

Algoritam za izracunavanje zatvaraca

1. $F = \{AB \rightarrow AC, CD \rightarrow E, A \rightarrow B, AE \rightarrow F\}$

$$AB \rightarrow A \quad AB \rightarrow C$$

ZATVARAC

$$(AD)^+ = AD$$

$$(AD)^+ = ADB \quad (A \rightarrow B)$$

$$(AD)^+ = ADBC \quad (AB \rightarrow C)$$

$$(AD)^+ = ADBCE \quad (CD \rightarrow E)$$

$$(AD)^+ = ADBCEF \quad (AE \rightarrow F)$$

2. $F = \{AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ACD \rightarrow B, D \rightarrow EG, BE \rightarrow C, CG \rightarrow BD, CE \rightarrow AG\}$

$$D \rightarrow E \quad D \rightarrow G$$

$$CG \rightarrow B \quad CG \rightarrow D$$

$$CE \rightarrow A \quad CE \rightarrow G$$

$$(BD)^+ = BDEGCA$$

3. $F = \{A \rightarrow B, A \rightarrow C, A \rightarrow E, D \rightarrow C, E \rightarrow I, BI \rightarrow J\}$

$$(AI)^+ = AIBCEJ$$

$$(DJ)^+ = DJC$$

$$(BE)^+ = BEIJ$$

Algoritam za trazenje kljuca

1. $R = \{A, B, C, D, E\}$

$$F = \{AB \rightarrow CDE, E \rightarrow A, CD \rightarrow B\}$$

$$AB \rightarrow C, AB \rightarrow D, AB \rightarrow E$$

$$(ABCDE)^+ = ABCDE = R / E$$

$$(ABCD)^+ = ABCDE = R / D$$

$$(ABC)^+ = ABCDE = R / C$$

$$(AB)^+ = ABCDE = R / B$$

$$(A)^+ = A$$

$$(B)^+ = B$$

$$K = \{AB, EB, ACD, ECD\}$$

$$2. \quad U = \{A, B, C, D, E, F\},$$

$$F = \{AB \rightarrow C, C \rightarrow A, C \rightarrow D, AB \rightarrow E, AB \rightarrow F, E \rightarrow F\}$$

$$(ABCDEF)^+ = ABCDEF = U \quad /F$$

$$(ABCDE)^+ = ABCDEF = U \quad /E$$

$$(ABCD)^+ = ABCDEF = U \quad /D$$

$$(ABC)^+ = ABCDEF = U \quad /C$$

$$(AB)^+ = ABCDEF = U \quad /B$$

$$(A)^+ = A$$

$$(B)^+ = B$$

$$K = \{AB, CB, \dots\}$$

$$3. \quad F = \{AB \rightarrow CE, C \rightarrow B, ED \rightarrow F, F \rightarrow G\}$$

$$R = \{A, B, C, D, E, F, G, H\}$$

H i D svakako mora jer se ne pojavljuje na desnim stranama FZ

$$(ABCDEFGH)^+ = ABCDEFGH \quad /G$$

$$(ABCDEFH)^+ = ABCDEFGH \quad /F$$

$$(ABCDEH)^+ = ABCDEFGH \quad /E$$

$$(ABCDH)^+ = ABCDEFGH \quad /C$$

$$(ABDH)^+ = ABCDEFGH \quad /B$$

$$(ADH)^+ = ADH$$

$$(BDH)^+ = BDH$$

$$K = \{ABDH, ACDH, \dots\}$$

Dokazivanje da je fz logicka posledica skupa fz prema Armstrongovim pravilima

$$1. \quad F = \{A \rightarrow B, B \rightarrow C, AC \rightarrow D, BD \rightarrow E, C \rightarrow E\}$$

$$U = \{A, B, C, D, E\}$$

a. $F \models A \rightarrow D$ ovo treba dokazati.

$$(A)^+ = ABCDE$$

$$\begin{array}{l} A \rightarrow B \\ B \rightarrow C \end{array} \} \Rightarrow_{A3} \quad \begin{array}{l} A \rightarrow C \\ A \in U \end{array} \} \Rightarrow_{A2} \quad \begin{array}{l} A \rightarrow AC \\ AC \rightarrow D \end{array} \} \Rightarrow_{A3} \quad A \rightarrow D$$

b. $F \models AD \rightarrow E$ ovo treba dokazati.

