

Prof. dr Dragan Ivetić

RAČUNARSKA GRAFIKA
skripta

SEDAMNAESTA GENERACIJA STUDENATA



Novi Sad, 2017. godine

Kome i kako?



RAČUNARSKA GRAFIKA (RI4A), 3 + 2
(na FTN od 2001./2002. školske godine)

Dr Dragan Ivetić, redovni profesor

E2 Primjenjene računarske nauke i informatika, 7. semestar
Animacija u inženjerstvu (ANI), 3. semestar

Nenad Milić, (E2, ANI)
Milan Adamović, (ANI, E2)

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O nastavniku



Dipl. ing. elek. - računarstvo i automatika, 1990, FTN,
Mr teh. nauka - formalizmi u SE, 1994, FTN,
Dr teh. nauka - integracija HCI i SE, 1999, FTN.
DAAD, RWTH Aachen – Primena multim. u industriji, 1997.
R. prof., FTN – elektrotehn. i računarstvo, 2010.



Grafički i multimedijalni sistemi, šk. 2001./2002.
Interakcija čovek računar, šk. 2002./2003.
Kompresija podataka, šk. 2005./2006.
Sistemi virtuelne realnosti, 2009./2010.
Razvoj računarskih igara, šk. 2013./2014.



Jugodrvo 202, Bulevar Oslobođenja 133, Novi Sad
(021) xxx-xxxx, 485-2424 (AI xx/yyyy i ftn)
<http://gim.ftn.uns.ac.rs> ivetic@uns.ac.rs

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Kako položiti predmet?**1. Predispitne obaveze, do 70 bodova:**

vežbe (poznavanje OpenGL) – **50 bodova + deskriptor.**

teorija u praksi (pitanja na vežbama u 2 navrata) – **20 bodova,**

Potpis se dobija bez uslova.

2. Završni ispit (moguće 3 isključive varijante)

1. BEZ (vežbe>24, T. pitanja>14 i nikada GIM) – 55..70 (potpisana saglasnost u januaru, junu ili septembru)

3. Usmeni 30 minuta (15.. 30), (vežbe>24), – 55 .. 100, termini na GIMu tokom JAN FEB MART APR MAJ, 2 puta maksimalno, u suprotnom sve ponovo

Literatura

1. SLAJDOVI SA PREDAVANJA **SA VASIM BELEŠKAMA**
2. Hughes, V. Dam, McGuire, Sklar, Foley, Feiner, & Akeley, **COMPUTER GRAPHICS Principles and Practice**, 2013.
3. Peter Shirley, Steve Marschner, with ..., **FUNDAMENTALS OF COMPUTER GRAPHICS**, 3rd Ed, 2009.
4. Akenine-Möller T., Heines E. and Hoffman N, **REAL-TIME RENDERING**, 3rd Ed., 2008.
5. Rick Parent, **COMPUTER ANIMATION: ALGORITHMS AND TECHNIQUES**, Morgan Kaufmann, 2002.
6. Shreiner, Sellers, Kessenich, Licea-Kane, **OpenGL 4.3 Programming Guide**, 8th ed, 2013.

Oblasti računarske grafike

su:

→ **Generativna grafika**

- konstrukcija objekata i generisanje slike,
- transformacija objekata i slike,
- identifikacija objekata i info. retrieval

→ **Obrada i analiza slike**

- unapređenje slike (kontrast, smetnje),
- evalvacija slike (veličine, oblika),
- prepoznavanje obrazaca (pattern)

→ **Kognitivna grafika**

ili “analiza scene” - identifikovanje i rad sa objektima fotografije ili kompjuterske slike (RTG film i elektronska kontura organa)

Osnovni pojmovi i procesi

Samo 3D esencijalni i perceptivni:

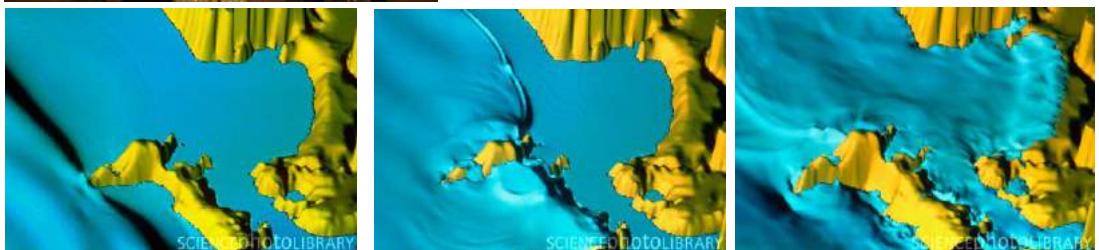
- Tačka, vertex, vertices
- Linija/linije, edge
- Trouglovi,
- Transformacije, 
- 3D/2D projekcija/skrivanje,
- Kliping,
- Bojenje,
- Senčenje,
- Teksture,
- Spajanje.

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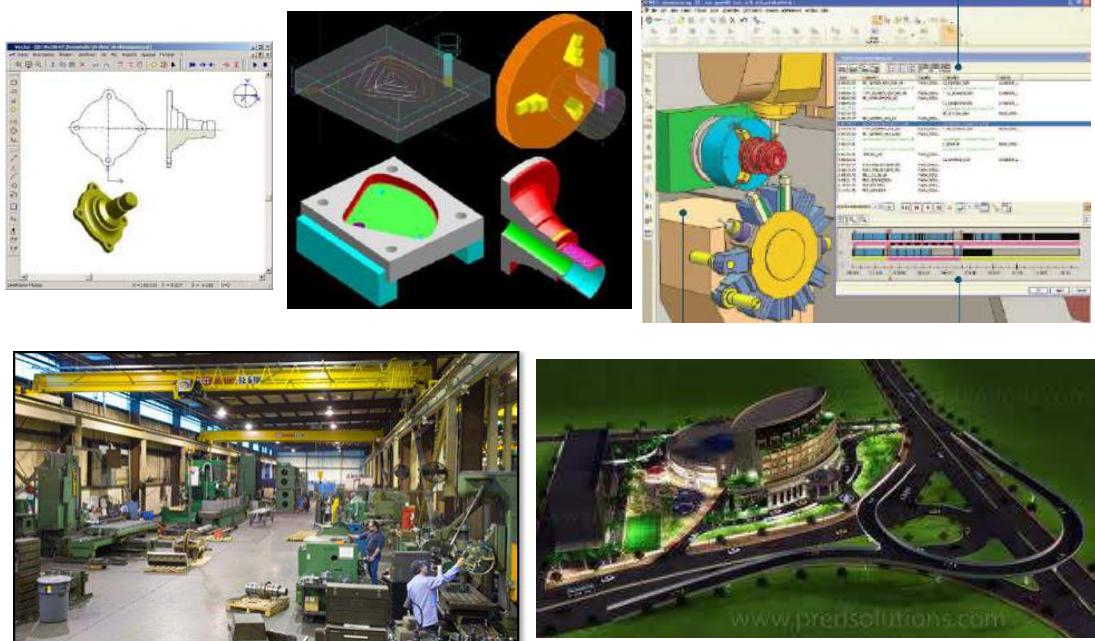
Real-Time (interaktivna) grafika
Simluacije

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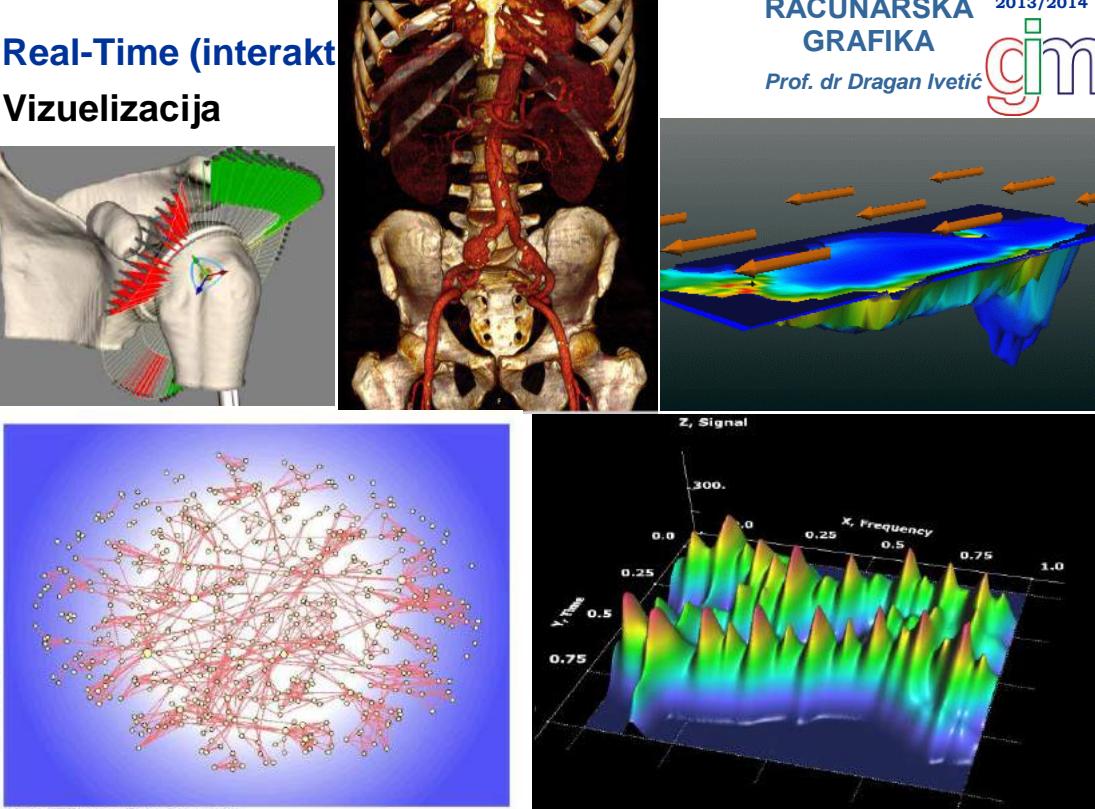
Real-Time (interaktivna) grafika CAD, CAA i CAM



The top section displays three screenshots of professional software: a 2D CAD program (SolidWorks) showing a part's cross-section and 3D view; a 3D CAD program (CATIA) showing a mold and a tool; and a CAM (Computer Aided Manufacturing) program showing a complex assembly with various components and tool paths. The bottom section contains two photographs: one of a large industrial facility with workers operating machinery, and another of a modern stadium at night, likely generated by a CAA (Computer Aided Architecture) or visualization software.

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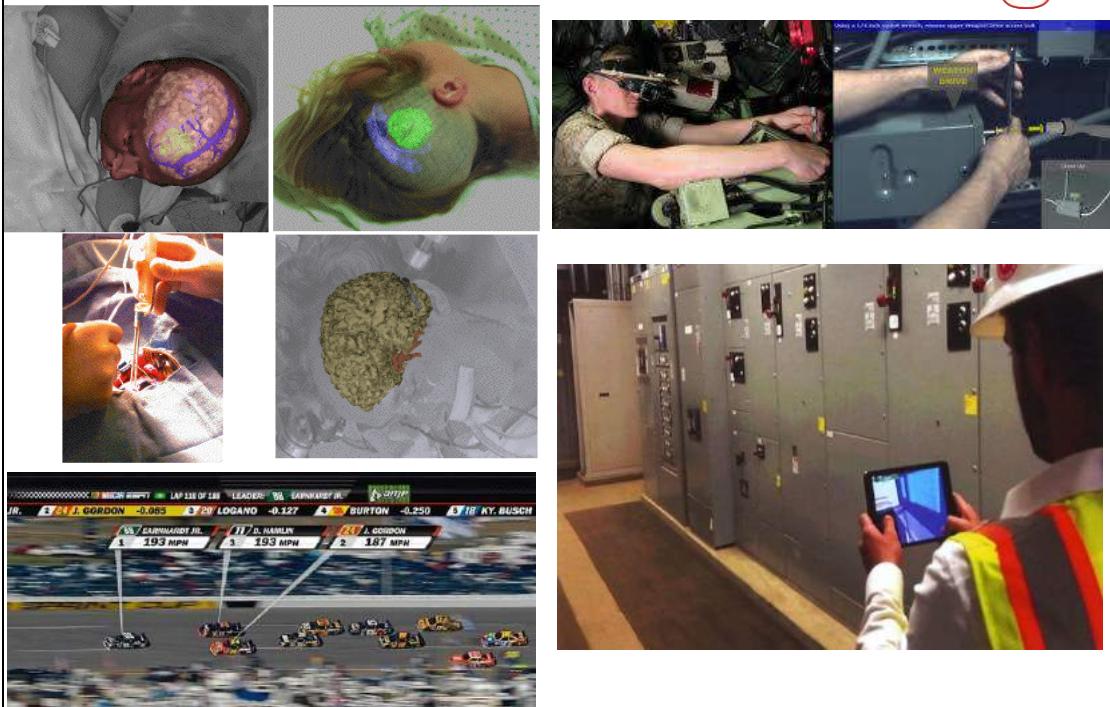
Real-Time (interakt) Vizuelizacija



The top section shows a 3D medical visualization of a human torso with internal organs, possibly a heart or blood vessels, highlighted in red. Next is a 3D simulation of a surface with orange arrows indicating flow or velocity. The bottom section features a complex network graph with many nodes and connections, and a 3D surface plot titled "Z, Signal" showing frequency and signal strength across a grid.

Real-Time (interaktivna) grafika Virtuelna/augmentovana stvarnost

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Real-Time (interaktivna) grafika HCI i novi infomacioni prostori

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Real-Time (interaktivna) grafika

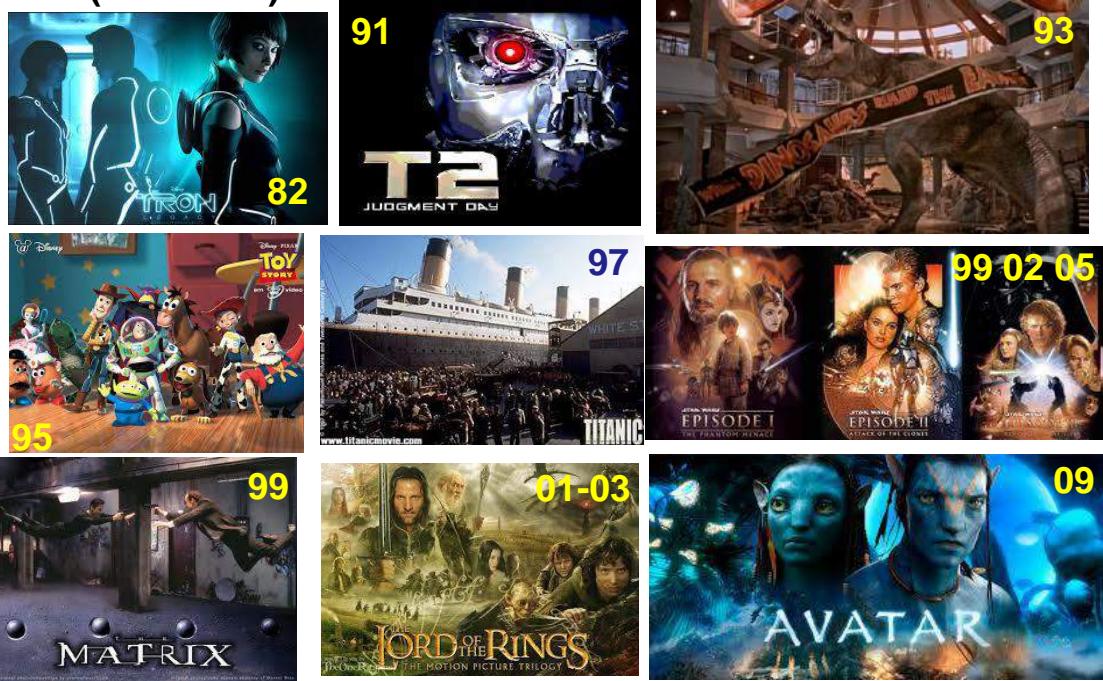
Računarske igre



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Non-Real-Time grafika

Film (umetnost)



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Non-Real-Time grafika

Film

 Shrek(01 04 07 10)	 Up (2009)	 Finding Nemo (2003)
 Monster Inc. (01 13)	 IceAge (06 09 12)	 Ratatouille (2007)
 Kung fu panda(08 11)	 Madagascar 05 08 12	 Despicable Me (10 13)
	 Brave (2012)	 Advent. of Tintin (2011)

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Non-Real-Time grafika

Film



Non-Real-Time grafika

Film

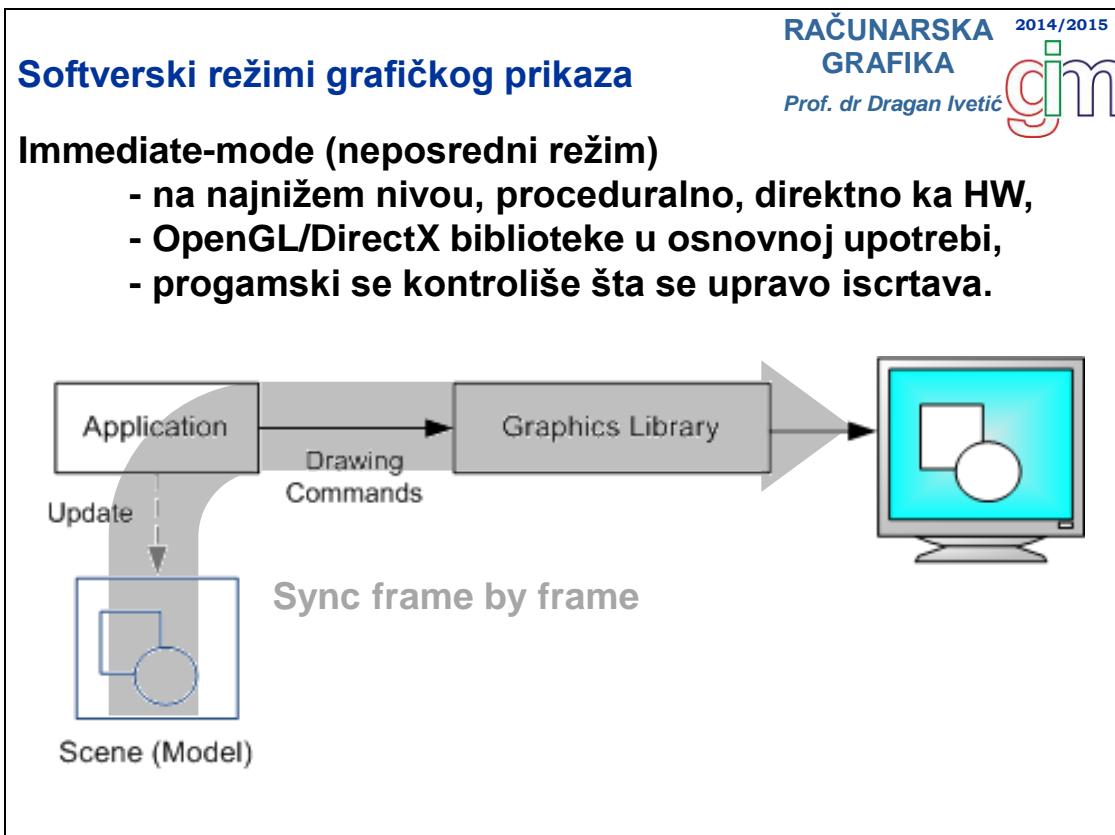


Non-Real-Time grafika

Film



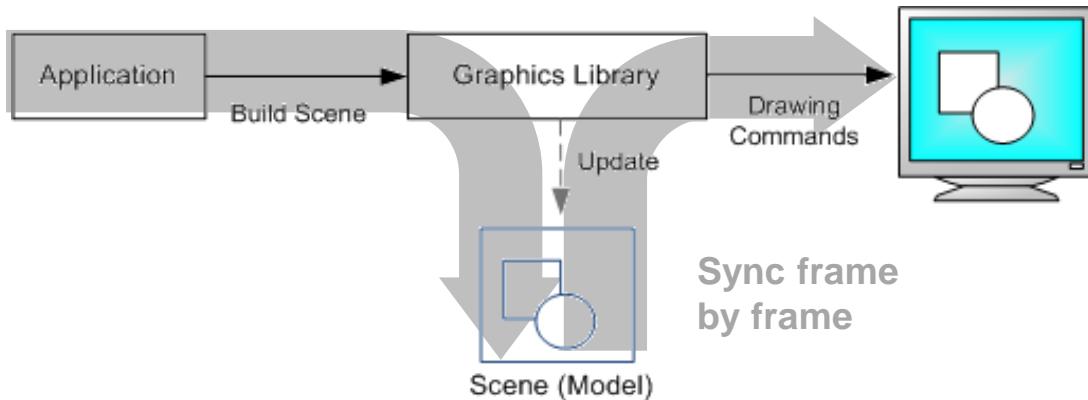
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Softverski režimi grafičkog prikaza

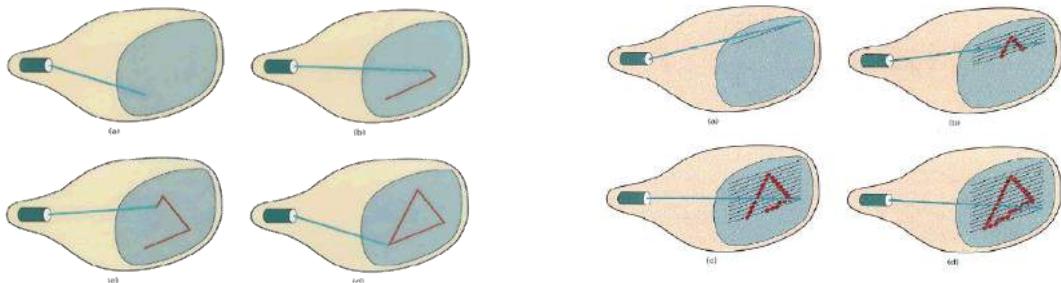
Retained-mode (posredni režim)

- na višem nivou, deklarativno,
- OpenGL/WPF(DirectX) biblioteke,
- briga programera samo pri promeni scene.



Ko je brži? Ko je manje komunikaciono zahtevan?

VEKTOR I/ILI TAČKA (raster) ...



a može biti sprovedeno na nivou:

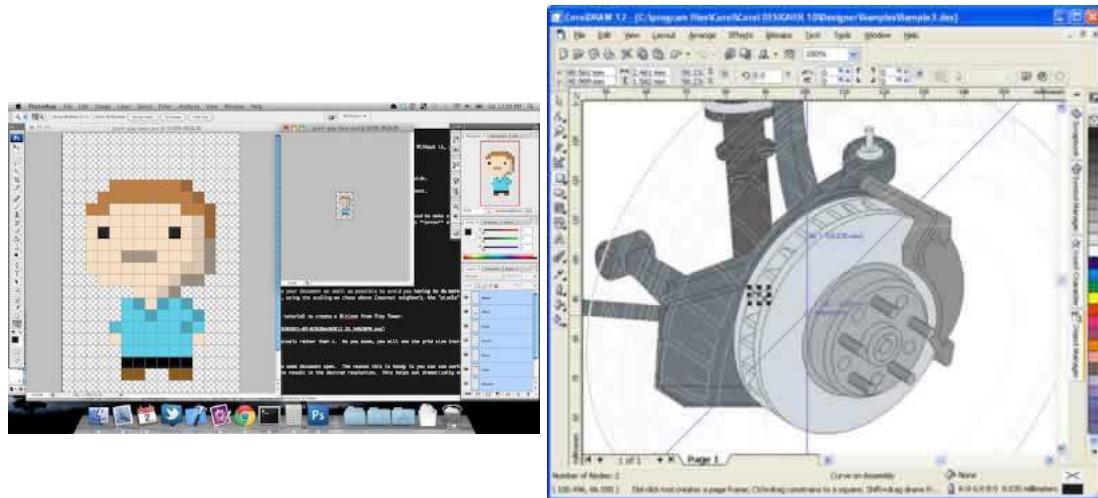
Softvera (logika) - i to na podnivou
instrukcije/komande, ili
podataka.

Hardvera (fizika).

... VEKTOR I/ILI TAČKA (raster) ...



Instrukciono logički (SW) – da li korisnik formira grafički prikaz angažujući komande nad tačkom (PhotoShop) ili vektorom (CorelDraw).



... VEKTOR I/ILI TAČKA (raster) ...



Data logic (File) – da li se komponovani grafički sadržaj trajno čuva kao skup tačaka (bmp, tiff, jpeg, raw, png, ...) ili vektora (cdr, svg, ai, ...).

Šta je sa *.wmf?

Koji fajl ide sa kojim SW?

Razmena?

8 level gray



```
22222222222222222222  
22222200000022222222  
22220055555500222222  
222055555555555502222  
2205555555555555502222  
22055555555555555502222  
220550555555555502222  
22055055555505502222  
22055005555505502222  
22005500000055022222  
222055555555555502222  
2220555555555555502222  
22220055555500222222  
22222200000022222222  
2222222222222222222222
```

```
<?xml version="1.0" standalone="no"?>  
<!DOCTYPE svg PUBLIC "-//W3C//DTD  
SVG 1.1//EN"  
"http://www.w3.org/Graphics/SVG/1.1/DTD/svg11.dtd">  
  
<svg  
xmlns="http://www.w3.org/2000/svg"  
version="1.1">  
  
 <circle cx="100" cy="50" r="40"  
stroke="black" stroke-width="2"  
fill="red" />  
  
</svg>
```

... VEKTOR I/ILI TAČKA (raster)

Fizički (HW) – kako se komponovani grafički sadržaj priprema za prikaz na ekranu prikaznog uređaja, kao skup vektora (vector HW) tačaka (raster HW).

Vektorski HW,

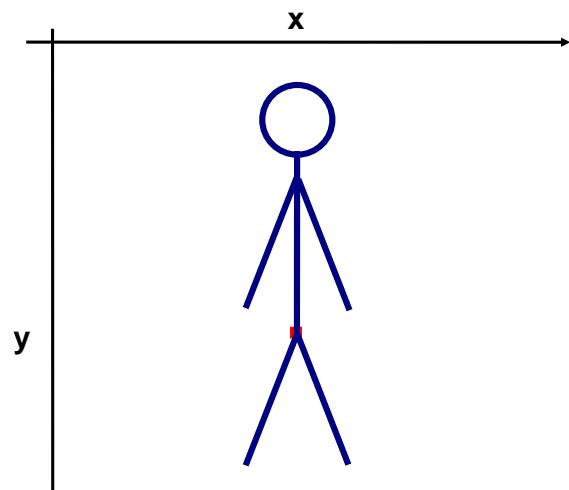
Rasterski HW se realizuje:

- bez GPU (deljena ili izolovana memorija),
- sa GPU (deljena ili izolovana memorija).

Koji format fajla je nativan za koji HW?

Komponovanje grafičkog prikaza

Dizajniramo



Programiramo

```
CrtajLiniju2D(x,y,x,y-24)
CrtajLiniju2D(x,y,x-6,y+17)
CrtajLiniju2D(x,y,x+6,y+17)
CrtajLiniju2D(x,y-20,x-6,y-7)
CrtajLiniju2D(x,y-20,x+6,y-7)

CrtajKrug2D(x,y-29,5)
```

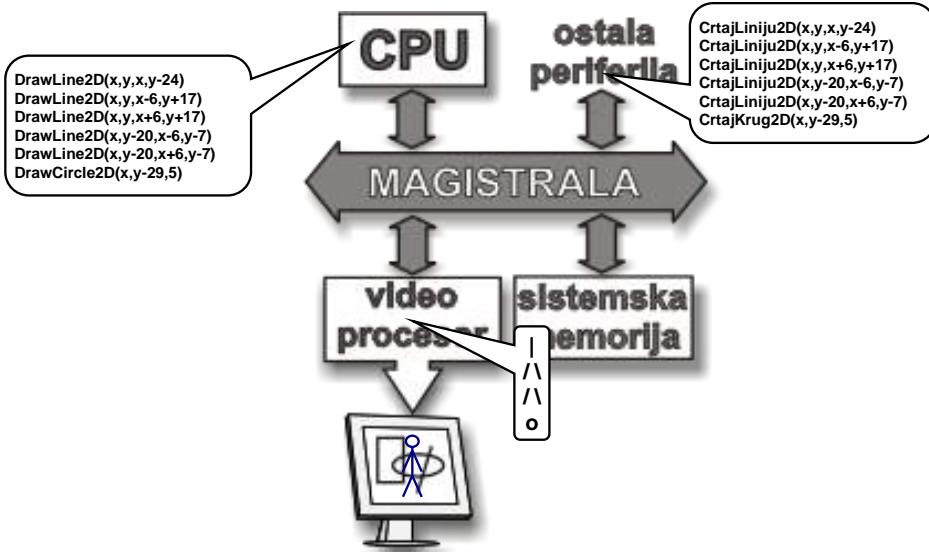
Tok aktivnosti prikaza na vektorskem HW

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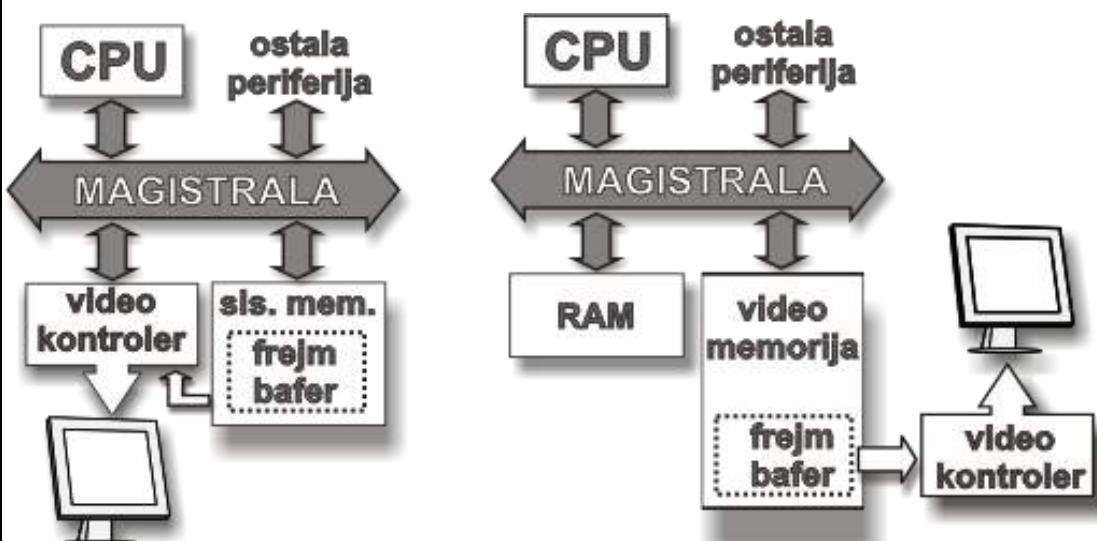
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HW arhitektura rasterskog HW bez GPU

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- Arhitektura sa deljenom memorijom.
 - Arhitektura sa izolovanom memorijom.

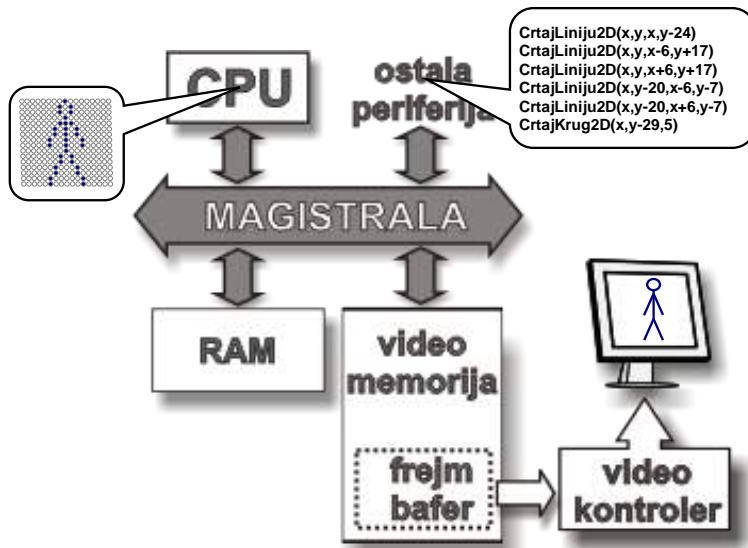
Tok aktivnosti prikaza na rasterkom HW bez GPU

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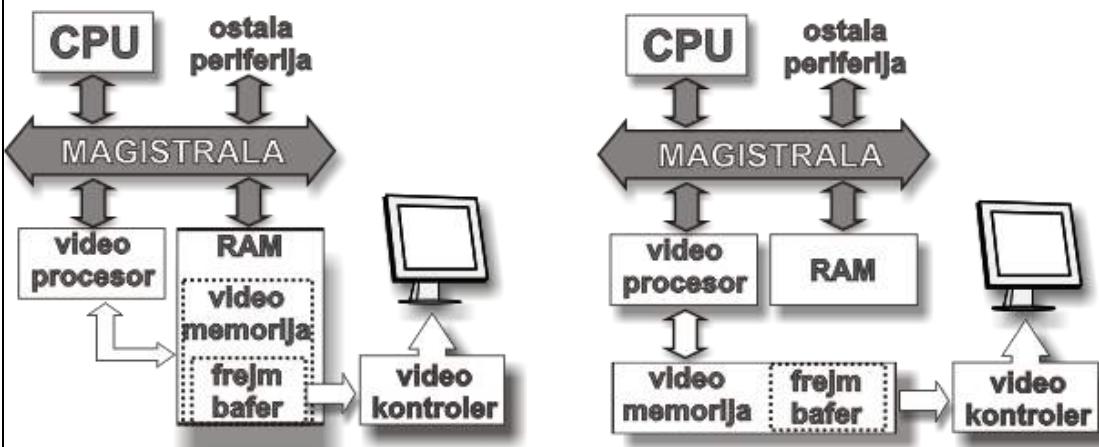
HW arhitektura rasterskog HW sa GPU

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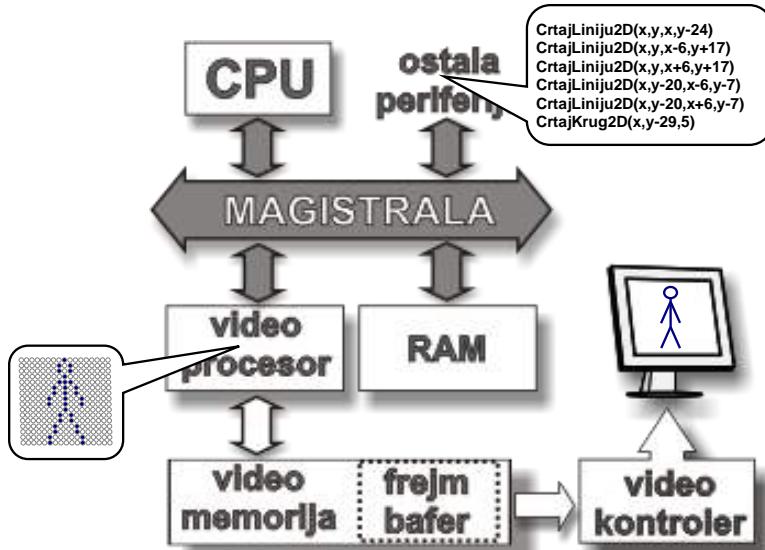
2013/2014



- Arhitektura sa deljenom memorijom.
 - Arhitektura sa izolovanom memorijom.

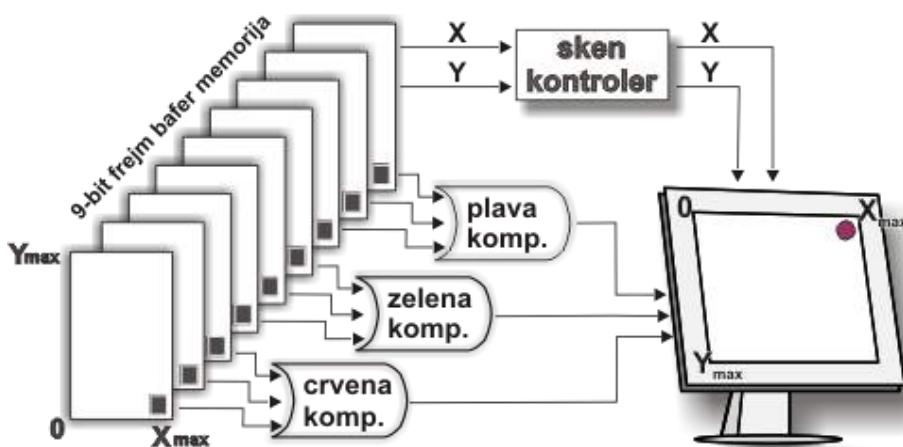
Tok aktivnosti prikaza na rasterskom HW sa GPU

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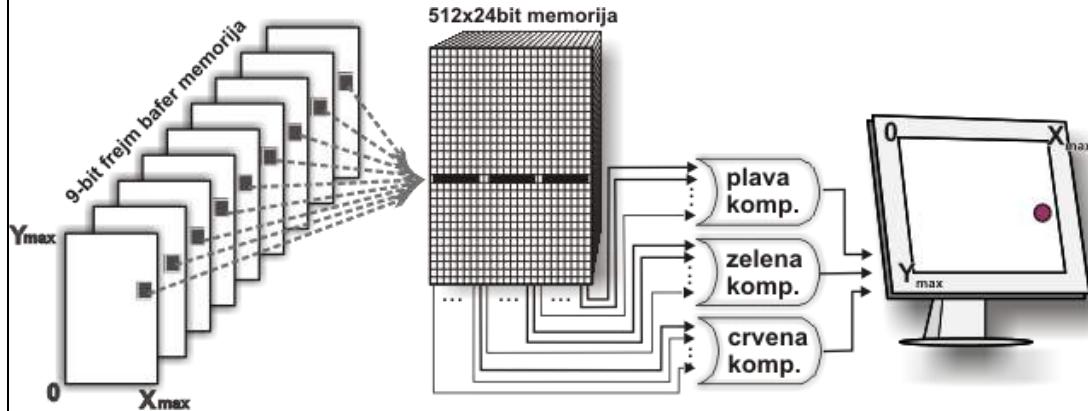
Video kontroler klasične arhitekture

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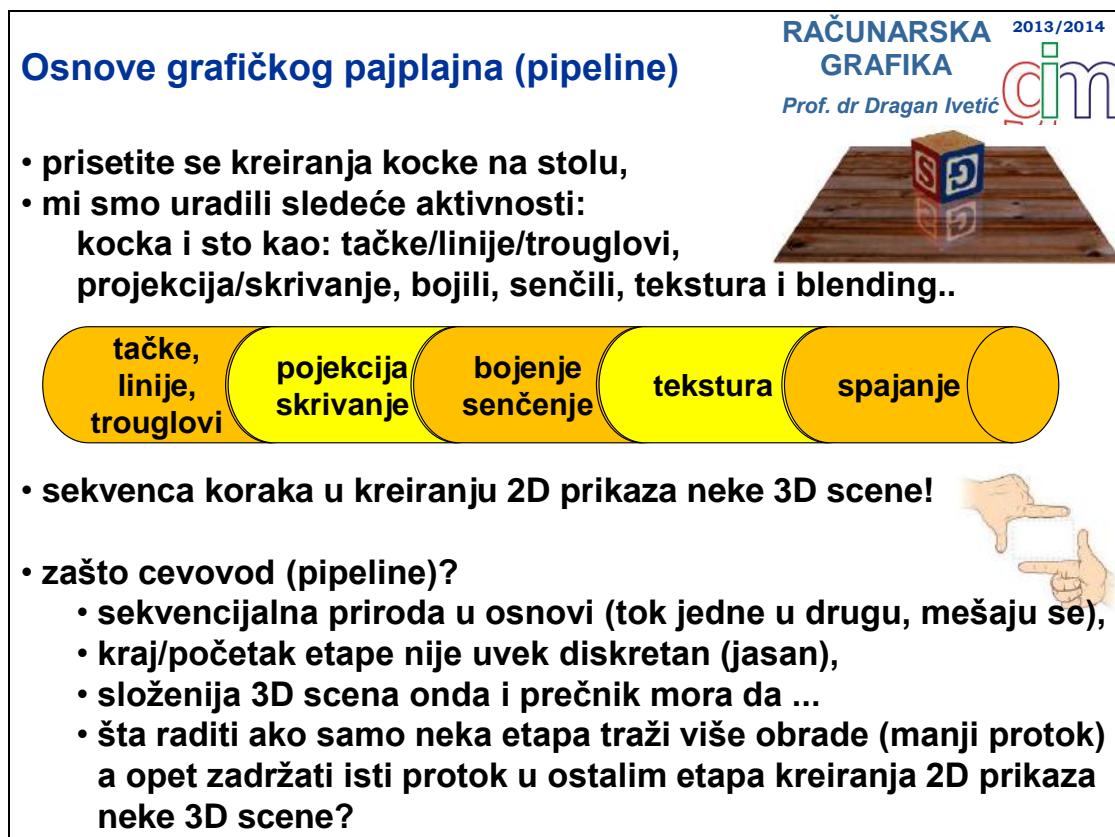
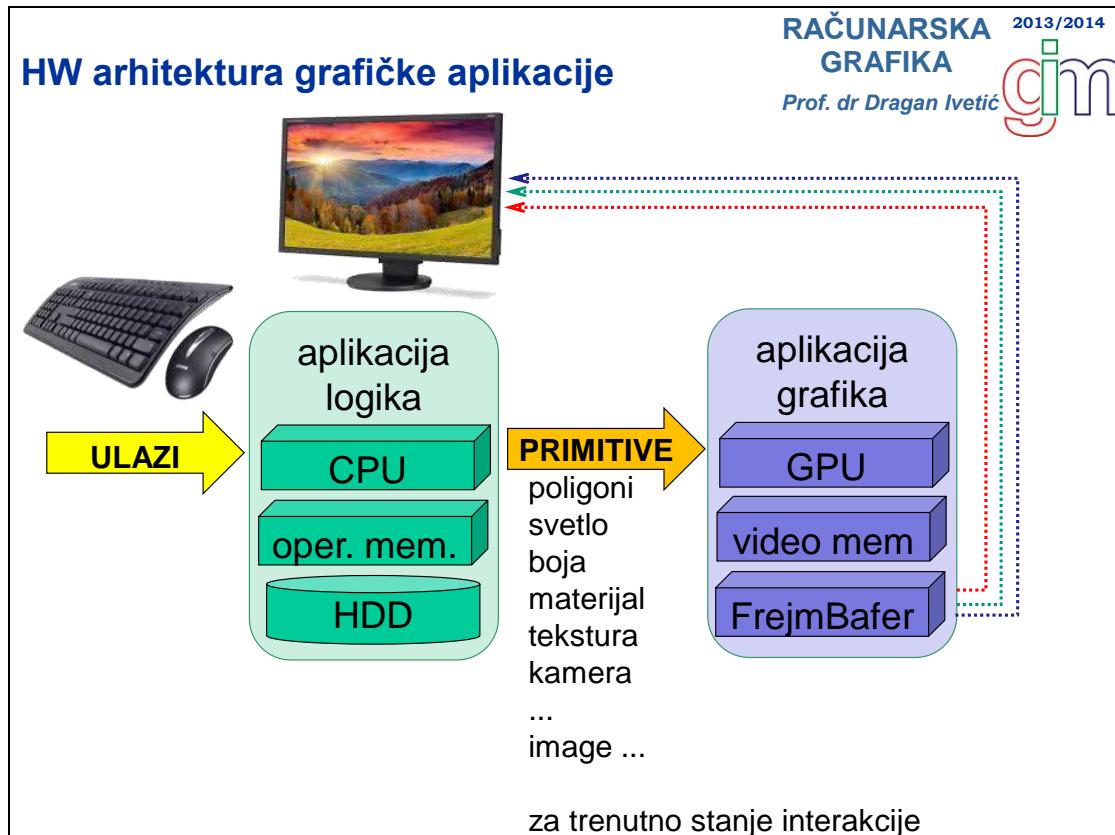



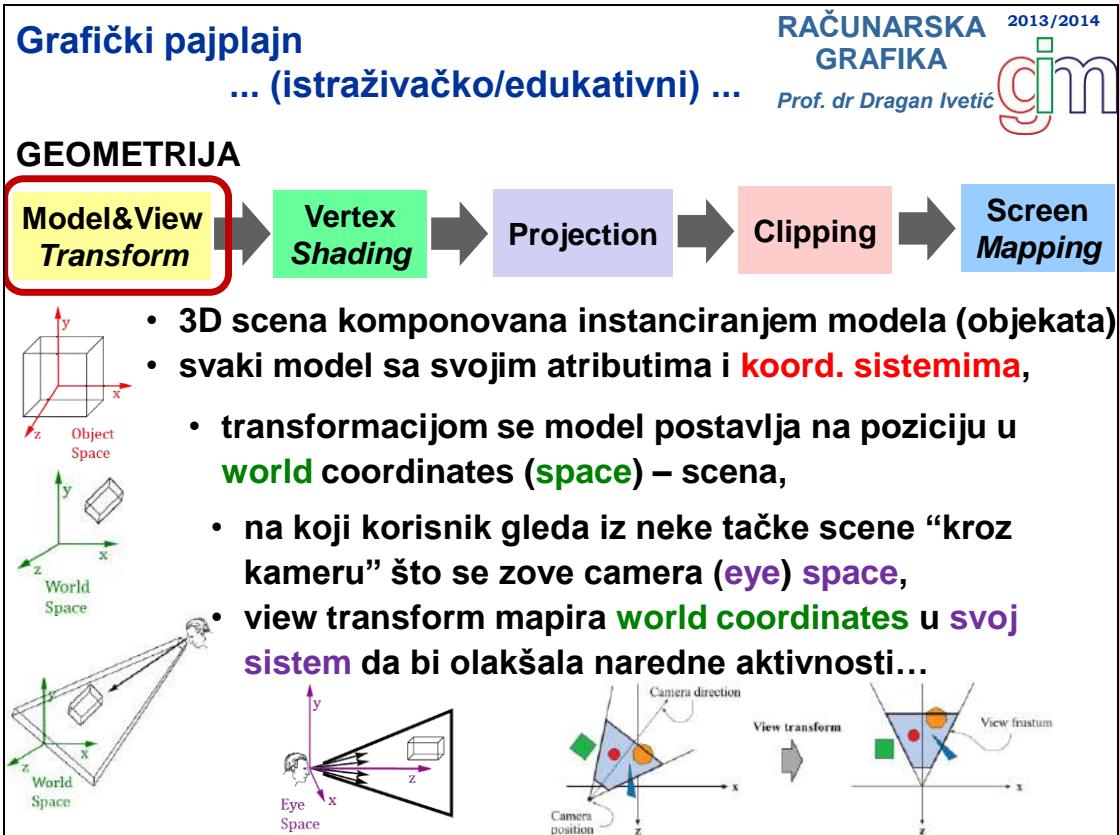
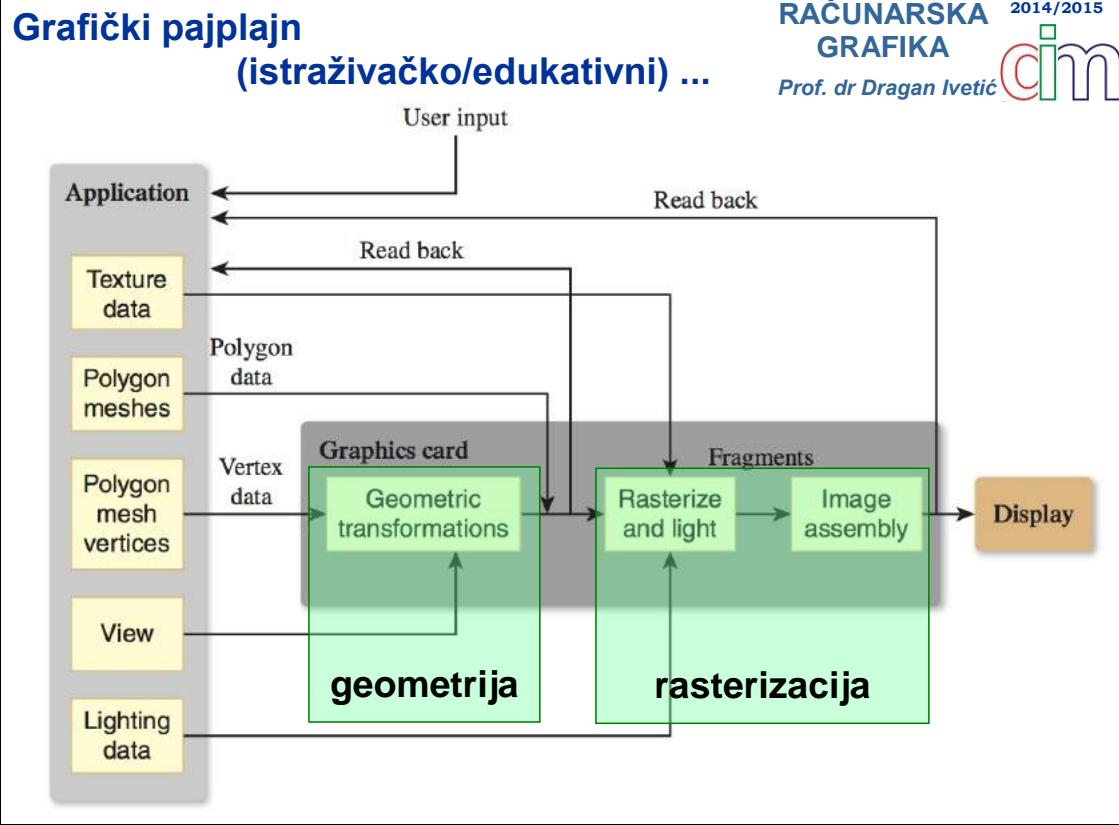
- za prikaz od **1024x1280** piksela i sa true-colour sistemom, **2²⁴** boja,
- veličina frejm bafra: **1.310.720 x 3** bajta = **3,75 Mbajta**.

