Scilab Textbook Companion for Mechanics Of Material by J. M. Gere¹

Created by
Rohit Deshmukh
Dual Degree
Others
IIT Bombay
College Teacher
Iit Bombay
Cross-Checked by

August 10, 2013

¹Funded by a grant from the National Mission on Education through ICT, http://spoken-tutorial.org/NMEICT-Intro. This Textbook Companion and Scilab codes written in it can be downloaded from the "Textbook Companion Project" section at the website http://scilab.in

Book Description

Title: Mechanics Of Material

Author: J. M. Gere

Publisher: Thomson Learning Inc.

Edition: 6

Year: 2004

ISBN: 0-534-41793-0

Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

Contents

List of Scilab Codes		
1	Tension Compression and Shear	8
2	Axially Loaded Members	14
3	Torsion	21
4	Shear Forces and Bending Moments	28
5	Stresses in Beams Basic Topics	30
6	Stresses in Beams Advanced Topics	41
7	Analysis of Stress and Strain	49
8	Applications of Plane Stress Pressure Vessels Beams and Combined Loadings	57
11	Columns	66
12	Review of Centroids and Moments of Inertia	76

List of Scilab Codes

Exa 1.1	Determine the compressive stress and strain in the post	8
Exa 1.2	Calculation of maximum stress	8
Exa 1.3	Determination of various structural properties of the pipe	9
Exa 1.4	Calculation of average shear and compressive stress in	
	a punch	10
Exa 1.5	Determination of various structural properties of the pin	10
Exa 1.7	Determination of allowable tensile load	11
Exa 1.8	Determination of required cross section area of the bar	12
Exa 2.1	Calculation of number of revolutions of the nut that are	
	required to bring the pointer back to the mark	14
Exa 2.2	Calculation of maximum allowable load	14
Exa 2.3	Calculation of vertical displacement at point C	15
Exa 2.6	Calculation of the allowable load	15
Exa 2.10	Determination of state of stress in a bar	16
Exa 2.11	Determination of minimum width of the bar	17
Exa 2.15	Comparison of energy absorbing capacity of the three	
	bolt	17
Exa 2.16	Calculation of maximum elongation and maximum ten-	
	sile stress in a bar	18
Exa 2.18	Determination of displacement at the lower end of the	
	bar under various conditions	19
Exa 3.1	Calculation of maximum shear stress and permissible	
	torque in the bar	21
Exa 3.2	Calculation of required diameter for solid and hollow	
	shaft	22
Exa 3.4	Determination of maximum shear stress in each part of	
	the shaft and the angle of twist	23
Exa 3.6	Calculation of various stress and strain in circular tube	24

Exa 3.7	Calculation of the required diameter d of the shaft	24
Exa 3.8	Calculation of maximum shear stress tmax in the shaft	
	and the angle of twist	25
Exa 3.10	evaluation of the strain energy for different cases	26
Exa 3.11	Evaluation of the strain energy of a hollow shaft	26
Exa 4.3	Calculation of the shear force and the bending moment	
	of the cross section	28
Exa 4.7	Shear force nd bending moment diagramme	29
Exa 5.1	Determination of radius of curvature and deflection in	
	a simply supported beam	30
Exa 5.2	Determination of the bending moment M and maximum	
	bending stress smax in the wire	30
Exa 5.3	Determination of maximum tensile and compressive stress	es
	in the beam due to bending	31
Exa 5.4	Determination the maximum tensile and compressive	
	stresses in the beam due to the uniform load	31
Exa 5.5	Selection of the suitable size for the beam	33
Exa 5.6	Calculation of minimum required diameter in the wood	
	and alluminium rod	33
Exa 5.7	Selection of the steel beam	34
Exa 5.8	Determination of the minimum required dimension b of	
	the posts	35
Exa 5.11	Determination of the normal stress and shear stress at	
	point C	35
Exa 5.12	Determination of the maximum permissible value Pmax	
	of the loads	36
Exa 5.13	Determination of the maximum shear stress in the pole	
	and diameter d0 of a solid circular pole	36
Exa 5.14	Determination of the maximum shear stress minimum	
	shear stress and total shear force in the web	37
Exa 5.15	Determination of the shear stress t1 at the top of the	
	web and the maximum shear stress tmax	37
Exa 5.16	determination of the maximum permissible longitudinal	
	spacing of the screws	38
Exa 5.17	Determination of the maximum tensile and compressive	
	stresses in the beam due to a load	39
Exa 6.1	Calculation of stresses in wood and steel	41

Exa 6.2	Determination of the maximum tensile and compressive stresses in the faces and the core	42
Exa 6.3	Calculation of stresses in wood and steel	43
Exa 6.4	Determination of the maximum tensile and compressive	40
Exa 0.4	stresses in the beam and locating the neutral axis	45
Exa 6.5	Determination of the maximum bending stresses in the	40
	beam	46
Exa 6.6	Calculation of the bending stresses and location of neu-	
	tral axis	46
Exa 6.9	Determination of the magnitude of the moment	47
Exa 7.1	Determination of the stresses acting on an inclined element	49
Exa 7.2	Determination of stresses acting on inclined element .	50
Exa 7.3	Determination of stresses acting on inclined element .	50
Exa 7.4	Determination of stresses acting on inclined element us-	
	ing mohrs circle	51
Exa 7.5	Determination of stresses acting on inclined element us-	
	ing Mohrs circle	51
Exa 7.6	Determination of stresses acting on inclined element us-	
	ing mohrs circle	53
Exa 7.7	Determination of various strain on inclined element	54
Exa 8.1	Calculation of maximum permissible pressure under var-	
	ious conditions	57
Exa 8.2	Calculation of various stresses and strain in cylindrical	
	part of the vessel	58
Exa 8.3	Investigation of the principal stresses and maximum shear	
_	stresses at cross section mn	59
Exa 8.4	Determination of stresses in the shaft	61
Exa 8.5	Determination of the maximum allowable internal pres-	61
Exa 8.6	sure	62
Exa 8.7	Determination of stresses due to loads	64
Exa 6.7	Determination of the allowable load using a factor of	04
E/Xa 11.1	safety with respect to Euler buckling of the column	66
Exa 11.2	Determine the minimum required thickness t of the column	
LAG 11.2	wrt Eular bucking of column	66
Exa 11.3	Determination of longest permissible length of rod	67
Exa 11.4	Calculation of compressive stress and factor of safety .	68

Exa 11.5	Calculation of allowable axial load and maximum per-	
	missible length	69
Exa 11.6	Finding the minimum required thickness for a steel pipe	
	column	70
Exa 11.7	Determination of the minimum required outer diameter	
	of aluminium tube	71
Exa 11.8	Determination of allowable axial load maximum allow-	
	able length and minimum width of the cross section .	73
Exa 12.2	Locating centroid C of the cross sectional area	76
Exa 12.5	Determination of the moment of inertia Ic with respect	
	to the horizontal axis	76
Exa 12.7	Determination of the orientations of the principal cen-	
	troidal axes and the magnitudes of the principal cen-	
	troidal moments of inertia for the cross sectional area.	77

Chapter 1

Tension Compression and Shear

Scilab code Exa 1.1 Determine the compressive stress and strain in the post

```
1 d_1 = 4; // inner diameter (inch)
2 d_2 = 4.5; //outer diameter (inch)
3 P = 26000; // pressure in pound
4 L = 16; // Length of cylinder (inch)
5 del = 0.012; // shortening of post (inch)
6 A = (%pi/4)*((d_2^2)-(d_1^2)) //Area (inch ^2)
7 s = P/A; // stress
8 disp("psi",s,"compressive stress in the post is")
9 e = del / L; // strain
10 disp(e,"compressive strain in the post is")
```

Scilab code Exa 1.2 Calculation of maximum stress

```
1 W = 1500; // weight (Newton)
2 d = 0.008; //diameter(meter)
3 g = 77000; // Weight density of steel
4 L = 40; // Length of bar (m)
```

```
5 A = (%pi/4)*(d^2) // Area
6 s_max = (1500/A) + (g*L) // maximum stress
7 disp("Pa",s_max,"Therefore the maximum stress in the rod is")
```

Scilab code Exa 1.3 Determination of various structural properties of the pipe

```
1 d1 = 4.5; // diameter in inch
2 d2 = 6; // diameter in inch
3 A = (\%pi/4)*((d2^2)-(d1^2)) // Area
4 P = 140 ; // pressure in K
5 s = -P/A ; // stress (compression)
6 E = 30000 ; // young's modulus in Ksi
7 e = s/E ; // strain
8 // Part (a)
9 del = e*4*12 // del = e*L ;
10 disp(del, "Change in length of the pipe is")
11 // Part (b)
12 v = 0.30; // Poissio's ratio
13 e_{-} = -(v*e)
14 disp(e_,"Lateral strain in the pipe is")
15 // Part (c)
16 \text{ del_d2} = e_*d2;
17 \text{ del_d1} = e_*d1;
18 disp("inch", del_d1, "Increase in the inner diameter
      is ")
19 // Part (d)
20 t = 0.75;
21 \text{ del_t} = e_*t;
22 disp("inch",del_t,"Increase in the wall thicness is"
23 \text{ del_t1} = (\text{del_d2-del_d1})/2 ;
24 \operatorname{disp}(\operatorname{del}_{t1} = \operatorname{del}_{t})
```

Scilab code Exa 1.4 Calculation of average shear and compressive stress in a punch

```
1 d = 0.02; // diameter in m
2 t = 0.008; // thickness in m
3 A = %pi*d*t; // shear area
4 P = 110000; // prassure in Newton
5 A1 = (%pi/4)*(d^2); // Punch area
6 t_aver = P/A; // Average shear stress
7 disp("Pa",t_aver," Average shear stress in the plate is ")
8 s_c = P/A1; // compressive stress
9 disp("Pa",s_c," Average compressive stress in the plate is ")
```

Scilab code Exa 1.5 Determination of various structural properties of the pin

```
1  P = 12;  // Pressure in K
2  t = 0.375 ;  // thickness of wall in inch
3  theta = 40 ;  // angle in degree
4  d_pin = 0.75 ;  // diameter of pin in inch
5  t_G = 0.625 ;  // thickness of gusset in inch
6  t_B = 0.375 ;  // thickness of base plate in inch
7  d_b = 0.50 ;  // diameter of bolt in inch
8  // Part (a)
9  s_b1 = P/(2*t*d_pin);  // bearing stress
10  disp("ksi",s_b1," Bearing stress between strut and pin")
11  // Part (b)
12  t_pin = (4*P)/(2*%pi*(d_pin^2));  // average shear stress in the
```

```
disp("ksi",t_pin,"Shear stress in pin is ")
// Part (c)
s_b2 = P/(2*t_G*d_pin); // bearing stress between
    pin and gusset
disp("ksi",s_b2," Bearing stress between pin and
    gussets is")
// Part (d)
s_b3 = (P*cosd(40))/(4*t_B*d_b); // bearing stress
    between anchor bolt and base plate
disp("ksi",s_b3,"Bearing stress between anchor bolts
    and base plate")
// Part (e)
t_bolt = (4*cosd(40)*P)/(4*%pi*(d_b^2)); // shear
    stress in anchor bolt
disp("ksi",t_bolt,"Shear stress in anchor bolts is")
```

