

```

[ > restart;
[ > m:=-15*sqrt(3)*T/2/a^5;

$$m := -\frac{15 \sqrt{3} T}{2 a^5}$$

[ > fai:=m*(x-a)*(x-sqrt(3)*y)*(x+sqrt(3)*y);

$$fai := -\frac{15 \sqrt{3} T (x-a) (x-\sqrt{3} y) (x+\sqrt{3} y)}{2 a^5}$$

[ > simplify(fai);

$$-\frac{15 \sqrt{3} T (x-a) (x^2-3 y^2)}{2 a^5}$$

[ > zy:=- (diff(fai,x));

$$zy := \frac{15 \sqrt{3} T (x-\sqrt{3} y) (x+\sqrt{3} y)}{2 a^5} + \frac{15 \sqrt{3} T (x-a) (x+\sqrt{3} y)}{a^5} + \frac{15 \sqrt{3} T (x-a) (x-\sqrt{3} y)}{a^5}$$

[ > # 切应力y
[ > simplify(zy);

$$\frac{15 \sqrt{3} T (3 x^2-3 y^2-2 a x)}{2 a^5}$$

[ > zx:=diff(fai,y);

$$zx := \frac{45 T (x-a) (x+\sqrt{3} y)}{2 a^5} - \frac{45 T (x-a) (x-\sqrt{3} y)}{2 a^5}$$

[ > # 切应力x
[ > simplify(zx);

$$45 \frac{T (x-a) \sqrt{3} y}{a^5}$$

[ >
[ > f:=(x,y)->-15/2*3^(1/2)*T*(-3*x^2+3*y^2+2*a*x)/a^5;

$$f := (x, y) \rightarrow -\frac{15 \sqrt{3} T (-3 x^2+3 y^2+2 a x)}{2 a^5}$$

[ > # 求 切应力y 的两个偏导
[ > fx:=D[1](f)(x,y);

$$fx := -\frac{15 \sqrt{3} T (-6 x+2 a)}{2 a^5}$$

[ > fy:=D[2](f)(x,y);

$$fy := -45 \frac{\sqrt{3} T y}{a^5}$$


```

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[ > #求 驻点
[ > solve({D[1](f)(x,y)=0,D[2](f)(x,y)=0},{x,y});
                                     
$$\{y=0, x=\frac{1}{3}a\}$$

[ > # 求ABC , 判断 是否为极值
[ > A:=D[1,1](f)(x,y);
                                     
$$A:=45\frac{\sqrt{3}T}{a^5}$$

[ > B:=D[1,2](f)(x,y);
                                     
$$B:=0$$

[ > C:=D[2,2](f)(x,y);
                                     
$$C:=-45\frac{\sqrt{3}T}{a^5}$$

[ >
[ > Delta:=A*C-B^2;
                                     
$$\Delta:=-6075\frac{T^2}{a^{10}}$$

[ > # 驻点切应力
[ > x0:=a/3;y0:=0;
                                     
