



Swerve Robotic Platform

Structural and Mechanical Analysis

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Report Outline

1. *Vehicle Introduction*
2. *Analysis Overview*
3. *Vehicle Structural Analysis*
4. *Vehicle Mechanical Analysis*
5. *References*
6. *Appendix*



1. Vehicle Introduction

Vehicle Performance, Component Detail

Vehicle Introduction

Analysis Overview

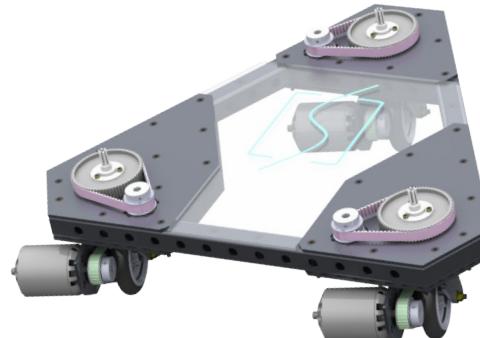
**Vehicle Structural
Analysis**

1. Vehicle Introduction

Performance Criteria

The vehicle is intended to accelerate and maneuver as quickly as possible. For design and analysis purposes, the acceleration rate was chosen to be 32.2 ft/s^2 (1g). Additionally, the vehicle is intended to carry a single passenger who stands on top of the vehicle in specifically marked locations. To accommodate different people, a large patron weight of 300lbs [1] was assumed for analysis purposes as a worst case. By leaning in a desired direction, the vehicle will accelerate in that direction, similar to a segway. Using pressure sensors, the vehicle accelerates at a rate that prevents the vehicle and leaning patron from tipping. Below is a rendered image of the proposed vehicle design.

The following is an structural and mechanical analysis package for the vehicle system. Using ABAQUS/CAE, a finite element model was created and analyzed per the specifications listed above. Additionally, supporting structural and mechanical calculations were completed to validate the proposed design.



1. Vehicle Introduction

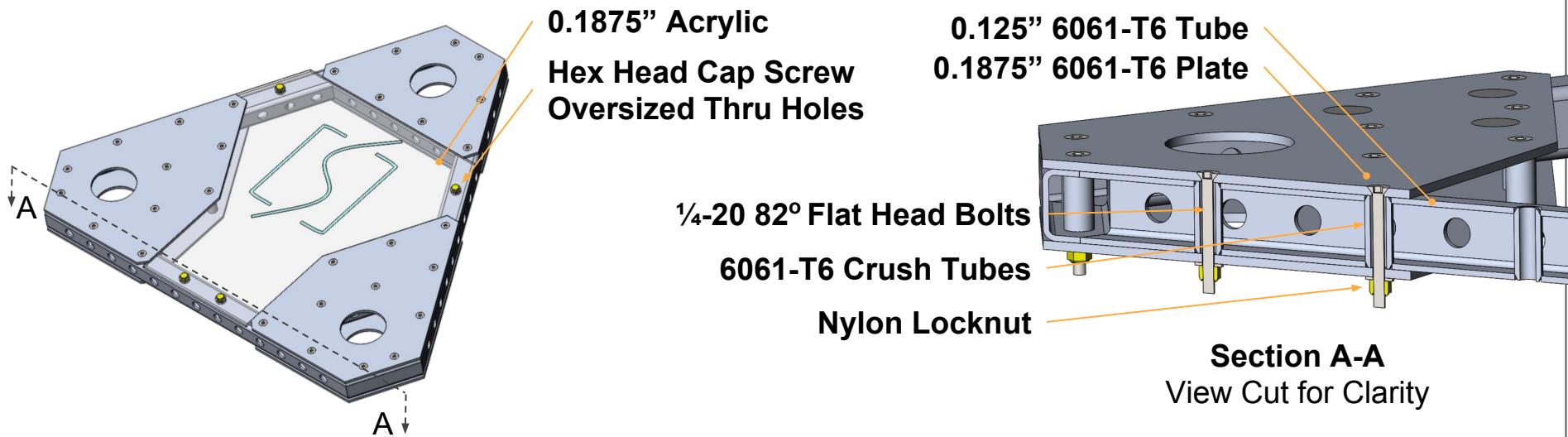
A Note About the Analysis

Per the university requirements, the timeline for this project was restricted to nine months, so the vehicle design and analysis were completed in parallel. As a result, some of the mechanical and structural components have changed since the formation of this report. However, the modifications that were made are expected to have little to no effect on the structural integrity of the system. Some changes that were made include the addition of small holes for mounting, modifications to hole size and location, etc. Over the course of the next few months, the team will return to this analysis to update accordingly, though the report will be used to validate the design for now.

1. Vehicle Introduction

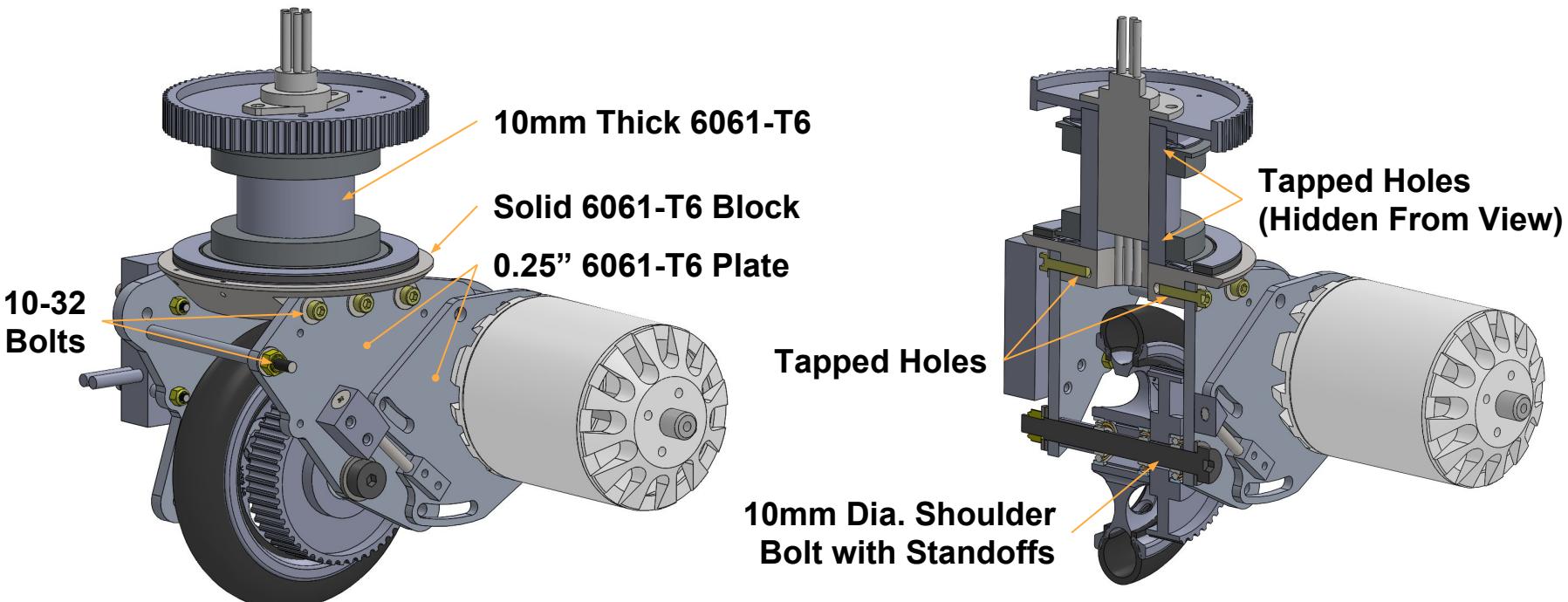
Chassis Mechanical / Structural Components

Below are the structural components of the chassis used for analysis. Due to the oversized holes in the acrylic, the acrylic is intended to be removed from the load path, and therefore it will not be used in the structural analysis.



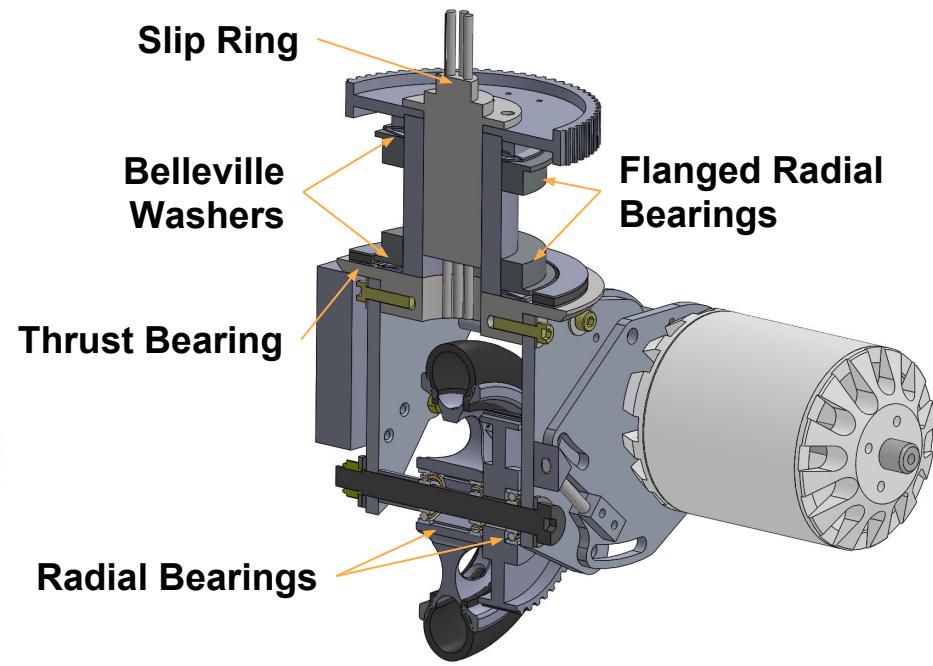
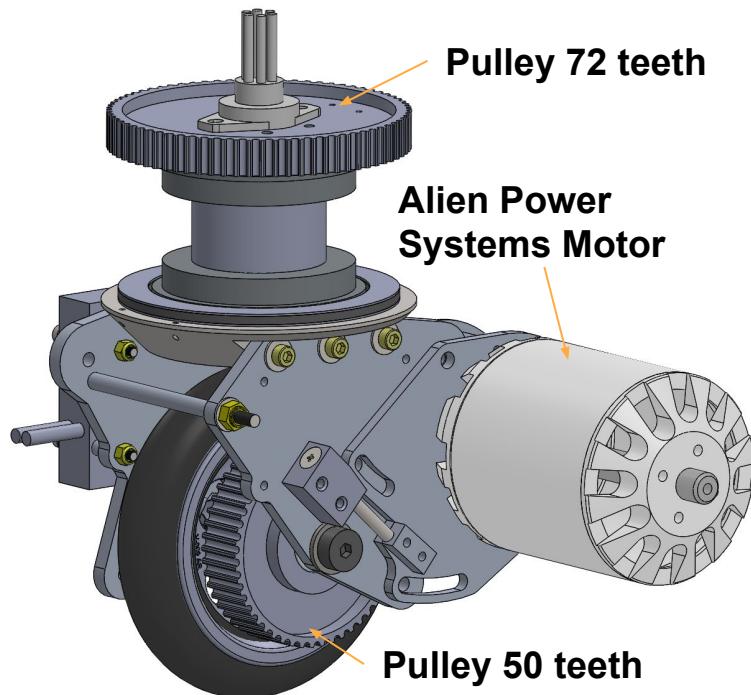
1. Vehicle Introduction

Wheel Assembly Structural Components



1. Vehicle Introduction

Wheel Assembly Mechanical Components



2. Analysis Overview

Assumptions, Success Criteria, Material Properties

Concept Design

Vehicle Introduction

Analysis Overview

Vehicle Structural
Analysis

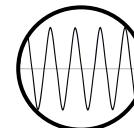
Vehicle Mechanical
Analysis



2. Analysis Overview

Analysis Assumptions and Considerations

Low-Cycle Life Expectancy - *Fatigue is Not Considered*



Conservative Safety Factors - *Compliant with Standards*



Consistent, Moderate Climate - *No Corrosion Considered*



This system is intended to be used for recreation, for short periods of time, and in dry as well as clean environments. Therefore, fatigue considerations and material corrosion are beyond the scope of these analyses. For analysis success, the mechanical and structural components are expected to pass conservative safety factors for strength load cases. A description of the loading criteria can be found on Page 13 of this report.

2. Analysis Overview

Material Properties and Allowables

Below are the material properties for the general materials used in the proceeding analysis. Additionally, the required safety factors for aluminum are listed as well. If a different material or safety factor is used for analysis, it will be noted specifically within that section of the report. The welded aluminum allowables are highlighted for clarification in addition to the aluminum safety factors used for the analyses. For simplicity, Building Type structures are static load dominated, while Bridge Type structures are dynamic load dominated.

Material Name	Density [lb / in ³]	E-Modulus [psi]	Poisson	Yield σ [psi]	Ult. σ [psi]	Reference
	-	-	-	-	-	
Aluminum 6061-T6	0.098	9.9E +06	0.33	35000	42000	2
Structural Steel A36	0.284	2.9E +07	0.32	36000	55000	2
Welded 6061-T6	0.098	9.9E +06	0.33	15000	24000	3

TABLE 6.1 Safety Margins in the Aluminum Specification [3]

Type of Structure	Yield Strength	Ultimate Strength
Building Type	1.65	1.95
Bridge Type	1.85	2.20

2. Analysis Overview

Component Material Information

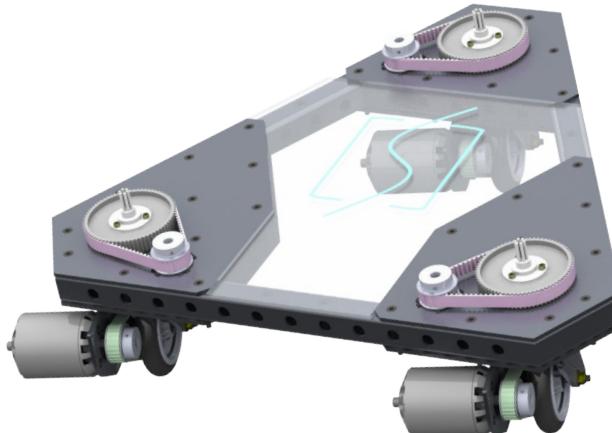
Chassis Components

Part	Material
Structural Beams	6061-T6
Gusset Plates	6061-T6
Crush Tubes	6061-T6

Wheel Assembly Components

Part	Material
Rotating Yaw Shaft	6061-T6
Connecting Block	6061-T6
Side Plates	6061-T6

To reduce the weight of the system, aluminum 6061-T6 was used for many of the structural and mechanical components. Unless otherwise specified, it was assumed that bulk material was manufactured from aluminum 6061-T6 and all bolts were made from A36 steel.