prvo zatvarac nad AD

$$(AD)^+ = ABCDE$$

$$\begin{array}{l} A \rightarrow B \\ D \in U \end{array} \} \Rightarrow_{A2} \quad \begin{array}{l} AD \rightarrow BD \\ BD \rightarrow E \end{array} \} \Rightarrow_{A3} \quad AD \rightarrow E$$

2. $F = \{ A \rightarrow F, AB \rightarrow CE, AC \rightarrow D, EB \rightarrow D, D \rightarrow A, F \rightarrow AE \}$

$$U = \{A, B, C, D, E, F\}$$

$$AB \rightarrow C, AB \rightarrow E, F \rightarrow A, F \rightarrow E$$

a. $F \models AB \rightarrow D$ ovo treba dokazati.

prvo zatvarac nad AB

$$(AB)^+ = ABFCED$$

$$\begin{array}{l} AB \rightarrow E \\ EB \rightarrow D \end{array} \} \Rightarrow_{A3} \quad EB \rightarrow D$$

$$\begin{array}{l} AB \rightarrow E \\ B \in U \end{array} \} \Rightarrow_{A2} \quad \begin{array}{l} AB \rightarrow EB \\ EB \rightarrow D \end{array} \} \Rightarrow_{A3} \quad AB \rightarrow D$$

3. $F = \{ AB \rightarrow C, C \rightarrow A, BC \rightarrow D, ACD \rightarrow B, D \rightarrow EG, BE \rightarrow C \}$

$$U = \{A, B, C, D, E, F, G\}$$

$$D \rightarrow E, D \rightarrow G, CG \rightarrow B, CG \rightarrow D, CE \rightarrow A, CE \rightarrow G$$

a. $F \models CE \rightarrow B$ ovo treba dokazati.

prvo zatvarac nad CE

$$(CE)^+ = ABCDEFG$$

$$\begin{array}{l} CE \rightarrow G \\ C \in U \end{array} \} \Rightarrow_{A2} \quad \begin{array}{l} CE \rightarrow CG \\ CG \rightarrow B \end{array} \} \Rightarrow_{A3} \quad CE \rightarrow B$$

b. $F \models BD \rightarrow C$ ovo treba dokazati.

prvo zatvarac nad BD

$$(BD)^+ = ABCDEFG$$

$$\begin{array}{l} D \rightarrow E \\ B \in U \end{array} \} \Rightarrow_{A2} \quad \begin{array}{l} BD \rightarrow BE \\ BE \rightarrow C \end{array} \} \Rightarrow_{A3} \quad BD \rightarrow C$$

c. $F \models CE \rightarrow D$ ovo treba dokazati.

prvo zatvarac nad CE

$(CE)^+ = ABCDEFG$

$CE \rightarrow G$ $CE \rightarrow CG$
 $C \in U$ $\} \Rightarrow A_2$ $CG \rightarrow D$ $\} \Rightarrow A_3$ $CE \rightarrow D$

d. $F \models ABG \rightarrow E$ ovo treba dokazati.

prvo zatvarac nad ABG

$(ABG)^+ = ABCDEFG$

$AB \rightarrow C$ $ABG \rightarrow CG$ $ABG \rightarrow D$
 $G \in U$ $\} \Rightarrow A_2$ $CG \rightarrow D$ $\} \Rightarrow A_3$ $D \rightarrow E$ $\} \Rightarrow A_3$ $ABG \rightarrow E$

e. $F \models CD \rightarrow B$ ovo treba dokazati.

prvo zatvarac nad CD

$(CD)^+ = ABCDEFG$

$D \rightarrow G$ $CD \rightarrow CG$
 $C \in U$ $\} \Rightarrow A_2$ $CG \rightarrow B$ $\} \Rightarrow A_3$ $CD \rightarrow B$

f. $F = \{AB \rightarrow AC, CD \rightarrow E, A \rightarrow B, AE \rightarrow F\}$

$U = \{A, B, C, D, E, F\}$

$F \models AD \rightarrow F$ ovo treba dokazati.

prvo zatvarac nad AD

$(AD)^+ = ABCDEF$

$A \rightarrow B$	$\} \Rightarrow A_2$	$A \rightarrow AB$	$\} \Rightarrow A_3$	$A \rightarrow C$	$\} \Rightarrow A_2$	$AD \rightarrow CD$	$\} \Rightarrow A_3$	$AD \rightarrow E$
$A \in U$		$AB \rightarrow C$		$D \in U$		$CD \rightarrow E$		$A \in U$
$\} \Rightarrow A_2$	$AD \rightarrow AE$	$\} \Rightarrow A_3$	$AD \rightarrow F$					
	$AE \rightarrow F$							