000);
63 y=csim('step',t,sysc);
64 figure (2)
65 plot(t,y);
```

```
66 exec .\fig_settings.sci; //custom script for setting
    figure properties
67 title(['Step response for K=127', 'and',...
68 '$ L(s)=\frac {s+5.4}{s(s+1)(s+20)}$']...
69 ,'fontsize',3)
70 xlabel('Time (sec)','fontsize',2)
71 ylabel('Amplitude','fontsize',2)
72 zoom_rect([0 0 1.8 1.4])
73
74 pl=roots(DenG*DenD+K*NumG*NumD) //closed loop poles
    at K=127;
75 scf(1)
76 plot(real(pl),imag(pl),'ro') //closed loop pole-
    locations at K=127;
77 //
```

fig\_settings.sci

Scilab code Exa 5.12 Negative root Locus for an Airplane

```
1 //Example 5.12
2 //Negative root Locus for an Airplane.
3
4 xdel(winsid())//close all graphics Windows 5 clear;
6 clc;
7
```

```
9 //
```

```
10 //System transfer function and its root locus
11
12 s=poly(0, 's');
13 Ls=-(s-6)/(s*(s^2+4*s+13));
14 evans (Ls)
15
16 //Title, labels and grid to the figure
17 exec .\fig_settings.sci; //custom script for setting
       figure properties
18 title(['Negative root locus for', \$L(s) = \frac{s-6}{s}
      (s^2+4s+13)}$'],...
19 'fontsize', 3)
20 zoom_rect([-5 -6 10 6])
21 h=legend(',');
22 \text{ h.visible} = "off"
23
24 //
```

### Chapter 6

# The Frequency Response Design Method

Scilab code Exa 6.2.b Frequency response characteristics of Lead compensator

```
(0.1 \text{ rad/sec})
16 fmax=100/2/%pi; //maximum frq. in Hz for response
      (100 \text{ read/sec})
17
18 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
19 //bode(g, fmin, fmax);
20 / OR
21 //Bode plot for frequency in rad/sec (scilab ver.
      5.5.1)
22 bode (sysD, fmin, fmax, "rad")
23
24 //
25 title('(a) Magnitude and (b) phase for the lead
      compensator',...
26 'fontsize',3)
27 exec .\fig_settings.sci; //custom script for setting
       figure properties
28
```

```
check Appendix AP 1 for dependency:

fig_settings.sci

check Appendix AP 1 for dependency:

fig_settings.sci
```

Scilab code Exa 6.3 Bode Plot for Real Poles and Zeros

```
1 / Example 6.3
2 //Bode Plot for Real Poles and Zeros.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function and its bode plot
9 K = 2000;
10 s=poly(0, 's');
11 Gs = syslin('c', (K*(s+0.5))/(s*(s+10)*(s+50)));
12
13 //The bode plot of the system
                       // mininmum frq. in rad/sec for
14 \text{ wmin} = 0.1;
      response
                      // maximum frq. in red/sec for
15 \text{ wmax} = 100;
      response
16 fmin=wmin/2/%pi
                      // mininmum frq. in Hz for
      response
                      // maximum frq. in Hz for response
17 fmax=wmax/2/\%pi
18 //
19 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
20 //bode(g, fmin, fmax)
21 / OR
22 //(Only for scilab ver. 5.5.1)
23 //Bode (frequency scale in rad/sec)
24 // or gainplot or phaseplot plot with asymptotes
25 figure (0)
26 gainplot (Gs, fmin, fmax);
27 bode_asymp(Gs,wmin,wmax);
28 xstring (0.03,22, "slope=-1(-20 db/dec)",0,0);
29 xstring(0.2,9,"slope=0",0,0);
30 xstring (3,7, "slope=-1(-20 db/dec)",0,0)
31 xstring (0.9, -8, "slope=-2(-40 \text{db/dec})", 0,0)
```

```
32 title ('Composit plots (a) magnitude plot', 'fontsize'
      ,3);
33 h=legend('');
34 exec .\fig_settings.sci; //custom script for setting
       figure properties
35 \text{ h.visible} = "off"
36 //
37
38 //phase plot for poles and zeros
39 zr=((s/0.5)+1)/s //infact this is zero and pole at
      origin.
40 zr=syslin('c', zr);
41 \text{ pl1=1/((s/10)+1)}
42 pl1=syslin('c', pl1);
43 pl2=1/((s/50)+1)
44 pl2=syslin('c', pl2);
45 figure (1)
46 phaseplot([Gs;zr;pl1;pl2],fmin,fmax);
47 xstring(5.5,-14,"\{ rac \{1 \} \{ s/0.5+1 \} \}",0,0);
48 xstring(2.8,-22,"\frac{1}{s}/frac\{1\}{s/50+1}$",0,0);
49 xstring (2.5, -60, "\frac{1}{s} frac \frac{1}{s} , 0,0);
50 xstring(1.2,-100,["Composite";"(Actual)"],0,0);
51 title ('Composit plots (b) Phase', 'fontsize', 3);
52 exec .\fig_settings.sci; //custom script for setting
       figure properties
53
54 //
55 figure (2)
56 bode (Gs, fmin, fmax, "rad"); //frequency scale n
      radians
57 bode_asymp(Gs,wmin,wmax);
58 exec .\fig_settings.sci; //custom script for setting
       figure properties
```

59 title('(c) magnitude plot and phase plot approximate

```
and actual...
60 ', 'fontsize',3)
61 xstring(2.8,-22,"$\frac{1}{s/50+1}$",0,0);
62 h=legend('');
63 h.visible = "off"
64
65 //
```

2 //Bode Plot with Complex Poles.

fig\_settings.sci

1 //Example 6.4

## Scilab code Exa 6.4 Bode Plot with Complex Poles

```
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //

8 //System transfer function and its bode plot
9 K=10;
10 s=poly(0,'s');
11 Gs=syslin('c',(K)/(s*(s^2+0.4*s+4)));
12 //The bode plot of the system
13
```

```
14 fmin=0.1/2/%pi; //mininmum frq. in Hz for response
      (0.1 \text{ rad/sec})
15 fmax=10/2/\%pi; //maximum frq. in Hz for response
      (100 read/sec)
16 //
17 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
18 //bode(g, fmin, fmax);
19 / OR
20 //Bode plot for frequency in rad/sec (scilab ver.
21 bode (Gs, fmin, fmax, 0.01, "rad")
22
23 //
24 title(['Bode plot for a transfer function with
      complex poles';...
    '(a) magnitude ...
25
26
    (b) phase'], 'fontsize',3)
27
28
```

fig\_settings.sci

Scilab code Exa 6.6 Bode Plot for Complex Poles and Zeros

```
1 //Example 6.62 //Bode Plot for Complex Poles and Zeros:
```

```
3 //Satellite with Flexible appendages.
5 xdel(winsid())//close all graphics Windows
6 clear;
7 clc;
8 //
9 //System transfer function and its bode plot
10 \quad K = 0.01;
11 s=poly(0, 's');
12 NumG = K * (s^2 + 0.01 * s + 1);
13 DenG=s^2*((s^2/4)+0.02*(s/2)+1)
14 sysG=syslin('c', NumG/DenG);
15
16 fmin=0.09/2/%pi; //mininmum frq. in Hz for response
      (0.1 \text{ rad/sec})
  fmax=11/2/%pi; //maximum frq. in Hz for response
      (100 read/sec)
18
  //
19 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
20 //bode(g, fmin, fmax);
21 / OR
22 //Bode plot for frequency in rad/sec (scilab ver.
      5.5.1)
23 bode (sysG, fmin, fmax, 0.01, "rad")
25 //
26 title(["Bode plot for a transfer function with
      complex ...
27 poles and zeros"; "(a) magnitude (b) phase"], '
      fontsize',3)
28 //
```

```
29
30 disp('NOTE: Result of the above example can be verified by checking the figures shown in example 6.5')
```

## Scilab code Exa 6.7 Computation of Kv

```
1 / Example 6.7
2 //Computation of velocity error constant Kv from
      Bode plot
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function and its bode plot
9 K = 10;
10 s = poly(0, 's');
11 Gs=syslin('c',(K)/(s*(s+1)));
12 //The bode plot of the system
13
14 fmin=0.01/2/%pi; //mininmum frq. in Hz for response
      (0.1 \text{ rad/sec})
15 fmax=10/2/%pi; //maximum frq. in Hz for response
      (100 read/sec)
16 //
```

```
17 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
18 //bode(g, fmin, fmax);
19 / OR
20 //Bode plot for frequency in rad/sec (scilab ver.
      5.5.1)
21 bode (Gs, fmin, fmax, 0.01, "rad")
22 title(['Determination of Ky from the Bode plot for
      the system',...
  \$10/[s(s+1)]\$'], 'fontsize',3)
23
24 //choose frequency (rad) and magnitude from bode
      plot and calculate Kv
\frac{25}{\text{Here at w}} = 0.01, magnitude in db is M=60
26 //i.e actual magnitude of the reponse is |A|=10 (M
      /20)
27 \quad w = 0.01;
                 // in rad
                 // in db
28 M = 60
29 \quad A = 10^{(M/20)}
                 //actual gain
30
31 // Velocity error constant Kv=w*|A(w)|
32 Kv = w * A;
33 disp(Kv,"The Velocity error Constant from bode plot
      is: ")
34
35 // Computation of the Kv
36 [frq repf]=repfreq(Gs,fmin,fmax);
37 //frq in Hz, repf is freq. response in rectangular
      form.
38 //From bode plot, Kv=w*|A(w)|
39 //i.e Kv=2*pi*f*|A(2*pi*f)|
40
41 idx=1;//selecting the frequency and response at that
       frequency from arrays
42 Kv=2*%pi*frq(idx)*abs(repf(idx))
43 disp(Kv,"The Velocity error Constant is computed at
      0.0015915 \text{ Hz } (0.01 \text{ rad/sec}) : ")
44 //
```

```
check Appendix AP 1 for dependency: fig_settings.sci
```

Scilab code Exa 6.8 Nyquist plot for a second order system

```
1 / Example 6.8
2 // Nyquist plot for a second order system.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function and its root locus
9 s=poly(0, 's');
10 g=1/(s+1)^2;
11 sysG=syslin('c',g);
12
13 evans(sysG);
14 exec .\fig_settings.sci; //custom script for setting
       figure properties
15 f=gca();
16 f.x_location = "origin"
17 f.y_location = "origin"
18 title(['Root locus of', 'G(s)=1/(s+1)^2', 'with
      respect to K'],...
19 'fontsize', 3)
20 \text{ zoom\_rect}([-3,-2,2,3])
21 h=legend('');
22 \text{ h.visible} = "off"
```

```
23 //
```

```
24 figure (1)
25 //The bode plot of the system
26 fmin=0.01/2/%pi; //mininmum frq. in Hz for response
      (0.1 \text{ rad/sec})
27 fmax=100/2/%pi; //maximum frq. in Hz for response
      (100 \text{ read/sec})
28
29 //Bode plot for frequency in Hz (scilab ver. 5.4.1)
30 //bode(g, fmin, fmax);
31 / OR
32 //Bode plot for frequency in rad/sec (scilab ver.
      5.5.1)
33 bode(sysG,fmin,fmax,0.01,"rad")
34 title(['Open loop bode plot for', 'G(s)=1/(s+1)^2',
     ], 'fontsize', 3);
35 exec .\fig_settings.sci; //custom script for setting
      figure properties
36 //
37
38 figure (2)
39 //The nyquist plot of the system
40 nyquist(sysG);
41 title ('Nyquist plot of the evaluation of KG(s) for
     s=C1 and K=1,...
42 , 'fontsize', 3);
43 exec .\fig_settings.sci; //custom script for setting
      figure properties
44 f=gca();
45 f.x_location = "origin"
46 f.y_location = "origin"
47 xset('color',2)
48 //
```

```
Scilab code Exa 6.9 Nyquist plot for a third order system
1 //Example 6.9
2 // Nyquist plot for a third order system.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s=poly(0, 's');
10 g=syslin('c',1/(s*(s+1)^2));
11
12 //The bode plot of the system
13 fmin=0.01/2/\%pi;
14 fmax = 100/2/\%pi;
15 //[frq, repf] = repfreq(g1, fmin, fmax, 0.01);
16 bode(g,fmin,fmax,"rad");
17 frq=[1,10]/2/%pi;
18 [frq, repf]=repfreq(g,frq);
19 [db, phi]=dbphi(repf);
20 plot(frq*2*%pi,db,'ro');
21 exec .\fig_settings.sci; //custom script for setting
       figure properties
```

fig\_settings.sci

```
22 title(["Bode plot for","G(s)=1/[s(s+1)^2]"],
       fontsize',3)
23 / zoom_rect([[0.1 \ 0] \ -70 \ [12 \ -180] \ 20])
24 xset ("font size", 3);
25
26 xstring(1,0,"C\setminus,\, (\omega=1)$",0,0);
27 xstring(2,-75,"$E\,\,\,\(\omega=10)$",0,0);
28 f=gca();
29
30 //
31 //The nyquist plot of the system
32 figure;
33 \text{nyquist}(g, 0.8/2/\%\text{pi}, 10/2/\%\text{pi}, 0.02)
34
35 exec .\fig_settings.sci; //custom script for setting
       figure properties
36 title(["Nyquist plot for", "G(s)=1/[s(s+1)]^2"], '
       fontsize',3)
37 f=gca();
38 f.x_location = "origin";
39 f.y_location = "origin";
40 \text{ zoom\_rect([-1 -0.2 0.5 0.2]);}
41 xset("clipping", -1.2, 0.2, 1.4,0.4);
42 xset("font size", 3);
43 xset("color",2);
44 xstring(-0.6,0.1," \{ \lceil fgcolor \{ blue \} \{ \rceil \} \} ",0,0)
45 xstring(-0.6, -0.1, " {\fgcolor{blue}{\omega>0}}$"
  xstring(-0.7,0.005," {\fgcolor{blue}{\omega=\pm 1}}$
46
      ",0,0);
47 xstring(-1,-0.2,...
48 "\{ \lceil g color \{ blue \} \{ \lceil text \{ From \rceil infty at \rceil each = 0^+ \} \} 
      ",0,0);
    xstring(-0.7,0.15,"${\fgcolor{blue}...
49
    {\det \{Towards \mid infty \ at \mid omega=0^-\}}",0,0);
50
```

```
51 xstring(-0.525,-0.04,"C",0,0);
52 xstring(-0.075,0,"E",0,0);
53 //
```

fig\_settings.sci

1 //Example 6.10

Scilab code Exa 6.10 Nyquist plot for an Open loop unstable system

```
2 // Nyquist plot for an Open-loop unstable system.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s=poly(0, 's');
10 sysG=(s+1)/(s*(s/10-1));
11 evans (sysG,50)
12 exec .\fig_settings.sci; //custom script for setting
      figure properties
13 title(["Root Locus for","G(s)=(s+1)/[s(s/10-1)]$"],
     'fontsize',3)
14 zoom_rect([-5 -4 5 4])
15 f=gca();
16 f.x_location = "origin"
```