Video kontroler LookUpTable arhitekture



- LUT – progr. sadržaj, 512 paleta od mogućih 2^{24} boja,
- Kolika je razlika u angažovanoj memoriji za prikaz od 1024×1280 piksela i sa 2^{24} boja, sa i bez LUT tabele?
- Koja arhitektura kontrolera je bolja? Zašto?
- Koji format grafičkog fajla odgovara ovom kontroleru?





Grafički pajplajn

... (istraživačko/edukativni) ...

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GEOMETRIJA

Model&View
Transform

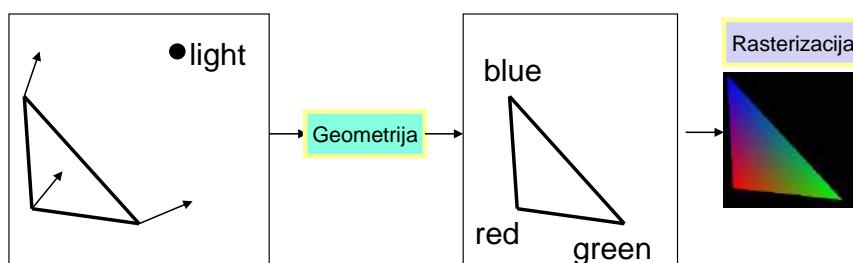
Vertex
Shading

Projection

Clipping

Screen
Mapping

- pored samog oblika objekata, prikazati materijal objekta i kontekst sredine gde se objekt nalazi – shading,
- određivanje svetlosne jednačine na nivou temena spremajući za rasterizaciju i pixel shading...
- nemoguće kreirati ili ukloniti teme, ali može podatke koji su pridruženi temenu,



Grafički pajplajn

... (istraživačko/edukativni) ...

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GEOMETRIJA

Model&View
Transform

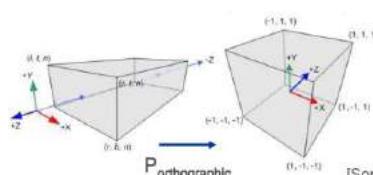
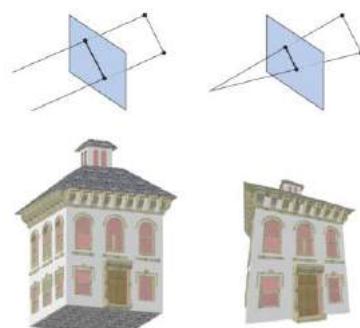
Vertex
Shading

Projection

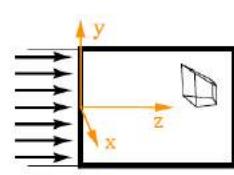
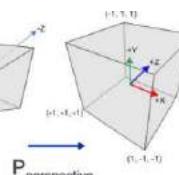
Clipping

Screen
Mapping

- paralelna ili perspektivna projekcija na view volume (unit cube),
- često je “uparalelizovana” sa narednom fazom,
- model je sada definisan u normalized device coordinates – **image space**,



[Song Ho Ahn]



Grafički pajplajn

... (istraživačko/edukativni) ...

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GEOMETRIJA

Model&View
Transform

Vertex
Shading

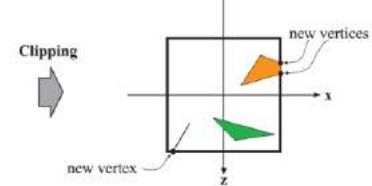
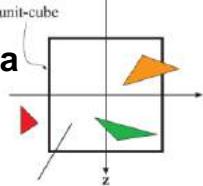
Projection

Clipping

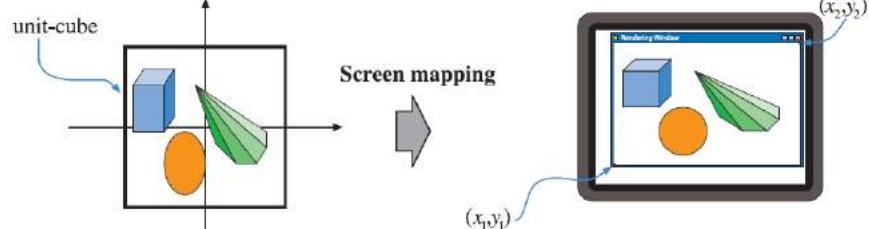
Screen
Mapping

- veličina 3D scene postaje invarijantna na mogućnosti prikaza,

- u unit cube stoje zahvaćena temena i novonastala temena koja su nastala isecanjem primitiva.



- x i y koordinate temena u/na unit cube, preslikavaju se u koordinate ekrana (int tip), a z se prosleđuje kao (0 ... 1).



Grafički pajplajn

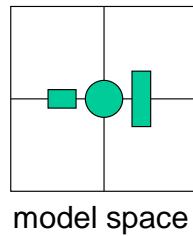
... (istraživačko/edukativni) ...

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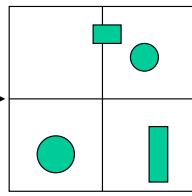
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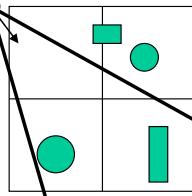
GEOMETRIJA ilustrativno kako to vidi Tomas Akenine-Möller



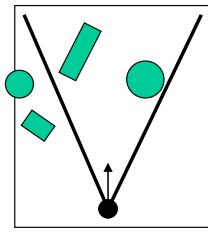
model space



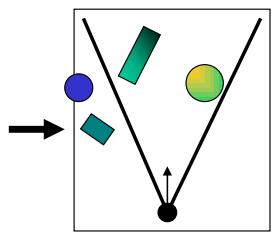
world space



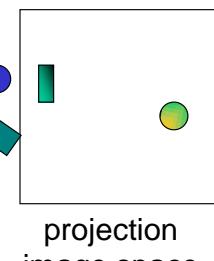
world space



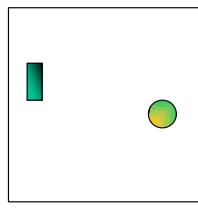
camera space



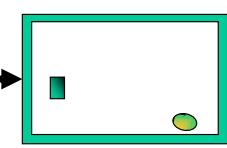
compute lighting



projection
image space



clip



map to screen

Grafički pajplajn

... (istraživačko/edukativni) ...

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RASTERIZACIJA (ili scan conversion) da 2D temena (sa pridruž. z vrednošću i različitim shading info) u piksele na ekranu,

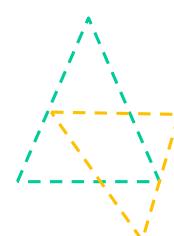
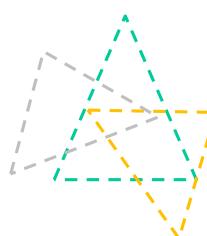
Triangle
Setup

Triangle
Traversal

Pixel
Shading

Merging

- sračunava (diferencijale ivica trouglova) podatke interesantne za određivanje površine u narednim fazama (pre svega scan conversion), obavlja fiksirano-operacioni hw moduli GPU,
- potom “backface culling” pa trouglovi koji nisu uništeni idu u narednu fazu - triangle traversal



Grafički pajplajn

... (istraživačko/edukativni) ...

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RASTERIZACIJA

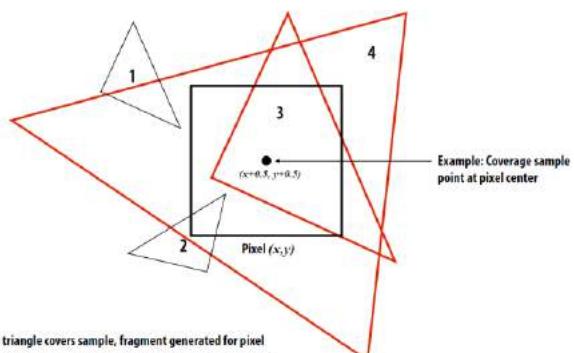
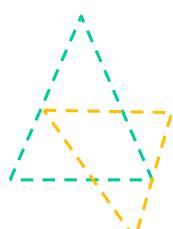
Triangle
Setup

Triangle
Traversal

Pixel
Shading

Merging

- ili scan conversion - formira fragmente (set of samples/pixels) od kojih se sastoji površina trougla,
- održava sve ostale podatke o fragmentu iz geometrije (Z, boje...),

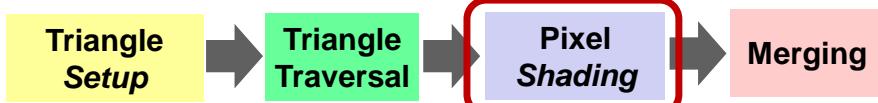


▲ = triangle covers sample, fragment generated for pixel
▼ = triangle does not cover sample, no fragment generated

Grafički pajplajn

... (istraživačko/edukativni) ...

RASTERIZACIJA



- sračunava konačnu boju fragmenta zavisno od izvora svetla, boje, materijala...
- izvšava (krajnje programabilna) jezgra GPU,
- komplikovano i zasnovano na mnoštvu ulaznih podataka,
- rezultat je samo vrednost boje,
- osnovne operacije su: texturing i per pixel lighting.



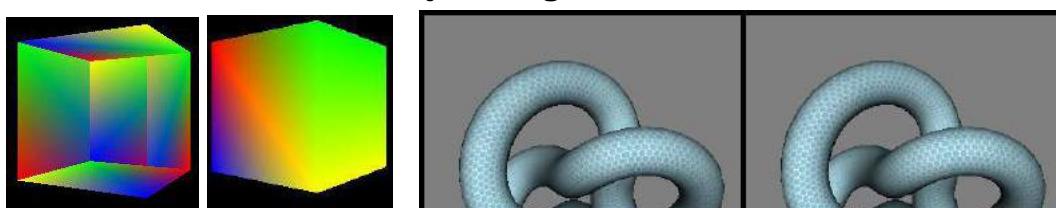
Grafički pajplajn

... (istraživačko/edukativni)

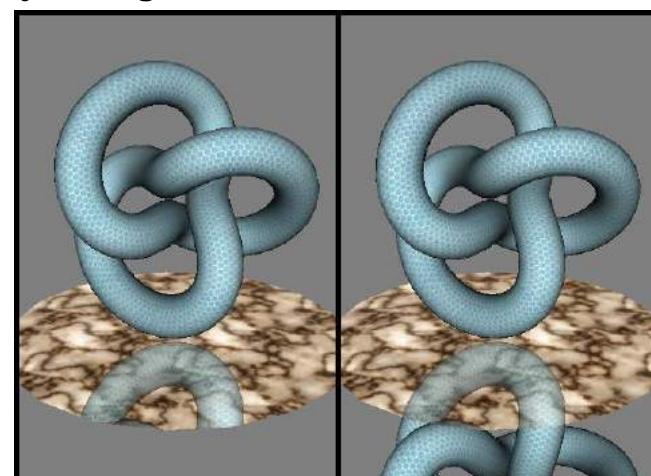
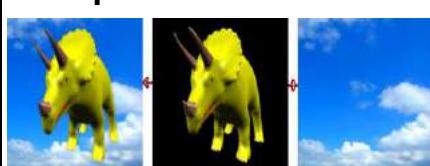
RASTERIZACIJA



- konačno uređuje frejm bafer za prikaz kombinujući (blending) osnovni kolor bafer sa bojom fragmenta i Z baferom,



- ali i sa stencil baferom,
- i alpha baferom.

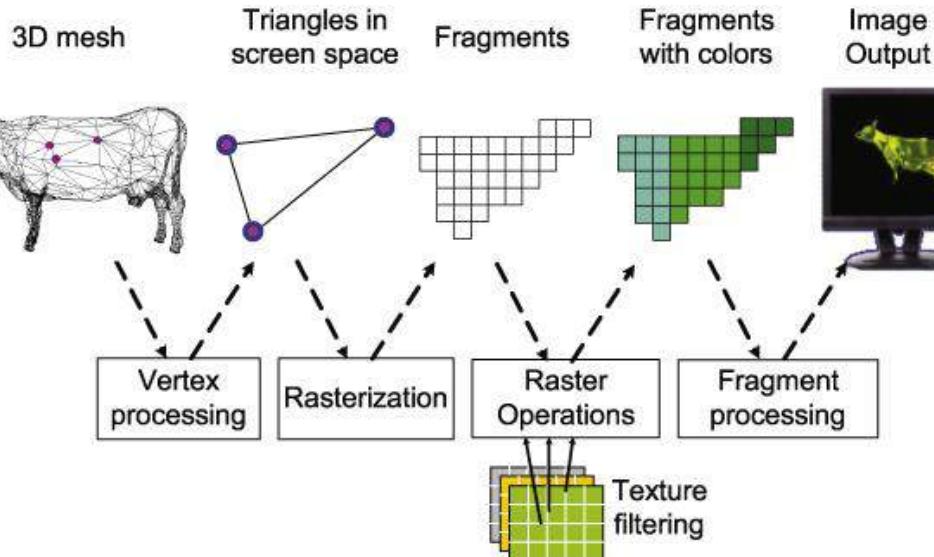


Grafički pajplajn

... u praksi ...

RAČUNARSKA
GRAFIKA 2013/2014
Prof. dr Dragan Ivetić 

Slikoviti pajplajn



Grafički pajplajn

... u praksi ...

RAČUNARSKA 2014/2015
GRAFIKA
Prof. dr Dragan Ivetić 

Ko izvršava aktivnosti grafičkog i rasterskog dela pajplajna?

Do 1995. godine –

CPU softversko renderovanje grafike
(prvo 2D, pa i 3D do 1995.),



Doom

1996. godine

prvi GPU automatizuje najjednostavnije
procese pajplajna:
mapiranje tekture i Z-bafer



Quake

(3dfx Voodoo 1996.),

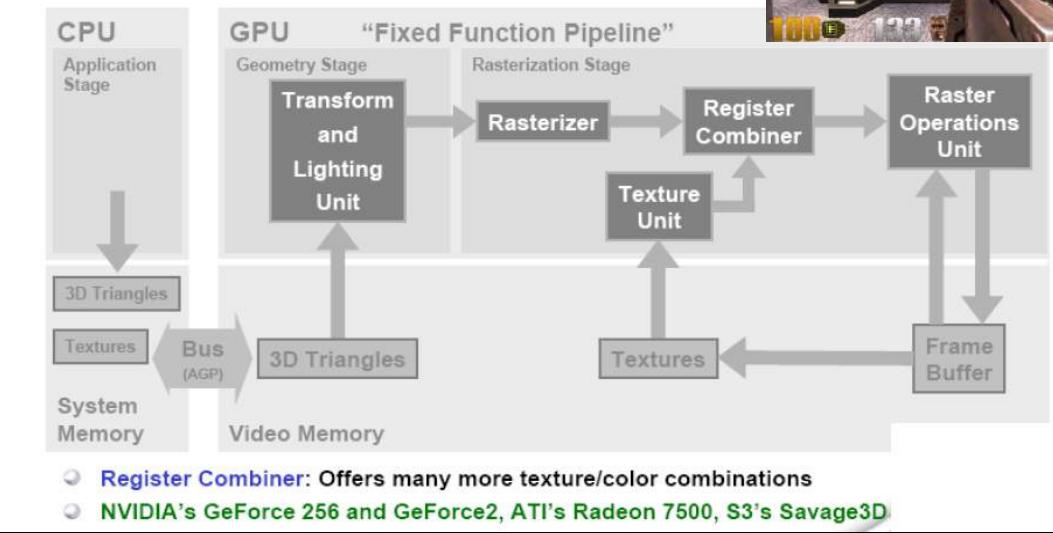
Grafički pajplajn



... u praksi ...

1998. Godine

GPU fiksne funkcije – obezbeđuje sve aktivnosti pajplajna kroz parametrizovane pozive



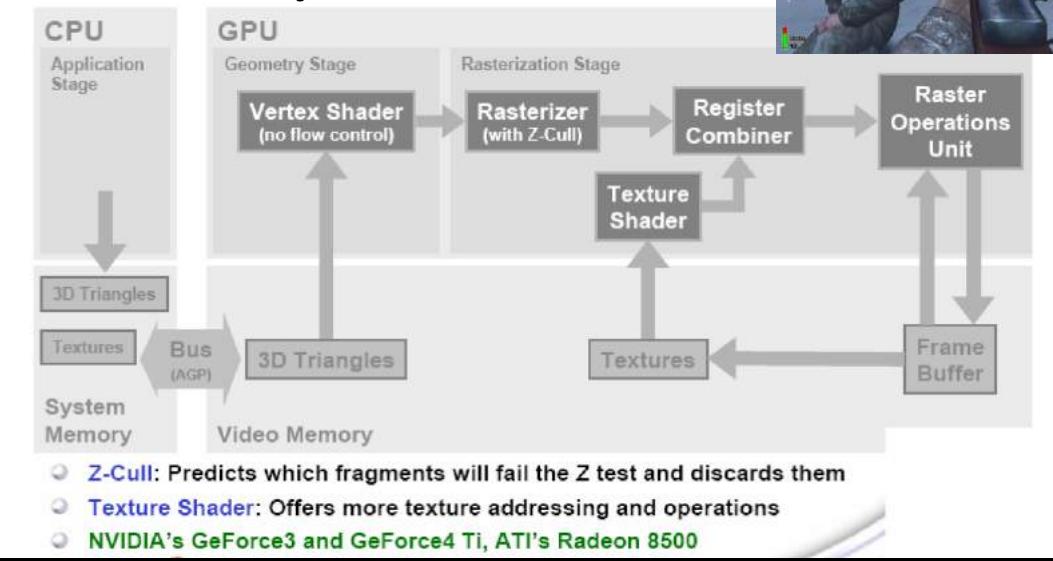
Grafički pajplajn



... u praksi ...

Od 2001. – 2002. godine

GPU program. funkcije statičnog toka – obezbeđuje izvršavanje programskog koda verteks šejdera,

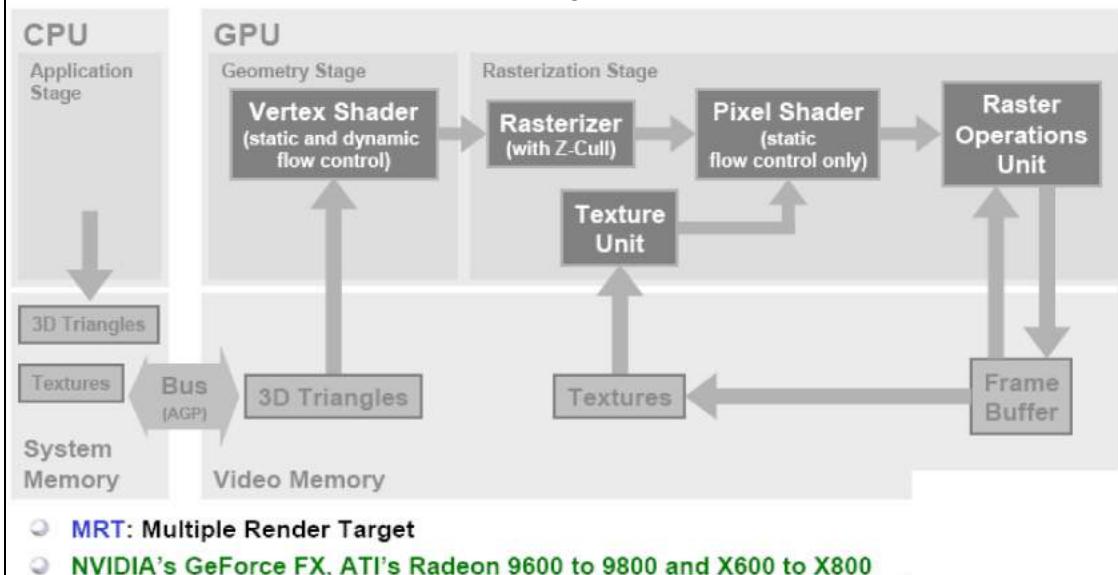


Grafički pajplajn

... u praksi ...

Od 2003. – 2004. godine

**GPU program. funkcije dinamičkog toka
verteks i piksel (statički) šejderi**

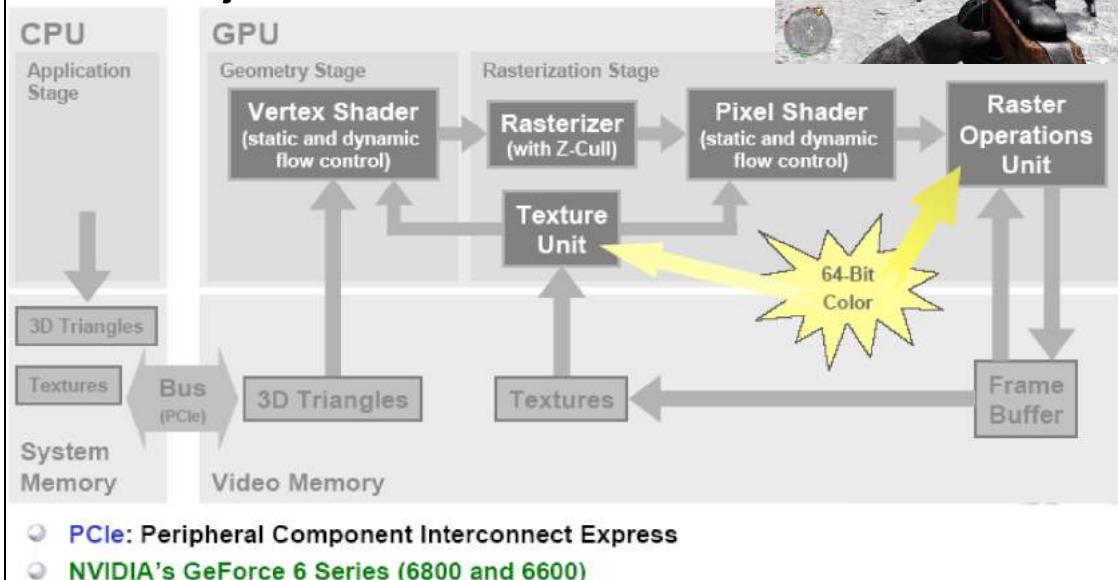


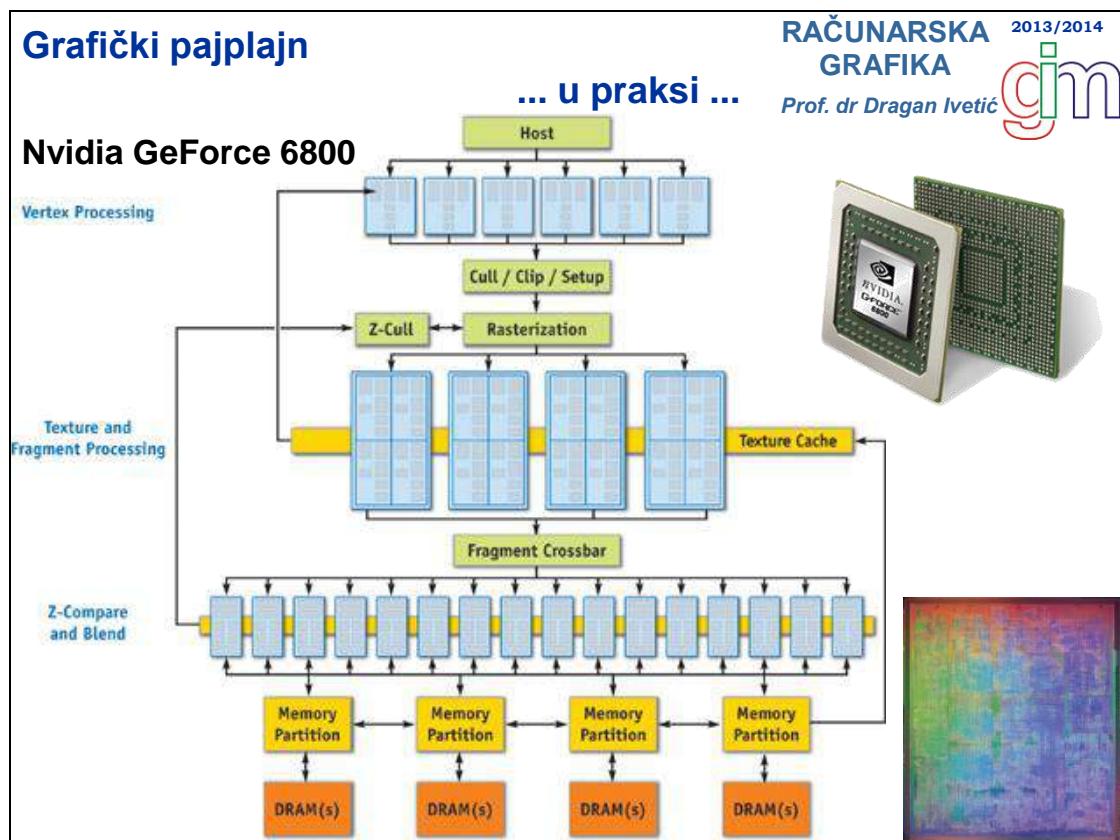
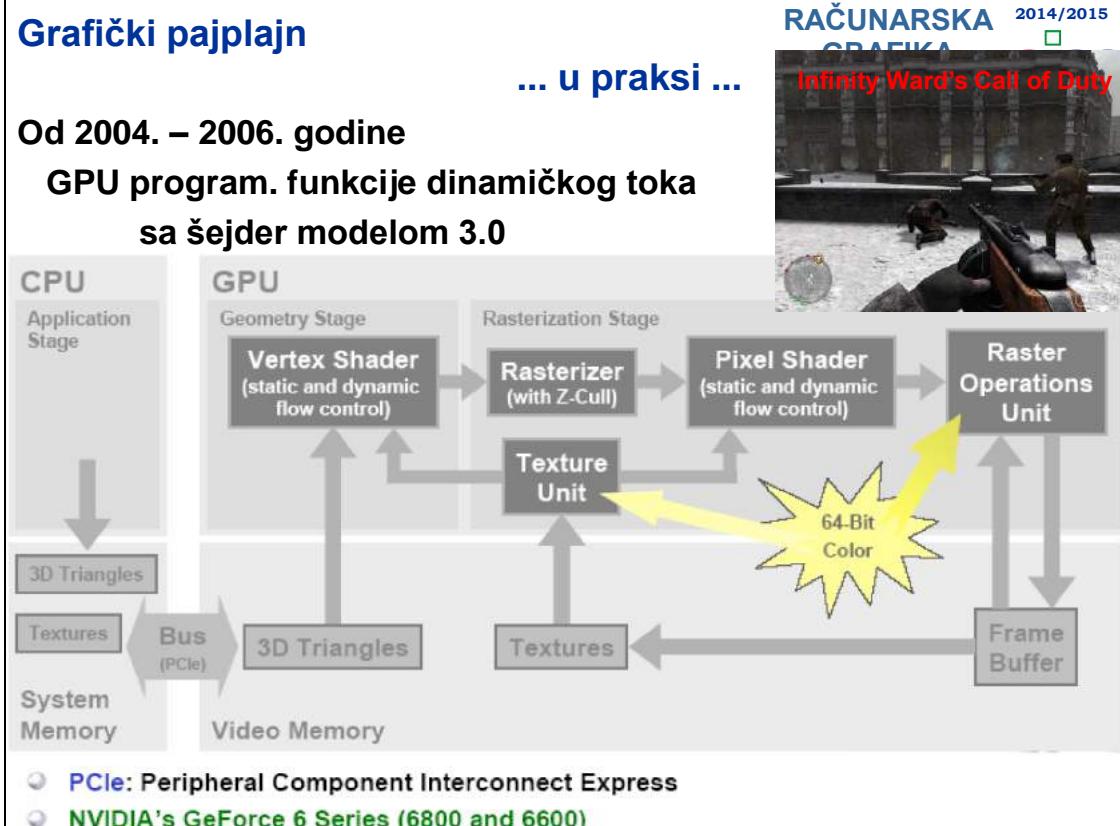
Grafički pajplajn

... u praksi ...

Od 2004. – 2006. godine

**GPU program. funkcije dinamičkog toka
sa šejder modelom 3.0**





Grafički pajplajn

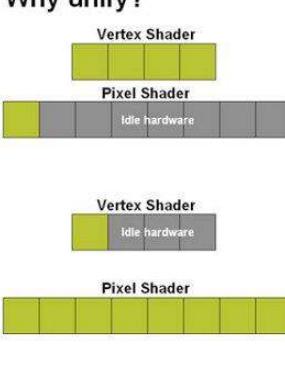
... u praksi ...

RAČUNARSKA GRAFIKA 2014/2015
Prof. dr Dragan Ivetić 

Od 2006. godine

GPU programabilne funkcije unificirani šejderi različitih vrsta (GeForce 8).

Why unify?



Separate Shaders	Unified Shader
Vertex Shader	Vertex Workload
Pixel Shader	Pixel Workload
Idle hardware	VerTEX

Heavy Geometry
Workload Perf = 4



Heavy Pixel
Workload Perf = 8

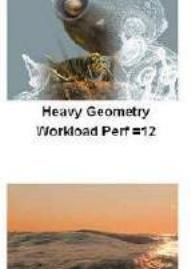


Why unify?



Separate Shaders	Unified Shader
Heavy Geometry	Heavy Geometry
Workload Perf = 12	Workload Perf = 12

Heavy Pixel
Workload Perf = 12

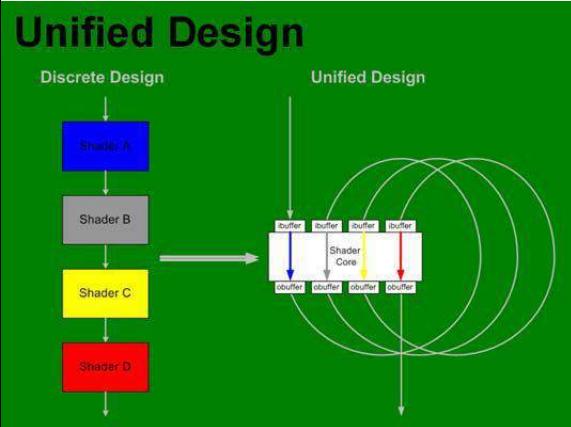


Grafički pajplajn

... u praksi ...

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Unified Design



Discrete Design: Shows four separate shaders (A, B, C, D) each with its own dedicated memory buffers.

Unified Design: Shows a central Shader Core sharing multiple memory buffers (labeled 'b'uf'fers) with other components.

Memory Resources (dashed box):

- Constant Buffers
- Textures
- Buffers

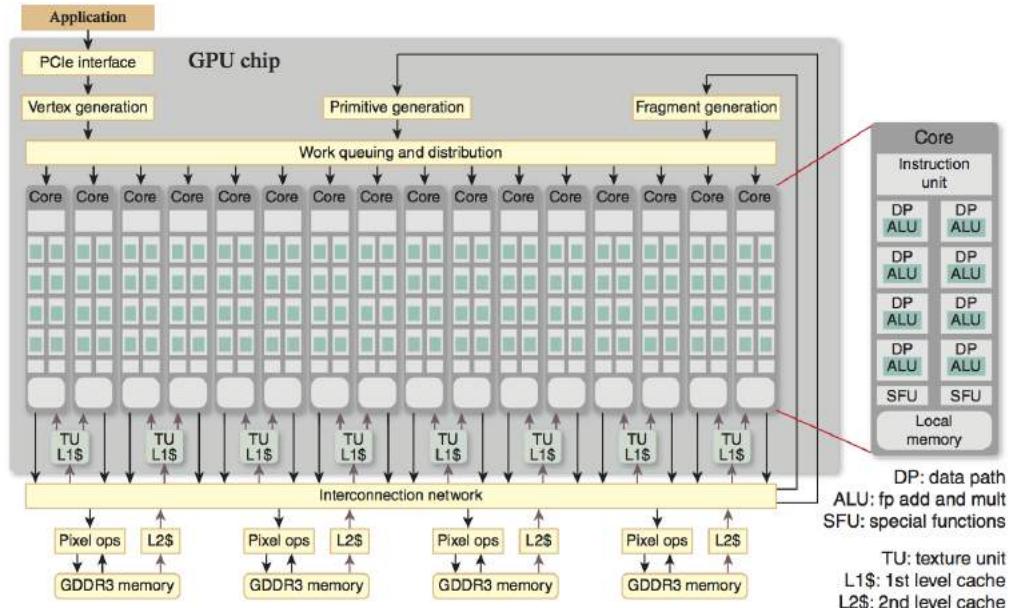
The flow of data is as follows:

- Input Data enters the Shader Code.
- Shader Code outputs Output Data.
- Output Data is processed by Samplers.
- Samplers output to Textures.
- Textures output to Constant Buffers.
- Constant Buffers output to the Shader Code.

Grafički pajplajn

... u praksi ...

GeForce 9800 GTX, 16 jezgara (stream multiprocessors), 8 sp + sfu



Nvidia GTX280, 24 jezgara (8 unified stream proces.)

Grafički pajplajn

... u praksi ...

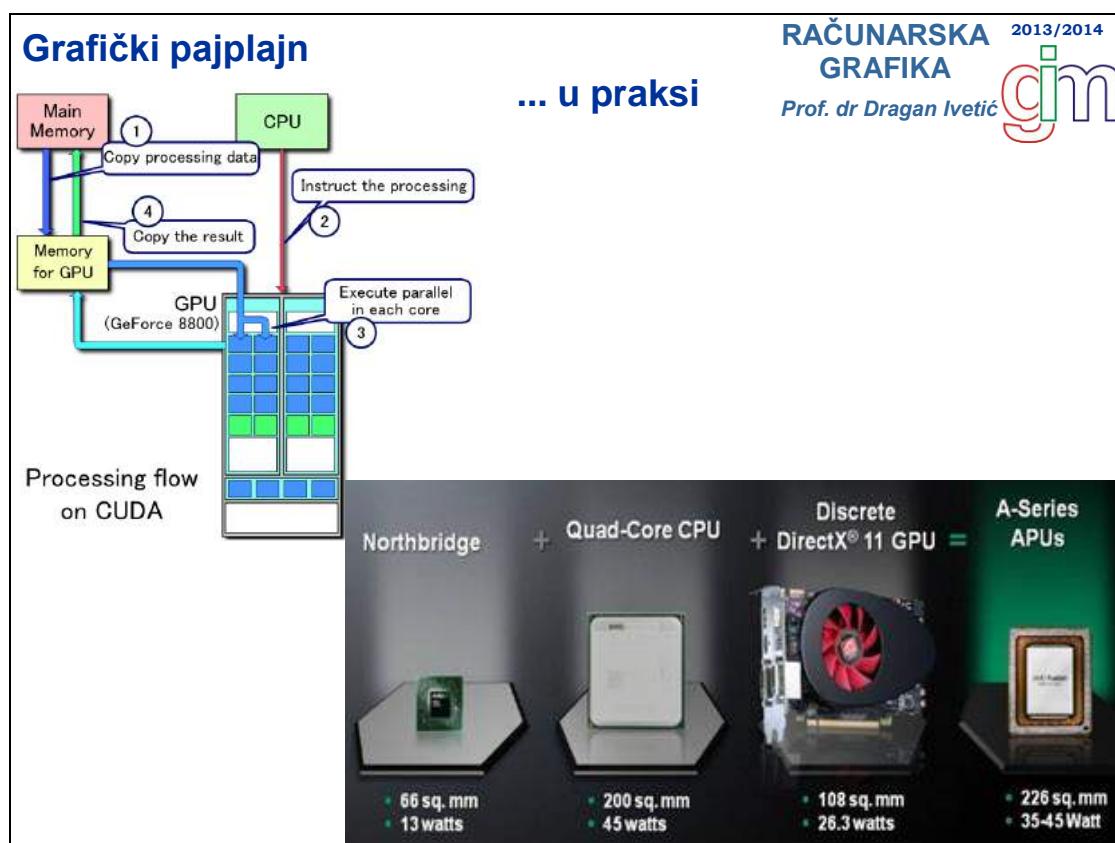
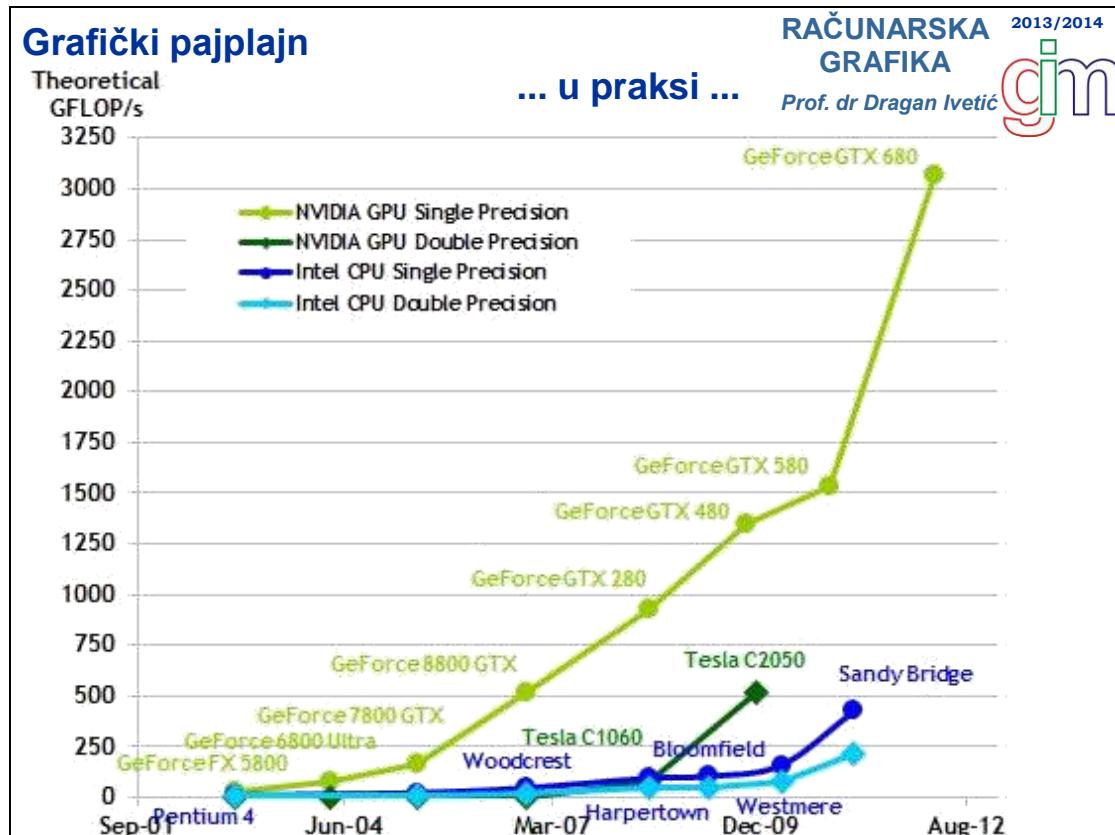
2010./2011. CRYTEK's Cryengine3.



