```
DS

莫队

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对拍

INT128
```

# DS

# 莫队

```
int n, m, len;
const int N = 200010;
bool cmp(array<int, 3> a, array<int, 3> b) {
   int x = a[0]/len;
   int y = b[0]/len;
   if (x != y) return x < y;
    else return a[1] < b[1];
}
void solve() {
    cin >> n >> m;
    vec<int> a(n+1,0);
    vec<int> cnt(N, 0);
    vec<array<int, 3>> evt;
    for (int i = 1; i <= n; i++) {
        cin >> a[i];
    }
    for (int i = 1; i <= m; i++) {
        int 1, r;
        cin >> 1 >> r;
        evt.pb({1, r, i});
    }
    len = max(111, (11) sqrtl(1.0 * n * n / m));
    sort(all(evt), cmp);
    11 ans = 0;
    int 1 = 0, r = 0;
    11 res[N];
    auto add = [\&] (int p) {
        cnt[a[p]]++;
        if (cnt[a[p]] == 2) ans++;
    };
    auto sub = [\&](int p) {
```

```
cnt[a[p]]--;
        if (cnt[a[p]] == 1) ans--;
    };
    for (auto x : evt) {
        while (r < x[1]) r++, add(r);
        while (r > x[1]) sub(r), r--;
        while (1 < x[0]) sub(1), 1++;
        while (1 > x[0]) 1--, add(1);
        res[x[2]] = ans;
    }
    for (int i = 1; i <= m; i++) {
        cout << (res[i]==0?"Yes":"No") << '\n';</pre>
    }
}
int main()
    ios::sync_with_stdio(false);
    cin.tie(nullptr);
    cout.tie(nullptr);
    int _;
    _{-} = 1;
    for (int i = 1; i <= _; i++) {
        solve();
   return 0;
}
```

# 树状数组(求逆序对)

```
// https://atcoder.jp/contests/abc296/submissions/40293683
const int N = 200010;
int c[N];
int n;
void modify (int x, int y) {
   for (x; x \le n; x += x \& -x) c[x] += y;
int query(int x) {
   int s = 0;
   for (x; x; x = x \& -x) s += c[x];
   return s;
}
void solve(int Tcase = 1) {
   cin >> n;
   vec<int> a(n), b(n);
   for (int i = 0; i < n; i++) {
        cin >> a[i];
   }
   for (int i = 0; i < n; i++) {
        cin >> b[i];
```

```
11 \text{ res1} = 0, \text{ res2} = 0;
    for (int i = n - 1; i >= 0; i--) {
        modify(a[i], 1);
        res1 += query(a[i] - 1);
    }
    for (int i = 1; i \le n; i++) c[i] = 0;
    for (int i = n - 1; i >= 0; i--) {
        modify(b[i], 1);
        res2 += query(b[i] - 1);
    }
    sort(a.begin(), a.end());
    sort(b.begin(), b.end());
    bool f = 0;
    for (int i = 0; i < n; i++) {
        if (a[i] != b[i]) {
             cout << "No\n";</pre>
             return ;
        }
        if (i && a[i] == a[i - 1]) {
            f = 1;
        }
    }
    if (f) {
        cout << "Yes\n";</pre>
        return ;
    cout << ((res1+res2)%2==0? "Yes":"No");</pre>
}
```

# 拓扑排序判环

```
// https://atcoder.jp/contests/abc296/submissions/40269554
const int N = 200010;
int n;
vec<int> e[N];
void solve(int Tcase = 1) {
    cin >> n;
    vec<int> a(n + 1, 0);
    vec<int> idg(n + 1, 0);
    for (int i = 1; i <= n; i++) {
        cin >> a[i];
        idg[a[i]]++;
        e[i].pb(a[i]);
    }
    queue<int> que;
    for (int i = 1; i <= n; i++) {</pre>
```

```
if (!idg[i]) que.push(i);
}
int ans = n;

while (!que.empty()) {
    int t = que.front();
    que.pop();
    ans--;
    for (auto v : e[t]) {
        if (--idg[v] == 0) {
            que.push(v);
        }
    }
}
cout << ans << '\n';
}</pre>
```

