Scilab Textbook Companion for Introduction To Modern Physics Volume 1 by R. B. Singh¹

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Book Description

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Scilab numbering policy used in this document and the relation to the above book.

Exa Example (Solved example)

Eqn Equation (Particular equation of the above book)

AP Appendix to Example(Scilab Code that is an Appednix to a particular Example of the above book)

For example, Exa 3.51 means solved example 3.51 of this book. Sec 2.3 means a scilab code whose theory is explained in Section 2.3 of the book.

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Chapter 1

The Special Theory of Relativity

Scilab code Exa 1.1.3 Ex 3

```
1 //variable initialization
2 x=50, y=20, z=10
                                               //x, y, z
      cordinates in meters (frame s)
3 t=5*10^{-8};
                                              //time in
     seconds (frame s)
4 velocity=0.6*3*10^8;
                                              //velocity
      of observer in s' frame relative to s in meter/
     second
                                              //speed of
5 c=3*10^8;
     light in meter/second
6 Beta=0.6;
7 Gamma=1/((1-Beta^2)^(1/2));
9 //calculation of cordinates in s' frame
                                               //value of
10 xdash=Gamma*(x-(velocity*t));
      x cordinate in frame s' in meters
                                               //value of
11 ydash=y;
      y cordinate in frame s' in meters
                                               //value of
12 zdash=z;
```

Scilab code Exa 1.1.4 Ex 4

```
1 //variable initialization
2 x1 = 20
                                                    //
      position of event 1 in meters (frame s)
3 t1=2*10^(-8);
                                                   //time
      of event 1 in seconds (frame s)
4 x2 = 60
                                                   //
      position of event 2 in meters (frame s)
5 t2=3*10^{-8};
                                                   //time
      of event 2 in seconds (frame s)
6 c=3*10^8;
                                                  //speed
      of light in meter/second
7 v=0.6*c;
                                                  //speed
      of frame s' relative to frame s (meter/second)
8 Beta=0.6
9 Gamma=1/((1-Beta^2)^(1/2));
10
11 //part(i):spatial separation of the events in frame
     _{\rm s} ,
12 separation=Gamma*((x2-x1)-v*(t2-t1));
      spatial separation of the events in frame s' (
      meter)
13
14 //part(ii):time interval between the two events in
     frame s'
```

```
15 interval=Gamma*((t2-t1)-(v*(x2-x1))/(c^2)); //time
    interval between the two events in frame s' (
    second)
16
17 printf("\nIn frame s':\n\t (i)spatial separation=%.2
    f meter\n\t (ii)time interval=%.2e second",
    separation,interval);
```

Scilab code Exa 1.1.5 Ex 5

```
1 //variable initialization
2 x1 = 24
                                                    //
      position of event 1 in meters (frame s)
                                                    //time
3 t1=8*10^{(-8)};
       of event 1 in seconds (frame s)
4 x2 = 48
      position of event 2 in meters (frame s)
5 t2=4*10^{-8};
                                                    //time
      of event 2 in seconds (frame s)
6 c=3*10^8;
                                                    //
      speed of light in meter/second
8 //calculation of velocity of the frame s' so that
     both the events occur simultaneously
9 v=((c^2)*(t^2-t^1))/(x^2-x^1);
                                                    //
      velocity of the frame s' (meter/second)
10
11 printf("\nvelocity of the frame s' = \%.1e meter/
      second", v);
```

Scilab code Exa 1.1.6 Ex 6

```
1 // variable initialization
```

```
2 interval_s=1
     time difference between two events in frame s (
     second)
3 interval_sdash=4
                                                //time
      difference between two events in frame s' (second
4 separation_s=0
      spatial separation of two events in frame s (
     meter)
5 c=3*10^8;
                                                      //
     speed of light (meter/second)
6 v=rand();
     //assign a random value to unknown velocity (meter
     /second)
8 //calculation of spatial separation of the events in
9 Gamma=interval_sdash/(interval_s-(v*(separation_s))
     /(c^2); // calculating gamma
10
11 separation = -2*(((Gamma^2)-1)^(1/2))*c;
                          //spatial separation in s' (
     meter)
12
13 printf("\nspatial separation of the events in frame
     s' = \%.2e meter", separation);
```

Scilab code Exa 1.1.7 Ex 7

1 //variable initialization

```
2 interval_s=0
     //time difference between two events in frame s (
     second)
3 separation_s=1;
     spatial separation of two events in frame s (
     meter)
4 separation_sdash=2;
     spatial separation of two events in frame s' (
     meter)
5 c=3*10^8;
     //speed of light (meter/second)
6 v=rand();
     //assign a random value to unknown velocity of
     frame s' with respect to frame s (meter/second)
8 //calculation of time interval between the events in
      frame s'
9 Gamma=separation_sdash/(separation_s-(v*interval_s))
                //calculating value of Gamma
10 Beta=(1-1/(Gamma^2))^(1/2);
                                         //calculating
     value of Beta
11 v=Beta*c;
     //velocity of s' with respect to s (meter/second)
12 interval_sdash=Gamma*(interval_s-((v*separation_s)/(
     c^2)));
               //time interval between the events in
     frame s' (second)
13
14 printf("\nThe time interval between the events in
     frame s' = \%.2e X0", interval_sdash);
```

Scilab code Exa 1.1.8 Ex 8

```
1 //variable initialization
2 \text{ IbyI_not=.99}
                                       //ratio of moving
      length and rest length
3 c=3*10^8;
                                       //speed of light
     (meter/second)
5 //calculation of velocity of rocket ship
6 Beta=(1-IbyI_not^2)^(1/2);
                                       //calculating
     value of Beta
                                       //velocity of
7 v=Beta*c;
     rocket ship (meter/second)
9 printf("\nThe velocity of the rocket ship = \%.2e
     meter/second",v);
```

Scilab code Exa 1.1.9 Ex 9

```
1 //variable initialization
2 l_dash=1

    //length of the rod in frame s' (meter)
3 Theta_dash_degree=45

    //angle of the rod with x-axis in frame s' (degree)
4 Beta=1/2

    //value of Beta
```

```
6 //calculation of the length of the rod and its
     inclination with x-axis in the frame s
7 Theta_dash_radian=Theta_dash_degree*(%pi/180);
     //conversion of angle Theta in radian from degree
      (radian)
^2))*((cos(Theta_dash_radian))^2))))^(1/2);
             //length of the rod in frame s (meter)
9 tan_theta=tan(Theta_dash_radian)/((1-Beta^2)^(1/2));
     //tan of angle of rod with x-axis in frame s
10 theta=atand(tan_theta);
     //angle of rod with x-axis in frame s (degree)
11
12 printf("\n\t The length of the rod = \%f meter\n\t
     Inclination of rod with x-axis = \%f degree",1,
     theta);
  Scilab code Exa 1.1.10 Ex 10
```

Scilab code Exa 1.1.11 Ex 11

```
//Variable initialization
E=0.25

//Energy of photon (MeV)
Theta=(120*%pi)/180;

//Scattering angle of photon (radian)
a=0.51

//Value of m0*c^2 (Mev)
//Calculation of energy of the photon
E_dash=E/(1+(E/a)*(1-cos(Theta)));

Energy of the scattered photon (MeV)

printf("\nEnergy of the scattered photon = %.3f Mev", E_dash);
```

Scilab code Exa 1.1.12 Ex 12

Scilab code Exa 1.1.13 Ex 13

```
9 printf("\nEnergy of the incident photon = \%.2 \, \mathrm{f} Mev", E);
```

Scilab code Exa 1.1.14 Ex 14

```
1 //variable initialization
2 c=3*10^8;
                                              //speed of
      light (meter/second)
3 u1=0.6*c;
                                              //speed of
      Beta particle 1 in lab frame (meter/second)
4 u2 = -0.8 * c;
                                              //speed of
      Beta particle 2 in lab frame (meter/second)
5 v=u1;
                                              //velocity
      of frame s' where frame s' is attached to the
      first Beta particle (meter/second)
7 //velocity of 2nd Beta particle relative to the 1st
     Beta particle (assuming frame s' is attached to
     the first Beta particle)
8 u2_dash=(u2-v)/(1-((u2*v)/c^2));
                                              //velocity
      of 2nd Beta particle relative to the 1st Beta
      particle (meter/second)
10 printf("\n\tThe velocity of 2nd Beta particle
     relative to the 1st Beta particle = \%.2e meter/
     second", u2_dash);
```

Scilab code Exa 1.1.15 Ex 15

```
//moving
3 m = 3 * m0;
     mass of particle (kg)
                                             //speed of
4 c=3*10^8;
     light (meter/second)
6 //calculation of speed of particle
7 Beta=(1-(m0/m)^2)^(1/2);
      Calculation fo Beta
                                             //speed of
8 v=Beta*c;
      particle (meter/second)
10 printf("\n\tThe speed of The particle = \%.2e meter/
     second", v);
  Scilab code Exa 1.1.23 Ex 23
1 //variable initialization
2 RestEnergy=0.51
                                                //energy
     of electron if the electron is at rest (Mev)
3 KineticEnergy=2
                                                //kinetic
      energy of electron (Bev)
                                                //speed
4 c=3*10^8;
     of light (meter/second)
6 //calculation of momentum of electron
7 p=(KineticEnergy*10^9)/c;
                                                        //
     momentum of electron neglecting rest energy
      relative to kinetic energy (Bev*second/meter)
```

Scilab code Exa 1.1.24 Ex 24

second/meter",p);

9 printf("\n\tThe momentum of the electron = $\%.2 \,\mathrm{f}$ ev*

```
1 //variable initialization
2 n = 0.01
                                      //fractional
     increase in momentum
                                      //speed of light (
3 c=3*10^8;
     meter/second)
5 //calculation of velocity of particle
6 Beta=(n*(2-n))^(1/2);
                                      //calculation of
     Beta
                                      //velocity of
7 v=Beta*c;
     particle (meter/second)
9 printf("\nBeta = \%.1e\nThe velocity of the particle
    = \%.2e meter/second", Beta, v);
```

Scilab code Exa 1.1.26 Ex 26

```
1 //variable initialization
                                                       //
2 RestEnergy=0.51
      rest energy of electron (Mev)
3 T=1
                                                       //
     potential difference i.e. kinetic energy (Mev)
4 c=3*10^8;
                                                       //
     speed of light (meter/second)
6 //calculation of speed of electron
7 Beta=(1-(RestEnergy/(T+RestEnergy))^2)^(1/2);
                                                       //
      calculation of Beta
8 v=Beta*c;
                                                       //
     speed of electron (meter/second)
10 printf("\ntThe speed of the electron = %.2e meter/
     second", v);
11
12 // Note: In the book answer of Beta is slightly wrong
```

Scilab code Exa 1.1.27 Ex 27

```
1 //variable initialization
2 RestEnergy=0.51
                                                       //
      rest energy of electron (Mev)
3 T = 2000
      potential difference i.e. kinetic energy (Mev)
5 //part(i) effective mass of electron in terms of its
      rest mass
6 EffectiveMass=1+(T/RestEnergy);
      ratio of effective mass of electron and rest mass
8 //part(ii)speed of electron in terms of the speed of
9 Beta=(1-(1/EffectiveMass)^2)^(1/2);
                                                       //
      Calculatio of Beta
10
11 printf("\n\t The effective mass of electron = \%.2 f*
     mo ; mo is rest mass of electron\n\t The speed
     of electron = \%.10 \, f * c
                             ; c is speed of light",
     EffectiveMass, Beta);
12
13 // Note: In the book answer of m/mo is slightly wrong
```

Scilab code Exa 1.1.28 Ex 28

```
1 //variable initialization
2 c=3*10^8;
    //speed of light(meter/second)
```

```
3 v1=0.6*c;
     //initial velocity of particle (meter/second)
4 v2=0.8*c;
     //final velocity of particle (meter/second)
5
6 // Calculation of work required to increase the
      velocity from v1 to v2:
8 // Classically
9 W_{Classic}=0.5*((v2/c)^2-(v1/c)^2);
                                      //ratio of work
     and m0*c^2 (mo is the rest mass of particle and c
      is the speed of light)
10
11 // Relativistically
12 W_Relative = (1/(1-(v2/c)^2)^(1/2))-(1/(1-(v1/c)^2)
     ^(1/2));
                       //ratio of work and m0*c^2 (mo
     is the rest mass of particle and c is the speed
     of light)
13
14 printf("\nWork required:\n\t Classically: Work = \%.2
      f*m0*c^2 \ N \ Eelativistically: Work = \%.3 f*m0*c
      ^2\nWhere m0:rest mass of particle & c:speed of
     light", W_Classic, W_Relative);
```

Scilab code Exa 1.1.29 Ex 29

```
wavelength (meter)
5 lambda2=0.1*10^-10
                                                          //
      wavelength (meter)
7 // Calculation of effective mass of photon:
9 //part(i): wavelength=5000
10 m1=h/(lambda1*c);
                                                           //
      effective mass of photon of wavelength 5000
11
12 / part(ii): wavelength = 0.1
13 m2=h/(lambda2*c);
                                                           //
      effective mass of photon of wavelength 0.1
14
15 printf("\neffective mass of photon:\n\t(i) mass = \%
      .2e \text{ kg} \ \text{(ii)} \ \text{mass} = \%.2e \text{ kg} \text{,m1,m2)};
   Scilab code Exa 1.1.30 Ex 30
1 //variable initialization
2 RestEnergy=0.51
                                                          //
      rest energy of electron (Mev)
4 //calculation of minimum energy of a gamma ray
      photon which is required to produce an electron
      positron pair
5 E=2*RestEnergy;
                                                           //
      minimum energy of gamma ray photon (Mev)
7 printf("\nMinimum energy required = \%.2 f Mev", E);
```