```
17 f.y_location = "origin"
18 h = legend('');
19 h.visible = "off"
20
21 g1=syslin('c',(s+1)/(s*(s/10-1)));
22 //
23 //The bode plot of the system
24 figure;
25 bode(g1,0.1/2/%pi,100/2/%pi,"rad")
26 exec .\fig_settings.sci; //custom script for setting
       figure properties
27 title(["Bode plot for","G(s)=(s+1)/[s(s/10-1)]"],
      fontsize',3)
28 //bode(g,2*\%pi*0.1,2*\%pi*100)
29 / /
30 figure;
31 //The nyquist plot of the system
32 nyquist(g1,0.5/2/%pi,100/2/%pi,0.05)
33 exec .\fig_settings.sci; //custom script for setting
       figure properties
34 title(["Nyquist plot for", "G(s)=(s+1)/[s(s/10-1)]$"
      ], 'fontsize', 3)
35 f=gca();
36 f.x_location = "origin";
37 f.y_location = "origin";
38 zoom_rect([-2 -2 1 2]);
39 xset("color",2);
40 xset("font size", 3);
41 xstring(-1,1.5," \{ \lceil fgcolor \{ blue \} \{ \rceil \} \} \}",0,0);
42 xstring(-1,-1.5," \{ \setminus fgcolor \{ blue \} \{ \setminus omega < 0 \} \} \}",0,0);
43 xstring(-1.5,0," {\fgcolor{blue}{\omega=\pm\sqrt}
      \{10\}\}\} %",0,0);
44 xstring(-0.5,0.1," {\fgcolor{blue}{\omega=\infty}}$"
      ,0,0);
```

```
45 xarrows([-0.2;0],[0.2;0],-1,2)
46 //
```

```
check Appendix AP 1 for dependency: fig_settings.sci
```

Scilab code Exa 6.11 Stability properties for a conditionally stable system

```
1 //Example 6.11
2 // Stability properties for a conditionally stable
      system.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 \text{ s=poly}(0, 's');
10 Gs=(s+10)^2/(s^3);
11 evans (Gs, 100)
12 exec .\fig_settings.sci; //custom script for setting
       figure properties
13 zoom_rect([-40 -20 5 20])
14 title(["Root locus for", "G(s)=(s+10)^2/s^3"],
      fontsize',3)
15 h=legend('');
16 h.visible = "off"
```

fig\_settings.sci

Scilab code Exa 6.12 Nyquist plot for a system with Multiple Crossover frequencies

```
6 clc;
7 //
8 //System transfer function
9 s=poly(0, 's');
10 K=85;
11 g1=K*(s+1)/(s^2*(s^2+2*s+82));
12 g2=(s^2+2*s+43.25)/(s^2+2*s+101);
13
14 Gs=syslin('c',g2*g1);
15 //
16 figure;
17 //The nyquist plot of the system
18 nyquist (Gs, 0.5/2/%pi, 100/2/%pi, 0.005)
19 title(["Nyquist plot for the complex system";...
20 "$G(s)=85(s+1)(s^2+2s+43.25)/[((s^2+2s+82)(s^2+2s))]
      +101)] $"],...
21 'fontsize',3)
22 exec .\fig_settings.sci; //custom script for setting
       figure properties
23 \text{ zoom\_rect([-2 -1 0.6 1])}
24 f=gca();
25 f.x_location = "origin";
26 f.y_location = "origin";
27 xset("color",2);
28 //
29 //The bode plot of the system
30 gm=g_margin(Gs);
31 pm=p_margin(Gs)
32 disp(pm, "Phase margin", gm, "Gain margin")
33 figure(1)
34 bode (Gs, 0.01/2/%pi, 100/2/%pi, 0.01)
35 title(["Bode plot for";...
```

13 //The bode plot of the system

fig\_settings.sci

12

Scilab code Exa 6.13 Use of simple design criterion for spacecraft attitude control

```
//Example 6.13
// Use of simple design criterion for spacecraft
attitude control.

xdel(winsid())//close all graphics Windows
clear;
clc;
///
system transfer function
s=poly(0,'s');
G=1/s^2;
g1=syslin('c',G);
```

```
14 zoom_rect([0.01 -20 100 60])
15 bode (g1,0.05/2/%pi,2/2/%pi,"rad")
16 exec .\fig_settings.sci; //custom script for setting
       figure properties
17 title ('Magnitude of the spacecrafts frequency','
      fontsize',3)
18 //
19
20 \text{ K=1};
21 Td=20;
22 \text{ Ds} = (\text{Td} * \text{s} + 1);
23 gd1=syslin('c',K*Ds*G);
24
25 ///The bode plot of compnenstaed open loop system
26 figure
27 bode (gd1,0.01/2/%pi,1/2/%pi,"rad")
28 exec .\fig_settings.sci; //custom script for setting
       figure properties
29 title('Bode plot for compensated open-loop transfer
      function'...
30 , 'fontsize', 3)
31 xstring (0.02,70,"-40db/decade",0,0);
32 xstring (0.2,40,"-20db/decade",0,0);
33
34 //The bode plot of compnenstaed closed loop system
35 \text{ K=0.01};
36 \text{ gc1}=K*\text{gd1}/(1+K*\text{gd1});
37 gcl1=syslin('c',gc1);
38 figure
39 bode (gcl1,0.01/2/%pi,10/2/%pi,"rad")
40 title ('Closesd loop frequency response', 'fontsize'
      , 3)
41 exec .\fig_settings.sci; //custom script for setting
       figure properties
42
43 //Bandwidth
```

```
44 [frq, repf, splitf] = repfreq(gc1,[0.01/2/%pi
      :0.001:10/2/%pi]);
45 [db, phi]=dbphi(repf);
46 \text{ w=find}(db \le db(1) - 3);
47 \text{ wc=w(1)};
48 \text{ frqc=frq(wc)*2*\%pi;}
49
50 plot2d3(frqc,db(wc),5)
51
52 [r c] = size(frq(1:w(1)));
53 magn=db(wc)*ones(r,c)
54 plot(frq(1:w(1))*2*%pi,magn,"b--")
55 temp_db=db(w);
56 [r c] = size(db(w));
57 temp_w=frqc*ones(r,c);
58 plot(temp_w,temp_db,"b--")
59 xset("font size", 3);
60 xstring(0.04, -16, "\$ \setminus omega_{-}\{BW\}\$");
61 xstring(frqc,-4,"-3db");
62 xset("line style",4)
63 xarrows([0.01;frqc],[-10;-10],-0.2,5)
64 xarrows([frqc;0.01],[-10;-10],-0.2,5)
65 //
66 //Step response of PD compnensation
67 figure
68 t=0:0.5:100;
69 v = csim('step',t,gcll);
70 \text{ plot2d(t,v)}
71
72 //Title, labels and grid to the figure
73 exec .\fig_settings.sci; //custom script for setting
       figure properties
74 title('Step response for PD compensation', 'fontsize'
      , 3)
75 xlabel('Time t (sec.)', 'fontsize',2)
76 ylabel('$\theta$', 'fontsize',2)
```

```
77 //
```

check Appendix AP 1 for dependency:
fig\_settings.sci

Scilab code Exa 6.14 Lead compensation for DC motor

```
1 //Example 6.14
2 //Lead compensation for DC motor.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s=poly(0,'s');
10 g=1/s/(s+1);
11 K=10; //DC gain
12 KGs = syslin('c', K*g);
13
14 //Lead compensator
15 numD=s/2+1;
16 \text{ denD=s/10+1};
17 D=numD/denD;
18 Ds=syslin('c',D);
19
20 KGDs=Ds*KGs; //compensated system
```

```
21 //
```

```
\frac{22}{a} //(a) The bode plot of the system
23 bode([KGs;KGDs],0.1/2/%pi,100/2/%pi,['KG(s)';'D(s)G(
      s)'],"rad");
24 exec .\fig_settings.sci; //custom script for setting
       figure properties
25 title ('Frequency response of lead compensation
      design', 'fontsize',3)
26
27 //root locus
28 figure(1)
29 evans (KGDs/K)
30 xset ("font size", 3);
31 xstring(-10,4,"KD(s) = \frac{s}{2+1} \frac{s}{10+1} ",0,0)
32 xstring(-10,2,"G(s) = \frac{1}{s(s+1)}",0,0)
33
34 //Title, labels and grid to the figure
35 exec .\fig_settings.sci; // custom script for
      setting figure properties
36 title('Root locus for lead compensation design','
      fontsize',3)
37 zoom_rect([-14 -8 4 8])
38 f=gca();
39 f.x_location = "origin";
40 f.y_location = "origin";
41 h=legend('');
42 h.visible = "off"
43 / /
44 //(b) digital version of lead compensator
45 // Discretize the system using sampling time Ts=0.05
      and Bilinear Transform
                    //in book its 0.005, which may not
46 \text{ Ts} = 0.05;
      give expected responses
47 D=tf2ss(KGDs/K/g);
```

```
48 sysD=cls2dls(D,Ts);
49
50 //Pulse transfer function
51 Ddz=ss2tf(sysD)
52 disp(Ddz, "Ddz=")
53
54 //
55 //(c) Compare step and ramp responses.
56 //step response switch sw=1 and for ramp response sw
57 //
58
59 //step response
60 \text{ sw=1};
61 importXcosDiagram(".\Ex6_14_model.xcos")
62
63 xcos_simulate(scs_m,4);
64 scs_m.props.context
65 figure,
66 	 al=newaxes();
67 a1.axes_bounds=[0,0,1.0,0.5];
68 plot(time_resp.time,time_resp.values)
69
70 xlabel('time');
71 ylabel('y');
72 title(["Lead-compensation design (a) step Response
    (b) ramp response"], 'fontsize', 3)
73
74 exec .\fig_settings.sci; //custom script for setting
       figure properties
  legend ("continuous controller", "digital controller"
76 //
```

```
77 //ramp response
78 \text{ sw} = 0;
79 importXcosDiagram(".\Ex6_14_model.xcos")
80
81 xcos_simulate(scs_m,4);
82 scs_m.props.context
83
84 \quad a2=newaxes();
85 a2.axes_bounds=[0,0.5,1.0,0.5];
86 plot(time_resp.time, time_resp.values)
87
88 xlabel('time');
89 ylabel('y');
90 title("(b)", 'fontsize',3)
91 exec .\fig_settings.sci; //custom script for setting
       figure properties
  legend ("continuous controller", "digital controller"
93 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 6.15 Lead compensation for Temperature Control System

```
1 //Example 6.15
2 //Lead compensation for Temperature Control System.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s = poly(0, 's');
10 numG=1;
11 denG=(s/0.5+1)*(s+1)*(s/2+1);
12 \text{ sysG=numG/denG};
13 //Dc gain
14 K = 9;
15
16 KGs = syslin('c', K*sysG);
17
18 //Lead compensator 1
19 numD=s+1;
20 \text{ denD=s/3+1};
21 D1=numD/denD;
22 D1s=syslin('c',D1);
23
24 KGD1s=D1s*KGs; //compensated system
25
26 //Lead compensator 2
27 \text{ numD=s/1.5+1};
28 \text{ denD=s/15+1};
29 D2=numD/denD;
30 D2s = syslin('c', D2);
31
32 KGD2s=D2s*KGs; //compensated system
33
34 //The bode plot of the system with K
35 bode([KGs; KGD1s; KGD2s],0.1/2/%pi,10/2/%pi,['KG';'
      KGD1'; 'KGD2'], "rad");
```

```
36 exec .\fig_settings.sci; // custom script for
      setting figure properties
37 title('Bode plot for lead compensation design','
      fontsize',3)
38 //
39 // Margins of uncompensated and compensated systems
40 [gm1, wcg1] = g_margin(KGs);
41 [pm1, wcp1]=p_margin(KGs);
42 disp(wcp1*2*%pi,"Wcp",wcg1*2*%pi,"Wcg",pm1,...
43 "Phase margin", gm1, "Gain margin", ...
44 "Uncompensated system:")
45
46 [gm2, wcg2] = g_margin(KGD1s);
47 [pm2, wcp2]=p_margin(KGD1s);
48 disp(wcp2*2*%pi,"Wcp",wcg2*2*%pi,"Wcg",pm2,...
49 "Phase margin", gm2, "Gain margin", ...
50 "System with D1 compensator:")
51
[gm3,wcg3]=g_margin(KGD2s);
53 [pm3, wcp3]=p_margin(KGD2s);
54 disp(wcp3*2*%pi,"Wcp",wcg3*2*%pi,"Wcg",pm3,...
55 "Phase margin", gm3, "Gain margin", ...
56 "System with D2 compensator:")
57 //
58 //step response comparison
59 //closed loop system
60 \text{ Gc1}=\text{KGD1s}/(\text{KGD1s}+1);
61 \text{ Gc2=KGD2s/(KGD2s+1)};
62 figure;
63 t=0:0.05:20;
64 v1 = csim('step',t,Gc1);
```

65 v2=csim('step',t,Gc2); 66 plot2d([t',t'],[v1',v2'])

67

```
68 //Title, labels and grid to the figure
69 exec .\fig_settings.sci; //custom script for setting
    figure properties
70 title('Step response for lead compensation design','
        fontsize',3)
71 xlabel('Time t (sec.)','fontsize',2)
72 ylabel('y','fontsize',2)
73
74 xset("font size", 3);
75 xarrows([2.5;1.5],[1.3;1.2],-1,1)
76 xstring(2.5,1.3,"D2",0,0)
77 xstring(4,1.2,"D1",0,0)
78 //
```

fig\_settings.sci

Scilab code Exa 6.16 Lead compensation for Servomechanism System

```
1 //Example 6.16
2 //Lead compensation for Servomechanism System.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

8 //System transfer function

```
9 s=poly(0, 's');
10 numG=10;
11 denG=s*(s/2.5+1)*(s/6+1);
12 G=numG/denG;
13 //Dc gain
14 K = 1;
15
16 KGs = syslin('c', K*G);
17
18 //Lead compensator 1
19 numD=s/2+1;
20 \text{ denD=s/20+1};
21 D1=numD/denD;
22 D1s=syslin('c',D1);
23
24 KGD1s=D1s*KGs; //compensated system
25
26 //Lead compensator 2
27 \text{ numD} = s/4+1;
28 \text{ denD=s/40+1};
29 D2=D1*numD/denD; //double compensator
30 D2s = syslin('c', D2);
31
32
33 KGD2s=D2s*KGs; //compensated system
34
35 //The bode plot of the system with K
36 bode([KGs; KGD1s; KGD2s],0.1/2/%pi,100/2/%pi,['KG';'
     KGD1'; 'KGD2'], "rad");
37 exec .\fig_settings.sci; //custom script for setting
       figure properties
38 title('Bode plot for lead compensation design','
      fontsize',3)
39 //
40 // Margins of uncompensated and compensated systems
```

41 [gm1, wcg1] = g\_margin(KGs);

```
42 [pm1, wcp1]=p_margin(KGs);
43 disp(wcp1*2*%pi,"Wcp",wcg1*2*%pi,"Wcg",pm1,...
44 "Phase margin", gm1, "Gain margin", "Uncompensated
       system :")
45
46 [gm2, wcg2] = g_margin(KGD1s);
47 [pm2, wcp2]=p_margin(KGD1s);
48 disp(wcp2*2*%pi,"Wcp",wcg2*2*%pi,"Wcg",pm2,...
49 "Phase margin", gm2, "Gain margin", "System with D1
       compensator :")
50
[gm3, wcg3] = g_margin(KGD2s);
52 [pm3, wcp3]=p_margin(KGD2s);
53 \operatorname{disp}(\operatorname{wcp3*2*\%pi}, \operatorname{"Wcp"}, \operatorname{wcg3*2*\%pi}, \operatorname{"Wcg"}, \operatorname{pm3}, \dots)
54 "Phase margin", gm3, "Gain margin", "System with D2
       compensator:")
55 //
```

fig\_settings.sci

Scilab code Exa 6.17 Lag compensation for Temperature Control System