Scilab code Exa 1.7 Determination of allowable tensile load

```
1 b1 = 1.5; // width of rectangular crosssection in
     inch
2 t = 0.5; // thickness of rectangular crosssection
     in inch
3 b2 = 3; // width of enlarged rectangular
     crosssection in inch
4 d = 1; // diameter in inch
5 // Part (a)
6 \text{ s\_1} = 16000; // \text{ maximum allowable tensile stress in}
     Psi
7 P_1 = s_1*t*b1;
8 disp("lb",P_1,"The allowable load P1 is")
9 // Part (b)
10 s_2 = 11000; // maximum allowable tensile stress in
     Psi
11 P_2 = s_2*t*(b2-d);
12 disp("lb", P_2, "allowable load P2 at this section is"
```

```
)
13 //Part (c)
14 s_3 = 26000; // maximum allowable tensile stress in
        Psi
15 P_3 = s_3*t*d
16 disp("lb",P_3,"The allowable load based upon bearing
        between the hanger and the bolt is")
17 // Part (d)
18 s_4 = 6500; // maximum allowable tensile stress in
        Psi
19 P_4 = (%pi/4)*(d^2)*2*s_4;
20 disp("lb",P_4,"the allowable load P4 based upon
        shear in the bolt is")
```

Scilab code Exa 1.8 Determination of required cross section area of the bar

```
1 // Horizontal component at A in N
2 R_ah = (2700*0.8 + 2700*2.6)/2;
3 // Horizontal component at C in N
4 R_ch = R_ah;
5 // vertical component at C in N
6 R_cv = (2700*2.2 + 2700*0.4)/3;
7 // vertical component at A in N
8 R_av = 2700 + 2700 - R_cv;
9 R_a = sqrt((R_ah^2) + (R_av^2))
10 R_c = sqrt((R_ch^2) + (R_cv^2))
11 Fab = R_a; // Tensile force in bar AB
12 Vc = R_c; // Shear force acting on the pin at C
13 s_allow = 125000000 ; // allowable stress in tension
14 t_allow = 45000000; // allowable stress in shear
15 Aab = Fab / s_allow; // required area of bar
16 Apin = Vc / (2*t_allow); // required area of pin
17 disp("m2", Apin, "Required area of bar is ")
18 d = sqrt((4*Apin)/\%pi); // diameter in meter
```

19 disp("m",d," Required diameter of pin is")

Chapter 2

Axially Loaded Members

Scilab code Exa 2.1 Calculation of number of revolutions of the nut that are required to bring the pointer back to the mark

```
1 W = 2; //lb
2 b = 10.5; //inch
3 c = 6.4; //inch
4 k = 4.2; //inch
5 p = 1/16; //inch
6 n = (W*b)/(c*k*p); //inch
7 disp(n," No. of revolution required = ")
```

Scilab code Exa 2.2 Calculation of maximum allowable load

```
1 Fce_ = 2; //dummy variable
2 Fbd_ = 3; //dummy variable
3 Lbd = 480; //mm
4 Lce = 600; //mm
5 E = 205e6; //205Gpa
6 Abd = 1020; //mm
7 Ace = 520; //mm
```

```
8  Dbd_ = (Fbd_*Lbd)/(E*Abd); //dummy variable
9  Dce_ = (Fce_*Lce)/(E*Ace); //dummy variable
10  Da = 1; //limiting value
11  P = ( ( ((450+225)/225)*(Dbd_ + Dce_) - Dce_ )^(-1) ) * Da ;
12  Fce = 2*P; // Real value in newton
13  Fbd = 3*P; //real value in newton
14  Dbd = (Fbd*Lbd)/(E*Abd); //displacement in mm
15  Dce = (Fce*Lce)/(E*Ace); // displacement in mm
16  a = atand((Da+Dce)/675); //alpha in degree
17  disp("degree",a,"alpha = ")
```

Scilab code Exa 2.3 Calculation of vertical displacement at point C

```
1 P1 = 2100; //lb
2 P2 = 5600; //lb
3 b = 25; //inch
4 \ a = 28; //inch
5 \text{ A1} = 0.25; // \text{inch}^2
6 \text{ A2} = 0.15; // \text{inch}^2
7 \text{ L1} = 20; // \text{inch}
8 L2 = 34.8; //inch
9 E = 29e6; //29Gpa
10 P3 = (P2*b)/a;
11 Ra = P3-P1;
12 \text{ N1} = -\text{Ra};
13 N2 = P1 ;
14 D = ((N1*L1)/(E*A1)) + ((N2*L2)/(E*A2)) ; //
       displacement
15 disp ("inch", D, "Downward displacement is = ")
```

Scilab code Exa 2.6 Calculation of the allowable load

```
1 // Numerical calculation of allowable load
2 d1 = 4; /mm
3 d2 = 3; /mm
4 \text{ A1} = (\%pi*(d1^2))/4 ; //area
5 \text{ A2} = (\%pi*(d2^2))/4 ; //area
6 L1 = 0.4; //meter
7 L2 = 0.3; //meter
8 E1 = 72e9 ; //Gpa
9 E2 = 45e9 ; //Gpa
10 f1 = L1/(E1*A1) * 1e6; // To compensate for the mm
      ^2
11 f2 = L2/(E2*A2) * 1e6;
12 s1 = 200e6; //stress
13 s2 = 175e6; // stress
14 P1 = ((s1*A1*(4*f1 + f2))/(3*f2)) * 1e-6 // To
      compensate for the mm<sup>2</sup>
15 P2 = ((s2*A2*(4*f1 + f2))/(6*f1)) * 1e-6
16 disp ("Newton", P2, "Minimum allowable stress aomong
      the two P1 and P2 is smaller one, therefore MAS =
      ")
```

Scilab code Exa 2.10 Determination of state of stress in a bar

```
1  P = 90000; //newton
2  A = 1200e-6 // meter^2
3  s_x = -P/A; //stress
4  t_1 = 25; //for the stresses on ab and cd plane
5  s_1 = s_x*(cosd(t_1)^2);
6  T_1 = -s_x*cosd(t_1)*sind(t_1);
7  t_2 = -65; //for the stresses on ad and bc plane
8  s_2 = s_x*(cosd(t_2)^2);
9  T_2 = -s_x*cosd(t_2)*sind(t_2);
10  disp("MPa respecively", s_1, T_1," The normal and shear stresses on the plane ab and cd are")
11  disp("MPa respecively", s_2, T_2," The normal and
```

Scilab code Exa 2.11 Determination of minimum width of the bar

```
1 // Value of s_x based on allowable stresses on glued
       joint
3 \text{ s_t = -750; } //\text{psi}
4 t = -50; //degree
5 \text{ T_t} = -500; // psi
6 	 sg_x_1 = s_t/(cosd(t)^2)
7 \text{ sg_x_2} = -T_t/(\cos d(t) * \sin d(t))
9 // Value of s_x based on allowable stresses on
      plastic
10
11 sp_x_1 = -1100; //psi
12 T_t_p = 600; //psi
13 t_p = 45; //degree
14 	 sp_x_2 = -T_t_p/(cosd(t_p)*sind(t_p))
15
16 // Minimum width of bar
17
18 P = 8000; //lb
19 A = P/sg_x_2;
20 b_min = sqrt(A) //inch
21 disp("inch", b_min, "The minimum width of the bar is")
```

Scilab code Exa 2.15 Comparison of energy absorbing capacity of the three bolt

```
1 //Bolt with reduced shank diameter
2 g = 1.50; // inch
```

Scilab code Exa 2.16 Calculation of maximum elongation and maximum tensile stress in a bar

```
1 // Maximum elongation
2 M = 20; //kg
3 \text{ g} = 9.81; //m/s^2
4 L = 2; //meter
5 E = 210e9; //210Gpa
6 h = 0.15; //meter
7 diameter = 0.015; //milimeter
8 A = (\%pi/4)*(diameter^2); //area
9 D_st = ((M*g*L)/(E*A));
10 D_{max} = D_{st}*(1+(1+(2*h/D_{st}))^0.5);
11 D_{\max_1} = \frac{sqrt(2*h*D_st)}{/} another approach to find
      D_max
12 i = D_max / D_st // Impact factor
13 disp("mm", D_max, "Maximum elongation is")
14 // Maximum tensile stress
15 s_max = (E*D_max)/L; //Maximum tensile stress
16 s_st = (M*g)/A; //static stress
17 i_1 = s_max / s_st //Impact factor
```

Scilab code Exa 2.18 Determination of displacement at the lower end of the bar under various conditions

```
1 P1 = 108000; //Newton
2 P2 = 27000; //Newton
3 L = 2.2; //meter
4 A = 480; /mm^2
  // Displacement due to load P1 acting alone
8 s = (P1/A) / stress in MPa
9 e = (s/70000) + (1/628.2)*((s/260)^10) / strain
10 D_b = e*L*1e3 //elongation in mm
11 disp("mm", D_b," elongation when only P1 load acting
     is = ")
12
13 // Displacement due to load P2 acting alone
14
15 s_1 = (P2/A) //stress in MPa
16 \text{ e\_1} = (s\_1/70000) + (1/628.2)*((s\_1/260)^10) //
      strain
17 D_b_1 = e_1*(L/2)*1e_3 //elongation in mm (no
      elongation in lower half)
18 disp("mm", D_b_1," elongation when only P2 load acting
      is = ")
19
20 // Displacement due to both load acting
     simontaneously
21
22 //upper half
23 s_2 = (P1/A) / stress in MPa
24 e_2 = (s_2/70000) + (1/628.2)*((s_2/260)^10) //
      strain
```

Chapter 3

Torsion

Scilab code Exa 3.1 Calculation of maximum shear stress and permissible torque in the bar

```
1 d = 1.5; // diameter of bar in inch
2 L = 54; // Length of bar in inch
3 G = 11.5e06; // modulus of elasticity in psi
4 // Part (a)
5 T = 250 ; // torque
6 t_max = (16*T*12)/(%pi*(d^3)); // maximum shear
     stress in bar
7 Ip = (\%pi*(d^4))/32; // polar miment of inertia
8 f = (T*12*L)/(G*Ip); // twist in radian
9 f_{-} = (f*180)/\%pi ; // twist in degree
10 disp("psi",t_max,"Maximum shear stress in the bar is
11 disp("degree",f_,"Angle of twist is")
12 // Part (b)
13 t_allow = 6000; // allowable shear stress
14 T1 = (\%pi*(d^3)*t_allow)/16; //allowable
     permissible torque in lb-in
15 T1_ = T1*0.0831658; //allowable permissible torque
     in lb-ft
16 f_allow = (2.5*\%pi)/180; // allowable twist in
```

```
radian
17 T2 = (G*Ip*f_allow)/L; // allowable stress via a
          another method
18 T2_ = T2*0.0831658; //allowable permissible torque
          in lb-ft
19 T_max = min(T1_,T2_); // minimum of the two
20 disp("lb-ft",T_max,"Maximum permissible torque in
          the bar is")
```

Scilab code Exa 3.2 Calculation of required diameter for solid and hollow shaft

```
1 T = 1200 ; // allowable torque in N-m \,
2 t = 40e06; // allowable shear stress in Pa
3 f = (0.75*\%pi)/180; // allowable rate of twist in
     rad/meter
4 G = 78e09; // modulus of elasticity
5 // Part (a) : Solid shaft
6 d0 = ((16*T)/(\%pi*t))^(1/3)
7 Ip = T/(G*f); // polar moment of inertia
8 d01 = ((32*Ip)/(\%pi))^(1/4); // from rate of twist
      definition
9 disp("m", d0, "The required diameter of the solid
      shaft is ")
10 // Part (b) : hollow shaft
11 d2 = (T/(0.1159*t))^(1/3); // Diamater of hollow
     shaft in meter
12 // The above equation comes from solving the
     following four equation
13 // t1 = 0.1*d2; thickness of shaft
14 // d1 = d2-(2*t1); // diameter of inner radius
15 // Ip = (\%pi/32)*((d2^4)-(d1^4)); // Polar moment of
      inertia
16 // r = d2/2
17 // t = (T*r)/Ip ; // allowable shear stress
```