$$x0:=\frac{1}{3}a$$

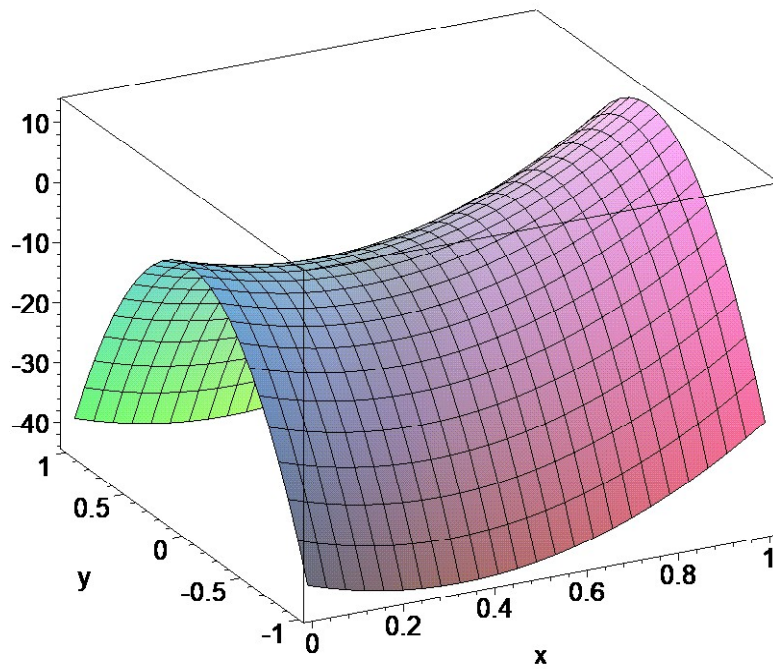
                                     
$$y0:=0$$

[ > f(x0,y0);
                                     
$$-\frac{5}{2}\frac{\sqrt{3}T}{a^3}$$

[ > # Delta<0, 非 极值
[ >
[ > # 作图取M=1,a=1
[ > ff:=-15/2*3^(1/2)*1*(-3*x^2+3*y^2+2*1*x)/1^5;
                                     
$$ff:=-\frac{15}{2}\sqrt{3}(-3x^2+3y^2+2x)$$

[ > plot3d(ff,x=0..1,y=-1..1);

```



> #真实最大切应力

> Ty:=f(a,0);

$$Ty := \frac{15 \sqrt{3} T}{2 a^3}$$

>

> # 同理计算切应力x

> f2:=(x,y)->-45\*T\*(-x+a)\*3^(1/2)\*y/a^5;

$$f2 := (x, y) \rightarrow -45 \frac{T(-x+a) \sqrt{3} y}{a^5}$$

> fx2:=D[1](f2)(x,y);

$$fx2 := 45 \frac{\sqrt{3} T y}{a^5}$$

> fy2:=D[2](f2)(x,y);

$$fy2 := -45 \frac{T(-x+a) \sqrt{3}}{a^5}$$

> solve({D[1](f2)(x,y)=0,D[2](f2)(x,y)=0},{x,y});

$$\{x=a, y=0\}$$

>

> AA:=D[1,1](f2)(x,y);

$$AA := 0$$

> BB:=D[1,2](f2)(x,y);

$$BB := 45 \frac{\sqrt{3} T}{a^5}$$

```
> CC:=D[2,2](f2)(x,y);
```

$$CC := 0$$

```
> Delta2:=AA*CC-BB^2;
```

$$\Delta 2 := -6075 \frac{T^2}{a^{10}}$$

```
> x2:=a;y2:=0;
```

$$x2 := a$$

$$y2 := 0$$

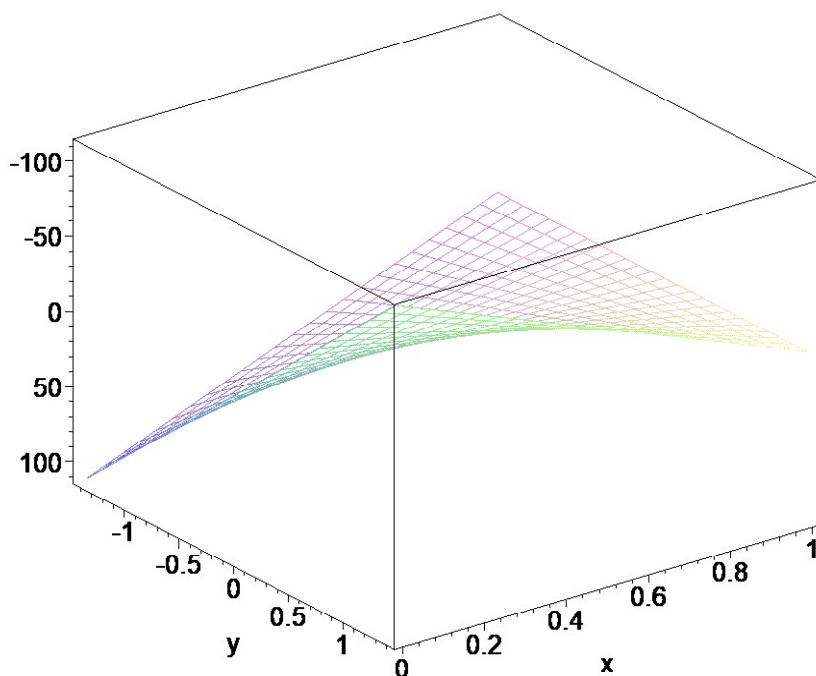
```
> f2(x2,y2);
```

$$0$$