NVIDIA Geforce GTX580

Interface: PCIe 2.0 x16
Shader Model: 5.0
DirectX: 11
Manufacturing Process: 40 nanomet
Core Clockspeed: 770MHz
Memory Amount: 1536MB
Memory Clockspeed: 2004MHz
Memory Bus: 384-bit
Transistors: 3 billion

16 stream multiprocessors
32 CUDA procesora (ALU+FPU)
4 SFU)



Programske biblioteke

- softverski interfejs ka grafičkom hardveru (API)
- najviše korišteni su:



- grafička biblioteka raspoloživa za sve SW/HW platforme: od Unix, Sun, HP, Microsoft, Apple, Android do ugradnih sistema,
- poveziv sa svim značajnjim jezicima: Ada, Basic, C#, Fortran, Java, Pascal, Perl, Python, Ruby...
- koristi se za svaki posao gde i računarska grafika...
- Direct3D za podršku grafike unutar DirectX ,
- samo pod Microsoft (Xbox),
- MS COM baziran: Delphi, MS Visual C++, C#, VB .NET (ostali indirektno)...
- uglavnom igrice...
- sw/hw proizvođači prate promene u DirectX dok OpenGL ide posle...

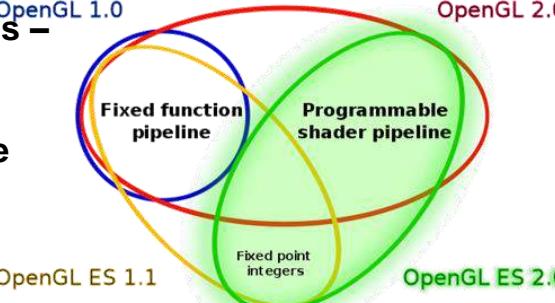
OpenGL ...

- SGI prvo razvio Integrated Raster Imaging System Graphics Library, 2D/3D API za IRIX grafičke stanice 1988. godine,
- IRIS GL nije bio formalno specifikovan i usaglašen, pa 1992. SGI krenuo u definisanje otvorenog standarda (i za druge platforme) OpenGL1.0,
 - ustanovljen OpenGL Architecture Review Board (SGI, DEC, IBM, Intel i Microsoft),
- 1997. donet OpenGL 1.1 koji je uneo pre svega glBindTexture,
- 1998. OpenGL 1.2 uveo rad sa slikama i 3D texture..,
- 2001. OpenGL 1.3 - multiteksture i kompresovane teksture...,
- 2002. OpenGL 1.4 – fog, stencil, window raster position,
- 2003. OpenGL 1.5 – buffer object, occlusion, shadow, MS out!
- 2004. OpenGL 2.0 – osnove verteks šejdera i GLSL jezika,
- 2006. OpenGL 2.1 – piksel bafer i specifikacija GLSL 1.2, pao SGI pa i ARB, preuređen u Khronos grupu,
- 2008 - 3.0, 2009. – 3.1 i 3.2, 2010. – 3.3,
- 2010. – 4.0 i 4.1, 2011. – 4.2, 2012. – 4.3, 2013. – 4.4.

... OpenGL ...

izvedeni standardi:  **1. OpenGL for Embedded Systems –** podskup OpenGL 3D API za ugradne sisteme – mobilni (Android, iOS), PDA, video game konzole...

- pojednostavljeni tipovi i sintaksa – glBegin, glEnd
- dve različite verzije.



2. OpenGL for the Web WebGL

- obezbeđuje GPU podržanu 3D grafiku na web stranici,
- HTML5 canvas element i javascript,
- diskutabilna podržanost od strane web klijenata,
- moguće mesto upada.



... OpenGL ...

Khronos grupa



BOARD OF PROMOTERS

AMD	ARM	EPIC GAMES	K H R O N O S GROUP		freescale	VIVANTE
Apple	SONY		Over 100 members worldwide any company is welcome to join		NOKIA	Imagination
SAMSUNG	intel				QUALCOMM	Texas Instruments



... OpenGL ...

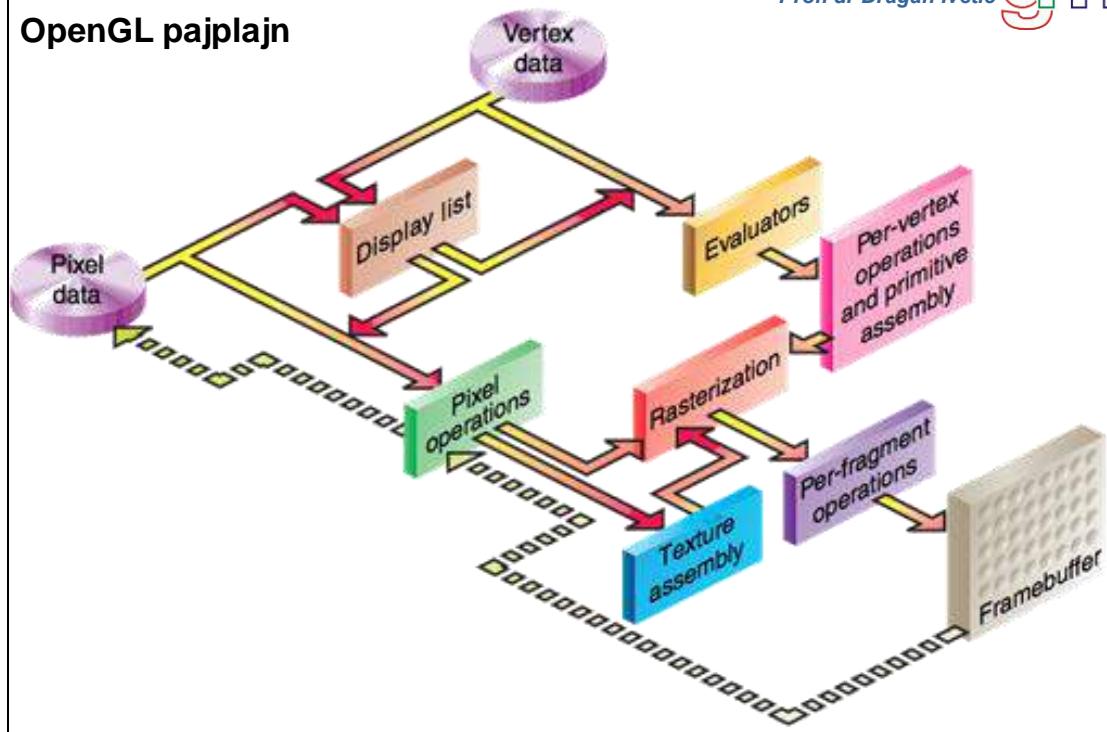
Khronos Visual Computing Ecosystem

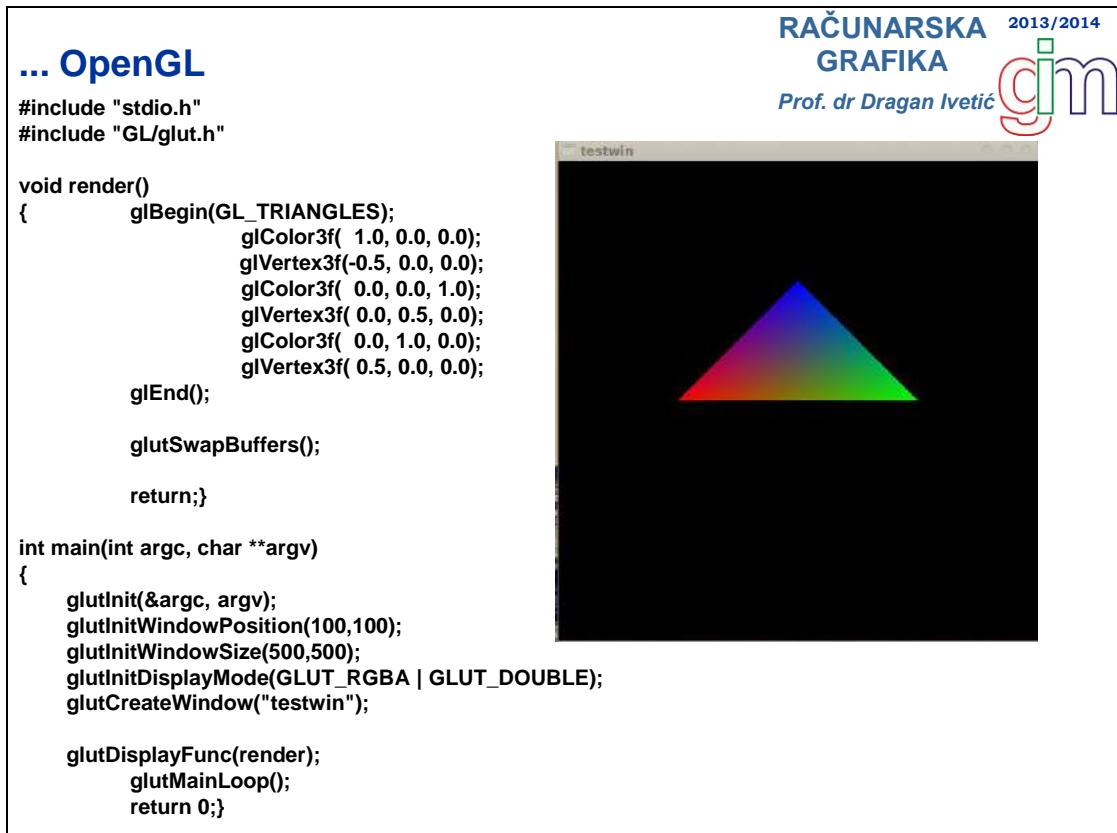
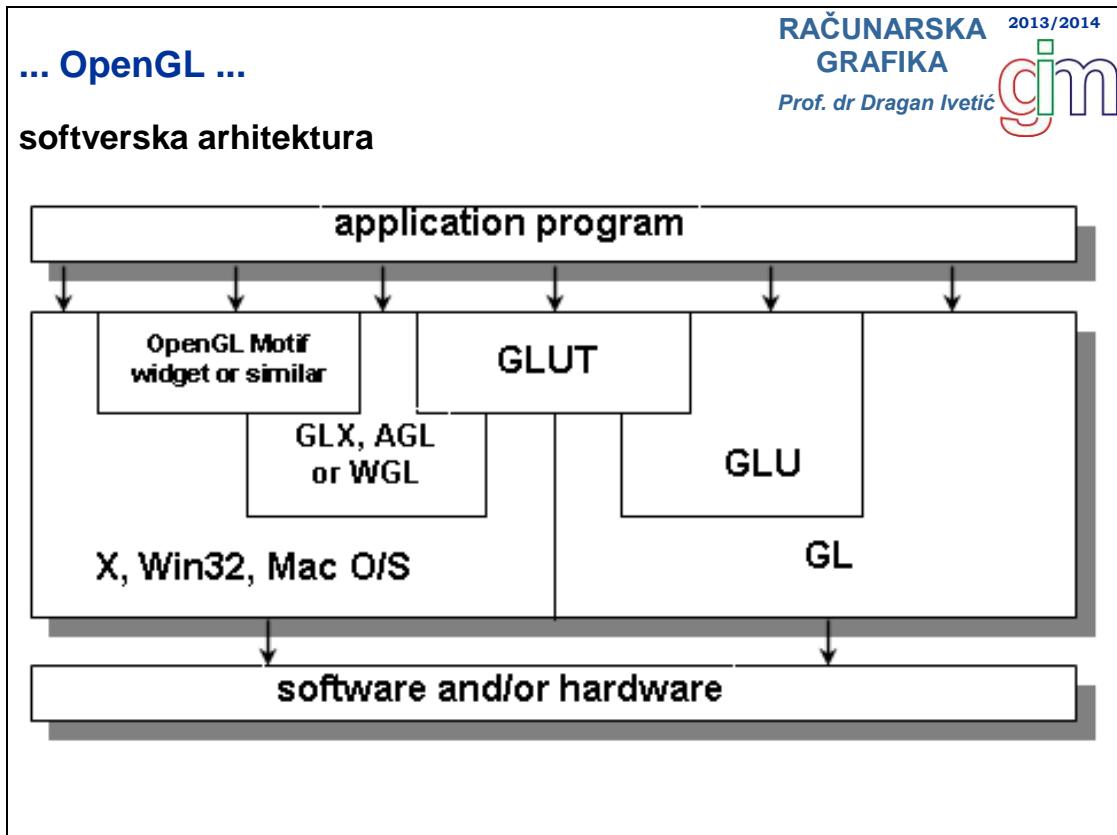


teme za diplomske rade

... OpenGL ...

OpenGL pajplajn

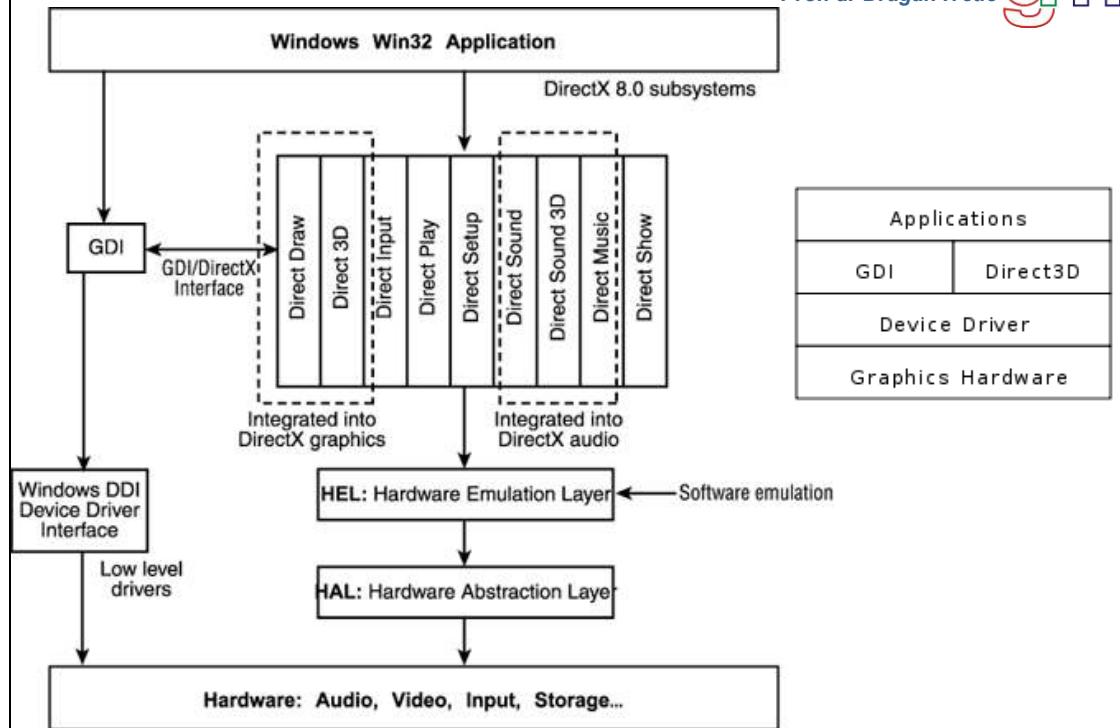


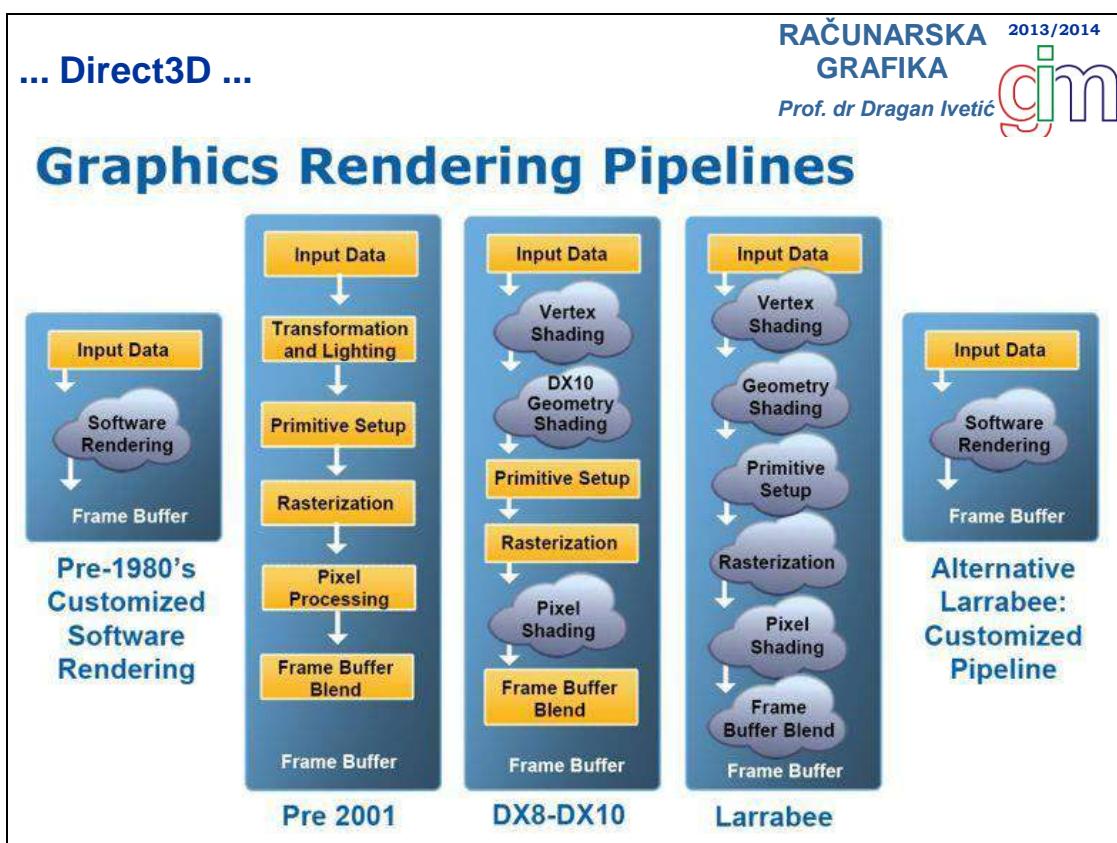
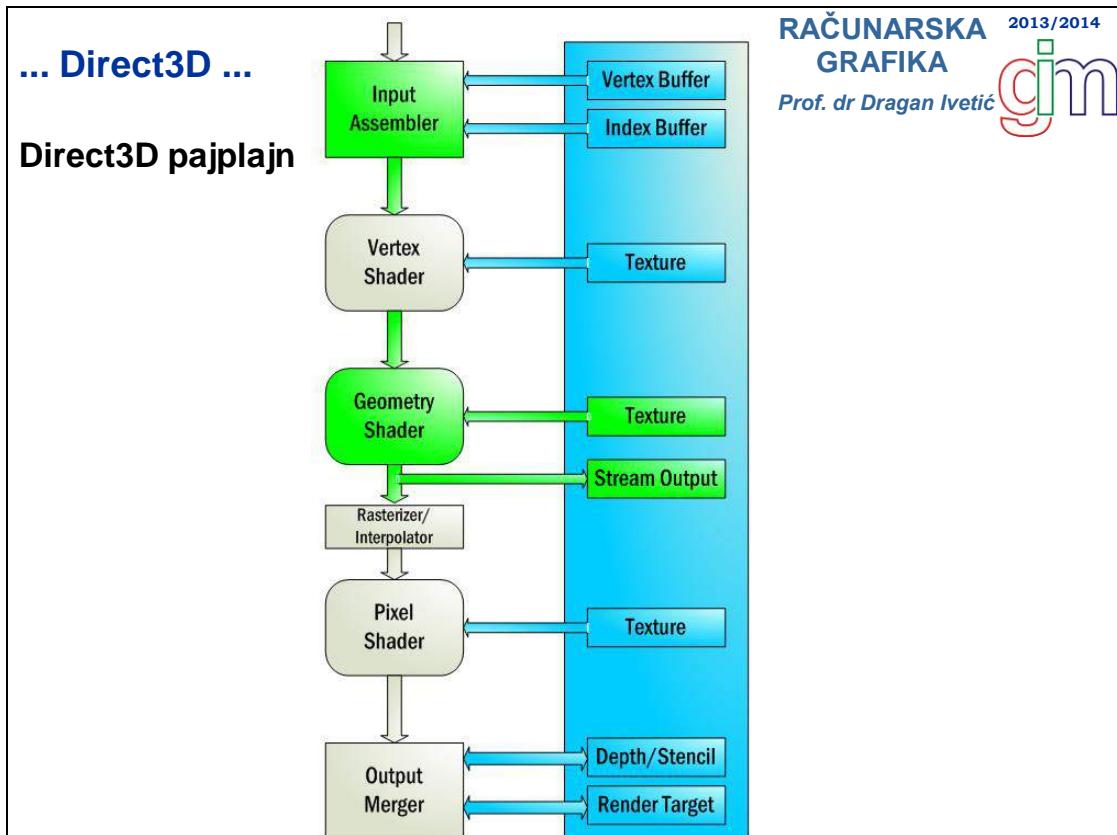


Direct3D ...

- Direct3D je grafička komponenta DirectX kolekcije API-ja za podršku multimediji,
- MS otkupio Reality Lab 3D API 1992. i ugradio u Win95 kao 3D engine, posle Win. games SDK, pa ugrađeno u DirectX 2.0 i 3.0,
 - execute buffer – parsiran od strane HW da bi prikazao scenu, DirectX 5.0 (97) i 5.2 (98) isključio execute bafer sa Draw API,
 - DirectX 6.0 (98) i 6.1 (99) optimizovao geometrijski pajplajn za x87,
 - DirectX 7.0 (99) i 7.1 (00) hardversko ubrzanje transformacija i osvetljenja sa Nvidia GeForce familijom GPU,
 - DirectX 8.0 (00), 8.1 (01) i 8.2 (02) programabilni šejderi,
 - DirectX 9.0 (03) i 9.0abc (svaka 2 meseca do juna 10) novi HLSL,
 - DirectX 10.0 (06) i 10.1 (08) novi šejder model 4.0 za Vistu, pajpalajn fiksne funkcije isključen
- DirectX 11.0 (09) i 11.1 (12) tessellation za Windows 7, odnosno Windows 8, quad buffering.

... Direct3D ...





... Direct3D ...

```
// include the basic windows header files and the Direct3D header file
#include <windows.h>
#include <windowsx.h>
#include <d3d9.h>

// define the screen resolution
#define SCREEN_WIDTH 800
#define SCREEN_HEIGHT 600

// include the Direct3D Library file
#pragma comment (lib, "d3d9.lib")

// global declarations
LPDIRECT3D9 d3d; // the pointer to our Direct3D interface
LPDIRECT3DDEVICE9 d3ddev; // the pointer to the device class
LPDIRECT3DVERTEXBUFFER9 v_buffer = NULL; // the pointer to the vertex buffer

// function prototypes
void initD3D(HWND hWnd); // sets up and initializes Direct3D
void render_frame(void); // renders a single frame
void cleanD3D(void); // closes Direct3D and releases memory
void init_graphics(void); // 3D declarations

struct CUSTOMVERTEX {FLOAT X, Y, Z, RHW; DWORD COLOR;};
#define CUSTOMFVF (D3DFVF_XYZRHW | D3DFVF_DIFFUSE)

// the WindowProc function prototype
LRESULT CALLBACK WindowProc(HWND hWnd, UINT message, WPARAM wParam, LPARAM lParam);
```

DirectX9

Lesson 4: Drawing a Triangle
<http://www.directxtutorial.com>

... Direct3D ...

```
// the entry point for any Windows program
int WINAPI WinMain(HINSTANCE hInstance, HINSTANCE hPrevInstance, LPSTR lpCmdLine, int nCmdShow)
{ HWND hWnd;
WNDCLASSEX wc;
ZeroMemory(&wc, sizeof(WNDCLASSEX));
wc.cbSize = sizeof(WNDCLASSEX);
wc.lpfnWndProc = WindowProc;
wc.hCursor = LoadCursor(NULL, IDC_ARROW);
RegisterClassEx(&wc);
hWnd = CreateWindowEx(NULL, L"WindowClass", L"Our Direct3D Program", WS_OVERLAPPEDWINDOW
0, 0, SCREEN_WIDTH, SCREEN_HEIGHT, NULL, NULL, hInstance, NULL);
ShowWindow(hWnd, nCmdShow);
// set up and initialize Direct3D
initD3D(hWnd);
// enter the main loop:
MSG msg;
while(TRUE)
{while(PeekMessage(&msg, NULL, 0, 0, PM_REMOVE))
{ TranslateMessage(&msg);
DispatchMessage(&msg); }
if(msg.message == WM_QUIT) break;
render_frame();
// clean up DirectX and COM
cleanD3D();
return msg.wParam; }
```

... Direct3D ...

```
// this is the main message handler for the program
LRESULT CALLBACK WindowProc(HWND hWnd, UINT message, WPARAM wParam, LPARAM lParam)
{ switch(message)
  { case WM_DESTROY: { PostQuitMessage(0); return 0; }
    break;}
  return DefWindowProc (hWnd, message, wParam, lParam);}

// this function initializes and prepares Direct3D for use
void initD3D(HWND hWnd)
{
  d3d = Direct3DCreate9(D3D_SDK_VERSION);

  D3DPRESENT_PARAMETERS d3dpp;

  ZeroMemory(&d3dpp, sizeof(d3dpp));
  d3dpp.SwapEffect = D3DSWAPEFFECT_DISCARD;
  d3dpp.BackBufferFormat = D3DFMT_X8R8G8B8;
  d3dpp.BackBufferHeight = SCREEN_HEIGHT;

  // create a device class using this information and the info from the d3dpp struct
  d3d->CreateDevice(D3DADAPTER_DEFAULT, D3DDEVTYPE_HAL, hWnd,
                      D3DCREATE_SOFTWARE_VERTEXPROCESSING, &d3dpp, &d3ddev);

  init_graphics(); // call the function to initialize the triangle }
```

... Direct3D ...

```
// this is the function used to render a single frame
void render_frame(void)
{
  d3ddev->Clear(0, NULL, D3DCLEAR_TARGET, D3DCOLOR_XRGB(0, 0, 0), 1.0f, 0);

  d3ddev->BeginScene();

  // select which vertex format we are using
  d3ddev->SetFVF(CUSTOMFVF);

  // select the vertex buffer to display
  d3ddev->SetStreamSource(0, v_buffer, 0, sizeof(CUSTOMVERTEX));

  // copy the vertex buffer to the back buffer
  d3ddev->DrawPrimitive(D3DPT_TRIANGLELIST, 0, 1);

  d3ddev->EndScene();

  d3ddev->Present(NULL, NULL, NULL, NULL);
}

// this is the function that cleans up Direct3D and COM
void cleanD3D(void)
{
  v_buffer->Release(); // close and release the vertex buffer
  d3ddev->Release(); // close and release the 3D device
  d3d->Release(); // close and release Direct3D
}
```

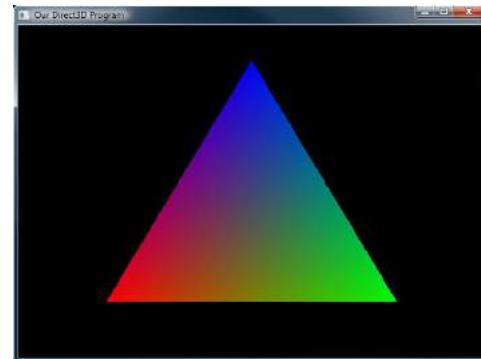
... Direct3D ...

```
// this is the function that puts the 3D models into video RAM
void init_graphics(void)
{
    // create the vertices using the CUSTOMVERTEX struct
    CUSTOMVERTEX vertices[] =
    {
        { 400.0f, 62.5f, 0.5f, 1.0f, D3DCOLOR_XRGB(0, 0, 255), },
        { 650.0f, 500.0f, 0.5f, 1.0f, D3DCOLOR_XRGB(0, 255, 0), },
        { 150.0f, 500.0f, 0.5f, 1.0f, D3DCOLOR_XRGB(255, 0, 0), },
    };

    // create a vertex buffer interface called v_buffer
    d3ddev->CreateVertexBuffer(3*sizeof(CUSTOMVERTEX),
        0,
        CUSTOMVF,
        D3DPOOL_MANAGED,
        &v_buffer,
        NULL);

    VOID* pVoid; // a void pointer

    // lock v_buffer and load the vertices into it
    v_buffer->Lock(0, 0, (void**)&pVoid, 0);
    memcpy(pVoid, vertices, sizeof(vertices));
    v_buffer->Unlock();
}
```



... Direct3D ...

```
using System;
using System.Windows.Forms;
using Microsoft.DirectX;
using Microsoft.DirectX.Direct3D;

namespace MDX_Tutorial2
{
    class MainClass:Form
    { private Device m_device = null;
```

Managed DirectX C# Graphics
Tutorial 2: Drawing a Triangle
<http://gregs-blog.com>

```
    MainClass()
    {     this.Text = "Managed DirectX Tutorial 2"; }

    void InitGraphics()
    { PresentParameters present_params = new PresentParameters();

        present_params.Windowed = true;
        present_params.SwapEffect = SwapEffect.Discard;

        m_device = new Device(0, DeviceType.Hardware, this,
            CreateFlags.SoftwareVertexProcessing, present_params); }
```

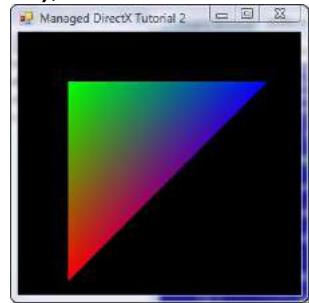
... Direct3D

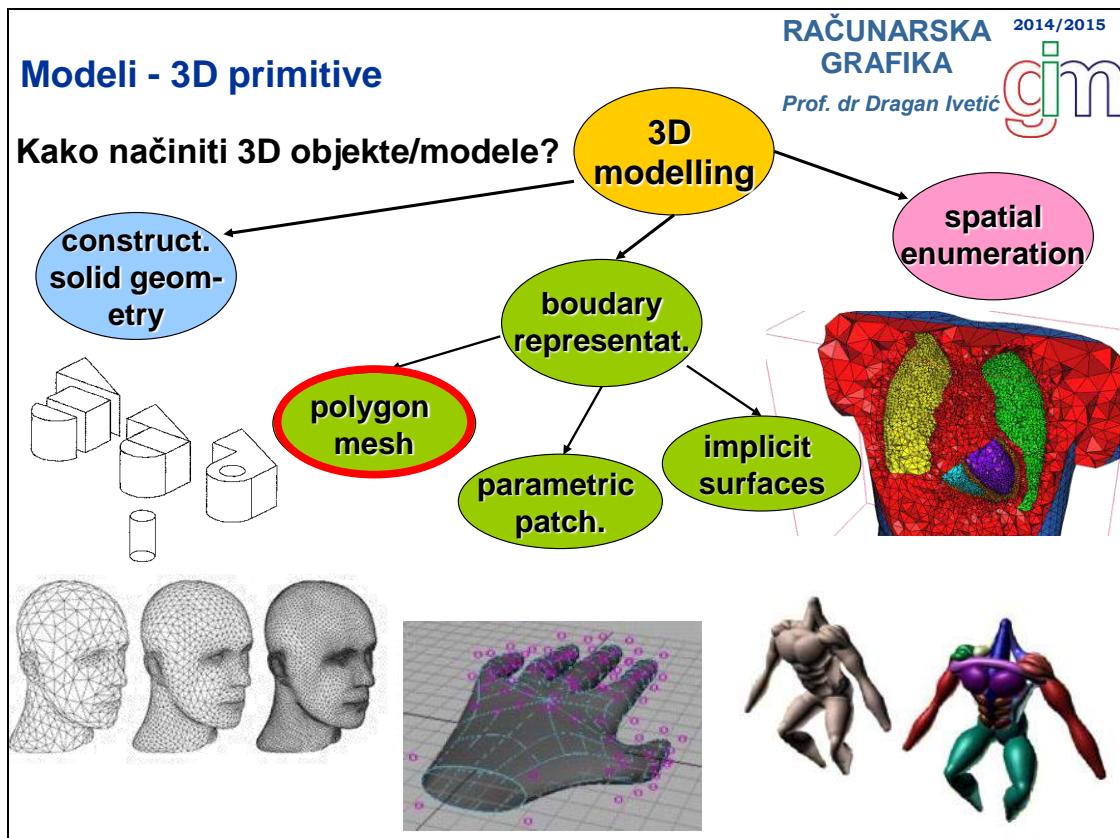
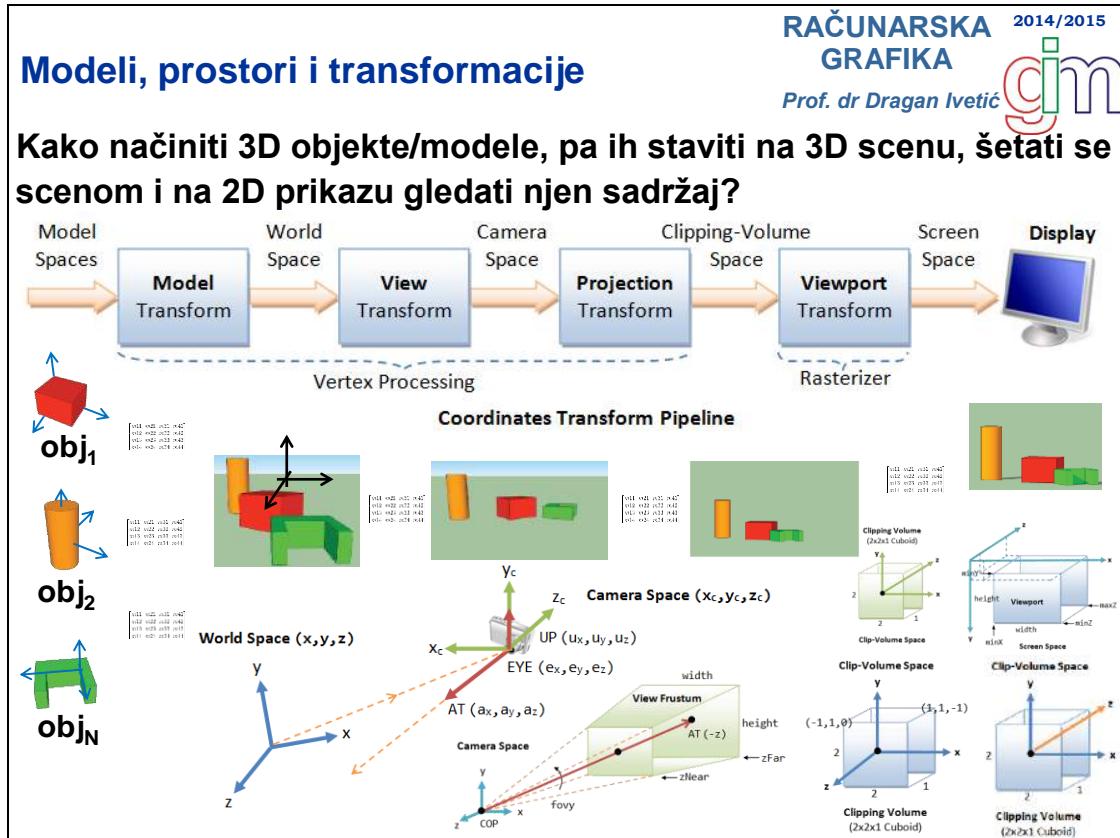
```
protected override void OnPaint(PaintEventArgs e)
{
    CustomVertex.TransformedColored[] vertexes = new CustomVertex.TransformedColored[3];

    vertexes[0].Position = new Vector4(50, 50, 0, 1.0f);
    vertexes[0].Color = System.Drawing.Color.FromArgb(0, 255, 0).ToArgb();
    vertexes[1].Position = new Vector4(250, 50, 0, 1.0f);
    vertexes[1].Color = System.Drawing.Color.FromArgb(0, 0, 255).ToArgb();
    vertexes[2].Position = new Vector4(50, 250, 0, 1.0f);
    vertexes[2].Color = System.Drawing.Color.FromArgb(255, 0, 0).ToArgb();

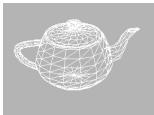
    m_device.Clear(ClearFlags.Target, System.Drawing.Color.FromArgb(0, 0, 0).ToArgb(), 1.0f, 0)
    m_device.BeginScene();
    m_device.VertexFormat = CustomVertex.TransformedColored.Format;
    m_device.DrawUserPrimitives(PrimitiveType.TriangleList, 1, vertexes);
    m_device.EndScene();
    m_device.Present();
}

static void Main()
{ MainForm MainForm = new MainForm();
  MainForm.InitGraphics();
  Application.Run(MainForm); } }:
```





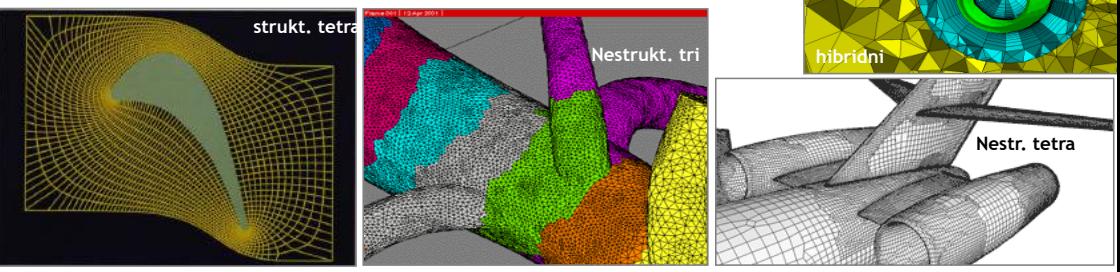
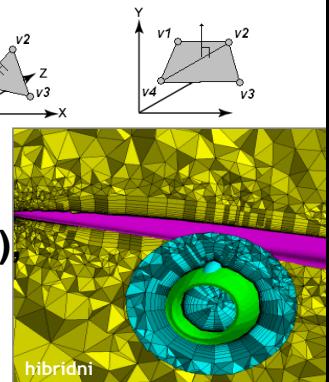
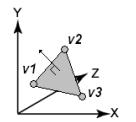
Modeli



Mreža poligona ...

Skup ivica, temena i poligona spojenih tako da:

- svaka ivica je deljena među najviše dva susedna poligona,
- ivica povezuje dva temena,
- poligon je zatvorena sekvenca ivica.
- ogroman broj algoritama
 - zavisno od oblika poligona (tri, tetra),
 - a i same mreže (nestrukt., strukt. – grid),

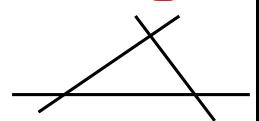


Modeli



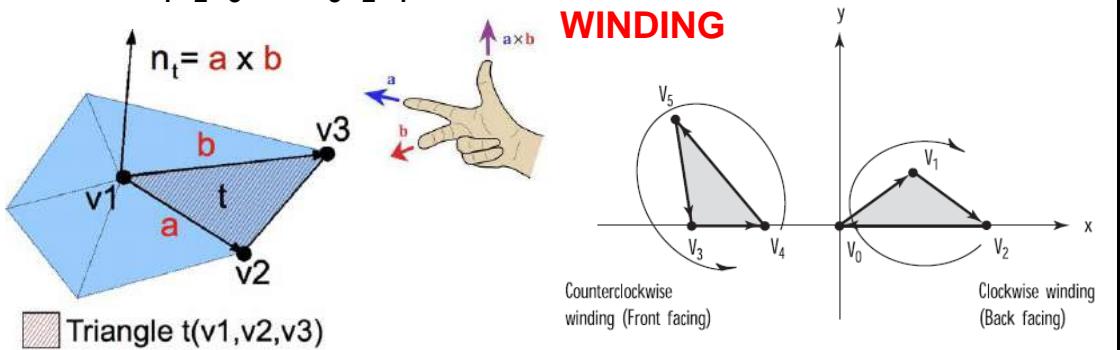
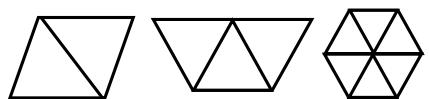
... Mreža poligona ...

Načiniti "kožu" objekta, iznutra su šuplji.

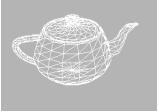


Da li koristiti trougao ili tetraedar?

- matematički jednostavno (3 tačke i 3 ivice),
- uvek planaran i nikad konkavan,
- gradivan za ostale oblike,
- ima prednju i zadnju stranu,
 - $v_1v_2v_3 == v_3v_2v_1 ??$



Modeli

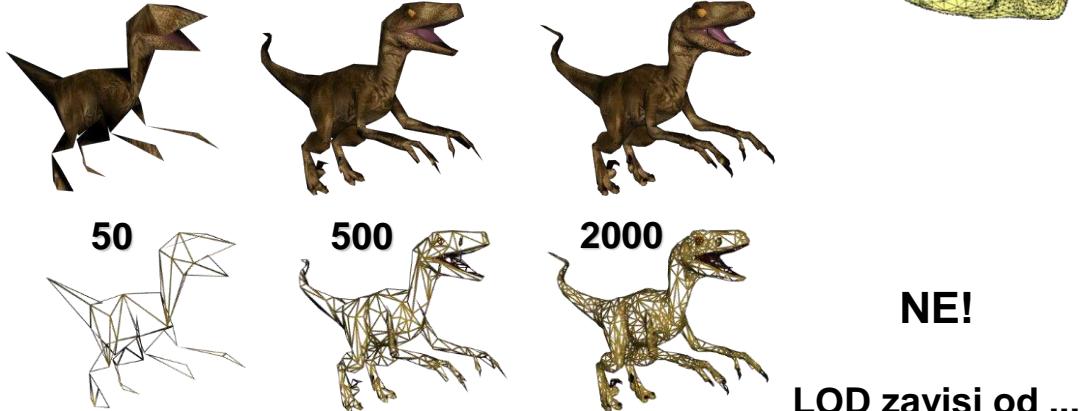


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... Mreža poligona ... Prof. dr Dragan Ivetić

Veća nepravilnost površine modela zahteva ? broj trouglova,

- kvalitet modela zavisi od broja trouglova,
- praviti modele sa najviše moguće trouglova?



NE!

LOD zavisi od ...

Modeli



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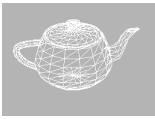
... Mreža poligona ... Prof. dr Dragan Ivetić

LOD opada sa rastojanjem gledaoc-objekat!



što opet povlači i zavisnot LOD od
ugla gledanja na objekat,
brzine objekta,
konteksta scene, ... ,
rezolucije projekcione površine!

Modeli



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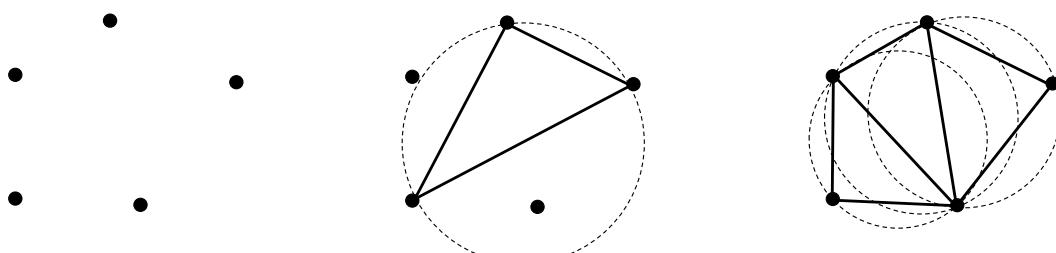
... Mreža poligona ... Prof. dr Dragan Ivetić



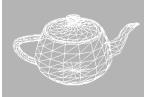
Kako da napravim 3D model objekta pomoću poligona sa odabranim LOD?

1. Generiše se skup tačaka koji pripadaju površini objekta:
ručno,
matematikom, ili
skeniranjem.

2. Primeni se Delaunay-ova triangulacija.



Modeli



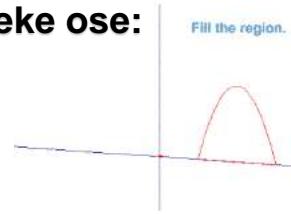
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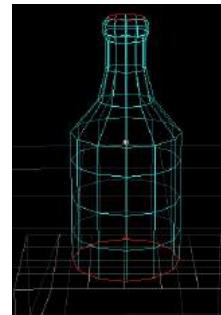
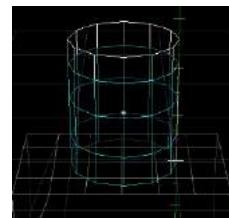
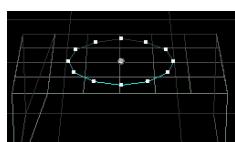
... Mreža poligona ... Prof. dr Dragan Ivetić
matematikom ...