Scilab code Exa 3.4 Determination of maximum shear stress in each part of the shaft and the angle of twist

```
1 d = 0.03; // diameter of the shaft in meter
2 T2 = 450 ; // Torque in N-m
3 T1 = 275 ; //
4 T3 = 175 ; //
5 Lbc = 0.5; // Length of shaft in meter
6 Lcd = 0.4; // Length of shaft in meter
7 G = 80e09; // Modulus of elasticity
8 Tcd = T2-T1 ; // torque in segment CD
9 Tbc = -T1; // torque in segment BC
10 tcd = (16*Tcd)/(\%pi*(d^3)); // shear stress in cd
     segment
11 disp("Pa",tcd, "Shear stress in segment cd is")
12 tbc = (16*Tbc)/(\%pi*(d^3)); // shear stress in bc
     segment
13 disp("Pa",tbc, "Shear stress in segment bc is")
14 Ip = (\%pi/32)*(d^4); // Polar monent of inertia
15 fbc = (Tbc*Lbc)/(G*Ip); // angle of twist in radian
16 fcd = (Tcd*Lcd)/(G*Ip); // angle of twist in radian
```

```
17 fbd = fbc + fcd; // angle of twist in radian
18 disp("radian",fbd," Angles of twist in section BD")
```

Scilab code Exa 3.6 Calculation of various stress and strain in circular tube

```
1 d1 = 0.06; // Inner diameter in meter
2 d2 = 0.08; // Outer diameter in meter
3 r = d2/2; // Outer radius
4 G = 27e09 ; // Modulus of elasticity
5 T = 4000 ; // Torque in N-m
6 Ip = (\%pi/32)*((d2^4)-(d1^4)); // Polar moment of
     inertia
7 t_max = (T*r)/Ip ; // maximum shear stress
8 disp("Pa",t_max,"Maximum shear stress in tube is ")
9 s_t = t_max ; // Maximum tensile stress
10 disp("Pa",s_t," Maximum tensile stress in tube is ")
11 s_c = -(t_max); // Maximum compressive stress
12 disp("Pa", s_c, "Maximum compressive stress in tube is
13 g_max = t_max / G ; // Maximum shear strain in
     radian
14 disp("radian",g_max,"Maximum shear strain in tube is
15 e_t = g_{max}/2; // Maximum tensile strain in radian
16 disp("radian", e_t, "Maximum tensile strain in tube is
 e_c = -g_max/2; // Maximum compressive strain in
17
     radian
18 disp("radian", e_c, "Maximum compressive strain in
     tube is ")
```

Scilab code Exa 3.7 Calculation of the required diameter d of the shaft

```
1 H = 40; // Power in hp
2 s = 6000; // allowable shear stress in steel in psi
3 // Part (a)
4 n = 500; // rpm
5 T = ((33000*H)/(2*%pi*n))*(5042/420); // Torque in lb-in
6 d = ((16*T)/(%pi*s))^(1/3); // diameter in inch
7 disp("inch",d,"Diameter of the shaft at 500 rpm")
8 // Part (b)
9 n1 = 3000; // rpm
10 T1 = ((33000*H)/(2*%pi*n1))*(5042/420); // Torque in lb-in
11 d1 = ((16*T1)/(%pi*s))^(1/3); // diameter in inch
12 disp("inch",d1,"Diameter of the shaft at 3000 rpm")
```

Scilab code Exa 3.8 Calculation of maximum shear stress tmax in the shaft and the angle of twist

```
1 d = 0.05; // diameter of the shaft
2 Lab = 1 ; // Length of shaft ab in meter
3 Lbc = 1.2 ; // Length of shaft bc in meter
4 Pa = 50000; // Power in Watt at A
5 Pb = 35000; // Power in Watt at B
6 Ip = (\%pi/32)*(d^4); // Polar moment of inertia
7 Pc = 15000; // Power in Watt at C
8 G = 80e09; // Modulus of elasticity
9 f = 10 ; // frequency in Hz
10 Ta = Pa/(2*\%pi*f) // Torque in N-m at A
11 Tb = Pb/(2*%pi*f) // Torque in N-m at B
12 Tc = Pc/(2*\%pi*f) // Torque in N-m at B
13 Tab = Ta ; // Torque in N-m in shaft ab
14 Tbc = Tc; // Torque in N-m in shaft bc
15 tab = (16*Tab)/(\%pi*(d^3)); // shear stress in ab
     segment
16 fab = (Tab*Lab)/(G*Ip); // angle of twist in radian
```

Scilab code Exa 3.10 evaluation of the strain energy for different cases

```
Ta = 100 ; // Torque in N-m at A
Tb = 150; // Torque in N-m at B
L = 1.6 ; // Length of shaft in meter
G = 80e09 ; // Modulus of elasticity
Ip = 79.52e-09; // polar moment of inertia in m4
Ua = ((Ta^2)*L)/(2*G*Ip) // Strain energy at A
disp("joule",Ua,"Torque acting at free end")
Ub = ((Tb^2)*L)/(4*G*Ip) // Strain energy at B
disp("joule",Ub,"Torque acting at mid point")
a = (Ta*Tb*L)/(2*G*Ip) // dummy variabble
Uc = Ua+a+Ub ; // Strain energy at C
disp("joule",Uc,"Total torque")
```

Scilab code Exa 3.11 Evaluation of the strain energy of a hollow shaft

```
1 t = 480; // Torque of constant intensity
2 L = 144; // Length of bar
3 G = 11.5e06; // Modulus of elasticity in Psi
4 Ip = 17.18; // Polar moment of inertia
5 U = ((t^2)*(L^3))/(G*Ip*6) // strain energy in in-lb
```

Chapter 4

Shear Forces and Bending Moments

Scilab code Exa 4.3 Calculation of the shear force and the bending moment of the cross section

```
1 q = 0.2; // Uniform load intensity in K/ft
2 P = 14; // Concentrated load in k
3 Ra = 11; // Reaction at A from wquation of equilibrium
4 Rb = 9; // Reaction at B from wquation of equilibrium
5 V = 11 - 14 - (0.2*15); // shear force in k
6 disp("k", V, "Shear force at section D")
7 M = (11*15) - (14*6) - (0.2*15*7.5); // Bending moment in K-ft
8 disp("k-ft", M, "Bending moment at section D")
9 V1 = -9+(0.2*15); // Shear firce from alternative method in k
10 M1 = (9*9) - (0.2*7.5*15); // Bending moment from alternative method in k-ft
```

Scilab code Exa 4.7 Shear force nd bending moment diagramme

```
1 q = 1; // Uniform load intensity in k/ft
2 M0 = 12; // Couple in k-ft
3 Rb = 5.25; // Reaction at B in k
4 Rc = 1.25; // Reaction at C in k
5 b = 4; // Length of section AB in ft
6 Mb = -(q*(b^2))/2; // Moment acting at B
7 disp("k-ft", Mb, "Bending moment at B")
```

Chapter 5

Stresses in Beams Basic Topics

Scilab code Exa 5.1 Determination of radius of curvature and deflection in a simply supported beam

```
1 L = 8 ; // length of beam in ft
2 h = 6 ; // Height of beam in inch
3 e = 0.00125 ; // elongation on the bottom surface of the beam
4 y = -3 ; // Distance of the bottom surface to the neutral surface of the beam in inch
5 r = -(y/e) ; // Radius of curvature
6 disp("ft",r,"radius of curvature is")
7 k = 1/r ; // curvature in in-1
8 disp("ft-1",k,"curvature")
9 theta = asind((L*12)/(2*r)) ; // angle in degree
10 disp("degree",theta,"Angle of twist")
11 del = r*(1-cosd(theta)); // Deflection in inch
```

Scilab code Exa 5.2 Determination of the bending moment M and maximum bending stress smax in the wire

```
1 d = 0.004; // thickness of wire in m
2 R0 = 0.5; // radius of cylinder in m
3 E = 200e09; // Modulus of elasticity of steel
4 s = 1200e06; // proportional limit of steel
5 M = (%pi*E*d^4)/(32*(2*R0+d)); // Bending moment in wire in N-m
6 disp("N-m",M,"Bending moment in the wire is ")
7 s_max = (E*d)/(2*R0+d); // Maximum bending stress in wire in Pa
8 disp("Pa",s_max,"Maximum bending stress in the wire is ")
```

Scilab code Exa 5.3 Determination of maximum tensile and compressive stresses in the beam due to bending

```
1 L = 22; // Span of beam in ft
2 q = 1.5; // Uniform load intensity in k/ft
3 P = 12; // Concentrated in k
4 b = 8.75; // width of cross section of beam in inch
5 h = 27; // height of cross section of beam in inch
6 Ra = 23.59; // Reaction at point A
7 Rb = 21.41; // Reacyion at point B
8 Mmax = 151.6; // Maximum bending moment
9 S = (b*h^2)/6; // Section modulus
10 s = (Mmax*12)/S // stress in k
11 st = s*1000; // Tensile stress
12 disp("psi",st,"Maximum tensile stress in the beam")
13 sc = -s*1000; // Compressive stress
14 disp("psi",sc,"Maximum compressive stress in the beam")
```

Scilab code Exa 5.4 Determination the maximum tensile and compressive stresses in the beam due to the uniform load

```
1 q = 3200; // Uniform load intensity in N/m
2 b = 0.3; // width of beam in m
3 h = 0.08; // Height of the beam in m
4 t = 0.012; // thickness of beam in m
5 Ra = 3600; // Reaction at A in N
6 \text{ Rb} = 10800 \text{ ; } // \text{ Reaction at B in N}
7 Mpos = 2025; // Moment in Nm
8 Mneg = -3600; // Moment in Nm
9 \text{ v1} = t/2;
10 A1 = (b-2*t)*t;
11 y2 = h/2;
12 A2 = h*t;
13 \text{ A3} = \text{A2};
14 c1 = ((y1*A1)+(2*y2*A2))/((A1)+(2*A2));
15 c2 = h - c1;
16 Ic1 = (b-2*t)*(t^3)*(1/12);
17 	 d1 = c1 - (t/2);
18 Iz1 = (Ic1)+(A1*(d1^2));
19 \text{ Iz2} = 956600e-12;
20 \text{ Iz3} = \text{Iz2};
21 Iz = Iz1 + Iz2 + Iz3; // Moment of inertia of the
      beam cross section
22 // Section Modulli
23 S1 = Iz / c1; // for the top surface
24 S2 = Iz / c2; // for the bottom surface
25 // Maximum stresses for the positive section
26 \text{ st} = \text{Mpos} / \text{S2};
27 disp ("Pa", st, "Maximum tensile stress in the beam in
      positive section is")
28 \text{ sc} = -Mpos / S1 ;
29 disp("Pa",sc," Maximum compressive stress in the beam
       in positive section is")
30 // Maximum stresses for the negative section
31 \text{ snt} = -Mneg / S1 ;
32 disp("Pa", snt, "Maximum tensile stress in the beam in
       negative section is")
33 \text{ snc} = \text{Mneg} / \text{S2};
34 disp("Pa", snc, "Maximum compressive stress in the
```

```
beam in negative section is")
35 // Conclusion
36 st_max = st;
37 sc_max = snc ;
```

Scilab code Exa 5.5 Selection of the suitable size for the beam

```
1 L = 12; // Length of beam in ft
2 q = 420; // Uniform load intensity in lb/ft
3 s = 1800; // Allowable bending stress in psi
4 w = 35; // weight of wood in lb/ft3
5 M = (q*L^2*12)/8; // Bending moment in lb-in
6 S = M/s; // Section Modulli in in3
7 // From Appendix F
8 q1 = 426.8; // New uniform load intensity in lb/ft
9 S1 = S*(q1/q); // New section modulli in in3
10 // From reference to appendix F, a beam of cross section 3*12 inch is selected
11 disp("Beam of crosssection 3*12 is sufficient")
```

Scilab code Exa 5.6 Calculation of minimum required diameter in the wood and alluminium rod

```
1 P = 12000; // Lataeral load at the upper end in N
2 h = 2.5; // Height of post in m
3 Mmax = P*h; // Maximum bending moment in Nm
4 // Part (a): Wood Post
5 s1 = 15e06; // Maximum allowable stress in Pa
6 S1 = Mmax/s1; // Section Modulli in m3
7 d1 = ((32*S1)/%pi)^(1/3); // diameter in m
8 disp("m",d1," the minimum required diameter d1 of the wood post is")
9 // Part (b): Alluminium tube
```