Scilab code Exa 1.1.33 Ex 33

```
1 // variable initialization
                                                    //
2 c=3*10^8;
     Speed of sound (meter/second)
3 M=1.97*10^30;
     Mass of sun (kg)
4 R=1.5*10^11;
     Mean radius of the earth orbit (meter)
5 \text{ sigma}=1.4*10^3;
     Solar energy received by the earth (joule/meter
     ^2*second)
7 //calculation of the fractional loss of mass of the
     sun per second
8 loss=(4*%pi*R^2*sigma)/(M*c^2);
     Fractional loss of mass of the sun per second
9
10 printf("\nThe fractional loss of mass of the sun per
      second = \%.0e",loss);
```

Chapter 2

Origin of Quantum Concepts

Scilab code Exa 2.1.1 Ex 1

```
1 // variable initialization
2 c1 = 0.01
3 c2=0.1
4 c3=1
5 c4 = 10
6 b=2.898*10^{-3};
     //Wien's constant (meter-kelvin)
7 h=(6.625*10^{-34})/(2*\%pi);
     //Planck's constant (joule-second)
8 c=3*10^8;
     //speed of light (meter/second)
9 k=1.38*10^-23;
     //Boltzmann constant (joule/kelvin)
10 T=3000
     //Temperature of black body (kelvin)
11 Delta_lembda=1*10^-9;
```

```
//wavelength interval (meter)
12
13 //(a) Average energy of Planck's oscillator:
14 E1=c1/(%e^c1-1);
      //Average energy of Planck's oscillator
15 E2=c2/(%e^c2-1);
      //Average energy of Planck's oscillator
16 E3=c3/(%e^c3-1);
      //Average energy of Planck's oscillator
17 E4=c4/(%e^c4-1);
      //Average energy of Planck's oscillator
18
19 //(b) Power radiated by a unit area of a black body
20 P=(4*\%pi^2*h*c^2*T^5*Delta_lembda)/(b^5*((%e^((2*\%pi^2)))))
                                       //The power radiated
      *h*c)/(b*k)))-1));
      per unit area (watt/meter^2)
21
22 printf("\n(a) The average energy of Planck's
      oscillator:\n\t (i) Energy = \%.3 f kT \cdot n \cdot t (ii)
      Energy = \%.2 \text{ f kT} \cdot \text{n} \cdot \text{t (iii)} Energy = \%.2 \text{ f kT} \cdot \text{n} \cdot \text{t (}
      iv) Energy = \%.5 f kT n t k: Boltzmann constant =
      %.2e joule/kelvin
                              T: Temperature \setminus n(b) The
      power radiated per unit area = \%.2 f watt/meter^2"
      ,E1,E2,E3,E4,k,P);
```

Scilab code Exa 2.1.2 Ex 2

```
1 //variable initialization
2 v=2*10^-2;
```

```
//side of the cube (meter)
3 lembda=5000*10^-10;
      //wavelength (meter)
4 delta_lembda=10*10^-10;
      //range of wavelength (meter)
5 k=1.38*10^-23;
     //Boltzmann constant (joule/kelvin)
6 T = 1500
     //Temperature of the cavity (kelvin)
8 //(i)Number of modes:
9 N=(8*\%pi*v^3*delta_lembda)/lembda^4;
                                                    //
     number of modes
10
11 //(ii) Total radiant energy in the cavity:
12 U = N * k * T;
     //energy density (joule)
13
14 printf("\n(a) Number of modes = \%.3e\n(b) Energy
      density = \%.2e joule", N, U);
15
16 //Note: In book the answers of both the parts are
      wrong by one order of magnitude
   Scilab code Exa 2.1.3 Ex 3
1 //variable initialization
2 m = 0.1
```

```
//mass of a spring-mass system (kg)
3 k = 10
     //spring constant of a spring-mass system (newton
     /meter)
4 A = 0.1
     //Amplitude of system oscillation (meter)
5 h=(6.625*10^-34)/(2*\%pi);
     //Planck's constant (joule-second)
6 delta_n=1
     //change in quantum number
8 //(a) Quantum number n associated with the energy of
      the oscillator
9 f = (k/m)^(1/2);
     //frequency of oscillator (radian/second)
10 E=0.5*f*A^2;
     //Energy of oscillator (joule)
11 n=E/(h*f);
     //Quantum number of the oscillator
12
13 //(b) Fractional change in energy
14 change_E=delta_n/n;
     //fractional change in energy
15
16 //(c) Conclusion: This example illustrates that the
      energy levels of macroscopic oscillators are so
      close together that even most delicate
     instruments cannot reveal the quantized nature of
      energy levels. All this is due to smallness of
      Planck s constant h. In the limit h->0, the
```

energy levels become continuous. 17 18 printf("\n(a) Quantum number of the oscillator = %.1 $e \setminus n(b)$ Fractional change in energy = $\%.1e \setminus n(c)$ This example illustrates that the energy levels of macroscopic oscillators are so close together that even most delicate instruments cannot reveal the quantized nature of energy levels. All this is due to smallness of Planck s constant h. In the limit h->0, the energy levels become continuous.",n,change_E); 19 20 // The answer given in the book for quantum number is just the order of it as it is a very large number. But the answer generated by the code is the exact value of it.

Scilab code Exa 2.1.4 Ex 4

```
//variable initialization
e=1.6*10^-19;

//Charge of electron (coulombs)
h=(6.625*10^-34)/(2*%pi);

//Planck's constant (joule-second)
c=3*10^8;

//Speed of light (meter/second)
//calculating ch by using ch = 2*pi*h*c
ch=(2*%pi*h*c*10^9)/e;

//Value of ch (eV nm)
```

```
9 printf("\nch = \%.0 f eV nm", ch);
```

```
Scilab code Exa 2.1.5 Ex 5
1 // variable initialization
2 h=(6.625*10^-34)/(2*\%pi);
      //Planck's constant (joule-second)
3 c=3*10^8;
      //speed of light (meter/second)
4 lembda=2000;
      //Wavelength of the light ( )
5 \text{ phi}=4.2
      //work function of aluminium surface (eV)
6 \text{ ch} = 12400
      //constant (eV )
8 //(a) maximum kinetic energy of photoelectrons
9 Tmax=(ch/lembda)-phi;
      //maximum kinetic energy of photoelectrons (eV)
10
11 //(b) minimum kinetic energy of photoelectrons
12 \text{ Tmin=0}
13
14 //(c) cut-off wavelength
15 lembda_cut=ch/phi;
     // cut-off wavelength ( )
16
17 //(d) stopping potential
```

```
//stopping potential (volt)

printf("\n(a) Maximum kinetic energy of
    photoelectrons = %.0 f eV\n(b) Minimum kinetic
    energy of photoelectrons = %.0 f\n(c) Cut-off
    wavelength = %.0 f \n(d) Stopping potential = %
    .0 f volt", Tmax, Tmin, lembda_cut, v);

//Note: In book answer of cut_off wavelength is
    wrong
```

Scilab code Exa 2.1.6 Ex 6

```
//variable initialization
lembda1=4000

//wavelength of light ( )
V1=2

//stopping potential (volt)
lembda2=6000

//wavelength of light ( )
V2=1

//stopping potential (volt)
e=1.6*10^-19;

//Charge of electron (coulombs)
c=3*10^8;

//speed of light (meter/second)
ch=12400
```

```
//constant (eV )
9 //(i) Planck's constant
10 h=(e*(V1-V2)*lembda1*10^-10*lembda2*10^-10)/(c*((
    lembda2*10^-10)-(lembda1*10^-10))); //Planck's
    constant (joule-second)
11
12 //(ii) Work function
13 phi=(ch/lembda1)-V1;

//work function of the material (eV)
14
15 printf("\n(i) Planck's constant = h = %.1e joule-
    second\n(ii) Work function of the material = %.1f
    eV",h,phi);
```

Scilab code Exa 2.1.7 Ex 7

```
//variable initialization
ch=12400

//constant (eV )
phi_Tantalum=4.2

//work function of Tantalum (eV)
phi_Tungsten=4.5

//work function of Tungsten (eV)
phi_Aluminium=4.2

//work function of Aluminium (eV)
phi_Barium=2.5

//work function of Barium (eV)
phi_Lithium=2.3
```

```
//work function of Lithium (eV)
9 // Calculation
10 lembda_Tantalum=ch/phi_Tantalum;
      Threshold wavelength of Tantalum (
11 lembda_Tungsten=ch/phi_Tungsten;
      Threshold wavelength of Tungsten (
12 lembda_Aluminium=ch/phi_Aluminium;
      Threshold wavelength of Aluminium ( )
13 lembda_Barium=ch/phi_Barium;
      //Threshold wavelength of Barium ( )
14 lembda_Lithium=ch/phi_Lithium;
      //Threshold wavelength of Lithium ( )
15
16 if (lembda_Tantalum < 8000&lembda_Tantalum > 4000) then
                                     //Checking whether
      Threshold wavelength of Tantalum lies in visible
      range or not
       disp ("Tantalum can be used for designing
17
          photocell")
18 end
19
20 if (lembda_Tungsten < 8000&lembda_Tungsten > 4000) then
                                     //Checking whether
      Threshold wavelength of Tungsten lies in visible
      range or not
21
       disp ("Tungsten can be used for designing
          photocell")
22 end
23
24 if (lembda_Aluminium < 8000&lembda_Aluminium > 4000) then
                                   //Checking whether
```

```
Threshold wavelength of Aluminium lies in visible
       range or not
       disp("Aluminium can be used for designing
25
          photocell")
26 \text{ end}
27
28 if (lembda_Barium < 8000&lembda_Barium > 4000) then
                                            //Checking
      whether Threshold wavelength of Barium lies in
      visible range or not
       disp("Barium can be used for designing photocell
29
          ")
30 \text{ end}
31
32 if (lembda_Lithium <8000&lembda_Lithium >4000) then
                                         //Checking
      whether Threshold wavelength of Lithium lies in
      visible range or not
       disp ("Lithium can be used for designing
33
          photocell")
34 end
   Scilab code Exa 2.1.8 Ex 8
```

```
1 //variable initialization
2 lembda_c=0.024

    //Compton wavelength of electron ( )
3 lembda=1

    //Wavelength of X-rays ( )
4 Theta1=(60*%pi)/180;

    //angle (radian)
5 Theta2=(90*%pi)/180;
```

```
//angle (radian)
6 Theta3=(180*\%pi)/180;
     //angle (radian)
7 ch=12400
     //constant (eV )
9 //(a) Compton shift
10 shift1=lembda_c*(1-cos(Theta1));
     Compton shift ( )
11 shift2=lembda_c*(1-cos(Theta2));
     Compton shift ( )
12 shift3=lembda_c*(1-cos(Theta3));
     Compton shift ( )
13
14 //(b) Kinetic energy imparted to the recoil electron
15 T1=(ch*shift1)/(lembda*(lembda+shift1));
                                               //Kinetic
      energy imparted to the electron (eV)
16 T2=(ch*shift2)/(lembda*(lembda+shift2));
                                               //Kinetic
      energy imparted to the electron (eV)
17 T3=(ch*shift3)/(lembda*(lembda+shift3));
                                               //Kinetic
      energy imparted to the electron (eV)
18
19 printf("\n(a) Compton shift:\nt (i) %.3 f
                                               \n\t (ii
             \nt (iii) %.3f \n(b) Kinetic energy
     imparted to the recoil electron:\n\t (i) \%.0f eV\
     n \setminus t (ii) %.0 f eV \setminus n \setminus t (iii) %.0 f eV", shift1, shift2
      ,shift3,T1,T2,T3);
```

```
Scilab code Exa 2.1.9 Ex 9
1 //variable initialization
2 lembda_c = 0.024
     //Compton wavelength of electron ( )
3 Theta=(45*\%pi)/180;
     //Scattering angle (radian)
5 // Calculation of wavelength of incident photon
6 lembda=lembda_c*(1-cos(Theta));
     //Wavelength of incident photon ( )
8 printf("\n(a) Wavelength of incident photon = \%.4 f
       \n(b) Photon lies in the gamma ray spectrum",
     lembda);
  Scilab code Exa 2.1.10 Ex 10
1 //variable initialization
2 E = 1
     //Energy of photon (MeV)
3 \text{ eta} = 0.25
     //Relative change in photon's wavelength
```

5 // Calculation of kinetic energy of electron

6 T=(E*eta)/(1+eta);

```
//Kinetic energy of recoil electron (MeV)
8 printf("\nThe kinetic energy of recoil electron = \%
     .1~\mathrm{f~MeV}", T);
  Scilab code Exa 2.1.11 Ex 11
1 // Variable initialization
2 E=0.25
     //Energy of photon (MeV)
3 Theta=(120*\%pi)/180;
     //Scattering angle of photon (radian)
4 a=0.51
     //Value of m0*c^2 (Mev)
6 // Calculation of energy of the photon
7 E_{das}=E/(1+(E/a)*(1-\cos(Theta)));
                                                      //
     Energy of the scattered photon (MeV)
9 printf("\nEnergy of the scattered photon = \%.3 f Mev"
     ,E_das);
  Scilab code Exa 2.1.12 Ex 12
1 //variable initialization
2 p=1.02
     //momentum of the photon (MeV/c)
```