### 树链剖分

```
// 树链剖分
const int N = 200010;
int n, m, a[N];
int dep[N], 1[N], r[N], top[N], id[N], e_to_p[N];
int son[N], sz[N], fa[N], tot, p_to_e[N];
// 1[x], r[x]求出的是第x个点在dfs序上的区间范围
// e_{to_p[x]} 求的是第x条边依附于哪个点
// p_to_e[x] 求的是第x个点的边是哪个
vec<P(int)> e[N];
void dfs1(int u, int f) {
   fa[u] = f;
   dep[u] = dep[f] + 1;
   son[u] = -1;
   sz[u] = 1;
   for (auto [v, p]: e[u]) {
       if (v == f) continue;
       dfs1(v, u);
       e_{to_p[p]} = v;
       p_{to} = [v] = p;
       sz[u] += sz[v];
       if (son[u] == -1 \mid \mid sz[son[u]] < sz[v]) {
           son[u] = v;
       }
   }
}
void dfs2(int u, int t) {
   top[u] = t;
   l[u] = ++tot;
   id[tot] = u;
   if (son[u] != -1) {
       dfs2(son[u], t);
   for (auto [v, p]: e[u]) {
       if (v == fa[u] || v == son[u]) continue;
       dfs2(v, v);
```

```
r[u] = tot;
}
struct seg{
   11 sum;
    seg operator + (const seg& R) const {
        return (seg){sum + R.sum};
   }
    seg operator - (const seg& R) const {
        return (seg){sum - R.sum};
   }
} tr[N << 4];</pre>
void pushup(int p) {
   tr[p] = tr[lp] + tr[rp];
void build(int p, int 1, int r) {
   if (1 == r) {
        tr[p] = {1|| * a[p_to_e[id[1]]]};
        int mid = (1 + r) / 2;
        build(lp, l, mid);
        build(rp, mid + 1, r);
        pushup(p);
   }
}
void modify(int p, int 1, int r, int pos, 11 d) {
   if (1 == r) {
        tr[p].sum = d;
   } else {
        int mid = (1 + r) / 2;
        if (pos <= mid) modify(lp, l, mid, pos, d);</pre>
        else modify(rp, mid + 1, r, pos, d);
        pushup(p);
   }
}
seg query(int p, int 1, int r, int q1, int qr) {
   if (q1 <= 1 && r <= qr) return tr[p];
   int mid = (1 + r)/2;
   if (q1 > mid)
        return query(rp, mid + 1, r, ql, qr);
   else if (qr <= mid)
        return query(lp, l, mid, ql, qr);
   else
        return query(lp, l, mid, ql, qr) +
        query(rp, mid + 1, r, ql, qr);
}
seg query(int u, int v) {
   seg ans = \{0\};
   int p = u, q = v;
   while (top[u] != top[v]) {
```

```
if (dep[top[u]] < dep[top[v]]) {</pre>
            if (u != v)
                ans = ans + query(1, 1, n, l[top[v]], l[v]);
            v = fa[top[v]];
        } else {
            if (u != v)
                 ans = ans + query(1, 1, n, 1[top[u]], 1[u]);
            u = fa[top[u]];
        }
    if (v == u) return ans;
    if (dep[v] < dep[u]) {</pre>
        ans = ans + query(1, 1, n, 1[v]+1, 1[u]);
        ans = ans + query(1, 1, n, l[u]+1, l[v]);
    return ans;
}
void solve(int caseT = 1) {
    cin >> n;
    for (int i = 1; i < n; i++) {
        int u, v, w;
        cin >> u >> v >> w;
        e[u].pb({v, i});
        e[v].pb({u, i});
        a[i] = w;
    }
    dfs1(1, 0);
    dfs2(1, 1);
    build(1, 1, n);
    cin >> m;
    for (int i = 1; i \le m; i++) {
        int op, x, y;
        cin >> op >> x >> y;
        if (op == 1) {
            modify(1, 1, n, l[e_to_p[x]], y);
            seg ans = query(x, y);
            cout << ans.sum << '\n';</pre>
        }
   }
}
```