```
1 //Example 6.17
2 //Lag compensation for Temperature Control System.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

```
8 //System transfer function
9 s=poly(0, 's');
10 numG=1;
11 denG=(s/0.5+1)*(s+1)*(s/2+1);
12 G=numG/denG;
13 //Dc gain
14 K=3; //to set phase requirement
15
16 KGs = syslin('c', K*G);
17
18 //Lag compensator
19 numD = 5*s+1;
20 \text{ denD} = 15 * s + 1;
21 D=3*numD/denD;
22 \quad Ds = syslin('c', D);
23
24 KGDs=Ds*KGs; //compensated system
25
26 //The bode plot of the system with K
27 bode([KGs; KGDs],0.01/2/%pi,10/2/%pi,['KG';'KGD'],"
      rad");
28 exec .\fig_settings.sci; //custom script for setting
       figure properties
29 title ('Frequency response of lag-compensation design
      ', 'fontsize', 3)
30
31 //
32 // Margins of uncompensated and compensated systems
33 [gm1, wcg1]=g_margin(KGs);
34 [pm1, wcp1]=p_margin(KGs);
35 disp(wcp1*2*%pi,"Wcp",wcg1*2*%pi,"Wcg",pm1,"Phase
      margin",...
36 gm1, "Gain margin", "Uncompensated system:")
37
38 [gm2, wcg2] = g_margin(KGDs);
39 [pm2, wcp2] = p_margin(KGDs);
```

```
40 disp(wcp2*2*%pi,"Wcp",wcg2*2*%pi,"Wcg",pm2,"Phase
      margin",...
41 gm2, "Gain margin", "Compensated system :")
42
43 //
44 //step response
45 //closed loop system
46 Gc = KGDs / (KGDs + 1);
47 figure;
48 t=0:0.05:20;
49 \text{ v=csim}('step',t,Gc);
50 \text{ plot2d(t,v)}
51
52 //Title, labels and grid to the figure
53 exec .\fig_settings.sci; //custom script for setting
       figure properties
54 title('Step response for lag compensation design','
      fontsize',3)
55 xlabel('Time t (sec.)', 'fontsize',2)
56 ylabel('y', 'fontsize',2)
57 //
```

```
check Appendix AP 1 for dependency:
```

fig\_settings.sci

Scilab code Exa 6.18 Lag compensation for DC motor

```
1 //Example 6.18
2 //Lag compensation for DC motor.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s = poly(0, 's');
10 g=1/s/(s+1);
11 K=10; //DC gain
12 KGs = syslin('c', K*g);
13
14 //Lag compensator
15 numD=10*s+1; //0.1
16 denD=100*s+1; //0.01
17 D=numD/denD;
18 Ds=syslin('c',D);
19
20 KGDs=Ds*KGs; //compensated system
21
22 //The bode plot of the system
^{23} bode([KGs;KGDs],0.001/2/%pi,10/2/%pi,[^{\prime}KG(s)^{\prime};^{\prime}D(s)G
      (s)'],"rad");
24 exec .\fig_settings.sci; // custom script for
      setting figure properties
  title ('Frequency response of lag-compensation design
    of DC motor', 'fontsize',3)
26
27
28 //step response
29 //closed loop system
30 \text{ Gc} = \text{KGDs} / (\text{KGDs} + 1);
```

31 figure;

```
32 t=0:0.05:50;
33 v=csim('step',t,Gc);
34 plot(t,v,2)
35
36 //Title, labels and grid to the figure
37 exec .\fig_settings.sci; // custom script for
        setting figure properties
38 title('Step response for Lag-compensation design...
39 of DC motor', 'fontsize',3)
40 xlabel('Time t (sec.)', 'fontsize',2)
41 ylabel('y', 'fontsize',2)
42 //
```

fig\_settings.sci

Scilab code Exa 6.19 PID compensation design for spacecraft attitude control

```
8 //System transfer function
9 s=poly(0, 's');
10 G1 = (0.9/s^2);
11 G2=(2/(s+2));
12 G = G1 * G2;
13 Gs = syslin('c',G);
14
15 // PID controller parameters
16 Td_{inv}=0.1; // Td_{inv}=1/Td=0.1
17 Kd=1/Td_inv; //Kd=Td=Td_inv (derivative gain)
18
19 Ti_{inv} = 0.005; // Ti_{inv} = 1/Ti = 0.005
20 Ki=Ti_inv; //Ki=Ti_inv (integral gain)
21
22 Kp=0.05 //Kp (Proportional gain)
23
D=Kp*(Kd*s+1)*(Ki/s+1); //PID Compensator
25
26 Dsc=syslin('c',D);
27
28 Ds=syslin('c',D/Kp); //PID Compensator with Kp=1
29 // Compensated system with Kp=1
30 \quad GDs = Gs * Ds;
31 //PID compensated system Kp=0.05;
32 \quad GDsc=Gs*Dsc;
33 //
34 //The bode plots
35 bode([Gs;GDs;GDsc],0.01/2/%pi,100/2/%pi,...
36 ['G(s)'; 'D(s)G(s) with Kp=1'; 'D(s)G(s) with Kp=1
      =0.05) '], "rad");
37 exec .\fig_settings.sci; //custom script for setting
       figure properties
38 title('Compensation for PID design', 'fontsize',3)
39
40 //Phase margin of pid compensated system with Kp
      =0.05;
```

```
[pm wcp]=p_margin(GDsc);
42
43 //
44 //closed loop system
45 //step response
46 \text{ Gc=GDsc/(GDsc+1)};
47 figure;
48 t=0:0.05:40;
49 y=csim('step',t,Gc);
50 plot(t,y,2)
51
52 //Title, labels and grid to the figure
53 exec .\fig_settings.sci; //custom script for setting
       figure properties
54 title ('Step response for PID compensation of
      spacecraft'...
55 , 'fontsize', 3)
56 xlabel('Time t (sec.)', 'fontsize',2)
57 ylabel('$theta$', 'fontsize',2)
58 //
59 //step disturbance response
60 Gc=G1/((G1*G2*D)+1);
61 Gcs=syslin('c',Gc);
62 figure;
63 t=0:0.5:1000;
64 u=0.1*ones(1,length(t));
65 \text{ y=csim}(u,t,Gcs)
66 plot(t,y,2)
67
68 //Title, labels and grid to the figure
69 exec .\fig_settings.sci; // custom script for
      setting figure properties
70 title ('Step disturbance response for PID
      compensation ...
```

```
71 of spacecraft', 'fontsize',3)
72 xlabel('Time t (sec.)', 'fontsize',2)
73 ylabel('$theta$', 'fontsize',2)
74 //
```

## Chapter 7

## State Space Design

Scilab code Exa 7.2.b Cruise control system step response

```
1 //Example 7.2
2 \ // \, {\tt Cruise \ control \ system \ step \ response} \, .
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 clc;
8 //
9 // Cruise control system parameters
10 m = 1000;
11 b=50;
12 u = 500;
13
14 // Transfer function
15 s = %s; // or
16 s=poly(0, 's');
17 sys1=syslin('c',(1/m)/(s+b/m));
18 disp(sys1)
19 //
```

```
20 F = [0 1; 0 -b/m];
21 G = [0; 1/m];
22 H = [0 1];
23 J = 0;
24 sys=syslin('c',F,G,H,J);
25 //
\frac{26}{\sqrt{\text{step response to u}}} = 500;
27 t=0:0.5:100;
v = csim('step',t,u*sys);
29 plot(t,v,2)
30
31 //Title, labels and grid to the figure
32 exec .\fig_settings.sci; // custom script for
      setting figure properties
33 title ('Responses of car velocity to a step in u', '
      fontsize',3)
34 xlabel('Time t (sec.)', 'fontsize',2)
35 ylabel('Amplitude', 'fontsize', 2)
36 //
```

fig\_settings.sci

Scilab code Exa 7.7 Analog computer Implementation

```
1 //Example 7.72 //Analog computer Implementation.
```

```
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 // State space model of the given system
9 F = [-6 -11 -6; 1 0 0; 0 1 0];
10 G = [6; 0; 0];
11 H = [0 \ 0 \ 1];
12 J=0;
13 sys_ss=syslin('c',F,G,H,J)
14 disp(sys_ss)
15 //
16 //Transfer function form
17 [d, Ns, Ds]=ss2tf(sys_ss)
18 Ns=clean(Ns);
19 G=syslin('c', Ns/Ds);
20 disp(G)
21 //
22 // convert numerator - denominator to pole - zero
      form
23 //gain (K) pole (P) and zeros (Z) of the system
24 temp=polfact(Ns);
25 Z=roots(Ns); //locations of zeros
26 P=roots(Ds); //locations of poles
27 K=temp(1); //first entry is always gain
28 disp(K, "Gain", P, "Poles", Z, "Zeros",)
29 //
```

# Scilab code Exa 7.8 Time scaling an oscillator

```
1 / \text{Example } 7.8
2 //Time scaling an oscillator.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 // State space model of an oscillator
9 wn=15000 // rad/sec
10 F = [0 1; wn^2 0];
11 G = [0; 10^6];
12 disp(G, "G", F, "F", "Given system");
13
14 //
15 // State space model of the time-scaled system for
16 // a millisecond scale w0=1e3;
17 w0=1e3; //rad/sec
18 F1=F/w0;
19 G1 = G/w0;
20 disp(G1, "G1", F1, "F1", "Time scaled system in mm");
21 //
```

Scilab code Exa 7.9 State Equations in Modal Canonical Form

```
1 / \text{Example } 7.9
2 //State Equations in Modal Canonical Form.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System transfer function
9 s=poly(0,'s');
10 g1=1/s^2;
11 g2=-1/(s^2+2*s+4);
12 Gs = g1 + g2;
13 //
14 // State space representation in modal canonical
      form
15 sys1=tf2ss(g1);
16 sys2=tf2ss(g2);
17 [F1,G1,T1] = canon(sys1.A, sys1.B)
18 H1=sys1.C*T1;
19
20 [F2,G2,T2] = canon(sys2.A, sys2.B)
21 \text{ H2=sys2.C*T2};
22
23 F=[F1 zeros(2,2); zeros(2,2) F2];
24 G=[G1;G2];
25 \text{ H=[H1,H2]};
26 J = 0;
27 disp(J, "J", H, "H", G, "G", F, "F", "System in modal
      canonical form")
28
29
    //As Y=G*U; consatnts k1 and k2 are taken out
```

from G1 and G2 will be

```
30    // multiplied to H1 and H2
31
32    // So alternately, it can be reprsented as
33    k1=-1; k2=-2;
34    F=[F1 zeros(2,2); zeros(2,2) F2];
35    G=[G1/k1; G2/k2];
36    H=[H1*k1, H2*k2];
37    J=0;
38    disp(J,"J",H,"H",G,"G",F,"F","System in modal canonical form")
39    //
```

Scilab code Exa 7.10 Transformation of Thermal System from Control to Modal Form

```
// State space representation in modal canonical
    form

T=[4 -3;-1 1]

Am=T\Ac*T;

Bm=T\Bc;

Cm=Cc*T;

Dm=Dc;

disp(Dm,"Dm",Cm,"Cm", Bm,"Bm",Am,"Am","Thermal
    System in modal canonical form")

//
```

Scilab code Exa 7.11 Poles and Zeros of Tape Drive System

```
1 //Example 7.11
2 // Poles and Zeros of Tape Drive System.
3 //Also, Transform the system into modal form
5 xdel(winsid())//close all graphics Windows
6 clear;
7 clc;
8 //
9 // State space matrices of Tape Drive System
10
11 F = [0 \ 2 \ 0 \ 0 \ 0;
12 -0.1 -0.35 0.1 0.1 0.75;
13 0 0 0 2 0;
14 0.4 0.4 -0.4 -1.4 0;
15 0 -0.03 0 0 -1];
16 G=[0 0 0 0 1]';
17 H2 = [0 \ 0 \ 1 \ 0 \ 0];
18 \text{ H3} = [0.5 \ 0 \ 0.5 \ 0 \ 0];
```

```
19 Ht = [-0.2 -0.2 0.2 0.2 0];
20 //
21 // Poles (eigen values) of the system
22 p=clean(spec(F));
23 disp(p, "Poles of Tape Drive System are")
24
25 //It requires complete state-space model.
26 sys=syslin('c',F,G,[Ht;H2;H3],[0;0;0])
27
28 // zeros of the system
29 [tr]=trzeros(sys)
30 disp(tr, "Transmission zeros of Tape Drive System are
      ")
31 //
32 // State space representation in modal canonical
      form with H3 output only.
33
34 \quad [m \quad Am1] = spec(F)
35 T1 = [1/2 -\%i/2; 1/2 \%i/2];
36 //transformation for a complex pair of eigen values.
37 \text{ temp} = \text{eye}(5,5);
38 T = [T1 zeros(2,3); zeros(3,2) eye(3,3)];
39 temp(1,1)=-1; temp(2,2)=-1; // for change in input
      output signs as desired
40 M=m*T*temp //real Modal transformation
41
42 Am = clean(M \setminus F * M);
43 Bm = clean(M \setminus G);
44 Cm = clean(H3*M);
45 \text{ Dm} = 0;
46
47 disp(Dm, "Dm", Cm, "Cm", Bm, "Bm", Am, "Am", "Tape Drive
      System in modal canonical form")
48 //
```

Scilab code Exa 7.12 Transformation of Thermal System from state description

```
1 //Example 7.12
2 //Transformation of Thermal System from state
      description
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 // State space model of Thermal System
9 s = %s;
10 F=[-7 -12; 1 0];
11 G = [1; 0];
12 H = [1 \ 2];
13 J=0;
14 sys=syslin('c',F,G,H,J)
15 //
16 // Transfer function model of Thermal System
17 [ch num den]=ss2tf(sys);
18 disp(num/den, "G=", Transfer function model of
     Thermal System")
19 //
```

Scilab code Exa 7.13 Zeros for the Thermal System from a State Description

```
1 //Example 7.13
2 //Zeros for the Thermal System from a State
      Description
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 // State space model of the given system
9 F = [-7 -12; 1 0];
10 G=[1;0];
11 H = [1 \ 2];
12 J=0;
13 sysG=syslin('c',F,G,H,J)
14 //
15 // Transfer function model
16 [d num den]=ss2tf(sysG);
17 zr=roots(num);
18 disp(zr, 'zr=');
19 // Alternately, it can be obtained as
20 zr=trzeros(sysG);
21 disp(zr, 'zr=');
22 //
```