2. Analysis Overview

Load Cases and Analysis Methodology

Structural Analysis Methodology

The structural components were analyzed for full-load, full performance operation. During operation, the patron will lean in a desired direction at a specific angle. This places the patron Center of Gravity (CG) away from the vehicle, and a calculated acceleration is required to avoid tipping. A lumped point mass of 300lbs was placed in the finite element model at the specified location to represent the patron CG. The contact locations of the wheels were constrained to only allow rotation (translations fixed) and global accelerations were applied to the model to represent the accelerations of the vehicle. Important factors and values are listed below:

- A Dynamic Factor was not added to loads since it is included in the required safety factor
- A 1.2 Impact Factor was applied to all accelerations per Reference 1 (ASTM F2291-17).
- The Patron CG is located 40.7in on top of the gusset plates per Reference 4.

Mechanical Analysis Methodology

The mechanical components were analyzed for full-load, full-performance operation as well as system abuse and impact while patrons are getting on and off the system. The component calculations were completed assuming all of the system and patron weight are applied to only one wheel assembly. This type of loading is unlikely and will therefore be considered conservative. All of the loads are derived assuming the system will accelerate and perform at the proposed 1g rate. Important factors are listed below:

- A 2.0 Impact Factor was used in many cases for system abuse



2. Analysis Overview

Patron Center of Gravity Information

Table for Estimated Percentiles

Percentile	Factor	Equation
99.9	3.000	99.9 = Mean + (3 x SD)
99.5	2.576	99.5 = Mean + (2.576 x SD)
99	2.326	99.0 = Mean + (2.326 x SD)
97.5	1.950	97.5 = Mean + (1.95 x SD)
97	1.880	97.0 = Mean + (1.88 x SD)
95	1.650	95.0 = Mean + (1.65 x SD)
90	1.280	90.0 = Mean + (1.28 x SD)
85	1.040	85.0 = Mean + (1.04 x SD)
80	0.840	80.0 = Mean + (0.84 x SD)
75	0.670	75.0 = Mean + (0.67 x SD)
50	0.000	50.0 = Mean + (0 x SD)
25	-0.670	25.0 = Mean + (-0.67 x SD)
20	-0.840	20.0 = Mean + (-0.84 x SD)
15	-1.040	15.0 = Mean + (-1.04 x SD)
10	-1.280	10.0 = Mean + (-1.28 x SD)
5	-1.650	5.0 = Mean + (-1.65 x SD)
3	-1.880	3.0 = Mean + (-1.88 x SD)
2.5	-1.950	2.5 = Mean + (-1.95 x SD)
1	-2.326	1.0 = Mean + (-2.326 x SD)
0.5	-2.576	0.5 = Mean + (-2.576 x SD)
0.1	-3.000	0.1 = Mean + (-3 x SD)

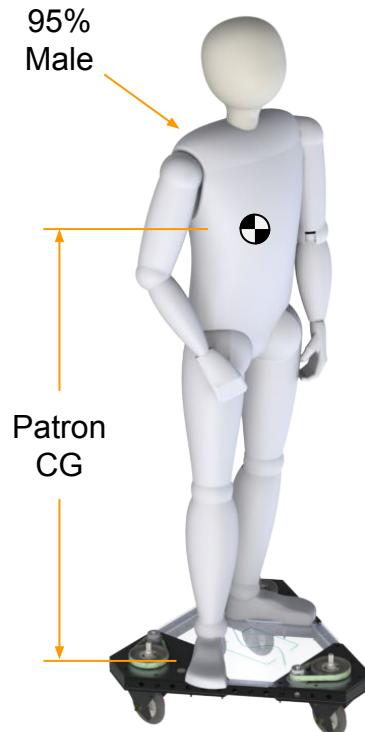
SD = Standard Deviation

Table Taken from *The Measure of Man & Woman*, John Wiley & Sons (C) 2002

Vertical CG Location (From Feet)

Percentile	Measurement
Mean Data:	50 37.9 in
2nd Data:	99 41.8 in
Standard Dev:	SD 1.68 in
Interpolated:	95 40.7 in

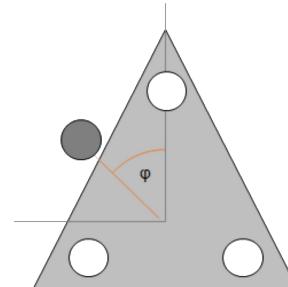
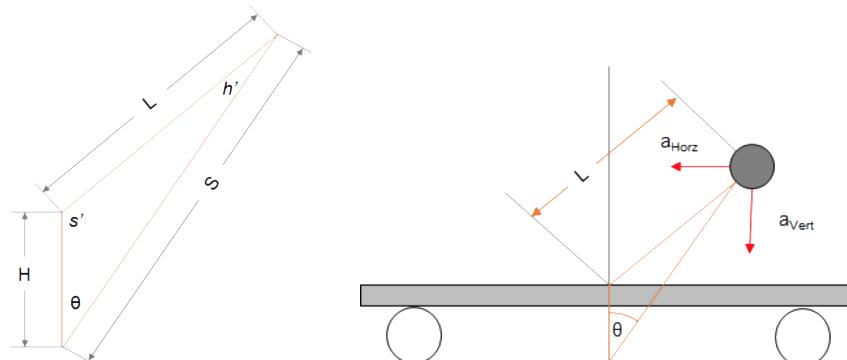
A 95 percentile male (73.7in tall) was the design patron height per Reference 1. This large patron height coupled with the large patron weight (300lbs) is conservative as the system would not accommodate riders larger than this.



2. Analysis Overview

Patron CG Positioning Calculation for Finite Element Model

All straight-line and perpendicular load cases are derived using the table to the right. These load cases are acceleration driven and the Patron CG location can be derived.



Determine CG Location due to Applied Accelerations

Name	Var	Value	Unit	Comment / Equation
User Input				
Gravitational Acceleration	g	1 g		Given
Vertical Acceleration	a _{Vert}	1.2 g		Vertical Loading on System
Horizontal Acceleration	a _{Horz}	1.2 g		Horizontal Loading on System
CG Height of Patron	L	40.7 in		Height From Chassis Platen
Platen Height off Floor	H	7.86 in		Height From Floor to Platen
Direction Off Straight	φ'	30 deg		Direction From Straight Travel

Geometry Calculations - Law of Sines

Direction Vector Angle	φ	0.5 rad	= (π/180) * φ'
Acceleration Vector Angle	θ	0.785 rad	= ATAN(a _{Horz} / a _{Vert})
Angle: Patron / Line of Act	h'	0.137 rad	= ASIN((H/L) * SIN(θ))
Angle: Internal Patron Lean	s'	2.2 rad	= π - θ - h'
CG to Floor - Dist Vector	S	45.9 in	= L * [SIN(s') / SIN(θ)]

Resulting Acceleration Components and Patron CG Location

Accel Comp-LAT	a _{lat}	-0.600 g	= a _{Horz} * SIN(φ)
Accel Comp-FWD	a _{fwd}	-1.039 g	= a _{Horz} * COS(φ)
Accel Comp-VERT	a _{vert}	-1.200 g	= a _{Vert}
CG Lateral Location	CG _{lat}	16.22 in	= S * SIN(θ) * SIN(φ)
CG Forward Location	CG _{fwd}	28.09 in	= S * SIN(θ) * COS(φ)
CG Vertical Location	CG _{vert}	24.58 in	= S * COS(θ) - h
Calc. Patron CG Height	L _{calc}	40.7 in	= (CG _{fwd} ² + CG _{lat} ² + CG _{vert} ²) ^(1/2)

Calculated Patron CG Height is Consistent with Input Data

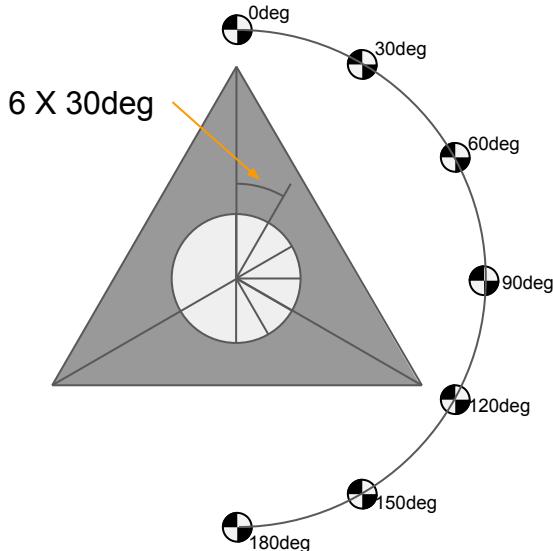
2. Analysis Overview

Load Cases for the Finite Element Model

Dead	Accel-X: 0.00 g	CG-X: 0.0 in
	Accel-Y: 0.00 g	CG-Y: 0.0 in
	Accel-Z: -1.20 g	CG-Z: 40.7 in
0deg	Accel-X: -1.20 g	CG-X: 32.4 in
	Accel-Y: 0.00 g	CG-Y: 0.0 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
30deg	Accel-X: -1.04 g	CG-X: 28.1 in
	Accel-Y: -0.60 g	CG-Y: 16.2 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
60deg	Accel-X: -0.60 g	CG-X: 16.2 in
	Accel-Y: -1.04 g	CG-Y: 28.1 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
90deg	Accel-X: 0.00 g	CG-X: 0.0 in
	Accel-Y: -1.20 g	CG-Y: 32.4 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
120deg	Accel-X: 0.60 g	CG-X: -16.2 in
	Accel-Y: -1.04 g	CG-Y: 28.1 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
150deg	Accel-X: 1.04 g	CG-X: -28.1 in
	Accel-Y: -0.60 g	CG-Y: 16.2 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
180deg	Accel-X: 1.20 g	CG-X: -32.4 in
	Accel-Y: 0.00 g	CG-Y: 0.0 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in
Perp.	Accel-X: 0.00 g	CG-X: 0.0 in
	Accel-Y: -1.20 g	CG-Y: 32.4 in
	Accel-Z: -1.20 g	CG-Z: 24.6 in

To simulate 1g acceleration in any direction, the patron CG and acceleration vectors were manipulated for load cases at 30deg increments from 0deg to 180deg. Since the structure is symmetric about the X-Z plane, only the first 180deg need to be analyzed. Nine load cases were analyzed using ABAQUS/CAE including 7 straight line acceleration load cases (0deg - 180deg) as well as one perpendicular load case where the wheels are oriented 90deg from the direction of travel. This case is to simulate high speed cornering at 1g.

The table to the left shows the cartesian vectors for the acceleration as well as the coordinates for the patron CG location per each load case. On the right is a visual representation of the patron CG location for each load case.



2. Analysis Overview

Welded Aluminum Specification and Discussion

"The damage is summarized in Aluminum Specification Table 3.3-2, Minimum Mechanical Properties for Welded Aluminum Alloys (included here as Appendix C and discussed in Section 4.5) ... The values in Table 3.3-2 for ultimate tensile strengths (F_{tuw}) must be multiplied by 0.9 before they are used for structural design. This is to account for the fact that welds may get only visual inspection and might not reliably attain the strengths in Table 3.3-2 due to undetected defects. This 0.9 factor is not applied to minimum properties other than ultimate tensile strength; here, as elsewhere in the Specification, the margin of safety against tensile fracture is the greatest concern." [3]

Although the text above recommends that a knockdown factor of 0.9 is to be used on the allowable stresses for welded aluminum, the proposed system is not intended for use at high cycles. Since inspection is not a concern, the 0.9 knockdown factor will be omitted, though the ultimate strength criteria for bridge type structures (as defined on Slide 10) will be used for the welded analysis.

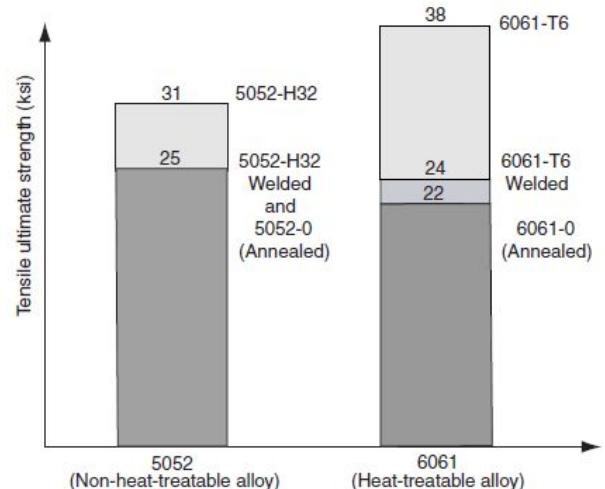


Figure 9.1 Effect of welding on tensile ultimate strength of alloys 5052 and 6061.

Ultimate Strength of Welded 6061-T6 (Defined in Graph) = **24.0ksi**
Required Ultimate Strength Factor of Safety (Bridge Type) = **2.20**
Corresponding Allowable Stress in Weld = $24.0\text{ksi} / 2.20 = 10.9\text{ksi}$

3. Vehicle Structural Analysis

Finite Element Model and Supporting Calculations

Vehicle Introduction

Analysis Overview

**Vehicle Structural
Analysis**

**Vehicle Mechanical
Analysis**

References

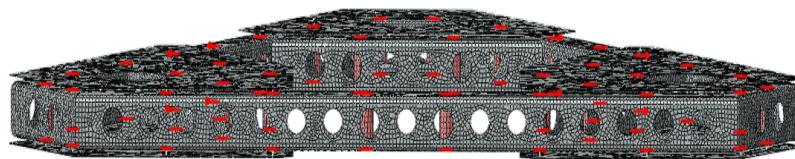


3. Vehicle Structural Analysis - Finite Element Model

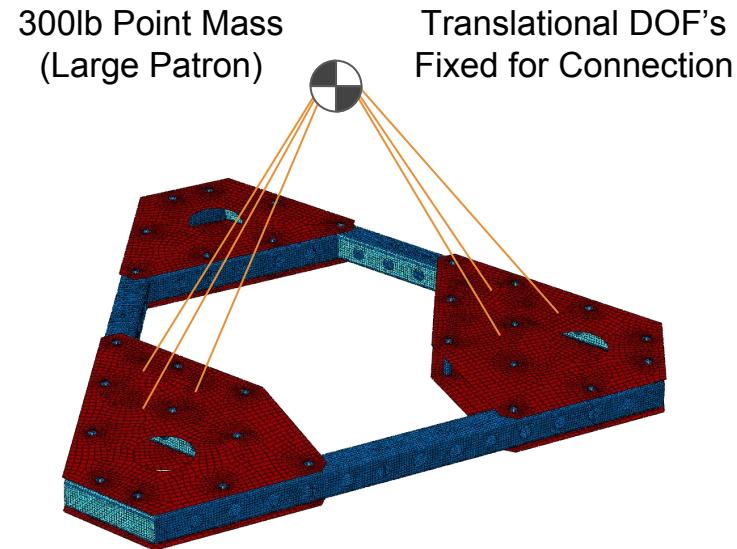
Finite Element Model of the Chassis

FEM Creation and Element Formation

- Gusset plates modeled with 2D, linear shell elements that are 0.25 in. big
- Beams and tubes modeled with 2D, linear shell elements that are 0.125 in. big
- bolts are modeled with 1D beam elements



The elements representing the crush tubes were stitched to the elements representing the beams. This is to model the welded connection by allowing direct transfer of load.