1. Tela koja se dobijaju vrtnjom krive oko neke ose:
sfera,
cilindar,
torus,
konus...



2. Izvlačenjem (extrude) napolje/unutra novog elementa po nekoj krivoj bez gubljenja volumena.

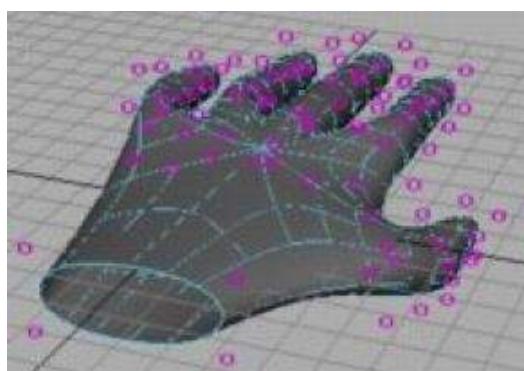
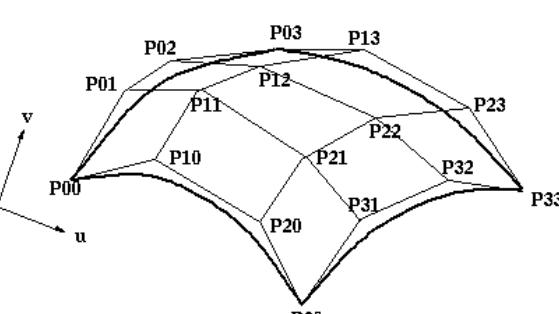
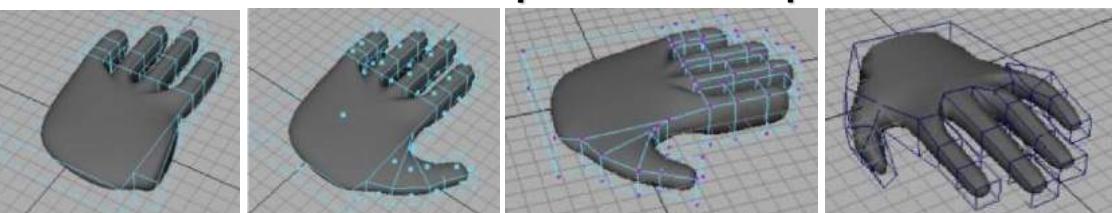


Modeli

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... Mreža poligona ... Prof. dr Dragan Ivetić
... matematikom

3. Non-Uniform Rational B-splines krivama/površinama

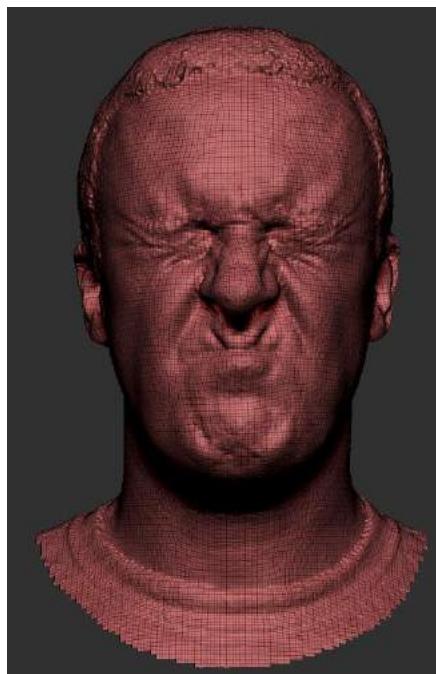


Modeli

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... Mreža poligona ... Prof. dr Dragan Ivetić
skeniranjem...

1. 3D face capture - 18 kamera svaka sa 4.096x4.096 piksela u 1/10.000 s,

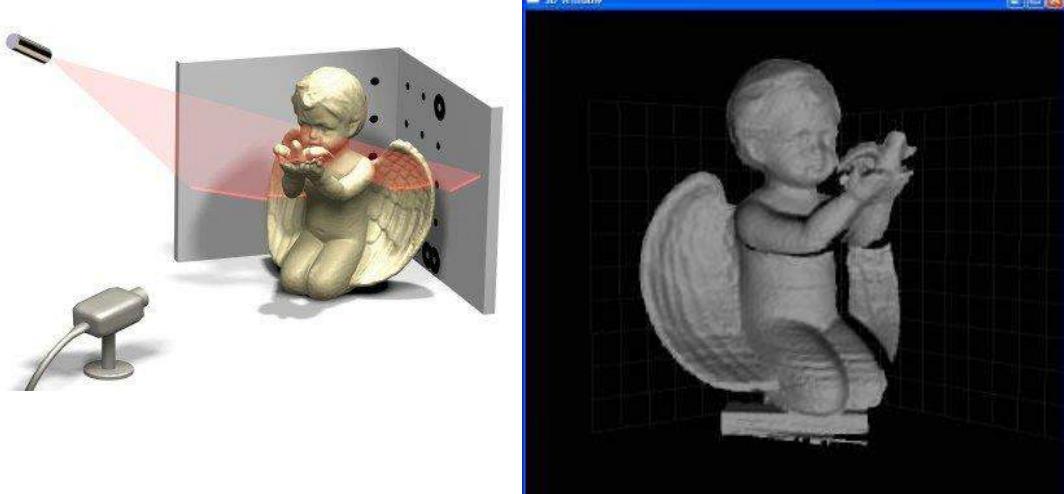


Modeli

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... Mreža poligona ... Prof. dr Dragan Ivetić
... skeniranjem

**2. lasersko 3D skeniranje,
DAVID-Laserscanner 2.6.1 - Portable,**



Modeli

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... Mreža poligona ... Prof. dr Dragan Ivetić

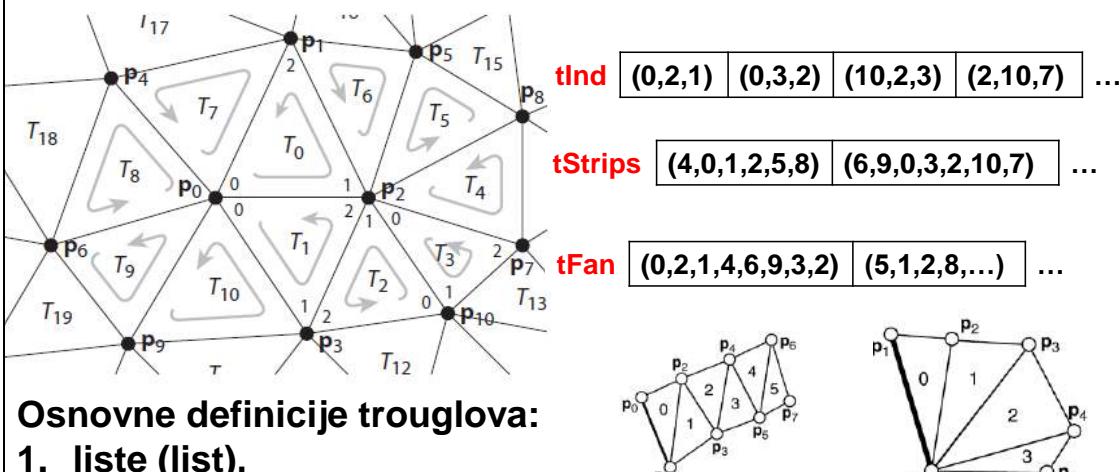
Kako definisati trouglove mreže na (skladišno i procesno) efikasan način?

verts (x_0, y_0, z_0) (x_1, y_1, z_1) (x_2, y_2, z_2) (x_3, y_3, z_3) ...

tInd $(0,2,1)$ $(0,3,2)$ $(10,2,3)$ $(2,10,7)$...

tStrips $(4,0,1,2,5,8)$ $(6,9,0,3,2,10,7)$...

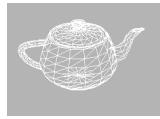
tFan $(0,2,1,4,6,9,3,2)$ $(5,1,2,8,...)$...



Osnovne definicije trouglova:

1. liste (list),
2. trake (strips), **Konzistentnost orientacije trouglova?**
3. ventilatori (fan).

Modeli



... Mreža poligona

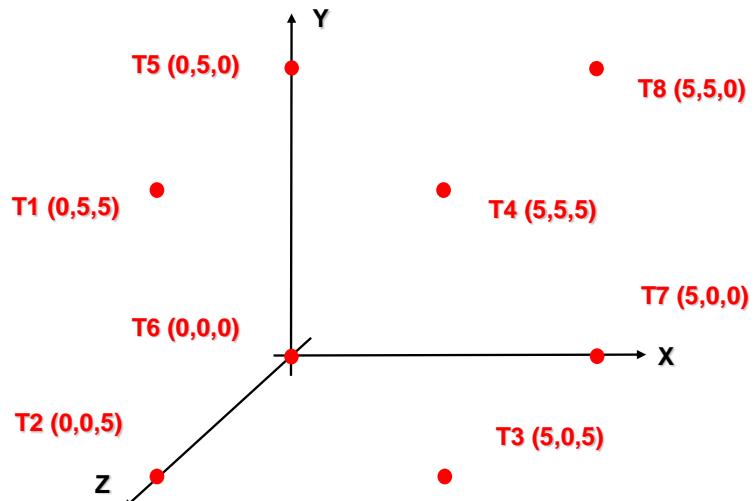
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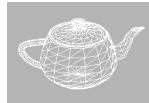


2014/2015

Predstaviti temena pomoću liste, ventilatora i trake.



Modeli



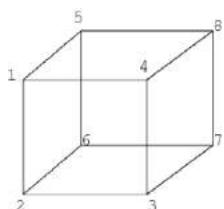
... Mreža poligona

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Prof. dr Dragan Ivetić

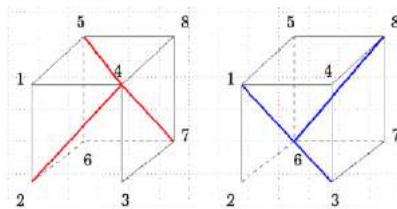


2014/2015



trouglovi:

T241, T234, T384, T378, T758, T765,
T615, T625, T451, T485, T273 i T267.

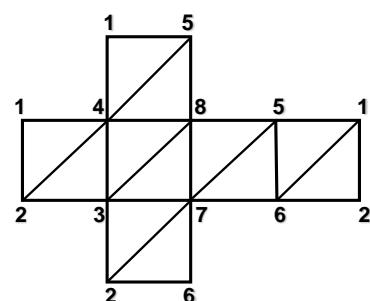


Fan

- 4 1 2 3 7 8 5 1
- 6 2 1 5 8 7 3 2

Strips

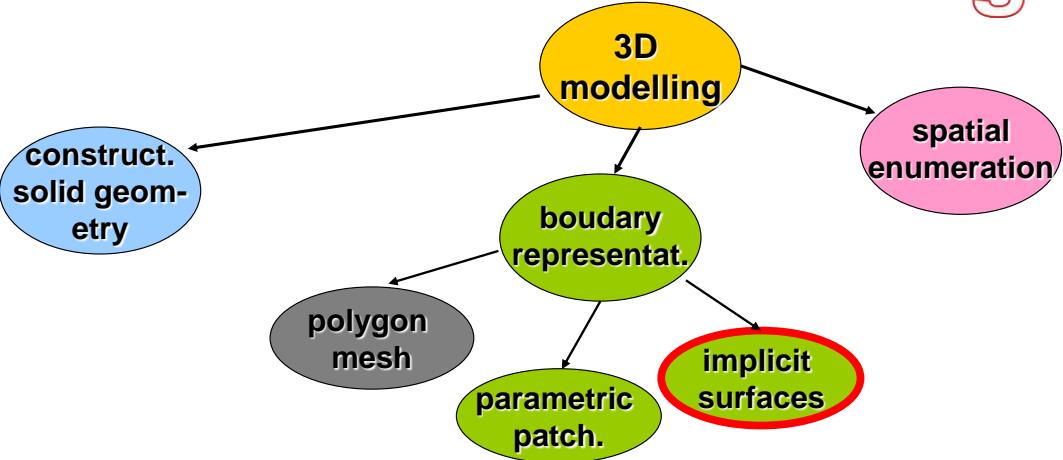
- 1 2 4 3 8 7 5 6 1 2
- 1 4 5 8
- 2 3 6 7



Modeli

Implicitne površine ...

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```

graph TD
    A[3D modelling] --> B[boundary representat.]
    A --> C[spatial enumeration]
    B --> D[polygon mesh]
    B --> E[parametric patch.]
    B --> F[implicit surfaces]
    style F fill:red,stroke:red
  
```

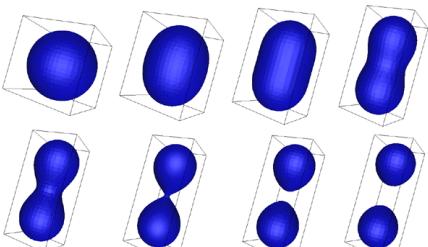
Definisanje isopovršina oslanjajući se na implicitnu definiciju lopte

$$x^2 + y^2 + z^2 = r^2$$

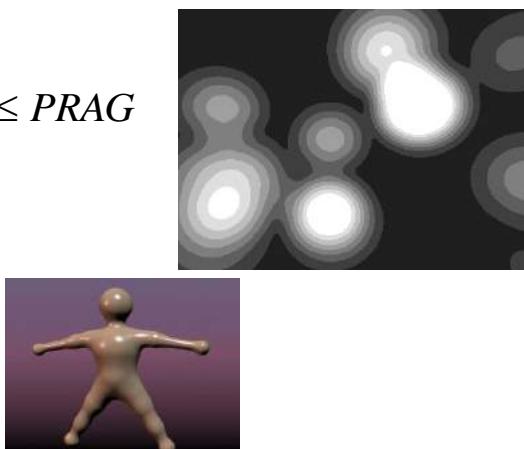
Kako bi nacrtali loptu za $r = 34$ sa centrom u (a,b,c) ?

Modeli

... Implicitne površine ... Prof. dr Dragan Ivetić 



Metaballs (blobby objects) - čestična tela radijalne gustine čiju površinu čine čestice gustine određenog praga!

$$\sum_{i=1}^N metaballs_i(x, y, z) \leq PRAG$$


Modeli

... Implicitne površine ...

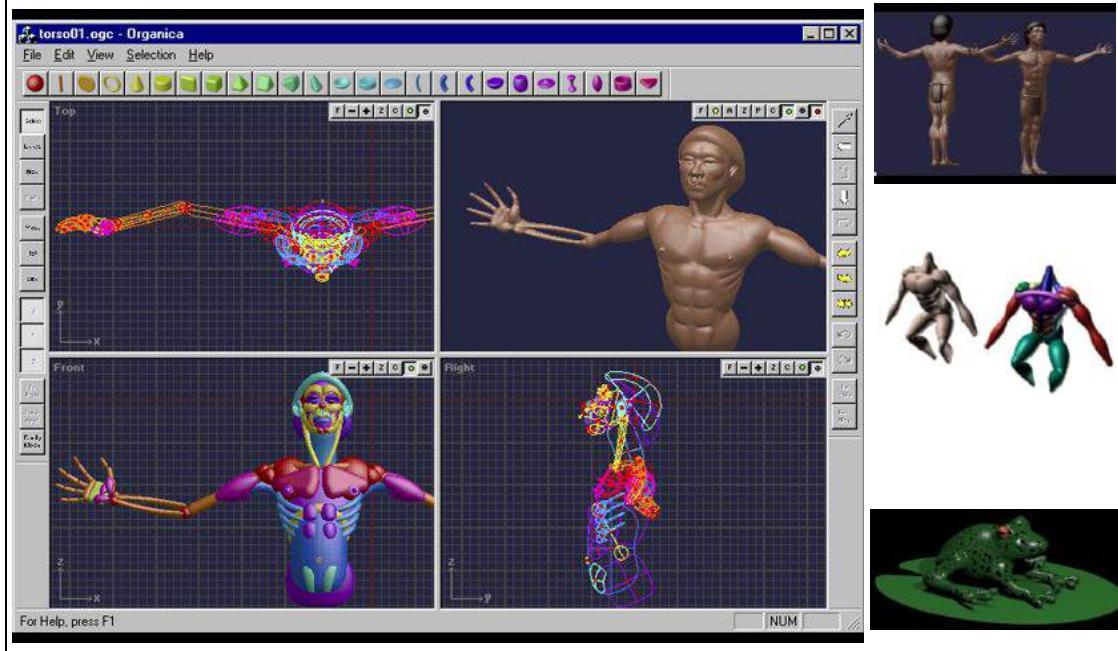
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Programsko okruženje Organica

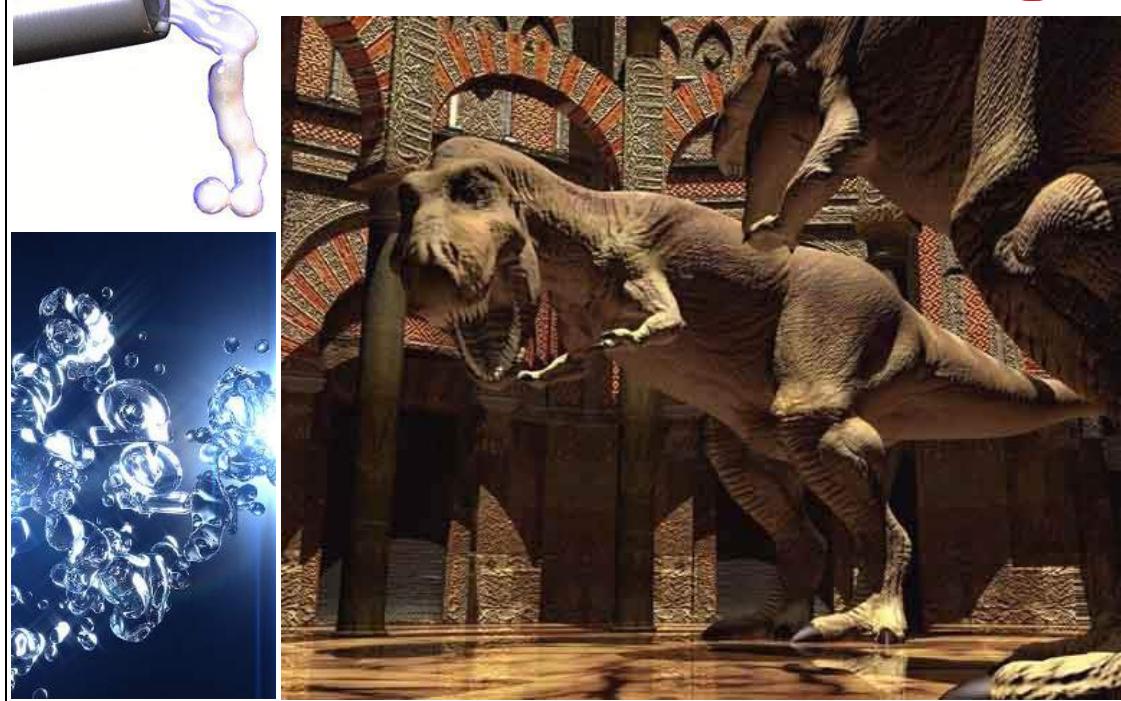


Modeli

... Implicitne površine

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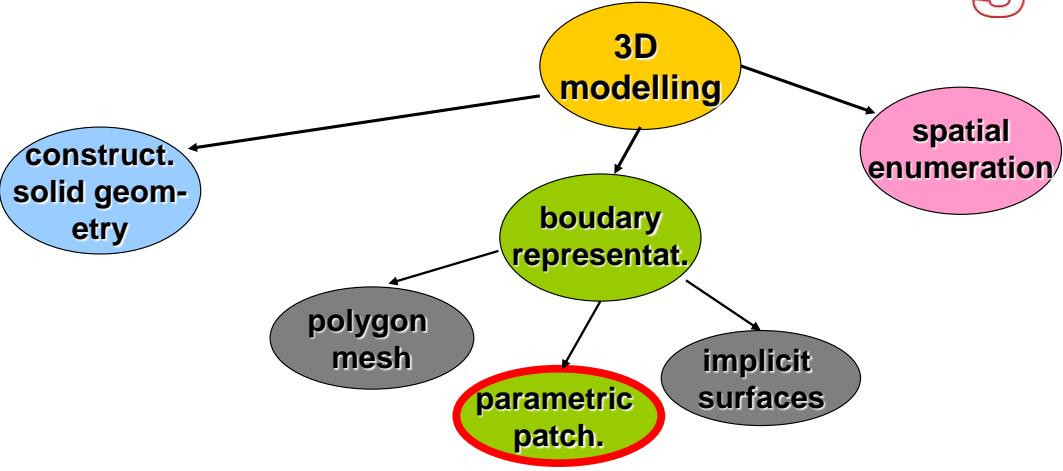
Prof. dr Dragan Ivetić



Modeli

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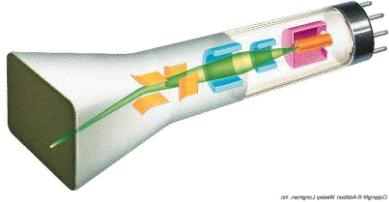
Parametarske zatrpe ...



```

graph TD
    A[3D modelling] --> B[boundary representat.]
    A --> C[construct. solid geom-etry]
    A --> D[spatial enumeration]
    B --> E[polygon mesh]
    B --> F[parametric patch.]
    B --> G[implicit surfaces]
    