Scilab code Exa 2.1.13 Ex 13

```
Scilab code Exa 2.1.14 Ex 14
1 // variable initialization
2 lembda0=2536*10^-10;
      //wavelength of exciting line (meter)
3 lembda = 2612 * 10^- - 10;
      //wavelength of Raman line (meter)
5 // Calculation of the Raman shift
6 \text{ v0=1/lembda0};
      //wave number of exciting line (1/meter)
7 v=1/lembda;
      //wave number of Raman line (1/meter)
8 \text{ shift=} v0-v;
      //the Raman shift (1/meter)
10 printf("\nThe Raman shift = \%.0 \, \text{f m-1}", shift);
12 // Note: Answer given in the book is an approximate
      answer
```

```
Scilab code Exa 2.1.15 Ex 15
```

```
1 // variable initialization
```

```
2 lembda0 = 5000 * 10^-10;
      //Wavelength of radiation (meter)
3 lembda=5050.5*10^-10;
      //Wavelength of Raman line (meter)
4
5 //(a) Raman frequency
6 \text{ v0=1/lembda0};
      //Wave number of radiation (1/meter)
7 v=1/lembda;
      //Wave number of Raman line (1/meter)
8 \text{ shift=} v0-v;
      //Raman shift (1/meter)
9 va=v0+shift;
      //Frequency of antistoke's line (1/meter)
10
  //(b) Position of the antistokes' line
12 lembdaa=10^10/va;
      //Wavelength of antistoke's line ( )
13
14 printf("\n(a) Raman frequency = %.2e m-1\n(b)
      Wavelength of antistoke's line = \%.2 \,\mathrm{f} ", va,
      lembdaa);
```

Wave Nature of Material Particles

Scilab code Exa 2.2.1 Ex 1

```
1 //variable initialization
2 m=9.1*10^-31;

    //mass of electron (kg)
3 h=6.6*10^-34;

    //planck's constant (joule-second)
4 e=1.6*10^-19;

    //charge of electron (coulomb)
5 //calculation of wavelength of electron
7 a=(h*10^10)/(2*m*e)^(1/2);

    //wavelength of electron = h/(2*m*e*v)^(1/2) ( )
8 printf("\n Wavelength of electron accelerated through a potential difference V = %.1 f/V^0.5 ",a);
```

```
Scilab code Exa 2.2.3 Ex 3
1 //variable initialization
2 \text{ m_e=9.1*10^--31};
      //mass of electron (kg)
3 m = 100 * 10^{-3};
     //mass of object (kg)
4 v = 1000
     //velocity of electron and object (meter/second)
5 h=6.63*10^{-34};
      //planck's constant (joule-second)
6 //(i) de Broglie wavelength of electron
7 lembda_e=h/(m_e*v);
      //de Broglie wavelength of electron
8
9 //(ii) de Broglie wavelength of object
10 lembda=h/(m*v);
      //de Broglie wavelength of object
11
12 printf("\n(i) de Broglie wavelength of electron = \%
      .3e \text{ meter} \setminus n(ii) de Broglie wavelength of object =
      %.2e meter\nOwing to extremely short wavelength
      of the object its wave behavior cannot be
      demonstrated.",lembda_e,lembda);
13
14 //Note: In the book the answer of part(ii) is wrong
```

Scilab code Exa 2.2.4 Ex 4

```
1 // variable initialization
2 e=1.6*10^-19;
      //charge of electron (coulomb)
3 T=100*e;
      //kinetic energy (joule)
4 \text{ m_e=9.1*10^--31};
      //mass of electron (kg)
5 \text{ m_p=1.67*10^--27};
      //mass of proton (kg)
6 \text{ m\_alpha=}4*\text{m\_p};
      //mass of alpha particle (kg)
7 h=6.63*10^-34;
      //planck's constant (joule-second)
9 //calculation of de Broglie wavelengths
10 lembda_e=(h*10^10)/(2*m_e*T)^(1/2);
                                                      //de
      Broglie wavelength of electron ( )
  lembda_p=(h*10^10)/(2*m_p*T)^(1/2);
                                                      //de
      Broglie wavelength of proton ( )
  lembda_alpha=(h*10^10)/(2*m_alpha*T)^(1/2);
                                             //de Broglie
      wavelength of alpha particle (
13
14 printf("\nde Broglie wavelength of electron = \%.2 f
```

```
\nde Broglie wavelength of proton = \%.3 \, f \nde Broglie wavelength of alpha particle = \%.3 \, f ", lembda_e,lembda_p,lembda_alpha);
```

Scilab code Exa 2.2.5 Ex 5

```
1 // variable initialization
2 h=6.63*10^{-34};
      //planck's constant (joule-second)
3 m=9.1*10^-31;
      //mass of electron (kg)
4 lembda=5896*10^-10;
     //wavelength of yellow spectral line of sodium (
      meter)
5 e=1.6*10^-19;
      //charge of electron (coulomb)
7 //calculation of kinetic energy of electron
8 T_j=h^2/(2*m*lembda^2);
      //kinetic energy of the electron (joule)
9 T_eV=T_j/e;
      //kinetic energy of the electron (eV)
10
11 printf("\n kinetic energy of electron = \%.2e joule =
      \%.1\,\mathrm{e}~\mathrm{eV}", T_j, T_eV);
```

Scilab code Exa 2.2.6 Ex 6

```
1 //variable initialization
2 h=6.63*10^{-34};
      //planck's constant (joule-second)
3 m_n=1.67*10^-27;
      //mass of neutron (kg)
4 T = 300
     //Temperature (kelvin)
5 k=1.38*10^-23;
     //Boltzmann constant (joule/kelvin)
7 //calculation of the wavelength of thermal neutron
8 E = (3*k*T)/2;
      //Kinetic energy of thermal neutron (joule)
9 lembda=(h*10^10)/(2*m_n*E)^(1/2);
                                                       //
      Wavelength of thermal neutron ( )
10
11 printf("\nThe wavelength of thermal neutron = \%.2 f
        ",lembda);
   Scilab code Exa 2.2.7 Ex 7
1 // variable initialization
2 h=6.63*10^{-34};
      //planck's constant (joule-second)
3 \text{ m}_H2 = 2*1.67*10^-27;
      //mass of hydrogen molecule (kg)
4 T=27+273;
```

```
//room temperature (kelvin)
5 k=1.38*10^-23;
     //Boltzmann constant (joule/kelvin)
7 //calculation of de Broglie wavelength of hydrogen
     molecule
8 lembda=(h*10^10)/(2*m_H2*k*T)^(1/2);
                                                    //de
      Broglie wavelength of hydrogen molecule (
10 printf("\nThe de Broglie wavelength of hydrogen
      molecules at their most probable speed = \%.2 f
      ,lembda);
  Scilab code Exa 2.2.8 Ex 8
1 // variable initialization
2 a=0.51
     //Value of m0*c^2 (Mev)
3
4 // Calculation of kinetic energy of electron
5 T=a*(sqrt(2)-1);
     //Kinetic energy (MeV)
7 printf("\n Kinetic energy of electron = \%.2 \, \text{f MeV}",T)
```

Scilab code Exa 2.2.9 Ex 9

```
1 // variable initialization
2 a=0.51
     //Value of m0*c^2 (MeV)
3 b=0.0124
     //Value of h*c (MeV
4 lembda_X=0.1
     //Short wavelength limit of continuous X-ray
     spectrum ( )
6 //calculation of de Broglie wavelength of electron
7 lembda=lembda_X/(1+(2*a*lembda_X)/b)^(1/2);
                                                 //de
     Broglie wavelength of relativistic electrons
9 printf("de Broglie wavelength of relativistic
     electrons = \%.3 \,\mathrm{f} ",lembda);
  Scilab code Exa 2.2.10 Ex 10
1 // variable initialization
2 r=0.53
     //Radius of the first Bohr orbit in hydrogen atom
      4 //calculation of de Broglie wavelength of electron
5 lembda=2*%pi*r;
     //de Broglie wavelength of electron in first Bohr
      orbit in hydrogen atom
```

7 printf("\nde Broglie wavelength of electron in first

Scilab code Exa 2.2.12 Ex 12

```
1 // variable initialization
2 v = 10000
     //speed of object (meter/second)
3 \text{ accu_v} = 0.0001
     //accuracy of speed of object
4 m_b = 0.05
     //mass of the bullet (kg)
5 h=1.054*10^-34;
     //planck's constant (joule-second)
6 m_e=9.1*10^-31;
      //mass of electron (kg)
8 //(a) fundamental accuracy of position for bullet
9 p_b = m_b * v;
     //momentum of bullet (kg m/s)
10 p_uncer_b=p_b*accu_v;
     //uncertainty in momentum of bullet (kg m/s)
11 x_uncer_b=h/p_uncer_b;
     //minimum uncertainty in position of bullet (
     meter)
12
13 //(b) fundamental accuracy of position for electron
14 p_e=m_e*v;
```

```
//momentum of electron (kg m/s)
15 p_uncer_e=p_e*accu_v;
     //uncertainty in momentum of electron (kg m/s)
16 x_uncer_e=h/p_uncer_e;
     //uncertainty in position of electron (meter)
17
18 printf("\n(a) uncertainty in position of bullet = %
      .1e meter\n(b) uncertainty in position of
      electron = \%.6 f meter\n The uncertainty in
      bullet s position is so small that it is far
     beyond the possibility of measurement.",x_uncer_b
      ,x_uncer_e);
19
20 //Note: The answers given in the book are wrong. Also
      in the solution they have used speed=1000 while
     in the question it is given to be equal to 10000.
  Scilab code Exa 2.2.13 Ex 13
1 //variable initialization
2 h=1.054*10^{-34};
     //planck's constant (joule-second)
3 m=9.1*10^-31;
     //mass of electron (kg)
4 x_uncer=1*10^-10;
     //uncertainty in the position of electrons (meter)
5 e=1.6*10^-19;
```

//charge of electron (coulomb)

```
6
7 //(i) uncertainty in the momentum of electron
8 p_uncer=h/x_uncer;

    //The uncertainty in the momentum of electron (kg m/s)
9
10 //(ii) kinetic energy of electron
11 T=p_uncer^2/(2*m*e);

    //kinetic energy of electron (eV)
12
13 printf("\n(i) The uncertainty in the momentum of electron = %.3e kg m/s\n(ii) Kinetic energy of electron = %.1f eV\n The ionization potential of atoms is of this order and hence the uncertainty in momentum is consistence with the binding energy of electrons in atoms.",p_uncer,T);
```

Scilab code Exa 2.2.14 Ex 14

```
1 //variable initialization
2 h=1.054*10^-34;

    //planck's constant (joule-second)
3 x=10^-14;

    //dimension of the nucleus (meter)
4 c=3*10^8;

    //speed of light (meter/second)
5 e=1.6*10^-19;

    //charge of electron (coulomb)
```

```
7 //(i) Uncertainty in the momentum of electron
8 p_uncer=h/x;
     //The uncertainty in the momentum of electron (kg
      m/s)
9
10 //(ii) kinetic energy of electron
11 T=(p_uncer*c)/(e*10^6);
     //kinetic energy of electron (MeV)
12
13 printf("\n(i) The uncertainty in the momentum of
     electron = \%.3e kg m/s\n(ii) Kinetic energy of
     electron = \%.0 f MeV\n Experiments show that
     energy of electrons in nuclear disintegration (
     beta decay) is very much less than %.0 f MeV.
     Hence the uncertainty principle rules out the
     possibility of electrons being a nuclear
     constituent.",p_uncer,T,T);
```

Scilab code Exa 2.2.15 Ex 15

```
1 //variable initialization
2 h=1.054*10^-34;

    //planck's constant (joule-second)
3 x=10^-14;

    //dimension of the nucleus (meter)
4 e=1.6*10^-19;

    //charge of electron (coulomb)
5 m=1.67*10^-27;
```

```
//mass of proton (kg)

//(i) Uncertainty in the momentum of electron
p_uncer=h/x;

//The uncertainty in the momentum of electron (kg m/s)

//(ii) kinetic energy of proton
T=(p_uncer^2)/(2*m*e*10^6);

//kinetic energy of proton (MeV)

printf("\n(i) The uncertainty in the momentum of electron = %.3e kg m/s\n(ii) Kinetic energy of proton = %.2f MeV\n The binding energies of nuclei are of this order.",p_uncer,T);
```