■ 6061-T6 : 0.188 in. Thick

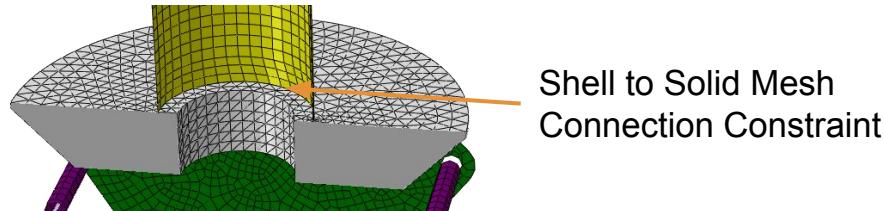
■ 6061-T6 : 0.125 in. Thick

3. Vehicle Structural Analysis - Finite Element Model

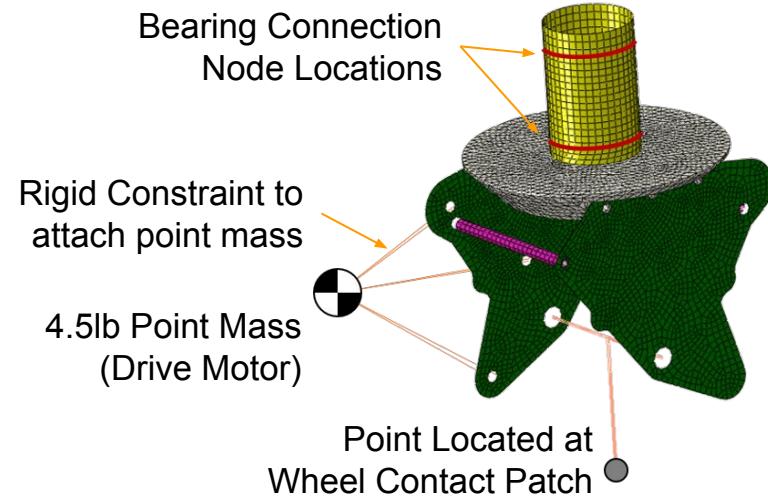
Finite Element Model of the Wheel Assembly

FEM Creation and Element Formation

- Side plates and shaft modeled with 2D, linear shell elements that are 0.125 in. big
- Connecting Plate modeled with 3D, linear tetrahedral elements that are 0.125 in. big
- bolts are modeled with 1D beam elements



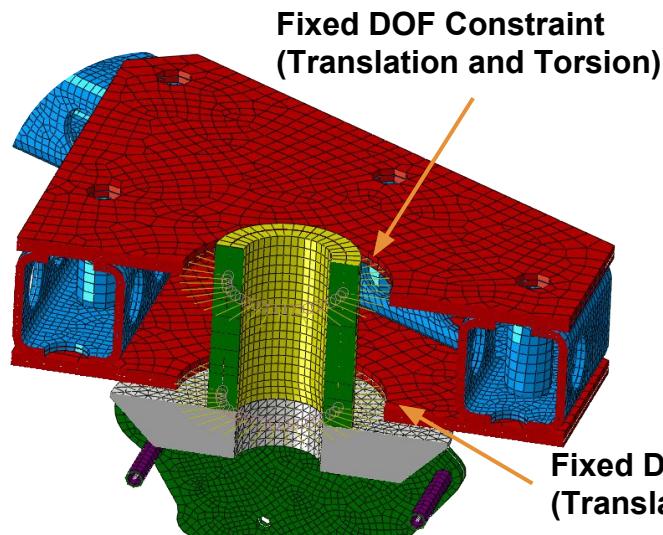
Instead of bolted connections, the nodes at the shaft and plate interface are merged to limit model size. Stresses in shaft connection are expected to be low.



3. Vehicle Structural Analysis - Finite Element Model

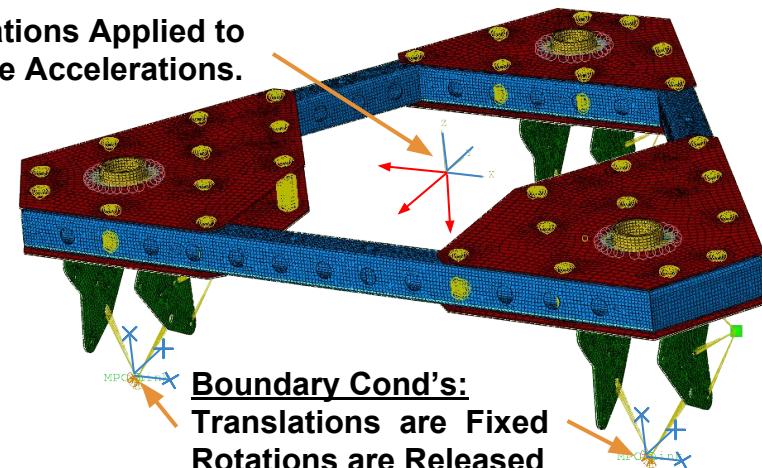
Finite Element Model of the Vehicle Assembly

The finite element assembly is shown on the right as well as the model loads and boundary conditions. Below is a detailed view of the part-to-part constraint that is consistent for all wheel assemblies.



LOADS:

Global Accelerations Applied to Simulate Vehicle Accelerations.



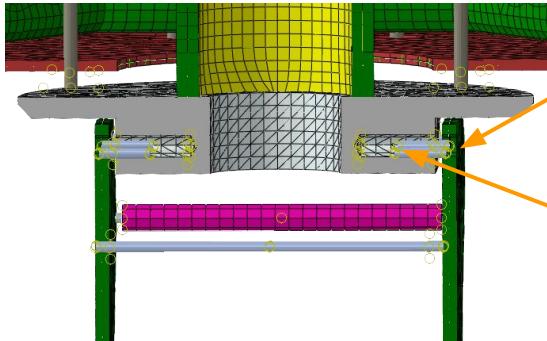
Total FEM Weight = 355.6 lbs

- Chassis Model 18.7 lbs
- Swerve Model (3) 12.3 lbs
- Large Patron 300 lbs

Assembly Bearing Connections
Shell Thickness Rendered for Clarity

3. Vehicle Structural Analysis - Finite Element Model

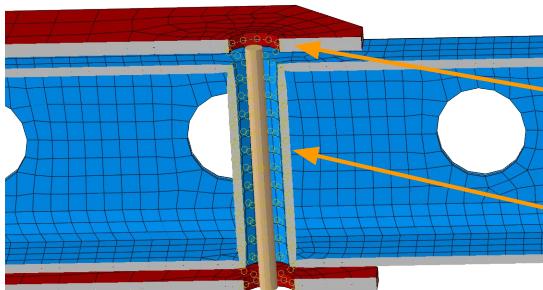
Modeling Bolted Connections



Bolted Connections in Wheel Assembly

End Nodes Connected
to Plate Shell Nodes

End Nodes Connected
to Solid Hole Nodes



Bolted Connections in Chassis

End Nodes Connected
to Plate Shell Nodes

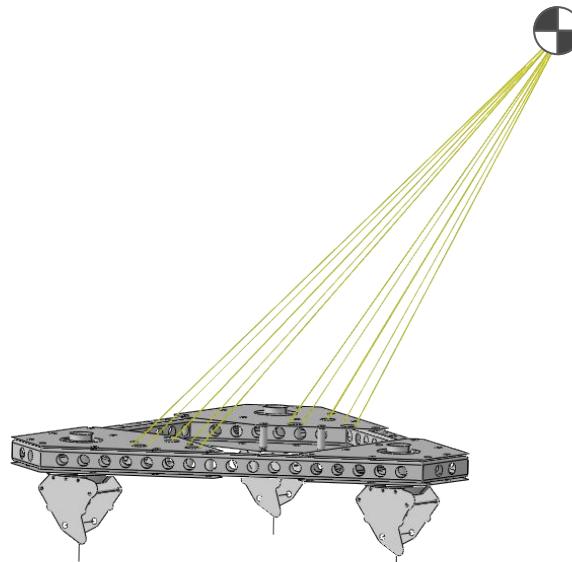
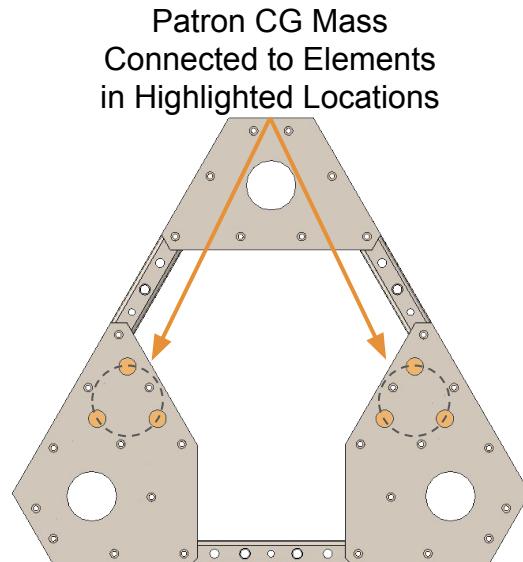
Mid Nodes Connected
to Tube Shell Nodes

For bolted connections, 1D beam elements were used with a simulation diameter twice the diameter of the proposed bolt. This is to ensure the model is adequately stiff and large deflections are avoided. The methodology used to the left is consistent for all bolted connections throughout this analysis. To account for preloaded bolts, rigid (fixed) elements were used to connect the beam nodes to the surface and solid nodes. This allows the transfer of both forces and moments.

3. Vehicle Structural Analysis - Finite Element Model

Modeling Patron Connections

To constrain the patron to the chassis, it was assumed that the feet would apply loads to the model in a distributed circle described on the below. Three smaller circles were created on the model to represent these force locations. The CG was then constrained using a Multi Point, Link constraint, the translation of the point mass was held constant while the CG was free to rotate, simulating the pitch/roll of the patron ankle.



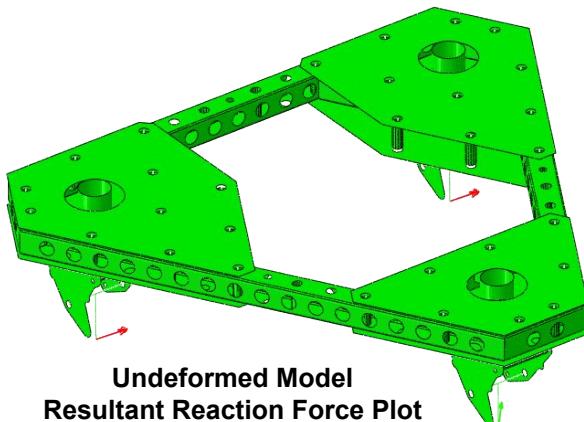
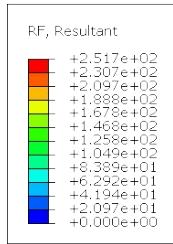
3. Vehicle Structural Analysis - Finite Element Model

Model Check: Simulation Reaction Forces

Reaction Forces

- Reactions Equal (*Model Mass * Accelerations*)
- Verify Loads, Masses, and Boundary Conditions

Load Case: 0deg



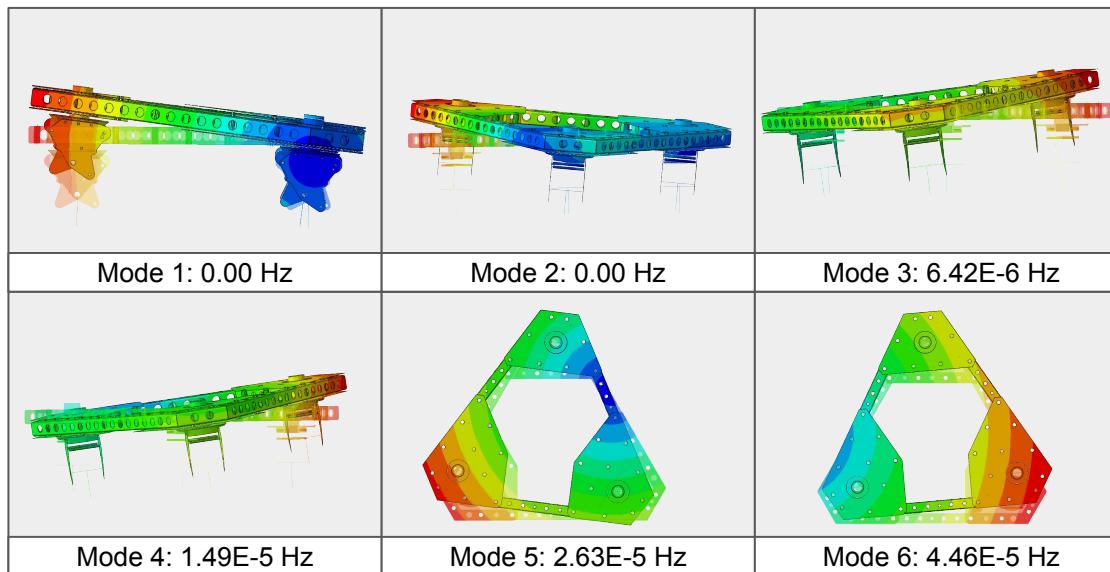
Load Case	Mass Information			MODEL REACTION FORCES AS COMPARED TO THE EXPECTED REACTION FORCES		
	Chassis Material	18.73 lbs	Output from Simulation	Expected Forces	Simulation Forces	Modeling Error
Dead Load	Patron (95th%)	300.0 lbs	Output from Simulation	Accel-X: 0.000 g Accel-Y: 0.000 g Accel-Z: -1.200 g	Force-X: 0.0 lbs Force-Y: 0.0 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
Wleg	Swerve System	38.84 lbs	Output from Simulation	Accel-X: -1.200 g Accel-Y: 0.000 g Accel-Z: -1.200 g	Force-X: -426.7 lbs Force-Y: 0.0 lbs Force-Z: -426.7 lbs	Percent Error: 100.0% Percent Error: 0.0% Percent Error: 0.0%
30deg	Total Mass	355.6 lbs	Mass Summation	Accel-X: -0.600 g Accel-Y: -1.039 g Accel-Z: -1.200 g	Force-X: -213.3 lbs Force-Y: -389.5 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
60deg				Accel-X: -1.039 g Accel-Y: -0.800 g Accel-Z: -1.200 g	Force-X: -389.5 lbs Force-Y: -213.3 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
90deg				Accel-X: -1.200 g Accel-Y: 0.000 g Accel-Z: -1.200 g	Force-X: -426.7 lbs Force-Y: 0.0 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
120deg				Accel-X: -1.039 g Accel-Y: 0.600 g Accel-Z: -1.200 g	Force-X: -389.5 lbs Force-Y: 213.3 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
150deg				Accel-X: -0.600 g Accel-Y: 1.039 g Accel-Z: -1.200 g	Force-X: -213.3 lbs Force-Y: 389.5 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%
180deg				Accel-X: 0.000 g Accel-Y: 1.200 g Accel-Z: -1.200 g	Force-X: 0.0 lbs Force-Y: 426.7 lbs Force-Z: -426.7 lbs	Percent Error: 0.0% Percent Error: 0.0% Percent Error: 0.0%

3. Vehicle Structural Analysis - Finite Element Model

Model Check: Free-Free Modes Analysis

Free-Free Modes

- Rigid body modes at least five orders below first flexural body mode
- Verify model is accurately constrained and all parts are connected



Below is a list of the first ten modes output by the Free-Free Modes Simulation. Note that the first six modes are the rigid body modes, while the modes following are flexural body modes. This is consistent with the rule listed above.