### **DSU** on Tree

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
const int N = 100010;
int hs[N], sz[N], l[N], r[N], tot, id[N];
vector<int> e[N];
int cnt[N];
```

```
int a[N], n;
11 sumcnt, maxcnt, ans[N];
void dfs(int u, int fa) {
   sz[u] = 1;
   hs[u] = -1;
   l[u] = ++tot;
   id[tot] = u;
   for (auto v : e[u]) {
        if (v == fa) continue;
        dfs(v, u);
        sz[u] += sz[v];
        if (hs[u] == -1 \mid | sz[v] > sz[hs[u]])
            hs[u] = v;
   }
   r[u] = tot;
void DSU(int u, int fa, bool keep) {
    for (auto v : e[u]) {
        if (v != fa && v != hs[u])
            DSU(v, u, false);
   if (hs[u] != -1) {
        DSU(hs[u], u, true);
   }
    auto add = [\&](int x) {
       int col = a[x];
        cnt[col]++;
        if (cnt[col] > maxcnt)
            maxcnt = cnt[col], sumcnt = col;
        else if (cnt[col] == maxcnt)
            sumcnt += col;
   };
   auto del = [\&](int x) {
        int col = a[x];
        cnt[col]--;
   };
    for (auto v : e[u]) {
        if (v != fa && v != hs[u]) {
            for (int x = 1[v]; x \ll r[v]; x++)
                add(id[x]);
        }
    }
    add(u);
   ans[u] = sumcnt;
   if (!keep) {
        maxcnt = 0;
        sumcnt = 0;
        for (int x = 1[u]; x \leftarrow r[u]; x++) {
            del(id[x]);
        }
   }
```

```
int main () {
    scanf("%d", &n);
    for (int i = 1; i <= n; i++) scanf("%d", a + i);
    for (int i = 1; i < n; i++) {
        int u, v;
        scanf("%d%d", &u, &v);
        e[u].push_back(v);
        e[v].push_back(u);
    }
    dfs(1, 0);
    DsU(1, 0, false);
    for (int i = 1; i <= n; i++)
        printf("%1ld%c", ans[i], " \n"[i == n]);
    return 0;
}</pre>
```

### 根号分治

```
#include <bits/stdc++.h>
using namespace std;
using 11 = long long;
const int N = 200010, M = 500;
int n, m, q;
ll tag[M + 10][M + 10], val[N];
void solve() {
   cin >> n >> q;
   for (int i = 0; i < q; i++) {
        int op, x;
        cin >> op >> x;
        if (op == 1) {
            int y, d;
            cin >> y >> d;
            if (x \ll M) {
                tag[x][y] += d;
            } else {
                for (int j = y; j <= n; j += x) {
                    val[j] += d;
                }
            }
        } else {
            ll ans = val[x];
            for (int j = 1; j <= M; j++) {
                ans += tag[j][x%j];
            cout << ans << '\n';</pre>
       }
   }
}
```

### 对拍

```
mt19937_64 rnd(time(0));
11 a = rnd();
```

#### 对拍代码

```
#include<bits/stdc++.h>
using namespace std;
int main() {
    for (int i = 1; i <= 1000; i++) {
        system("rand > a.in"); // linuxF ./rand
        system("ac < a.in > ac.out"); // linuxF ./ac
        system("wa < a.in > wa.out"); // linuxF ./wa
        if (system("fc ac.out wa.out")) { // // linuxF diff
            printf("Case %i is wa!!!\n", i);
            exit(0);
        } else {
            printf("Case %i is Ac!!!\n", i);
        }
    }
}
```

#### **INT128**

```
#include <bits/stdc++.h>
#define P __int128
using namespace std;
P read() {
   P s = 0, f = 1;
   char c = getchar();
   while (c < '0' || c > '9') {
       if (c == '-') f = -1;
       c = getchar();
   while ('0' <= c && c <= '9') {
       s = s * 10 + c - '0';
       c = getchar();
   return s * f;
}
void write(P x) {
   if (x \ge 10) write(x/10);
   putchar(x%10+'0');
}
int main() {
   Pa = read();
   write(a);}
```