### Scilab code Exa 7.14 Analysis of state equations of Tape Drive

```
1 //Example 7.14
2 // Analysis of state equations of Tape Drive.
3 //compute the poles, zeros and transfer function of
      Tape Drive System.
5 xdel(winsid())//close all graphics Windows
6 clear;
7 clc;
8 //
9 // State space matrices of Tape Drive System
10
11 F = [0 \ 2 \ 0 \ 0 \ 0]
12 -0.1 -0.35 0.1 0.1 0.75;
13 0 0 0 2 0;
14 0.4 0.4 -0.4 -1.4 0;
15 0 -0.03 0 0 -1];
16 G = [0 0 0 0 1];
17 H2 = [0 \ 0 \ 1 \ 0 \ 0];
18 \text{ H3} = [0.5 \ 0 \ 0.5 \ 0 \ 0];
19 Ht = [-0.2 -0.2 0.2 0.2 0];
20 //
21 //Poles (eigen values) of the system
22 p=clean(spec(F));
23
24 disp(p,"P","Poles of Tape Drive System are (for any
     output)")
25 disp("
      *************************
```

```
")
26
27
  disp("pole and zero polynomials and transfer
     function ...
29
    for a system with output H2")
30 sys2=syslin('c',F,G,H2,0);
31 [d2 num2 den2]=ss2tf(sys2);
32 \text{ N2=coeff(num2)};
33 D2=coeff(den2);
34 disp(D2,"D2",N2,"N2")
35 // zeros of the system with output H2
36 [zer2]=trzeros(sys2)
37 disp(zer2, "ZER2", "zeros are")
38 // transfer function of the system with output H2
39 G2=clean(num2/den2);
40 disp(G2, "G2(s)=N2(s)/D2(s)=")
41 disp("
     ************************
     ")
42
43 disp("pole and zero polynomials and transfer
     function for a...
   system with output H3")
44
45 sys3 = syslin('c', F, G, H3, 0);
46 [d3 num3 den3]=ss2tf(sys3);
47 N3 = coeff(num3);
48 D3=coeff(den3);
49 disp(D3,"D3",N3,"N3")
50 // zeros of the system with output H3
51 [zer3]=trzeros(sys3)
52 disp(zer3,"ZER3","zeros are")
53 // transfer function of the system with output H3
54 \quad G3 = clean (num2/den2);
55 disp(G3, "G3(s)=N3(s)/D3(s)=")
56 disp("
     ************************
     ")
```

```
57
58
59 disp("pole and zero polynomials and transfer
      function for a...
60
    system with output Ht")
61 syst=syslin('c',F,G,Ht,0);
62 [dt numt dent]=ss2tf(syst);
63 Nt=coeff(numt);
64 Dt=coeff(dent);
65 disp(Dt,"Dt",Nt,"Nt","zeros are")
66 // zeros of the system with output Ht
67 [zert]=trzeros(syst)
68 disp(zert, "ZERT")
69 // transfer function of the system with output Ht
70 Gt=clean(numt/dent);
71 \operatorname{\texttt{disp}}(\operatorname{\texttt{Gt}},\operatorname{"G(s)}=\operatorname{Nt(s)}/\operatorname{Dt(s)}=\operatorname{"})
72 disp("
       **********************
73 //
```

fig\_settings.sci

#### Scilab code Exa 7.15 Control law for a pendulum

```
1 //Example 7.15
2 //Control law for a pendulum.
3
4 xdel(winsid())//close all graphics Windows 5 clear;
6 clc;
```

```
8 //Pendulum state model;
9 \text{ w0} = 1;
10
11 F = [0 1; -w0^2 0];
12 G=[0 1];
13 H=eye(2,2); //representing x1 and x2 states as
      outputs
14 J=[0 0]';
15
16 sys=syslin('c',F,G,H,J); //open loop system
17
18 x0=[1 \ 0], //initial condition
19 t=0:0.2:7;
20 y=csim('impulse',t,sys); //open loop response
21 //
22
23 //simulation for closed loop system
24 x0=[1 \ 0], //initial condition
25
26 //control law u=-Kx;
27 K = [3*w0^2 4*w0];
28 syscl=syslin('c',(F-G*K),G,H,J); //closed loop
      system
29
30
31 t=0:0.1:7;
32 \text{ u=zeros}(1, \text{length}(t));
33 [x z]=csim(u,t,syscl,x0); //closed loop response
34 plot(t',x');
35
36 \quad u = -K * x;
37 plot(t',u'/4,'r-'); //control law u plot (scaled to
       1/4 in figure);
```

7 //

```
38 legend("x1","x2","u/4")
39
40 //Title, labels and grid to the figure
41 exec .\fig_settings.sci; //custom script for setting
        figure properties
42 title('Impulse response of undamped oscillator with
        full-state...
43 feedback(w0=1)','fontsize',3)
44 xlabel('Time t (sec.)','fontsize',2)
45 ylabel('Amplitude','fontsize',2)
46 //
```

acker\_dk.sci

1 //Example 7.16

Scilab code Exa 7.16 Ackermanns formula for undamped oscillator

```
13 H=eye(2,2); //representing x1 and x2 states as
    outputs
14 J=[0 0]';
15 //

16 //Ackermann's formula for feedback gain computation
17
18 pc=[-2 -2]; //desired poles
19 exec('./acker_dk.sci', -1);
20 [K,eig]=acker_dk(F,G,pc)
21 disp(K,"Feedback gain K=")
22 disp(eig,"Closed loop eigen values are ")
23 //
```

acker\_dk.sci

#### Scilab code Exa 7.17 How zero location affect control law

```
11
12 // State space representation
13 Ao = [-7 \ 1; -12 \ 0];
14 Bo = [1 -z0]';
15 Co = [1 \ 0];
16 Do = 0;
17
18 // Desired poles
19 Pd = [1 \ 2 \ 4];
20 Pc=roots(Pd);
21
22
23 // State feedback gain matrix for system zero at
      -2.0
24 \text{ K=ppol}(Ao,Bo,Pc)
25 disp(K, "K=", "State feeback gain for a system with
      zero at 2")
26 //
27 //Location of system Zero
28 z0 = -2.99
29 B = [1 -z0];
30 // State feedback gain matrix for system zero...
31 // at -2.99 (by ackermann's formula)
32 exec('./acker_dk.sci', -1);
33 K1=acker_dk(Ao,B,Pc)
34 disp(K1, "K1", "State feeback gain for a system with
      zero at -2.99")
35 //
```

```
check Appendix AP 2 for dependency:
acker_dk.sci
check Appendix AP 1 for dependency:
fig_settings.sci
```

## Scilab code Exa 7.18 Introducing the reference input

```
1 //Example 7.18
2 //Introducing the reference input.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //Pendulum state model;
9 \text{ w0} = 1;
10
11 F = [0 1; -w0^2 0];
12 G = [0 1];
13 H=[1 \ 0]; //representing x1 and x2 states as outputs
14 J=0;
15 n=sqrt(length(F));
16
17 //computing state feedback matrix to place poles at
      [-2 \ -2]
18 exec('./acker_dk.sci', -1);
19 K=acker_dk(F,G,[-2, -2]);
20 //
21 //augmented matrix for tracking the reference
22 A=[F G;H J];
23 N=A\[zeros(1,n) 1]';
24 \text{ Nx=N(1:n)};
25 Nu = N(n+1);
26
27 //feedforward gain (input weight)
```

```
28 Ntilde=Nu+K*Nx;
29
30 //---
31 // Alternately, it can be computed as /
32 Ntilde1=-inv(H*inv(F-G*K)*G); //
33 //--
34
35 //Closed loop system and step response
36 syscl=syslin('c',(F-G*K),G*Ntilde,H,J); //closed
     loop system
37
38 t=0:0.1:7;
39 [y x]=csim('step',t,syscl); //closed loop response
40 plot(t',x');
41
42 \quad u = -K * x + Ntilde;
43 plot(t', u', 4, 'r-'); //control law u plot (scaled to
       1/4 in figure);
44 legend("x1","x2","u/4");
45 xset('font size',3);
46 xstring (5,0.93, "x_{ss}")
47 xstring(5,0.25,"u_{-}{ss}\$")
48
49 //Title, labels and grid to the figure
50 exec .\fig_settings.sci; //custom script for setting
       figure properties
51 title ('Step response of undamped oscillator to
      reference input',...
52 'fontsize',3);
53 xlabel('Time t (sec.)', 'fontsize',2);
54 ylabel('Amplitude', 'fontsize',2);
55
56 //
```

```
acker_dk.sci
      check Appendix AP 1 for dependency:
      fig_settings.sci
   Scilab code Exa 7.19 Reference input to Type1 control system DC Motor
1 //Example 7.19
2 // Reference input to Type-1 control system: DC Motor
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
9 //Location of system Zero
10 z0=2;
12 // State space representation
13 F = [0 \ 1; 0 \ -1];
14 G = [0 1];
15 H = [1 0];
16 J = 0;
17 n=sqrt(length(F)); //order of the system
19 //computing state feedback matrix to place poles at
      assumed location \begin{bmatrix} -1 & -2 \end{bmatrix}
20 exec('./acker_dk.sci', -1);
```

11

18

21 K=acker\_dk(F,G,[-1, -2]); //assume pd=[-1 -2]

```
22 //
```

```
23 //augmented matrix for tracking the reference
24 A = [F G; H J];
25 N=A\setminus[zeros(1,n) 1];
26 Nx = N(1:n);
27 Nu = N(n+1);
28 disp(Nx,"Nx",Nu,"Nu")
29
30 //feedforward gain (input weight)
31 Ntilde=Nu+K*Nx;
32 disp(Ntilde, "N_tilde", "Input gain: N_tilde =Nu+K Nx"
      )
33 //
34 // Verify if ||y-r|| -> 0;
35
36 syscl=syslin('c',(F-G*K),G*Ntilde,H,J); //closed
      loop system
37
38 t=0:0.1:10;
39 r=ones(1,length(t));//reference input
40 [y x]=csim('step',t,syscl); //closed loop response
41
42 e=sqrt((r-y).^2) //norm of error
43 plot(t,y);
44 plot(t,r, 'm: '); //reference input
45 plot(t,e,'r-.'); //norm of error
46 xset ('font size',3);
47 xstring(3,0.83,"y")
48 xstring(2,1,"r")
49 xstring(3,0.1,"\$ | e | \$")
50 //Title, labels and grid to the figure
51 exec .\fig_settings.sci; // custom script for
      setting figure properties
52 title ('Step response of undamped oscillator to
```

```
reference input', 'fontsize',3);
53 xlabel('Time t (sec.)', 'fontsize',2);
54 ylabel('Amplitude', 'fontsize',2);
55 zoom_rect([0 -0.1 10 1.1])
56 //
```

```
check Appendix AP 2 for dependency:
acker_dk.sci
check Appendix AP 1 for dependency:
fig_settings.sci
```

Scilab code Exa 7.20 Pole Placement as a Dominant Second Order System

```
1 //Example 7.20
2 // Pole Placement as a Dominant Second-Order System
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

```
8
9 clc;
10 clear all;
11
12 // State space representation
13 F=[0 2 0 0 0; -0.10 -0.35 0.1 0.1 0.75; 0 0 0 2 0;...
14 0.4 0.4 -0.4 -1.4 0; 0 -0.03 0 0 -1];
```

```
15 G=[0 0 0 0 1]';
16 H=[0.5\ 0\ 0.5\ 0\ 0]; //Tape position at the head
17 Ht=[-0.2 -0.2 0.2 0.2 0]; //Tension output
18 J=0;
19 n=sqrt(length(F))
20 // Desired poles
21 Pc = [-0.707+0.707*\%i -0.707-0.707*\%i -4 -4 -4]/1.5;
22 //
23 // State feedback gain matrix via LQR (riccati
     equation)
24 \ Q = eye(5,5);
25 R = 1
26 // Riccati equation
27 P=riccati(F, G*inv(R)*G', Q, 'c')
28 \text{ K1} = inv(R)*G'*P
29 //
30 // State feedback gain matrix via pole-placement
31 exec('./acker_dk.sci', -1);
32 K2=acker_dk(F,G,Pc);
33 disp(K2, 'K2=', "Gain by ackermans formula");
34 / /
35 Ntilde1=-inv(H*inv(F-G*K1)*G); //input gain for LQR
      feedback gain.
36 Ntilde2=-inv(H*inv(F-G*K2)*G); //input gain for
      Ackerman's feedback gain.
37
38 syscl1=syslin('c',(F-G*K1),G*Ntilde1,H,J); //closed
      loop system with K1
  syscl2=syslin('c',(F-G*K2),G*Ntilde2,H,J); //closed
      loop system with K2
40
41 t=0:0.1:12;
```

```
42 [y1 x1]=csim('step',t,syscl1); //response of
      position head with K1
  [y2 x2]=csim('step',t,syscl2); //response of
43
      position head with K2
44
45 //plot of a position of read write head
46 plot(t,y1,"m-."); //Design via LQR
47 plot(t, y2,2); // Design via Ackerman's Formula
48
49 //Title, labels and grid to the figure
50 exec .\fig_settings.sci; // custom script for
      setting figure properties
51 title ('Step response of tape servomotor designs','
      fontsize',3);
52 xlabel('Time t (sec.)', 'fontsize',2);
53 ylabel('Tape Posotion', 'fontsize',2);
54
55 xstring(2.5,1.1,"LQR")
56 xarrows([3;4],[1.1;0.95],-1,1)
57 xstring(5,0.7,["Dominant"; "second order"])
58 xarrows ([5;4.2],[0.8;0.9],-1.5,1)
59 //
60
61 //response as a tape tension
62 \text{ yt1} = \text{Ht} * \text{x1};
63 \text{ yt2=Ht}*x2;
64
65 figure (1)
66 plot(t,yt1,"m-."); //Design via LQR
67 plot(t, yt2,2); // Design via Ackerman's Formula
68
69 //Title, labels and grid to the figure
70 exec .\fig_settings.sci; // custom script for
      setting figure properties
71 title('Tension plots for tape servomotor step
      responses', 'fontsize', 3);
```

```
72 xlabel('Time t (sec.)', 'fontsize',2);
73 ylabel('Tape Tension', 'fontsize',2);
74
75 xstring(3.5,0,"LQR")
76 xarrows([3.7;4.7],[0;0],-1)
77 xstring(6.1,-0.015,["Dominant";"second order"])
78 xarrows([6;6],[-0.013;-0.002],-1)
79 //
```

fig\_settings.sci

1 //Example 7.21

Scilab code Exa 7.21 Symmetric root locus for servo speed control

```
13 num_s=1;
14 \text{ den_s=-s+a};
15 GOs=syslin('c', nums/dens); //GO(s)
16 GO_s = syslin('c', num_s/den_s); //GO(-s)
17
18 evans (GOs)
19 evans (GO_s)
20 zoom_rect([-3 -0.1 3 0.1])
21 f=gca();
22 \text{ f.x\_location} = " \text{ origin}"
23 f.y_location = "origin"
24 xset("color",2);
25 h=legend('');
26 h.visible = "off"
27
28 //Title, labels and grid to the figure
29 exec .\fig_settings.sci; // custom script for
      setting figure properties
30 title('Symmetric root locus for a first order system
      ', 'fontsize', 3);
31 //
32 //Root locus design
33 //\text{rho} > 0; choose rho=2
34 \text{ rho}=2;
35 //optimal pole p=-sqrt(a^2+rho)
36 p = -sqrt(a^2 + rho)
37 sig=real(p);
38 omega=imag(p);
39 plot(sig,omega,'ro')
40 xstring(-2.5,0.02,["pole location at";"\$\rho=2$"])
41 xarrows([-2.2;-2.07],[0.02;0.002],-1.5,1)
42 //
```

```
acker_dk.sci
      check Appendix AP 1 for dependency:
      fig_settings.sci
   Scilab code Exa 7.22 SRL design for satellite attitude control
1 //Example 7.22
2 // SRL design for satellite attitude control
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //Transfer function for satellite attitude control
      system
9 s=poly(0, 's');
10 nums=1;
11 dens=s^2;
12 num_s=1;
13 den_s = (-s)^2;
14 GOs=syslin('c',nums/dens); //GO(s)
15 GO_s = syslin('c', num_s/den_s); //GO(-s)
16 / \text{evans} (G0s*G0\_s)
17 \text{ evans} (1/s^4)
18 zoom_rect([-3 -3 3 3])
19 f=gca();
20 \text{ f.x\_location} = "origin"
```

21 f.y\_location = "origin"