Frame	
Index	Description
0	Increment 0: Base State
1	Mode 1: Value = -3.33695E-08 Freq = 0.0000 (cycles/time)
2	Mode 2: Value = -1.62283E-08 Freq = 0.0000 (cycles/time)
3	Mode 3: Value = 1.62733E-09 Freq = 6.42034E-06 (cycles/time)
4	Mode 4: Value = 8.76245E-09 Freq = 1.48982E-05 (cycles/time)
5	Mode 5: Value = 2.73584E-08 Freq = 2.63248E-05 (cycles/time)
6	Mode 6: Value = 7.86217E-08 Freq = 4.46264E-05 (cycles/time)
7	Mode 7: Value = 657.16 Freq = 4.0800 (cycles/time)
8	Mode 8: Value = 837.53 Freq = 4.6060 (cycles/time)
9	Mode 9: Value = 1193.8 Freq = 5.4991 (cycles/time)
10	Mode 10: Value = 1858.1 Freq = 6.8604 (cycles/time)

3. Vehicle Structural Analysis

Safety Factor Summary by Load Case

Load Case	Assem. Criteria	Allow σ [ksi]	Expect σ [ksi]	Expect SF	Required SF
0deg	Chassis Assembly	35.0	14.28	2.45	1.85
	Chassis Welded	24.0	7.14	3.36	2.20
	Wheel Assemblies	35.0	6.32	5.54	1.85
30deg	Chassis Assembly	35.0	14.75	2.37	1.85
	Chassis Welded	24.0	7.81	3.07	2.20
	Wheel Assemblies	35.0	8.77	3.99	1.85
60deg	Chassis Assembly	35.0	8.67	4.04	1.85
	Chassis Welded	24.0	8.63	2.78	2.20
	Wheel Assemblies	35.0	5.66	6.18	1.85
90deg	Chassis Assembly	35.0	6.80	5.15	1.85
	Chassis Welded	24.0	7.78	3.08	2.20
	Wheel Assemblies	35.0	8.31	4.21	1.85
120deg	Chassis Assembly	35.0	10.68	3.28	1.85
	Chassis Welded	24.0	5.43	4.42	2.20
	Wheel Assemblies	35.0	6.70	5.22	1.85
150deg	Chassis Assembly	35.0	12.49	2.80	1.85
	Chassis Welded	24.0	4.26	5.64	2.20
	Wheel Assemblies	35.0	6.35	5.51	1.85
180deg	Chassis Assembly	35.0	10.82	3.24	1.85
	Chassis Welded	24.0	3.61	6.66	2.20
	Wheel Assemblies	35.0	4.82	7.26	1.85
Perpendicular	Chassis Assembly	35.0	7.13	4.91	1.85
	Chassis Welded	24.0	8.53	2.81	2.20
	Wheel Assemblies	35.0	8.61	4.07	1.85

The expected stresses and resulting safety factors for the structural components are listed to the left. All analyzed components meet the required strength. The load cases with the smallest margin for each part is highlighted in green and corresponding stress contours are displayed on the following slides. For convenience, the minimum required safety factors for aluminum are listed below.

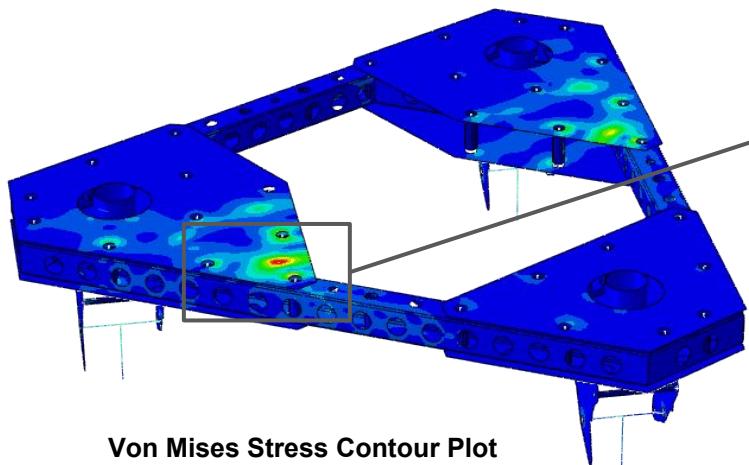
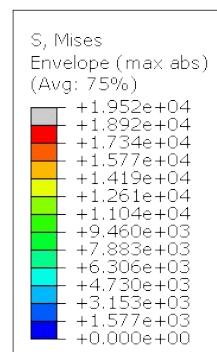
TABLE 6.1 Safety Margins in the Aluminum Specification [3]

Type of Structure	Yield Strength	Ultimate Strength
Building Type	1.65	1.95
Bridge Type	1.85	2.20

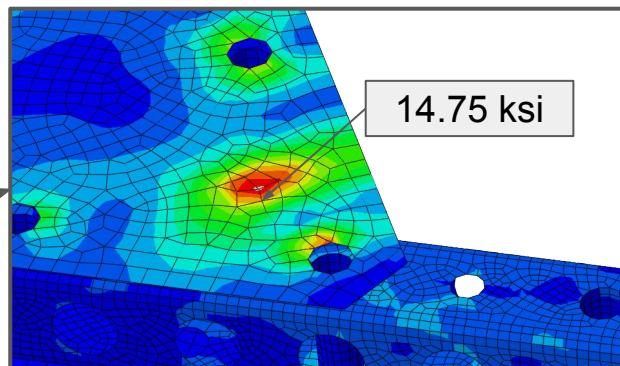
3. Vehicle Structural Analysis - Finite Element Model

Expected Von Mises Stresses are Acceptable in Chassis Gusset Plates

Load Case: 30deg



Units above are in psi
 $35 \text{ ksi} / 1.85 = 18.9 \text{ ksi}$



Components Removed for Clarity

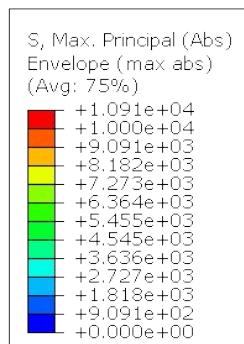
Yield Strength of 6061-T6 = 35 ksi
Expected Stress in Part = 14.75 ksi
Resulting FoS = **2.37 > 1.85**

Stresses evaluated in the chassis gusset plates are compared to the dynamic loading (bridge type) yield safety factor of 1.85. Stresses near bolted and patron connections are evaluated two elements away from the connection to ignore singularities and artifacts of the simulation. This provides a nominal stress in the parent material at the connection location.

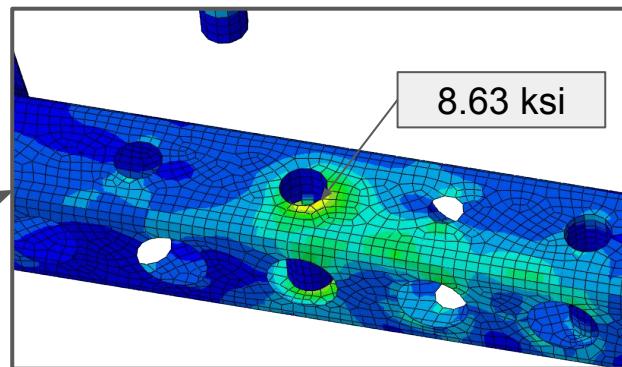
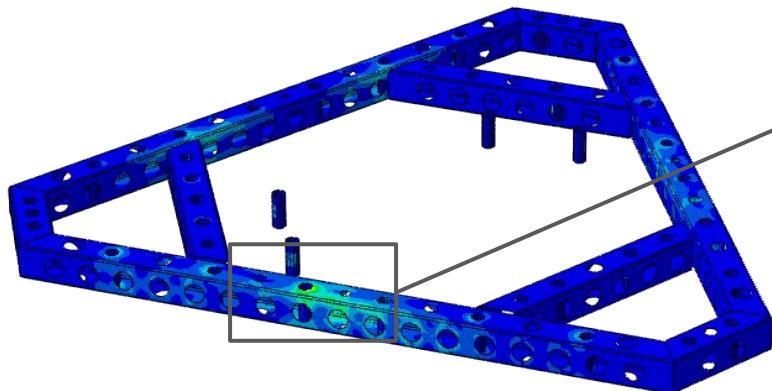
3. Vehicle Structural Analysis - Finite Element Model

Expected Principal Stresses are Acceptable in Welded 6061-T6 Material

Load Case: 60deg



Units above are in psi
 $24 \text{ ksi} / 2.20 = 10.9 \text{ ksi}$



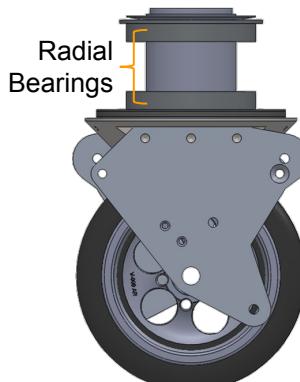
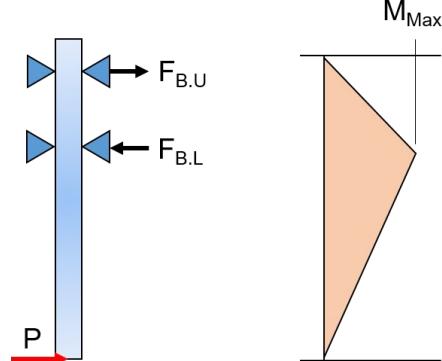
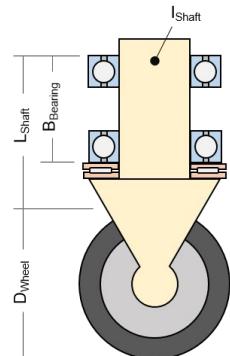
Ult. Strength Welded 6061-T6 = 24 ksi
Expected Stress in Part = 8.63 ksi
Resulting FoS = **2.78 > 2.20**

Stresses evaluated in the chassis beam members are compared to the dynamic loading (bridge type) ult safety factor of 2.20. Stresses at welded connections are evaluated at the worst nodal location, typically at the node connecting the crush tube and the chassis beam. Evaluating stresses at this location is to account for welding defects despite the conservative stress values due to the singularity of connecting shell elements at 90deg angles.

3. Vehicle Structural Analysis - Supporting Calculations

Bending Stresses in Rotating Yaw Shaft

Bending Stresses Induced in Rotating Yaw Shaft				
Name	Var	Val	Unit	Comment / Equation
<i>System Geometry</i>				
Wheel Diameter	D _{Wheel}	5	in	Assumed
Shaft Length Above Wheel	L _{shaft}	3.29	in	Assumed
Distance Between Bearings	Bearing	2.03	in	Height of Beams
Shaft Outer Diameter	d _{outer}	1.97	in	50mm Shaft to Inches
Shaft Inner Diameter	d _{inner}	1.18	in	Required for Slip Ring
<i>Load Information (Assumed on One Wheel)</i>				
Acceleration of Vehicle	a	1.0 g		Specified from Stakeholder
Weight of Passenger	w _p	300 lbs		95th Percentile Male
Weight of System	w _s	62.5 lbs		Assumed per Weight Budget
Total Weight of System	W	363 lbs		= w _p + w _s
Total Mass of System	m	0.94 slug*in		= W / 386.4
Applied Load at Bottom of Wheel	P	363 lbs		= m * (a * 386.4)
<i>Modeled as an Overhang Beam</i>				
Shaft Area Moment of Inertia	I _{shaft}	0.64 in ⁴		= ($\pi/64$) * (d _{outer} ⁴ - d _{inner} ⁴)
Effective Beam Length	L _{eff}	8.29 in4		= D _{Wheel} + L _{shaft}
Reaction Force on Lower Bearing	F _{B,L}	1478 lbs		= (P * L _{eff}) / Bearing
Reaction Force on Upper Bearing	F _{B,U}	-1116 lbs		= P - F _{B,L}
Maximum Bending Moment	M _{Max}	-2267 in-lbs		= F _{B,U} * Bearing
Bending Stress on Shaft	σ_{Bend}	3476 psi		= M _{Max} * (d _{outer} / 2) / I _{shaft}
Aluminum 6061-T6 Yield Strength	σ_{Yield}	35000 psi		Referenced in MMPDS
Resulting Factor of Safety	FoS	10.1 > 1.85		= σ_{Yield} / σ_{Bend}



The bending stresses in the vehicle rotating yaw shaft were determined by modeling the shaft as an effective beam. Although the bolt preload and the bolt holes are not considered, the significant strength margin proves the design is sufficient.

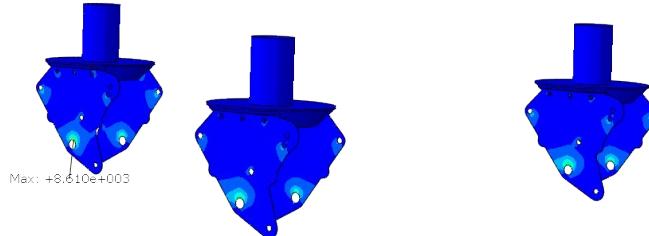
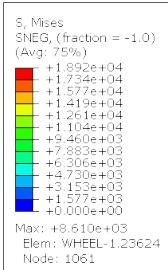
3. Vehicle Structural Analysis - Finite Element Model

Small Hole Analysis Methodology

The wheel assembly includes small holes for mounting electronics and sensors. These holes affect the mesh size and can increase the solve time. The model is idealized by removing these small holes and a nominal stress through the section is determined by the finite element solver. Using the stress concentration equations on the right, the adjusted stress can be calculated. For simplicity, the same concentration factor equations apply to holes in near proximity to others.

The maximum stresses were calculated in the wheel assembly plates over all load cases. It was determined that the *Perpendicular* load case was the most severe, and it can be seen below.

Load Case:
Perpendicular



Von Mises Stress Contour Plot

Units above are in psi

$$35 \text{ ksi} / 1.85 = 18.9 \text{ ksi}$$

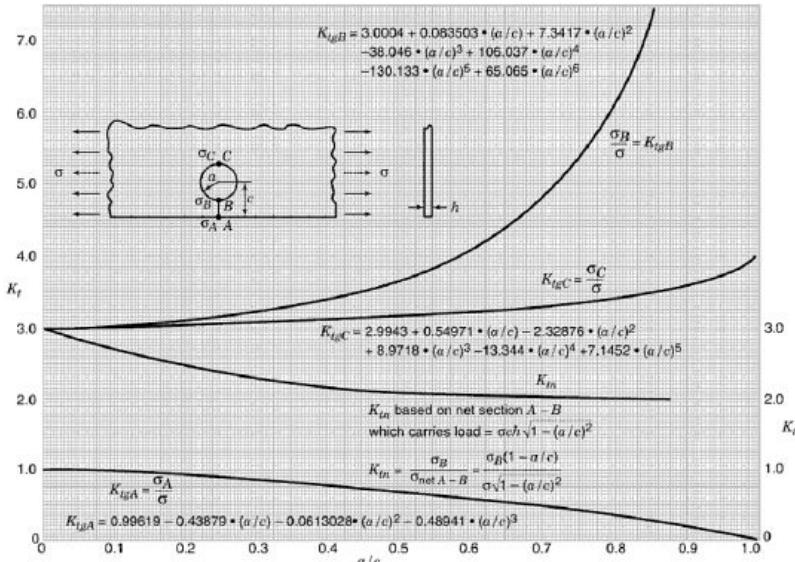


Figure above taken from Reference 5.