Scilab code Exa 2.2.17 Ex 17

```
//variable initialization
h=1.054*10^-34;

//planck's constant (joule-second)
delta_t=10^-12;

//time for which nucleus remains in excited state (second)

//calculation of uncertainty in the energy of the gamma ray photon emitted by the nucleus
delta_E=h/delta_t;

//uncertainty in the energy of the gamma ray photon (joule)
```

```
8 printf("\nThe uncertainty in the energy of the gamma
      ray photon = \%.3e joule", delta_E);
  Scilab code Exa 2.2.18 Ex 18
1 //variable initialization
2 delta_t=10^-8;
     //life-time of the average excited atom (second)
4 //calculation of the minimum uncertainty in the
     frequency of photon
5 delta_f=1/delta_t;
     //minimum uncertainty in the frequency of photon
     (radian/second)
7 printf("\nminimum uncertainty in the frequency of
     photon = \%.0e radian/second", delta_f);
  Scilab code Exa 2.2.19 Ex 19
1 // variable initialization
2 h=1.054*10^{-34};
     //planck's constant (joule-second)
3 e=1.6*10^-19;
     //charge of electron (coulomb)
4 m=9.1*10^-31;
     //mass of electron (kg)
```

```
// E0=8.8542*10^-12;
// permittivity of free space (C^2/N*m^2)

//(i) radius of ground state of hydrogen atom
r=(4*%pi*E0*h^2)/(m*e^2);

//radius of ground state of hydrogen atom (meter)

//(ii) Binding energy of electron in hydrogen atom in the ground state

E=(-0.5*m*e^4)/(4*%pi*E0*h)^2;

//binding energy of electron in hydrogen atom in the ground state (joule)

printf("\n(i) Radius of ground state of hydrogen atom = %.3 e meter\n(ii) Binding energy of electron in ground state of hydrogen atom = %.2 e joule",r,E);
```

Particle in a Box

Scilab code Exa 2.6.1 Ex 1

```
//variable initialization
x=(1/3):.01:(2/3);
x0=1/3;
x1=2/3;
//calculation
P=2*integrate('(sin(%pi*x))^2', 'x', x0, x1);
printf("The required probability = %.2f",P);
```

Scilab code Exa 2.6.2 Ex 2

```
1 // variable initialization
2 x=0:.001:(1/3);
3 y=0:.001:(1/3);
4 x0=0;
5 x1=1/3;
6 y0=0;
```

Scilab code Exa 2.6.3 Ex 3

```
1 //variable initialization
2 L = 10;
3 n = 2;
4
5 //Calculation
6 X = L/2;
7 X_square = ((L^2)/3)-((L^2)/(2*(n^2)*(3.14^2)));
8
9 printf("\nExpectation of X = %.2f",X);
10 printf("\nExpectation of X^2 = %.2f",X_square);
```

Particle in a Central Force Field

Scilab code Exa 2.9.2 Ex 2

```
1 //variable initialization
2 x=0:0.1:9999;
3 x0=0;
4 x1=9999;
5
6 //calculation
7 I=integrate('x^2*exp(-x)','x',x0,x1);
8 A=sqrt(1/(I*(%pi/2)));
9 r=(1/4)*integrate('x^3*exp(-x)','x',x0,x1);
10
11 printf("\n A = %f*a0^-1.5\n r = %.1f*a0",A,r);
```

Scilab code Exa 2.9.3 Ex 3

```
1 // variable initialization
2 r=0:.01:1;
```

```
3 r0=0;
4 r1=1;
5
6 //calculation
7 P=4*integrate('r^2*exp(-2*r)','r',r0,r1);
8
9 printf("\n Probability = %.2f",P);
```

Scilab code Exa 2.9.4 Ex 4

```
//variable initialization
r=0:.01:9999;
theta=0:.01:%pi;
phi=0:.01:2*%pi;

//calculation
Il=integrate('r^4*exp(-r)','r',0,9999);
I2=integrate('sin(theta)*(cos(theta))^2','theta',0,%pi);
I3=integrate('1','phi',0,2*%pi);
A=sqrt(1/(2*%pi*I1*I2*I3));
printf("\n A = %f*a0^(-5/2)",A);
```

Preliminary Concepts

```
Scilab code Exa 3.1.1 Ex 1
1 //variable initialization
2 N=2
     //no. of particles
3 n1 = 2
     //occupation no. of particles
4 g1=3
     //degeneracy of particles
6 //(i) particles are distinguishable
7 state1=(factorial(N)*g1^n1)/factorial(n1);
                                            //possible
     microstates of distinguishable particles
8
9 //(ii) particles are indistinguishable bosons
10 state2=factorial(n1+g1-1)/(factorial(n1)*factorial(
     g1-1));
                                    //possible
     microstates of indistinguishable bosons
11
```

Scilab code Exa 3.1.2 Ex 2

```
1 //variable initialization
2 N=4
       //no. of particles
3 \quad A1 = [2 \quad 0 \quad 0 \quad 2];
       //possible macrostate
4 \quad A2 = [1 \quad 1 \quad 1 \quad 1];
       //possible macrostate
5 \quad A3 = [0 \quad 3 \quad 0 \quad 1];
       //possible macrostate
6 \quad A4 = [1 \quad 0 \quad 3 \quad 0];
       //possible macrostate
7 \quad A5 = [0 \quad 2 \quad 2 \quad 0];
       //possible macrostate
8 g1=1
       //degeneracy of particles
9 g2=2
```

```
//degeneracy of particles
10 g3=2
     //degeneracy of particles
11 g4=1
     //degeneracy of particles
12
13 //(i) particles are distinguishable
14 printf("\n(i)) Possible macrostates are \n ");
15 disp(A5, A4, A3, A2, A1);
16 micro1=((factorial(N)*g1^A1(1)*g2^A1(2)*g3^A1(3)*g4^
     A1(4))/(factorial(A1(1))*factorial(A1(2))*
                                               //The
     factorial(A1(3))*factorial(A1(4)));
     number of microstates
17 micro2 = ((factorial(N)*g1^A2(1)*g2^A2(2)*g3^A2(3)*g4^
     A2(4))/(factorial(A2(1))*factorial(A2(2))*
     factorial(A2(3))*factorial(A2(4))));
                                                //The
     number of microstates
18 micro3 = ((factorial(N)*g1^A3(1)*g2^A3(2)*g3^A3(3)*g4^
     A3(4))/(factorial(A3(1))*factorial(A3(2))*
                                               //The
     factorial(A3(3))*factorial(A3(4))));
     number of microstates
19 micro4=((factorial(N)*g1^A4(1)*g2^A4(2)*g3^A4(3)*g4^
     A4(4))/(factorial(A4(1))*factorial(A4(2))*
     factorial(A4(3))*factorial(A4(4))));
                                                //The
     number of microstates
20 micro5=((factorial(N)*g1^A5(1)*g2^A5(2)*g3^A5(3)*g4^
     A5(4))/(factorial(A5(1))*factorial(A5(2))*
     factorial(A5(3))*factorial(A5(4))));
                                              //The
     number of microstates
21 printf("\n most probable macrostates are\n");
22 if (micro1>=micro2 & micro1>=micro3 & micro1>=micro4
     & micro1>=micro5) then
23
       disp(A1);
24 end
25 if (micro2 >= micro1 & micro2 >= micro3 & micro2 >= micro4
```

```
& micro2>=micro5) then
26
       disp(A2);
27 end
28 if(micro3>=micro1 & micro3>=micro2 & micro3>=micro4
     & micro3>=micro5) then
29
       disp(A3);
30 end
31 if (micro4 >= micro1 & micro4 >= micro2 & micro4 >= micro3
     & micro4>=micro5) then
32
       disp(A4);
33 end
34 if (micro5 >= micro1 & micro5 >= micro2 & micro5 >= micro3
     & micro5>=micro4) then
35
       disp(A5);
36 end
37
38 //(ii) particles are indistinguishable bosons
39 printf("\n(ii) Possible macrostates are\n");
40 disp(A5, A4, A3, A2, A1);
41 micro1=(factorial(A1(1)+g1-1)*factorial(A1(2)+g2-1)*
     factorial(A1(3)+g3-1)*factorial(A1(4)+g4-1))/(
     factorial(A1(1))*factorial(A1(2))*factorial(A1(3))
     )*factorial(A1(4))*factorial(g1-1)*factorial(g2
     -1)*factorial(g3-1)*factorial(g4-1));
42 micro2=(factorial(A2(1)+g1-1)*factorial(A2(2)+g2-1)*
     factorial(A2(3)+g3-1)*factorial(A2(4)+g4-1))/(
     factorial(A2(1))*factorial(A2(2))*factorial(A2(3))
     )*factorial(A2(4))*factorial(g1-1)*factorial(g2
     -1)*factorial(g3-1)*factorial(g4-1));
43 micro3=(factorial(A3(1)+g1-1)*factorial(A3(2)+g2-1)*
     factorial(A3(3)+g3-1)*factorial(A3(4)+g4-1))/(
     factorial(A3(1))*factorial(A3(2))*factorial(A3(3))
     )*factorial(A3(4))*factorial(g1-1)*factorial(g2
     -1) *factorial(g3-1) *factorial(g4-1));
44 micro4=(factorial(A4(1)+g1-1)*factorial(A4(2)+g2-1)*
     factorial(A4(3)+g3-1)*factorial(A4(4)+g4-1))/(
     factorial(A4(1))*factorial(A4(2))*factorial(A4(3))
     )*factorial(A4(4))*factorial(g1-1)*factorial(g2
```

```
-1)*factorial(g3-1)*factorial(g4-1));
45 micro5=(factorial(A5(1)+g1-1)*factorial(A5(2)+g2-1)*
      factorial(A5(3)+g3-1)*factorial(A5(4)+g4-1))/(
      factorial(A5(1))*factorial(A5(2))*factorial(A5(3))
     )*factorial(A5(4))*factorial(g1-1)*factorial(g2
      -1)*factorial(g3-1)*factorial(g4-1));
46 printf("\nMost probable macrostate is\n ");
47 if (micro1 >= micro2 & micro1 >= micro3 & micro1 >= micro4
     & micro1>=micro5) then
       disp(A1);
48
49 end
50 if (micro2 >= micro1 & micro2 >= micro3 & micro2 >= micro4
     & micro2>=micro5) then
51
       disp(A2);
52 end
53 if(micro3>=micro1 & micro3>=micro2 & micro3>=micro4
     & micro3>=micro5) then
       disp(A3);
54
55 end
56 if (micro4 >= micro1 & micro4 >= micro2 & micro4 >= micro3
     & micro4>=micro5) then
57
       disp(A4);
58 end
59 if (micro5 >= micro1 & micro5 >= micro2 & micro5 >= micro3
      & micro5>=micro4) then
60
       disp(A5);
61 end
62
63 //(iii) Particles are indistinguishable fermions
64 printf("\n(iii) Possible macrostates are\n ");
65 \text{ disp}(A5,A2);
66 micro2=4/(factorial(A2(1))*factorial(A2(2))*
      factorial(A2(3))*factorial(A2(4))*factorial(g1-A2
      (1))*factorial(g2-A2(2))*factorial(g3-A2(3))*
      factorial(g4-A2(4)));
67 micro5=4/(factorial(A5(1))*factorial(A5(2))*
      factorial(A5(3))*factorial(A5(4))*factorial(g1-A5
      (1))*factorial(g2-A5(2))*factorial(g3-A5(3))*
```

```
factorial(g4-A5(4)));
68 printf("\nMost probable macrostate is\n ");
69 if(micro2>=micro5) then
70     disp(A2);
71 end
72 if(micro5>=micro2) then
73     disp(A5);
74 end
```

Scilab code Exa 3.1.3 Ex 3

```
1 // vairable initialization
2 N=4
      //no. of particles
3 \quad A1 = [4 \quad 0];
      //possible macrostate
4 \quad A2 = [3 \quad 1];
      //possible macrostate
5 \quad A3 = [2 \ 2];
      //possible macrostate
6 \quad A4 = [1 \ 3];
      //possible macrostate
7 \quad A5 = [0 \quad 4];
      //possible macrostate
9 //calculation
10 printf("\nPossible\ macrostates\ are\n");
11 disp(A5,A4,A3,A2,A1);
12 micro1=factorial(N)/(factorial(A1(1))*factorial(A1
```

```
(2)));
                                     //no. of microstate
      corresponding to macrostate1
13 micro2=factorial(N)/(factorial(A2(1))*factorial(A2
      (2))):
                                     //no. of microstate
       corresponding to macrostate2
14 micro3=factorial(N)/(factorial(A3(1))*factorial(A3
      (2)));
                                     //no. of microstate
       corresponding to macrostate3
15 micro4=factorial(N)/(factorial(A4(1))*factorial(A4
      (2)));
                                     //no. of microstate
       corresponding to macrostate4
16 micro5=factorial(N)/(factorial(A5(1))*factorial(A5
      (2)));
                                     //no. of microstate
       corresponding to macrostate5
17 printf("\nTotal no. of microstates are %.0f", micro1+
     micro2+micro3+micro4+micro5);
18 printf("\nMost probable macrostate is\n ");
19 if (micro1>=micro2 & micro1>=micro3 & micro1>=micro4
     & micro1>=micro5) then
20
       disp(A1);
21 end
22 if (micro2 >= micro1 & micro2 >= micro3 & micro2 >= micro4
     & micro2>=micro5) then
23
       disp(A2);
25 if (micro3 >= micro1 & micro3 >= micro2 & micro3 >= micro4
     & micro3>=micro5) then
26
       disp(A3);
27 end
28 if (micro4 >= micro1 & micro4 >= micro2 & micro4 >= micro3
     & micro4>=micro5) then
29
       disp(A4);
30 end
31 if (micro5>=micro1 & micro5>=micro2 & micro5>=micro3
     & micro5>=micro4) then
32
       disp(A5);
33 end
```