Scilab code Exa 5.7 Selection of the steel beam

```
1 q = 2000; // Uniform load intensity in lb/ft
2 s = 18000 ; // Maximum allowable load in Psi
3 \text{ Ra} = 18860 \text{ ; } // \text{ Reaction at point } A
4 Rb = 17140 ; // Reaction at point B
5 \times 1 = Ra/q; // Distance in ft from left end to the
     point of zero shear
6 Mmax = (Ra*x1) - ((q*(x1^2))/2); // Maximum bending
     moment in lb-ft
7 S = (Mmax*12)/s; // Section Modulli in in 3
8 // Trial Beam
9 Ra_t = 19380 ; // Reaction at point
10 Rb_t = 17670 ; // Reaction at point
11 x1_t = Ra_t/q; // Distance in ft from left end to
      the point of zero shear
12 Mmax_t = (Ra_t*x1_t) - ((q*(x1_t^2))/2); // Maximum
     bending moment in lb-ft
13 S_t = (Mmax_t*12)/s; // Section Modulli in in 3
14 // From table E beam 12*50 is selected
15 disp("in3",S_t,"Beam of crosssection 12*50 is
      selected with section modulli")
```

Scilab code Exa 5.8 Determination of the minimum required dimension b of the posts

```
1 g = 9810 ; // Specific weight of water in N/m3
2 h = 2; // Height of dam in m
3 s = 0.8 ; // Distance between square cross section in m
4 sa = 8e06 ; // Maximum allowable stress in Pa
5 b = ((g*(h^3)*s)/sa)^(1/3) ; // Dimension of croossection in m
6 disp("m",b," the minimum required dimension b of the posts")
```

Scilab code Exa 5.11 Determination of the normal stress and shear stress at point C

```
1 L = 3 ; // Span of beam in ft
2 q = 160 ; // Uniform load intensity in lb/in
3 b = 1; // Width of cross section
4 h = 4; // Height of cross section
5 // Calculations from chapter 4
6 Mc = 17920 ; // Bending moment in ld-in
7 Vc = -1600 ; // Loading in lb
8 //
9 I = (b*(h^3))/12; // Moment of inertia in in4
10 sc = -(Mc*1)/I; // Compressive stress at point C in psi
11 Ac = 1*1 ; // Area of section C in inch2
12 yc = 1.5 ; // distance between midlayers od section C and cross section of beam
13 Qc = Ac*yc; // First moment of C cross section in inch3
```

```
14 tc = (Vc*Qc)/(I*b); // Shear stress in Psi
15 disp("psi",sc,"Normal stress at C")
16 disp("psi",tc,"Shear stress at C")
```

Scilab code Exa 5.12 Determination of the maximum permissible value Pmax of the loads

```
1 s = 11e06; // allowable tensile stress in pa
2 t = 1.2e06; // allowable shear stress in pa
3 b = 0.1; // Width of cross section in m
4 h = 0.15; // Height of cross section in m
5 a = 0.5; // in m
6 P_bending = (s*b*h^2)/(6*a); // Bending stress in N
7 P_shear = (2*t*b*h)/3; // shear stress in N
8 Pmax = P_bending; // Because bending stress governs the design
9 disp("N", Pmax," the maximum permissible value Pmax of the loads")
```

Scilab code Exa 5.13 Determination of the maximum shear stress in the pole and diameter d0 of a solid circular pole

```
1  d2 = 4; // Outer diameter in inch
2  d1 = 3.2; // Inner diameter in inch
3  r2 = d2/2; // Outer radius in inch
4  r1 = d1/2; // inner radius in inch
5  P = 1500 ; // Horizontal force in lb
6  // Part (a)
7  t_max = ((r2^2+(r2*r1)+r1^2)*4*P)/(3*%pi*((r2^4)-(r1^4))); // Mximum shear stress in Psi
8  disp("psi",t_max,"Maximum shear stress in the pole is")
9  // Part (b)
```

Scilab code Exa 5.14 Determination of the maximum shear stress minimum shear stress and total shear force in the web

```
1 b = 0.165; // in m
2 h = 0.320 ; // in m
3 \text{ h1} = 0.290 \text{ ; } // \text{ in m}
4 t = 0.0075; // in m
5 V = 45000; // Vertical force in N
6 I = (1/12)*((b*(h^3))-(b*(h1^3))+(t*(h1^3))) //
     Moment of inertia of the cros section
7 t_{max} = (V/(8*I*t))*((b*(h^2))-(b*(h1^2))+(t*(h1^2))
     ); // Maximum shear stress in Pa
8 \text{ t_min} = ((V*b)/(8*I*t))*(h^2-h1^2); // Minimum shear
      stress in Pa
9 T = ((t*h1)/3)*(2*t_max + t_min); // Total shear
      force in Pa
10 t_avg = V/(t*h1); // Average shear stress in Pa
11 disp("Pa",t_max," Maximum shear stress in the web is"
12 disp("Pa",t_min,"Minimum shear stress in the web is"
13 disp("Pa",T," Total shear stress in the web is")
```

Scilab code Exa 5.15 Determination of the shear stress t1 at the top of the web and the maximum shear stress tmax

```
1 V = 10000; // Vertical shear force in lb
2 b = 4; // in inch
```

```
3 t = 1; // in inch
4 h = 8; // in inch
5 \text{ h1} = 7; // \text{ in inch}
6 A = b*(h-h1) + t*h1 ; // Area of cross section
7 Qaa = ((h+h1)/2)*b*(h-h1) + (h1/2)*(t*h1); // First
     moment of cross section
8 c2 = Qaa/A; // Position of neutral axis in inch
9 c1 = h-c2; // Position of neutral axis in inch
10 Iaa = (b*h^3)/3 - ((b-t)*h1^3)/3; // Moment of
     inertia about the line aa
11 I = Iaa - A*c2^2 // Moment of inertia of
     crosssection
12 Q1 = b*(h-h1)*(c1-((h-h1)/2)); // First moment of
     area above the line nn
13 t1 = (V*Q1)/(I*t) // Shear stress at the top of web
      in Psi
14 Qmax = (t*c2)*(c2/2); // Maximum first moment of
     inertia below neutral axis
15 t_max = (V*Qmax)/(I*t); // Maximum Shear stress in
     Psi
16 disp("psi",t1,"Shear stress at the top of the web is
17 disp("Psi",t_max,"Maximum Shear stress in the web is
```

Scilab code Exa 5.16 determination of the maximum permissible longitudinal spacing of the screws

```
1 Af = 40*180; // Area of flange in mm2
2 V = 10500; // Shear force acting on cross section
3 F = 800; // Allowable load in shear
4 df = 120; // Distance between centroid of flange and neutral axis in mm
5 Q = Af*df; // First moment of cross section of flange
```

```
6 I = (1/12)*(210*280^3) - (1/12)*(180*200^3); //
     Moment of inertia of entire cross section in mm4
7 f = (V*Q)/I; // Shear flow
8 s = (2*F)/f // Spacing between the screw
9 disp("mm",s,"The maximum permissible longitudinal spacing s of the screws is")
```

Scilab code Exa 5.17 Determination of the maximum tensile and compressive stresses in the beam due to a load

```
1 L = 60; // Length of beam in inch
2 d = 5.5; // distance from the point of application
     of the load P to the longitudinal axis of the
     tube in inch
3 b = 6; // Outer dimension of tube in inch
4 A = 20; // Area of cross section of tube in inch
5 I = 86.67; // Moment of inertia in in4
6 P = 1000; // in lb
7 theta = 60; // in degree
8 Ph = P*sind(60); // Horizontal component
9 Pv = P*cosd(60); // Vertical component
10 M0 = Ph*d; // Moment in lb-in
11 y = -3; // Point at which maximum tensile stress
     occur in inch
12 N = Ph ; // Axial force
13 M = 9870; // Moment in lb-in
14 st_max = (N/A)-((M*y)/I); // Maximum tensile stress
      in Psi
15 yc = 3; // in inch
16 M1 = 5110 ; // moment in lb-in
17 sc_left = (N/A)-((M*yc)/I); // Stress at the left
     of point C in Psi
18 sc_right = -(M1*yc)/I; // Stress at the right of
     point C in Psi
19 sc_max = min(sc_left,sc_right); // Because both are
```

negative quantities

Chapter 6

Stresses in Beams Advanced Topics

Scilab code Exa 6.1 Calculation of stresses in wood and steel

```
1 // 4*6 inch wood beam dimension
2 // 4*0.5 inch steel beam dimension
3 M = 60 ; // Moment in k-in
4 E1 = 1500 ; // in Ksi
5 E2 = 30000; // in Ksi
6 h1 = 5.031; // Distance between top surface and
     neutral axis of the beam in inch by solving
     1500*(h1-3)*24 + 30000*(h1-6.25)*2 = 0
7 h2 = 6.5 - h1;
8 I1 = (1/12)*(4*6^3) + (4*6)*(h1-3)^2; // Momeny of
     inertia of the wooden cross section
9 I2 = (1/12)*(4*0.5^3) + (4*0.5)*(h2-0.25)^2; //
     Momeny of inertia of the steel cross section
10 I = I1 + I2 ; // Moment of inertia of whole cross
     section
11 // Material 1
12 \text{ s1a} = -(M*h1*E1)/((E1*I1)+(E2*I2)) ; // Maximum
     compressive stress in ksi where y = h1
13 s1c = -(M*(-(h2-0.5))*E1)/((E1*I1)+(E2*I2)); //
```

```
Maximum tensile stress in ksi where y = -(h2-0.5)

14 disp("ksi",s1a," Maximum compressive stress in wood is")

15 disp("ksi",s1c," Maximum tensile stress in wood is")

16 // Material 2

17 s2a = -(M*(-h2)*E2)/((E1*I1)+(E2*I2)); // Maximum tensile stress in ksi where y = -h2

18 s2c = -(M*(-(h2-0.5))*E2)/((E1*I1)+(E2*I2)); // Minimum tensile stress in ksi where y = -(h2-0.5)

19 disp("ksi",s2a," Maximum tensile stress in steel is")

20 disp("ksi",s2c," Minimum tensile stress in steel is")
```

Scilab code Exa 6.2 Determination of the maximum tensile and compressive stresses in the faces and the core

```
1 M = 3000; // moment in N-m
2 t = 0.005; // thickness of alluminium in m
3 E1 = 72e09; // Modulus of elasticity of alluminium
4 E2 = 800e06; // Modulus of elasticity of Plastic
     core in Pa
5 b = 0.2; // Width of cross section in m
6~h = 0.160 ; // Height of cross section in m
7 hc = 0.150; // Height of Plastic core cross section
      in m
  I1 = (b/12)*(h^3 - hc^3); // Moment of inertia of
     alluminium cross section
9 I2 = (b/12)*(hc^3); // Moment of inertia of Plastic
      core cross section
10 f = (E1*I1) + (E2*I2); // Flexural rigidity of the
     cross section
11 s1_max = (M*(h/2)*E1)/f;
12 s1c = -s1_max; // Maximum compressive stress in
```

```
alluminium core in Pa
13 s1t = s1_max ; // Maximum tensile stress in
     alluminium core in Pa
14 disp("Pa", s1c," Maximum compressive stress on
     alluminium face by the general theory for
     composite beams is")
15 disp("Pa", s1t," Maximum tensile stress on alluminium
      face by the general theory for composite beams
     is")
16 \text{ s2_max} = (M*(hc/2)*E2)/f;
17 s2c = -s2_{max}; // Maximum compressive stress in
      Plastic core in Pa
18 s2t = s2_max ; // Maximum tensile stress in Plastic
      core in Pa
19 disp("Pa", s2c," Maximum compressive stress in
      plastic core by the general theory for composite
     beams is")
20 disp("Pa", s2t," Maximum tensile stress in plastic
     core by the general theory for composite beams is
     ")
21 // Part (b) : Calculation from approximate theory of
      sandwitch
22 \text{ s1_max1} = (M*h)/(2*I1);
23 s1c1 = -s1_max1; // Maximum compressive stress in
      alluminium core in Pa
24 s1t1 = s1_max1 ; // Maximum tensile stress in
     alluminium core in Pa
25 disp("Pa", s1c1," Maximum compressive stress on
     alluminium core by approximate theory of
     sandwitch is")
26 disp("Pa", s1t1," Maximum tensile stress on
     alluminium core by approximate theory of
     sandwitch is")
```