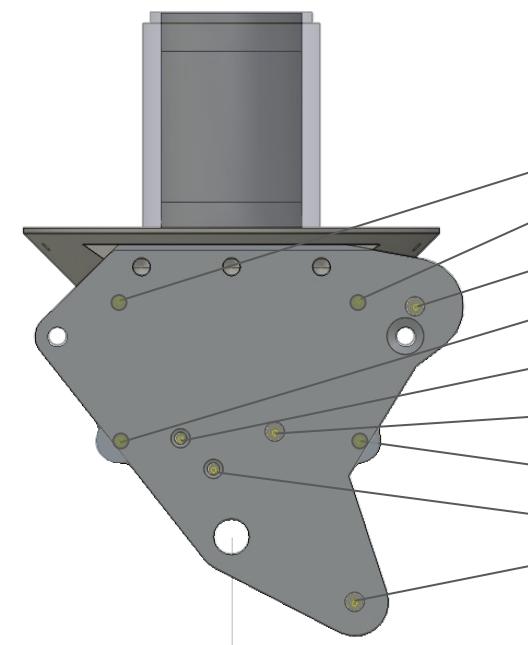
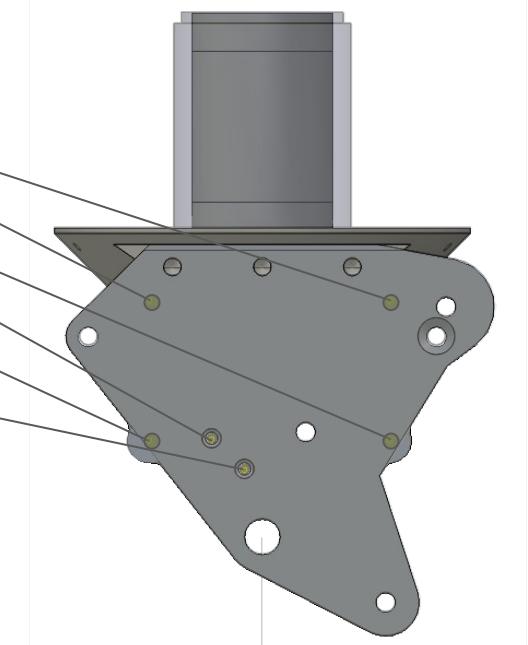
The stress contour plot for the front wheel assembly is detailed on following slides.

3. Vehicle Structural Analysis - Finite Element Model

Small Hole Locations in Wheel Assembly Side Plates

The holes shown below were idealized out of the finite element model. The hole diameter and distance away from the nearest edge or adjacent hole was recorded and used to determine the appropriate stress concentration factor. The results are tabulated on the following pages and the adjusted stress value is compared to the allowable.

Hole	Dia. [in]
L1	0.130
L2	0.130
L3	0.130
L4	0.136
L5	0.130
L6	0.136



Hole	Dia. [in]
R1	0.130
R2	0.130
R3	0.213
R4	0.130
R5	0.136
R6	0.213
R7	0.130
R8	0.136
R9	0.213

3. Vehicle Structural Analysis - Finite Element Model

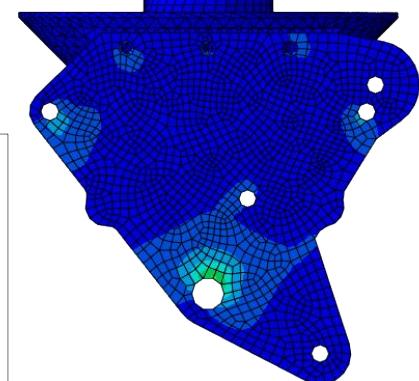
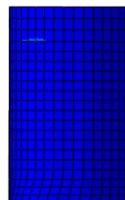
Small Hole Stresses in Left Side Plate of Wheel Assembly

Hole	Dia. [in]	Dist [in]	Rad/Dist	K _{tgA}	K _{tgB}	K _{tgC}	Nom. σ	Adjust σ
L1	0.130	0.459	0.14	0.92	3.09	3.05	0.74	2.28
L2	0.130	0.353	0.18	0.89	3.12	3.06	1.30	4.06
L3	0.130	0.250	0.26	0.83	3.20	3.08	0.50	1.59
L4	0.136	0.432	0.16	0.91	3.10	3.05	0.82	2.55
L5	0.130	0.250	0.26	0.83	3.20	3.08	0.48	1.54
L6	0.136	0.432	0.16	0.91	3.10	3.05	2.35	7.29

The most severe load case for the wheel assemblies is the *Perpendicular* load case. A detailed view of the nominal stress in the left side plate of the front wheel assembly is shown to the right. The table above uses values from this contour plot.

Max Expected Stress = 7.29 ksi
6061-T6 Yield Stress = 35.0 ksi
FoS 35.0 / 7.29 = 4.80 > 1.85

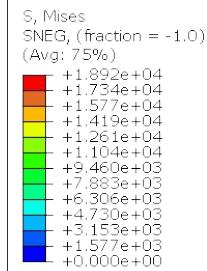
Front Wheel Assembly
Left Side Shown



Von Mises Stress Contour Plot
Units above are in psi
35 ksi / 1.85 = 18.9 ksi

Front Wheel Assembly Left Side Shown

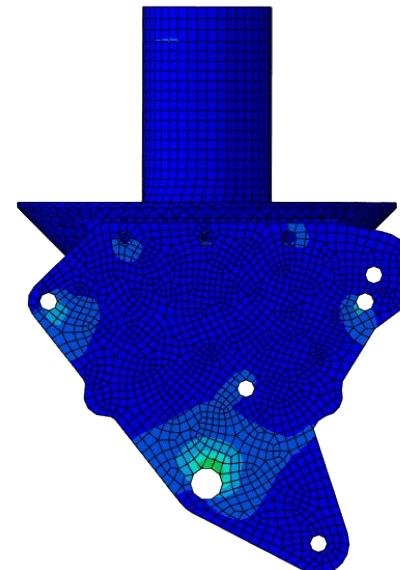
*Load Case:
Perpendicular*



Units above are in psi

$$35 \text{ ksi} / 1.85 = 18.9 \text{ ksi}$$

Max Expected Stress = 7.29 ksi
6061-T6 Yield Stress = 35.0 ksi
FoS 35.0 / 7.29 = 4.80 > 1.85



Von Mises Stress Contour Plot

3. Vehicle Structural Analysis - Finite Element Model

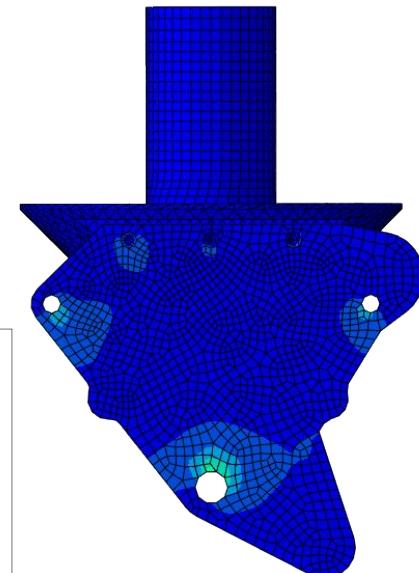
Small Hole Stresses in Right Side Plate of Wheel Assembly

Hole	Dia. [in]	Dist [in]	Rad/Dist	K _{tgA}	K _{tgB}	K _{tgC}	Nom. σ	Adjust σ
R1	0.130	0.459	0.14	0.92	3.09	3.05	1.72	5.31
R2	0.130	0.353	0.18	0.89	3.12	3.06	0.94	2.92
R3	0.213	0.155	0.69	0.25	4.73	3.30	0.07	0.35
R4	0.130	0.250	0.26	0.83	3.20	3.08	0.62	1.99
R5	0.136	0.432	0.16	0.91	3.10	3.05	0.72	2.22
R6	0.213	0.730	0.15	0.92	3.09	3.05	0.67	2.08
R7	0.130	0.250	0.26	0.83	3.20	3.08	0.45	1.44
R8	0.136	0.432	0.16	0.91	3.10	3.05	1.53	4.75
R9	0.213	0.375	0.28	0.81	3.23	3.09	0.15	0.47

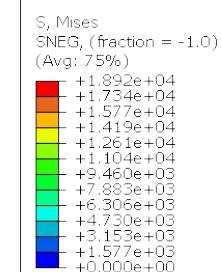
The most severe load case for the wheel assemblies is the *Perpendicular* load case. A detailed view of the nominal stress in the right side plate of the front wheel assembly is shown to the right. The table above uses values from this contour plot.

Max Expected Stress = 5.31 ksi
6061-T6 Yield Stress = 35.0 ksi
FoS 35.0 / 5.31 = 6.59 > 1.85

Front Wheel Assembly
Right Side Shown



Load Case:
Perpendicular



Units above are in psi
35 ksi / 1.85 = 18.9 ksi

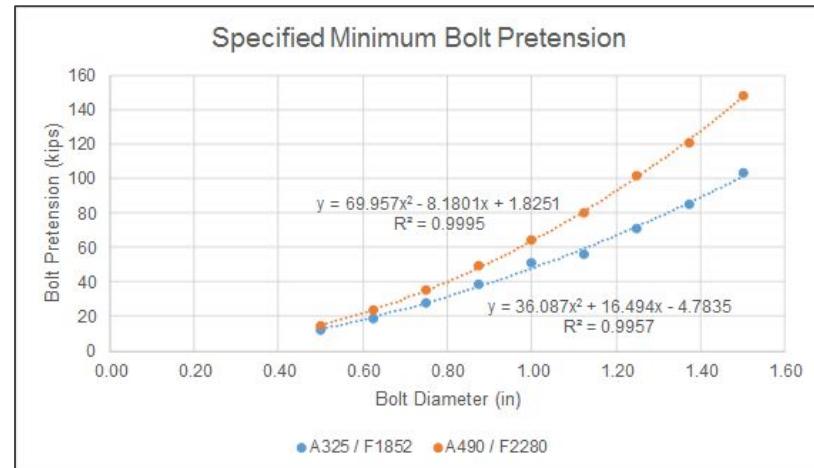
Von Mises Stress Contour Plot

3. Vehicle Structural Analysis - Finite Element Model

Required Pretension for Bolted Structural Connections

Nominal Bolt Diameter	Specified Minimum Bolt Pretension, T_m (kips)	
	ASTM A325 and F1852	ASTM A490 and F2280
1/2	12	15
5/8	19	24
3/4	28	35
7/8	39	49
1	51	64
1 1/8	56	80
1 1/4	71	102
1 3/8	85	121
1 1/2	103	148

Table 7.1 Minimum Bolt Pretension for Pre-Installation Verification [6]



Interpolating to a Different Diameter Bolt

Diameter = 0.25 in	1.60 kips	4.15 kips
Bolt Specification:	A325 / F1852	A490 / F2280

To accurately analyze the bolted connections, preload values for the structural connections were required. Using Table 7.1 presented in the *Specification for Structural Joints Using High-Strength Bolts* from the Research Council on Structural Connections (RCSC), a quadratic fit was calculated using the documented values, and different bolt pretensions were determined. It is shown on the next page that the A325 / F1852 value is required for slip-critical joints, though the system is expected to operate safely in the event of bolt slipping.

3. Vehicle Structural Analysis - Finite Element Model

Bolted Joint Analysis: RCSC Calculations

RCSC Bolt Calculations for 1/4 - 20 Bolts					
Name	Var	Val	Unit	Comment / Equation	Eqn #
<i>Constants and Factors for Bolted Connection</i>					
Required Tensile Strength	T_u	0.35 kips		Output From FEM Simulation Defined by CAD Geometry	
Required Shear Strength	V_u	0.37 kips			
Nominal Diameter of Bolt	d_b	0.25 in			
Clamped Material Thickness	t	0.19 in			
Hole Clearance Distance	L_c	0.06 in			
Resistance Factor	Φ	0.75		RCSC Specified, Except for Slip Critical	
<i>Shear and Tension Check</i>					
Nominal Strength per Unit Area	F_{n-Ten}	90 ksi		Values Referenced in Table 5.1	
Nominal Strength per Unit Area	$F_{n-Shear}$	54 ksi			
Bolt Cross-sectional Area	A_b	0.05 in ²		$= (\pi / 4) * d_b^2$	
Nominal Tensile Strength of Bolt	R_{n-Ten}	5.89 kip		$= F_{n-Ten} * A_b / \Phi$	(5.1)
Nominal Shear Strength of Bolt	$R_{n-Shear}$	3.53 kip		$= F_{n-Shear} * A_b / \Phi$	(5.1)
Resulting Tension Safety Factor	$X_{Tension}$	16.7 > 1.67		$= R_{n-Ten} / T_u$	
Resulting Shear Safety Factor	X_{Shear}	9.6 > 1.67		$= R_{n-Shear} / V_u$	

The required tensile and resultant shear strengths were extracted from the finite element model beam elements. For conservatism, it was assumed that the maximum shear and tensile forces acted on the same bolt. The equations and analysis procedure were referenced using Reference 6, and the resulting tension and shear safety factors are referenced using Reference 7.