```
22 xset("color",2);
23 h=legend(',');
24 \text{ h.visible} = "off"
25
26 //Title, labels and grid to the figure
27 exec .\fig_settings.sci; //custom script for setting
       figure properties
28 title('Symmetric root locus for the satellite','
      fontsize',3);
29
30 //Root locus design
31 //choose rho=4.07 that places pole at -1+-j
32 \text{ rho} = 4.07;
33 \text{ chr_eqn} = (1+\text{rho}*\text{GOs}*\text{GO_s})
34 p = [-1 + \%i, -1 - \%i];
35 sig=real(p);
36 omega=imag(p);
37 plot(sig,omega, 'ro')
38 xstring(-2.2,0.5,["pole locations at";"\$\rho=4.07\$"
      ])
39
40 //pole-placement design;
41 sys=tf2ss(G0s);
42 exec('./acker_dk.sci', -1);
43 K=acker_dk(sys.A,sys.B,p);
44 syscl=syslin('c',(sys.A-sys.B*K),sys.B, sys.C, sys.D
45 disp(spec(syscl.A), "Closed loop eigen values");
46 //
```

```
acker_dk.sci
     check Appendix AP 1 for dependency:
     fig_settings.sci
   Scilab code Exa 7.23 SRL design for an inverted pendulum
1 //Example 7.23
2 // SRL Design for an Inverted Pendulum
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
9 //Transfer function model of Inverted Pendulum.
10 s=poly(0, 's');
12 nums = -(s+2);
13 dens = (s^2-1)
14 num_s = -(-s+2);
15 den_s = ((-s)^2 - 1)
16 GOs=syslin('c',nums/dens); //GO(s)
17 GO_s = syslin('c', num_s/den_s); //GO(-s)
18 sysGG=G0s*G0_s;
19 evans (sysGG)
```

8

11

20 title('Symmetric root locus for Inverted Pendulum')

21 zoom\_rect([-3 -2 3 2])

22 f=gca();

```
23 f.x_location = "origin"
24 f.y_location = "origin"
25 xset("color",2);
26 h=legend('');
27 \text{ h.visible} = "off"
28
29 //Title, labels and grid to the figure
30 exec .\fig_settings.sci; // custom script for
      setting figure properties
31 title('Symmetric root locus for the inverted
      pendulum', 'fontsize',3);
32 / /
33 //Root locus design
34 //choose rho=1 that places pole at -1.36+-j0.606
35 \text{ rho}=1;
36 p = [-1.36 + 0.606 * \%i, -1.36 - 0.606 * \%i];
37 sig=real(p);
38 omega=imag(p);
39 plot(sig,omega,'ro')
40 xstring(-1.25,0.5,["pole locations at";"$\rho=1$"])
41 //
42 //pole-placement design;
43 Ac = [0 \ 1; 1 \ 0]; Bc = [0 \ -1]'; Cc = [2 \ 1]; Dc = 0;
44 exec('./acker_dk.sci', -1);
45 K=acker_dk(Ac,Bc,p);
46 disp(K, "K=", spec(Ac-Bc*K), "Closed loop eigen values"
      );
47
48 //input gain calculation
49 n=sqrt(length(Ac));
50 A = [Ac Bc; Cc Dc];
51 N=A\[zeros(1,n) 1]';
52 \text{ Nx} = \text{N}(1:n);
53 \text{ Nu} = \text{N}(n+1);
```

```
54
55 //feedforward gain (input gain)
56 \text{ Ntilde=Nu+K*Nx};
57
58 //Step respose
59 t=0:0.1:4.5;
60 syscl=syslin('c',(Ac-Bc*K),Bc*Ntilde, Cc, Dc)
61 [y x]=csim('step',t,syscl); //closed loop response
62 figure,
63 plot(t,y);
64
65 //Title, labels and grid to the figure
66 exec .\fig_settings.sci; // custom script for
      setting figure properties
67 title('Step response for inverted pendulum','
      fontsize',3);
68 xlabel('Time t (sec.)', 'fontsize',2);
69 ylabel(["Position", "$x_1$"], 'fontsize', 2);
70 //
```

fig\_settings.sci

Scilab code Exa 7.24 LQR Design for a Tape Drive

```
1 //Example 7.24
2 // LQR Design for a Tape Drive
3
4 xdel(winsid())//close all graphics Windows
```

```
5 clear;
6 clc;
7 //
8 // State space model for a Tape Drive
9 F = [0 2 0 0 0; -0.10 -0.35 0.1 0.1 0.75; 0 0 0 2 0;
      0.4 \ 0.4 \ -0.4 \ -1.4 \ 0; \ 0 \ -0.03 \ 0 \ 0 \ -1];
10 G = [0 0 0 0 1];
11 H3 = [0.5 \ 0 \ 0.5 \ 0 \ 0];
12 //
13 // State feedback gain matrix via LQR (riccati
      equation)
14 // (a) Continuous LQR for rho=1
15 rho=1;
16 R1=1;
17 Q1=rho*H3'*H3;
18 // Riccati equation
19 P1=riccati(F, G*inv(R1)*G', Q1, 'c')
20 K1 = inv(R1) *G' *P1
21 disp(K1, 'K1')
22 //
23 // State feedback gain matrix via LQR (riccati
      equation)
24 // (a) Comparision in step response with rho
      =0.1,1,10.
25 \text{ rho} = 0.1;
26 R2=1;
27 \quad Q2 = rho * H3' * H3;
28 // Riccati equation
29 P2=riccati(F, G*inv(R2)*G', Q2, 'c')
30 K2 = inv(R2) *G' *P2
31
32 \text{ rho} = 10;
```

```
33 R3 = 1;
34 \ Q3=rho*H3'*H3;
35 // Riccati equation
36 P3=riccati(F, G*inv(R3)*G', Q3, 'c')
37 \text{ K3} = inv(R3) *G'*P3
38 //
39 //input gains for step reference with rho = 0.1, 1, 10.
40 Ntilde1=-inv(H3*inv(F-G*K1)*G);
41 Ntilde2=-inv(H3*inv(F-G*K2)*G);
42 Ntilde3=-inv(H3*inv(F-G*K3)*G);
43
44 //Closed loop system with rho = 0.1, 1, 10.
45 syscl1=syslin('c',(F-G*K1),G*Ntilde1,H3,0);
46 syscl2=syslin('c',(F-G*K2),G*Ntilde2,H3,0);
47 syscl3=syslin('c',(F-G*K3),G*Ntilde3,H3,0);
48
49 //step response with rho = 0.1, 1, 10.
50 t=0:0.1:12;
51 [y1 x1]=csim('step',t,syscl1); //closed loop
      response
52 [y2 x2]=csim('step',t,syscl2); //closed loop
      response
53 [y3 x3]=csim('step',t,syscl3); //closed loop
      response
54
55 figure,
56 	 a1=newaxes();
57 \quad a1.axes\_bounds = [0,0,1.0,0.5];
58 plot(t,y1);
59 plot(t, y2, 'r-.');
60 plot(t,y3, 'm: ');
61
62 //Title, labels and grid to the figure
63 exec .\fig_settings.sci; // custom script for
      setting figure properties
64 title('(a)Step response of step servo motor for LQR
```

```
Design', 'fontsize', 3);
65 xlabel('Time t (sec.)', 'fontsize',2);
66 ylabel(["Tape Position", "$x_3$"], 'fontsize', 2);
67
68 xstring(4.1,0.85,"$\rho=1$")
69 xstring (5.5,0.75, "\frac{1}{3}\rho=0.1\frac{1}{3}")
70 xstring(2.1, 1.05, "\$\rho=10\$")
71 //
72 //Tensions for the Tape
73 //For tape output is Ht = [-0.2 \ -0.2 \ 0.2 \ 0.2 \ 0];
74 Ht = [-0.2 -0.2 0.2 0.2 0];
75 H3 = Ht;
76 //input gains can not be computed because of
      singularity. so set it 1;
77 Ntilde1=1;
78 Ntilde2=1;
79 Ntilde3=1;
80
81 //Closed loop system with rho = 0.1, 1, 10.
82 syscl1=syslin('c',(F-G*K1),G*Ntilde1,H3,0);
83 sysc12=syslin('c', (F-G*K2), G*Ntilde2, H3, 0);
84 \operatorname{syscl3} = \operatorname{syslin}('c', (F-G*K3), G*Ntilde3, H3, 0);
85
86 //step response with rho = 0.1, 1, 10.
87 t=0:0.1:12;
88 [y1 x1]=csim('step',t,syscl1); //closed loop
      response
89 [y2 x2]=csim('step',t,syscl2); //closed loop
      response
90 [y3 x3]=csim('step',t,syscl3); //closed loop
      response
91
92 	 a2=newaxes();
93 a2.axes_bounds=[0,0.5,1.0,0.5];
94 plot(t,y1);
95 plot(t,y2, 'r-.');
```

fig\_settings.sci

Scilab code Exa 7.25 An estimator design for a simple pendulum

```
1 //Example 7.25
2 // An estimator design for a simple pendulum
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

8 // State space representation

```
9 \text{ w0} = 1;
10 F = [0 1; -w0^2 0];
11 G=[0 1]';
12 H = [1 \ 0];
13 J=0;
14 n=sqrt(length(F));//order of the system
15 // Desired estimator poles
16 Pe = [-10*w0 -10*w0];
17 // Observer gain matrix for system
18 Lt=ppol(F',H',Pe);
19 L=Lt';
20 disp(L,"L=");
21 //
22 //simulation for closed loop system
23 x0=[1 \ 0], //initial condition
24
25 //State feedback control law u=-Kx; (from Ex7_15)
26 \quad K = [3*w0^2 \ 4*w0];
27 //
28 //Augmented plant and observer
29 Faug=[F-G*K, zeros(n,n); L*H, F-L*H];
30 Gaug=[0 0 0 0]';
31 Haug=[H -H];
32 Jaug=0;
33
34 sys_aug=syslin('c', Faug, Gaug, Haug, Jaug);
35 t=0:0.1:4;
36 \quad u=zeros(1, length(t));
37 \times 0 = [1 \ 0 \ 0 \ 0]';
38 [x z]=csim(u,t,sys_aug,x0); //closed loop response
39 plot(t,z(1,:));
40 plot(t,z(2,:), 'm');
41 plot(t,z(3,:), 'b:');
42 plot(t,z(4,:), 'm:');
```

```
43
44  //Title , labels and grid to the figure
45  exec .\fig_settings.sci; // custom script for
        setting figure properties
46  title(['Initial condition response of oscillator
        showing',...
47  '$\mathbf{x}$', 'and', '$\hat{\mathbf{x}}$'], 'fontsize
        ',3)
48  xlabel('Time t (sec.)', 'fontsize',2)
49  ylabel('Amplitude', 'fontsize',2)
50  legend('$x_1$', '$x_2$', '$\hat{x}_1$', '$\hat{x}_2$')
51  xset('font size',2)
52  //
```

fig\_settings.sci

10  $F = [0 1; -w0^2 0];$ 

Scilab code Exa 7.26 A reduced order estimator design for pendulum

```
1 //Example 7.26
2 // A reduced order estimator design for pendulum
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 // State space representation
9 w0=1;
```

```
11 G=[0 1]';
12 H = [1 \ 0];
13 J=0;
14 n=sqrt(length(F));//order of the system
15
16 //partioned system
17 Faa=F(1,1); Fab=F(1,2);
18 Fba=F(2,1); Fbb=F(2,2);
19
20 // Desired estimator poles
21 Pe = [-10];
22 // Observer gain matrix for system
23 L=ppol(Fbb',Fab',Pe);
24 L=L';
25 disp(L,"L=");
26 //
27 //simulation for closed loop system
28 x0=[1 \ 0 \ 10], //initial condition
29
30 //State feedback control law u=-Kx; (from Ex7_15)
31 K = [3*w0^2 4*w0];
32 / /
33 //Augmented plant and observer
34 Faug=[F-G*K, zeros(n,1); Fab, L*Fab, Fbb-L*Fab];
35 Gaug=[0 0 0]';
36 Haug=[H 0];
37 J=0;
38
39 sys_aug=syslin('c', Faug, Gaug, Haug, J);
40 t = 0:0.1:4;
41 u=zeros(1,length(t));
42 [x z]=csim(u,t,sys_aug,x0); //closed loop response
43 plot(t,z(1,:), 'b');
44 plot(t,z(2,:), 'r');
```

```
45 plot(t,z(3,:),'r--');
46
47
48 //Title, labels and grid to the figure
49 exec .\fig_settings.sci; // custom script for
        setting figure properties
50 title('Initial condition response of the reduced
        order estimator', 'fontsize',3)
51 xlabel('Time t (sec.)', 'fontsize',2)
52 ylabel('Amplitude', 'fontsize',2)
53 legend('$x_1$','$x_2$','$\hat{x}_2$')
54 xset('font size',2)
55 //
```

check Appendix AP 1 for dependency:

fig\_settings.sci

1 //Example 7.27

10 G=[0 1]';

Scilab code Exa 7.27 SRL estimator design for a simple pendulum

```
// SRL estimator design for a simple pendulum

xdel(winsid())//close all graphics Windows
clear;
clc;
//

State space representation
F=[0 1; -1 0];
```

```
11 H = [1 \ 0];
12 J=0;
13
14 //Transfer function
15 sys=syslin('c',F,G,H,J)
16 sysGG=ss2tf(sys)
17
18 //Symmetric root locus for the inverted pendulum
      estimator design
19 //
20 //Root locus design
21 evans (sysGG*sysGG)
22 zoom_rect([-5 -5 5 5])
23 f=gca();
24 f.x_location = "origin"
25 f.y_location = "origin"
26 xset("color",2);
27 h=legend('');
28 h.visible = "off"
29 //Title, labels and grid to the figure
30 exec .\fig_settings.sci; // custom script for
      setting figure properties
31 title ('Symmetric root locus for inverted the
      pendulum estimator design',...
32 'fontsize',3);
33 //
\frac{34}{\text{pole locations for }} = 365; p = -3 + -j3.18
35 p = [-3+3.18*\%i -3-3.18*\%i]
36 sig=real(p);
37 omega=imag(p);
38 plot(sig,omega, 'ro')
39 xstring(-4,1,["pole location at";"q=365"])
40 xarrows([-3.5;-3.05],[2;3.1],-1.5,1)
41 //
```

```
check Appendix AP 1 for dependency:
fig_settings.sci
check Appendix AP 3 for dependency:
zpk_dk.sci
```

Scilab code Exa 7.28 Full order compensator design for satellite attitude control

```
1 //Example 7.28
2 // Full order compensator design for satellite
      attitude control.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
9 // State space representation
10 A = [0 \ 1; \ 0 \ 0];
11 B=[0 1]';
12 C = [1 0];
13 D=0;
14 n=sqrt(length(A));
15 // Desired poles for the satellite attitude control
      system.
16 Pc = [-0.707+0.707*\%i -0.707-0.707*\%i]
```