Scilab code Exa 6.3 Calculation of stresses in wood and steel

```
1 // 4*6 inch wood beam dimension
2 // 4*0.5 inch steel beam dimension
3 M = 60 ; // Moment in k-in
4 E1 = 1500 ; // in Ksi
5 E2 = 30000; // in Ksi
6 b = 4; // width of crosssection in inch
7 // Transformed Section
8 n = E2/E1 ; // Modular ratio
9 b1 = n*4; // Increased width of transformed cross
     section
10 // Neutral axis
11 h1 = ((3*4*6)+(80*0.5*6.25))/((4*6)+(80*0.5)); //
     Distance between top surface and neutral axis of
     the beam in inch
12 h2 = 6.5 - h1 ; // in inch
13 // Moment of inertia
14 It = (1/12)*(4*6^3) + (4*6)*(h1-3)^2 + (1/12)
     *(80*0.5^3) + (80*0.5)*(h2-0.25)^2; // Moment of
      inertia of transformed cross section
15 // Material 1
16 s1a = -(M*h1)/It; // Maximum tensile stress in ksi
     where y = h1
17 s1c = -(M*(-(h2-0.5)))/It; // Maximum compressive
      stress in ksi where y = -(h2 - 0.5)
18 disp("psi",s1a*1000,"Maximum tensile stress in wood
     is")
19 disp("psi",s1c*1000,"Maximum compressive stress in
     wood is")
20 // Material 2
21 s2a = -(M*(-h2)*n)/It; // Maximum tensile stress in
      ksi where y = -h2
22 \text{ s2c} = -(M*(-(h2-0.5)*n))/It ; // Minimum tensile
      stress in ksi where y = -(h2 - 0.5)
23 disp("psi", s2a*1000," Maximum tensile stress in
      steel")
24 disp("psi",s2c*1000," Minimum tensile stress in
      steel")
```

Scilab code Exa 6.4 Determination of the maximum tensile and compressive stresses in the beam and locating the neutral axis

```
1 q = 3000; // Uniform load intensity in N/m
2 a = 26.57; // tilt of the beam in degree
3 b = 0.1; // width of the beam
4 h = 0.15; // height of the beam
5 L = 1.6; // Span of the beam
6 \text{ qy} = q*cosd(a); // Component of q in y direction
7 qz = q*sind(a); // Component of q in z direction
8 My = (qz*L^2)/8; // Maximum bending moment in y
      direction
  Mz = (qy*L^2)/8; // Maximum bending moment in z
      direction
10 Iy = (h*b^3)/12; // Moment of inertia along y
11 Iz = (b*h^3)/12; // Moment of inertia alon z
12 s = ((3*q*L^2)/(4*b*h))*((sind(a)/b)+(cosd(a)/h));
13 sc = -s; // Maximum compressive stress
14 st = s; // Maximum tensile stress
15 disp("Pa", sc, "Maximum compressive stress in the beam
      is")
16 disp("Pa", st, "Maximum tensile stress in the beam is"
17 // Neutral axis
18 \ 1 = (h/b)^2;
19 t = sind(a)/cosd(a);
20 \quad j = 1*(sind(a)/cosd(a));
21 be = atand(j); // Inclination of Neutral axis to z
22 disp ("degree", be, "Inclination of Neutral axis to z
     axis is")
```

Scilab code Exa 6.5 Determination of the maximum bending stresses in the beam

```
1 L = 12; // Length of the beam in ft
2 P = 10 ; // Load in k acting in vertical direction
3 // Part (a)
4 h = 24; // Height of beam in inch
5 Iz = 2100; // Moment of inertia along z axis in in4
6 Iy = 42.2; // Moment of inertia along y axis in in4
7 s_max = (P*(h/2)*L*12)/Iz; // Maximum stress in Ksi
8 disp("psi",s_max*1000, "Maximum tensile stress in the
      beam at the top of the beam")
9 disp("psi",-s_max*1000,"Maximum compressive stress
     in the beam at the bottom of the beam")
10 // Part (b)
11 a = 1; // Angle between y axis and the load
12 My = -(P*sind(a))*L*12; // Moment along y-axis in K
13 Mz = -(P*cosd(a))*L*12; // Moment along z-axis in K
14 ba = atand((My*Iz)/(Mz*Iy)); // Orientation of
     neutral axis
15 z = -3.5; y = 12; // Coordinates of the point A and
      B where maximum stress occur
16 s = ((My*z)/Iy)-((Mz*y)/Iz); // Stress in Ksi
17 sa = s; // Tensile stress at A
18 sb = -s; // Compressive stress in B
19 disp("psi", sa*1000, "The tensile stress at A is")
20 disp("psi", sb*1000, "The compressive stress at B is")
```

Scilab code Exa 6.6 Calculation of the bending stresses and location of neutral axis

```
1 M = 15; // Bending moment in k-in
2 t = 10; // Angle between line of action of moment
```

```
and z-axis
3 // Properties of cross section
4 c = 0.634; // Location of centroid on the axis of
     symmetry
5 Iy = 2.28; // Moment of inertia in y-direction in
6 Iz = 67.4; // Moment of inertia in z-direction in
     in4
7 ya = 5; za = -2.6+0.634; // Coordinates of point A
8 yb = -5; zb = 0.634; // Coordinates of point B
9 My = M*sind(t); // Moment along y-axis
10 Mz = M*cosd(t); // Moment along z-axis
11 sa = ((My*za)/Iy)-((Mz*ya)/Iz); // Bending stress
     at point A in ksi
12 sb = ((My*zb)/Iy)-((Mz*yb)/Iz); // Bending stress
     at point B in ksi
13 disp("psi", sa*1000, "The bending stress at point A is
14 disp("psi", sb*1000, "The bending stress at point B is
15 // Neutral axis
16 j = (Iz/Iy)*(sind(t)/cosd(t));
17 be = atand(j); // Inclination of neutral axis to z-
     axis in degree
18 disp ("degree", be, "Inclination of neutral axis to z-
     axis is")
```

Scilab code Exa 6.9 Determination of the magnitude of the moment

```
1  b = 5 ; // in inch
2  b1 = 4 ; // in inch
3  h = 9 ; // in inch
4  h1 = 7.5 ; // in inch
5  sy = 33 ; // stress along y axis in ksi
6  M = (sy/12)*((3*b*h^2)-(b+(2*b1))*(h1^2)) ; //
```

```
Bending moment acting in k-in 7 disp("k-in", M," the magnitude of the moment M is")
```

Chapter 7

Analysis of Stress and Strain

Scilab code Exa 7.1 Determination of the stresses acting on an inclined element

```
1 // Let x1, y1 be the transformed direction inclined
      at 45 deegree to the original
2 sx = 16000; // Direct stress in x-direction in psi
3 sy = 6000; // Direct stress in y-direction
4 txy = 4000; // Shear stress in y-direction
5 tyx = txy; // Shear stress in x-direction
6 t = 45; // Inclination pf plane in degree
7 \text{ sx1} = (\text{sx+sy})/2 + ((\text{sx-sy})*(\text{cosd}(2*t))/2) + \text{txy*sind}
      (2*t); // Direct stress in x1-direction in psi
8 \text{ sy1} = (\text{sx+sy})/2 - ((\text{sx-sy})*(\text{cosd}(2*t))/2) - \text{txy*sind}
      (2*t); // Direct stress in y1-direction in psi
9 \text{ tx1y1} = -((sx-sy)*(sind(2*t))/2) + txy*cosd(2*t)
        // Shear stress in psi
10 disp("psi", sx1, "The direct stress on the element in
      x1-direction is")
11 disp("psi", sy1, "The direct stress on the element in
      y1-direction is")
12 disp("psi", tx1y1, "The shear stress on the element")
```

Scilab code Exa 7.2 Determination of stresses acting on inclined element

```
1 // Let x1, y1 be the transformed direction inclined
      at 15 deegree to the original
2 \text{ sx} = -46\text{e}06; // Direct stress in x-direction in Pa
3 sy = 12e06; // Direct stress in y-direction ""
4 txy = -19e06; // Shear stress in y-direction ""
5 t = -15; // Inclination of plane in degree
6 \text{ sx1} = (\text{sx+sy})/2 + ((\text{sx-sy})*(\text{cosd}(2*t))/2) + \text{txy*sind}
             // Direct stress in x1-direction in Pa
  sy1 = (sx+sy)/2 - ((sx-sy)*(cosd(2*t))/2) - txy*sind
      (2*t) // Direct stress in y1-direction in Pa
8 \text{ tx1y1} = -((sx-sy)*(sind(2*t))/2) + txy*cosd(2*t)
         // Shear stress in Pa
9 disp("Pa", sx1,"The direct stress on the element in
     x1-direction is")
10 disp("Pa", sy1," The direct stress on the element in
      y1-direction is")
11 disp("Pa",tx1y1,"The shear stress on the element")
```

Scilab code Exa 7.3 Determination of stresses acting on inclined element

```
9 tx1y1 = -R*sind(2*t); // shear stress at point D
10 disp("Pa",sx1,"The direct stress at point D is")
11 disp("Pa",tx1y1,"The shear stress at point D is")
12 // Point D'; at 2t = 240
13 sx2 = savg + R*cosd(90 + t); // Direct stress at point D
14 tx2y2 = R*sind(90 + t); // shear stress at point D
15 disp("Pa",sx2,"The direct stress at point D_desh is")
16 disp("Pa",tx2y2,"The shear stress at point D_desh is ")
```

Scilab code Exa 7.4 Determination of stresses acting on inclined element using mohrs circle

Scilab code Exa 7.5 Determination of stresses acting on inclined element using Mohrs circle

```
1 sx = 15000; // Direct stress in x-direction in psi
2 sy = 5000; // Direct stress in y-direction ""
3 txy = 4000; // Shear stress in y-direction ""
4 savg = (sx+sy)/2; // Average in-plane direct stress
5 \text{ sx1} = 15000; \text{ tx1y1} = 4000; // \text{Stress acting on face}
      at theta = 0 degree
6 \text{ sx1}_{-} = 5000; \text{ tx1y1}_{-} = -4000; // \text{ Stress acting on}
      face at theta = 0 degree
7 R = sqrt(((sx-sy)/2)^2+(txy)^2) // Radius of mohr
      circle
8 // Part (a)
9 t = 40; // Inclination of the plane in degree
10 f1 = atand (4000/5000); // Angle between line CD and
      x1-axis
11 f2 = 80 - f1; // Angle between line CA and x1-axis
12 // Point D ;
13 sx1 = savg + R*cosd(f2); // Direct stress at point
     D
14 tx1y1 = -R*sind(f2); // shear stress at point D
15 disp("psi", sx1, "The direct stres at point D")
16 disp("psi",tx1y1,"The shear stress at point D")
17 // Point D';
18 sx2 = savg - R*cosd(f2) // Direct stress at point D
19 tx2y2 = R*sind(f2) // shear stress at point D'
20 disp("psi", sx2, "The direct stres at point D_desh")
21 disp("psi",tx2y2,"The shear stress at point D_desh")
22 //Part (b)
23 sp1 = savg + R ; // Maximum direct stress in mohe
      circle (at point P1)
24 tp1 = f1/2; // Inclination of plane of maximum
      direct stress
25 disp("degree",tp1,"with angle","psi",sp1,"The
     maximum direct stress at P1 is ")
  sp2 = savg - R; // Minimum direct stress in mohe
      circle (at point P2)
27 \text{ tp2} = (f1+180)/2; // Inclination of plane of
     minimum direct stress
```