```

Da li crtati 2D krivu eksplisitno
 $y = A x^3 + B x^2 + C x + D$
i to krivu u obliku petlje?



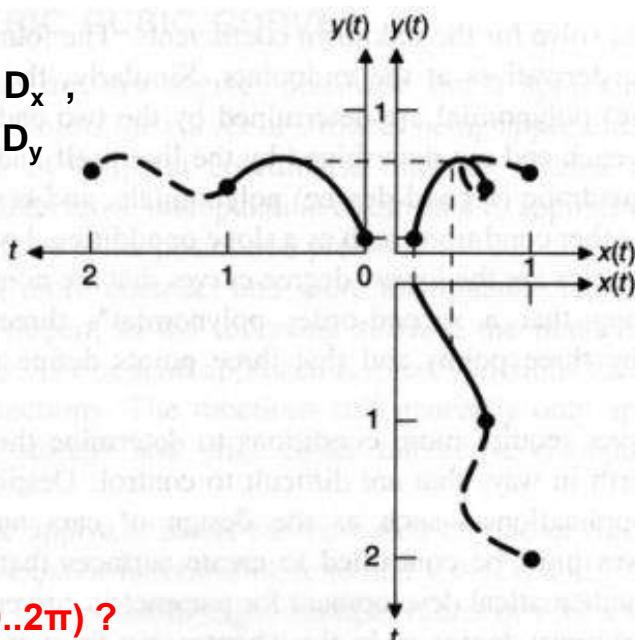
Modeli

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... Parametarske zatrpe ...

Jednostavnije parametarskom predstavom krive

$x(t) = A_x t^3 + B_x t^2 + C_x t + D_x$,
 $y(t) = A_y t^3 + B_y t^2 + C_y t + D_y$



Šta će se prikazati za
 $(x,y) = (\cos t, \sin t)$, $t \in (0..2\pi)$?

Modeli

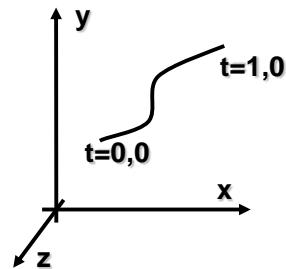
... Parametarske zakepte ...

Šta bi bilo formirano sa

$$x(t) = A_x t^3 + B_x t^2 + C_x t + D_x ,$$

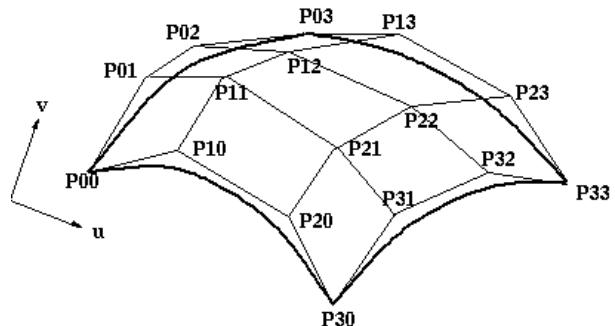
$$y(t) = A_y t^3 + B_y t^2 + C_y t + D_y ,$$

$$z(t) = A_z t^3 + B_z t^2 + C_z t + D_z .$$



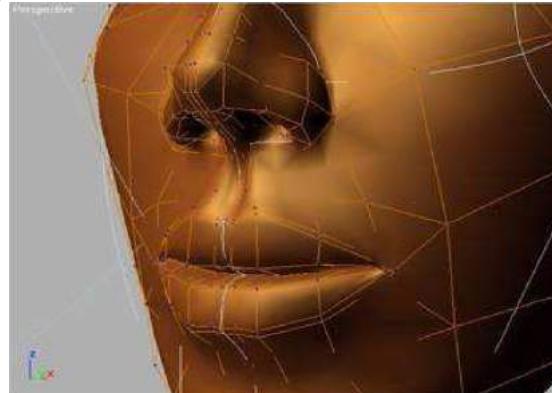
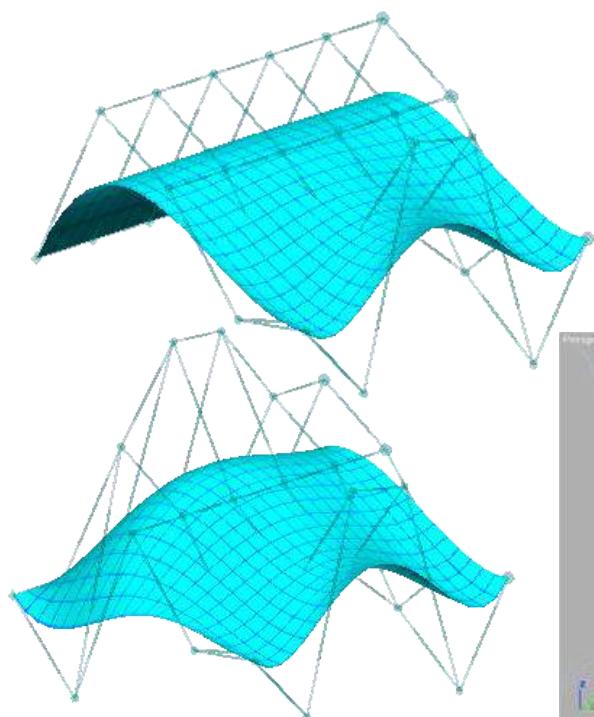
Šta bi bilo formirano sa

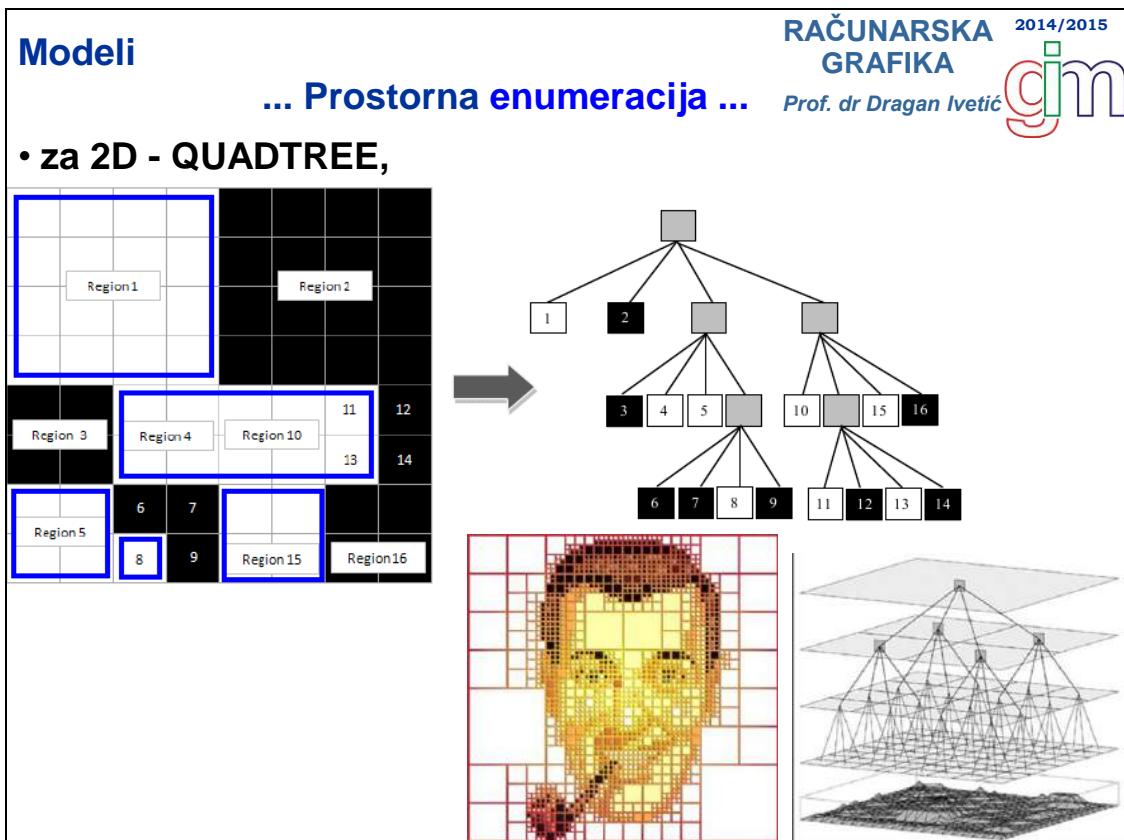
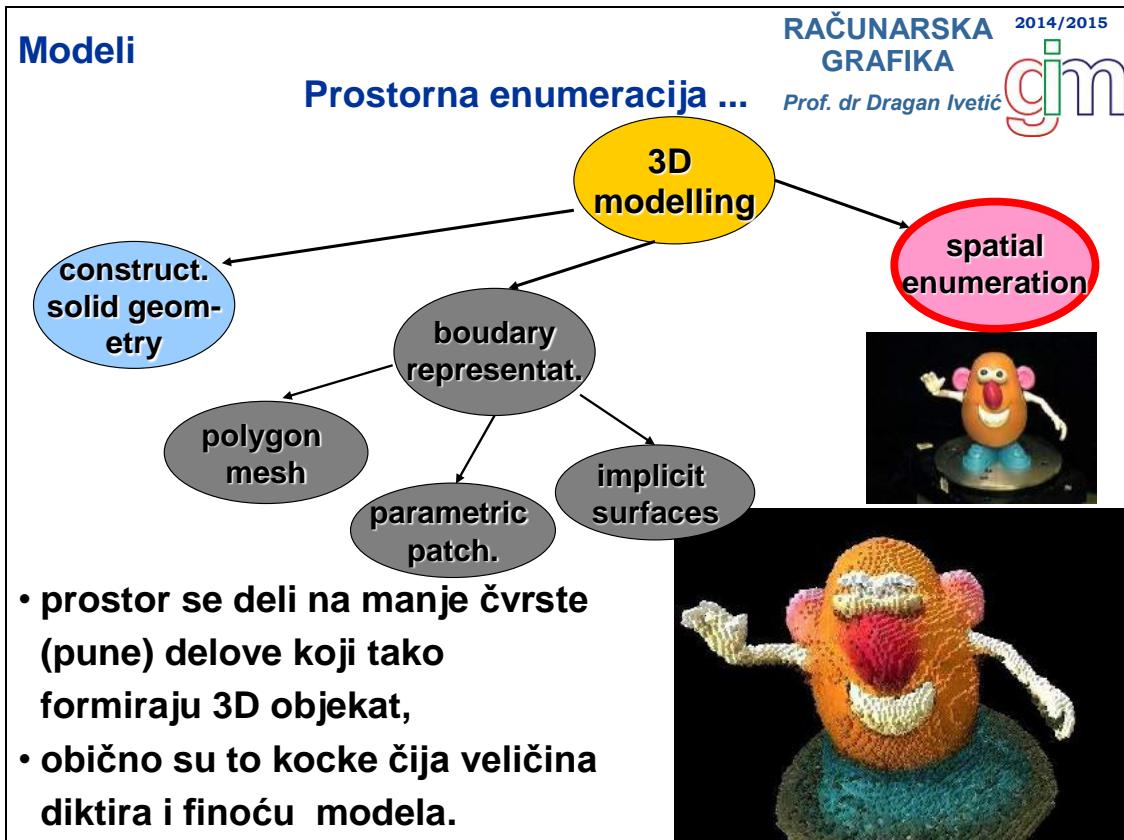
$$x(u,v) , y(u,v) , z(u,v) .$$



Modeli

... Parametarske zakepte





Modeli

... Prostorna enumeracija

• za 3D - OCTREE, voxels,

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Modeli

Modelovanje punim telom ...

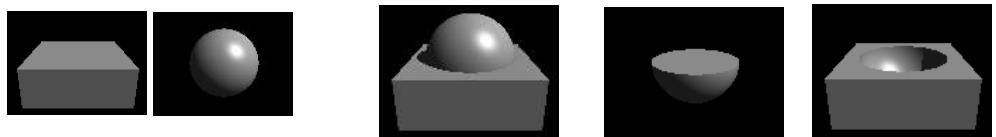
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- solid modeling - kreirali za CAD,

Modeli

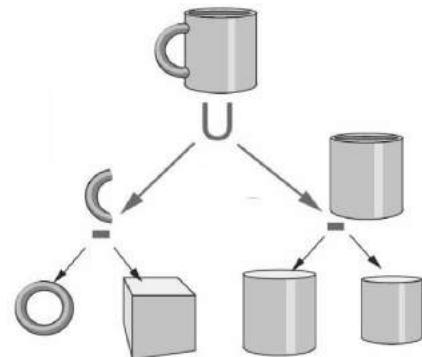
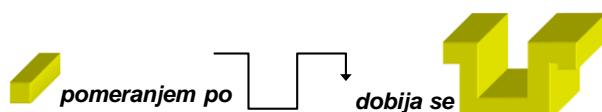
... Modelovanje punim telom ...

- solid modeling - kreirali za CAD,
- operacija skupova (U , ∩ , /)



nad primitivama (geometrijska tela),

- sweep.



Modeli

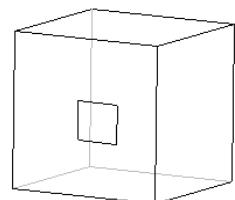
... Modelovanje punim telom ...

- posle su dodali nove funkcije modelovanja ...

Solid Extrusion – obično za kreiranje osnovnih modela za nove gradnje.



Cut/Slot Extrusion – obično za otvore, rupe, ključaonice, polaze, žljebove i sl.



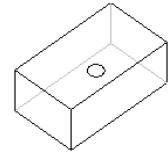
Revolved Extrusion – obično za osnovne modele, cevi, torusne oblike, rebra i sl.



Modeli

... Modelovanje punim telom

Revolved Cut – obično za unutrašnje cevi, odlivci, hlađenje SUS motora.



Loft – obično za nove osnovne oblike sa topološki sličnim terminalima.



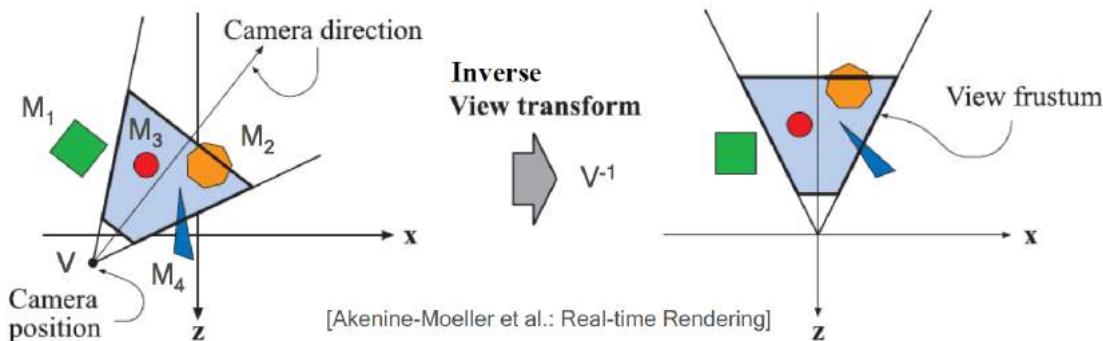
Shell – obično za šolje, činije, stvari sa tankim okvirom/zidom.



3D transformacije

Zašto ...

- da pozicioniramo, preoblikujemo i animiramo objekte, svetla i virtuelnu kameru u 3D prostoru,



- M_i i V su 4×4 matrice 3D transformacija,
- M_1 , M_2 , M_3 i M_4 pozicioniraju objekte a V kameru na scenu,
- pa V^{-1} sve pomera u koordinatni početak uz $-Z$ osu,
- tj., na objekat i sprovodi modelview transformaciju $V^{-1}M_i$.

3D transformacije

Elementarne transformacije ...

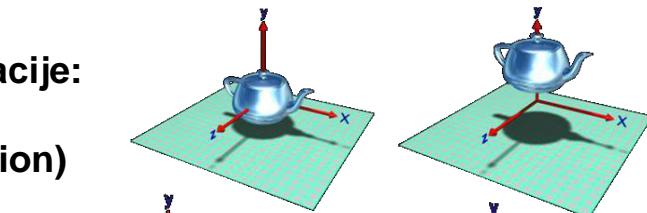
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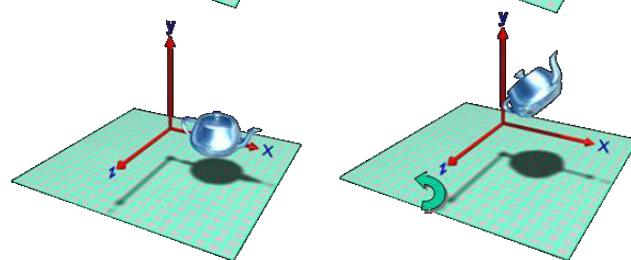


Elementarne transformacije:

TRANSLACIJA (translation)



ROTACIJA (rotation)



3D transformacije

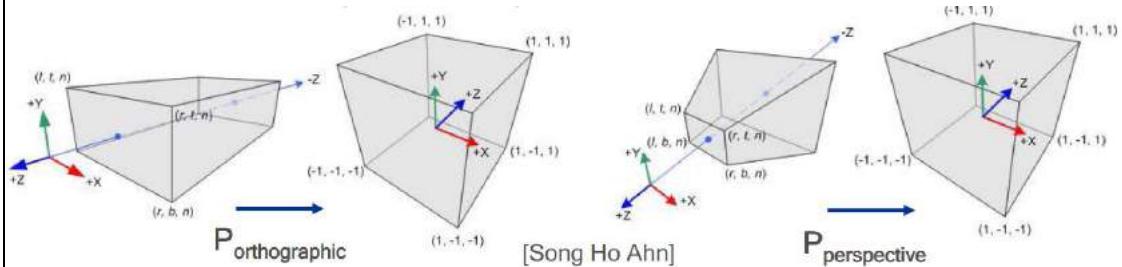
... Zašto

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- da ortografski ili perspektivno projektujemo 3D geometriju na ravan,



- matrica P transformiše view volume (kuboid ili frustum) na kanonski view volume (unit cube),
- transformacija se primjenjuje i na temena i na normale,
- temena i normale se predstavljaju 4D vektorima.

3D transformacije

... Elementarne transformacije

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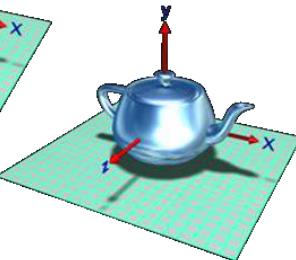
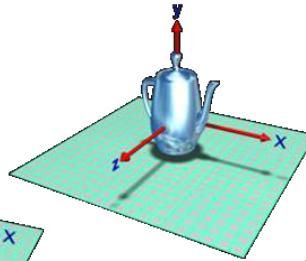
GRAFIKA

Prof. dr Dragan Ivetić

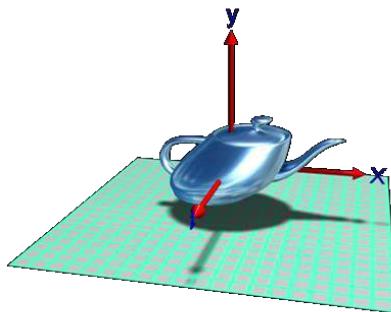
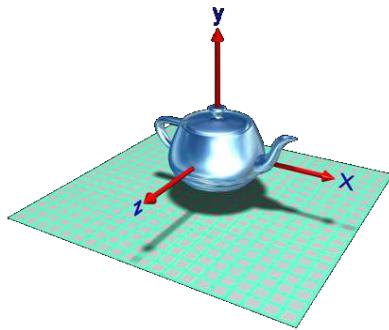
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SKALIRANJE (scaling) (ne)uniformno



SMICANJE (shear)



3D transformacije

Afina transformacije

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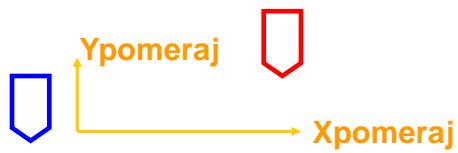


Afina transformacija (affine transformation)

- održava kolinearnost
 - tačke na liniji se transformišu u tačke na liniji,
- održava proporciju
 - odnosi razdaljina među tačkama ostaju isti,
- održava paralelizam
 - paralelne linije ostaju paralelne i posle transformacije,
- uglovi i dužine se ne održavaju,
- translacija, rotacija, skaliranje, smicanje i refleksija su afine transformacije,
- ortografska projekcija jeste kombinacija afine transform.,
- perspektivna transformacija nije affine.

3D transformacije**Primeri u 2D ...****2D TRANSLACIJA**

$$\begin{bmatrix} x_t \\ y_t \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} x_{pomeraj} \\ y_{pomeraj} \end{bmatrix}$$

**2D SKALIRANJE**

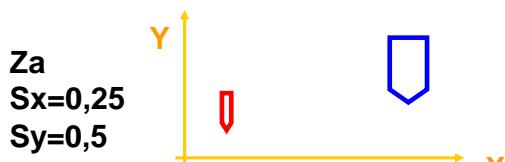
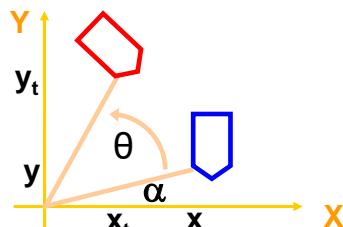
$$\begin{bmatrix} x_t \\ y_t \end{bmatrix} = \begin{bmatrix} S_x & 0 \\ 0 & S_y \end{bmatrix} * \begin{bmatrix} x \\ y \end{bmatrix}$$

Uniformno , $S_x=S_y$

- $S_x, S_y > 1$, veće i dalje od (0,0),
- $S_x, S_y < 1$, manje i bliže

Neuniformno, $S_x \neq S_y$

- $S_x, S_y > 1$, veće i dalje od (0,0),
- $S_x, S_y < 1$, manje i bliže

**3D transformacije****... Primeri u 2D ...****2D ROTACIJA**

$$\begin{aligned} x &= r \cos(\alpha) \\ y &= r \sin(\alpha) \end{aligned}$$

$$\begin{aligned} x_t &= r \cos(\alpha+\theta) = r \cos(\alpha) \cos(\theta) - r \sin(\alpha) \sin(\theta) = x \cos(\theta) - y \sin(\theta) \\ y_t &= r \sin(\alpha+\theta) = r \cos(\alpha) \sin(\theta) + r \sin(\alpha) \cos(\theta) = x \sin(\theta) + y \cos(\theta) \end{aligned}$$

$$\begin{bmatrix} x_t \\ y_t \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} * \begin{bmatrix} x \\ y \end{bmatrix}$$

Kako rotirati 2D objekat za ugao α oko njegovog temena na koordinatama (x , y) ?

3D transformacije

... Primeri u 2D

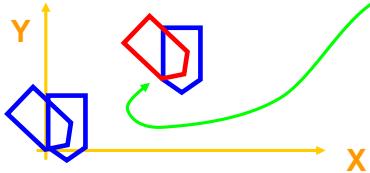
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Rotiranje 2D objekta za ugao α oko temena (x, y)



Translacija za $(-x, -y)$ u koord. početak

Rotacija za ugao α

Translacija za (x, y) u početni položaj

$$\begin{bmatrix} x_t \\ y_t \end{bmatrix} = \begin{bmatrix} x_{pom} \\ y_{pom} \end{bmatrix} + \left(\begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix} * \left(\begin{bmatrix} -x_{pom} \\ -y_{pom} \end{bmatrix} + \begin{bmatrix} x \\ y \end{bmatrix} \right) \right)$$

Dosta nesretno rešenje u pogledu efikasnosti!

Zašto?

Kome i kako pomoći da se dobije na efikasnosti?

3D transformacije

Homogenizacija

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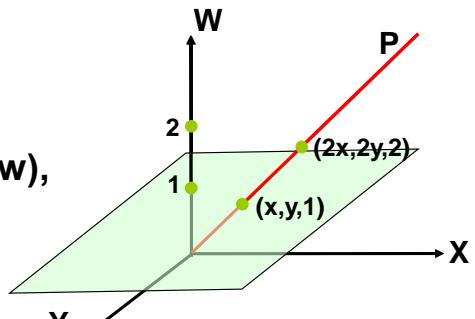
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HOMOGENE KOORDINATE, zakomplikujemo da bi postalo sve jednostavnije:

- 1D - tačka (x) postaje (x, w) ,
- 2D - tačka (x, y) postaje (x, y, w) ,
- 3D - tačka (x, y, z) postaje (x, y, z, w) ,
-
- **gde je uvek $w \geq 1$!!**
- **u RG je $w = 1$ za tačku,**

$$(x, y, 1) \equiv (2x, 2y, 2) \equiv (3x, 3y, 3) \equiv \dots \equiv (\textcolor{red}{nx}, \textcolor{red}{ny}, \textcolor{red}{n})$$



Kako iz Homogenih (a, b, w) u Dekartove koordinate?

Za $w \rightarrow 0$, x i y koordinate $\rightarrow \infty$.

Koordinata $(x, y, 0)$ je tačka u beskonačnosti,
u RG se naziva vektorom u pravcu (x, y) .

3D transformacije

Homog. 2D trans. ...

2D TRANSLACIJA

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & x_{pomeraj} \\ 0 & 1 & y_{pomeraj} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

2D SKALIRANJE

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

2D ROTACIJA

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) & 0 \\ \sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

2D SMICANJE

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & S_{saY} & 0 \\ S_{saX} & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

2D REFLEKSIJA oko ose koja zaklapa ugao θ sa x osom

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(2\theta) & \sin(2\theta) & 0 \\ \sin(2\theta) & -\cos(2\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

3D transformacije

... Homog. 2D trans.

Rotiranje 2D objekta za ugao α oko temena (x_p, y_p)

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} x_{pom} \\ y_{pom} \\ 1 \end{bmatrix} + \left(\begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix} * \left(\begin{bmatrix} -x_{pom} \\ -y_{pom} \end{bmatrix} + \begin{bmatrix} x \\ y \end{bmatrix} \right) \right)$$

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & x_{pomeraj} \\ 0 & 1 & y_{pomeraj} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) & 0 \\ \sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & -x_{pomeraj} \\ 0 & 1 & -y_{pomeraj} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x_t \\ y_t \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) & x_{pomeraj}(1-\cos(\alpha)) + y_{pomeraj}\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) & y_{pomeraj}(1-\cos(\alpha)) - x_{pomeraj}\sin(\alpha) \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

3D transformacije

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Homog. 3D trans. ...

3D TRANSLACIJA

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & x_{pomeraj} \\ 0 & 1 & 0 & y_{pomeraj} \\ 0 & 0 & 1 & z_{pomeraj} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

3D SKALIRANJE

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

3D SMICANJE

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & S_{XsaY} & S_{XsaZ} & 0 \\ S_{YsaX} & 1 & S_{YsaZ} & 0 \\ S_{ZsaX} & S_{ZsaY} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Kako bi izgledale matrice inverzne transformacije?

3D REFLEKSIJA po ravnima $x=0, y=0$ i $z=0$

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

3D transformacije

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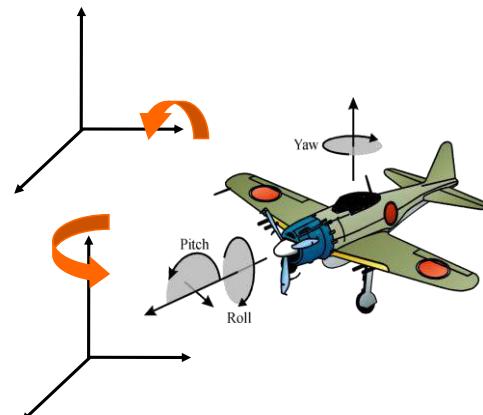
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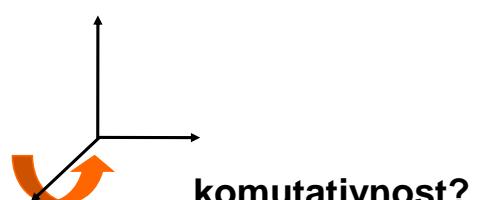
3D ROTACIJA po svakoj od osa

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\alpha) & -\sin(\alpha) & 0 \\ 0 & \sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$



$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(\alpha) & 0 & \sin(\alpha) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(\alpha) & 0 & \cos(\alpha) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x_t \\ y_t \\ z_t \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) & 0 & 0 \\ \sin(\alpha) & \cos(\alpha) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$



komutativnost?

3D transformacije

... Homog. 3D trans.

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Doprinos homogenih koordinata -
homogenizacija matrice transformacija

$$\begin{bmatrix} m_{00} & m_{01} & m_{02} & t_0 \\ m_{10} & m_{11} & m_{12} & t_1 \\ m_{20} & m_{21} & m_{22} & t_2 \\ p_0 & p_1 & p_2 & w \end{bmatrix}$$

pri čemu su

m_{ii}

t_i

p_i

w

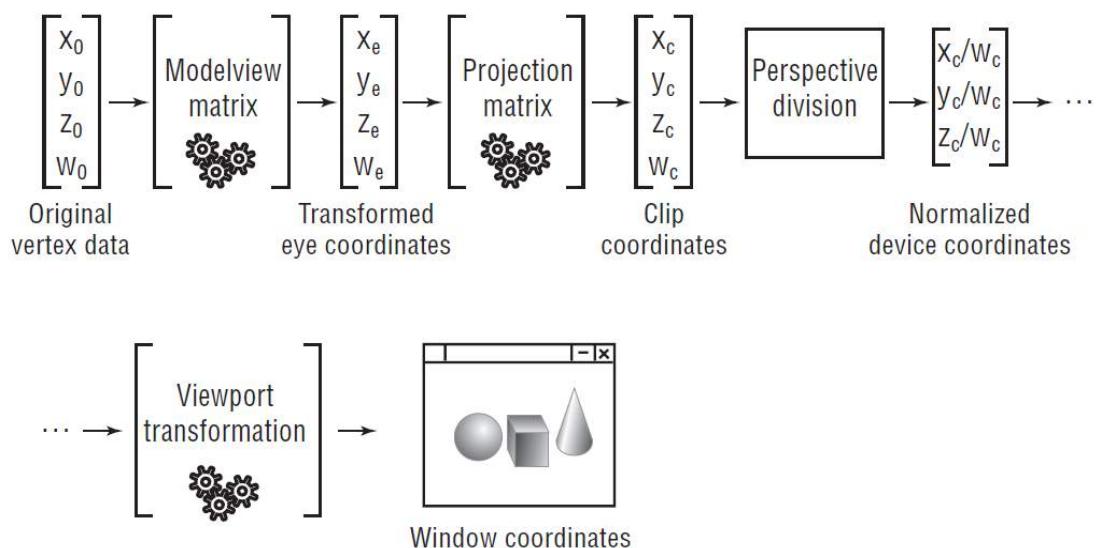
3D transformacije

Pajplajn transformacija temena

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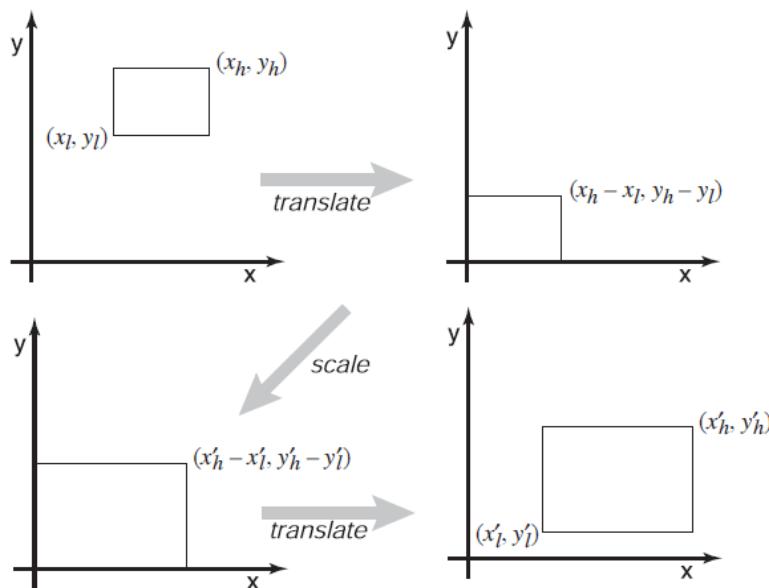


3D transformacije

Transformacija prozora ...

Kreirati matricu koja bi tačke iz jednog pravougaonika