RC SC Bolt Calculations for 1/4 - 20 Bolts (Continued)					
Name	Var	Val	Unit	Comment / Equation	Eqn #
<i>Combined Shear and Tension Check</i>					
Design Strength in Tension	$(\Phi R_n)_t$	4.42 kip		$= R_{n-Ten} / T_u$	
Design Strength in Shear	$(\Phi R_n)_v$	2.65 kip		$= R_{n-Shear} / V_u$	
Limit-State of Bolt Configuration	L_{Comb}	0.03		$= [T_u / (\Phi R_n)_t]^2 + [V_u / (\Phi R_n)_v]^2$ (5.2)	
Resulting Combination Margin	X_{Comb}	38.9 > 1.67		$= 1 / L_{Comb}$	
<i>Bearing Strength Calculations</i>					
Tensile Strength for 6061-T6	F_u	35.0 ksi		Yield Material in Bearing	
Capacity of Material (Lowest Factor)	R_{Cap}	3.28 kip		$= 2 * d_b * t * F_u$	(5.5)
Required Bolt Load (Highest Factor)	R_n	0.62 kip		$= 1.5 * L_c * t * F_u$	(5.4)
Resulting Combination Margin	$X_{Bearing}$	5.3 > 1.85		$= R_{Cap} / R_n$	
<i>Slip Critical Connection</i>					
Resistance Factor for Slip Critical	Φ	0.85		Specified RCSC Section 5.4.1	
Mean Slip Coefficient	μ	0.33		Assume Lowest Slip Coefficient	
Pretension Multiplier	D_u	1.0		Assume Bolt Pretensioned to Minimum	
Number of Bolts in Joint	N_b	1		Assume Load on One Bolt	
Specified Minimum Pretension	T_m	1.60 kip		Interpolated From Table 7.1	
Nominal Slip Resistance of Plane	R_n	0.41 kip		$= \mu * D_u * T_m * N_b [1 - T_u / (D_u T_m N_b)]$ (5.6)	
Resulting Slip Critical Margin	X_{Slip}	1.1 > 1.0		$= R_n / V_u$	

Equations and Analysis Procedure Correspond to RCSC 2009 [6]

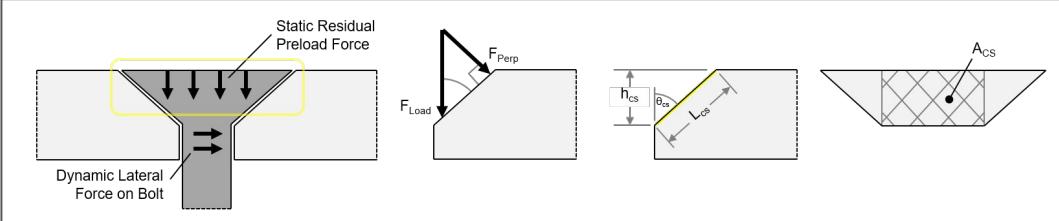
Load Case: 150deg Configuration

3. Vehicle Structural Analysis - Supporting Calculations

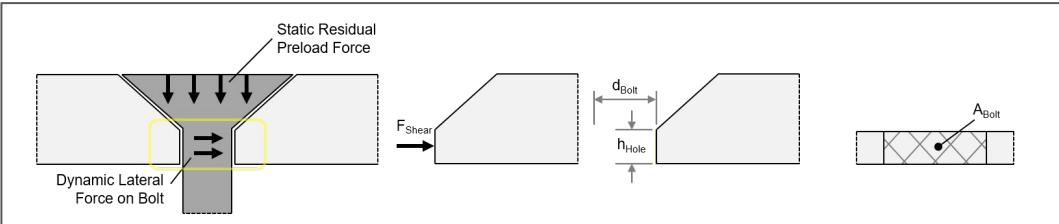
Countersunk Bolted Connections on Chassis Gusset Plates

Countersink Preload and Dynamic Bolt Loading			
Name	Var	Val	Unit
<i>Material Specifications and System Geometry</i>			
Bearing Strength 6061-T6	$\sigma_{Bearing}$	50000 psi	Referenced in MMPDS
Angle of Countersink	θ_{CS}	100 deg	Given
Gusset Plate Thickness	t_{Gusset}	0.188 in	Specified in CAD
Height of Countersink	h_{CS}	0.095 in	Specified by Countersink
Inner Diameter of Countersink	d_{Bolt}	0.25 in	1/4-20 Bolt Diameter
<i>Preload Derivation and Dynamic Loading</i>			
Preload Applied to Joint	F_{Load}	1600 lbs	Assumed Preload Applied
Angle of Taper (1/2 Side)	$\theta_{Working}$	0.873 rad	$= (\pi/180) * (\theta_{CS}/2)$
Perpendicular Force	F_{Perp}	1226 lbs	$= F_{Load} * \sin(\theta_{Working})$
Max Shear Force on Bolt	F_{Shear}	369 lbs	Output From FEM
<i>Projected Area Derivation</i>			
Height of Through Hole	h_{Hole}	0.092 in	$= t_{Gusset} - h_{CS}$
Countersink Taper Length	L_{CS}	0.148 in	$= h_{CS} / \cos(\theta_{Working})$
Projected Countersink Area	A_{CS}	0.116 in ²	$= \pi * L_{CS} * d_{CS}$
Projected Bolt Shank Area	A_{Bolt}	0.023 in ²	$= h_{Hole} * d_{CS}$
<i>Expected Stresses - Preload and Dynamic</i>			
Preload Bearing Stress	$\sigma_{PreLoad}$	10533 psi	$= F_{Perp} / A_{CS}$
Dynamic Bearing Stress	$\sigma_{Dynamic}$	16002 psi	$= F_{Shear} / A_{Bolt}$
Expected Total Bearing Stress	σ_{Expect}	26535 psi	$= \sigma_{PreLoad} + \sigma_{Dynamic}$
Bearing Strength Safety Factor: 1.88 > 1.85 OK			

Preload Residual Stresses



Dynamic Bearing Stresses



The total stress in the countersink connection is the superposition of residual stresses due to preload and the dynamic stresses due to loading. It is conservative to add the stresses together. The shear and preload values are referenced on previous pages.

4. Vehicle Mechanical Analysis

Supporting Calculations

Analysis Overview

Vehicle Structural
Analysis

Vehicle Mechanical
Analysis

References

Appendix

4. Vehicle Mechanical Analysis

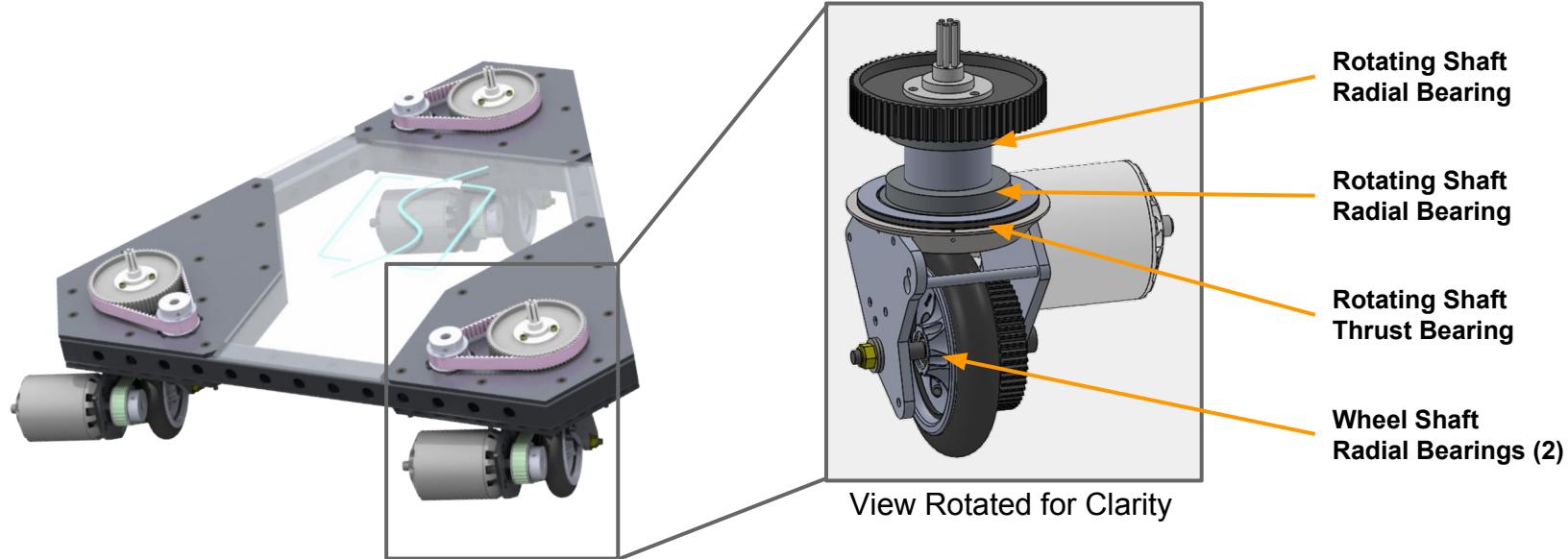
Safety Factor Summary by Component

The expected stresses and resulting safety factors for the mechanical components are listed below. For the mechanical components, either stresses or forces were analyzed and were then compared to documented allowables. The resulting safety factor is calculated below and compared to the required safety factor. If the component is a consumer off the shelf (COTS) part, the required safety factor is 1.0. The cutsheets for the COTS parts can be found in the appendix.

<u>Component</u>	<u>Specification</u>	<u>Allowable</u>	<u>Expected</u>	<u>Expect SF</u>	<u>Required SF</u>
<i>Radial Bearing Yaw Shaft</i>	Force Margin	2.63 kip	1.5 kip	1.78	> 1.00
<i>Thrust Bearing Yaw Shaft</i>	Force Margin	11.6 kip	0.6 kip	19.3	> 1.00
<i>Radial Bearing Wheel Shaft</i>	Force Margin	405 lbs	300 lbs	1.35	> 1.00
<i>Timing Belt</i>	Force Margin	750 lbs	587 lbs	1.28	> 1.00
<i>Wheel Shaft Shoulder Bolt</i>	Axial Stress	160 ksi	102 ksi	1.57	> 1.00
	Shear Stress	160 ksi	6.0 ksi	26.8	> 1.00
	Bearing Stress	54 ksi	7.4 ksi	7.33	> 1.85
<i>Motor Bolts</i>	Shear Stress	500 MPa	17.9 MPa	27.9	> 1.00
	Bearing Stress	372 MPa	47.9 MPa	7.78	> 1.85

4. Vehicle Mechanical Analysis

Vehicle Bearings - Design



Each wheel assembly includes two radial bearings on the rotating yaw shaft as well as a thrust bearing. Additionally, each assembly includes two radial bearings pressed into the wheel hub and another radial bearing pressed into the timing belt pulley (enveloped in the following calculations).

4. Vehicle Mechanical Analysis

Vehicle Bearings - Force Margins

Force Margin for Bearings

Name	Var	Val	Unit	Comment / Equation
<i>Rotating Yaw Shaft - Radial Bearing</i>				
Max Expected Load on Bearing	P_{Expect}	1.48 kip		Reaction Force on Lower Bearing
Allowable Load on Bearing (KN)	P_{Allow}	11.7 KN		VXB F6910ZZ Static Load
Allowable Load on Bearing (lbs)	P_{Allow}	2.63 kip		Conversion to Imperial Units
Resulting Force Margin	X_{Thrust}	1.78		$= P_{Allow} / P_{Expect}$

Rotating Yaw Shaft - Thrust Bearings

Maximum Patron Load	W_{Patron}	300 lbs	Max Patron Allowable
Abuse Loading Factor	f_{Abuse}	2.0	Conservative Impact Factor
Max Expected Load on Bearing	P_{Expect}	0.60 kip	$= W_{Patron} * f_{Abuse} / 1000$
Allowable Load on Bearing (KN)	P_{Allow}	51.6 KN	Koyo NRB NTA-5266 Dynamic Load
Allowable Load on Bearing (lbs)	P_{Allow}	11.6 kip	Conversion to Imperial Units
Resulting Force Margin	X_{Thrust}	19.3	$= P_{Allow} / P_{Expect}$

Wheel Shaft - Radial Bearing

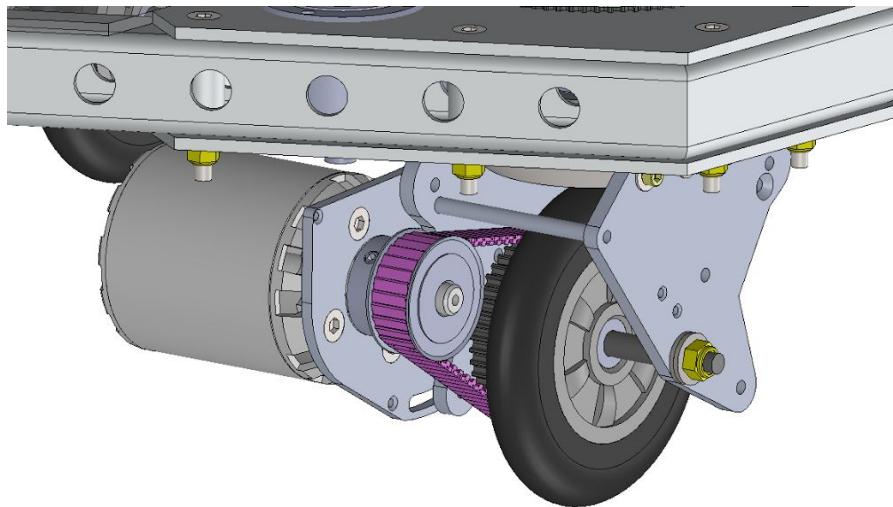
Number of Bearings	$N_{Bearing}$	2	Bearings Pressed into Wheel Hub
Max Expected Load on Bearing	P_{Expect}	600 lbs	$= W_{Patron} * f_{Abuse}$
Allowable Load on Bearing (KN)	P_{Allow}	1800 N	AST 71900C Static Load
Allowable Load on Bearing (lbs)	P_{Allow}	404.7 lbs	Conversion to Imperial Units
Resulting Force Margin	X_{Thrust}	1.35	$= P_{Allow} / (P_{Expect} / N_{Bearing})$

Using bearing cutsheets available online, the expected forces through the bearings were compared to the rated allowables. All bearing force margins were calculated considering a 300lb patron moving at the maximum acceleration, and in the most severe direction, in order to react the forces on one wheel assembly.

For the bearing reaction force calculation, please refer to the *Bending Stresses in Rotating Yaw Shaft* calculations. In all calculations shown to the left, the expected forces, P-Expect, are compared against the allowable force, P-Allow.

4. Vehicle Mechanical Analysis

Timing Belt Pulley - Design



Single Wheel Assembly
Shown for Clarity

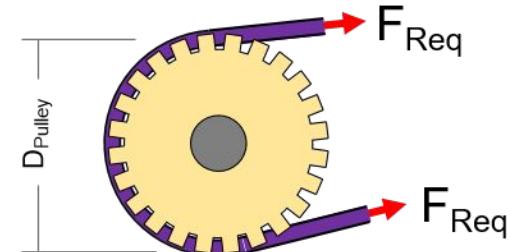
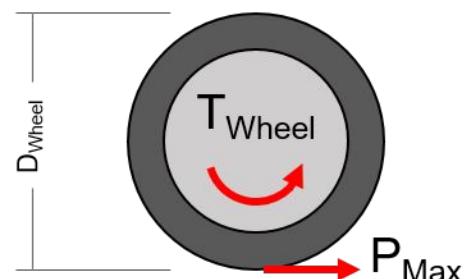
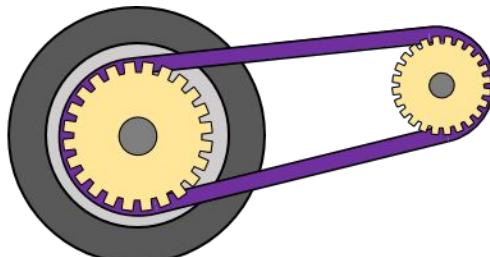
An L-Series timing belt is proposed for the propulsion system (shown in purple). The belt will be tensioned by rotating the motor mount plate away from the wheel. The wheel pulley is attached to the wheel through six bolts to transfer the torque. By using the maximum expected load on the wheel as well as the maximum acceleration, the load through the timing belt could be calculated.