17

```
18 // State feedback gain
19 K=ppol(A,B,Pc)
20 disp(K, 'K=', "State feedback gain")
21
22 //Estimator - error roots are at
23 Pe = [-2.5+4.3*\%i -2.5-4.3*\%i]
24 L=ppol(A',C',Pe);
25 L=L';
26 disp(L, 'L=', "Observer gain")
28 //Compensator Design
29 sys1=syslin('c',A,B,C,D);
30 G=ss2tf(sys1);
31 \text{ s=poly}(0, 's');
32
33 Ds = -K * inv(s * eye(n,n) - A + B * K + L * C) * L;
34
35 exec('./zpk_dk.sci', -1);
36 [pl,zr Kp]=zpk_dk(Ds);
37 D=poly(zr,'s','roots')/poly(pl,'s','roots')
38
39 evans(G*D)
40 zoom_rect([-8 -6 8 6])
41
42 f=gca();
43 f.x_location = "origin"
44 f.y_location = "origin"
45 xset("color",2);
46 h=legend('');
47 \text{ h.visible} = "off"
48
49 //Title, labels and grid to the figure
50 exec .\fig_settings.sci; //custom script for setting
       figure properties
51 title('Root locus for combined control and estimator
      , . . .
```

```
check Appendix AP 1 for dependency:
fig_settings.sci
check Appendix AP 3 for dependency:
zpk_dk.sci
```

Scilab code Exa 7.29 A reduced order compensator design for a satellite attitude control

```
5 clear;
6 clc;
7 //
8 // State space representation
9 F = [0 1; 0 0];
10 G=[0 1]';
11 H = [1 \ 0];
12 J=0;
13 n=sqrt(length(F));//order of the system
14
15 // partioned system
16 Faa=F(1,1); Fab=F(1,2);
17 Fba=F(2,1); Fbb=F(2,2);
18 Ga=G(1); Gb=G(2);
19
20 // Desired estimator poles
21 Pe = [-5];
22 // Observer gain matrix for system
23 L=ppol(Fbb',Fab',Pe);
24 L=L;
25 disp(L,"L=");
26 //
27 //State feedback control law u=-Kx=-(K+[L*k2 \ 0])[y]
      xc]';
28 k1=1; k2=sqrt(2);
29 \text{ K=[k1 k2]};
30 \text{ Kc}=K+[L*k2 0];
31 //
32 //compensator differential equation
33 //xc_dot = (Fbb-L*Fab)*xb_hat + (Fba - L*Faa)*y + (Gb)
      - L*Ga)*u
34 //xc_{dot} = ((Fbb-L*Fab)-k2)*xc + [(Fba - L*Faa)-(Gb - L*Faa)]
```

```
L*Ga)*(k1+L*k2)+L*(Fbb-L*Fab)]*y
35 \text{ Fc} = (\text{Fbb} - \text{L} * \text{Fab}) - \text{Gb} * \text{k2}
36 \text{ Fy} = (\text{Fba} - \text{L*Faa}) - (\text{Gb} - \text{L*Ga}) * (\text{k1} + \text{k2} * \text{L}) + (\text{Fbb} - \text{L*Fab}) * \text{L}
37 //compensator transfer function
38 \text{ s=poly}(0, 's');
39 Gest=syslin('c',Fy/(s-Fc))//estimator transfer
       function
40 Dcr=-[k1+L*k2+k2*Gest]
41 disp(Dcr, 'Dcr', 'compensator transfer function')
42 //
43 //Root locus with reduced order compensator
44 G=1/s^2;
45 \text{ G=syslin}('c',G);
46 exec('./zpk_dk.sci', -1);
47 [pl,zr Kp]=zpk_dk(Dcr);
48
49 Dcr=poly(zr, 's', 'roots')/poly(pl, 's', 'roots')
50 Dcr=syslin('c',Dcr);
51 evans (G*Dcr)
52 zoom_rect([-8 -4 2 4])
53
54 f=gca();
55 f.x_location = "origin"
56 f.y_location = "origin"
57 xset("color",2);
58 h=legend('');
59 \text{ h.visible} = "off"
60
61 //Title, labels and grid to the figure
62 exec .\fig_settings.sci; //custom script for setting
        figure properties
63 title(['Root locus of a reduced order controller and
      ',"$1/s^2$",...
    "process"], 'fontsize',3);
64
65 //
```

```
// Frequency response for 1/s^2 and compensated
figure,
figure,
bode([-Kp*G*Dcr;G],0.01/2/%pi,100/2/%pi,"rad");
title(["Frequency response","$G(s)=1/s^2$", "with a reduced...
order estimator"], 'fontsize',3)
exec .\fig_settings.sci; //custom script for setting figure properties
legend('Compensated', 'Uncompensated')
//
```

```
check Appendix AP 1 for dependency: fig_settings.sci check Appendix AP 3 for dependency: zpk_dk.sci
```

Scilab code Exa 7.30 Full Order Compensator Design for DC Servo

```
1 //Example 7.30
2 // Full-Order Compensator Design for DC Servo.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

```
9 // State space representation
10 //Transfer function model for DC Servo
11 s=poly(0, 's');
12 \text{ num} = 10;
13 den=s*(s+2)*(s+8);
14 Gs=syslin('c', num/den);
15
16 // State space representation
17 F=[-10 1 0;-16 0 1;0 0 0];
18 G = [0 \ 0 \ 10]';
19 H = [1 \ 0 \ 0];
20 J = 0;
21 n=sqrt(length(F));
22 //Desired poles for the DC Servo system.
23 Pc = [-1.42 -1.04 + 2.14 * \%i -1.04 - 2.14 * \%i]
24
25
26 // State feedback gain
27 \text{ K=ppol}(F,G,Pc)
28 disp(K, 'K=', "State feedback gain")
29
30 //Estimator - error roots are at
31 Pe = [-4.25 -3.13+6.41*\%i -3.13-6.41*\%i]
32 L=ppol(F',H',Pe);
33 L=L';
34 disp(L, 'L=', "Observer gain")
35 //
36 //Compensator Design
37 DK = -K * inv(s * eye(n,n) - F + G * K + L * H) * L;
38
39 exec('./zpk_dk.sci', -1);
40 [p,z]=zpk_dk(DK);
41 D=poly(z, 's', 'roots')/poly(p, 's', 'roots')
42
43 evans (Gs*D)
```

```
44 zoom_rect([-8 -9 3 9])
45
46 f=gca();
47 f.x_location = "origin"
48 f.y_location = "origin"
49 xset("color",2);
50 h=legend('');
51 h.visible = "off"
52
53 //Title, labels and grid to the figure
54 exec .\fig_settings.sci; // custom script for setting figure properties
55 title('Root locus for DC servo pole assignment',' fontsize',3);
56 //
```

check Appendix AP 1 for dependency:

fig\_settings.sci

Scilab code Exa 7.31 Reduced Order Estimatortor Design for DC Servo

```
1 //Example 7.31
2 // Reduced-Order Estimator Design for DC Servo.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

8

```
9 // State space representation
10 //Transfer function model for DC Servo
11 s=poly(0, 's');
12 \text{ num} = 10;
13 den=s*(s+2)*(s+8);
14 Gs=syslin('c', num/den);
15 // State space representation
16 \quad F = [-10 \quad 1 \quad 0; -16 \quad 0 \quad 1; 0 \quad 0]
17 G = [0 \ 0 \ 10]';
18 H = [1 0 0];
19 J = 0;
20 n=sqrt(length(F));
21 //Desired poles for the DC Servo system.
22 Pc = [-1.42 -1.04 + 2.14 * \%i -1.04 - 2.14 * \%i]
23 // State feedback gain
24 \text{ K=ppol}(F,G,Pc)
25 disp(K, 'K=', "State feedback gain")
26
27 //
28 //Estimator - error roots are at
29 //partioned system
30 Faa=F(1,1); Fab=F(1,2:3);
31 Fba=F(3,1); Fbb=F(2:3,2:3);
32 \text{ Ga=G(1); Gb=G(2:3);}
33
34 Pe = [-4.24+4.24*\%i, -4.24-4.24*\%i]
35 // Observer gain matrix for system
36 L=ppol(Fbb',Fab',Pe);
37 L=L';
38 disp(L,"L=");
39 //
40
41 //State feedback control law u=-Kx=-(K+[L*k2 \ 0])[y]
      xc]';
```

```
42 \text{ k1=K(1)}; \text{ k2=K(2:3)};
43
44 //
45 //compensator transfer function
46 \text{ s=poly}(0, 's');
47 num = (-0.735+s)*(1.871+s);
48 den=poly([-0.990 + 6.12* \%i, -0.990 - 6.12* \%i], 's'
      , 'roots')
49 Dcr=syslin('c',num/den);
50 disp(Dcr, 'Dcr', 'compensator transfer function')
51 //
52 //Root locus with reduced order compensator
53 evans (-Dcr*Gs)
54 zoom_rect([-8 -9 3 9])
55
56 f=gca();
57 f.x_location = "origin"
58 f.y_location = "origin"
59 xset("color",2);
60 h = legend('');
61 h.visible = "off"
62
63 //Title, labels and grid to the figure
64 exec .\fig_settings.sci; // custom script for
      setting figure properties
65 title('Root locus for DC servo reduced order
      controller', 'fontsize',3);
66 //
```

check Appendix AP 2 for dependency:

```
acker_dk.sci
check Appendix AP 1 for dependency:
fig_settings.sci
check Appendix AP 3 for dependency:
zpk_dk.sci
```

#### Scilab code Exa 7.32 Redesign of the Dc servo compensator using SRL

```
1 //Example 7.32
2 // Redesign of the Dc servo compensator using SRL
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
9 // State space representation
10 //Transfer function model for DC Servo
11 s=poly(0, 's');
12 num=10;
13 den=s*(s+2)*(s+8);
14 Gs=syslin('c', num/den);
15
16 // State space representation
17 F = [-10 \ 1 \ 0; -16 \ 0 \ 1; 0 \ 0]
18 G = [0 0 10]';
19 H = [1 \ 0 \ 0];
20 J = 0;
21 n=sqrt(length(F));
22 // Desired poles for the DC Servo system.
```

23 Pc = [-2+1.56\*%i -2-1.56\*%i -8.04]

```
24
25
26 // State feedback gain
27 \text{ K=ppol}(F,G,Pc)
28 disp(K, 'K=', "State feedback gain")
29
30 //Estimator - error roots are at
31 Pe = [-4+4.49*\%i -4-4.49*\%i -9.169]
32 exec .\acker_dk.sci;
33 Lt=ppol(F',H',Pe);
34 L=clean(Lt');
35 disp(L, 'L=', "Observer gain")
36 //Error in book, Gain values are different in book.
37 //
38 //Compensator Design
39 DK = -K * inv(s * eye(n,n) - F + G * K + L * H) * L;
40 DK = syslin('c', DK)
41 exec('./zpk_dk.sci', -1);
42 [pl,zr,Kp]=zpk_dk(DK);
43 Dc=poly(zr, 's', 'roots')/poly(pl, 's', 'roots')
44 //
45 //symmetric root locus
46 G_s = horner(Gs, -s);
47 \text{ evans}(Gs*G_s)
48 zoom_rect([-10 -5 10 5])
49 f=gca();
50 \text{ f.x\_location} = "origin"
51 f.y_location = "origin"
52 xset("color",2);
53 h=legend(',');
54 h.visible = "off"
55 //Title, labels and grid to the figure
56 exec .\fig_settings.sci; //custom script for setting
       figure properties
```

```
57 title('Symmetric root locus', 'fontsize', 3);
58 //
59 //root locus
60 figure,
61 evans(Gs*Dc) //Correct root locus
62 zoom_rect([-11 -6 1 6])
63 f = gca();
64 f.x_location = "origin"
65 f.y_location = "origin"
66 xset("color",2);
67 h=legend('');
68 \text{ h.visible} = "off"
69 //Title, labels and grid to the figure
70 exec .\fig_settings.sci; // custom script for
      setting figure properties
71 title ('Root locus for pole assignment from the SRL',
      'fontsize',3);
72 //
73 // Discrete-time controller
74 nc=94.5*conv([7.98 1],[2.52 1])
75 dc=conv([59.5348 8.56 1],[10.6 1])
76 sysDc=poly(nc, 's', 'coeff')/poly(dc, 's', 'coeff');
77 sysDc_ss=syslin('c',tf2ss(sysDc));
78 \text{ ts} = 0.1;
79 sysDd=dscr(sysDc_ss,ts)
80 Gdz=ss2tf(sysDd);
81
82 disp(sysDc, "Continuous-time compensator")
83 disp(Gdz, "Discrete-time compensator")
84 //
85 //step responses
```

86 importXcosDiagram(". $\Ex7_32_model.xcos$ ")

```
87
88 xcos_simulate(scs_m,4);
89 scs_m.props.context
90 figure,
91 plot(yt.time,yt.values(:,1),2)
92 plot(yt.time,yt.values(:,2),'r--')
93 xlabel('Time (sec)');
94 ylabel('y');
95 title ("Comaprison of step responses for continuous
      and discrete ...
     controllers", 'fontsize',3)
96
97 exec .\fig_settings.sci; //custom script for setting
       figure properties
98 legend ("continuous controller", "digital controller"
       ,4)
99
100 //Control inputs
101 figure,
102 plot(ut.time, ut.values(:,1),2)
103 plot(ut.time, ut.values(:,2), 'r---')
104 xlabel('Time(sec)');
105 ylabel('u');
106 title ("Comaprison of control signals for continuous
      and discrete ...
    controllers", 'fontsize',3)
107
108 exec .\fig_settings.sci; //custom script for setting
       figure properties
109 legend("continuous controller", "digital controller")
110 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 2 for dependency:

```
acker_dk.sci
check Appendix AP 3 for dependency:
zpk_dk.sci
```

Scilab code Exa 7.33 DC servo system redesign with modified with dominant second order pole locations

```
1 //Example 7.33
2 // DC servo system redesign with modified with
         dominant second
3 // order pole locations.
4
5 xdel(winsid())//close all graphics Windows
6 clear;
7 clc;
8 //
```

```
9
10 // State space representation
11 //Transfer function model for DC Servo
12 s=poly(0, 's');
13 num=10;
14 den=s*(s+2)*(s+8);
15 Gs=syslin('c',num/den);
```

```
16
17 // State space representation
18 F = [-10 \ 1 \ 0; -16 \ 0 \ 1; 0 \ 0]
19 G = [0 \ 0 \ 10]';
20 H = [1 0 0];
21 J = 0;
22 n=sqrt(length(F));
23 // Desired poles for the DC Servo system.
24 Pc = [-1.41+1.41*\%i -1.41-1.41*\%i -8]
25
26
27 // State feedback gain
28 \text{ K=ppol}(F,G,Pc)
29 disp(K, 'K=', "State feedback gain")
30
31 //Estimator - error roots are at
32 Pe = [-4.24+4.24*\%i -4.24-4.24*\%i -8]
33 exec .\acker_dk.sci;
34 Lt=ppol(F',H',Pe);
35 L=clean(Lt');
36 disp(L, 'L=', "Observer gain")
37 // Error in book, Gain values are different in book.
38 //
39 //Compensator Design
40 DK = -K * inv(s * eye(n,n) - F + G * K + L * H) * L;
41 DK = syslin('c', DK)
42 exec('./zpk_dk.sci', -1);
43 [pl,zr,Kp]=zpk_dk(DK*10);
44 disp(zr, "zeros",pl, "Poles", Kp*10, "Gain(includung
      system gain)")
45 Dcs=poly(zr, 's', 'roots')/poly(pl, 's', 'roots')
46 disp(Dcs, 'Dcs=', "Compensator transfer function")
47 //
```