$[x_l, x_h] \times [y_l, y_h]$ u drugi pravougaonik $[x'_l, x'_h] \times [y'_l, y'_h]$!



3D transformacije

... Transformacija prozora ...

$$M = T_{x'_l, y'_l} \times S \times T_{-x_l, -y_l} =$$

$$= \begin{bmatrix} 1 & 0 & x'_l \\ 0 & 1 & y'_l \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \frac{x'_h - x'_l}{x_h - x_l} & 0 & 0 \\ 0 & \frac{y'_h - y'_l}{y_h - y_l} & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & -x_l \\ 0 & 1 & -y_l \\ 0 & 0 & 1 \end{bmatrix} =$$

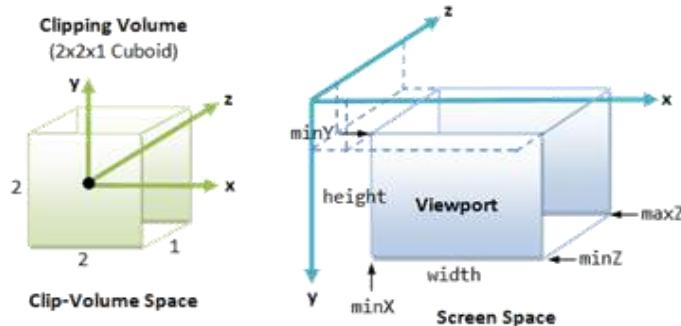
$$= \begin{bmatrix} \frac{x'_h - x'_l}{x_h - x_l} & 0 & \frac{x'_l x_h - x'_h x_l}{x_h - x_l} \\ 0 & \frac{y'_h - y'_l}{y_h - y_l} & \frac{y'_l y_h - y'_h y_l}{y_h - y_l} \\ 0 & 0 & 1 \end{bmatrix}$$

**Kako bi izgledalo za
matricu
transformacije
tačaka jednog
kuboida u drugi?**

3D transformacije

... Transformacija prozora

Kreirana matrica je Viewport transformacija!



$$M = \begin{bmatrix} \frac{width}{2} & 0 & \min X + \frac{width}{2} \\ 0 & \frac{height}{2} & \min Y + \frac{length}{2} \\ 0 & 0 & 1 \end{bmatrix}$$

3D transformacije

Transformacija prostora ...

Kako animirati vožnju Homera kroz Springfield?



3D transformacije

... Transformacije prostora ...

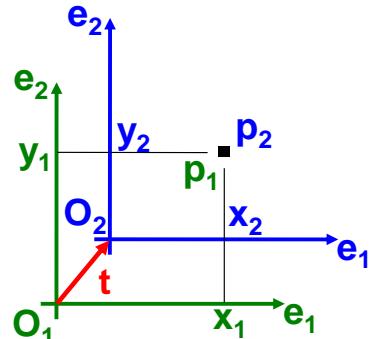
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Translacija koordinatnog sistema

$$C_1 = (O_1, \{e_1, e_2, e_3\}), \text{ u}$$

$$C_2 = (O_2, \{e_1, e_2, e_3\})$$



$$p_2 = p_1 - t, \text{ odnosno } p_2 = T(-t) p_1$$

translacija koord. početka za **t** odgovara translaciji objekata za **-t**

3D transformacije

... Transformacije prostora ...

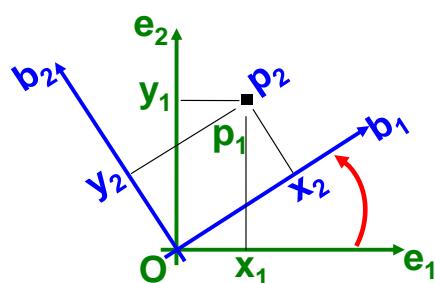
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Rotacija koordinatnog sistema

$$C_1 = (O, \{e_1, e_2, e_3\}), \text{ u}$$

$$C_2 = (O, \{b_1, b_2, b_3\})$$



$$p_2 = R(-\theta) p_1$$

3D transformacije

... Transformacije prostora ...

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Kako renderovati unutrašnjost auta dok Homer vozi napred, odnosno kada skreće?

Kako prikazivati ulice i zgrade Springfilda na vetrobranskom staklu dok Homer vozi napred, odnosno kada skreće?

Kako prikazivati scenu vožnje iz treće kamere?



3D transformacije

... Transformacije prostora ...

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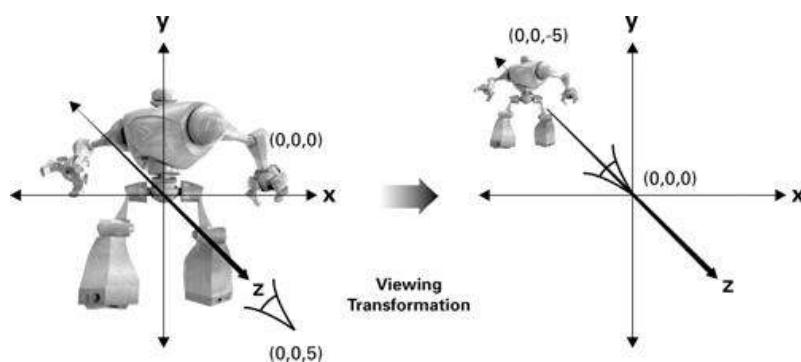


Primena transformacija koordinatnih sistema

view transform - WS → VS

$$(O_1, \{e_1, e_2, e_3\}) \rightarrow (O_2, \{b_1, b_2, b_3\})$$

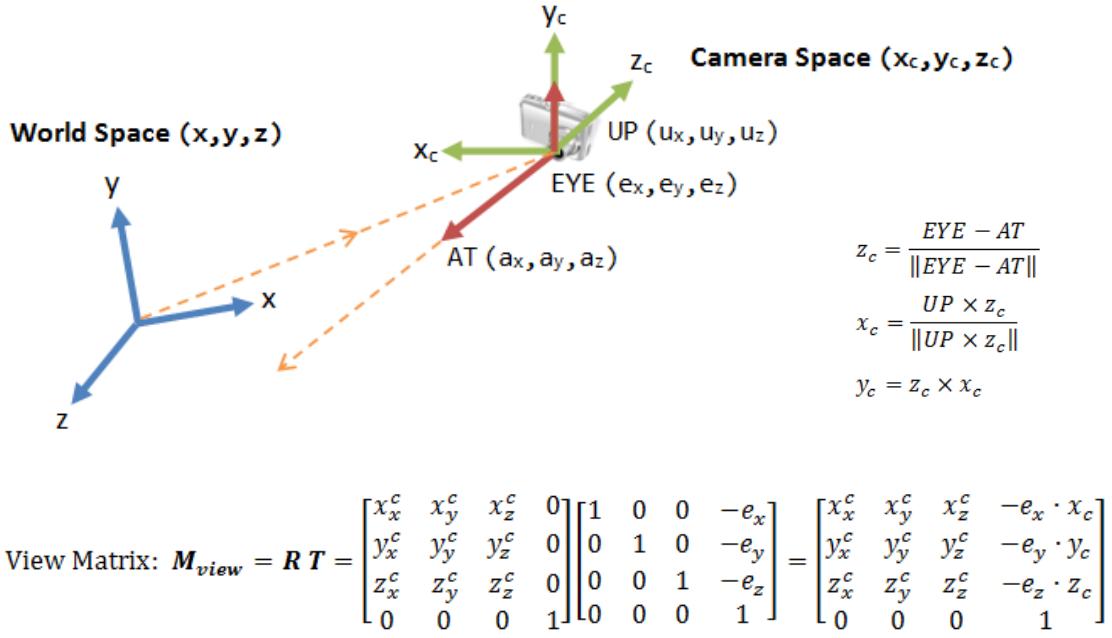
kompozicija T_{kamera} i R_{kamera} u komp. svaki objekat T_{kamera}^{-1} i R_{kamera}^{-1}



3D transformacije

Transformacije prostora

Apstrakcija kamere za ModelView transformaciju



Kako deo 3D prostora prikazati na 2D?

Moguće su dve strategije:

1. Raytracing algoritmima – non-real-time grafika?

Problem!

Moguća orto. projekcija?
Kako ubrzati? Kako utiče na pajplajn?

2. Matricama projekcione transformacije

PROJEKCIJA

projection pipeline,

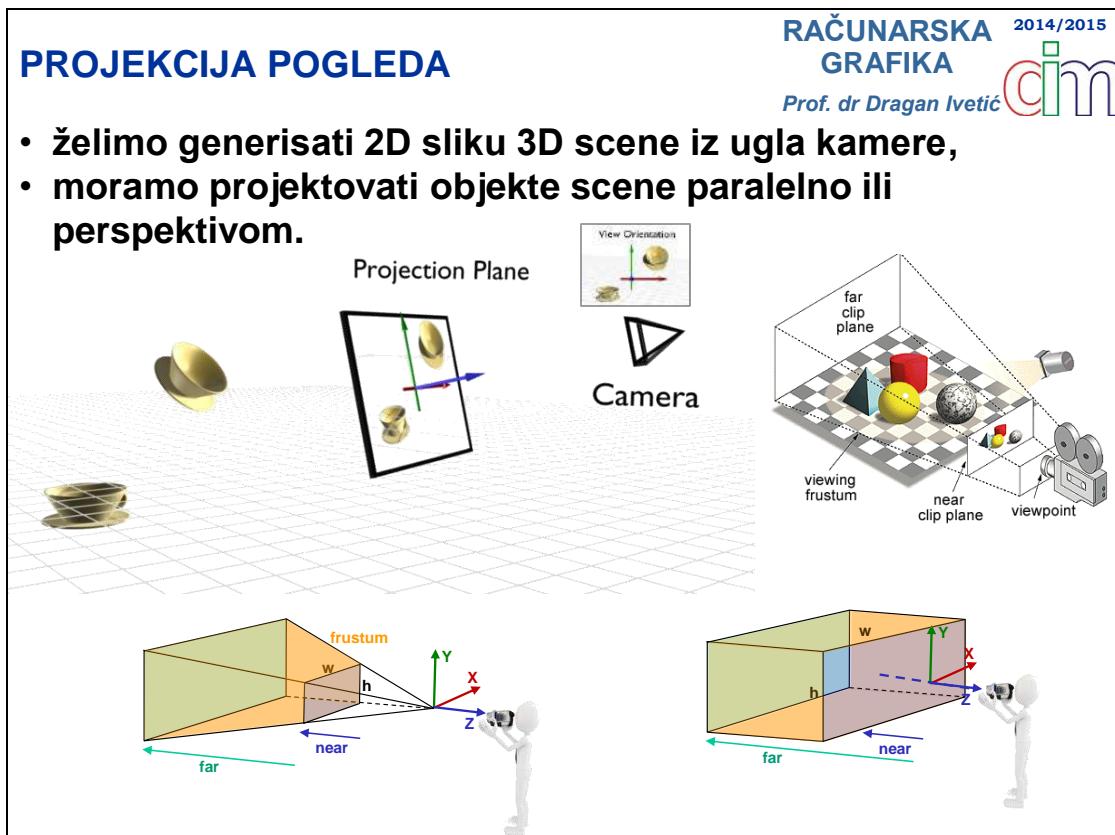
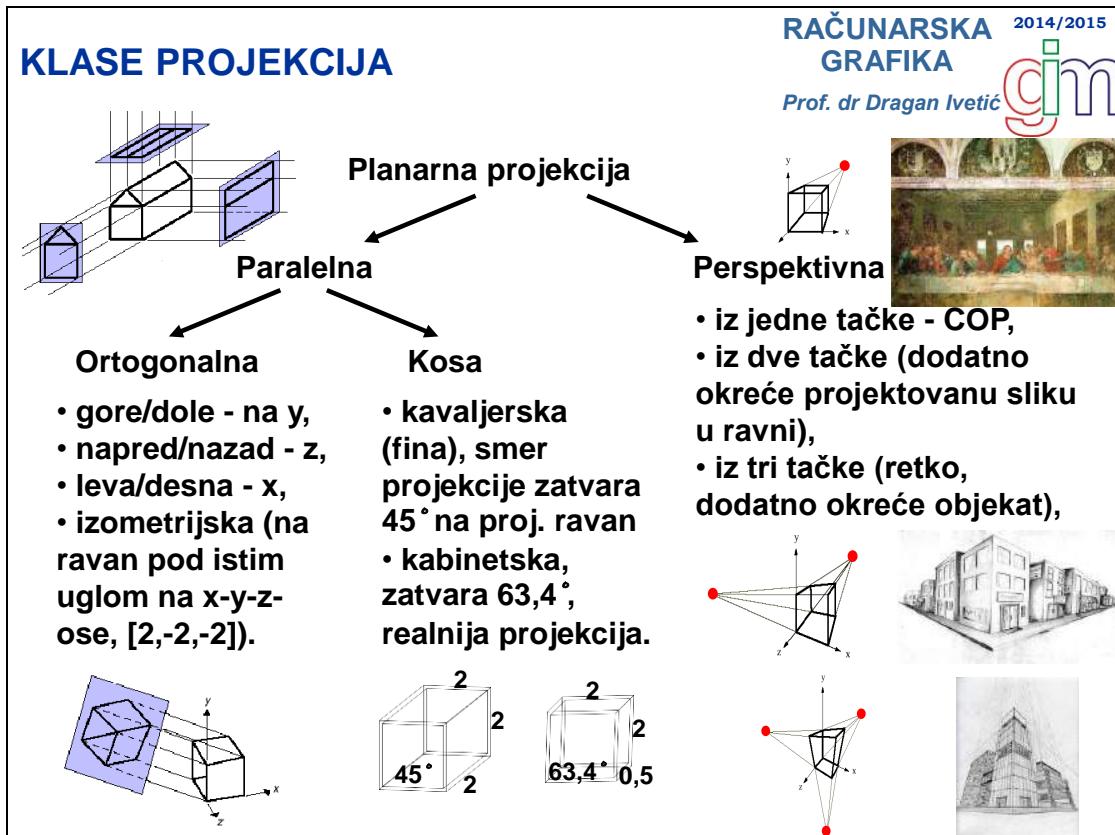
Koordinate modela

Koordinate pogleda

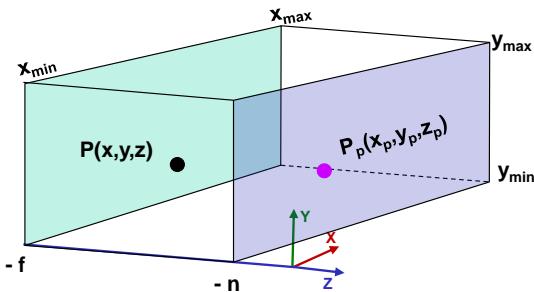
Normirane koordinate

Projektovane normirane koordinate

Koordinate prozora



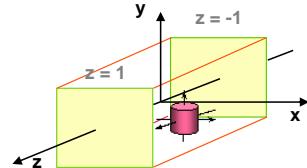
ORTOGONALNA PROJEKCIJA na projekcionu ravan



- bilo koju tačku $P(x,y,z)$ projektovati na front (-n),
- odrediti koordinate P_p
 x_p, y_p, z_p

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & d \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- uvedemo projekcionu ravan d: $0 \dots -f$,
- Kako na kraju svesti kuboid na normiranu kocku? Normirane koordinate



ORTOGONALNA PROJEKCIJA na normiranu kocku ...

- OpenGL, $[x_p, y_p, z_p, 1]^T = M_{OrthoNorm} [x, y, z, 1]^T$

$$M_{OrthoNorm} = \begin{bmatrix} \frac{2}{x_{\max} - x_{\min}} & 0 & 0 & 0 \\ 0 & \frac{2}{y_{\max} - y_{\min}} & 0 & 0 \\ 0 & 0 & -\frac{2}{f-n} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 & -\frac{(x_{\max} + x_{\min})}{2} \\ 0 & 1 & 0 & -\frac{(y_{\max} + y_{\min})}{2} \\ 0 & 0 & 1 & \frac{(f+n)}{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$M_{OrthoNorm} = \begin{bmatrix} \frac{2}{x_{\max} - x_{\min}} & 0 & 0 & -\frac{(x_{\max} + x_{\min})}{(x_{\max} - x_{\min})} \\ 0 & \frac{2}{y_{\max} - y_{\min}} & 0 & -\frac{(y_{\max} + y_{\min})}{(y_{\max} - y_{\min})} \\ 0 & 0 & -\frac{2}{f-n} & -\frac{(f+n)}{(f-n)} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

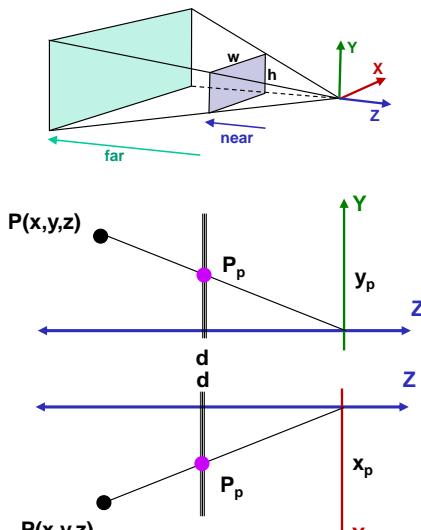
ORTOGONALNA PROJEKCIJA na normiranu kocku ...

- DirectX (LH sistem, max 1,1,1 i min -1,-1, 0)

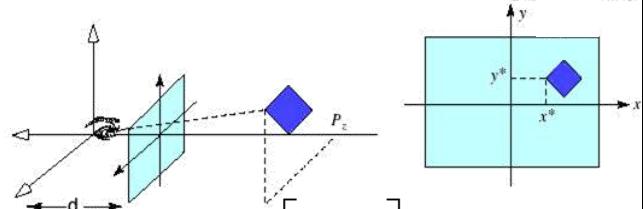
$$M_{OrtoNorm} = \begin{bmatrix} \frac{2}{x_{\max} - x_{\min}} & 0 & 0 & 0 \\ 0 & \frac{2}{y_{\max} - y_{\min}} & 0 & 0 \\ 0 & 0 & \frac{1}{f-n} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 & -(x_{\max} + x_{\min})/2 \\ 0 & 1 & 0 & -(y_{\max} + y_{\min})/2 \\ 0 & 0 & 1 & -n \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$M_{OrtoNorm} = \begin{bmatrix} \frac{2}{x_{\max} - x_{\min}} & 0 & 0 & -(x_{\max} + x_{\min})/(x_{\max} - x_{\min}) \\ 0 & \frac{2}{y_{\max} - y_{\min}} & 0 & -(y_{\max} + y_{\min})/(y_{\max} - y_{\min}) \\ 0 & 0 & \frac{1}{f-n} & -n/(f-n) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

PROJEKCIJA U PERSPEKTIVI na projekcionu ravan d



$$\begin{aligned} x_p &=? & \frac{x_p}{d} &= \frac{x}{-z}, & \frac{y_p}{d} &= \frac{y}{-z} \\ y_p &=? \end{aligned}$$



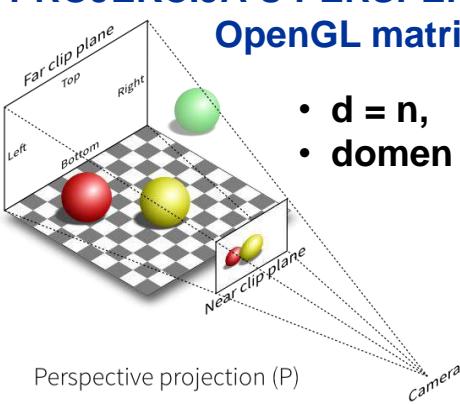
$$\begin{bmatrix} x_p \\ y_p \\ -d \\ 1 \end{bmatrix} = \begin{bmatrix} -d \frac{x}{z} \\ -d \frac{y}{z} \\ -d \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \\ -\frac{z}{d} \end{bmatrix}$$

$$M_{Persp} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -\frac{1}{d} & 0 \end{bmatrix}$$

PROJEKCIJA U PERSPEKTIVI

OpenGL matrica projekcije ...

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- $d = n$,
- domen x_p vrednosti $l \leq x_p \leq r$

$$0 \leq x_p - l \leq r - l$$

$$0 \leq \frac{x_p - l}{r - l} \leq 1 \xrightarrow{*2} 0 \leq 2 \frac{x_p - l}{r - l} \leq 2$$

$$\xrightarrow{-1} -1 \leq 2 \frac{x_p - l}{r - l} - 1 \leq 1 \longrightarrow -1 \leq \frac{2x_p - 2l - r + l}{r - l} \leq 1$$

$$\longrightarrow -1 \leq \frac{2x_p}{r - l} - \frac{r + l}{r - l} \leq 1 \xrightarrow{x_p = n \frac{x}{-z}} -1 \leq \frac{2nx}{-z(r - l)} - \frac{r + l}{r - l} \leq 1$$

- domen y_p vrednosti $b \leq y_p \leq t \longrightarrow -1 \leq \frac{2ny}{-z(t - b)} - \frac{t + b}{t - b} \leq 1$

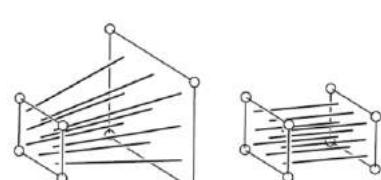
PROJEKCIJA U PERSPEKTIVI

... OpenGL matrica projekcije ...

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Kako domene $-1 \leq \frac{2nx}{-z(r - l)} - \frac{r + l}{r - l} \leq 1 \quad -1 \leq \frac{2ny}{-z(t - b)} - \frac{t + b}{t - b} \leq 1$

ugraditi u matricu projekcije?

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{2n}{r - l} & 0 & \frac{r + l}{r - l} & 0 \\ 0 & \frac{2n}{t - b} & \frac{t + b}{t - b} & 0 \\ 0 & 0 & A & B \\ 0 & 0 & -1 & 0 \end{bmatrix} * \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$


Kako ugraditi pseudo dubinu u matricu projekcije, z_p ?

$$z_p = \frac{A^* z + B}{-z}$$

PROJEKCIJA U PERSPEKTIVI

... OpenGL matrica projekcije

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- kako do a i b u pseudo_dubini?

$$\bullet \text{pseudo dubina} = -1 \text{ ako je } z = -n \text{ (near)} \quad -1 = \frac{A * (-n) + B}{n}$$

$$\bullet \text{pseudo dubina} = 1 \text{ ako je } z = -f \text{ (far)} \quad 1 = \frac{A * (-f) + B}{f}$$

$$A = \frac{-(f+n)}{f-n}$$

$$B = \frac{-2fn}{f-n}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix} * \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

CLIPPING

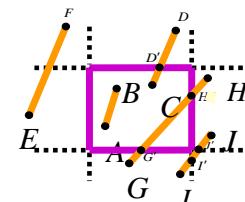
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- razlika u veličini generativne grafike i rezolucije prikaznog uređaja,
- clipping linije, poligona, kruga, teksta u 2D,
- slično u 3D samo je reč o clipping kocki,



Mogući pristupi:

1.analitički - previše uzaludnog rada za mali (veliki) clipping prozor,

2.algoritamski - logičko usecanje prema graničnim pravama i/ili ravnima, radimo prvo 2D pa onda 3D:

Cohen-Sutherland-ov algoritam, linija,

Sutherland-Hodgman-ov algoritam, poligon.

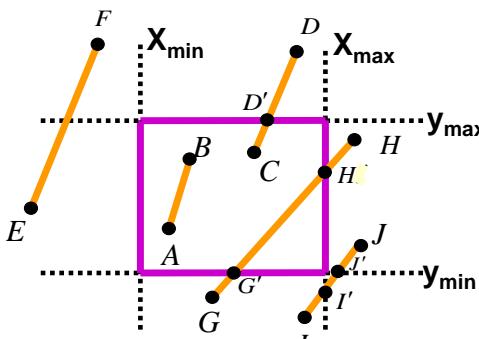
CLIPPING

Opšta ideja algoritma:

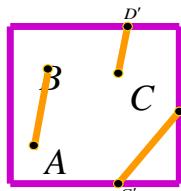
1. prihvati trivijalno unutru, i odbaci trivijalno spoljašnje linije,

$X_{\text{maxLinija}} < X_{\text{max}}$, $X_{\text{minLinija}} > X_{\text{min}}$, $Y_{\text{maxLinija}} < Y_{\text{max}}$, $Y_{\text{minLinija}} > Y_{\text{min}}$
kako?

**2. prihvati delove ostalih linija koje se nalaze unutar prozora,
podela na (pri) horizontalnim (vertikalnim) linijama,**



Implementacija?

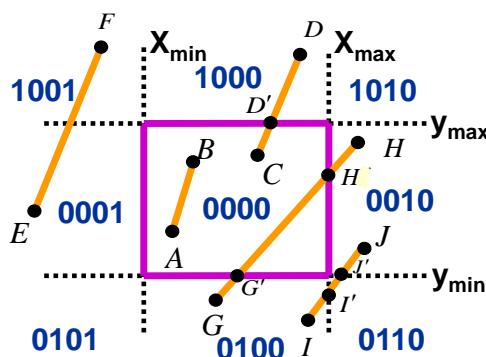


Koliko selekcija?

Vreme izvršavanja?

CLIPPING

- pametna podela ravni i njihovo kodiranje tetrada,**
- do tetrade šifovanjem uлево predznaka ($y_{\text{max}}-y$) па ($y-y_{\text{min}}$)
па ($x_{\text{max}}-x$) и ($x-x_{\text{min}}$), tj. iznad, ispod, udesno i uлево,**



- linija EF ima tetrade (0001, 1001),**
- kako jednostavno detektovati trivijalno prihvativljive,
odnosno neprihvativljive linije?**

CLIPPING

... Cohen-Sutherland

- trivialno neprihvatljiv je ($tetrađa_A \text{ and } tetrađa_B \neq 0$), a trivialno prihvatljiv?
- kako preostale linije?

npr. GH → 0100 and 0010 = 0000, pa se deli na

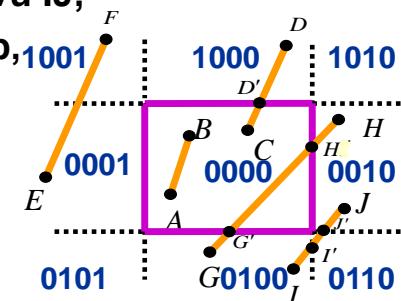
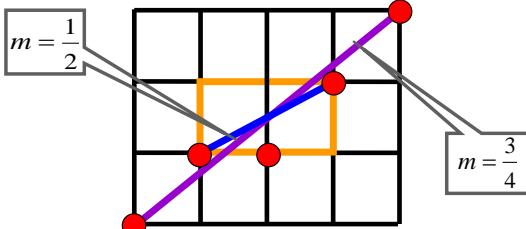
$GG' \rightarrow 0100 \text{ and } 0100 = 0100$, trivialno neprihvatljiv,

$G'_+ H' \rightarrow 0000 \text{ i } 0000$, trivialno prihvatljiv pa u $G'H'$,

$H'_+ H \rightarrow 0010 \text{ and } 0010 = 0010$, trivialno neprihvatljiv,

- nedostatak algoritma je račun za pravu IJ,

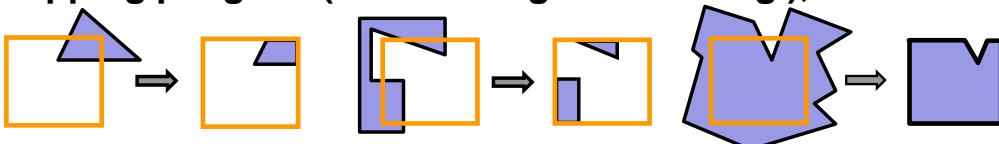
- ukrojena kriva može imati drugi nagib, 1001



CLIPPING

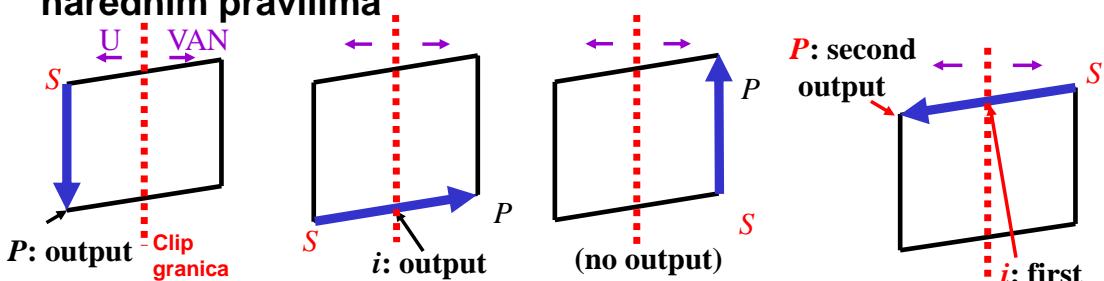
Sutherland-Hodgman ...

- clipping poligona (konveksnog i konkavnog),



Opšta ideja algoritma:

- Clip prema beskonačnim graničnim linijama prema narednim pravilima



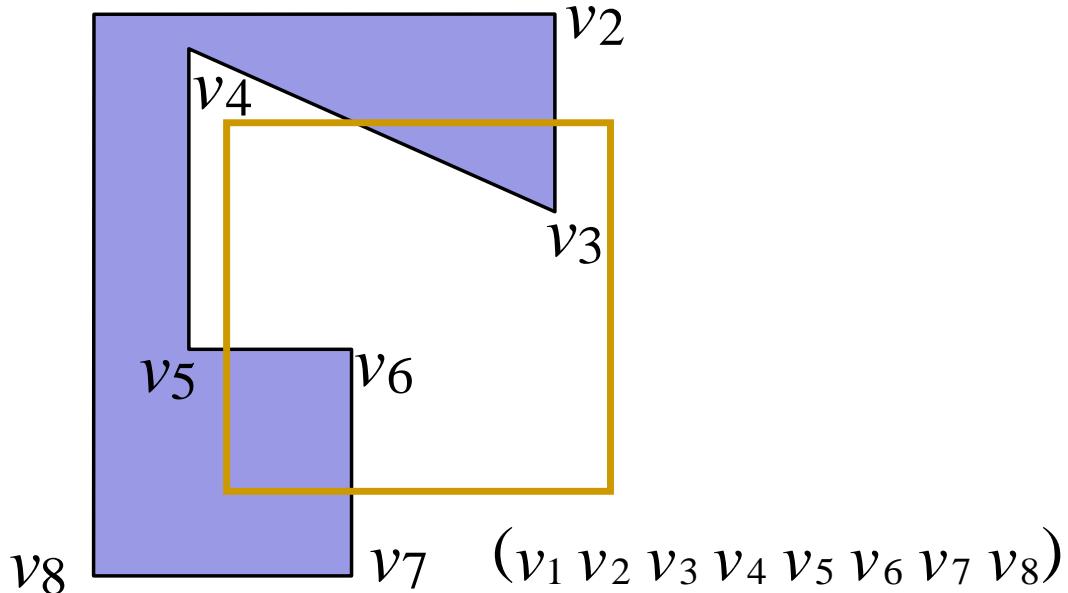
- vektor tačaka poligona $t_1..t_N$ se menja svakim prolazom za svaku graničnu liniju (obično 4),

CLIPPING

... Sutherland-Hodgman ...

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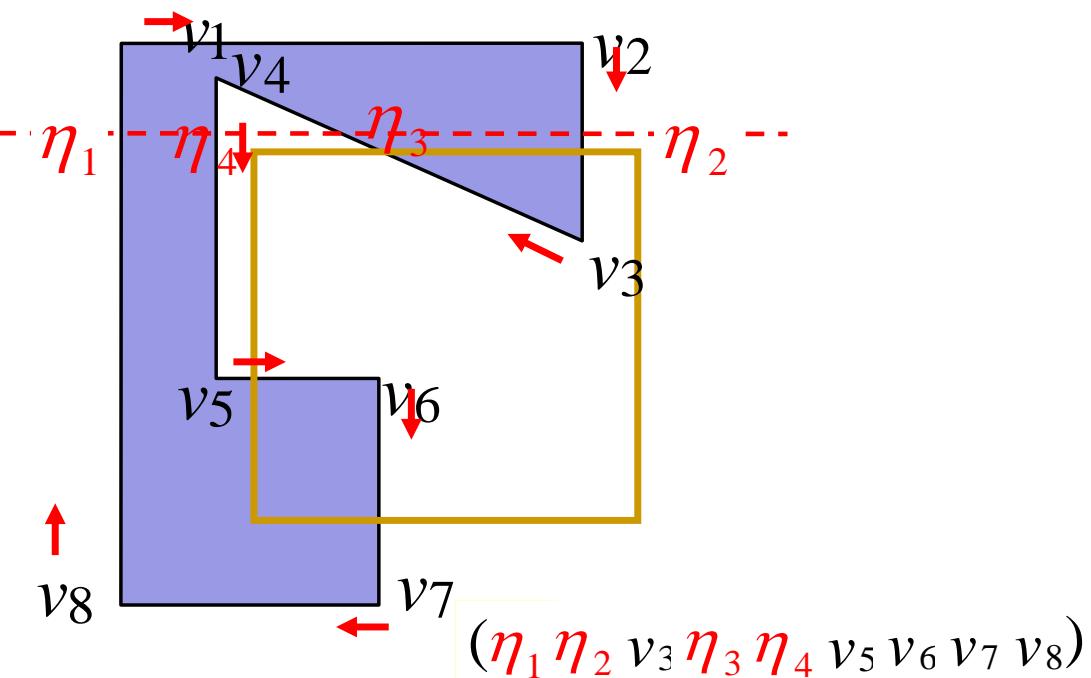


CLIPPING

... Sutherland-Hodgman ...

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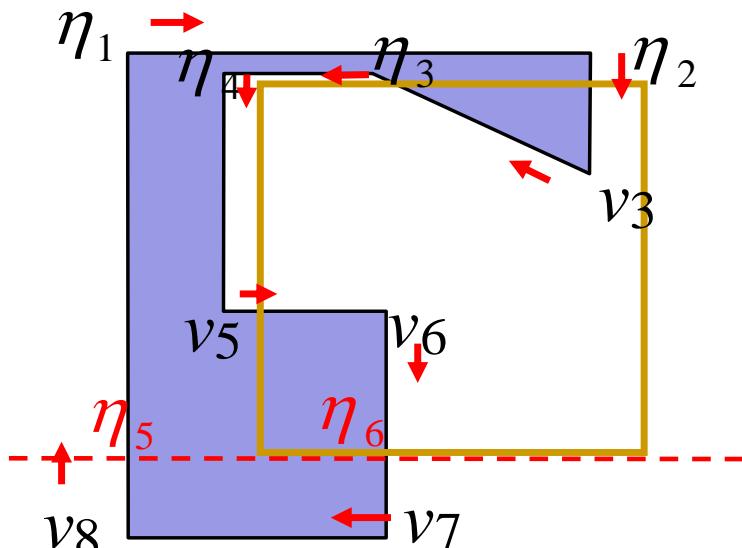


CLIPPING

... Sutherland-Hodgman ...

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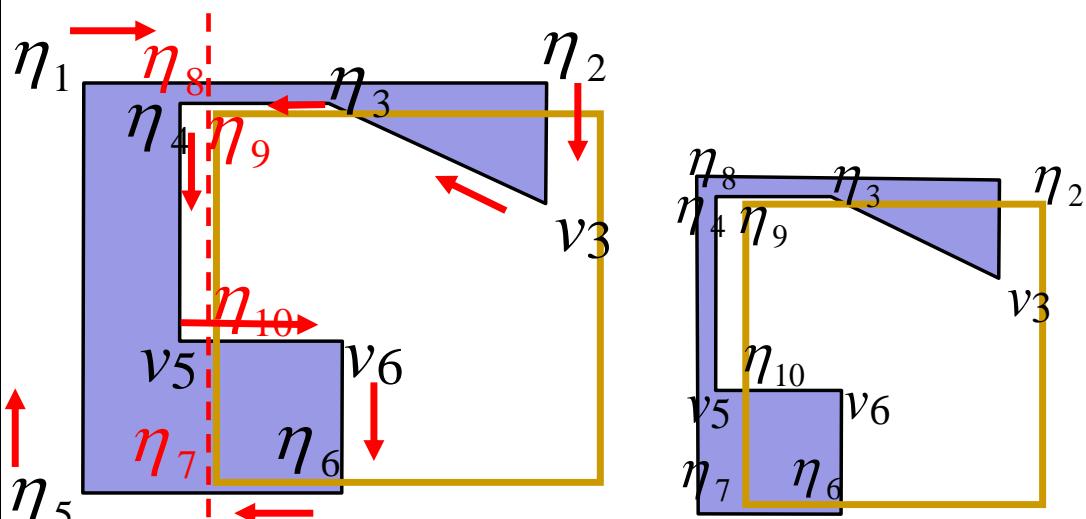
$(\eta_5 \eta_1 \eta_2 v_3 \eta_3 \eta_4 v_5 v_6 \eta_6)$

CLIPPING

... Sutherland-Hodgman

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$(\eta_7 \eta_8 \eta_2 v_3 \eta_3 \eta_9 \eta_{10} v_6)$

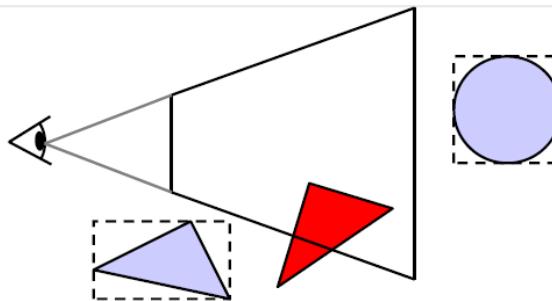
3D CLIPPING

v.s. culling

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Culling:

- odbacivanje prema graničnom volumenu,