Scilab code Exa 7.6 Determination of stresses acting on inclined element using mohrs circle

```
1 sx = -50e06; // Direct stress in x-direction in psi
2 sy = 10e06; // Direct stress in y-direction ""
3 \text{ txy} = -40\text{e}06 \text{ ; } // \text{ Shear stress in y-direction ""}
4 savg = (sx+sy)/2; // Average in-plane direct stress
5 \text{ sx1} = -50\text{e}06; \text{ tx1y1} = -40\text{e}06; // \text{Stress acting on}
      face at theta = 0 degree
6 \text{ sx1}_{-} = 10e06; \text{ tx1y1}_{-} = 40e06; // \text{ Stress acting on}
      face at theta = 0 degree
7 R = sqrt(((sx-sy)/2)^2+(txy)^2); // Radius of mohr
      circle
8 // Part (a)
9 t = 45; // Inclination of the plane in degree
10 f1 = atand (40e06/30e06) // Angle between line CD
      and x1-axis
11 f2 = 90 - f1; // Angle between line CA and x1-axis
12 // Point D ;
13 sx1 = savg - R*cosd(f2); // Direct stress at point
14 tx1y1 = R*sind(f2); // shear stress at point D
15 disp("Pa", sx1, "The direct stres at point D")
16 disp("Pa",tx1y1,"The shear stress at point D")
17 // Point D';
18 sx2 = savg + R*cosd(f2); // Direct stress at point
```

```
D'
19 tx2y2 = -R*sind(f2); // shear stress at point D'
20 disp("Pa", sx2, "The direct stres at point D_desh")
21 disp("Pa",tx2y2,"The shear stress at point D_desh")
22 // Part (b)
23 sp1 = savg + R; // Maximum direct stress in mohe
      circle (at point P1)
24 tp1 = (f1+180)/2; // Inclination of plane of maximum
       direct stress
25 disp ("degree", tp1, "with angle", "Pa", sp1, "The maximum
       direct stress at P1 is ")
26 sp2 = savg - R; // Minimum direct stress in mohe
      circle (at point P2)
27 \text{ tp2} = f1/2; // Inclination of plane of minimum
      direct stress
28 disp("degree", tp2, "with angle", "Pa", sp2, "The maximum
       direct stress at P2 is ")
29 // Part (c)
30 \text{ tmax} = R; // Maximum shear stress in mohe circle
31 ts1 = (90 + f1)/2; // Inclination of plane of
     maximum shear stress
32 disp("degree",ts1," with plane incilation of", "Pa",
     tmax, "The Maximum shear stress is")
```

Scilab code Exa 7.7 Determination of various strain on inclined element

```
(2*t)) ); // Shear starin
8 ey1 = ex+ey-ex1; // Strain in y1 direction (located
       at 30 degree)
9 disp(ex1," Strain in x1 direction (located at 30
      degree) is")
10 disp(tx1y1, "shear strain is")
11 disp(ey1," Strain in y1 direction (located at 30
      degree) is")
12 // Part (b)
13 e1 = (ex+ey)/2 + sqrt(((ex-ey)/2)^2 + (txy/2)^2); //
       Principle stress
14 e2 = (ex+ey)/2 - sqrt(((ex-ey)/2)^2 + (txy/2)^2); //
      Principle stress
15 tp1 = (0.5)*atand(txy/(ex-ey)); // Angle to
      principle stress direction
16 tp2 = 90 + tp1 ; // Angle to principle stress
      direction
17 e1 = (ex+ey)/2 + ((ex-ey)/2)*cosd(2*tp1) + (txy/2)*(
     sind(2*tp1)); // Principle stress via another
     method
18 e2 = (ex+ey)/2 + ((ex-ey)/2)*cosd(2*tp2) + (txy/2)*(
     sind(2*tp2)); // Principle stress via another
     method
19 disp("degree",tp1," with angle",e1," The Principle
      stress is ")
20 disp("degree", tp2, "with angle", e2, "The Principle
      stress is ")
21 // Part (c)
22 \text{ tmax} = 2*sqrt(((ex-ey)/2)^2 + (txy/2)^2); // Maxmum
     shear strain
23 ts = tp1 + 45; // Orientation of element having
     maximum shear stress
24 \text{ tx1y1}_{-} = 2*(-((ex-ey)/2)*sind(2*ts) + (txy/2)*(
     cosd(2*ts)) ); // Shear starin assosiated with
      ts direction
25 disp("degree", ts, "with angle", tx1y1_, "The Maximum
     shear strain is ")
26 \text{ eavg} = (e1+e2)/2; // Average atrain
```

27 disp(eavg, "The average strain is")

Chapter 8

Applications of Plane Stress Pressure Vessels Beams and Combined Loadings

Scilab code Exa 8.1 Calculation of maximum permissible pressure under various conditions

```
1 d = 18; // inner idameter of the hemisphere in inch
2 t = 1/4; // thickness of the hemisphere in inch
3 // Part (a)
4 sa = 14000; // Allowable tensile stress in Psi
5 Pa = (2*t*sa)/(d/2); // Maximum permissible air
      pressure in Psi
6 disp("psi", Pa, " Maximum permissible air pressure in
      the tank (Part(a)) is")
7 // Part (b)
8 \text{ sb} = 6000 \text{ ; } // \text{ Allowable shear stress in Psi}
9 Pb = (4*t*sb)/(d/2); // Maximum permissible air
      pressure in Psi
10 disp("psi",Pb," Maximum permissible air pressure in
      the tank (Part(b)) is")
11 // Part (c)
12 e = 0.0003 ; // Allowable Strain in Outer sufrface
```

```
of the hemisphere
13 E = 29e06; // Modulus of epasticity of the steel in
14 v = 0.28; // Poissions's ratio of the steel
15 Pc = (2*t*E*e)/((d/2)*(1-v)); // Maximum
     permissible air pressure in Psi
16 disp("psi",Pc," Maximum permissible air pressure in
     the tank (Part(c)) is")
17 // Part (d)
18 Tf = 8100 ; // failure tensile load in lb/in
19 n = 2.5; // Required factor of safetty against
     failure of the weld
20 Ta = Tf / n ; // Allowable load in ld/in
21 sd = (Ta*(1))/(t*(1)); // Allowable tensile stress
     in Psi
  Pd = (2*t*sd)/(d/2); // Maximum permissible air
     pressure in Psi
  disp("psi",Pd," Maximum permissible air pressure in
     the tank (Part(d)) is")
24 // Part (e)
25 Pallow = Pb ; // Because Shear stress in the wall
     governs allowable pressure inside the tank
26 disp ("Because Shear stress in the wall governs
     allowable pressure inside the tank", "psi", Pallow,
     " Maximum permissible air pressure in the tank (
     Part(e)) is")
```

Scilab code Exa 8.2 Calculation of various stresses and strain in cylindrical part of the vessel

```
1 a = 55; // Angle made by helix with longitudinal
        axis in degree
2 r = 1.8; // Inner radius of vessel in m
3 t = 0.02; // thickness of vessel in m
4 E = 200e09; // Modulus of ealsticity of steel in Pa
```

```
5 v = 0.3; // Poission's ratio of steel
6 P = 800e03; // Pressure inside the tank in Pa
7 // Part (a)
8 s1 = (P*r)/t; // Circumferential stress in Pa
9 s2 = (P*r)/(2*t); // Longitudinal stress in Pa
10 // Part (b)
11 t_{max_z} = (s1-s2)/2; // Maximum inplane shear
      stress in Pa
12 t_max = s1/2; // Maximum out of plane shear stress
     in Pa
13 // Part (c)
14 e1 = (s1/(2*E))*(2-v); // Strain in circumferential
      direction
15 e2 = (s2/E)*(1-(2*v)); // Strain in longitudinal
     direction
16 // Part (d)
17 // x1 is the direction along the helix
18 \text{ theta} = 90 - a ;
19 sx1 = ((P*r)/(4*t))*(3-cosd(2*theta)); // Stress
      along x1 direction
20 tx1y1 = ((P*r)/(4*t))*(sind(2*theta)); // Shear
      stress in x1y1 plane
21 sy1 = s1+s2-sx1; // Stress along y1 direction
22 // Mohr Circle Method
23 savg = (s1+s2)/2; // Average stress in Pa
24 R = (s1 - s2)/2; // Radius of Mohr's Circle in Pa
25 \text{ sx1} = savg - R*cosd(2*theta); // Stress along x1
      direction
26 tx1y1_ = R*sind(2*theta); // Shear stress in x1y1
     plane
```

Scilab code Exa 8.3 Investigation of the principal stresses and maximum shear stresses at cross section mn

```
1 L = 6; // Span of the beam in ft
```

```
2 P = 10800; // Pressure acting in lb
3 c = 2 ; // in ft
4 b = 2; // Width of cross section of the beam in inch
5 h = 6; // Height of the cross section of the beam in
      inch
6 \times 9 : // in inch
7 Ra = P/3; // Reaction at point at A
8 V = Ra ; // Shear force at section mn
9 M = Ra*x; // Bending moment at the section mn
10 I = (b*h^3)/12 // Moment of inertia in in4
11 y = -3:0.1:3; // Variation along height
12 sx = -(M/I)*y; // Normal stress on crossection
13 Q = (b*(h/2-y)).*(y+(((h/2)-y)/2))); // First
     moment of rectangular cross section
14 txy = (V*Q)/(I*b); // Shear stress acting on x face
     of the stress element
15 s1 = (sx/2) + sqrt((sx/2).^2 + (txy).^2); // Principal
     Tesile stress on the cross section
16 s2 = (sx/2)-sqrt((sx/2).^2+(txy).^2); // Principal
     Compressive stress on the cross section
17 tmax = sqrt((sx/2).^2+(txy).^2); // Maximum shear
      stress on the cross section
18 plot(sx,y,'o')
19 plot(txy,y,'+')
20 plot(s1,y,'--')
21 plot(s2,y,'<')
22 plot(tmax,y)
23 disp("psi",s1,"Principal Tesile stress on the cross
     section")
24 disp("psi", s2," Principal Compressive stress on the
      cross section")
25 // Conclusions
26 \text{ s1\_max} = 14400 \text{ ; } // \text{ Maximum tensile stress in Psi}
27 txy_max = 900 ; // Maximum shear stress in Psi
28 t_max = 14400/2 ; // Largest shear stress at 45
     degree plane
```

Scilab code Exa 8.4 Determination of stresses in the shaft

```
1 d = 0.05; // Diameter of shaft in m
2 T = 2400 ; // Torque transmitted by the shaft in N-m
3 P = 125000; // Tensile force
4 s0 = (4*P)/(\%pi*d^2) // Tensile stress in
5 t0 = (16*T)/(\%pi*d^3) // Shear force
6 // Stresses along x and y direction
7 \text{ sx} = 0;
8 \text{ sy} = \text{s0};
9 \text{ txy} = -t0;
10 s1 = (sx+sy)/2 + sqrt(((sx-sy)/2)^2 + (txy)^2); //
     Maximum tensile stress
11 s2 = (sx+sy)/2 - sqrt(((sx-sy)/2)^2 + (txy)^2); //
     Maximum compressive stress
12 tmax = sqrt(((sx-sy)/2)^2 + (txy)^2); // Maximum
     in plane shear stress
13 disp("Pa", s1, "Maximum tensile stress")
14 disp("Pa",s2,"Maximum compressive stress")
15 disp("Pa", tmax, "Maximum in plane shear stress")
```