Scilab code Exa 3.1.4 Ex 4

```
1 //variable initialization
2 N=4
      //no. of particles
3 \quad A1 = [1 \quad 0 \quad 1 \quad 2];
      //possible macrostate
4 \quad A2 = [0 \quad 2 \quad 0 \quad 2];
      //possible macrostate
5 A3=[0 1 2 1];
      //possible macrostate
6 \quad A4 = [0 \quad 0 \quad 4 \quad 0];
      //possible macrostate
8 //calculation
9 printf("\nPossible macrostates are\n");
10 disp(A4,A3,A2,A1);
11 micro1=factorial(N)/(factorial(A1(1))*factorial(A1
      (2))*factorial(A1(3))*factorial(A1(4)));
                                //no. of microstate
      corresponding to macrostate1
12 micro2=factorial(N)/(factorial(A2(1))*factorial(A2
      (2))*factorial(A2(3))*factorial(A2(4)));
                                //no. of microstate
      corresponding to macrostate2
13 micro3=factorial(N)/(factorial(A3(1))*factorial(A3
      (2))*factorial(A3(3))*factorial(A3(4)));
                                //no. of microstate
      corresponding to macrostate3
```

Scilab code Exa 3.1.5 Ex 5

```
1 function[probability]=p(A)
        //function to calculate probability
 2
          probability=1;
          i = 1
 4
          for i=1:7
                probability=probability*(factorial(A(i)+2)
                    /(2*factorial(A(i))));
 6
          end
 7 endfunction
 9 //variable initialization
10 \quad A1 = [5 \quad 0 \quad 0 \quad 0 \quad 0 \quad 1];
        //possible macrostate
11 A2 = [4 \ 1 \ 0 \ 0 \ 1 \ 0];
        //possible macrostate
12 \quad A3 = [4 \quad 0 \quad 1 \quad 0 \quad 1 \quad 0 \quad 0];
        //possible macrostate
13 \quad A4 = [3 \quad 2 \quad 0 \quad 0 \quad 1 \quad 0 \quad 0];
        //possible macrostate
14 \quad A5 = [4 \quad 0 \quad 0 \quad 2 \quad 0 \quad 0];
```

```
//possible macrostate
15 \quad A6 = [3 \quad 1 \quad 1 \quad 0 \quad 0 \quad 0];
       //possible macrostate
16 \quad A7 = [2 \quad 3 \quad 0 \quad 1 \quad 0 \quad 0];
       //possible macrostate
17 A8 = [3 \ 0 \ 3 \ 0 \ 0 \ 0];
       //possible macrostate
18 \quad A9 = [2 \quad 2 \quad 2 \quad 0 \quad 0 \quad 0];
       //possible macrostate
19 A10 = [1 \ 4 \ 1 \ 0 \ 0 \ 0];
       //possible macrostate
20 \quad A11 = [0 \quad 6 \quad 0 \quad 0 \quad 0 \quad 0];
       //possible macrostate
21
22 //calculation
23 p1=p(A1);
       //Thermodynamic probability of macrostate 1
24 p2=p(A2);
       //Thermodynamic probability of macrostate 2
25 p3=p(A3);
       //Thermodynamic probability of macrostate 3
26 p4=p(A4);
       //Thermodynamic probability of macrostate 4
27 p5=p(A5);
       //Thermodynamic probability of macrostate 5
28 p6=p(A6);
```

```
//Thermodynamic probability of macrostate 6
29 p7 = p(A7);
      //Thermodynamic probability of macrostate 7
30 p8=p(A8);
      //Thermodynamic probability of macrostate 8
31 p9=p(A9);
      //Thermodynamic probability of macrostate 9
32 p10=p(A10);
      //Thermodynamic probability of macrostate 10
33 p11=p(A11);
      //Thermodynamic probability of macrostate 11
34
35 printf ("\nP1 = \%.0 f, P2 = \%.0 f, P3 = \%.0 f, P4 = \%.0 f
      , P5 = \%.0 \, f, P6 = \%.0 \, f, P7 = \%.0 \, f, P8 = \%.0 \, f, P9
      = \%.0 \,\mathrm{f}, P10 = \%.0 \,\mathrm{f}, P11 = \%.0 \,\mathrm{f}", p1, p2, p3, p4, p5, p6
      ,p7,p8,p9,p10,p11);
36 printf("\nThermodyanmic probability of the system =
      \%.0 \text{ f}", p1+p2+p3+p4+p5+p6+p7+p8+p9+p10+p11);
```

Scilab code Exa 3.1.6 Ex 6

```
1 function[micro]=p(A)

    //function to calculate no. of microstates
2    micro=1;
3    i=1
4    for i=1:5
5    micro=micro*(6/(factorial(A(i))*factorial(3-A(i))));
```

```
end
 7 endfunction
9 //variable initialization
10 A1 = [3 2 0 0 1];
      //possible macrostate
11 A2 = [3 \ 1 \ 1 \ 0];
      //possible macrostate
12 \quad A3 = [2 \quad 3 \quad 0 \quad 1 \quad 0];
      //possible macrostate
13 A4 = [3 \ 0 \ 3 \ 0 \ 0];
      //possible macrostate
14 \quad A5 = [2 \quad 2 \quad 2 \quad 0 \quad 0];
       //possible macrostate
15
16 //calculation
17 p1=p(A1);
      //no. of microstates
18 p2=p(A2);
       //no. of microstates
19 p3=p(A3);
      //no. of microstates
20 p4=p(A4);
      //no. of microstates
21 p5=p(A5);
       //no. of microstates
22
23 printf("\nPossible microstates are : \%.0 \, f, \%.0 \, f, \%.0
```

```
f\,,\,\%.0\,f\,,\,\%.0\,f\,\text{",p1,p2,p3,p4,p5);} 24 <code>printf("\nThe thermodynamic probability of the system = \%.0\,f\,\text{",p1+p2+p3+p4+p5);}</code>
```

Atomic Spectra I

```
eV)
8 n1=1;
9 n2=2;
10 R=1.097*10^7;
     //Rydberg constant (m-1)
11
12 //(i) radius of first Bohr orbit
13 r=a0/2;
     //radius of first Bohr orbit ( )
14
15 //(ii) velocity of electron in the first orbit
16 v = A * (z/n);
     // velocity of electron in the first orbit (m/s)
17
18 //(iii) orbital frequency in the first orbit
19 omega=B*(z^2/n^3);
     //orbital frequency in the first orbit (rad/s)
20
21 //(iv) kinetic and binding energy
22 KE=E0*(z^2/n^2);
     //kinetic energy of electron in the ground state
      (eV)
23 BE=KE;
      //binding energy of electron in the ground state
     (eV)
24
25 //(v) ionization potential and first excitation
      potential
26 	ext{ IP=KE};
     //ionization potential (eV)
27 EE=E0*z^2*((1/n1^2)-(1/n2^2));
```

Scilab code Exa 4.1.2 Ex 2

```
//variable initialization
z=1
//atomic no. of H atom
m=1.68*10^-27;

//mass of H atom (kg)
h=1.054*10^-34;

//Planck's constant (joule second)
R=10967800;

//Rydberg constant (m-1)
e=1.6*10^-19;

//Charge of electron (coulombs)
c=3*10^8;
```

```
//speed of light (m/s)
9 //(i) recoil velocity
10 v = (3*\%pi*h*R*z^2)/(2*m);
      //\operatorname{recoil} velocity of H atom (m/s)
11
12 //(ii) recoil kinetic energy
13 Er=(9/8)*((\%pi*h*R*z^2)^2/(m*e));
                                                            //
      recoil kinetic energy of H atom (eV)
14
15 //(iii) energy of emitted photon
16 E=(1.5*\%pi*h*c*R*z^2)/e;
      //energy of emitted photon (eV)
17
18 printf("\n(i) recoil velocity = \%.2 \text{ f m/s} \setminus n(ii)
      recoil kinetic energy = \%.1e eV\n(iii) energy of
      emitted photon = \%.2 \,\mathrm{f} eV", v, Er, E);
```

Scilab code Exa 4.1.3 Ex 3

```
1 // variable initialization
2 z=2

    //atomic no. of He atom
3 h=1.054*10^-34;

    //Planck's constant (joule second)
4 R=10967800;

    //Rydberg constant (m-1)
5 e=1.6*10^-19;
```

```
//Charge of electron (coulombs)
6 c=3*10^8;
     //speed of light (m/s)
8 //calculation
9 E=1.5*%pi*h*c*R*z^2;
     //The energy of the emitted photon (J)
10 IE=2*\%pi*h*c*R;
     //Ionization energy of H atom (J)
11 KE=(E-IE)/e;
     //Kinetic energy of the photoelectron (eV)
12
13 printf("\nKinetic energy of photoelectron = %.1 f eV"
      ,KE);
   Scilab code Exa 4.1.4 Ex 4
1 // variable initialization
2 \text{ ratio}=4
     //ratio of wavelengths
3 z1=1
     //atomic no. of hydrogen atom
5 //calculation
6 z2=sqrt(ratio*z1^2);
     //atomic no. of unknown element
7
```

```
8 printf("\natomic no. = %.0 f", z2);
Scilab code Exa 4.1.5 Ex 5
```

```
1 // variable initialization
2 lembda1=108.5*10^-9;
      //wavelength (m)
3 lembda2=30.4*10^-9;
     //wavelength (m)
4 R=1.097*10^7;
      //Rydberg constant (m-1)
5 z=2
      //atomic no. of He
6 n0 = 1
      //ground state
8 //calculation
9 n = sqrt(1/((1/n0^2) - (((1/lembda1) + (1/lembda2)))/(R*z)
      ^2))));
                                      //quantum no.
      corresponding to the excited state of He+
10
11 printf("\nn = \%.0 \, f",n);
```

```
Scilab code Exa 4.1.6 Es 6
```

```
1 //variable initialization
```

```
2 z = 2
      //atomic no. of He+ ion
3 lembda=133.7*10^-9;
      //difference b/w the first lines of the Balmer
      and Lyman series (m)
4 n1=1
5 n2 = 2
6 n3=3
8 //calculation
9 R=(1/(lembda*z^2))*((1/((1/n2^2)-(1/n3^2)))-(1/((1/n2^2)-(1/n3^2))))
      n1^2)-(1/n2^2))));
                                     //Rudberg constant (
     m-1
10
11 printf("\nR = \%.3e m-1",R);
   Scilab code Exa 4.1.7 Ex 7
1 //variable initialization
2 R=1.097*10^7;
      //Rydberg constant (m-1)
3 lembda=59.3*10^-9;
      //wavelength difference b/w first lines of Balmer
       and Lyman series (m)
5 //calculation
6 z=sqrt(88/(15*R*lembda));
      //atomic no.
8 printf("\nZ = \%.0 \, f",z);
```

Scilab code Exa 4.1.8 Ex 8

```
//variable initialization
R=1.097*10^7;

//Rydberg constant (m-1)
ratio=1836;

//ratio of mass of tritium and hydrogen

//calculation
lembda=(36*2*10^10)/(5*R*3*ratio);

separation of the first line of the Balmer series
( )

printf("\ n = %.1f ",lembda);
```

Atomic Spectra II

Scilab code Exa 4.2.4 Ex 4

```
1 //variable initialization
2 \text{ rP} = 4;
3 \text{ rD} = 5;
4 LP = 1;
5 LP = 2;
6 	 jP = [5/2, 3/2, 1/2];
7 \text{ jD} = [4, 3, 2, 1, 0];
9 // Calculation
10 SP = (rP-1)/2;
11 SD = (rD-1)/2;
12 i = 1;
13 for i=1:3
14
        JP(i) = sqrt(jP(i)*(jP(i)+1));
15 end
16 i=1;
17 for i=1:5
       JD(i) = sqrt(jD(i)*(jD(i)+1));
19 end
20
21 printf("\nAngular moments allowed for 4P: %.2f", JP)
```

```
22 printf("\nAngular moments allowed for 5D : %.2f", JD)
   Scilab code Exa 4.2.9 Ex 9
1 // variable initialization
2 1=1
3 s = 1/2
4 j = 3/2
6 //calculation
7 angle=((j*(j+1))-(l*(l+1))-(s*(s+1)))/(2*sqrt(l*s*(l+1)))
      +1)*(s+1)));
                                    //value of cos
9 printf("\n cos = \%.3 f", angle);
   Scilab code Exa 4.2.10 Ex 10
1 // variable initialization
2 e=1.6*10^-19;
      //charge of electron (C)
3 m=9.1*10^-31;
     //mass of electron (kg)
4 B = 0.1
      //external magnetic field (Wb/m^2)
6 mu = 9.27*10^-24;
      //(J/T)
```

```
8 //calculation
9 E=g*mu*B;
      //The spacing of adjacent sub-levels (J)
10 v=(e*B)/(4*\%pi*m);
      //Larmor frequency (Hz)
11
12 printf("\n The spacing of adjacent sub-levels = \%e J
      \n Larmor frequency = \%.1e Hz", E, v);
   Scilab code Exa 4.2.11 Ex 11
1 //variable initialization
2 \text{ mu} = 9.27 * 10^{-24};
      //(J/T)
3 g=2;
4 \text{ ms} = 1/2;
5 dB = 2 * 10^2;
      //gradient of magnetic field (T/m)
6 m=1.67*10^-27;
      //maas of hydrogen atom (kg)
71=0.2;
      //distance travelled by hydrogen atom (m)
8 v = 2*10^5;
      //speed of hydrogen atom (m/s)
9
10 //calculation
11 muz=g*mu*ms;
```

```
//Resolved part of magnetic moment in the
    direction of magnetic field (J/T)

12 Fz=muz*dB;

    //Force on the atom (N)

13 z=0.5*(Fz/m)*(1/v)^2;

    //Displacement of beam (m)

14 sep=2*z;

    //Total separation (m)

15

16 printf("\n Total separation = %.2e m", sep);
```