- scena = hijerarhija graničnih volumena.

Clipping:

- parcijalno vidljivi objekti se moraju iskrojiti prema datom volumenu.

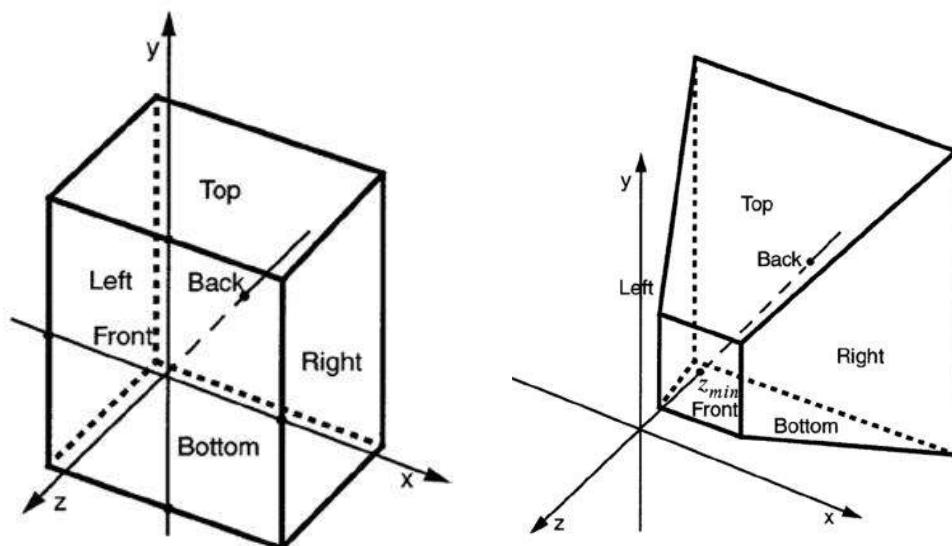
3D CLIPPING

i volumeni gledanja

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3D CLIPPING

Cohen-Sutherland

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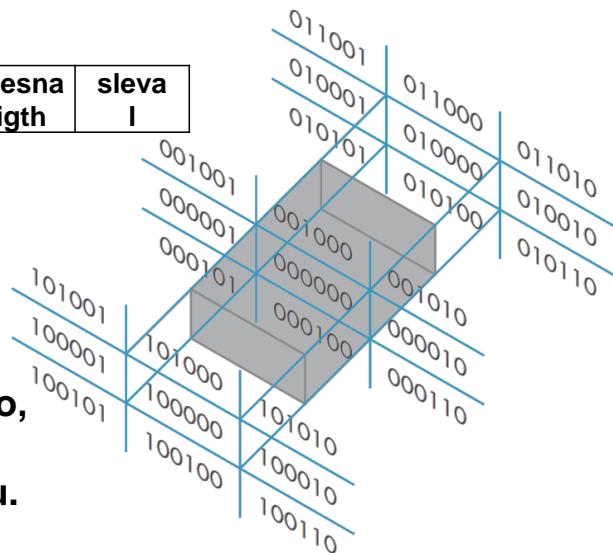
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2014/2015

**4-bitovski 2D algoritam (9 podravni) proširen na
6-bitovski 3D algoritam (27 potprostora).**

ispred front	iza back	iznad top	ispod bottom	sdesna rigth	sleva I
-----------------	-------------	--------------	-----------------	-----------------	------------



Nadalje kao u 2D:

**a == b == 0 unutra trivijalno,
a & b == 0 moguće unutra,
a & b != 0 trivijalno napolju.**

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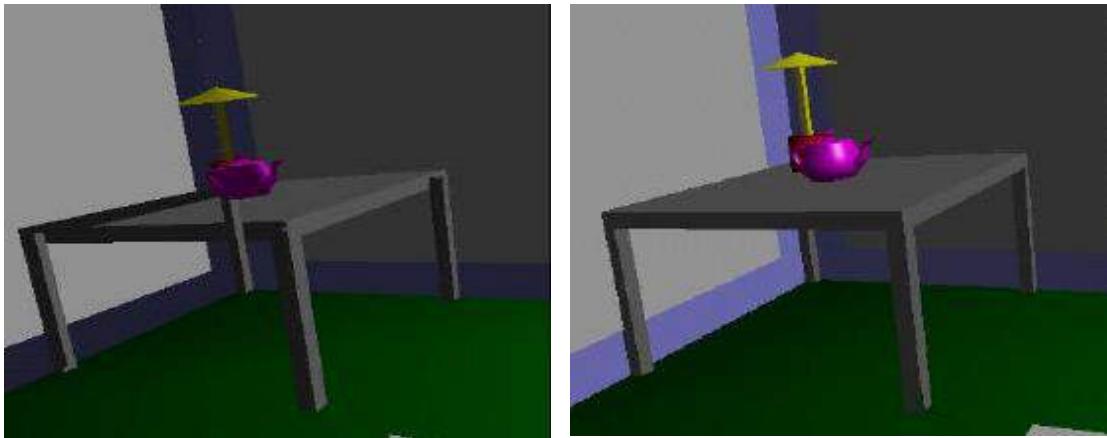
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Zašto? ...

Prof. dr Dragan Ivetić



- nisu vidljive baš sve površine na sceni,
- trošiti GPU na njih?
- realnost?



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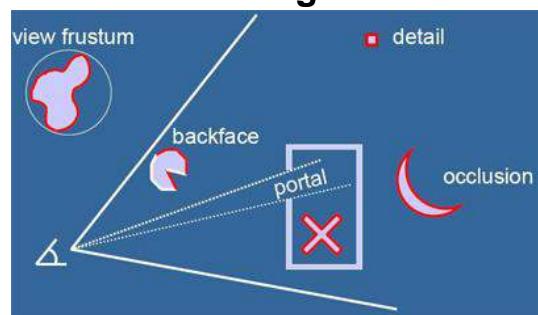
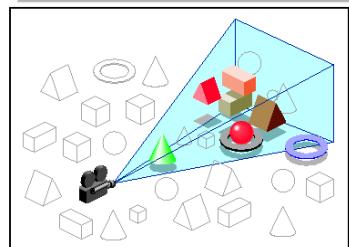
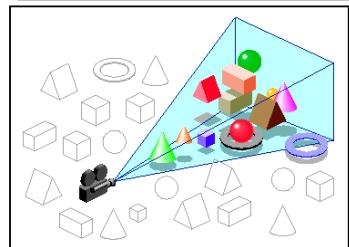
2012/2013

... Zašto?

Prof. dr Dragan Ivetić



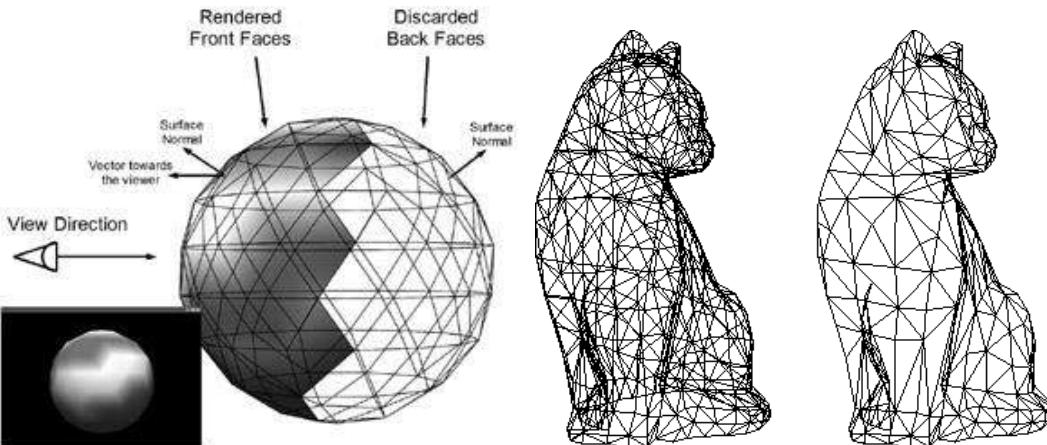
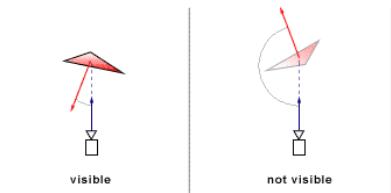
- površina postaje nevidljiva (hidden surface removal) jer je:
 - van vidnog polja viewing frustum culling,
 - pripada pozadini objekta back face culling,
 - je zaklanja jedan ili više objekata koji su bliži posmatraču occlusion culling.



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Back face culling

- ne prikazati površinu koja “gleda” u istom smeru kao i kamera,
- formalnije prikazati površinu akko $V_{\text{kamere}} \neq 0$? $N_{\text{površine}} \neq 0$.



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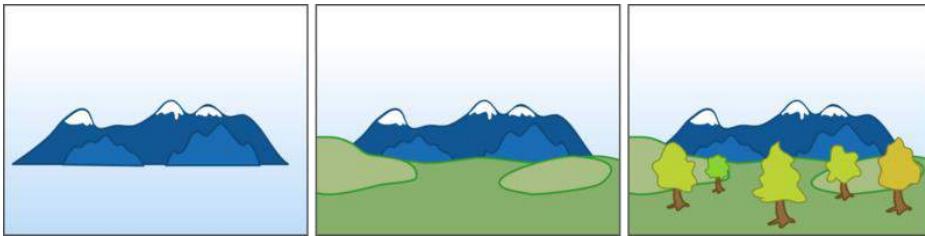
Algoritmi za uklanjanje skrivenih površina

- da uklone (deo) površine koje su zaklonjene drugom/drugim površinama,
- pre rasterizacije temena - Object-space techniques
 - Painter’s algorithm,
 - BSP trees,
 - portal culling,
- posle rasterizacije temena - Image-space techniques
 - Z – buffer,
 - α – buffer,
 - ray tracing.

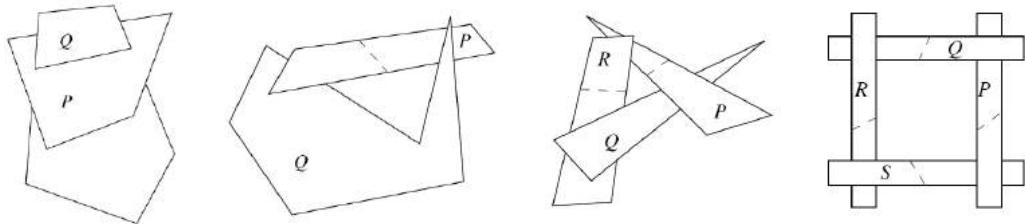
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Painter's algorithm

- prikazivanje površina od pozadinskih prema frontalnim,



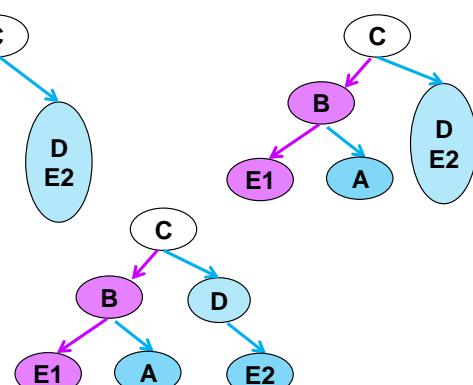
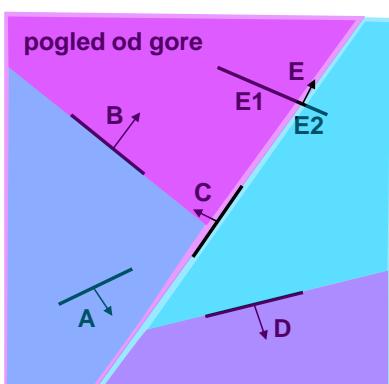
- podržava transparentnost,
- problemi sa sortiranjem površina (broj, pozicija kamere...).



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BSP stablo ...

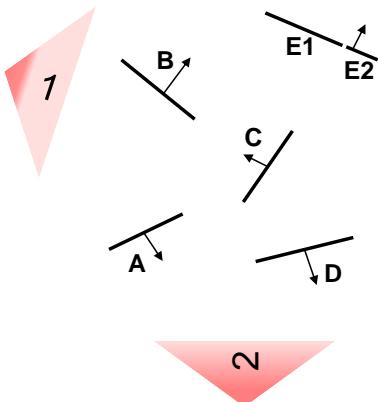
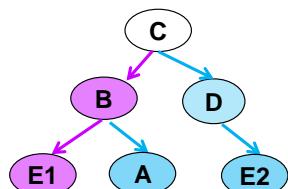
- Binary Space Partitioning tree,
- prostor se deli na **ispred** / **iza** ravni koja sadrži poligon,
- ako ravan preseca neki drugi poligon, on se deli na dva potpoligona...,
- nastaviti dok svaki čvor stabla bude jedan poligon,
- takvo stablo će definisati redosled prikaza poligona,



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... BSP stablo

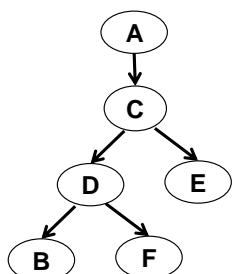
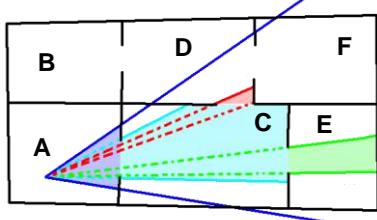
- kako prolaziti kroz stablo do liste redosleda prikaza?
- gledalac ispred → potprostor desnog podstabla, koren, potprostor levog podstabla,
- gledalac iza → potprostor levog podstabla, koren, potprostor desnog podstabla,
- gledalac na granici → ?
- gledalac 1 → D E2 C E1 B A,
- gledalac 2 → ?



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Portal culling

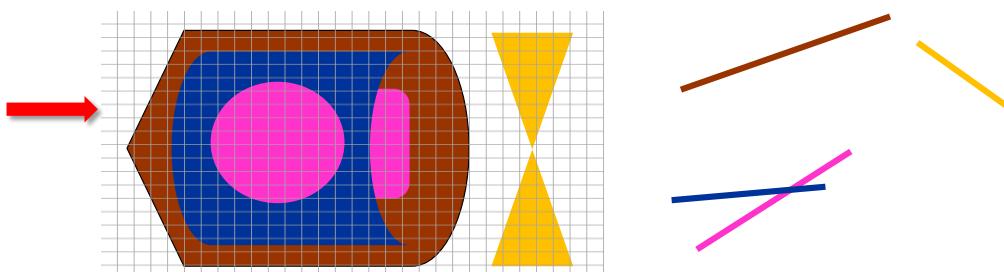
- zasnovan na grafu ćelija i portala (vrata),
- prvo se renderuje ćelija gde je posmatrač, pa onda onoliko koliko se vidi kroz portale...



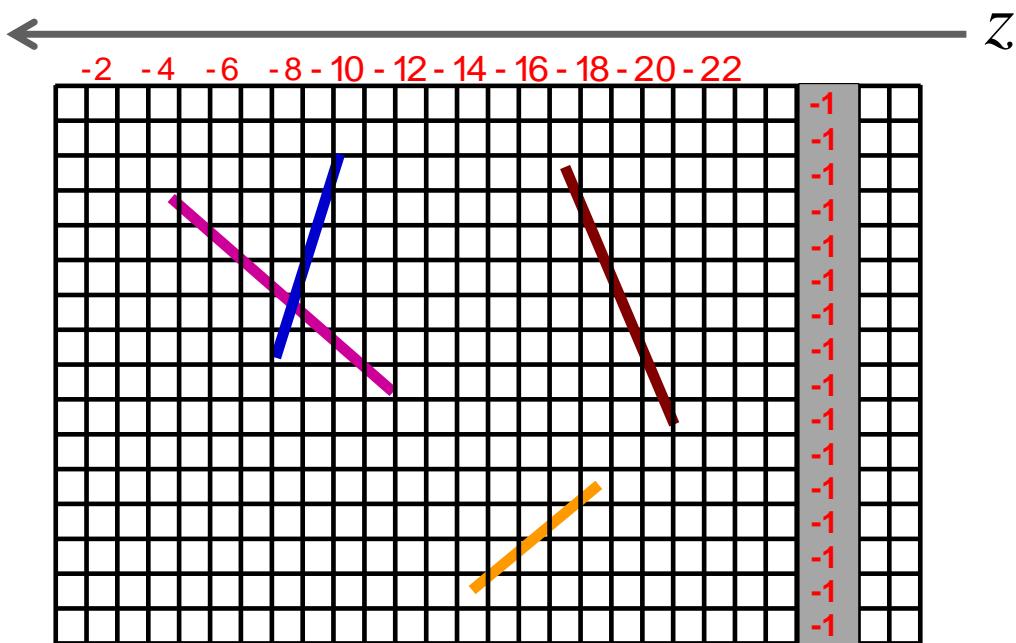
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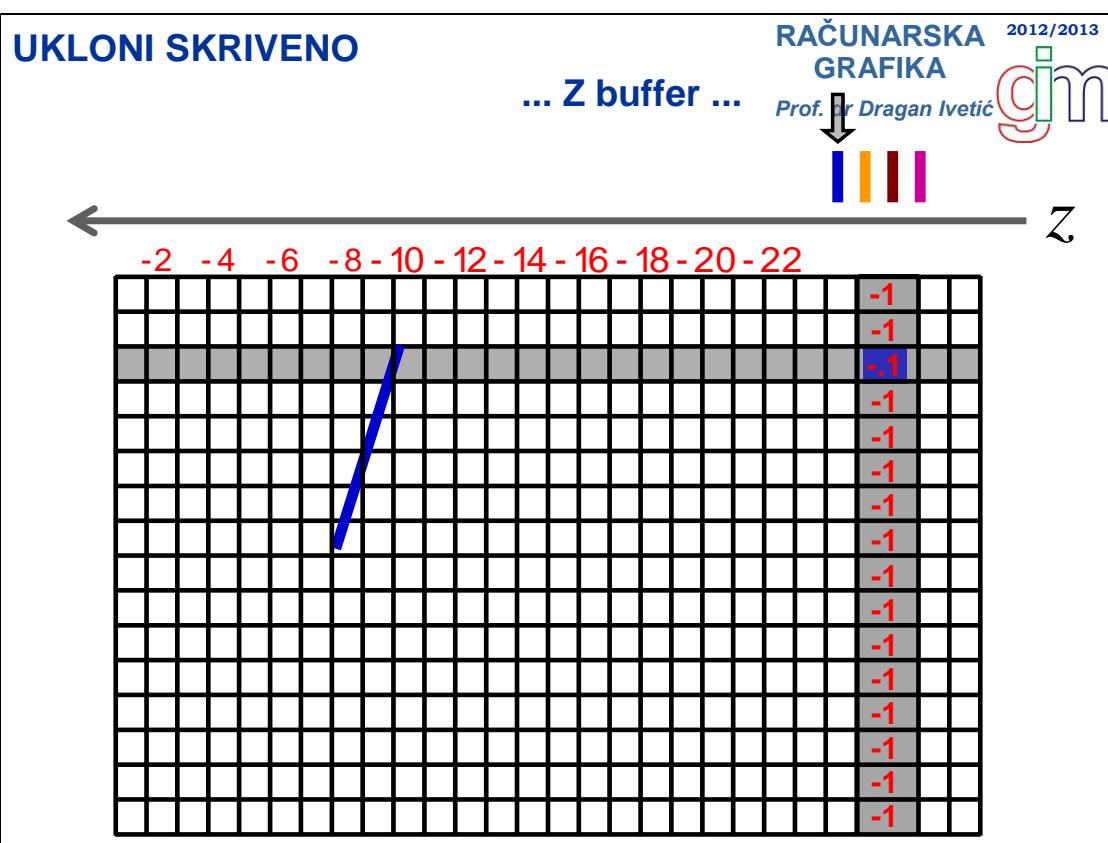
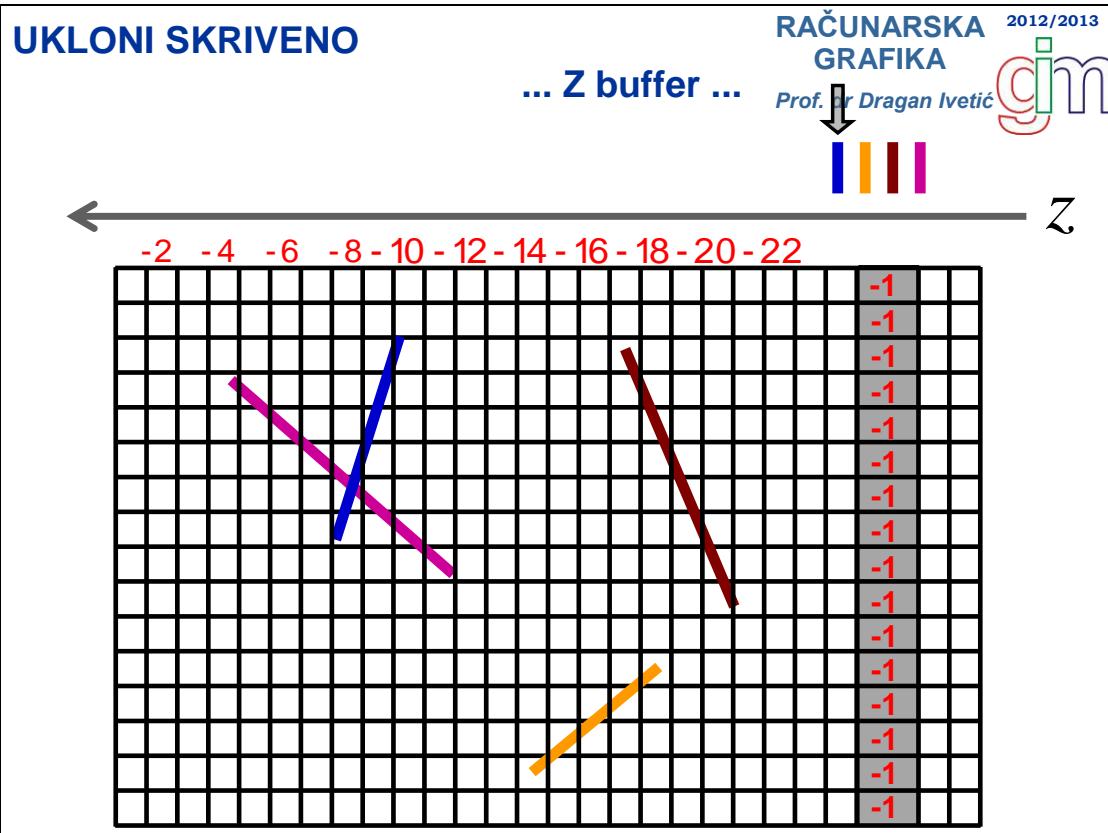
- image-space tehnika,
- osnovna ideja Z-buffer:

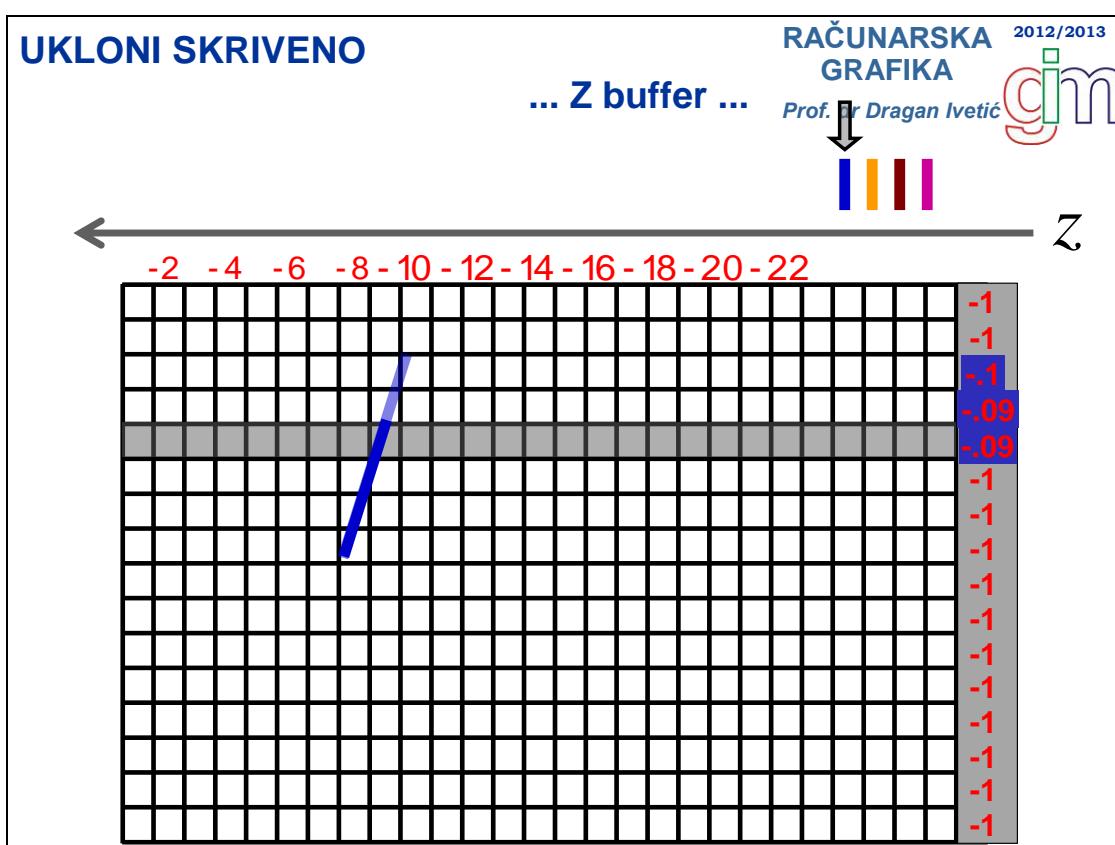
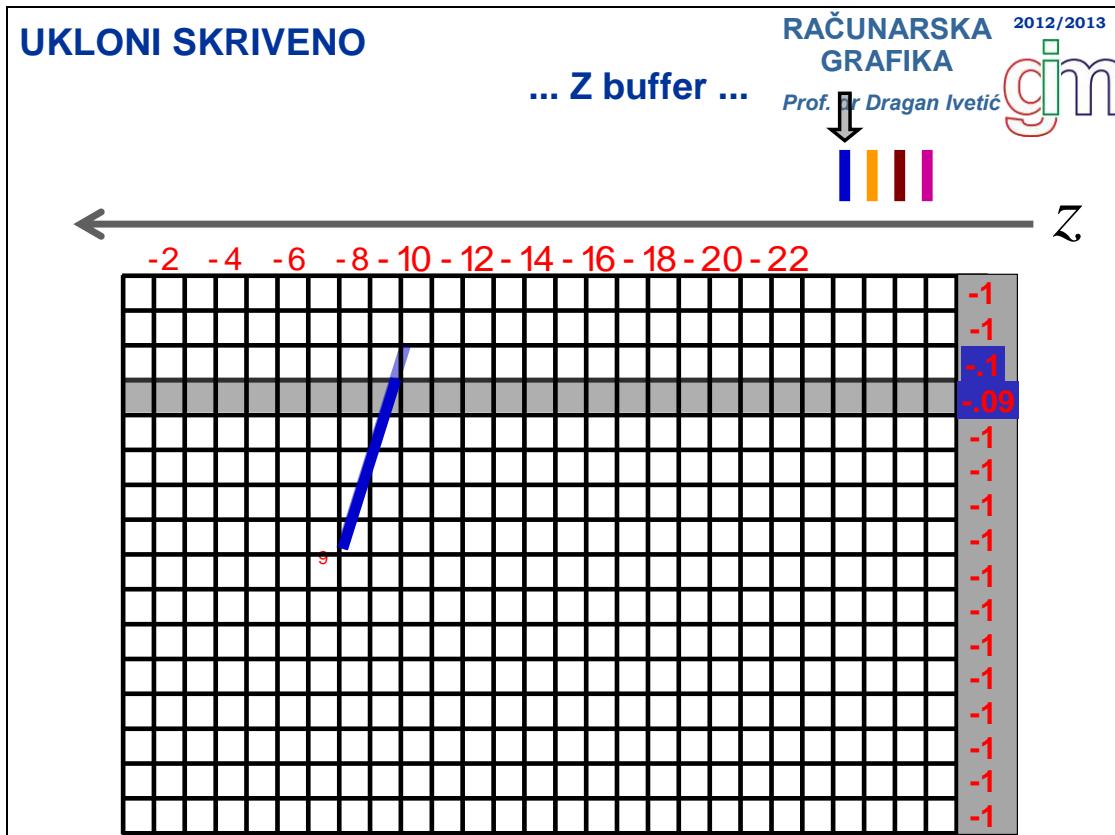
- inicijalno Z-buffer elementi na -1,
- rasterizuj svaki ulazni poligon,
 - za svaki piksel interijera, interpoliraj njegov Z,
 - upiši (Z vrednost i) boju u njegov deo bafera akko je Z veća od postojeće u baferu,
- prikaži vrednosti boja iz bafera.



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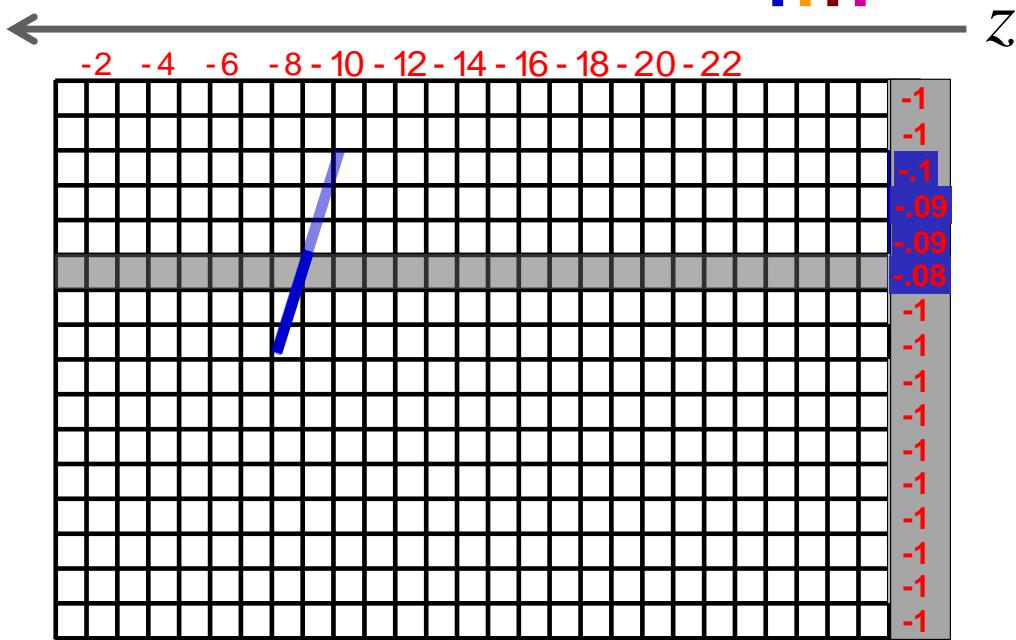
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... Z buffer ...

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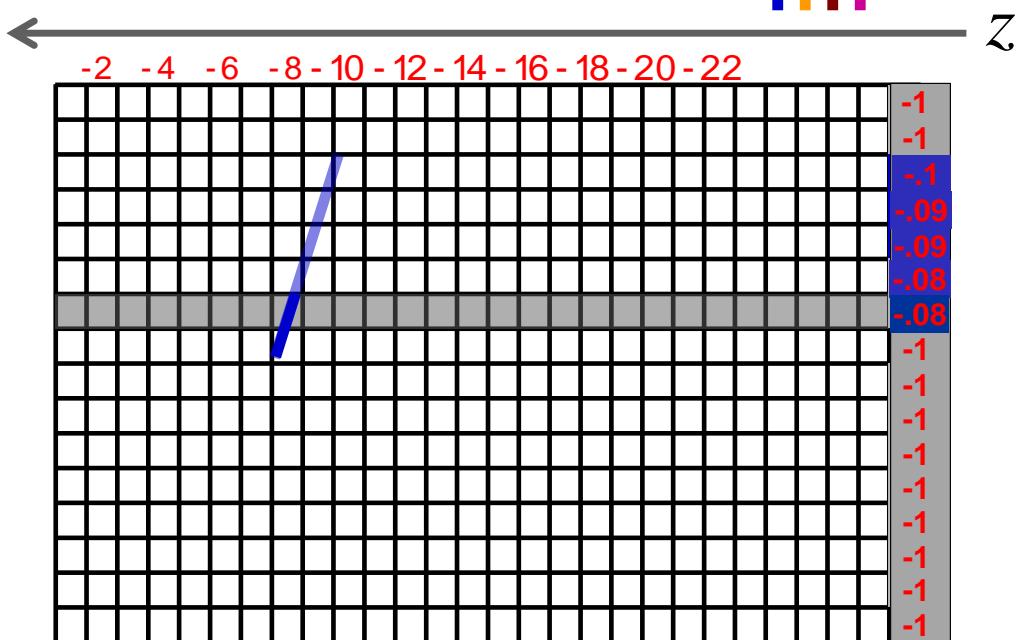
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... Z buffer ...

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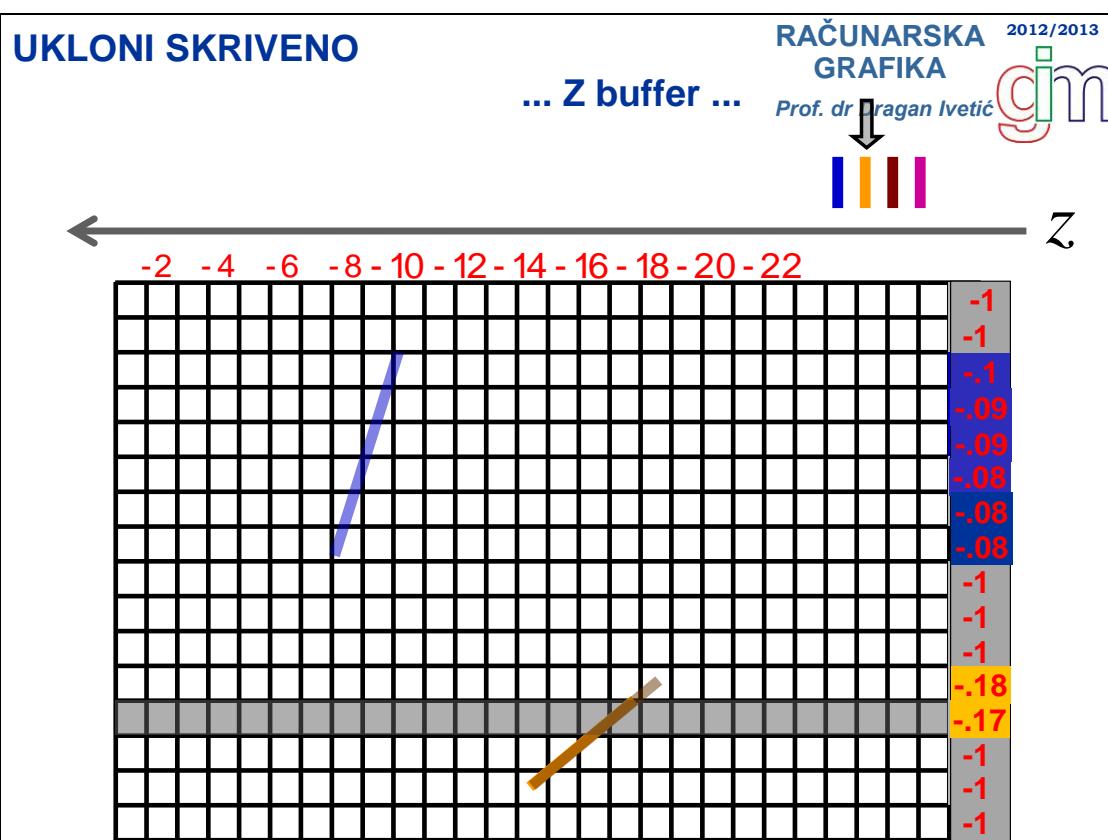
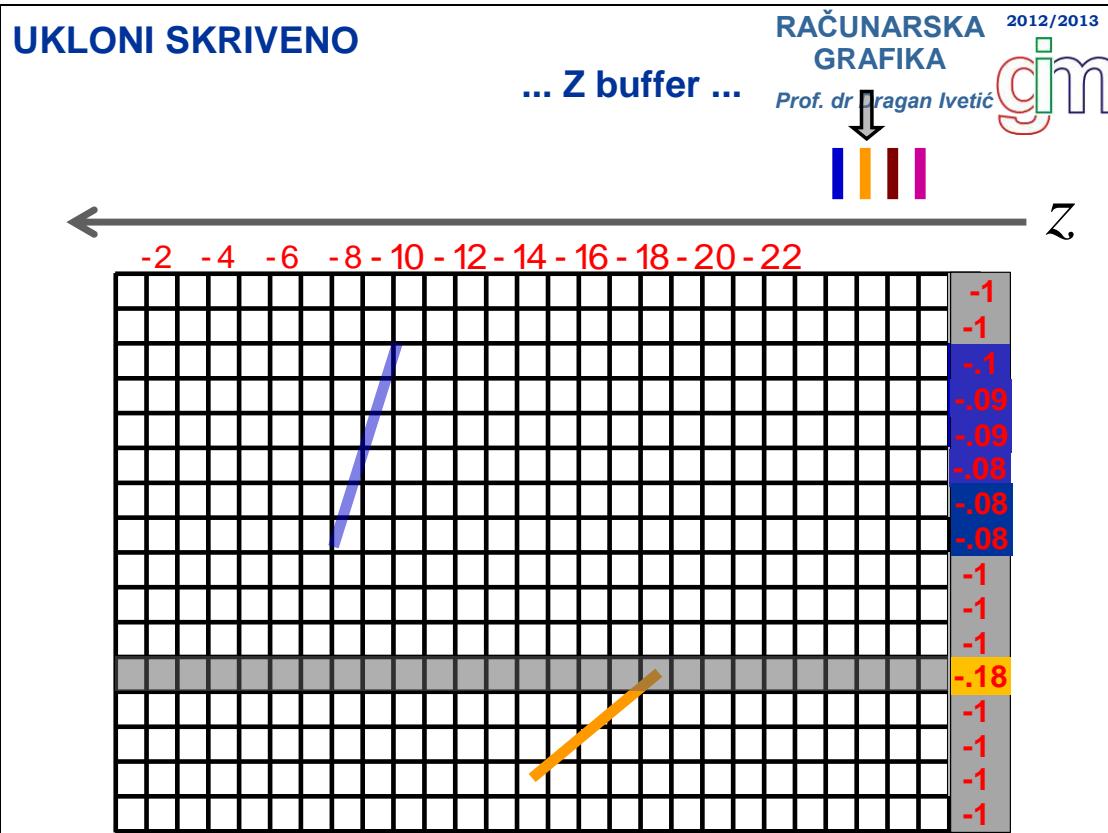


The diagram shows a 2D grid representing a frame buffer. A horizontal axis at the top is labeled "Z" with tick marks and numerical values from -2 to -22. To the left of the grid is a vertical arrow pointing downwards, indicating the depth direction. The grid itself is composed of small squares. A thick blue diagonal line starts from the bottom-left and extends towards the top-right. This line passes through several grid squares. To the right of the grid, there is a vertical column of gray boxes, each containing a numerical value. The values are as follows:

-1
-1
.1
-.09
-.09
-.08
-.08
-.08
-.08
-1
-1
-1
-1
-1
-1
-1
-1

The values represent depth information stored in the Z buffer. The "-1" values indicate that the corresponding grid squares are not visible because they are behind the blue line, while the other values represent the depth of the blue line.

The diagram shows a 2D grid representing a screen or frame buffer. The horizontal axis is labeled z and has tick marks from -2 to -22. The vertical axis has an arrow pointing left. A vertical column of 16 gray boxes on the right represents the **Z buffer**. The first two boxes are filled with the value -1. The next four boxes are filled with -.1. The following four boxes are filled with -.09. The next four boxes are filled with -.08. The last two boxes are filled with -.07. Four lines are drawn across the grid: a magenta line from (-4, -1) to (-1, -6), a blue line from (-8, -1) to (-1, -14), a dark red line from (-14, -1) to (-1, -19), and an orange line from (-18, -1) to (-1, -21). The magenta and blue lines overlap, while the dark red and orange lines overlap.



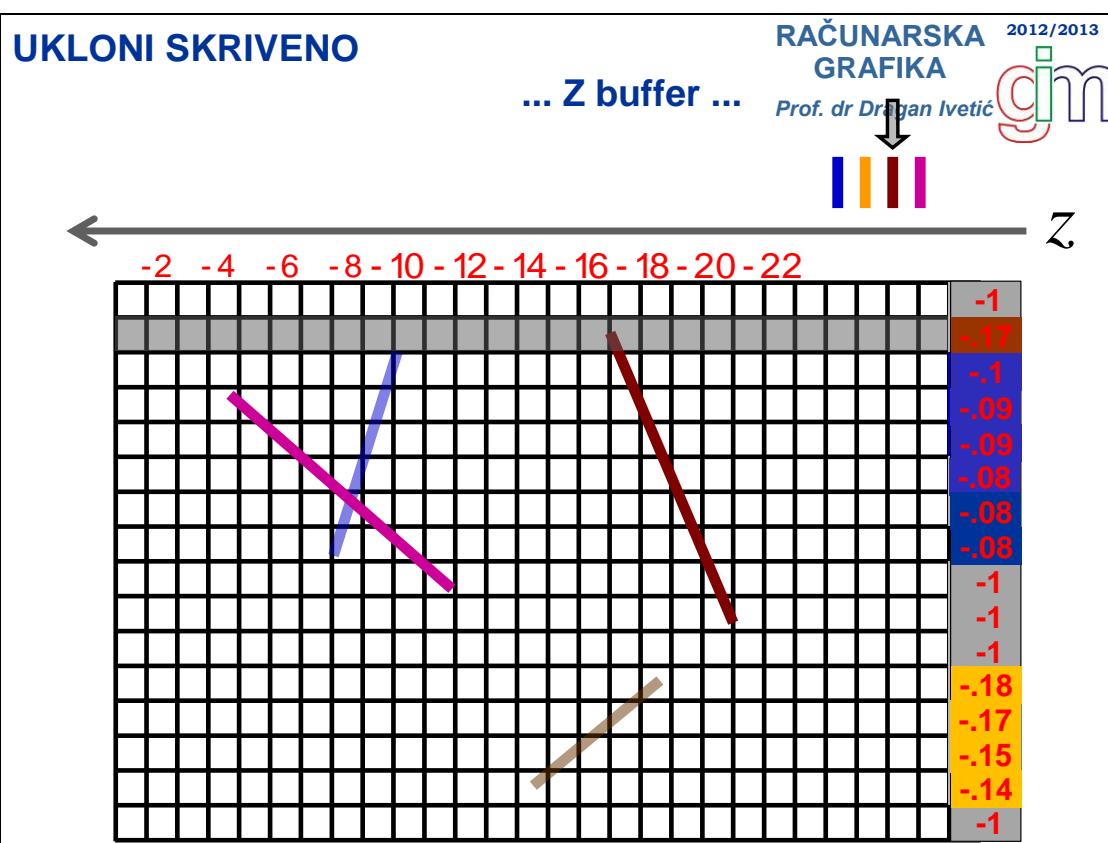
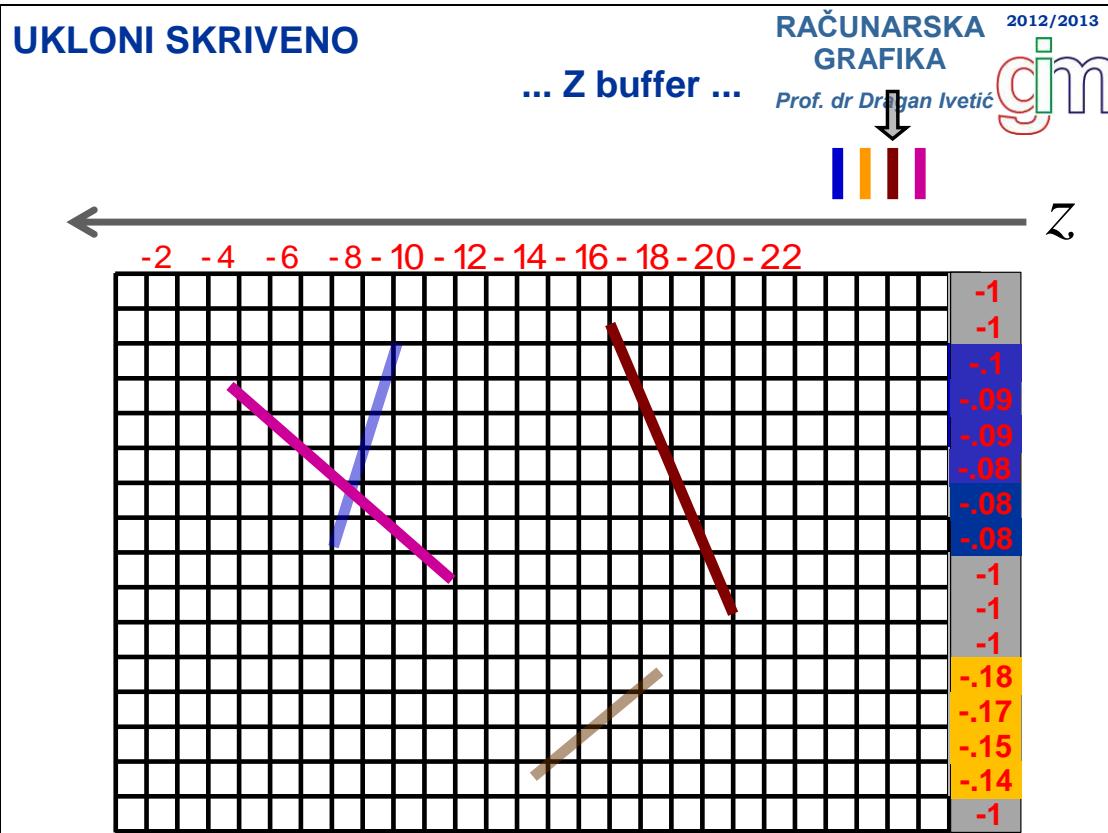
The diagram shows a 2D grid representing a frame buffer. A horizontal axis at the top is labeled Z and has tick marks from -2 to -22. To the left of the grid is a vertical arrow pointing downwards. The grid itself is composed of small squares. On the right side of the grid, there is a vertical column of color-coded numbers representing depth values. The colors range from dark blue (-1) at the top to yellow (-18) at the bottom. The numbers are: -1, -1, -.1, -.09, -.09, -.08, -.08, -.08, -.08, -.1, -.1, -.1, -.1, -.18, -.17, -.15, -1, -1.

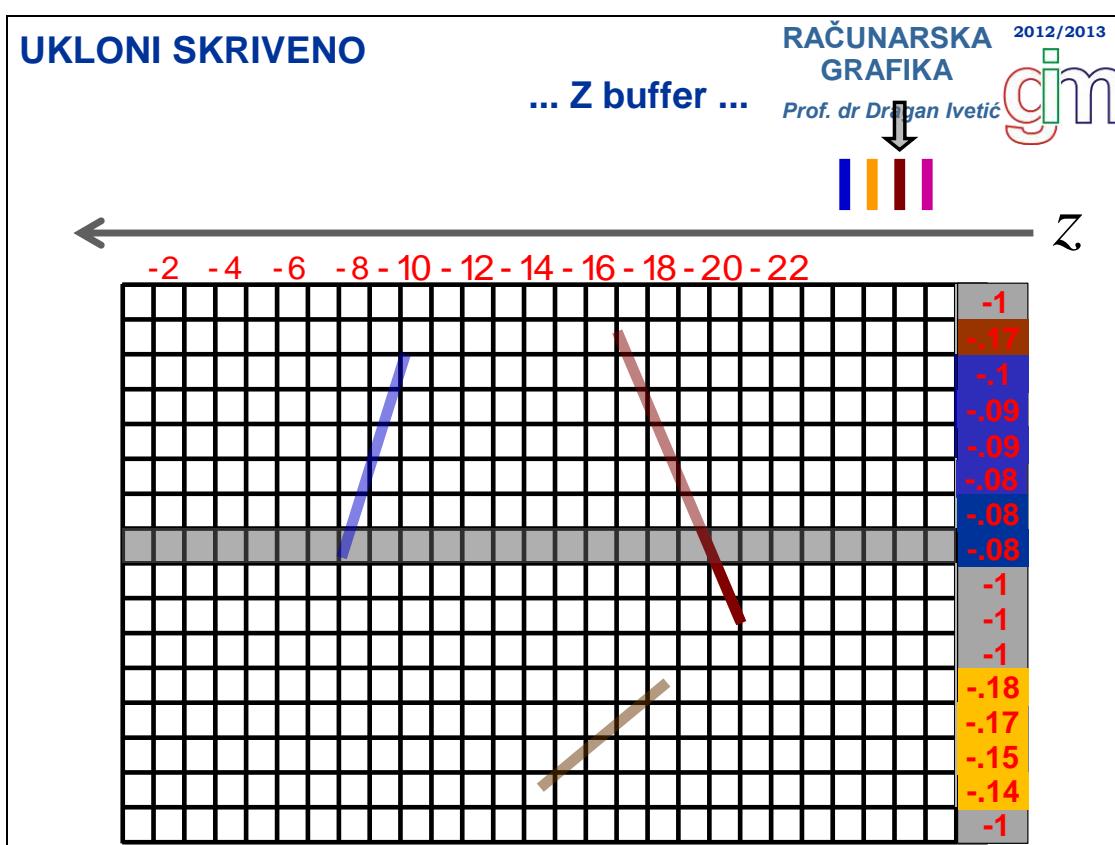
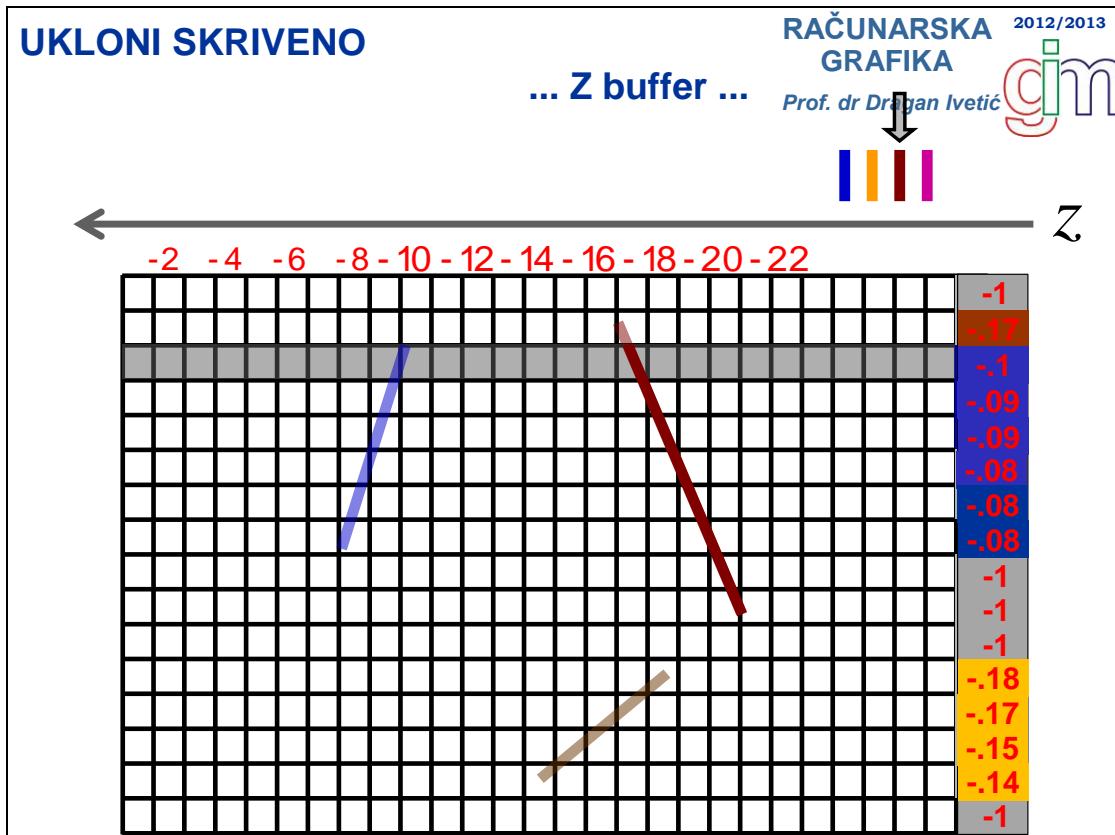
The diagram shows a 2D grid representing a frame buffer. The horizontal axis is labeled Z and has tick marks from -2 to -22. The vertical axis has an arrow pointing left. The grid is divided into four color-coded regions:

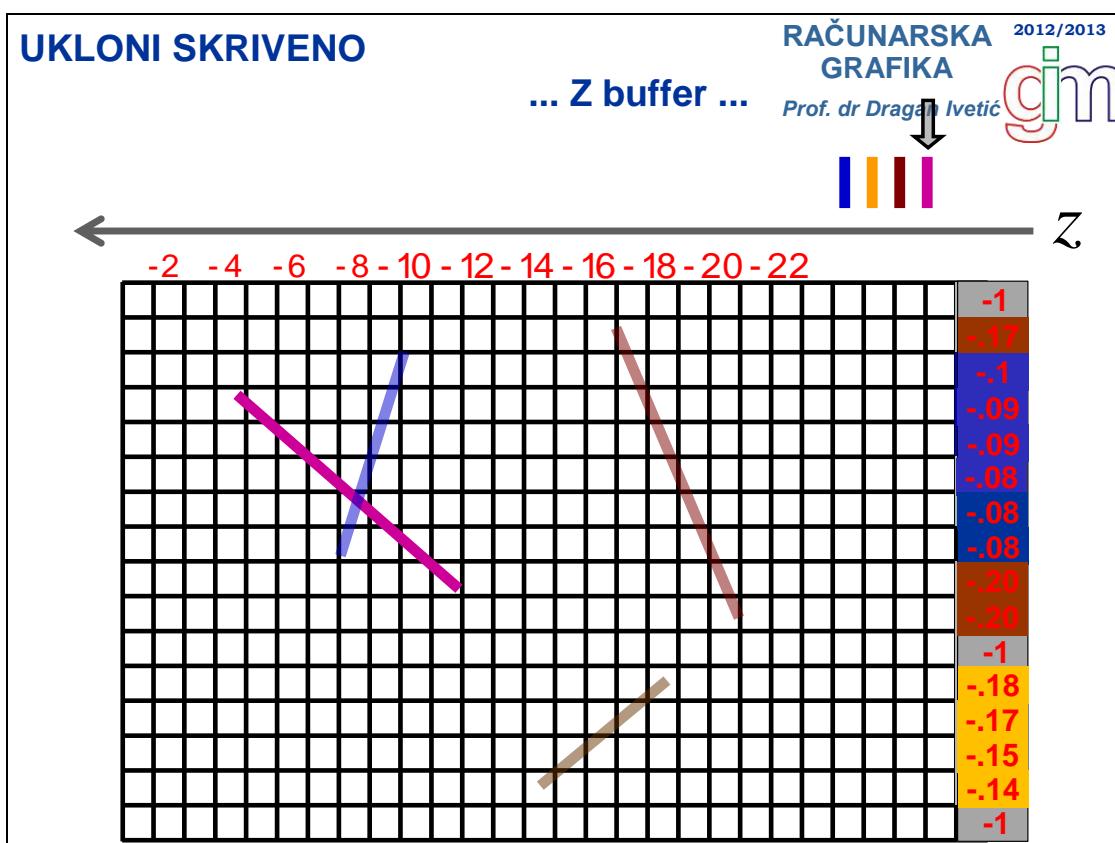
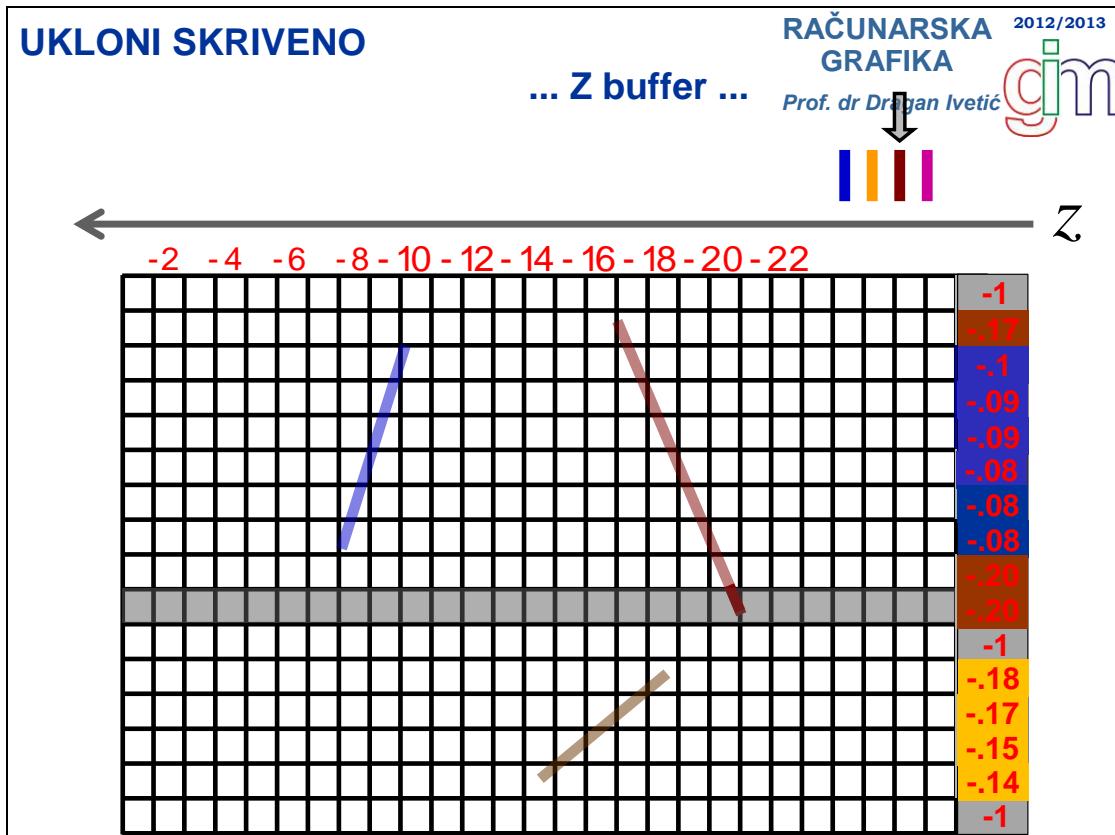
- Blue Region (Top Left):** Contains a blue diagonal line segment.
- Yellow Region (Bottom Left):** Contains a brown diagonal line segment.
- Grey Region (Bottom):** A horizontal band at the bottom of the grid.
- Orange Region (Right):** A vertical column on the right side of the grid.

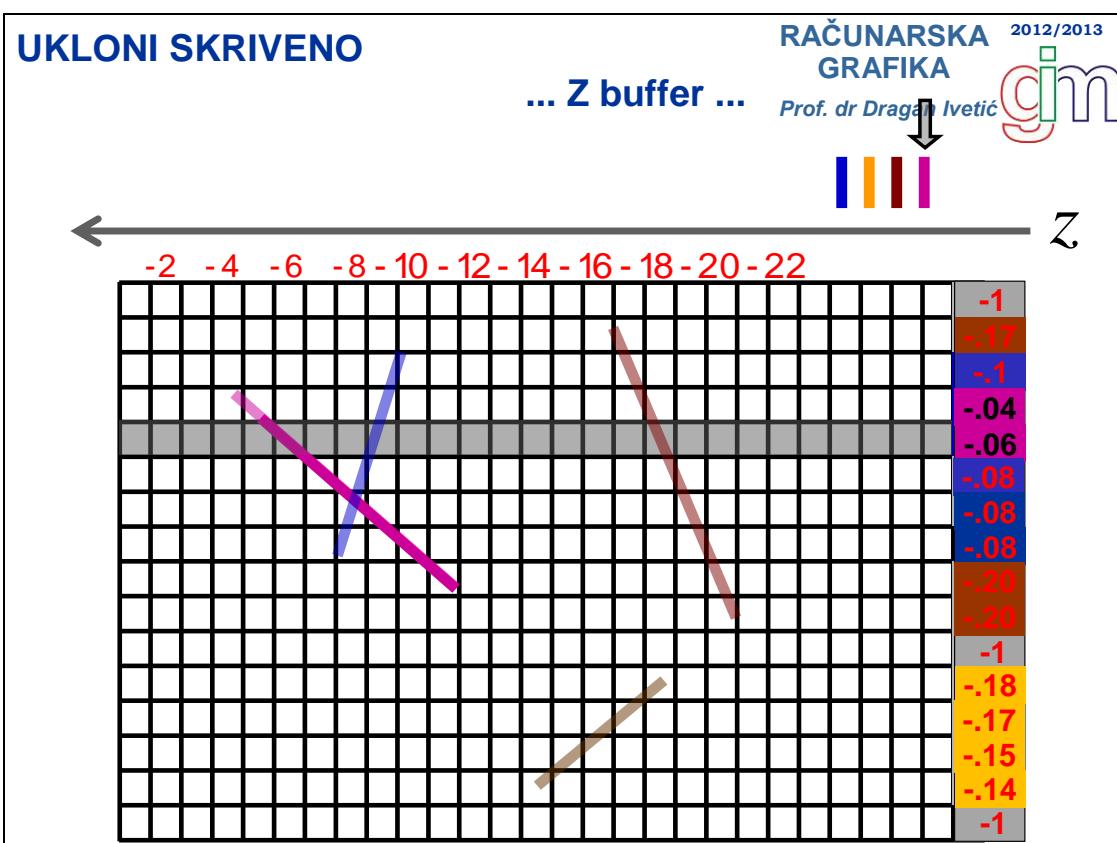
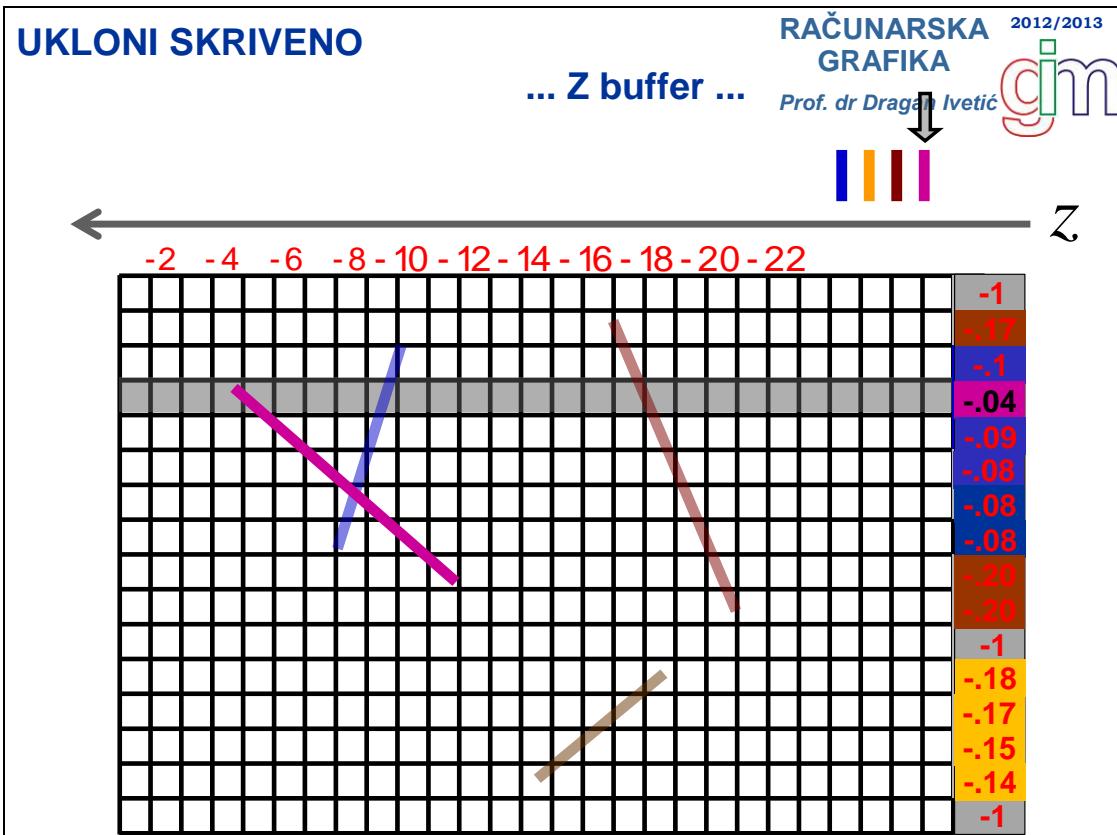
To the right of the grid, there is a vertical column of numerical values representing depth or Z-values:

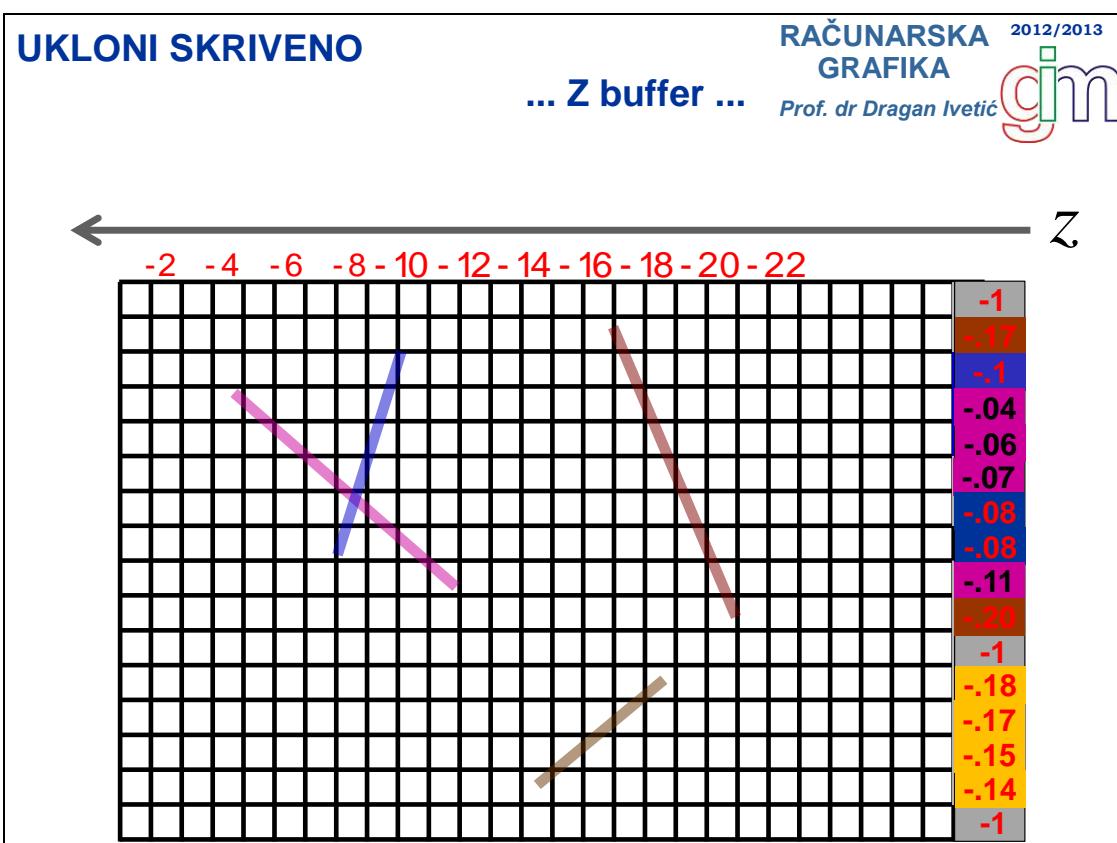
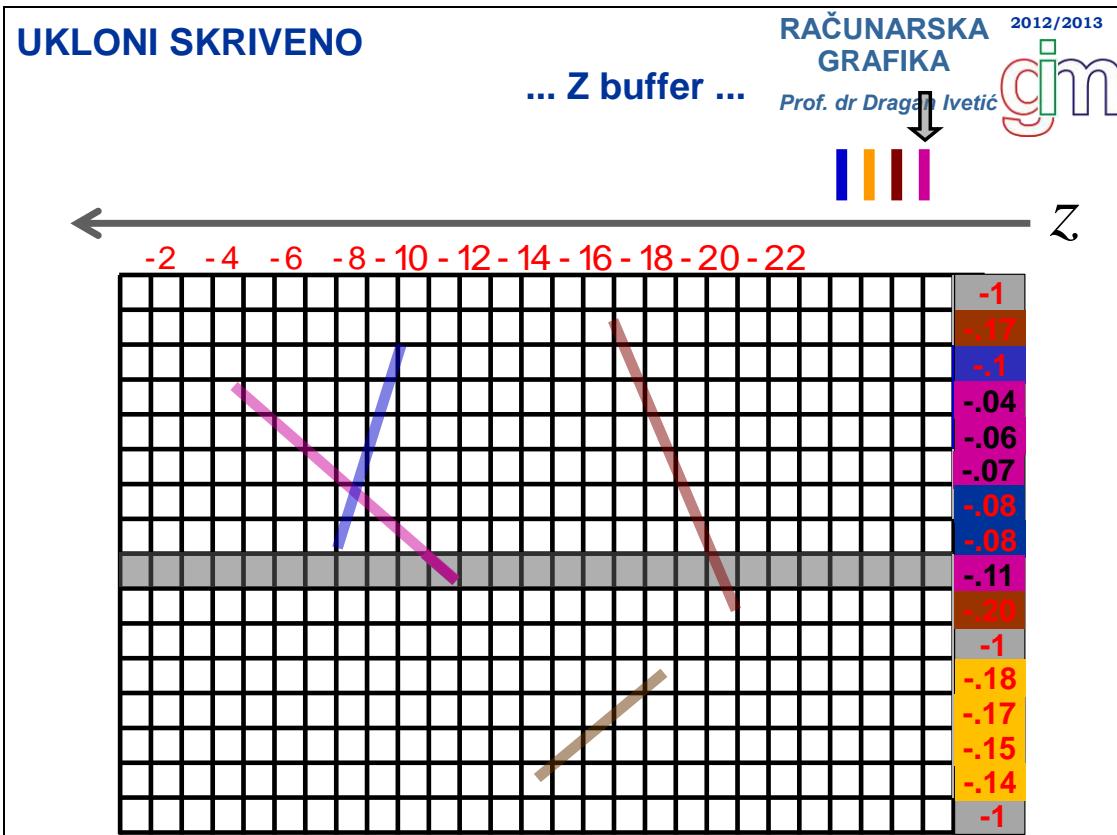
-1
-1
-.1
-.09
-.09
-.08
-.08
-.08
-1
-1
-1
-1
-18
-17
-15
-14
-1











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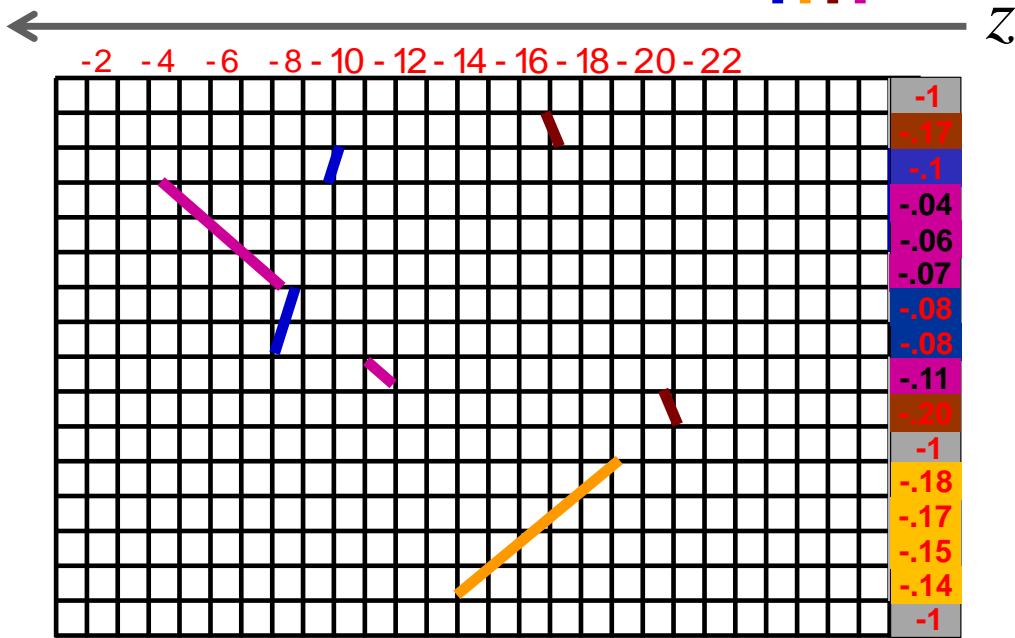
... Z buffer ...

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... Z buffer

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ZA

- jednostavan algoritam, ide u HW,
- za svaku scenu, nema sortiranja,
- kompleksnost $O(N)$,
- nema zavisnosti od redosleda poligona,
- dušu dao za paralelnu obradu.

PROTIV

- zahtevan za memorijom,
- radi i sa očigledno skrivenim (BSP, portal culling),
- nezgodan za antialiasing, transparentnost, foreground/background, i sl.

The diagram shows a 2D grid representing a frame buffer. The horizontal axis is labeled Z and has tick marks from 1 to 22. The vertical axis has an arrow pointing left. The grid contains several colored lines representing objects:

- A magenta line from (4, 4) to (10, 10).
- A blue line from (8, 4) to (10, 10).
- A red line from (16, 4) to (20, 10).
- An orange line from (16, 6) to (20, 10).

Cells in the grid are colored based on their depth value:

- Cells with values 1 through 10 are white.
- Cells with values 12, 14, 16, 18, 20, and 22 are gray.
- Cells with values greater than 22 are red.
- Cells containing the magenta, blue, red, and orange lines are also red.

This illustrates how the alpha buffer is used to determine the depth of each pixel during rendering.

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... α buffer ...

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z

1 2 3 4 5 6 7 8 9 10 12 14 16 18 20 22

∞
 ∞
10
9
9
8
8
8
 ∞
 ∞
 ∞
18
17
15
14
 ∞

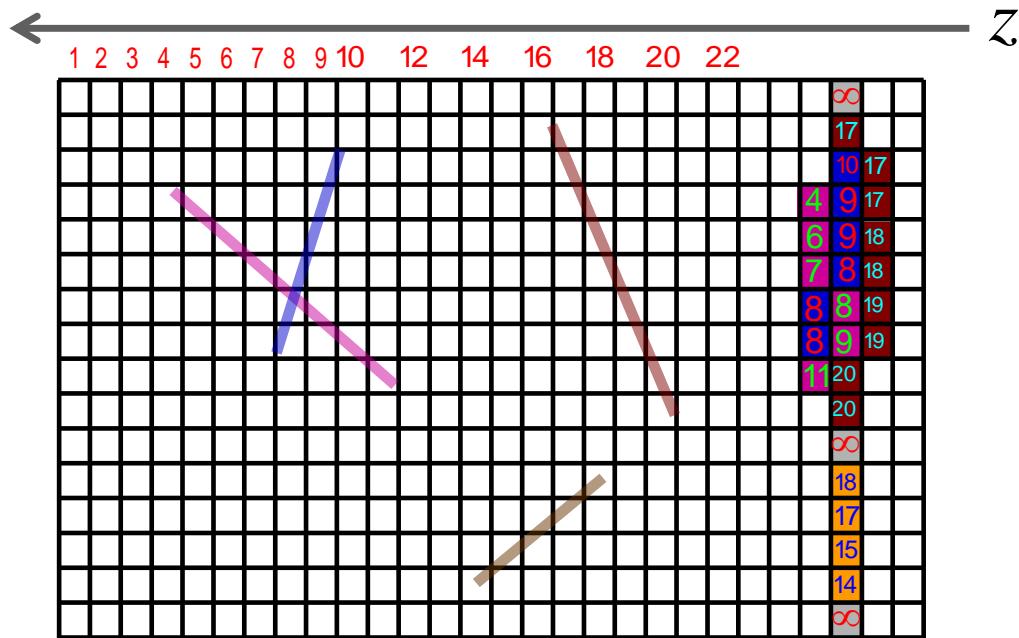
UKLONI SKRIVENO

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... α buffer ...

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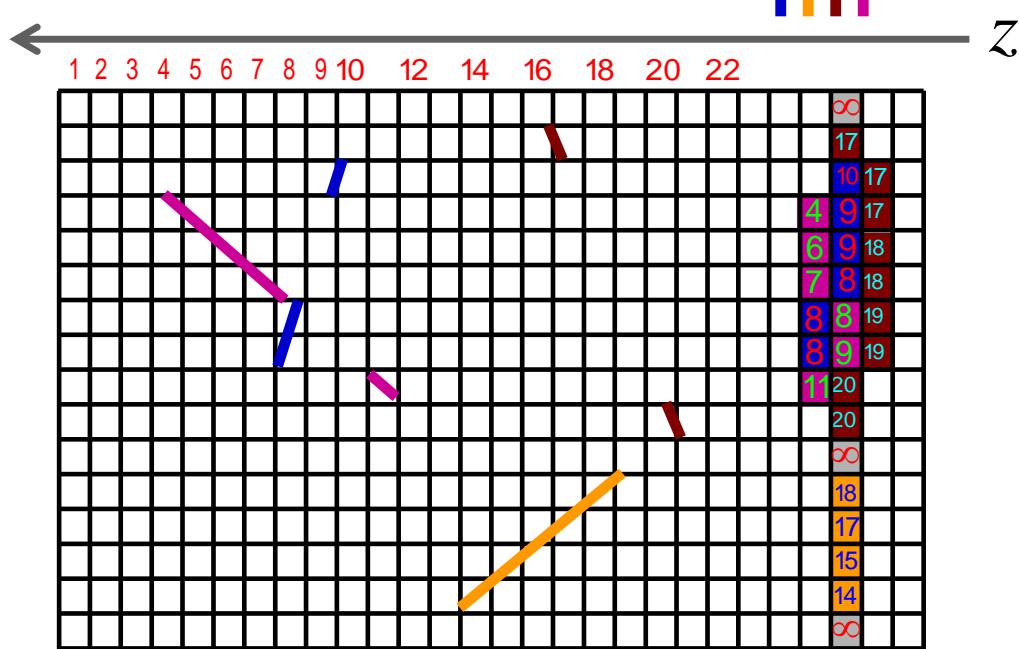
UKLONI SKRIVENO

... α buffer

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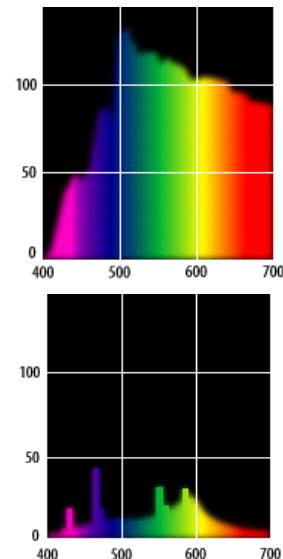
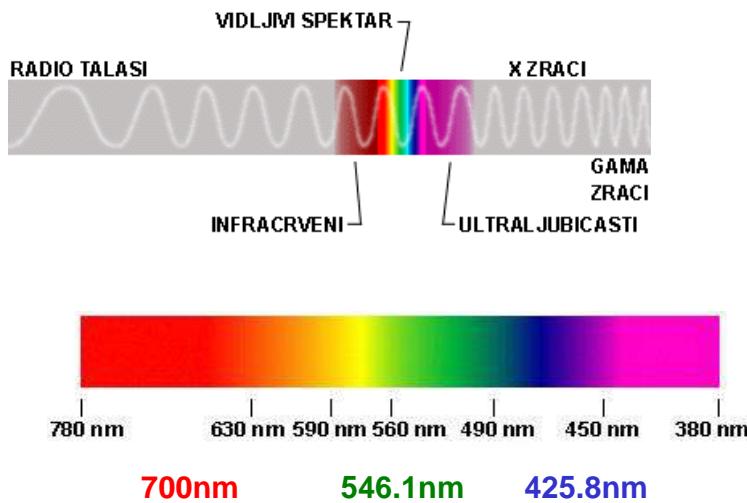
2012/2013

Prof. dr Dragan Ivetić



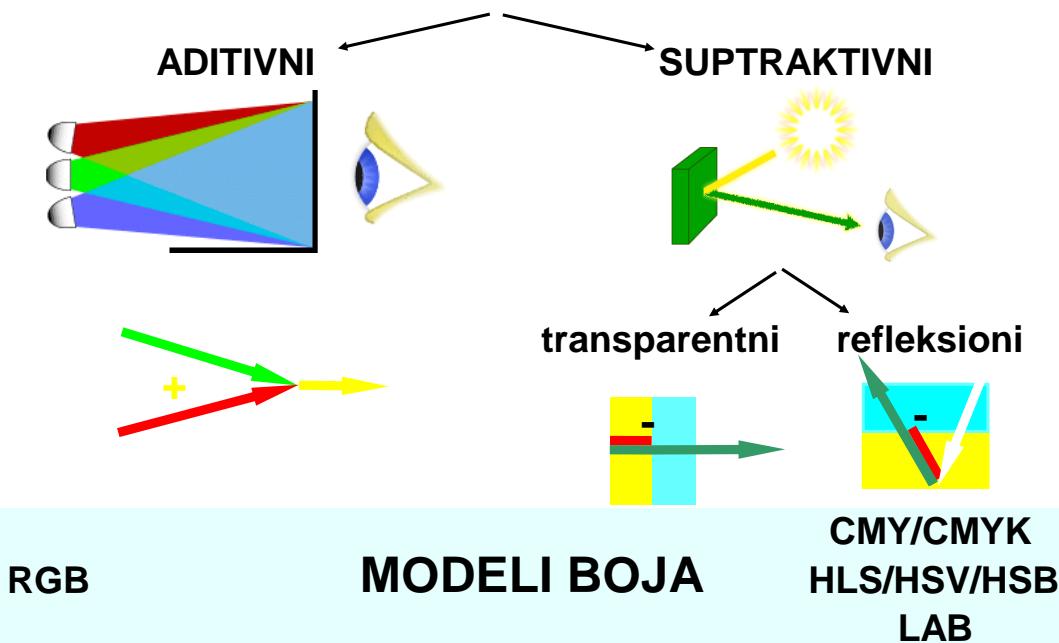
TEORIJA BOJA

- elektromagnetni talasi - fotoni,
- talasna dužina se percepira kao boja,
- energija je obrnuto srazmerna talasnoj dužini,



TEORIJA BOJA

Klase medija i modela boja



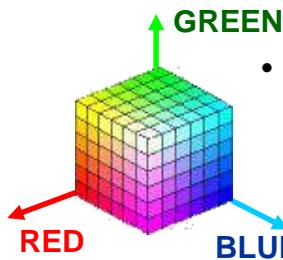
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RGB model

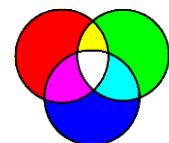
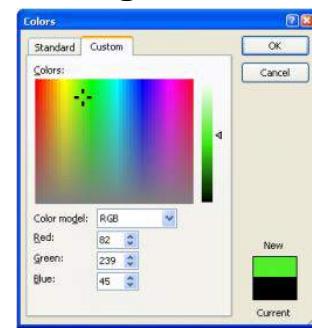
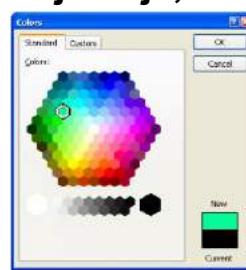
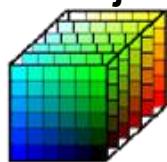
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- definisan prostor po RGB bojama,
RGB (0,0,0) je koord. početak - crno
- RGB (1,0,0) - zasićena (puna) crvena
- RGB (0,1,0) - zasićena zelena
- RGB (0,0,1) - zasićena plava
- RGB (1,1,1) - bela
- od (0,0,0)-(1,1,1) su nijanse sivog
- RGB kocka za prikaz mešanja boja,
- ravni RGB kocke za 2D selektovanje boje.