Scilab code Exa 8.5 Determination of the maximum allowable internal pressure

```
1 P = 12; // Axial load in K
2 r = 2.1; // Inner radius of the cylinder in inch
3 t = 0.15; // Thickness of the cylinder in inch
4 ta = 6500; // Allowable shear stress in Psi
5 // From in plane sg=hear stress
6 p1 = (ta - 3032)/3.5; // allowable internal pressure
```

```
7 // Above equation comes from solving the following
     equation
8 // sx = (p*r)/(2*t) - (P)/(2*\%pi*r*t);
9 // sy = (p*r)/t ;
10 // s1 = sy
11 // s2 = sx
12 // ta = (s1-s2)/2
13
14 // From out of the plane shear stress
15 // ta = s1/2
16 p2 = (ta + 3032)/3.5 ; // allowable internal
     pressure
17 // ta = s2/2
18 p3 = 6500/7; // allowable internal pressure
19
20 p_allow = min(p1,p2,p3); // Minimum pressure would
     govern the design
21 disp("Becausem inimum pressure would govern the
     design", "psi", p_allow, "Maximum allowable internal
      pressure ")
```

Scilab code Exa 8.6 Determination of stresses due to wind pressure

```
cross section of the pole
11 sa = (M*d2)/(2*I); // Tensile stress at A
12 Ip = (\%pi/32)*(d2^4-d1^4); // Polar momet of
      inertia of cross section of the pole
13 t1 = (T*d2)/(2*Ip); // Shear stress at A and B
14 r1 = d1/2; // Inner radius of circular pole in m
15 r2 = d2/2; // Outer radius of circular pole in m
16 A = \text{pi}*(r2^2-r1^2); // Area of the cross section
17 t2 = ((4*V)/(3*A))*((r2^2 + r1*r2 + r1^2)/(r2^2 + r1^2)
      ) ; // Shear stress at point B
18 // Principle stresses
19 \text{ sxa} = 0 \text{ ; sya} = \text{sa} \text{ ; txya} = \text{t1;}
20 \text{ sxb} = 0 \text{ ; syb} = 0 \text{ ; txyb} = t1+t2 \text{ ;}
21 // Stresses at A
22 \text{ s1a} = (\text{sxa+sya})/2 + \text{sqrt}(((\text{sxa-sya})/2)^2 + (\text{txya})^2)
      ; // Maximum tensile stress
23 \text{ s2a} = (\text{sxa+sya})/2 - \text{sqrt}(((\text{sxa-sya})/2)^2 + (\text{txya})^2)
       ; // Maximum compressive stress
24 \text{ tmaxa} = \frac{\text{sqrt}(((sxa-sya)/2)^2 + (txya)^2)}{};
      Maximum in plane shear stress
25 disp("Pa",s1a," Maximum tensile stress at point A is"
26 disp("Pa",s2a,"Maximum compressive stress at point A
       is")
27 disp("Pa",tmaxa,"Maximum in plane shear stress at
      point A is")
28 // Stress at B
29 	ext{ s1b} = (sxb+syb)/2 + sqrt(((sxb-syb)/2)^2 + (txyb)^2)
      ; // Maximum tensile stress
30 \text{ s2b} = (\text{sxb+syb})/2 - \text{sqrt}(((\text{sxb-syb})/2)^2 + (\text{txyb})^2)
       ; // Maximum compressive stress
31 \text{ tmaxb} = \frac{\sqrt{((sxb-syb)/2)^2 + (txyb)^2}}{\sqrt{(sxb-syb)/2}}
      Maximum in plane shear stress
32 disp("Pa", s1b, "Maximum tensile stress at point B is"
33 disp("Pa", s2b, "Maximum compressive stress at point B
        is")
34 disp("Pa", tmaxb, "Maximum in plane shear stress at
```

Scilab code Exa 8.7 Determination of stresses due to loads

```
1 b = 6; // Outer dimension of the pole in inch
2 t = 0.5; // thickness of the pole
3 P1 = 20*(6.75*24); // Load acting at the midpoint of
       the platform
4 d = 9; // Distance between longitudinal axis of the
       post and midpoint of platform
5 P2 = 800; // Load in lb
6 \ h = 52; // Distance between base and point of
      action of P2
7 M1 = P1*d; // Moment due to P1
8 M2 = P2*h; // Moment due to P2
9 A = b^2 - (b-2*t)^2; // Area of the cross section
10 sp1 = P1/A; // Comoressive stress due to P1 at A
     and B
11 I = (1/12)*(b^4 - (b-2*t)^4); // Moment of inertia
      of the cross section
12 sm1 = (M1*b)/(2*I); // Comoressive stress due to M1
      at A and B
13 Aweb = (2*t)*(b-(2*t)); // Area of the web
14 tp2 = P2/Aweb; // Shear stress at point B by lpad
15 sm2 = (M2*b)/(2*I); // Comoressive stress due to M2
16 sa = sp1+sm1+sm2; // Total Compressive stress at
      point A
17 sb = sp1+sm1; // Total compressive at point B
18 tb = tp2; // Shear stress at point B
19 // Principle stresses
20 \text{ sxa} = 0 \text{ ; sya} = -\text{sa} \text{ ; txya} = 0;
21 \text{ sxb} = 0; \text{syb} = -\text{sb}; \text{txyb} = \text{tp2};
22 // Stresses at A
```

```
23 \text{ s1a} = (\text{sxa+sya})/2 + \text{sqrt}(((\text{sxa-sya})/2)^2 + (\text{txya})^2)
     ; // Maximum tensile stress
24 	ext{ s2a} = (sxa+sya)/2 - sqrt(((sxa-sya)/2)^2 + (txya)^2)
      ; // Maximum compressive stress
25 \text{ tmaxa} = \frac{\text{sqrt}(((sxa-sya)/2)^2 + (txya)^2)}{};
      Maximum in plane shear stress
26 disp("Psi", s1a, "Maximum tensile stress at point A is
27 disp("Psi", s2a, "Maximum compressive stress at point
      A is")
28 disp("Psi", tmaxa, "Maximum in plane shear stress at
      point A is")
29 // Stress at B
30 	ext{ s1b} = (sxb+syb)/2 + sqrt(((sxb-syb)/2)^2 + (txyb)^2)
      ; // Maximum tensile stress
31 	ext{ s2b} = (sxb+syb)/2 - sqrt(((sxb-syb)/2)^2 + (txyb)^2)
      ; // Maximum compressive stress
32 \text{ tmaxb} = \frac{\text{sqrt}(((sxb-syb)/2)^2 + (txyb)^2)}{}; //
      Maximum in plane shear stress
33 disp("Psi", s1b, "Maximum tensile stress at point B is
34 disp("Psi", s2b, "Maximum compressive stress at point
      B is")
35 disp("Psi", tmaxb, "Maximum in plane shear stress at
      point B is")
```

Chapter 11

Columns

Scilab code Exa 11.1 Determination of the allowable load using a factor of safety with respect to Euler buckling of the column

```
1 E = 29000; // Modulus of elasticity in ksi
2 spl = 42; // Proportional limit in ksi
3 L = 25; // Total length of coloum in ft
4 n = 2.5; // factor of safety
5 I1 = 98; // Moment of inertia on horizontal axis
6 I2 = 21.7; // Moment of inertia on vertical axis
7 A = 8.25 ; // Area of the cross section
8 Pcr2 = (4*\%pi^2*E*I2)/((L*12)^2); // Criticle load
     if column buckles in the plane of paper
9 Pcr1 = (%pi^2*E*I1)/((L*12)^2); // Criticle load if
      column buckles in the plane of paper
10 Pcr = min(Pcr1, Pcr2); // Minimum pressure would
     govern the design
11 scr = Pcr/A ; // Criticle stress
12 Pa = Pcr/n; // Allowable load in k
13 disp("k", Pa, "The allowable load is ")
```

Scilab code Exa 11.2 Determine the minimum required thickness t of the columns wrt Eular bucking of column

```
1 L = 3.25; // Length of alluminium pipe in m
2 d = 0.1; // Outer diameter of alluminium pipe
3 P = 100000; // Allowable compressive load in N
4 n =3; // Safety factor for eular buckling
5 E = 72e09; // Modulus of elasticity in Pa
6 1 = 480e06; // Proportional limit
7 Pcr = n*P; // Critic; e load
8 t = (0.1 - (55.6e-06)^(1/4))/2 ; // Required
     thickness
9 // Above formula comes from solving following
     equation
10 // d2 = d ; d1 = d-2*t ; Pcr = n*P ; I = (\%pi/64)*(
     d2^4-d1^4; Pcr = (2.406*\%pi^2*E*I)/((L)^2);
11 \text{ tmin} = t;
12 disp("mm", tmin*1000, "The minimum required thickness
     of the coloumn is")
13 // Supplimentry calculatios
14 I = (\%pi/64)*(d^4-(d-2*t)^4); // Moment of inertia
15 A = (\%pi/4)*(d^2-(d-2*t)^2); // Area of cross
     section
16 r = sqrt(I/A);
17 s = L/r // slenderness ratio
18 scr = Pcr/A ; // Criticle stress
```

Scilab code Exa 11.3 Determination of longest permissible length of rod

```
1 P = 1500 ; // Load in lb
2 e = 0.45 ; // ecentricity in inch
3 h = 1.2 ; // Height of cross section in inch
4 b = 0.6 ; // Width of cross section in inch
5 E = 16e06 ; // Modulus of elasticity
6 del = 0.12 ; // Allowable deflection in inch
```

```
7 L = asec(1.2667)/0.06588 ; // Maximum allowable
length possible
8 // Above formula comes from solving following
equation
9 // Pcr = (%pi^2*E*I)/(4*(L)^2); I = (h*b^3)/12; del
= e*(sec((%pi/2)*sqrt(P/Pcr))-1)
10 disp("inch",L,"The longest permissible length of the
bar is")
```

Scilab code Exa 11.4 Calculation of compressive stress and factor of safety

```
1 L = 25; // Length of coloum in ft
2 P1 = 320 ; // Load in K
3 P2 = 40 ; // Load in K
4 E = 30000; // Modulus of elasticity of steel in Ksi
5 P = 360 ; // Euivalent load
6 e = 1.5; // Ecentricity of compressive load
7 A = 24.1; // Area of the Cross section
8 r = 6.05 ; // in inch
9 c = 7.155 ; // in inch
10 sy = 42; // Yeild stress of steel in Ksi
11 smax = (P/A)*(1+(((e*c)/r^2)*sec((L/(2*r))*sqrt(P/(E)
     *A))))); // Maximum compressive stress
12 disp("ksi", smax, "The Maximum compressive stress in
     the column ")
13 // Bisection method method to solve for yeilding
14 function [x] = stress(a,b,f)
15
     N = 100;
16
     eps = 1e-5;
     if((f(a)*f(b))>0) then
17
       error('no root possible f(a)*f(b)>0');
18
19
       abort;
20
     end;
21
     if(abs(f(a)) < eps) then</pre>
22
       error('solution at a');
```

```
23
       abort;
24
25
     if(abs(f(b)) < eps) then</pre>
       error('solution at b');
26
27
       abort;
28
     end
29
     while(N>0)
       c = (a+b)/2
30
       if(abs(f(c))<eps) then</pre>
31
32
         x = c;
33
         х;
34
         return;
35
       end;
       if((f(a)*f(c))<0) then
36
37
         b = c;
38
       else
39
          a = c;
40
       end
       N = N-1;
41
42
     end
     error('no convergence');
43
44
     abort;
45 endfunction
46
47 deff('[y]=p(x)', ['y = x + (0.2939*x*sec(0.02916*sqrt)]
      (x))) - 1012
48 x = stress(710,750,p);
49 Py = x; // Yeilding load in K
50 n = Py/P; // Factor of safety against yeilding
51 disp(n,"The factor of safety against yeilding is")
```