```
check Appendix AP 2 for dependency:
acker_dk.sci
check Appendix AP 1 for dependency:
fig_settings.sci
```

Scilab code Exa 7.34 Servomechanism increasing the velocity constant through zero assignment

```
1 //Example 7.34
2 // Servomechanism, increasing the velocity constant through
3 // zero assignment.
4 
5 xdel(winsid())//close all graphics Windows clear;
7 clc;
8 //
```

```
9
10  // State space representation
11  //Transfer function model for DC Servo
12  s=poly(0, 's');
13  num=1;
14  den=s*(s+1);
15  Gs=syslin('c',num/den);
16
17  // State space representation
18  F=[0 1;0 -1]
19  G=[0 1]';
20  H=[1 0];
21  J=0;
22  n=sqrt(length(F));
```

```
23 //Desired poles for the DC Servo system.
24 \text{ Pc} = [-2 -2]
25
26 // State feedback gain
27 exec .\acker_dk.sci;
28 K=acker_dk(F,G,Pc)//Gain computed in book is
      incorrect.
29 disp(K, 'K=', "State feedback gain")
30 //
31 //Overall transfer function with reduced order
      estimator.
32 \text{ Gred} = 8.32*(0.096+s)/(0.1 +s)/(8 + 4*s+s^2)
33 Gred=syslin('c',Gred)
34 disp(Gred, 'Ys/Rs'," Overall transfer function with
      reduced ...
    order estimator")
35
36
37 //Compensator
38 D = (0.096+s)*(s+1)/(4.08 +s)/(0.0196+s)
39 Ds = syslin('c', D*8.32)
40 disp(Ds, 'Ds=', "Compensator transfer function")
41 //
42 //root locus
43 figure (0)
44 evans (D*Gs,100) // Correct root locus
45 zoom_rect([-0.2 -0.1 0.1 0.1])
46 f=gca();
47 f.x_location = "origin"
48 f.y_location = "origin"
49 xset("color",2);
50 h = legend('');
51 h.visible = "off"
52 //Title, labels and grid to the figure
```

53 exec .\fig\_settings.sci; // custom script for

```
setting figure properties
54 title('Root locus of lag-lead compensation','
      fontsize',3);
55 //
56 //Bode plot
57 figure(1)
58 bode (Ds*Gs, 0.01/2/%pi, 100/2/%pi, "rad") // Correct
      root locus
59
60 f = gca();
61 h=legend('');
62 \text{ h.visible} = "off"
63 //Title, labels and grid to the figure
64 exec .\fig_settings.sci; //custom script for setting
       figure properties
65 title ('Frequency response of lag-lead compensation',
      'fontsize',3);
66 //
67 //step response of the system with lag compensation
68 t=0:0.1:5;
69 ylag=csim('step',t,8.32*Gs*D/(1+8.32*Gs*D));
70 figure
71 plot(t, ylag, 2);
72 xlabel('Time (sec)');
73 ylabel('y');
74 title ("Step response of the system with lag
      compensation", 'fontsize',3)
75 exec .\fig_settings.sci; //custom script for setting
       figure properties
76 //
77 // Discrete-time controller
78 sysDc_ss=syslin('c',tf2ss(Ds));
```

```
79 \text{ ts} = 0.1;
80 sysDd=dscr(sysDc_ss,ts)
81 Gdz=ss2tf(sysDd)
82
83 disp(Gdz, "Discrete-time compensator")
84 //
85 //step responses comparision
86 importXcosDiagram(".\Ex7_34_model.xcos")
87
88 xcos_simulate(scs_m,4);
89 scs_m.props.context
90 figure,
91 plot(yt.time,yt.values(:,1),2)
92 plot(yt.time,yt.values(:,2),'r--')
93 xlabel('Time (sec)');
94 ylabel('y');
95 title ("Comaprison of step responses for continuous
      and discrete ...
     controllers", 'fontsize',3)
96
97 exec .\fig_settings.sci; //custom script for setting
        figure properties
98 legend ("continuous controller", "digital controller"
       ,4)
99
100 //Control inputs
101 figure,
102 plot(ut.time, ut.values(:,1),2)
103 plot(ut.time, ut.values(:,2), 'r--')
104 xlabel('Time (sec)');
105 ylabel('u');
106 title ("Comaprison of control signals for continuous
      and discrete ...
     controllers", 'fontsize',3)
107
108 exec .\fig_settings.sci; //custom script for setting
        figure properties
109 legend ("continuous controller", "digital controller")
```

```
110 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 7.35 Integral Control of a Motor Speed System

```
18 G = [0 1]
19 H = [1 \ 0];
20 J = 0;
21
22 // Desired poles for augmented system
23 \text{ Pc} = [-5 -5]
24
25 // State feedback gain is
26 \text{ K=ppol}(F,G,Pc)
27 disp(K, 'K=')
28
29 //Estimator
30 \text{ Pe} = [-10]
31 L=ppol(sys.A',sys.C',Pe)
32 disp(L', 'L=')
33
34 //
35 //(c) Compare step reference and disturbance
      response.
36 //step reference response switch r=1 and w=0;
37 r=1; w=0;
38 importXcosDiagram(".\Ex7_35_model.xcos")
39 //The diagram data structure
40 xcos_simulate(scs_m,4);
41 scs_m.props.context
42 figure (0)
43 plot(yt.time,yt.values)
44 xlabel('time');
45 ylabel('y');
46
47 figure (1)
48 plot(ut.time,ut.values)
49 xlabel('time');
50 ylabel('y');
51 //
```

```
52 // Step disturbance response switch r=0 and w=1;
53 \text{ w=1; r=0;}
54 importXcosDiagram(".\Ex7_35_model.xcos")
55 //The diagram data structure
56 xcos_simulate(scs_m,4);
57 scs_m.props.context
58
59 scf(0)
60 plot(yt.time,yt.values, 'r--')
61 xlabel('time');
62 ylabel('y');
63 title("step Response", 'fontsize',3)
64 exec .\fig_settings.sci; // custom script for
      setting figure properties
65 legend("y1","y2")
66 xset('font size',3);
67 xstring(0.9,0.9,"$y_1$");
68 xstring(0.25, 0.12, "\$y_2\$");
69
70
71 scf(1)
72 plot(ut.time,ut.values, 'r--')
73 xlabel('time');
74 ylabel('y');
75 title("Control efforts", 'fontsize', 3)
76 exec .\fig_settings.sci; // custom script for
      setting figure properties
77 legend("u1","u2")
78 xset('font size',3);
79 xstring(0.25, 2.5, "\$u_1\$");
80 xstring(1,-1,"\$u_2\$");
81 //
```

169

This code can be downloaded from the website wwww.scilab.in

## Chapter 8

# Digital Control

```
check Appendix AP 1 for dependency:
    fig_settings.sci
```

Scilab code Exa 8.1 Digital Controller using tustin approximation

```
1 ///Example 8.1
2 // Digital Controller using tustin approximation.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
```

```
8 // Cntroller
9 s=poly(0,'s');
10 numD=s/2+1;
11 denD=s/10+1;
12 D=10*numD/denD;
13 Ds=syslin('c',D);
14 //sampling freq. = 25 times bandwidth
15 Wbw=10;
```

```
16 \ \text{Ws} = 25 * \text{Wbw};
17 fs=Ws/2/\%pi;
18 T=1/fs; //sampling time
19 a=1; b=-1;
20 c=1; d=1;
21 // Digital controller
22 z=poly(0, 'z');
23 Dz = horner(Ds, 2/T*(a*z+b)/(c*z+d));
24 disp(Dz, 'Digital Controller: ')
25
26 //
27 //step response and control efforts.
28 figure(0);
29 importXcosDiagram(".\Ex8_1_model.xcos")
30 //The diagram data structure
31 xcos_simulate(scs_m,4);
32 scs_m.props.context
33 plot(yt.time,yt.values(:,1), 'r--')
34 plot(yt.time,yt.values(:,2),2)
35
36 \text{ xlabel}('Time (sec.)');
37 ylabel('Position, y');
38 title(["Comparison between digital and continuous
      controller step ...
    response"; "with a sample rate 25 times bandwidth";"
39
       (a) Position "],...
    'fontsize',3);
41 exec .\fig_settings.sci; // custom script for
      setting figure properties
42
43 //control effort
44
45 figure (1);
46 plot(ut.time, ut.values(:,1), 'r--')
47 plot2d2(ut.time, ut.values(:,2),2)
48
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 8.2 Design of a Space Station Attitude Digital Controller using Discrete Equivalents

```
8 //
9 // State space representation of continuous time
      system
10 s=poly(0, 's');
11 num=1;
12 den=(s^2);
13 Gs=syslin('c', num/den);
14 Ds=0.81*(s+0.2)/(s+2);
15 Ds = syslin('c', Ds);
16 \text{ sysc=Gs*Ds};
17
18 //Root locus
19 evans (sysc)
20 \text{ zoom\_rect}([-2 -0.4 0.5 0.4])
21 f=gca();
22 f.x_location = "origin"
23 f.y_location = "origin"
24 h=legend('');
25 h.visible = "off"
26 exec .\fig_settings.sci; //custom script for setting
       figure properties
27 title('s-plane locus with respect to K', 'fontsize'
      , 3)
28
29 //Contonuous time response of the system
30 figure,
31 \text{ tc=0:0.1:30};
32 syscl=sysc/(1+sysc)
33 yc=csim("step",tc,syscl);
34 plot(tc,yc, 'b')
35 //
```

36 // Discretization of the system at

```
37 z = poly(0, 'z')
38 // sampling time Ts=1 sec
39 \text{ Ts} = 1;
40 Dz1=horner(Ds, 2/Ts*(z-1)/(z+1))
41 disp(Dz1, "Dz1=", "Discrete-time controller with Ts=1
      sec.")
42
43 // sampling time Ts=0.5 sec
44 Ts2=0.5;
45 Dz2=horner(Ds, 2/Ts2*(z-1)/(z+1))
46 disp(Dz2, "Dz2=", "Discrete-time controller with Ts
      =0.5 \text{ sec.}")
47
48 //discrete-time response of the system.
49
50 importXcosDiagram(".\Ex8_2model.xcos")
51 //The diagram data structure
52 xcos_simulate(scs_m,4);
53 //scs_m.props.context
54 plot(yt1.time,yt1.values, 'm-.') //with Ts=1sec.
55 plot(yt2.time,yt2.values,'r--') //with Ts=0.5 sec.
56 //
57
58 title('step responses of continous and digital
      implementations', 'fontsize', 3)
59
60 exec .\fig_settings.sci; // custom script for
      setting figure properties
61 xlabel('Time (sec)', 'fontsize', 2)
62 ylabel('Plant output', 'fontsize',2)
63 legend ("Continuous design", "Discrete equivalent
      design, T=1 sec."...
64 ," Discrete equivalent design, T=0.5 sec.",4)
65 //
```

This code can be downloaded from the website wwww.scilab.in

## Chapter 9

## Nonlinear Systems

```
check Appendix AP 1 for dependency:
    fig_settings.sci
```

Scilab code Exa 9.5 Changing Overshoot and Saturation nonlinearity

```
//Example 9.5
//Changing Overshoot and Saturation nonlinearity.

xdel(winsid())//close all graphics Windows
clear;
clc;
//

system transfer function and its root locus

s=poly(0,'s');
num=(s+1)
den=(s^2);
Gs=syslin('c',num/den)
//Root locus
```

```
16 \text{ evans} (Gs, 5)
17 title(["Root locus of", "(s+1)/(s^2)", "with
      saturation removed"],...
18 'fontsize', 3);
19 f=gca();
20 f.x_location = "origin"
21 f.y_location = "origin"
22 h=legend('');
23 \text{ h.visible} = "off"
24 exec .\fig_settings.sci; //custom script for setting
       figure properties
25 //
26 // Step response
27 K = 1;
28 i = [2 4 6 8 10 12];
29 figure(1);
30 importXcosDiagram(".\Ex9_5model.xcos")
31
32 for r=i
33 xcos_simulate(scs_m,4);
34 scs_m.props.context
35 plot(yt.time,yt.values)
36 end
37
38 xlabel('time');
39 ylabel('y');
40 title ("Step response of the system for various input
       sizes", 'fontsize',3);
41 exec .\fig_settings.sci; //custom script for setting
       figure properties
42
43 xset('font size',3);
44 xstring(4,2.5,"\$r=2\$");
45 xstring(6,5.5,"$4$");
46 xstring(8,8.7,"$6$");
47 xstring(10,12.2,"$8$");
```

```
48 xstring(12,15.4,"$10$");
49 xstring(14,18.4,"$12$");
50 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 9.6 Stability of conditionally stable system using root locus

```
//Example 9.6
//Stability of conditionally stable system using root locus.

xdel(winsid())//close all graphics Windows
clear;
clc;
//System transfer function and its root locus

s=poly(0,'s');
num=(s+1)^2
den=(s^3);
Gs=syslin('c',num/den)
//Root locus
```

```
14 evans (Gs, 7)
15 title(["Root locus for", "(s+1)^2/(s^3)", "for
     system"],...
16 'fontsize', 3);
17 f=gca();
18 f.x_location = "origin"
19 f.y_location = "origin"
20 h=legend('');
21 h.visible = "off"
22 exec .\fig_settings.sci; //custom script for setting
       figure properties
23 //
24 //Response of the system
25 \text{ K}=2;
26 i = [1 2 3 3.475];
27 figure(1);
28
29 importXcosDiagram(".\Ex9_6_model.xcos")
30
31 for r=i
32 xcos_simulate(scs_m,4);
33 scs_m.props.context
34 plot(yt.time,yt.values)
35 end
36
37 xlabel('Time (sec.)');
38 ylabel('Amplitude');
39 title("Step response of the system", 'fontsize', 3);
40
41 exec .\fig_settings.sci; //custom script for setting
       figure properties
42 xset('font size',3);
43 xstring(3,6.5,"\$r = 3.475\$");
44 xstring(2.5,5.2,"$3$");
45 xstring(2,3,"$2$");
46 xstring(1,1.4,"$1$");
```

```
47 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 9.7 Analysis and design of the system with limit cycle using the root locus

```
//Example 9.7
//Analysis and design of the system with limit cycle
using the root locus.

xdel(winsid())//close all graphics Windows

clear;

clc;

//System transfer function and its root locus

s=poly(0, 's');

num=0.1;

den=(s^2+0.2*s+1)*(s);

gs=syslin('c',num/den);

//Root locus
evans(Gs,40)
```

```
16 title(["Root locus of", "(0.1/s(s^2+0.2*s+1)"],"
      fontsize',3);
17 f=gca();
18 f.x_location = "origin"
19 f.y_location = "origin"
20 h=legend('');
21 h.visible = "off"
22 exec .\fig_settings.sci; // custom script for
      setting figure properties
23 //
24 //Response of the system
25 figure;
26 //Response of the system
27 \text{ K=0.5};
28 i = [1 4 8];
29 importXcosDiagram(".\Ex9_7_model.xcos")
30
31 for r=i
32 xcos_simulate(scs_m,4);
33 scs_m.props.context
34 plot(yt.time,yt.values)
35 end
36
37 \text{ xlabel}('Time (sec.)');
38 ylabel('Amplitude');
39 title("Step response of the system", 'fontsize', 3);
40 exec .\fig_settings.sci; // custom script for
      setting figure properties
41 zoom_rect([0 0 150 9])
42
43 xset('font size',3);
44 xstring(80, 1.6, "\$r=1\$");
45 xstring(80,4.6,"\$r=4\$");
46 xstring(80,8.2,"$r=8$");
47 //
```

