

# Самый Правильный

N1

a) верно

$$b) (x + \bar{O}(x))(2x^2 + \bar{O}(x^2)) = 2x^3 + \bar{O}(x^3) + \bar{O}(2x^3) + \bar{O}(x^3) = 2x^3 + \bar{O}(x^3) - \text{верно}$$

$$c) \bar{O}(1) + \bar{O}(2) + \bar{O}(3) + \bar{O}(4) = \bar{O}(1) + \bar{O}(1) + \bar{O}(1) + \bar{O}(1) = \bar{O}(1) \Rightarrow \text{верно}$$

$$d) \bar{O}(1) - \bar{O}(1) = \bar{O}(1) + \bar{O}(-1) = \bar{O}(1) + \bar{O}(1) = \bar{O}(1) \Rightarrow \text{неверно}$$

N2

$$a) \lim_{x \rightarrow 0} \left\{ \frac{19x - x}{\sin x - x} = \frac{x + \frac{1}{3}x^3 - x + \bar{O}(x^3)}{x - \frac{1}{6}x^3 - x + \bar{O}(x^3)} = \frac{\frac{1}{3} + \bar{O}(x^3)}{-\frac{1}{6} + \bar{O}(x^3)} \right\} = -2$$

$$b) \lim_{x \rightarrow 0} \left\{ \frac{1 + x \cos x - \sqrt{1+2x}}{\ln(1+x) - x} = \frac{1 + x - \frac{x^2}{2} + \bar{O}(x^2)}{x - \frac{x^2}{2} + \frac{x^3}{3} + \bar{O}(x^3)} = \frac{2x - \frac{x^2}{2} + \bar{O}(x^2)}{-\frac{x^2}{2} + \bar{O}(x^2)} = \frac{x(2 - \frac{x}{2} + \bar{O}(x))}{x(-\frac{x}{2} + \bar{O}(x))} = \frac{2 - \frac{x}{2} + \bar{O}(x)}{-\frac{x}{2} + \bar{O}(x)} = \infty + 1$$

$$c) \lim_{x \rightarrow 0} \left\{ \frac{\sqrt{1+2x} - 1}{\sqrt[4]{1+x} \sqrt{1-x}} = \frac{1 + \frac{2x}{5} - \frac{8x^2}{25} - 1 + \bar{O}(x^2)}{1 + \frac{x}{4} - \frac{3x^2}{32} - 1 + \frac{x}{2} + \frac{x^2}{8} + \bar{O}(x^2)} = \frac{\frac{2x}{5} + \bar{O}(x)}{\frac{3x}{4} + \bar{O}(x)} = \frac{\frac{2}{5} + \bar{O}(1)}{\frac{3}{4} + \bar{O}(1)} \right\} = \frac{8}{15}$$

$$d) \lim_{x \rightarrow 0} \left\{ \frac{(1-x)^x - 1}{x^2} = \frac{e^{\ln(1-x)x} - 1}{x^2} = \frac{1 + \ln(1-x)x + \frac{1}{2}(\ln(1-x)x)^2 + o(x^2)}{x^2} \right\} = 1$$