Scilab code Exa 11.5 Calculation of allowable axial load and maximum permissible length

```
1 E = 29000; // Modulus of elasticity in ksi
```

```
2 sy = 36; // Yeilding stress in ksi
3 L = 20; // Length of coloumn in ft
4 r = 2.57; // radius of gyration of coloumn
5 K = 1; // Effetive Length factor
6 s = sqrt((2*%pi^2*E)/sy) // Criticle slenderness
     ratio (K*L)/r
7 s_{-} = (L*12)/r; // Slenderness ratio
8 // Part(a)
9 n1 = (5/3)+((3/8)*(s_/s))-((1/8)*((s_^3)/(s^3)));/
     Factor of safety
10 sallow = (sy/n1)*(1-((1/2)*((s_^2)/(s^2)))); //
     Allowable axial load
11 A = 17.6; // Cross sectional area from table E1
12 Pallow = sallow*A ; // Allowable axial load
13 disp("k", Pallow, "Allowable axial load is")
14 // Part (b)
15 Pe = 200; // Permissible load in K
16 L_{-} = 25 ; // Assumed length in ft
17 s_{-} = (L_*12)/r; // Slenderness ratio
18 n1_{-} = (5/3) + ((3/8) * (s_{-}/s)) - ((1/8) * ((s_{-}^3)/(s^3)));
     // Factor of safety
19 sallow_ = (sy/n1_)*(1-((1/2)*((s__^2)/(s^2)))); //
     Allowable axial load
20 A = 17.6; // Area of the cross section in 2
21 Pallow = sallow_*A // Allowable load
22 L1 = [24 24.4 25];
23 \text{ P1} = [201 \ 194 \ 190];
24 L_max = interpln([P1;L1],Pe); // Interpolation for
      getting the length corresponding to permissible
     load
25 disp("ft",L_max,"The maximum permissible length is")
```

Scilab code Exa 11.6 Finding the minimum required thickness for a steel pipe column

```
1 L = 3.6; // Length of steel pipe coloumn
2 d = 0.16; // Outer diameter in m
3 P = 240e03; // Load in N
4 E = 200e09; // Modulus of elasticity in Pa
5 \text{ sy} = 259e06 \text{ ; } // \text{ yeilding stress in Pa}
6 Le = 2*L; // As it in fixed-free condition
7 sc = sqrt((2*%pi^2*E)/sy); // Critical slenderness
      ratio
8 K = 2;
9 // First trial
10 t = 0.007; // Assumed thick ness in m
11 I = (\%pi/64)*(d^4-(d-2*t)^4) // Moment of inertia
12 A = (\%pi/4)*(d^2-(d-2*t)^2) // Area of cross
      section
13 r = sqrt(I/A); // Radius of gyration
14 sc_ = (K*L)/r ; // Slender ness ratio
15 n2 = 1.98; // From equation 11.80
16 sa = (sy/(2*n2))*(sc^2/sc_^2) // Allowable stress
17 Pa = sa*A; // Allowable axial load in N
18 // Interpolation
19 t = [7 8 9];
20 \text{ Pa} = [196 \ 220 \ 243];
21 t_min = interpln([Pa;t],240); // Interpolation for
      getting the minimum length
22 disp("mm", t_min, "The minimum required thickness of
     the steel pipe is")
```

Scilab code Exa 11.7 Determination of the minimum required outer diameter of aluminium tube

```
1 L = 16; // Effective length in inch
2 P = 5; // axial load in K
3 // Bisection method for solvong the quaderatic
4 function [x] = stress(a,b,f)
5 N = 100;
```

```
6
     eps = 1e-5;
7
     if((f(a)*f(b))>0) then
       error('no root possible f(a)*f(b)>0');
8
       abort;
9
10
     end;
11
     if (abs(f(a)) < eps) then
12
       error('solution at a');
13
       abort;
14
     end
     if(abs(f(b)) < eps) then</pre>
15
16
       error('solution at b');
17
       abort;
18
     end
     while(N>0)
19
       c = (a+b)/2
20
21
       if(abs(f(c))<eps) then
22
         x = c;
23
         х;
24
         return;
25
       end;
26
       if((f(a)*f(c))<0) then
27
         b = c;
28
       else
29
         a = c;
30
       end
31
       N = N-1;
32
     end
     error('no convergence');
33
34
     abort;
35 endfunction
36
37 deff('[y]=p(x)',['y = 30.7*x^2 - 11.49*x -17.69'])
38 x = stress(0.9,1.1,p);
39 d = x; // Diameter in inch
40 sl = 49.97/d ; // Slenderness ration L/r
41 dmin = d ; // Minimum diameter
42
43 // The above equation comes from solving the
```

```
following equationd for d
44  // S_allow = 13.7 - 0.23*(L/r) = P/ A ;
45  // A = (%pi/4)*(d^2-(d-2t)^2)
46  // I = (%pi/64)*(d^4-(d-2t)^4)
47  // r = sqrt(I/A)
48  disp("inch",dmin,"The minimum required outer diameter of the tube is")
```

Scilab code Exa 11.8 Determination of allowable axial load maximum allowable length and minimum width of the cross section

```
1 Fc = 11e06; // Compressive desing stress in Pa
2 E = 13e09; // Modulus of elasticity in Pa
3 // Part (a)
4 \text{ Kce} = 0.3 ;
5 c = 0.8;
6 A = 0.12*0.16; // Area of cross section
7 Sl = 1.8/0.12; // Slenderness ratio
8 fi = (Kce*E)/(Fc*Sl^2); // ratio of stresses
9 Cp = ((1+fi)/(2*c)) - sqrt(((1+fi)/(2*c))^2-(fi/c));
      // Coloumn stability factor
10 Pa = Fc*Cp*A; // Allowable Axial load
11 disp("N", Pa, "The allowable axial load is")
12 // Part (b)
13 P = 100000; // Allowable Axial load
14 Cp_ = P/(Fc*A); // Coloumn stability factor
15 // Bisection method method to solve for fi
16 function [x] = stress(a,b,f)
    N = 100;
17
18
     eps = 1e-5;
19
     if((f(a)*f(b))>0) then
20
       error ('no root possible f(a)*f(b)>0');
21
       abort;
22
     end;
23
     if(abs(f(a))<eps) then
```

```
24
        error('solution at a');
25
        abort;
26
      end
27
      if (abs(f(b)) < eps) then
28
         error('solution at b');
29
         abort;
30
      end
31
      while (N>0)
32
        c = (a+b)/2
        if(abs(f(c))<eps) then</pre>
33
34
           x = c;
35
           х;
36
           return;
37
        end;
        if((f(a)*f(c))<0) then
38
39
           b = c;
40
        else
41
           a = c;
42
        end
43
        N = N-1;
44
      error('no convergence');
45
      abort:
46
47 endfunction
48
49 deff('[y]=p(x)',['y=((1+x)/(2*c)) - sqrt(((1+x)/(2*c)))
       /(2*c))^2-(x/c) - Cp_-
50 x = stress(0.1,1,p);
51 \text{ fi}_{-} = x
52 d_{-} = 0.12 ; // Diameter in m
53 L_max = d_*sqrt((Kce*E)/(fi_*Fc)); // Maximum length
        in m
54 disp("m",L_max,"The minimum allowable length is")
55 // Part (c)
56 \text{ b1} = [0.130 \ 0.131 \ 0.132]; // \text{Two choices}
57 \text{ Sl1} = 2.6./\text{b1} // \text{slenderness ratio}
58 \text{ fil} = (\text{Kce*E})./(\text{Fc*Sl1^2}) // \text{Ratio}
59 \text{ Cp1} = ((1+\text{fi1})/(2*\text{c})) - \text{sqrt}(((1+\text{fi1})/(2*\text{c})).^2-(\text{fi1})
```

```
/c)); // Coloumn stability factor
60 P1 = 11000.*Cp1.*b1^2; // Allowable atress
61 Pa1 = 125; // Given allowable stress
62 // Does not require display of result analysis has been shown for b = 0.131
```

Chapter 12

Review of Centroids and Moments of Inertia

Scilab code Exa 12.2 Locating centroid C of the cross sectional area

```
1 A1 = 6*0.5 ; // Partial Area in in2
2 A2 = 20.8 ; // from table E1 and E3
3 A3 = 8.82 ; // from table E1 and E3
4 y1 = (18.47/2) + (0.5/2) ; // Distance between centroid C1 and C2
5 y2 = 0 ; // Distance between centroid C2 and C2
6 y3 = (18.47/2) + 0.649 ; // Distance between centroid C3 and C2
7 A = A1 + A2 + A3 ; // Area of entire cross section
8 Qx = (y1*A1) + (y2*A2) - (y3*A3) ; // First moment of entire cross section
9 y_bar = Qx/A ; // Distance between x-axis and centroid of the cross section
10 disp("inch", -y_bar, "The distance between x-axis and centroid of the cross section is ")
```

Scilab code Exa 12.5 Determination of the moment of inertia Ic with respect to the horizontal axis

```
1 // Following variables are obtained from example
     12.2
2 A1 = 6*0.5; // Partial Area in in2
3 A2 = 20.8; // from table E1 and E3
4 A3 = 8.82; // from table E1 and E3
5 \text{ y1} = (18.47/2) + (0.5/2); // Distance between}
     centroid C1 and C2
6 \text{ y2} = 0; // Distance between centroid C2 and C2
7 \text{ y3} = (18.47/2) + 0.649; // Distance between centroid
      C3 and C2
8 A = A1 + A2 + A3; // Area of entire cross section
9 Qx = (y1*A1) + (y2*A2) - (y3*A3); // First moment of
      entire cross section
10 y_bar = Qx/A; // Distance between x-axis and
     centroid of the cross section
11 c_{bar} = -(y_{bar});
13 I1 = (6*0.5^3)/12; // Moment of inertia of A1
14 I2 = 1170; // Moment of inertia of A2 from table E1
15 I3 = 3.94; // Moment of inertia of A3 from table E3
16 Ic1 = I1 + (A1*(y1+c_bar)^2); // Moment of inertia
     about C-C axis of area C1
17
  Ic2 = I2 + (A2*(y2+c_bar)^2); // Moment of inertia
     about C-C axis of area C2
18 Ic3 = I3 + (A3*(y3-c_bar)^2); // Moment of inertia
     about C-C axis of area C3
19 Ic = Ic1 + Ic2 + Ic3; // Moment of inertia about C-
     C axis of whole area
20 disp("in^4", Ic, "The moment of inertia of entire
     cross section area about its centroidal axis C-C"
     )
```

Scilab code Exa 12.7 Determination of the orientations of the principal centroidal axes and the magnitudes of the principal centroidal moments of inertia for the cross sectional area

```
1 Ix = 29.29e06; // Moment of inertia of crosssection
      about x-axis
2 Iy = 5.667e06; // Moment of inertia of crosssection
      about y-axis
3 \text{ Ixy} = -9.336 \text{ e}06; // Moment of inertia of
      crosssection
4 tp1 = (atand(-(2*Ixy)/(Ix-Iy)))/2; // Angle definig
       a Principle axix
5 \text{ tp2} = 90 + \text{tp1} // ""
6 disp("degree",tp1,"The Principle axis is inclined at
       an angle")
7 disp ("degree", tp2, "Second angle of inclination of
      Principle axis is")
  Ix1 = (Ix+Iy)/2 + ((Ix-Iy)/2)*cosd(tp1) - Ixy*sind(
      tp1); // Principle Moment of inertia
      corresponding to tp1
9 \text{ Ix2} = (\text{Ix+Iy})/2 + ((\text{Ix-Iy})/2)*\cos d(\text{tp2}) - \text{Ixy*sind}(
      tp2); // Principle Moment of inertia
      corresponding to tp2
10 disp("mm^4", Ix1," Principle Moment of inertia
      corresponding to tp1")
11 disp("mm^4", Ix2, "Principle Moment of inertia
      corresponding to tp2")
```