```
48 //System with notch compensation
49 D=123*(s^2+0.18*s+0.81)/(s+10)^2;
50
51 //Root locus
52 figure,
53 evans (Gs*D, 40)
54 title(["Root locus including notch compensation"],'
      fontsize',3);
55 f=gca();
56 	ext{ f.x_location} = "origin"
57 f.y_location = "origin"
58 h=legend('');
59 \text{ h.visible} = "off"
60 exec .\fig_settings.sci; //custom script for setting
       figure properties
61 zoom_rect([-14 -2 2 2])
62 //
63 //Response of the system witth notch filter
64 figure;
65 \text{ K=0.5};
66 i = [2 4];
67 importXcosDiagram (". \times \text{Ex9-7-model-notch.xcos}")
68
69 for r=i
70 xcos_simulate(scs_m,4);
71 scs_m.props.context
72 plot(yt.time,yt.values)
73 end
74
75 xlabel('Time(sec.)');
76 ylabel('Amplitude');
77 title("Step response of the system with notch filter
      ", 'fontsize', 3);
78 exec .\fig_settings.sci; //custom script for setting
       figure properties
```

```
79 xset('font size',3);
80 xstring(30,2.2,"$r=2$");
81 xstring(34,3.75,"$r=4$");
82 //
```

This code can be downloaded from the website wwww.scilab.in This code

can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

10 //Response of the system

11 kp=2;

Scilab code Exa 9.8 Antiwindup compensation for a PI controller

```
1 //Example 9.8
2 //Antiwindup compensation for a PI controller.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //System Model
```

```
12 ki = 4;
13
14 // Without antiwindup
15 \text{ ka=0};
16 importXcosDiagram (". \times Ex9_8 - model \cdot xcos")
17 xcos_simulate(scs_m,4);
18 scs_m.props.context
19 figure (0)
20 plot(yt.time,yt.values, 'm-.')
21 figure (1)
22 plot(ut.time,ut.values, 'm-.')
23
24 //With antiwindup
25 \text{ ka=10};
26 xcos_simulate(scs_m,4);
27 scf(0)
28 plot(yt.time,yt.values)
29 exec .\fig_settings.sci; // custom script for
      setting figure properties
30 xlabel('Time (sec.)');
31 ylabel('Output');
32 title ("Integrator antiwindup (a) step response.",
      fontsize',3);
33
34
35 scf(1)
36 plot(ut.time,ut.values);
37 exec .\fig_settings.sci; // custom script for
      setting figure properties
38 xlabel('Time (sec.)');
39 ylabel('Control');
40 title ("Integrator antiwindup (b) Control effort.",
      fontsize',3);
41 zoom_rect([0 -1.2 10 1.2])
42
43 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 9.9 Describing Function for a saturation nonlinearity

```
1 / Example 9.9
2 // Describing Function for a saturation nonlinearity.
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //Response of the saturation nonlinearity to
     sinusoidal input
9 figure;
10 importXcosDiagram(".\Ex9_9_model.xcos")
11 xcos_simulate(scs_m,4);
12 scs_m.props.context
13 plot(yt.time,yt.values(:,1), 'r--')
14 plot(yt.time,yt.values(:,2), 'b')
15
16 xlabel('Time (sec.)');
17 ylabel('Amplitude');
18 title ("Saturation nonlinearity output to sinusoidal
     input",...
```

```
19 'fontsize', 3);
20 exec .\fig_settings.sci; //custom script for setting
       figure properties
21 //
22 // Describing Functin for saturation nonlinearity.
23 k = 1;
24 N = 1;
25 i = 1;
26 \text{ Keq} = [];
27
28 for a=0:0.2:10
       if k*a/N > 1 then
29
30
       Keq(i,1)=2/\%pi*(k*asin(N/a/k)+N/a*sqrt(1-(N/k/a))
          ^2))
31
       else
32
       Keq(i,1)=k
33
       end
34
       i=i+1;
35 end
36
37 \quad a=0:0.2:10;
38 \ a=a';
39 figure,
40 plot(a, Keq)
41 xlabel('$a$');
42 ylabel('K_{eq}}$');
44 xset('font size',3);
45 title ("Describing Function for a saturation
      nonlinearity ...
    with k=N=1", 'fontsize', 3);
46
47 exec .\fig_settings.sci; //custom script for setting
       figure properties
48 zoom_rect([0 0 10 1.1])
49 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

Scilab code Exa 9.11 Describing Function for a relay with hysteresis non linearity

```
1 //Example 9.11
2 // Describing Function for a relay with hysteresis
     nonlinearity.
3
4 xdel(winsid())//close all graphics Windows
5 clear;
6 clc;
7 //
8 //Response of the saturation noninearity to
     sinusoidal input
9 figure;
10 importXcosDiagram(".\Ex9_11_model.xcos")
11 xcos_simulate(scs_m,4);
12 scs_m.props.context
13 plot(yt.time,yt.values(:,1),'r--')
14 plot(yt.time,yt.values(:,2), 'b')
15
16 xlabel('Time (sec.)');
```

```
17 ylabel('Amplitude');
18 title ("Relay with hysteresis nonlinearity output to
      sinusoidal...
    input", 'fontsize',3);
19
20 exec .\fig_settings.sci; //custom script for setting
       figure properties
21 zoom_rect([0 -1.2 5 1.2])
22 //
23 ///Describing Functin for relay with hysteresis
      nonlinearity.
24 h = 0.1;
25 N = 1;
26 i = 1;
27
28 for a=0.1:0.025:1
29
       if a<h then
            Keq(i,1)=0;
30
            ro(i,1)=0;
31
32
            theta(i,1)=0
33
       else
            Keq(i,1)=4*N/(%pi*a)*(sqrt(1-(h/a)^2)-%i*h/a
34
            [r th] = polar(Keq(i,1));
35
36
            ro(i,1)=r; //magnitude
            theta(i,1)=clean(th); //angle in radians
37
38
       end
39
       i=i+1;
40 \, \text{end}
41
42 \quad a=0.1:0.025:1
43 = a';
44 figure,
45
46 subplot (2,1,1), plot (a,ro)
47 xlabel('$a$');
48 ylabel(['Magnitude', '|K_{q}|']);
```

```
49
50 xset('font size',3);
51 exec .\fig_settings.sci; //custom script for setting
       figure properties
52 title ("Describing Functin for relay with hysteresis
      nonlinearity ...
    with h=0.1 and N=1", 'fontsize',3);
53
54
55 subplot(2,1,2), plot(a,theta*180/%pi)
56 xlabel('$a$');
57 ylabel(['Phase', '\ \angle K<sub>-</sub>{eq}\', 'deg.']);
58 xset('font size',3);
59 exec .\fig_settings.sci; //custom script for setting
       figure properties
60 //
```

This code can be downloaded from the website wwww.scilab.in check Appendix AP 1 for dependency:

```
fig_settings.sci
```

## Scilab code Exa 9.12 Conditionally stable system

```
1 //Example 9.12
2 //Conditionally stable system.
3 xdel(winsid())//close all graphics Windows 4 clear;
5 clc;
```

```
6 //
```

```
7 //System transfer function and its root locus
9 s = poly(0, 's');
10 num=0.1;
11 den=(s^2+0.2*s+1)*(s);
12 Gs=syslin('c',num/den)
13
14 // Nyquist plot of the system
15 nyquist (Gs, 0.035, 10)
16 title ("Nyquist plot and describing function to
      determine limit ...
    cycle", 'fontsize',3);
17
18
19 f=gca();
20 f.x_location = "origin"
21 f.y_location = "origin"
22 h=legend('');
23 \text{ h.visible} = " \text{ off"}
24 xset("color",2);
25
26 // Nyquist Plot of Describing Function for
      saturation nonlinearity.
27 omegat=0.05:0.05:%pi;
28 \quad a=sin(omegat);
29 N = 0.1;
30 k = 1;
31
32 \text{ Keq} = 2/\% pi*(k*asin(N ./a /k)+N ./a .* sqrt(1-(N/k ./a))
      ) .^2));
33 DF_nyq=-1 ./Keq;
34
35 plot(DF_nyq,zeros(1,length(DF_nyq)), 'm-.')
36 exec .\fig_settings.sci; //custom script for setting
       figure properties
37 zoom_rect([-0.8 -0.5 0.2 0.5])
```

```
38
39 //limit cycle points
40 plot(-0.5,0,'bo');
41
42 xset ('font size',3)
43 xstring(-0.78,0.08,"limit cycle point");
44 xarrows([-0.6;-0.52],[0.1;0.02],-1)
45 xstring(-0.62,-0.22,"$-\frac\{1\}\{K_{-}\{eq\}\}");
46 xarrows([-0.55;-0.55],[-0.1;0],-1)
47 //
48 // Describing Functin for saturation nonlinearity.
49 \text{ Keq} = []
50 i = 1;
51
52 for a=0:0.2:10
        if k*a/N > 1 then
53
       Keq(i,1)=2/\%pi*(k*asin(N/a/k)+N/a*sqrt(1-(N/k/a))
54
           ^2))
55
       else
       Keq(i,1)=k
56
57
       end
58
        i=i+1;
59 end
60
61 \quad a=0:0.2:10;
62 \ a=a';
63
64 figure,
65 plot(a, Keq)
66 xlabel('$a$');
67 ylabel('K_{eq}');
68
69 xset('font size',3);
70 title ("Describing Function for a saturation
      nonlinearity ...
    with N=0.1 and k=1", 'fontsize', 3);
71
```

check Appendix AP 1 for dependency:

```
fig_settings.sci
```

13 //

Scilab code Exa 9.13 Determination of stability with a hysteresis nonlinearity

```
14 // Nyquist Plot of the system
15 nyquist (Gs, 0.25, 3)
16
17 // Nyquist Plot of Describing Function for
      hysteresis nonlinearity
18 N = 1;
19 h=0.1;
20 i = 1;
21
22 for omegat=0:0.05:%pi-0.1;
       a=sin(omegat);
23
       DF_nyq(i,1) = -\%pi/4/N*(sqrt(a^2-h^2) + h * \%i)
24
25
       i=i+1;
26 \, \text{end}
27
28 plot(real(DF_nyq), imag(DF_nyq), 'm-.')
29 exec .\fig_settings.sci; // custom script for
      setting figure properties
30 zoom_rect([-0.3 -0.3 0 0.3])
31 title ('Nyquist plot of system and describing
      function to ...
32
    determine limit cycle', 'fontsize', 3)
33
34 //limit cycle points
35 plot(-0.1714,-0.0785, 'ro');
36 xstring(-0.25,0,"limit cycle point");
37 xarrows([-0.2;-0.172],[0;-0.077],-1);
38
39 //
40 //Response of the system
41 K=2;
42 r = 1
43 figure (1);
44 importXcosDiagram (". \times \text{Ex9}_{-13}_model.xcos")
45 xcos_simulate(scs_m,4);
46 scs_m.props.context
```

```
47 plot(yt.time,yt.values)
48
49 xlabel('Time (sec.)');
50 ylabel('Output, y');
51 title("Step response displaying limit cycle
        oscillations", 'fontsize',3);
52 exec .\fig_settings.sci; //custom script for setting
        figure properties
53 //
```

This code can be downloaded from the website wwww.scilab.in

## **Appendix**

Scilab code AP 1 figure setting file

1 //

```
6 / K = acker_dk(a, b, pl)
7 //a:- System matrix.
8 //b:- input matrix.
9 //p:- Desired poles.
10 / K:-State feedback gain for the control law u=-Kx.
11 //lambda:- Eigen values of (a-b*k)
12 //
13 //
14
  function [K, lambda] = acker_dk(a, b, pl)
            [lhs, rhs] = argn(0)
16
17
       if rhs == 0 then
18
            disp(["K=acker_dk(a, b, pl)"; "[K, lambda]=
19
               acker_dk(a, b, pl)"]);
            disp(["a:- System matrix";"b:- input matrix"
20
               ; "p:- Desired poles"]);
            disp(["K:-State feedback gain for the
21
               control law u=-Kx";...
    "lambda:- Eigen values of (a-b*k)"]);
22
23
            return;
24
       \quad \text{end} \quad
25
   [ra ca] = size(a);
26
   [rb cb] = size(b);
27 l=length(pl);
28
29 CO=cont_mat(a,b);
30
31 if ra~=1 then
       error(["Dimension error:"; "number of desired
32
          poles must equal ...
    to order of the system"]);
33
34 elseif ra~=ca then
       error (["Dimension error:"; "system matrix should
35
```

```
be . . .
    a sqaure matrix"]);
36
37 elseif rb~=ra then
       error (["Dimension error:","Input matrix should
38
          have ...
39
    as many rows as a system matrix."]);
40 elseif rank(CO) < ra then
       error("system is not controllable");
41
42 end
43 //
44 //controllable canonical form
45 [Ac,Bc,T,ind]=canon(a,b);
46
47 //CO = zeros(ra, cb);
48 for i=1:ra
       CO(:,ra+1-i)=Ac^{(i-1)}*Bc;
50 end
51 //
52 chr_eq=poly(pl,'s');
53 des_chr_coeff=coeff(chr_eq);
54
55 des_chr_coeff=des_chr_coeff(1:ra);
56 alpha_c=Ac^ra;
57
58 for k=1:ra
       alpha_c=alpha_c + des_chr_coeff(k)*Ac^(k-1)
59
60 \text{ end}
61 //
62 //State feedback gain
63 temp=zeros(1,ra);
64 \text{ temp (1) = 1;}
65 K=temp*inv(CO)*alpha_c;
```

```
66 \text{ K=K/T};
67 lambda=spec(a-b*K);
68 endfunction
69 //
   Scilab code AP 3 ZPK computation
1 //
2 //
3 //A function written by Deepti Khimani.
4 //Usage:-
5 //p = zpk_dk(sl)
6 //[p, z] = zpk_{d}k(sl)
7 //[p, z, k] = zpk_{dk}(sl)
8 //p:- Poles of the system
9 //z:- zeros of the system
10 //k:- DC gain of the system
11 //
12 //
13
14 function[pl,zr,k]=zpk_dk(sysmodel)
       [lhs, rhs] = argn(0)
15
16
       if rhs == 0 then
17
        disp(["p=zpk_dk(sl)";"[p, z]=zpk_dk(sl)";"[p, z
18
           , k = zpk_dk(sl)";
        disp(["p:- Poles of the system"; "z:- zeros of
19
           the system"]);
```

```
20
        disp("k:- DC gain of the system");
21
        return;
22
       end
23
24
       if typeof(sysmodel) == "rational" then
            sys=tf2ss(sysmodel);
25
           pl=spec(sys.A);
26
           zr=trzeros(sys);
27
           temp1=poly(zr,'s','roots')/poly(pl,'s','
28
               roots');
           temp2=sysmodel/temp1;
29
30
           temp3=tf2ss(temp2);
31
           k = temp3.D;
       elseif typeof(sysmodel) == "state-space" then
32
33
           pl=spec(sysmodel.A);
           zr=trzeros(sysmodel);
34
35
           g=ss2tf(sysmodel);
           temp1=poly(zr,'s','roots')/poly(pl,'s','
36
              roots');
           temp2=g/temp1;
37
38
           temp3=tf2ss(temp2);
39
           k = temp3.D
40
       else
           error("Wrong type of input argument.")
41
42
       end
43 endfunction
```