4. Vehicle Mechanical Analysis

Timing Belt Pulley - Force Margin

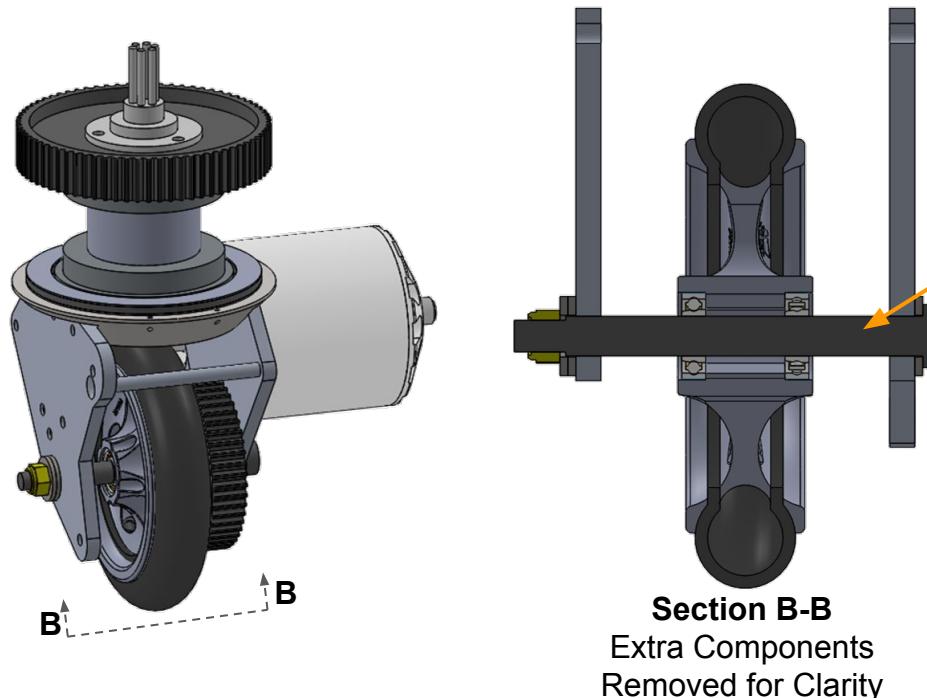
Force Margin for Timing Belt Pulley				
Name	Var	Val	Unit	Comment / Equation
System Geometry and Belt Specifications				
Maximum Force on Wheel	P _{Max}	362.5 lbs		Weight of System and Patron
Diameter of Wheel	D _{Wheel}	5.0 in		5in Pneumatic Wheel
Diameter of Pulley (mm)	D _{Pulley}	78.4 mm		SDP-SI Pulley Listed Below
Diameter of Pulley (inch)				Convert to Inch Measurement
Belt Breaking Strength (per Width)	F _{Break}	125 lbs/(1/8")		SDP-SI L Timing Belts
Width of Timing Belt	W _{Belt}	0.75 in		SDP-SI L Timing Belts
Resulting Calculations for Timing Belt				
Total Breaking Strength on Belt	F _{Belt}	750.0 lbs	= F _{Break} * (W _{Belt} / 0.125)	
Effective Torque on Pulley	T _{Wheel}	906.3 in-lbs	= P _{Max} * (D _{Wheel} / 2)	
Force Required by Belt	F _{Req}	587.2 lbs	= T _{Wheel} / (D _{Pulley} / 2)	
Resulting Force Margin	X _{Force}	1.28	= F _{Belt} / F _{Req}	

Using the total weight of the system (300lb patron and 62.5lb vehicle), a conservative force margin in the timing belt was calculated. Since it is assumed that the total weight is on one pulley assembly, the narrow force margin listed to the left is acceptable.



4. Vehicle Mechanical Analysis

Wheel Shaft - Design

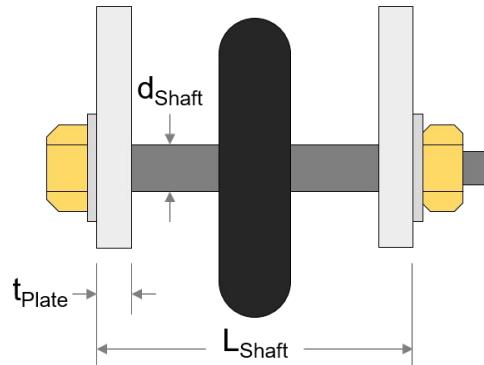


Analyzed Shaft

A 10mm diameter shoulder bolt supports the wheel and pulley assembly. The bolt is secured to the side plates of the wheel assembly and load is transferred through the bearings.

4. Vehicle Mechanical Analysis

Wheel Shaft - Calculations

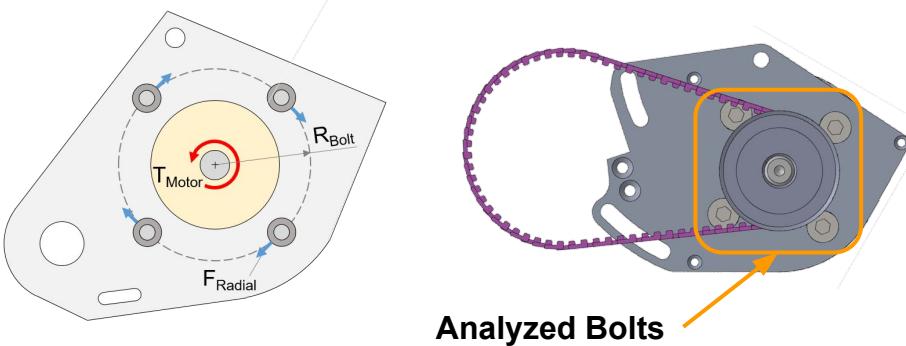


Using the total weight of the system (300lb patron and 62.5lb vehicle) and an impact / abuse factor, conservative strength safety factors for the wheel shaft were calculated. Considering the bending and shear of the shaft as well as the bearing loads in the plate, the calculated margins are acceptable and the design is sufficient for the expected loads.

Wheel Shaft Strength Calculations				
Name	Var	Val	Unit	Comment / Equation
<i>System Geometry and System Loading</i>				
Shaft Diameter (mm)	d_{Shaft}	10 mm	10mm Shoulder Bolt Diameter	
Shaft Diameter (in)	d_{Shaft}	0.39 in	Conversion to Imperial Units	
Unsupported Length	L_{Shaft}	3.4 in	Unsupported Length of Bolt	
Thickness of Plate Support	t_{Plate}	0.25 in	Side Plate Thickness	
Total Weight of System	W	363 lbs	Weight of System and Patron	
Abuse Loading Factor	f_{Abuse}	2.0	Conservative Impact Factor	
<i>Aluminum and Bolt Allowables</i>				
Aluminum 6061-T6 Yield Strength	σ_{Alum-Y}	35.0 ksi	Referenced in MMPDS	
Aluminum 6061-T6 Bearing Strength	σ_{Alum-B}	54.0 ksi	Referenced in MMPDS	
Class 12.9 Min Yield Strength (MPa)	σ_{Bolt-Y}	1100 MPa	Class 12.9 Allowable	
Class 12.9 Min Yield Strength (ksi)	σ_{Bolt-Y}	160 ksi	Conversion to Imperial Units	
<i>Bending Stress in Bolt</i>				
Shaft Moment of Inertia	I_{Shaft}	0.001 in^4	$= (\pi / 64) * d_{Shaft}^4$	
Max Expected Load on Bearing	P_{Expect}	725 lbs	$= W * f_{Abuse}$	
Max Bending Moment in Shaft	M_{Max}	610 in-lbs	$= P_{Expect} * L_{Shaft} / 4$ Simply Support	
Bending Stress in Shaft	σ_{Bend}	102 ksi	$= M_{Max} * (d_{Shaft} / 2) / (I_{Shaft} * 1000)$	
Resulting Factor of Safety	FoS	1.57	$= \sigma_{Yield} / \sigma_{Bend}$	
<i>Shear and Bearing Stresses</i>				
10mm Bolt Shear Area	A_{Shear}	0.122 in^2	$= (\pi / 4) * d_{Shaft}^2$	
Shear Stress in Bolt	σ_{Shear}	5.96 ksi	$= P_{Expect} / (A_{Shear} * 1000)$	
Resulting Shear Safety Factor	X_{Shear}	26.8	$= \sigma_{Shear} / \sigma_{Bolt-Y}$	
Plate Bearing Area	$A_{Bearing}$	0.098 in^2	$= d_{Shaft} * t_{Plate}$	
Bearing Stress in Plate	$\sigma_{Bearing}$	7.37 ksi	$= P_{Expect} / (A_{Bearing} * 1000)$	
Max Bending Moment in Shaft	X_{Bearing}	7.33	$= \sigma_{Bearing} / \sigma_{Alum-B}$	

4. Vehicle Mechanical Analysis

Motor Bolts Strength Calculations



The torque required from the motor will be reacted by the bolts mounted to the motor plate. Assuming the torque is reacted equally to all bolts in the bolt pattern, the resultant load per bolt can be calculated. The shear stress in the bolt and the bearing stress in the plate were analyzed and compared to allowables.

Motor Bolts Strength Calculations				
Name	Var	Val	Unit	Comment / Equation
System Geometry and Allowable Strengths				
Motor Bolt Diameter	d_{Bolt}	6 mm		Bolts Used to Mount Motor
Bolt Pattern Radius	R_{Bolt}	28 mm		Center to Center Distance
Engaged Length of Bolt	L_{Bolt}	1.8 mm		Thickness After Countersink
Diameter of Motor Pulley	D_{Pulley}	43.4 mm		SDP-SI Timing Belt Pulley
DIN 965 Bolt Tensile Strength	σ_{Bolt-T}	500 MPa		Referenced Bolted Allowable
6061-T6 Bearing Strength (ksi)		54 ksi		Referenced in MMPDS
6061-T6 Bearing Strength (MPa)	σ_{Alum-B}	372 MPa		Conversion to Metric Units
Effective Forces on Motor Bolts				
Force Through Belt (lbs)		587 lbs		Weight of System and Patron
Force Through Belt (N)	F_{Req}	2612 N		Conversion to Metric Units
Expected Torque on Motor	T_{Motor}	56,695 N-mm		$= F_{Req} * (D_{Pulley} / 2)$
Radial Loads on Bolts	F_{Radial}	2025 N		$= T_{Motor} / R_{Bolt}$
Resulting Safety Factors for Bolts and Aluminum				
Shear Area on Single Bolt	A_{shear}	28.3 mm^2		$= (\pi / 4) * d_{Bolt}^2$
Shear Stress in Bolt	σ_{Shear}	17.9 MPa		$= (F_{Radial} / 4) / A_{shear}$
Resulting Shear Safety Factor	X_{Shear}	27.9		$= \sigma_{Bolt-T} / \sigma_{Shear}$
Bearing Area on Single Bolt	$A_{Bearing}$	10.6 mm^2		$= d_{Bolt} * L_{Bolt}$
Bearing Stress in Plate	$\sigma_{Bearing}$	47.9 MPa		$= (F_{Radial} / 4) / A_{Bearing}$
Resulting Bearing Safety Factor	$X_{Bearing}$	7.78		$= \sigma_{Alum-B} / \sigma_{Bearing}$

5. References

Vehicle Structural
Analysis

Vehicle Mechanical
Analysis

References

Appendix

5. References

Publications Used for Analysis

- [1] ASTM International F2291-17 “*Standard Practice for Design of Amusement Rides and Devices*” 2017.
- [2] D.O.T, “*Metallic Materials Properties Development and Standardization*”. January, 2003.
- [3] J. Randolph Kissell. “*Aluminum Structures: A Guide to Their Specifications and Design*” 2002.
- [4] John Wiley and Sons. “*The Measures of Man and Woman Revised Edition*”. Human Factors in Design. 2002.
- [5] Walter D. Pilkey, “*Peterson’s Stress Concentration Factors, Third Edition*” 2008.
- [6] Research Council on Structural Connections “*Specification for Structural Joints Using High-Strength Bolts*” 2014.
- [7] American Institute of Steel Construction 360-16 “*Specification for Structural Steel Buildings*” 2016.

6. Appendix

Specific References, COTS Cutsheets

6. Appendix: 6061-T6 Material Properties

Metallic Materials Properties Development and Standardization (2003)

Table 3.6.2.0(b ₂). Design Mechanical and Physical Properties of 6061 Aluminum Alloy Plate												
Specification	AMS 4026 and AMS-QQ-A-250/11			AMS QQ-A- 250/11			AMS 4025, AMS 4027 and AMS-QQ-A-250/11					
Form	Plate											
Temper	T451				T42 ^a				T651 and T62 ^b			
Thickness, in.	0.250-2.000		2.001-3.000		0.250- 1.000	1.001- 3.000	0.250-2.000		2.001-3.000	3.001- 4.000	4.001- 6.000 ^c	
Basis	A	B	A	B	S	S	A	B	A	B	S	S
Mechanical Properties:												
F_u , ksi:												
L												
LT	30	32	30	32	30	30	42	43	42	43	40	
F_y , ksi:												
L												
LT	16	18	16	18	14	14	36	38	35	37	35	
F_s , ksi:												
L												
LT	16	18	35	37	
F_w , ksi:												
...	20	21	27	28	
F_{by} , ksi:												
(e/D = 1.5)	48	52	67	69	
(e/D = 2.0)	63	67	88	90	
F_{by} , ksi:												
(e/D = 1.5)	22	25	50	53	
(e/D = 2.0)	26	29	58	61	
e , percent:												
L	d	...	16	...	18	16	d	...	6	...	6	
E , 10^3 ksi							9.9					
E_z , 10^3 ksi								10.1				
G , 10^3 ksi									3.8			
μ										0.33		
Physical Properties:												
ω , lb/in. ³	0.098											
C, K, and α	See Figure 3.6.2.0											

^a Design allowables were based upon data obtained from testing samples of material, supplied in the O temper, which were heat treated to demonstrate response to heat treatment by suppliers. Properties obtained by the user may be lower than those listed if the material has been formed or otherwise cold or hot worked, particularly in the annealed temper, prior to solution heat treatment.

^b Design allowables were based upon data obtained from testing T651 plate and from testing samples of plate, supplied in the O temper, which were heat treated to demonstrate response to heat treatment by suppliers. Properties obtained may be lower than those listed if the material has been formed or otherwise cold worked, particularly in the annealed temper, prior to solution heat treatment.

^c Properties for this thickness apply only to T651 temper.

^d See Table 3.6.2.0(b).