Scilab code Exa 4.2.12 Ex 12

```
//total angular momenta

12 theta1=(180/%pi)*acos(((j1*(j1+1))-(1*(1+1))-(s*(s+1)))/(2*sqrt(1*(1+1))*sqrt(s*(s+1)))); // angle b/w l and s (degree)

13 theta2=(180/%pi)*acos(((j2*(j2+1))-(1*(1+1))-(s*(s+1)))/(2*sqrt(1*(1+1))*sqrt(s*(s+1)))); // angle b/w l and s (degree)

14 printf("\n L = %f*h\n S = %f*h\n J = %f*h, %f*h\n l = %.0f degree\n 2 = %.0f degree",L,S,J1,J2, theta1,theta2);
```

Scilab code Exa 4.2.13 Ex 13

```
//variable initialization
B=0.5

//magnetic field (T)
s=1/2;
g=2;
//calculation
S=sqrt(s*(s+1));

//Magnitude of spin vector
theta1=(180/%pi)*acos(0.5/S);

//Orientation of spin vector (degree)
theta2=(180/%pi)*acos(-0.5/S);

//Orientation of spin vector (degree)
E=2*g*B;

//Separation of the energy levels (in terms of)
```

```
11
12 printf("\n
                = \%.1 f degree and \%.1 f degree\n
             ",theta1,theta2,E);
     \%.0 f*
   Scilab code Exa 4.2.15 Ex 15
1 // variable initialization
2 zH=1
      //atomic no. of H
3 \text{ zHe}=2
      //atomic no. of He
4 deltaHe=5.84
      //doublet splitting of the first excited state of
       He (cm-1)
6 //calculation
7 deltaH=deltaHe*(zH/zHe)^4;
      //doublet splitting for hydrogen atom (cm-1)
9 printf("\n doublet splitting for H atom = \%.3 f cm-1"
      ,deltaH);
   Scilab code Exa 4.2.16 Ex 16
1 // variable initialization
2 z = 1
      //atomic no. of hydrogen atom
3 n=2
```

```
4 l=1
5
6 //calculation
7 delta=(5.84*z^4)/(n^3*l*(l+1));

    //spin-orbit interaction splitting (cm-1)
8
9 printf("\n spin-orbit interaction splitting = %.3 f cm-1", delta);
```

Atomic Spectra III

Scilab code Exa 4.3.4 Ex 4

```
Scilab code Exa 4.3.5 Ex 5
1 // variable initialization
2 R=109737
     //(cm-1)
3 n=1.805
     //effective quantum number for the ground state
     of rubidium
4
5 //calculation
6 T=R/(8065*n^2);
     //ionization potential of rubidium (eV)
8 printf("\nThe ionization potential of rubidium = \%.3
     f \ eV", T);
  Scilab code Exa 4.3.6 Ex 6
1 // variable initialization
2 \text{ ratio} = 2.5
     //ratio of ionization potential of hydrogen and
     sodium
3 n=3
5 //calculation
6 z=sqrt(n^2/ratio);
     //effective atomic number of sodium
```

8 printf("\nEffective atomic number of sodium = $\%.2 \,\mathrm{f}$ ",

z);

```
Scilab code Exa 4.3.7 Ex 7
1 //variable initialization
2 hc = 12400
     //value of product of plank's constant and speed
      of light (eV
3 E1=3.18
     //separation of 4s and 3s level (eV)
4 lembda=5890
     //wavelength of the first member of principal
      series of sodium ( )
6 //calculation
7 E2=hc/lembda;
     //separation of 3s and 3p levels (eV)
8 deltaE=E1-E2;
     //separation of 4s and 3p level (eV)
9 lembda1=hc/deltaE;
      //wavelength of the first member of sharp series
10
11 printf("\ n = \%.0 \, f ",lembda1);
```

Scilab code Exa 4.3.8 Ex 8

```
1 // variable initialization
2 lembda1 = 5890*10^-10;
     //wavelength of doublet ( )
3 \ lembda2 = 5896 * 10^-10;
     //wavelength of doublet ( )
4 h=6.63*10^{-34};
     //Plank's constant (Js)
5 c=3*10^8;
     //speed of light (m/s)
6 e=1.6*10^-19;
     //Charge of electron (coulombs)
8 //calculation
9 deltaV=(lembda2-lembda1)/(lembda1*lembda2);
                                            //wave no. (m
      -1)
10 deltaE=(h*c*deltaV)/e;
     //separation of energy levels (eV)
11
12 printf("\n E = \%.2e eV", deltaE);
   Scilab code Exa 4.3.9 Ex 9
1 // variable initialization
2 deltaT=2.1*10^-3;
     //(eV)
3 lembda=5893*10^-8;
```

```
//( )
5 //calculation
6 deltaV=deltaT*8065;
     //(cm-1)
7 deltalembda=deltaV*lembda^2;
     //(cm)
9 printf("\ n = \%.2e cm", deltalembda);
  Scilab code Exa 4.3.10 Ex 10
1 //variable initialization
2 E1=16960
     //mean position of the level (cm-1)
3 E2=24490
     //convergence limit of sharp series (cm-1)
5 //calculation
6 I = (E1+E2)/8065;
     //ionization energy of sodium atom (eV)
8 printf("\nI = \%.4 f eV",I);
  Scilab code Exa 4.3.11 Ex 11
1 // variable initialization
```

```
2 E1=41450
     //principal series for sodium atom (cm-1)
3 E2=24477
     //sharp series for sodium atom (cm-1)
5 //calculation
6 I = (E1+E2)/8065;
     //ionization energy of sodium atom (eV)
8 printf("\nI = \%.4 f eV",I);
  Scilab code Exa 4.3.12 Ex 12
1 //variable initialization
2 E1=14904
     //\text{mean position of the level } (\text{cm}-1)
3 E2=28583
     //convergence limit of sharp series (cm-1)
5 //calculation
6 I = (E1 + E2) / 8065;
     //ionization energy of Li atom (eV)
8 printf("\nI = \%.2 f eV",I);
```

Scilab code Exa 4.3.13 Ex 13

```
1 // variable initialization
2 R=109734
     //(cm-1)
3 T = 24477
     //(cm-1)
4 \text{ Zeff=1}
5 n=3
7 //calculation
8 delta=n-(Zeff*sqrt(R/T));
      //quantum defect for 3p configuration of sodium
10 printf("\ n = \%.3 \, f", delta);
   Scilab code Exa 4.3.14 Ex 14
1 // variable initialization
2 z1=1
      //atomic no.
3 z2=2
      //atomic no.
4 deltaT2=5.84
      //doublet splitting of the first excited state
      for z=2 (cm-1)
6 //calculation
7 deltaT1=deltaT2*(z1/z2)^4;
      //separation in hydrogen atom (cm-1)
```

```
8 9 printf("\n separation in hydrogen atom = \%.3 \, \mathrm{f} \, \mathrm{cm}{-1}", deltaT1);
```

Magneto Optic and Electro Optic Phenomena

```
Scilab code Exa 4.4.1 Ex 1

// variable initialization
e=1.6*10^-19;

//charge of electron (Coulomb)

B=0.5

//magnetic field (Tesla)

lembda=6438*10^-10;

//wavelength of the line (m)

m=9.1*10^-31;

//mass of electron (kg)

c=3*10^8;

//speed of light (m/s)

//speed of light (m/s)

//calculation
dlembda=(e*B*lembda^2*10^10)/(4*%pi*m*c);
```

```
//normal
      Zeeman splitting ( )
10
11 printf("\nZeeman shift = \%.3 \,\mathrm{f} ", dlembda);
   Scilab code Exa 4.4.2 Ex 2
1 // variable initialization
2 e=1.6*10^-19;
      //charge of electron (Coulomb)
3 B=1
      //magnetic field (Tesla)
4 lembda=612*10^-9;
     //wavelength of the line (m)
5 m=9.1*10^-31;
      //mass of electron (kg)
6 c=3*10^8;
      //speed of light (m/s)
8 //calculation
9 dlembda1 = (e*B*lembda^2*10^10)/(4*\%pi*m*c);
                                              //normal
      Zeeman splitting (
10 dlembda2=2*dlembda1;
      //Separation of outer lines ( )
11
12 printf("\nSeparation of outer lines = \%.2 \,\mathrm{f}",
      dlembda2);
```

```
Scilab code Exa 4.4.3 Ex 3
1 // variable initialization
2 \text{ mu} = 9.27 * 10^{-24};
      //(J/T)
3 B=1*10^-1;
      //external magnetic field (T)
4 h=1.054*10^-34;
      //Plank's constant (Js)
5 J=3/2;
6 L=1;
7 S=1/2;
9 //calculation
10 g=1+(((J*(J+1))+(S*(S+1))-(L*(L+1)))/(2*J*(J+1)));
                                      //Lande g-factor
11 omega=(g*mu*B)/h;
      //angular velocity of precession (rad/s)
12
13 printf("\ n = \%.1e \text{ rad/sec}", omega);
   Scilab code Exa 4.4.4 Ex 4
1 //(i)
2 printf("\n(i) Energy level does not split");
```

4 //(ii) 5 J=5/2;

```
6 sub=2*J+1;
7 printf("\n(ii) number of sub-shells = %.0f", sub);
8
9 //(iii)
10 printf("\n(iii) Energy level does not split");
```

Scilab code Exa 4.4.5 Ex 5

```
1 //variable initialization
2 S1=0
3 L1=2
4 J1=2
5 g1=1
6 S2 = 1
7 L2 = 3
8 J2 = 4
9 g2 = 5/4
10 B = 0.25
      //magnetic field (T)
11 mu=5.79*10^-5;
      // \text{mass} (eV/T)
12
13 //(i)
14 E1 = 4 * g1 * mu * B;
      //total splitting (eV)
15
16 //(ii)
17 E2=8*g2*mu*B;
      //total splitting (eV)
18
19 printf("\n(i) total splitting = %.2e eV\n(ii) total
```

Scilab code Exa 4.4.7 Ex 7 1 // variable initialization $2 \text{ mu} = 9.27 * 10^-24;$ //(J/T)3 B=0.45;//magnetic field (b/m^2) 4 $h=1.054*10^-34$; //Plank's constant (Js) $5 k = [5/3 \ 1 \ 1/3 \ -1/3 \ -1 \ -5/3];$ //value of g'Mj'-gMj 7 //calculation 8 c = (mu*B)/h;//constant (rad/s)9 deltaomega1=c*k(1); //displacement of Zeeman component (rad/s) 10 deltaomega2=c*k(2); //displacement of Zeeman component (rad/s) 11 deltaomega3=c*k(3); //displacement of Zeeman component (rad/s) 12 deltaomega4=c*k(4); //displacement of Zeeman component (rad/s) 13 deltaomega5=c*k(5);

```
//displacement of Zeeman component (rad/s)

14 deltaomega6=c*k(6);

    //displacement of Zeeman component (rad/s)

15

16 printf("\ndisplacement of Zeeman component = %.2e, %.2e, %.2e, %.2e, %.2e rad/s", deltaomega1, deltaomega2, deltaomega3, deltaomega4, deltaomega5, deltaomega6);
```

Scilab code Exa 4.4.8 Ex 8

```
//variable initialization
m=9.1*10^-31;

//mass of electron (Kg)
h=1.054*10^-34;

//Plank's constant (Js)
B=1.2

//magnetic field (mu*b/m^2)
sgs=2

//for a pure spin system
J=0.5;

//for a pure spin system
mub=h/(2*m);

//(eV/T)
deltaE=2*gs*mub*B*J;
```

```
//energy difference b/w electrons (eV)
11
12 printf("\n E = \%.2e \text{ eV}", deltaE);
   Scilab code Exa 4.4.9 Ex 9
1 // variable initialization
2 m=9.1*10^-31;
     //mass of electron (Kg)
3 h=1.054*10^-34;
     //Plank's constant (Js)
4 B=5
     //magnetic field (T)
5 lembda=1210
     //wavelength of spectral line ( )
6 M = [1 0 -1 1 0 -1];
     //value of Ml+2*Ms
7 ch=12400
     //product of speed of light and Plank's constant
     (eV*)
9 //calculation
10 dE=(h/(2*m))*B*M;
     //value of dE(upper)-dE(lower) (eV)
11 dlembda=(lembda^2/ch)*dE;
     //wavelengths of the spectral lines in the
```

```
pattern ( )  
12  
13  printf("\nwavelengths of the line = \%.0\,\mathrm{f}+\%.3\,\mathrm{f}, \%.0\,\mathrm{f}+ \%.0\,\mathrm{f}, \%.0\,\mathrm{f}\%.3\,\mathrm{f} ",lembda,dlembda(1),lembda, dlembda(2),lembda,dlembda(3));
```