```
> ff2:=-45*1*(-x+1)*3^(1/2)*y/1^5;
```

$$ff2 := -45(-x+1)\sqrt{3}y$$

```
> plot3d(ff2,x=0..1,y=-1.414..1.414);
```



```
> # 求条件极值
```

```
> ff3:=simplify(-45*1*(-x+1)*x);
```

$$ff3 := 45(x-1)x$$

```
> f3:=(x)->-45*T*(-x+a)*x/a^4;
```

$$f3 := x \rightarrow -45 \frac{T(-x+a)x}{a^4}$$

```
> solve({D[1](f3)(x)=0},{x});
```

$$\{x = \frac{1}{2}a\}$$

```
[ > #真实最大切应力
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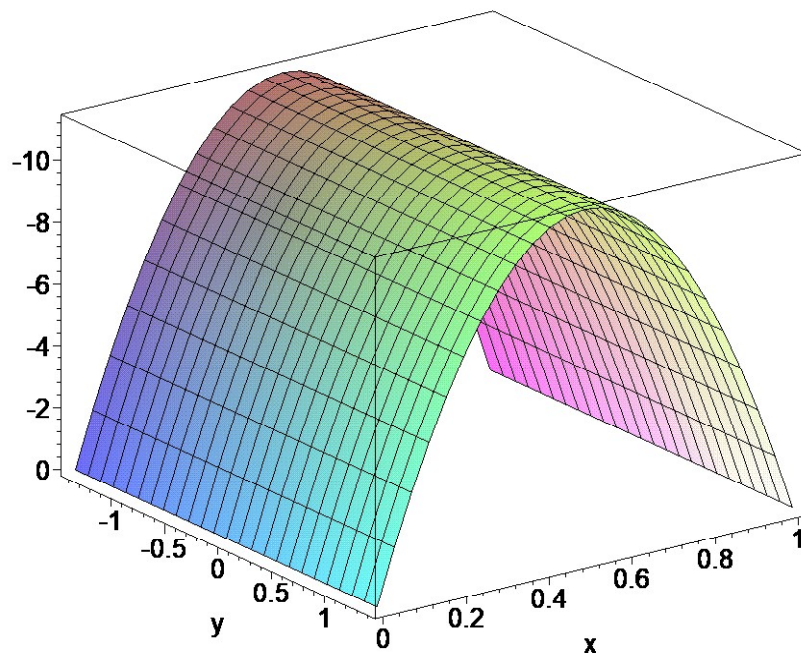
```
[ > Tx:=f3(a/2,0);
```

$$Tx := -\frac{45}{4} \frac{T}{a^2}$$

```
[ >
```

```
[ >
```

```
[ > plot3d(ff3,x=0..1,y=-1.414..1.414);
```



```
[ > # 比较两方向最大切应力，取T=1，a=1
```

```
[ > 15*sqrt(3.)/2;
```

12.99038106

```
[ > 45/4.;
```

11.25000000

```
[ > Tmax:=Ty;
```

$$Tmax := \frac{15}{2} \frac{\sqrt{3} T}{a^3}$$

```
[ >
```