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CMY/CMYK model

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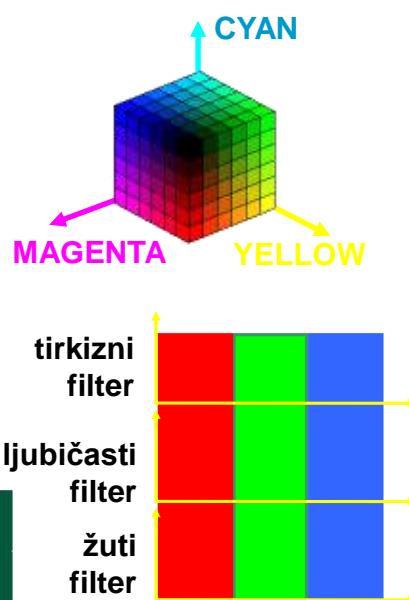
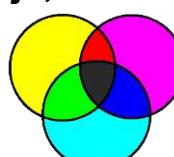
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- za suptraktivni medij,
- slaganje filtera (RGB?),
- filtri propuštaju i dijagonalnu boju,
- nema čistih (zasićenih) boja,
- bleda slika (bolesna).

CMY 2 CMYK model

- dodata crna (black),
- tj. filter/zaslon za svetlost,
- popravili "istopljenost" CMY kocke, ljubičasti filter
- i dalje nema zasićenih boja.



TEORIJA BOJA

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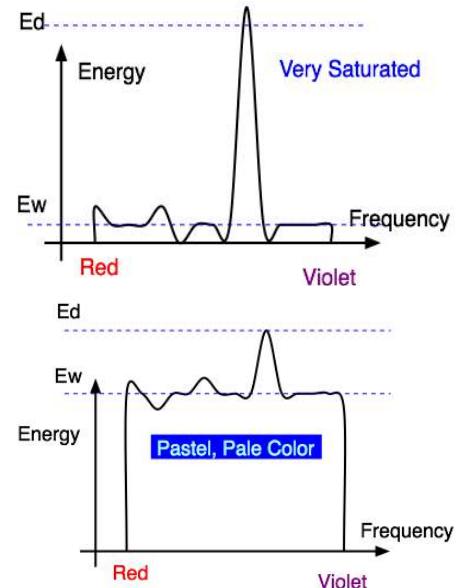
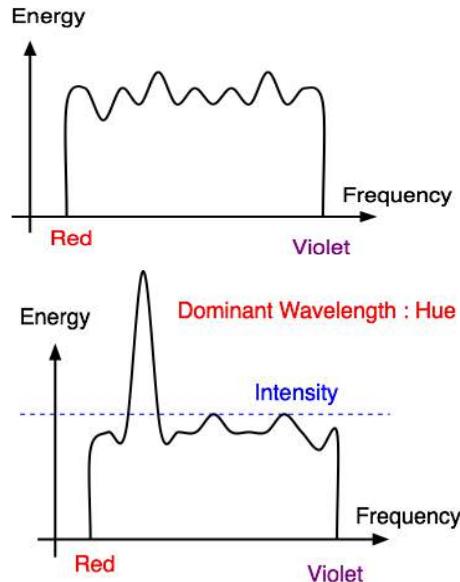
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HLS/HSV/HSB model ...

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HLS (Hue Luminosity Saturation), HSV (Value), HSB (Brightness)



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... HLS/HSV/HSB model

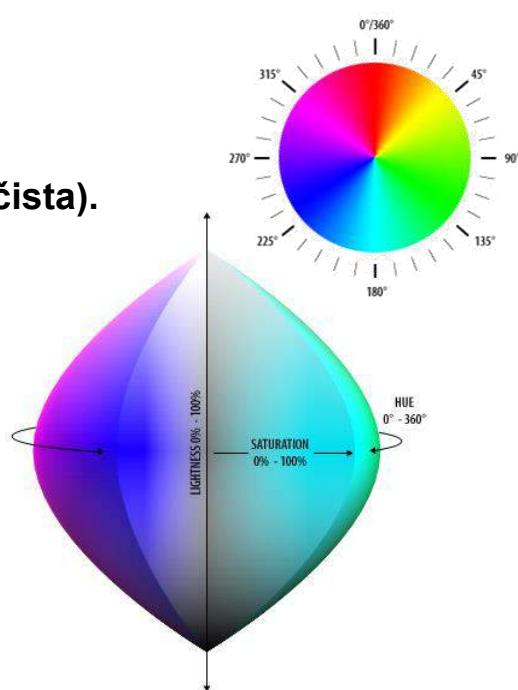
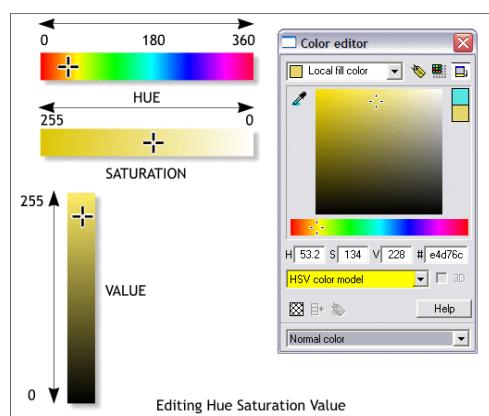
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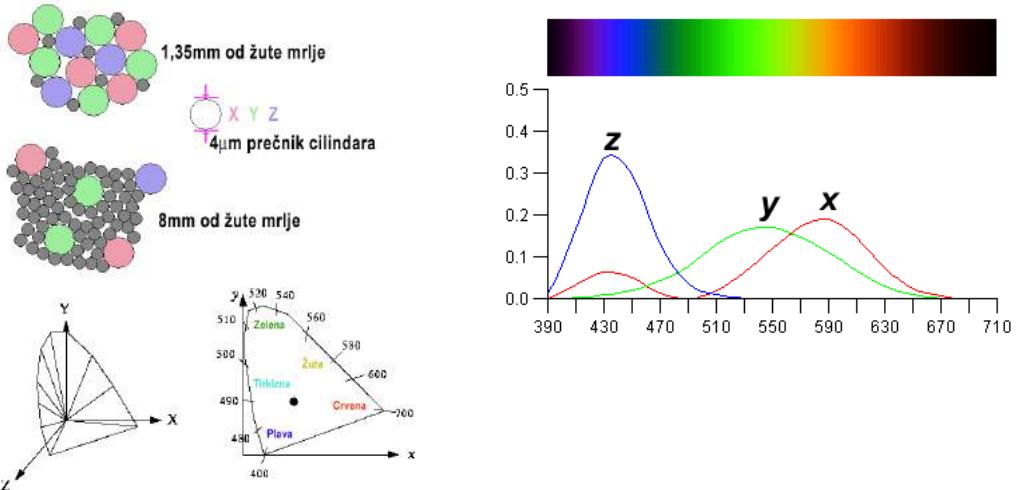


**Prati čovekov mentalni model,
izabere boju,
koliko ona treba biti svetla,
koliko zasićena (puno sivog - čista).**



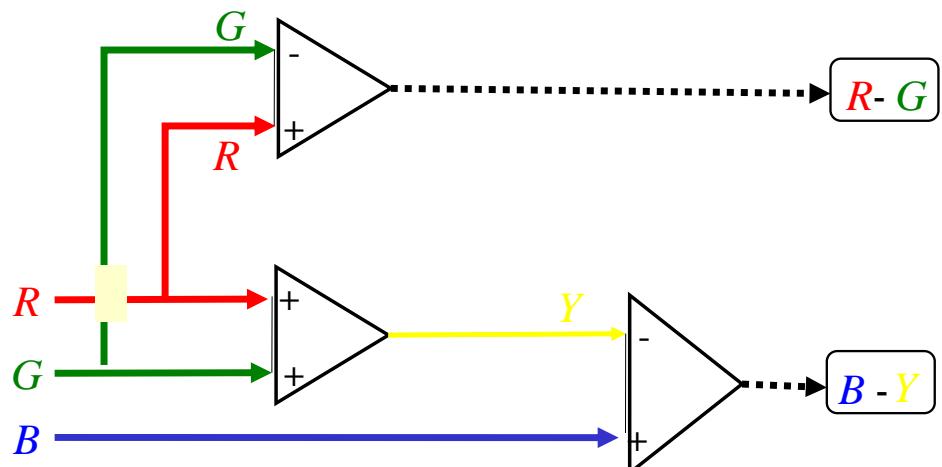
TEORIJA BOJA

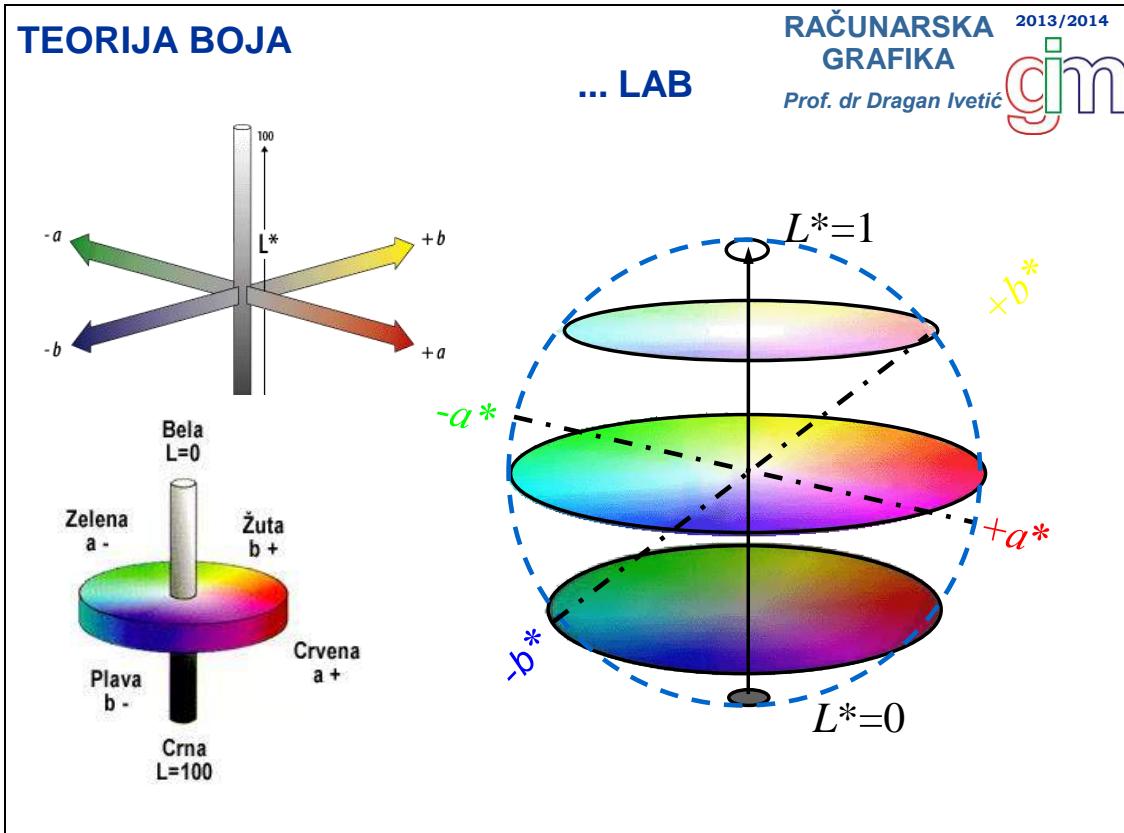
- 1931. godine CIE (Commission Internationale de L'Eclairage), Internacionalna komisija o iluminaciji ustanovila model koji je omogućio predstavljanje punih boja



TEORIJA BOJA

- 1976. godine razvijen CIA LAB po otkriću da se prenose razlike crno/belo (L^* dimenzija), crveno/zeleno (a^*) i žuto/plavo (b^*).





TEORIJA BOJA

... Dithering ...

RAČUNARSKA

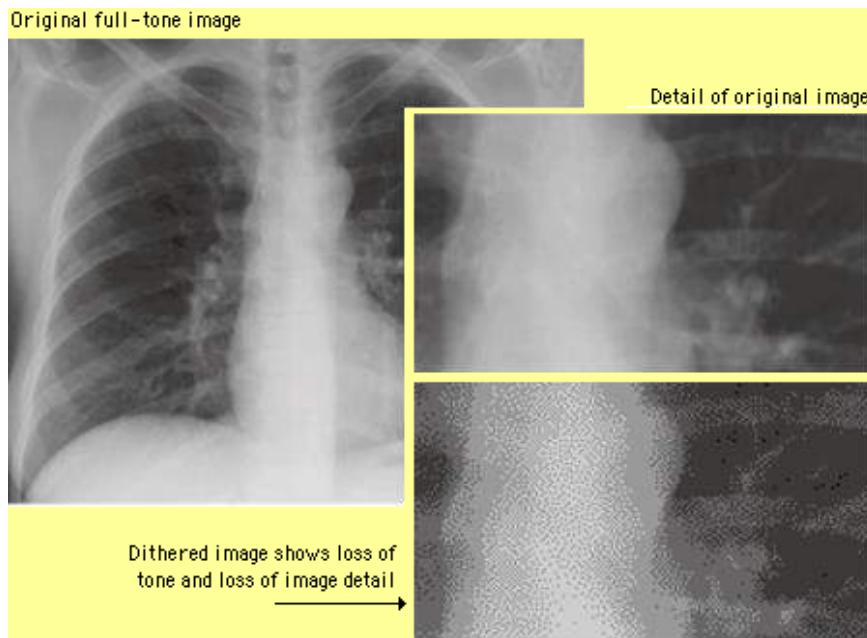
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- nije uvek poželjno!



TEORIJA BOJA

... Dithering ...

RAČUNARSKA

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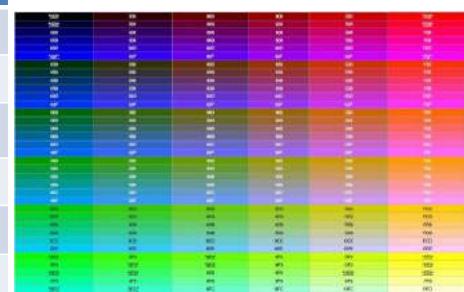
2013/2014

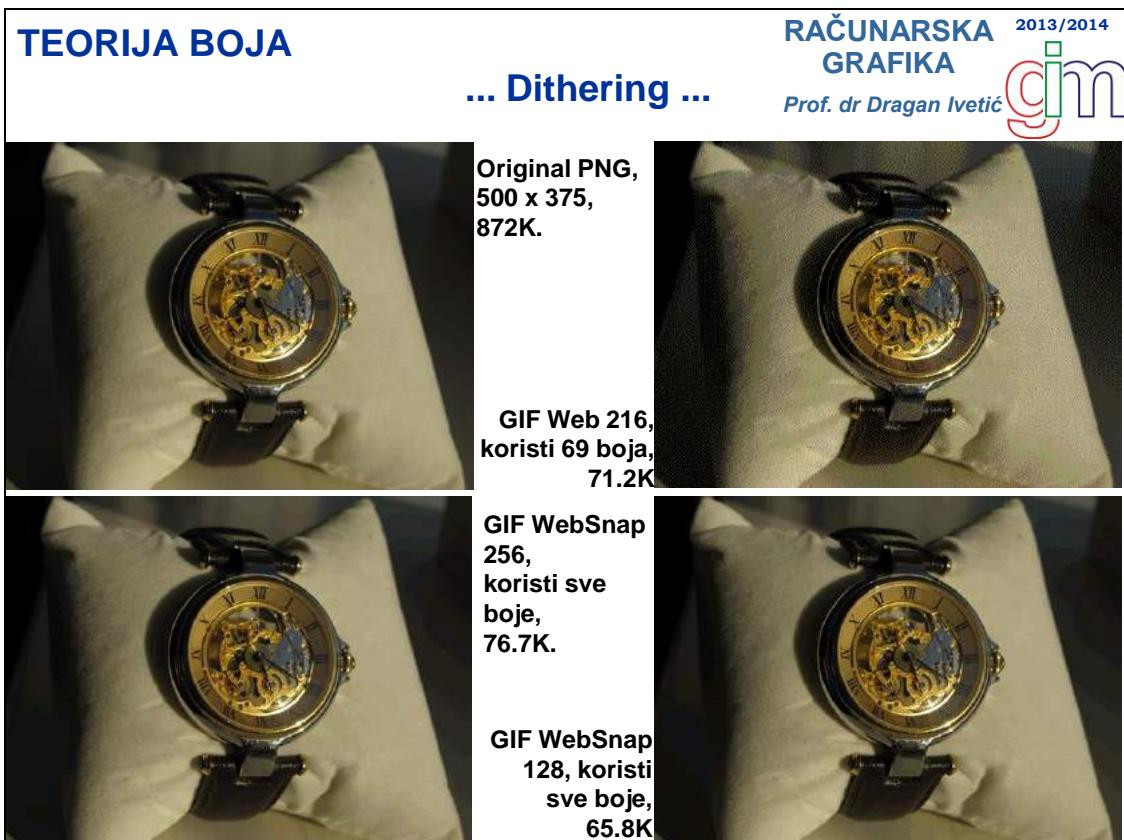


- WEB-safe color palette,
 - RGB model boja gde svaka dimenzija ima 256 nivoa
- | | | | | | |
|---------|---------|---------|---------|---------|---------|
| #ffffff | #ff0000 | #00ff00 | #0000ff | #ffff00 | #000000 |
|---------|---------|---------|---------|---------|---------|
- što bi bila paleta od $16.777.216$ boja indeksirana sa 3 bajta,
 - inženjerski - varamo posmatrača jukstapozicioniranjem boja iz palete od 216 boja (0,0129 % originalne RGB palete),

Za svaku RGB boju usvojeno 6 nivoa ($6 \times 6 \times 6$)

Frakcija	Ključ	Heks	Decimal
0,0	0	00	0
0,2	3	33	51
0,4	6	66	102
0,6	9	99	153
0,8	C	CC	204
1,0	F	FF	255





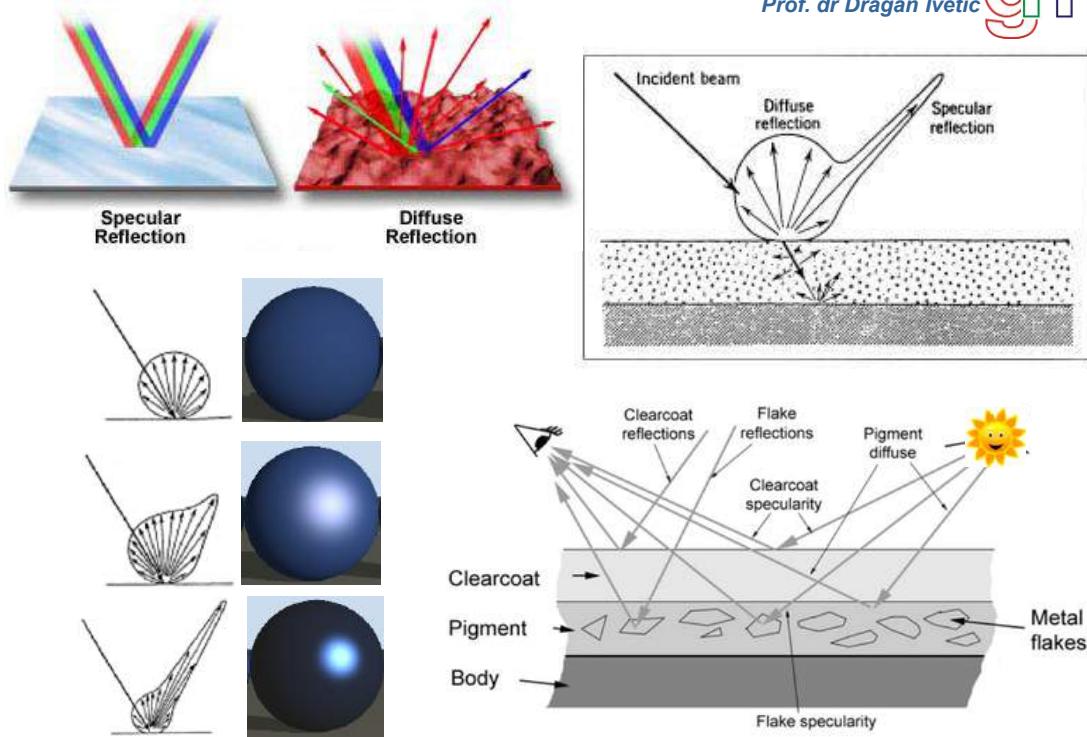
Faktori koji utiču na to kako se boje perceptuju?



Illumination v.s. shading

- Isto?
- sračunavamo interakciju svetla sa objektom na osnovu iluminacionog modela (illumination/reflection/lighting model)
- u obzir uzimamo broj i tip izvora svetlosti, kao i karakteristike materijala,
- ali sve mora da bude veoma brzo pa stoga:
 - koriste samo lokalne informacije po temenu/fragmentu:
 - boja, pravac i udaljenost izvora,
 - boja (materijala) objekta i normala površine,
 - pravac posmatrača,
 - ne rukuje se međurefleksijom objekata i zaklonjenim izvorima.
- sada samo lokalna iluminacija.

Tipovi refleksije svetla



Ideja Phong-ovog iluminacionog modela

Ideja za određivanje $I_{\text{tačke}}$

- ambijentno svetlo je uvek prisutno - ambijentna refleksija,
- može biti i tačkasti izvor
 - difuzna refleksija,
 - spekularna refleksija!
$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + I_{\text{r. tač. sv.}}$$

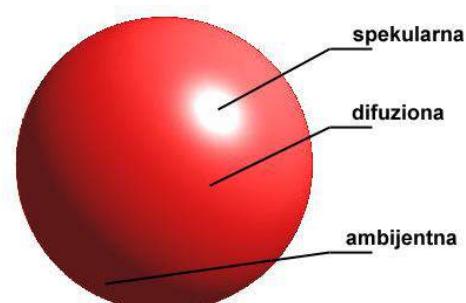
$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + I_{\text{difuz. refl.}} + I_{\text{spek. refl.}}$$

$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + \sum I_{\text{r. tač. sv.}}$$

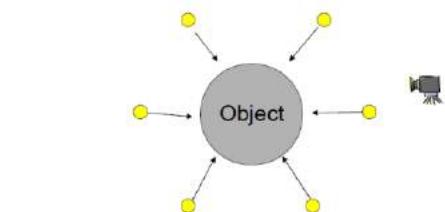
$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + \sum I_{\text{r. tač. sv.}}$$

$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + \sum I_{\text{r. tač. sv.}}$$

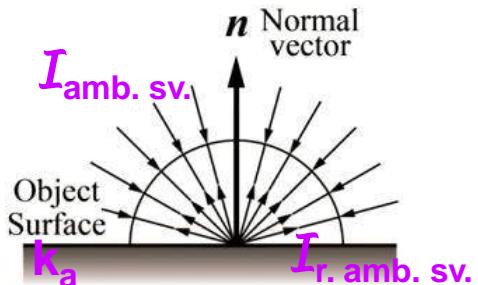
$$I_{\text{tačke}} = I_{\text{r. amb. sv.}} + \sum I_{\text{r. tač. sv.}}$$



Refleksija ambijentne svetlosti



$$I_{r. \text{ amb. sv.}} = k_a I_{\text{amb. sv.}}$$



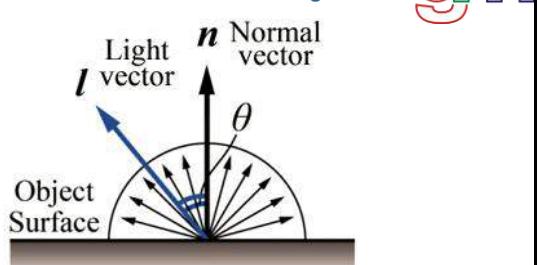
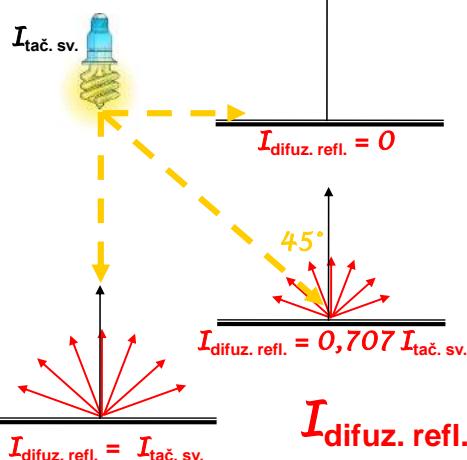
$$I_{r. \text{ amb. sv.R}} = O_{dR} k_a I_{\text{amb. sv.R}}$$

$$I_{r. \text{ amb. sv.G}} = O_{dG} k_a I_{\text{amb. sv.G}}$$

$$I_{r. \text{ amb. sv.B}} = O_{dB} k_a I_{\text{amb. sv.B}}$$



Difuziona refleksija ...



$$I_{\text{difuz. refl.}} = k_d I_{\text{tač. sv.}} \cos(\theta)$$

$$I_{\text{difuz. refl.R}} = O_{dR} k_d I_{\text{tač. sv.R}} \cos(\theta)$$

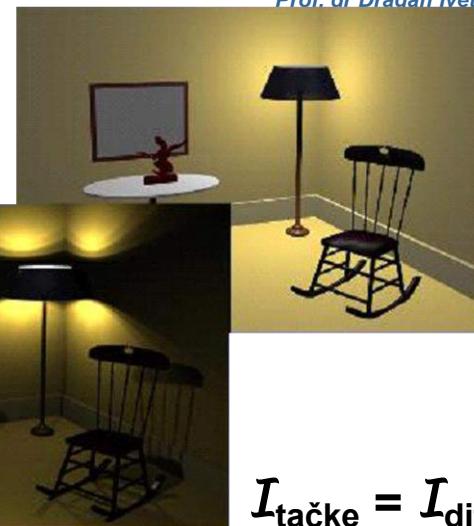
$$I_{\text{difuz. refl.G}} = O_{dG} k_d I_{\text{tač. sv.G}} \cos(\theta)$$

$$I_{\text{difuz. refl.B}} = O_{dB} k_d I_{\text{tač. sv.B}} \cos(\theta)$$



Primer ambijentne i difuzione refleksije

$$I_{\text{tačke}} = I_{\text{r. amb. sv.}}$$

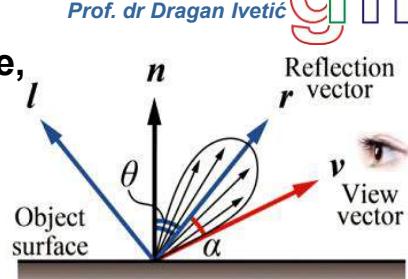
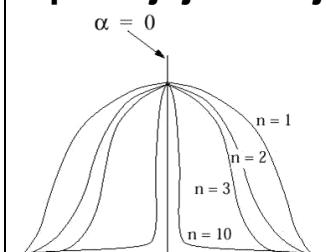


$$I_{\text{tačke}} = I_{\text{difuz. refl.}}$$

$$\begin{aligned} I_{\text{tačke}} &= I_{\text{r. amb. sv.}} + I_{\text{difuz. refl.}} = \\ &= k_a I_{\text{amb. sv.}} + k_d I_{\text{tač. sv.}} \cos(\theta) \end{aligned}$$

Spekularna refleksija

- usmerena refleksija sa sjajne površine,
- kada će intenzitet refleksije biti najveći?
 - za što veće α , ili $\alpha = 0$?
- po kojoj funkciji?



$$I_{\text{spek. refl.}} = k_s I_{\text{tač. sv.}} \cos^n(\alpha)$$

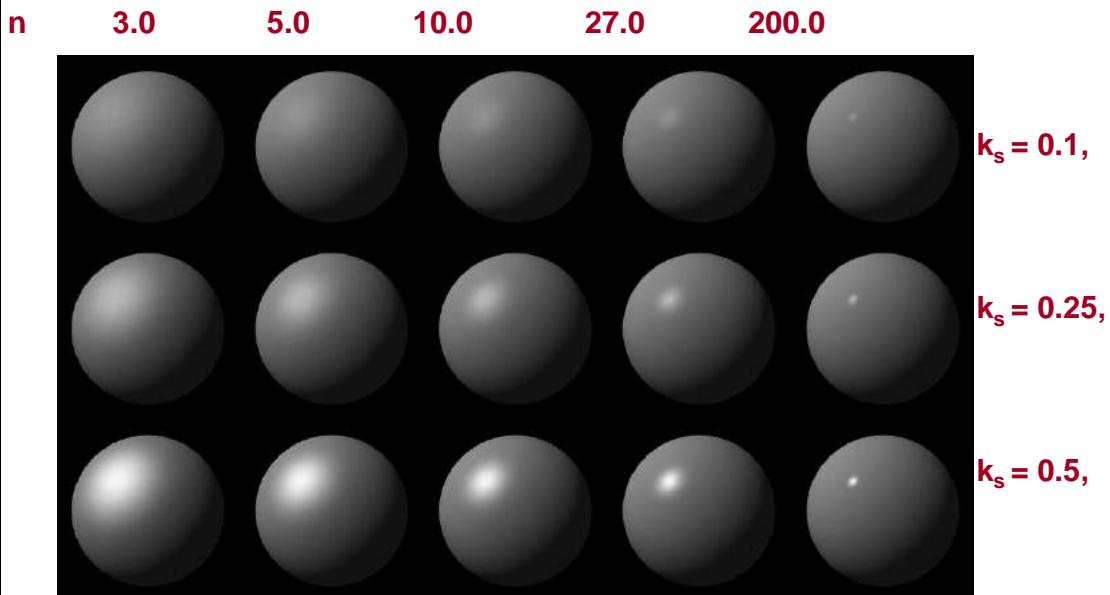
$$I_{\text{spek. refl.R}} = O_{sR} k_s I_{\text{tač. sv.R}} \cos^n(\alpha)$$

$$I_{\text{spek. refl.G}} = O_{sG} k_s I_{\text{tač. sv.G}} \cos^n(\alpha)$$

$$I_{\text{spek. refl.B}} = O_{sB} k_s I_{\text{tač. sv.B}} \cos^n(\alpha)$$



Primeri spekularne reflekcije

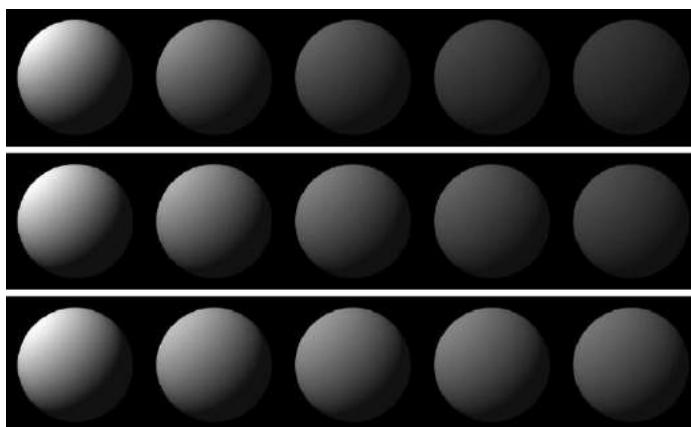


Slabljenje reflektovane svetlosti

$$f_{slabi} = 1 / d^2$$

$$f_{slabi} = \min\left(\frac{1}{c_1 + c_2d + c_3d^2}, 1\right)$$

d 1.0 1.375 1.75 2.125 2.5

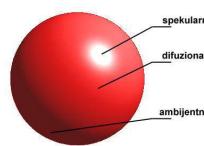


$c_1 = c_2 = 0.0, c_3 = 1.0,$

$c_1 = c_2 = 0.25, c_3 = 0.5,$

$c_1 = c_3 = 0.0, c_2 = 1.0,$

Na koji tip refleksije (A, D, S) treba primeniti slabljenje? Zašto?

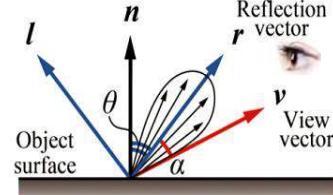
Phong-ov iluminacioni model

$$I_{\text{tačke}} = k_a I_{\text{amb. sv.}} + f_{\text{slabi}} \sum I_{\text{tač. sv.}} [k_d \cos(\theta) + k_s \cos^n(\alpha)]$$

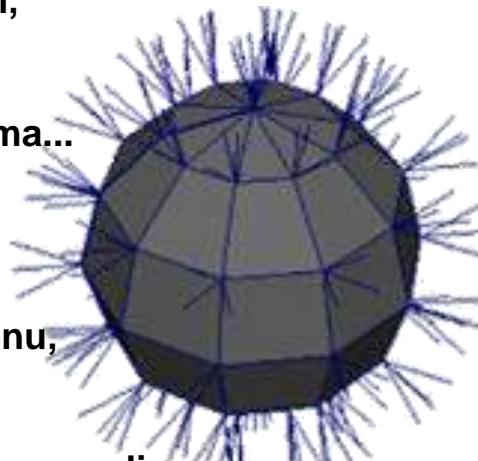
$$I_{\text{tačke}\lambda} = O_{d\lambda} k_a I_{\text{amb. sv.}\lambda} + f_{\text{slabi}} \sum I_{\text{tač. sv.}\lambda} [O_{d\lambda} k_d \cos(\theta) + O_{s\lambda} k_s \cos^n(\alpha)]$$

a da se ne računaju ugovi θ i α

$$I_{\text{tačke}\lambda} = O_{d\lambda} k_a I_{\text{amb. sv.}\lambda} + f_{\text{slabi}} \sum I_{\text{tač. sv.}\lambda} [O_{d\lambda} k_d (\bar{n} \cdot \bar{l}) + O_{s\lambda} k_s (\bar{v} \cdot \bar{r})^n]$$

**Senčenje ...**

- treba da obojimo površinu bojom,
- kako da odredimo boju?
- kako da obojimo?
- imamo samo normale po temenima...
- zavisno od modela senčenja:
 - konstantno senčenje,
 - $I_{\text{tačke}}$ ide jednom po poligonu,
 - skroman hardver,
 - Gouraud senčenje,
 - $I_{\text{tačke}}$ ide koliko ima temena po poligonu,
 - šta je sa normalom za dato $I_{\text{tačke}}$?
 - Phong senčenje,
 - $I_{\text{tačke}}$ ide više od broja temena poligona, koliko max?
 - zahtevan hardver.



... Senčenje ...

konstantno ...

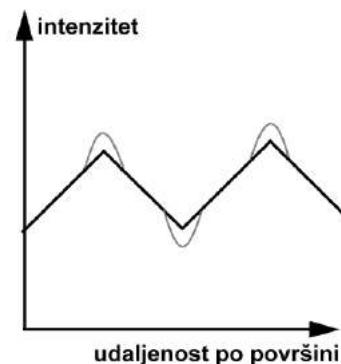
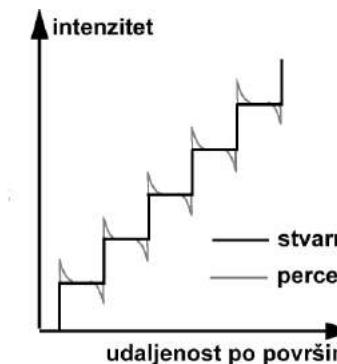
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Prepostavke:

- izvor svetla i gledalac su jako (∞) udaljeni,
- jedna iluminaciona vrednost $I_{tačke}$ po poligonu,
- OK ako poligon koji se senči nije aproksimacija površine,
 - suprotno, biće veoma naglašena nepovezanost poligona.

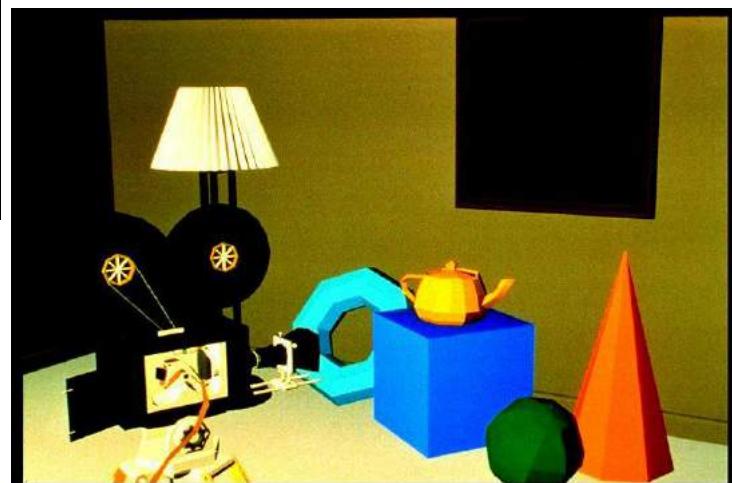
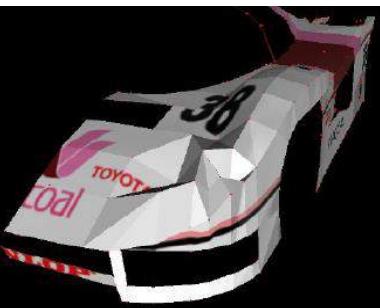


... Senčenje ...

... konstantno

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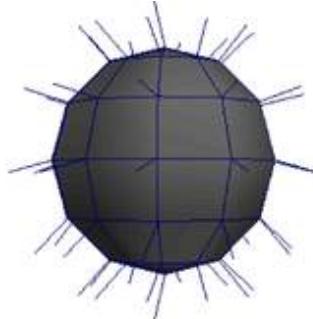


... Senčenje ...

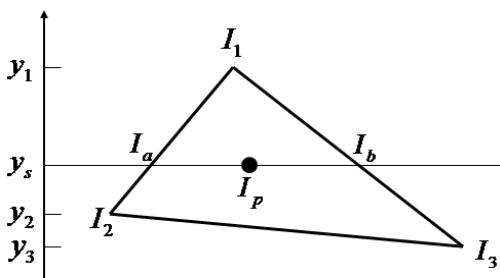
Gouraud ...

- kako da eliminiše prelaze sa jednog na drugi poligon?

$$\bar{N}_v = \frac{\sum_{1 \leq i \leq n} \bar{N}_i}{\left| \sum_{1 \leq i \leq n} \bar{N}_i \right|}$$



- pa računa $I_{\text{tačke}}$ po temenima poligona,
- pa ih interpolira po ostatku poligona.



$$I_a = I_1 \frac{y_s - y_2}{y_1 - y_2} + I_2 \frac{y_1 - y_s}{y_1 - y_2}$$

$$I_b = I_1 \frac{y_s - y_3}{y_1 - y_3} + I_3 \frac{y_1 - y_s}{y_1 - y_3}$$

$$I_p = I_a \frac{x_b - x_p}{x_b - x_a} + I_b \frac{x_p - x_a}{x_b - x_a}$$

... Senčenje ...

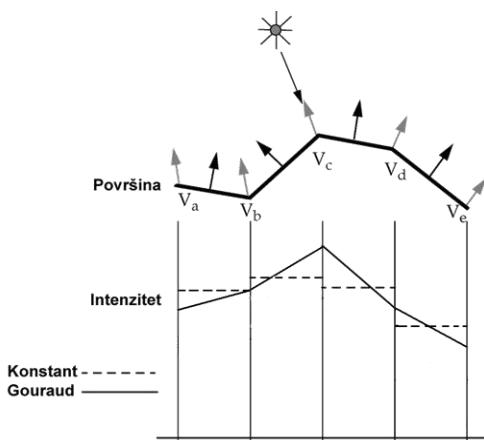
Gouraud ...



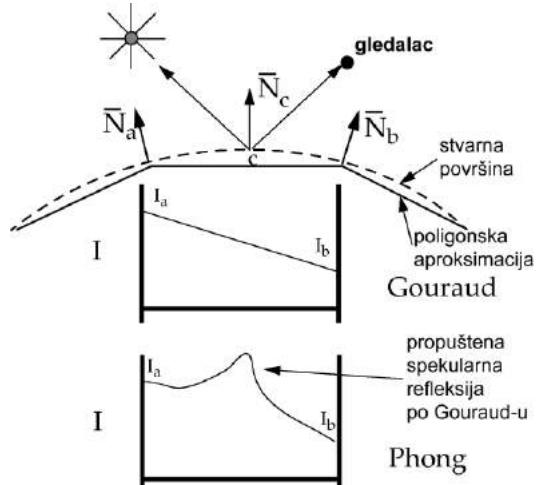
... Senčenje ...

... Gouraud

v.s. konstantno



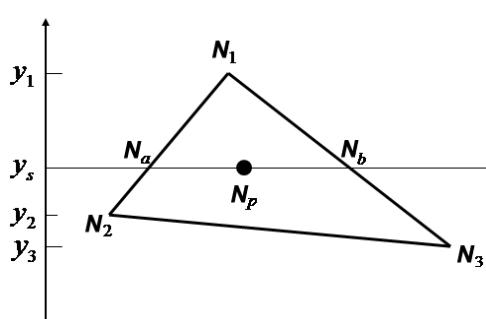
- koncentracija na usrednjene normale i interpolacija iluminacije unutar poligona,
- veliki nedostatak, koji?



... Senčenje ...

Phong ...

- kako da korektno senči kada ima i spekularne refleksije?
- što kasnije da računa $I_{\text{tačke}}$, unutar poligona.



$$N_a = N_1 \frac{y_s - y_2}{y_1 - y_2} + N_2 \frac{y_1 - y_s}{y_1 - y_2}$$

$$N_b = N_1 \frac{y_s - y_3}{y_1 - y_3} + N_3 \frac{y_1 - y_s}{y_1 - y_3}$$

$$\tilde{N}_p = \frac{N_a}{\|N_a\|} \left[\frac{x_b - x_p}{x_b - x_a} \right] + \frac{N_b}{\|N_b\|} \left[\frac{x_p - x_a}{x_b - x_a} \right]$$

- kada odredi N_p tada računa i $I_{\text{tačke}}$ u p.
- koliko puta se sada sračunava iluminacija?

... Senčenje ...

... Phong ...

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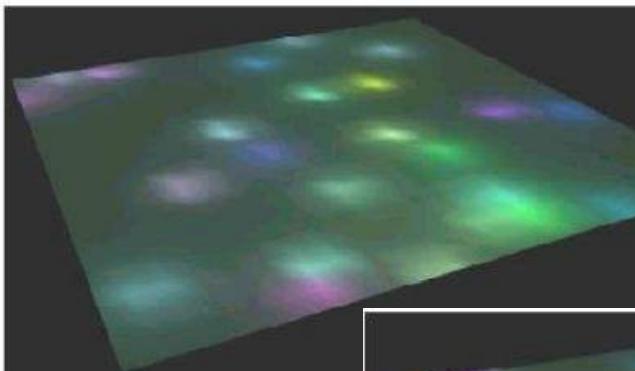
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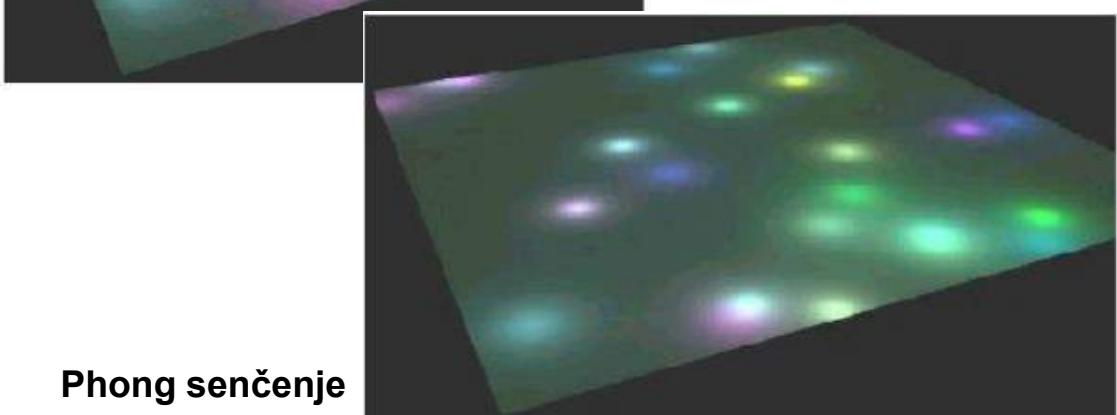
... Senčenje ...

... Phong ...

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GRAFIKA
Prof. dr Dragan Ivetić



Gouraud senčenje diskopoda, problem i kada je mali broj poligona...

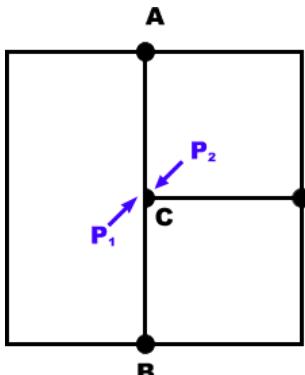


Phong senčenje

... Senčenje ...

problemi sa interpolacijama ...

- problem sa sračunavanjem normala u temenima,



- A i B temena dele svi poligoni, a C teme dele samo oni s desne strane,
- P_1 sračunat na osnovu (A, B), a P_2 biće baš C, odnosno u okolini kao (A,C) i (C,B),
- značajan diskontinuitet u senčenju.

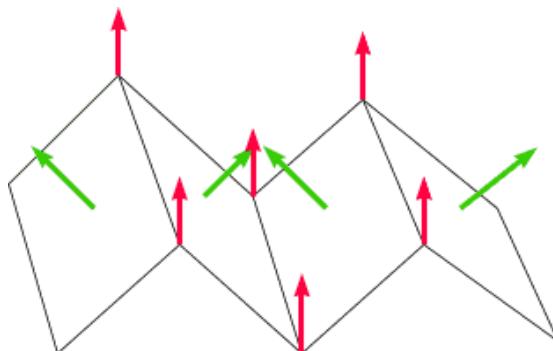
- rešenja:

- podeli sve na trouglove,
- uključi fantomsko teme C za P_1 .

... Senčenje ...

... problemi sa interpolacijama ...

- problem sa sračunavanjem normala u temenima,
- normale površina su usrednjene u zajedničkim temenima,
- kako će izgledati ove površine kada se osenče?

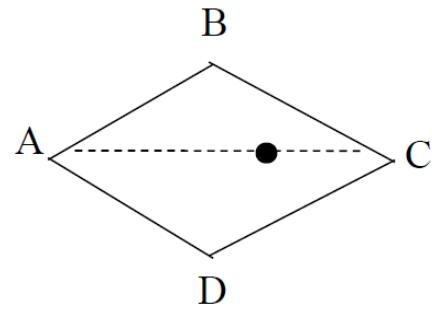
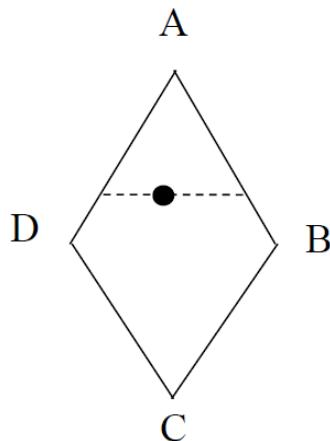


- rešenje?

... Senčenje ...

... problemi sa interpolacijama

- interpolacija iluminacije nije invarijantna za rotaciju površine sa barem 4 temena?



- rešenje?

... Senčenje