X Rays and X Ray Spectra

```
Scilab code Exa 4.5.1 Ex 1
1 // variable initialization
2 ch=12400
     //product of speed of light and Plank's constant
     (eV*
3 lembda1 = 0.024;
     //Compton wavelength of X-ray ( )
4 lembda2=1
     //wavelength of X-ray ( )
6 //(i)
7 x1=ch/lembda1;
     //minimum voltage across X-ray tube (V)
8
9 //(ii)
10 x2=ch/(lembda2*10^3);
     //minimum voltage across X-ray tube (kV)
```

```
11
12 //(iii)
13 \times 3 = 1.02
      //minimum energy of X-ray photon (M*eV)
14
15 printf("\n(i) voltage = \%.2e V\n(ii) voltage = \%.1 f
      KV \setminus n(iii) energy = \%.2 f MeV", x1, x2, x3);
   Scilab code Exa 4.5.2 Ex 2
1 // variable initialization
2 n=3/2;
3 \text{ dlembda=}26*10^-2;
      //shifting in short wave limit of X-ray spectrum
4 ch=12400
      //product of speed of light and Plank's constant
      (eV*)
5 e=1.6*10^-19;
      //charge of electron (Coulomb)
7 //solution
8 V=((n-1)/n)*(ch/(dlembda*10^3));
                                                        //
      initial voltage applied to the tube (KV)
10 printf("\nInitial voltage = %.1 f KV", V);
```

Scilab code Exa 4.5.3 Ex 3

```
1 // variable initialization
2 R=10972900
     //(m-1)
3 lembda=1.54*10^-10;
     //wavelength of K line (m)
4
5 //calculation
6 z=1+sqrt(4/(3*lembda*R));
     //atomic number of the target element
8 printf("\nZ = \%.0 f",z);
  Scilab code Exa 4.5.4 Ex 4
1 //variable initialization
2 z1 = 29
     //atomic no. of Copper
3 z2 = 26
     //atomic no. of Iron
4 lembda1=193
     // wavelength of K line in Iron (pm)
6 //calculation
7 lembda=((z2-1)/(z1-1))^2*lembda1;
                                                      //
     wavelength of K line in Copper (pm)
8
9 printf("\n = \%.0 f pm",lembda);
```

```
Scilab code Exa 4.5.5 Ex 5
1 // variable initialization
2 z1 = 13
     //atomic no. of Al
3 z2 = 27
     //atomic no. of Co
4 R=1.097*10^7;
     //(m-1)
6 //calculation
7 lembda1=(4*10^12)/(3*R*(z1-1)^2);
      wavelength of K line in Al (pm)
8 lembda2=(4*10^12)/(3*R*(z2-1)^2);
      wavelength of k line in Co (pm)
10 printf("\n wavelength of Al = \%.0 f pm\n wavelength
      of Co = \%.0 f pm", lembda1, lembda2);
   Scilab code Exa 4.5.6 Ex 6
1 // variable initialization
2 lembda1=250*10^-12;
     //wavelength of K-alpha line (m)
3 \ lembda2 = 179 * 10^-12;
```

```
//wavelength of K-alpha line (m)
4 R=10972900
      //(m-1)
5
6 //calculation
7 z1=1+sqrt(4/(3*lembda1*R));
      //atomic number
8 z2=1+sqrt(4/(3*lembda2*R));
      //atomic number
9 printf("\nThe required elements are: Z =");
10 for i=z1+1:1:z2-1
       printf(" \%.0 \, f",i);
11
12 end
   Scilab code Exa 4.5.7 Ex 7
1 // variable initialization
2 \text{ ch} = 12400
      //product of speed of light and Plank's constant
      (eV*)
3 \text{ Rch} = 13.6
      //product of speed of light, Plank's constant and
      R (eV)
4 z = 23
      //atomic no. of vanadium
5 lembda=24
      //wavelength of L absorption edge ( )
6
```

```
7 //calculation
8 El=ch/(lembda*10^3);
      //binding energy of L electron (KeV)
9 Ek = ((3/(4*10^3))*Rch*(z-1)^2)+E1;
                                                        //
      binding energy of K electron (KeV)
10
11 printf("\nBinding energy of K-electron = \%.2 \, \text{f KeV}",
      Ek);
   Scilab code Exa 4.5.8 Ex 8
1 // variable initialization
2 \text{ ch} = 12.4
      //product of speed of light and Plank's constant
      (\text{KeV}*
3 lembda1 = 0.178
      //wavelength of K-alpha line ( )
4 lembda2 = 0.210
      //wavelength of K line ( )
6 //calculation
7 Ek=ch/lembda1;
      //binding energy of K electron (KeV)
8 El=Ek-(ch/lembda2);
      //binding energy of K-alpha electron (KeV)
9 lembda=ch/El;
      //wavelength of L absorption edge ( )
```

```
10
11 printf("\nWavelength of L absorption edge = \%.2 \,\mathrm{f}
      ,lembda);
   Scilab code Exa 4.5.9 Ex 9
1 // variable initialization
2 \text{ ch} = 12.4
      //product of speed of light and Plank's constant
      (KeV*)
3 lembdak=0.18
      //wavelength of K absorption edge ( )
4 lembda=0.1
      //wavelength of incident photon ( )
6 //calculation
7 Ek=ch/lembdak;
      //binding energy of K electron (KeV)
8 E=ch/lembda;
      //energy of incident photon (KeV)
9 K=E-Ek;
      //maximum kinetic energy of ejected electron (KeV
10
11 printf("\n KE = %.2 f KeV",K);
```

Scilab code Exa 4.5.10 Ex 10

```
1 // variable initialization
2 ch = 12.4
     //product of speed of light and Plank's constant
      (KeV*
3 Rch=13.6/10<sup>3</sup>;
     //product of speed of light, Plank's constant and
      R (KeV)
4 lembdak=1.74
     //K band absorption edge wavelength of iron ( )
5 z=30;
     //atomic no. of zinc
7 //calculation
8 Ek=ch/lembdak;
     //binding energy of K electron in iron (KeV)
9 E=(3/4)*Rch*(z-1)^2;
     //energy of photon of K-alpha radiation (KeV)
10 K=E-Ek;
     //kinetic energy of the photoelectrons liberated
     from iron (KeV)
11
12 printf("\n KE = \%.3 f KeV", K);
```

Chapter 27

Raman Spectra

Scilab code Exa 5.5.1 Ex 1

```
1 //function for calculating the wave number
2 function[wave]=F(j)
       wave=B*j*(j+1);
4 endfunction
6 //variable initialization
7 r=1.21*10^-10;
     //internuclear distance (meter)
8 m=2.7*10^-26;
     //mass of oxygen atom (kg)
9 h=6.626*10^{-34};
     //Plank's constant (joule second)
10 c=3*10^8;
     //speed of light (meter/second)
11
12 //(a) moment of inertia
13 mu=m/2;
```

```
14 I=mu*r^2;
      //moment of inertia (kg m<sup>2</sup>)
15
16 //(b) rotational constant
17 B=h/(8*\%pi^2*I*c);
      // rotational constant (m-1)
18
19 //(c) wave number
20 waveno=F(1)-F(0);
      //wave no. of the line corresponding to the
      transition J=0 to J=1 (m-1)
21
22 printf("\n(a) I = \%.3 e kg m<sup>2</sup>\n(b) B = \%.1 f m-1\n(c)
       wave number = \%.0 \text{ f m-1}", I, B, waveno);
   Scilab code Exa 5.5.2 Ex 2
1 //function for calculating the energy level
2 function[energy]=F(j)
       energy=a*j*(j+1);
4 endfunction
6 //variable initialization
7 m=1.6738*10^-27;
      //mass of hydrogen atom (kg)
8 r = 0.74 * 10^{-10};
      //intermolecular distance of hydrogen molecule (
      meter)
```

//reduced mass (kg)

```
9 h=1.054*10^-34;
      //Planck's constant (joule second)
10 e=1.6*10^-19;
      //Charge of electron (coulombs)
11
12 //calculation of rotational energy levels
13 mu=m/2;
      //reduced mass of hydrogen atom (kg)
14 I=mu*r^2;
      //moment of inertia of molecule (kg meter^2)
15 a=h^2/(2*I*e);
      //constant (eV)
16 E0 = F(0);
      //energy of level 0 (eV)
17 E1=F(1);
      //energy of level 1 (eV)
18 E2=F(2);
      //energy of level 2 (eV)
19 E3=F(3);
      //energy of level 3 (eV)
20
21 printf("\nE0 = \%.0 \ f \nE1 = \%.2 \ e \ eV \nE2 = \%.2 \ e \ eV \nE3
      = \%.2 \,\mathrm{e} \,\mathrm{eV}", E0, E1, E2, E3);
```

Scilab code Exa 5.5.3 Ex 3

```
1 // variable initialization
2 u=1.68*10^-27;
     //mass of hydrogen atom (kg)
3 m1 = 16;
     //mass of oxygen atom in terms u
4 m2=1;
     //mass of hydrogen atom in terms of u
5 I=1.48*10^-47;
     //moment of inertia of OH-radical (kg m^2)
6 h_bar=1.054*10^-34;
     //Planck's constant (joule second)
7 j=5;
     //energy level of OH-radical
8 c=3*10^8;
     //speed of light (meter/second)
9 h=6.626*10^{-34};
     //Plank's constant (joule second)
10
11 //(a) internuclear distance
12 mu = ((m1*m2)/(m1+m2))*u;
     //reduced mass of the molecule (kg)
13 r=(sqrt(I/mu))*10^10;
     //internuclear distance of molecule ( )
14
15 //(b) angular momentum
16 P=h_bar*sqrt(j*(j+1));
     //angular momentum of molecule (joule second)
```

```
17
18 //(c) angular velocity
19 omega=P/I;
      //angular velocity of molecule (radian/second)
20
21 //(d) wave number
22 B=h/(8*\%pi^2*I*c);
      // rotational constant (m-1)
23 no=2*B*(j+1);
      //wave no. of line corresponding to transition j
      =5 to j=6 (m-1)
24
25 //(e) energy absorbed
26 E=c*h*no;
      //energy absorbed in the transition j=6 to j=5 (
      joule)
27
28 printf("\n(a) r = %.3 f \n(b) J = %.2 e joule second
              = \%.2e \text{ radian/second/n(d)} wave number =
     \%.2e \text{ m-1/n(e)} \text{ E} = \%.1e \text{ joule",r,P,omega,no,E)};
   Scilab code Exa 5.5.4 Ex 4
1 // variable initialization
2 h=6.63*10^{-34};
      //Plank's constant (joule second)
3 v=1.153*10^11;
      //Frequency of absorption line (Hz)
4 mu = 11.38 * 10^-27;
```

```
//Recuced mass of the molecule (kg)
6 // Calculation of the internuclear distance
7 I=h/(4*\%pi^2*v);
      //moment of inertia of CO molecule (kg m<sup>2</sup>)
8 r=sqrt(I/mu)*10^10;
      //Internuclear distance ( )
10 printf("\n Internuclear distance = \%.2 f ",r);
   Scilab code Exa 5.5.5 Ex 5
1 // variable initialization
2 \text{ mu} = 1.62 * 10^{-27};
      //Reduced mass of HCL (kg)
3 c=3*10^8;
      //Velocity of light (m/s)
4 h=6.62*10^{-34};
      //Plank's constant (joule second)
5 v1_P = 2906.3
      //Wave no. of P branch (cm-1)
6 v2_P = 2927.5
      //Wave no. of P branch (cm-1)
7 v3_P = 2948.7
      //Wave no. of P branch (cm-1)
8 v4_P = 2969.9
```

```
//Wave no. of P branch (cm-1)
9 v1_R=3012.2
      //Wave no. of R branch (cm-1)
10 \text{ v2}_R = 3033.4
      //Wave no. of R branch (cm-1)
11 v3_R=3054.6
      //Wave no. of R branch (cm-1)
12 \quad v4_R = 3078.8
      //Wave no. of R branch (cm-1)
13
14 //(i) Equilibrium internuclear distance
15 \text{ delta_v=v2_P-v1_P};
      //Separation of successive line of P and R branch
       (cm-1)
16 B=delta_v/2;
      // rotational constant (cm-1)
17 I=h/(8*\%pi^2*B*10^2*c);
      //Moment of inertia (kg m<sup>2</sup>)
18 r=sqrt(I/mu)*10^10;
      //Equilibrium internuclear distance ( )
19
20 //(ii) Force constant
21 \quad v0 = (v4_P + v1_R)/2;
      //Equlibrium frequency (cm-1)
22 k=4*\%pi^2*mu*c^2*v0^2*10^4;
      //Force constant of HCl (N/m)
23
```

```
24 printf("\n(i) Equilibrium internuclear distance = %
          \n(ii) Force constant = \%.0 \, f \, N/m, r,k);
25
26 // Note: the answer of (ii) part is wrong in the book
   Scilab code Exa 5.5.6 Ex 6
1 // variable initialization
2 \text{ mu} = 8.37 * 10^-28;
      //Reducec mass of hydrogen molecule (kg)
3 h=6.58*10^-16;
      //Plank's constant (eV s)
4 E0 = 0.273
      //Ground state vibrational energy of hydrogen
      molecule (eV)
5
6 //calculation of force constant of the molecule
7 k=mu*((2*E0)/h)^2;
      //force constant of hydrogen molecule (N/m)
9 printf("\n Force constant = \%.0 \, \text{f N/m}",k);
   Scilab code Exa 5.5.7 Ex 7
1 //variable initialization
2 m1=1;
      //molar mass of H atom (amu)
```

```
3 m2 = 35;
     //molar mass of Cl atom (amu)
4 u=1.68*10^-27;
     //atomic mass unit (kg)
5 v = 2885.9 * 100;
     // wave no. of line (m-1)
6 c=3*10^8;
     //Velocity of light (m/s)
8 //calculation of force constant
9 mu = ((m1*m2)/(m1+m2))*u;
      //reduced mass of HCl molecule (kg)
10 k=4*(\%pi*c*v)^2*mu;
      //force constant of HCl molecule (N/m)
11
12 printf("\n force constant = \%.2 \, f \, N/m",k);
   Scilab code Exa 5.5.8 Ex 8
1 //function for calculating the various vibrational
      energy levels of CO molecule
2 function[energy]=F(V)
       energy=((V+.5)*h*v)/e;
4 endfunction
6 //function for converting eV to cm-1
7 function[energy]=G(V)
       energy=((V+.5)*h*v*8065)/e;
9 endfunction
```

```
10
11 // variable initialization
12 \text{ m} 1 = 12;
      //molar mass of C atom (amu)
13 \text{ m} 2 = 16;
      //molar mass of O atom (amu)
14 u=1.68*10^-27;
      //atomic mass unit (kg)
15 k = 1870
      //force constant of CO molecule (N/m)
16 h=6.6*10^-34;
      //Plank's constant (joule second)
17 e=1.602*10^-19;
      //charge of electron (Coulomb)
18
19 //calculation of energy levels
20 mu = ((m1*m2)/(m1+m2))*u;
      //reduced mass of CO molecule (kg)
21 v=(1/(2*\%pi))*sqrt(k/mu);
      //frequency of vibration of CO molecule (Hz)
22 \text{ e1=F(0)};
      //energy of 1st level of CO molecule (eV)
23 \text{ E1=G(0)};
      //energy of 1st level of CO molecule (cm-1)
24 \text{ e}2=F(1);
      //energy of 2nd level of CO molecule (eV)
25 \quad E2=G(1);
```

```
//energy of 2nd level of CO molecule (cm-1)
26 \text{ e3=F(2)};
     //energy of 3rd level of CO molecule (eV)
27 E3=G(2);
     //energy of 3rd level of CO molecule (cm-1)
28
  printf("\nE = \%.3 \text{ f eV}, \%.3 \text{ f eV}, \%.3 \text{ f eV}
      \dots \dots  n = \%.1 f cm-1, \%.1 f
     E3);
  Scilab code Exa 5.5.9 Ex 9
1 // variable initialization
2 \text{ mu} = 1.61 * 10^{-27};
     //reduced mass of HCl molecule (kg)
3 c=3*10^8;
     //speed of light (m/s)
4 lembda=3.465*10^-6;
     //wavelength of infrared radiation (m)
6 //calculation of force constant
7 v=c/lembda;
     //frequency of radiation (s-1)
8 k=4*(\%pi*v)^2*mu;
     //force constant of HCl molecule (N/m)
9
```

```
Scilab code Exa 5.5.10 Ex 10
1 // variable initialization
2 h=6.6*10^-34;
      //Plank's constant (joule second)
3 \text{ mu} = 1.62 * 10^{-27};
     //reduced mass of HCl molecule (kg)
4 c=3*10^8;
     //speed of light (m/s)
5 v=2.886*10^5;
      //wave no. of absorption line in infrared
      spectrum (m-1)
6
7 //calculation of amplitude of vibration
8 k=4*(\%pi*c*v)^2*mu;
     //force constant of HCl molecule (N/m)
9 amp=sqrt((h*c*v)/k)*10^10;
     //amplitude of vibration in the ground state ( )
10
                                              ",amp);
11 printf("\namplitude of vibration = \%.2 f
   Scilab code Exa 5.5.11 Ex 11
1 // variable initialization
```

```
2 v1=214330
      //fundamental band for CO molecule (m-1)
3 v2 = 425970
      // first overtone for CO molecule (m-1)
4 A = [1 -2; 2 -6];
      //coefficient matrix
5 b = [v1; v2];
      //right hand side matrix
7 //calculation
8 x = inv(A)*b;
      //values of omega and x*omega (m-1)
10 printf("\ n e = \%.0 \text{ f m-1} \times \text{e} = \%.0 \text{ f m-1}", x(1), x
      (2));
   Scilab code Exa 5.5.12 Ex 12
1 //variable initialization
2 v1=288600
      //intense absorption (m-1)
3 v2 = 566800
      //intense absorption (m-1)
4 v3=834700
      //intense absorption (m-1)
5 \quad A = [1 \quad -2; 2 \quad -6];
```

```
//coefficient matrix
6 b=[v1;v2];
      //right hand side matrix
7 mu=1.61*10^-27;
      //reduced mass (kg)
8 c=3*10^8;
      //speed of light (m/s)
9
10 //calculation
11 x = inv(A) *b;
      //values of omega and x*omega (m-1)
12 k=4*(\%pi*c*x(1))^2*mu;
      //force constant (N/m)
13
14 printf("\ n e = \%.0 \text{ f m-1} \times \text{e} = \%.0 \text{ f m-1} \times \text{force}
      constant = \%.1 \, f \, N/m, x(1), x(2), k);
   Scilab code Exa 5.5.13 Ex 13
1 // variable initialization
2 v1=8.657*10^13;
      //frequency of rotation absorption spectrum (Hz)
3 v2=8.483*10^13;
      //frequency of rotation absorption spectrum (Hz)
4 h=6.6*10^-34;
      //Plank's constant (joule second)
5 mu=1.544*10^-27;
```

```
//Recuced mass of CH molecule (kg)
7 //(i) equilibrium separation
8 I=h/(2*\%pi^2*(v1-v2));
      //Moment of inertia (kg m<sup>2</sup>)
9 r=sqrt(I/mu);
      //equilibrium internuclear distance (m)
10
11 //(ii) force constant of molecule
12 v0 = (v1 + v2)/2;
      //Central frequency (Hz)
13 k=4*mu*(%pi*v0)^2;
      //Force constant of CH molecule (N/m)
14
15 printf("\n (i) equilibrium separation = \%.2e meter\n
       (ii) force constant = \%.0 \, \text{f N/m}, r, k);
   Scilab code Exa 5.5.14 Ex 14
1 // variable initialization
2 k = 448
      //force constant of CH molecule (N/m)
3 \text{ mu} = 4.002 * 10^-27;
      //reduced mass of CH molecule (kg)
4 r=0.112*10^-9;
      //internuclear distance (m)
5 h=6.6*10^-34;
```

```
//Plank's constant (joule second)
7 // Calculation of peak frequencies
8 v0=(1/(2*\%pi))*sqrt(k/mu);
      // central frequency (s-1)
9 I=mu*r^2;
      //moment of inertia of molecule (kg m<sup>2</sup>)
10 x=h/(4*\%pi^2*I);
      //additional frequency (s-1)
11 v1 = v0 + x;
      //peak frequency (Hz)
12 v2 = v0 - x;
      //peak frequency (Hz)
13
14 printf("\n Peak frequencies = \%.3e Hz, \%.3e Hz", v1,
      v2);
   Scilab code Exa 5.5.15 Ex 15
1 //variable initialization
2 v1 = 2174.07
      // peak wave number (cm-1)
3 v2 = 2166.35
      // peak wave number (cm-1)
4 h=6.6*10^-34;
      //Plank's constant (joule second)
```

```
5 c=3*10^8;
      //Speed of light (m/s)
6 mu=1.145*10^-26;
      //Reduced mass of CO molecule (kg)
8 //(a) central frequency
9 B=(v1-v2)/4;
      //Rotational constant (cm-1)
10 v0 = (v1 + v2)/2;
      //Central frequency (cm-1)
11
12 //(b) internuclear distance
13 I=h/(8*\%pi^2*B*100*c);
      //moment of inertia of molecule (kg m^2)
14 r=sqrt(I/mu)*10^10;
      //equilibrium internuclear distance ( )
15
16 //(c) force constant
17 k=4*mu*(\%pi*c*v0*100)^2;
      //force constant (N/m)
18
19 printf("\n(a) central frequency = \%.2 \text{ f cm}-1 \setminus n(b)
      internuclear distance = \%.2 \,\mathrm{f} \n(c) force
      constant = \%.0 f N/m", v0, r,k);
```

Scilab code Exa 5.5.16 Ex 16

1 // variable initialization

```
2 \text{ mu} = 3.142 * 10^{-27};
      //reduced mass of the molecule (kg)
3 r=1.288*10^-10;
      //internuclear distance (m)
4 h=6.6*10^-34;
      //Plank's constant (joule second)
5 c=3*10^8;
      //Speed of light (m/s)
6 v0 = 201100
      //central frequency (m-1)
8 // Calculation
9 I=mu*r^2;
      //moment of inertia of molecule (kg m^2)
10 B=h/(8*\%pi^2*I*c);
      //Rotational constant (m-1)
11 vR0 = v0 + (2*B);
      //wave no. of 1st line of R-branch (m-1)
12 vR1 = v0 + (4*B);
      //wave no. of 2nd line of R-branch (m-1)
13 vP1=v0-(2*B);
      //wave no. of 1st line of P-branch (m-1)
14 vP2=v0-(4*B);
      //wave no. of 2nd line of P-branch (m-1)
15
16 printf("\n V_R(0) = \%.0 f m-1\n V_R(1) = \%.0 f m-1\n
      V_{P}(1) = \%.0 \text{ f m-1/n } V_{P}(2) = \%.0 \text{ f m-1}, vR0, vR1,
```

Scilab code Exa 5.5.17 Ex 17

```
1 // variable initialization
2 \text{ mu} = 1.62 * 10^-27;
      //reduced mass of HCl molecule (kg)
3 r=1.293*10^-10;
      //internuclear distance (m)
4 h=6.6*10^-34;
      //Plank's constant (joule second)
5 c=3*10^8;
      //Speed of light (m/s)
7 // Calculation of separation between lines R(0) and P
      (1) of the fundamental band of HCl 35
8 I=mu*r^2;
      //moment of inertia of molecule (kg m^2)
9 B=h/(8*\%pi^2*I*c);
      //Rotational constant (m-1)
10 sep = 4 * B;
      // separation b/w lines R(0) and P(1) (m-1)
11
12 printf("\ n = \%.0 \text{ f m-1}", sep);
```

Scilab code Exa 5.5.18 Ex 18

```
1 //variable initialization
2 a=214.6*100;
     //(m-1)
3 b=0.6*100;
     //(m-1)
4 h=6.6*10^-34;
     //Plank's constant (joule second)
5 c=3*10^8;
     //Speed of light (m/s)
6 no=1/(\%e);
      //number of molecules in state with respect to
     ground state
7 k=1.38*10^-23;
     //Boltzmann constant (J K-1)
9 // Calculation
10 deltaE=h*c*(a-2*b);
     //difference in the energies of state 0 and state
      1 (J)
11 T1=deltaE/k;
     //temperature at which number of molecules in
      state 1 is 1/e times of state 0 (K)
12 T2=deltaE/(k*log(10));
     //temperature at which number of molecules in
      state 1 is 10% of state 0 (K)
13
14 printf("n(i) T = \%.0 f K \setminus n(ii) T = \%.0 f K", T1, T2);
```

```
Scilab code Exa 5.5.19 Ex 19
1 // variable initialization
2 \text{ vexc} = 4358 * 10^{-10};
      //wavelength of exciting line (m)
3 \text{ vsto} = 4458 * 10^{-10};
      //wavelength of Stokes line (m)
5 //calculation of wavelength of Anti-stokes line
6 vbar_exc=1/vexc;
      //wave number of exciting line (m-1)
7 vbar_sto=1/vsto;
      //wave number of Stokes line (m-1)
8 delta_vbar=vbar_exc-vbar_sto;
      //Raman shift (m-1)
9 vbar_antistoke=vbar_exc+delta_vbar;
                                                      //
      Wave number of Anti-Stokes line (m-1)
10 lembda_antistoke=(1/vbar_antistoke)*10^10;
                                              //Wavelength
       of Anti-Stokes line ( )
11
12 printf("\nwavelength of Anti-stokes line = \%.1 f
      lembda_antistoke);
```

Scilab code Exa 5.5.20 Ex 20

```
1 // variable initialization
2 h=6.62*10^{-34};
      //Plank's constant (joule second)
3 c=3*10^8;
      //Speed of light (m/s)
4 x=62.4*100;
      //(m-1)
5 y = 41.6 * 100;
      //(m-1)
  //calculation of the moment of inertia of HCl
      molecule
8 B = y/4;
      //Rotational constant of HCl (m-1)
9 I=h/(8*\%pi^2*B*c);
      //Moment of inertia (kg m<sup>2</sup>)
10
11 printf("\n I = \%.1e kg m<sup>2</sup>,I);
   Scilab code Exa 5.5.21 Ex 21
1 //function for calculating the vibrational energy of
       O2 molecule
2 function[energy]=F(v)
       energy=(((v+.5)*a)-(((v+.5)^2)*b))*h*c;
4 endfunction
6 //variable initialization
7 h=6.62*10^-34;
```

```
//Plank's constant (joule second)
8 c=3*10^8;
     //Speed of light (m/s)
9 a=1580.36*100;
     // value of e (m-1)
10 b=12.07*100;
     // value of exe (m-1)
11
12 // Calculation of zero point energy
13 E0=F(0);
     //Zero point energy of the molecule (J)
14
15 // Calculation of vibrational Raman shift
16 shift=(F(1)-F(0))/(h*c);
      //Expected vibrational Raman shift (m-1)
17
18 printf("\nZero point energy = \%.3e J\nExpected
      vibrational Raman shift = \%.0 \, \text{f m-1}", E0, shift);
```