6061-T6 Plate

Tensile Ultimate Strength

Tensile Yield Strength

Shear Ultimate Strength

Bearing Yield Strength

Mechanical Properties

6. Appendix: 1025 Steel Material Properties

Metallic Materials Properties Development and Standardization (2003)

Table 2.2.1.0(b). Design Mechanical and Physical Properties of AISI 1025 Carbon Steel			
Specification	AMS 5046 and AMS-S-7952	AMS 5075, AMS 5077 and AMS-T-5066 ^a	ASTM A 108
Form	Sheet, strip, and plate	Tubing	Bar
Condition	Annealed	Normalized	All
Thickness, in.
Basis	S	S	S ^b
Mechanical Properties:			
F_u , ksi:			
L	55	55	55
LT	55	55	55
ST	55
F_y , ksi:			
L	36	36	36
LT	36	36	36
ST	36
F_{sy} , ksi:			
L	36	36	36
LT	36	36	36
ST	36
F_{su} , ksi	35	35	35
F_{bys} , ksi:			
(e/D = 1.5)
(e/D = 2.0)	90	90	90
F_{byy} , ksi:			
(e/D = 1.5)
(e/D = 2.0)
ϵ , percent:			
L	...	c	c
LT	c
E , 10^6 ksi	29.0		
E_c , 10^6 ksi	29.0		
G , 10^6 ksi	11.0		
μ	0.32		
Physical Properties:			
ω , lb/in. ²	0.284		
C, Btu/(lb)(°F)	0.116 (122 to 212°F)		
K, Btu/[(lb)(ft) ² (°F)/ft]	30.0 (at 32°F)		
a , 10^{-6} in./in./°F	See Figure 2.2.1.0		

^a Noncurrent specification.

^b Design values are applicable only to parts for which the indicated F_u has been substantiated by adequate quality control testing.

^c See applicable specification for variation in minimum elongation with ultimate strength.

Plain Carbon Steel

Tensile Ultimate Strength

Tensile Yield Strength

Shear Ultimate Strength

Mechanical Properties

6. Appendix: 6061-T6 Welded Allowables

Aluminum Structures: A Guide to Their Specifications and Design

Minimum Mechanical Properties of Aluminum Alloys (Welded) (U.S. Units)

Alloy	Temper	Product	Thickness Range		Tension		Compression F_c (ksi)	Shear F_s (ksi)
			from (in.)	to (in.)	F_u (ksi)	F_y (ksi)		
Alclad	1100	H12, H14	All		11	3.5	3.5	8
	3003	H12, H14, H16, H18	All		14	5	5	10
	3003	H12, H14, H16, H18	All		13	4.5	4.5	10
	3004	H32, H34, H36, H38	All		22	8.5	8.5	14
	3004	H32, H34, H36, H38	All		21	8	8	13
	3005	H25	Sheet		17	6.5	6.5	12
	5005	H12, H14, H32, H34	All		15	5	5	9
	5050	H32, H34	All		18	6	6	12
	5052	H32, H34, O	All		25	9.5	9.5	16
	5083	H111, O	Extrusions		39	16	15	23
5083	5083	H116, H321, O	Sheet and Plate	0.188	1,500	40	18	24
	5083	H116, H321, O	Plate	1.501	3,000	39	17	24
	5086	H111, O	Extrusions		35	14	13	21
	5086	H112, H32, H34, H116, O	Sheet and Plate		35	14	14	21
	5154	H38	Sheet		30	11	11	19
	5454	H111, O	Extrusions		31	12	11	19
	5454	H112	Extrusions		31	12	12	19
	5454	H32, H34, O	Sheet and Plate		31	12	12	19
	5456	H116, H321, O	Sheet and Plate	0.188	1,500	42	19	25
	5456	H116, H321, O	Plate	1.501	3,000	41	18	25
6005	6005	T5	Extrusions	0.250	24	13	13	15
	6061	T6, T651, T6510, T6511(2)	All		24	15	15	15
	6061	T6, T651, T6510, T6511(3)	All	0.375	24	11	11	15
	6063	T5, T52, T6	All		17	8	8	11
	6351	T5, T6(2)	Extrusions		24	15	15	15
	6351	T5, T6(3)	Extrusions	0.375	24	11	11	15
	6463	T6	Extrusions	0.125	0.500	17	8	11
7005	7005	T53	Extrusions	0.750	40	24	24	22

Notes

(1) Yield strengths are based on a 2 in. gauge length.

(2) Values when welded with 5183, 5356, or 5556 filler, regardless of thickness, and to thicknesses ≤ 0.375 in., when welded with 4043, 5554, or 5654 filler.

(3) Values when welded with 4043, 5554, or 5654 filler.

6. Appendix: Cutsheets

Bearings for Yaw Shaft and Wheels / Pulley Mechanisms

All Categories > Extra Thin Metric Series Bearings > Flanged Shielded Extra Thin Metric Ball Bearings > Item # F6910ZZ

Item # F6910ZZ, 1.9685 Inch (in) Bore Diameter (d) Flanged Shielded Extra Thin Metric Ball Bearing

[Request Information](#)

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All bearings are available in 52100 Chrome Steel or 440 Stainless Steel.
Bearings also available with single shield or seal : suffix Z, RS, RU.

[Specifications](#) | [Ball Complement](#)

Specifications

Bearing Type	Extra Thin Metric Bearing
Bore Diameter (d)	50 mm 1.9685 in
Outer Diameter (D)	72 mm 2.8346 in
Flange Diameter (D _f)	75.0 mm 2.9528 in
Min. Radius (r _s)	0.60 mm 0.0235 in
Width (B)	12.0 mm 0.4724 in
Flange Width (B _f)	2.5 mm 0.0984 in
Load Rating (Cr)	14540 N
Load Rating (Cor)	11710 N

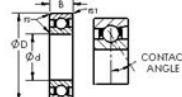
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1. 15 degree contact angle, relieved outer ring
2. Also available with metal shields (ZZ) or rubber seals (2RS)
3. The desired preload must be specified.

Product Details

Specifications			Documentation		
Bearing Type	15 deg contact angle		General	Nomenclature	Material
Bore Dia (d)	10.000	mm	Cages and Retainers	Tolerances and Precision	Lubrication
Outer Dia (D)	22.000	mm	Fitting and Mounting	Load and Life Calculation Information	
Width (B)	6.000	mm	eDrawings file (.ePRT, .eASM)		
Radius (min) (r _s)	0.30	mm			
Dynamic Load Rating (Cr)	2,900	N			
Static Load Rating (Cor)	1,800	N			
Max Speed (Grease)	70,000	rpm			
Max Speed (Oil)	110,000	rpm			

6. Appendix: Cutsheets

Bearings for Yaw Shaft Axial Loading

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Koyo.

Koyo NRB NTA-5266 \$36.99 each

Needle Roller Thrust Bearing - 3-1/4 in Bore, 4-1/8 in OD, 1/8 in Width IN STOCK

Mi Item #: 00094529 Quantity

★★★★★ 0 Reviews - Be the first to review this item.

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Please Note: Photo may not represent actual item, please refer to title and product specifications for all details.

Product Content Feedback

Specifications

Bore diameter:	3-1/4 in	Dynamic load capacity:	51.6 kN
Outside diameter:	4-1/8 in	Cage material:	Steel
Bearing width:	1/8 in	Maximum rpm:	4000 RPM
Thrust bearing type:	Roller & Cage Assembly	Compatible washer:	TRA-5266
Bearing material:	Steel	Series:	NTA
Static load capacity:	294.9 kN		

6. Appendix: Cutsheets

Timing Belt Pulley

L TIMING BELTS • 3/8" OR 9.525 mm PITCH

SDPSI

BELT WIDTHS
INCH - 1/2, 3/4 & 1 in.
METRIC - 12.5, 19 & 25.4 mm

MATERIAL:
Nylon Covered, Fiberglass Reinforced, Neoprene

SPECIFICATIONS:
Breaking Strength:
125 lbf per 1/8 in. (175 N per 1 mm) Belt Width; not representative of the load-carrying capacity of the belt.
Temperature Range:
-30°F to +185°F (-34°C to +85°C)

MODIFICATIONS:
Special Widths - cut to size from sleeves available from stock.

Pulleys are available with inch or metric standards.

INCH COMPONENT CATALOG NUMBER

A	6R	4	□□□□	□□□
No. of Grooves	Code			

Belt Width	Width
1/2	675
3/4	675
1	100

METRIC COMPONENT CATALOG NUMBER

A	6R	4M	□□□□	□□□
No. of Grooves	Code			

Belt Width	Width
12.5	15
19	190
25.4	254

2-86

PHONE: 516.328.3300 • FAX: 516.326.8827 • WWW.SDP-SI.COM

0 1 Inch

NOTE: Dimensions in () are mm.

Continued on the next page

L TIMING BELTS • 3/8" OR 9.525 mm PITCH

SDPSI

BELT WIDTHS
INCH - 1/2, 3/4 & 1 in.
METRIC - 12.5, 19 & 25.4 mm

MATERIAL:
Nylon Covered, Fiberglass Reinforced, Neoprene

SPECIFICATIONS:
Breaking Strength:
125 lbf per 1/8 in. (175 N per 1 mm) Belt Width; not representative of the load-carrying capacity of the belt.
Temperature Range:
-30°F to +185°F (-34°C to +85°C)

MODIFICATIONS:
Special Widths - cut to size from sleeves available from stock.

Pulleys are available with inch or metric standards.

INCH

2

Groove Code

Inch	mm
.026	657.23
.037	952.43
.033	814.33
.035	13.125
.036	13.500
.038	13.875
.040	15.000
.041	15.375
.042	15.750
.044	16.125
.045	16.875
.046	17.250
.047	17.625
.048	18.000
.052	19.500
.053	19.875
.054	20.250
.055	20.625
.056	21.000
.058	21.750
.060	22.500
.062	23.250
.063	23.625
.064	24.000
.065	24.375
.066	24.750
.067	25.125
.068	25.500

3

Groove Code

Inch	mm
.069	657.23
.072	77.000
.074	27.750
.076	28.500
.078	30.000
.081	30.375
.082	30.750
.084	31.500
.085	31.875
.089	33.250
.090	33.500
.092	34.000
.094	35.250
.095	35.500
.096	36.000
.098	36.750
.100	37.500
.104	39.000
.105	39.375
.112	42.000
.114	42.750
.116	43.500
.118	44.250
.119	44.625
.120	45.000
.123	46.125

4

5

0 1 Inch

NOTE: Dimensions in () are mm.

6. Appendix: Cutsheets

Pulley - Attached to Motor

GT® 2 / GT® 3 TIMING BELT PULLEYS • 5 mm PITCH



FOR 15 mm BELTS
FOR USE WITH GT®2 and GT®3 BELTS
DOUBLE FLANGE
TRUE METRIC PROFILE

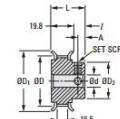


> MATERIAL:
Aluminum Alloy

> FINISH:
Clear Anodized

> SPECIFICATIONS:
D Tolerance: 12 to 16 grooves is +0.050
17 to 32 grooves is +0.030
34 grooves is +0.10/0

Pulleys with 12 and 13 grooves have 1 set screw; others have 2 set screws at 90°



METRIC COMPONENT

Catalog Number	No. of Grooves	P.D.	D Dia. ± 0.4	D ₁ Dia. ± 0.4	d Bore ± 0.025	L Length ± 0.4	D ₂ Hub Dia. ± 0.4	I Hub Proj. ± 0.4	A	Set Screw
A 6ASMM012DF1506	12	19.1	17.96	22.2	6	26.2	11.1	6.4	3.2	M3
A 6ASMM013DF1506	13	20.7	19.56	23.8	6	26.2	12.7	6.4	3.2	M3
A 6ASMM014DF1506	14	22.68	21.13	24.4	6	26.2	14.2	6.4	3.2	M3
A 6ASMM015DF1506	15	24.68	22.8	25.9	6	26.2	15.8	6.4	3.2	M3
A 6ASMM016DF1506	16	25.48	24.33	27.8	6	26.2	14.2	6.4	3.2	M3
A 6ASMM017DF1506	17	27.05	25.91	30.2	6	26.2	15.9	6.4	3.2	M3
A 6ASMM018DF1506	18	28.65	27.51	31.8	6	26.2	17.5	6.4	3.2	M3
A 6ASMM019DF1506	19	30.25	29.05	33.4	6	26.2	19.1	6.4	3.2	M3
A 6ASMM020DF1506	20	31.83	30.68	34.9	6	26.2	20.6	6.4	3.2	M3
A 6ASMM021DF1506	22	35.03	33.88	38.1	6	26.2	23.8	6.4	4.8	M5
A 6ASMM022DF1506	24	38.7	37.45	43.9	10	26.2	26.2	6.4	4.8	M5
A 6ASMM023DF1506	25	39.78	38.45	45.9	10	26.2	27.8	6.4	4.8	M5
A 6ASMM024DF1510	26	41.38	40.23	44.5	10	37.5	27	9.5	6.4	M6
A 6ASMM025DF1510	28	44.55	43.41	47.6	12	37.5	30.2	12.7	6.4	M6
A 6ASMM026DF1510	30	47.75	46.61	49.8	12	37.5	32.5	12.7	6.4	M6
A 6ASMM027DF1512	32	50.93	49.79	54	12	37.5	31.8	12.7	6.4	M6
A 6ASMM028DF1512	34	54.1	52.96	57.2	12	37.5	35	12.7	6.4	M6

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METRIC COMPONENT

Catalog Number	No. of Grooves	P.D.	D Dia. ± 0.4	D ₁ Dia. ± 0.4	d Bore ± 0.025	L Length ± 0.4	D ₂ Hub Dia. ± 0.4	I Hub Proj. ± 0.4	A	Set Screw
A 6A55M012DF1506	12	19.1	17.96	22.2	6	26.2	11.1	6.4	3.2	M3
A 6A55M013DF1506	13	20.7	19.56	23.8	6	26.2	12.7	6.4	3.2	M3
A 6A55M014DF1506	14	22.68	21.13	24.4	6	26.2	14.2	6.4	3.2	M3
A 6A55M015DF1506	15	24.68	22.8	25.9	6	26.2	15.8	6.4	3.2	M3
A 6A55M016DF1506	16	25.48	24.33	27.8	6	26.2	14.2	6.4	3.2	M3
A 6A55M017DF1506	17	27.05	25.91	30.2	6	26.2	15.9	6.4	3.2	M3
A 6A55M018DF1506	18	28.65	27.51	31.8	6	26.2	17.5	6.4	3.2	M3
A 6A55M019DF1506	19	30.25	29.11	33.4	6	26.2	19.1	6.4	3.2	M3
A 6A55M020DF1506	20	31.83	30.68	34.9	6	26.2	20.6	6.4	3.2	M3
A 6A55M022DF1506	22	35.03	33.88	38.1	6	26.2	23.8	6.4	4.8	M5
A 6A55M024DF1510	24	38.2	37.06	41.3	10	29.4	25.4	9.5	4.8	M5
A 6A55M025DF1510	25	39.78	38.63	42.9	10	29.4	25.4	9.5	4.8	M5
A 6A55M026DF1510	26	41.38	40.23	44.5	10	37.5	27	9.5	6.4	M6
A 6A55M028DF1512	28	44.55	43.41	47.6	12	32.5	30.2	12.7	6.4	M6
A 6A55M030DF1512	30	47.75	46.61	50.8	12	32.5	30.2	12.7	6.4	M6
A 6A55M032DF1512	32	50.93	49.79	54	12	32.5	31.8	12.7	6.4	M6
A 6A55M034DF1512	34	54.1	52.96	57.2	12	32.5	35	12.7	6.4	M6

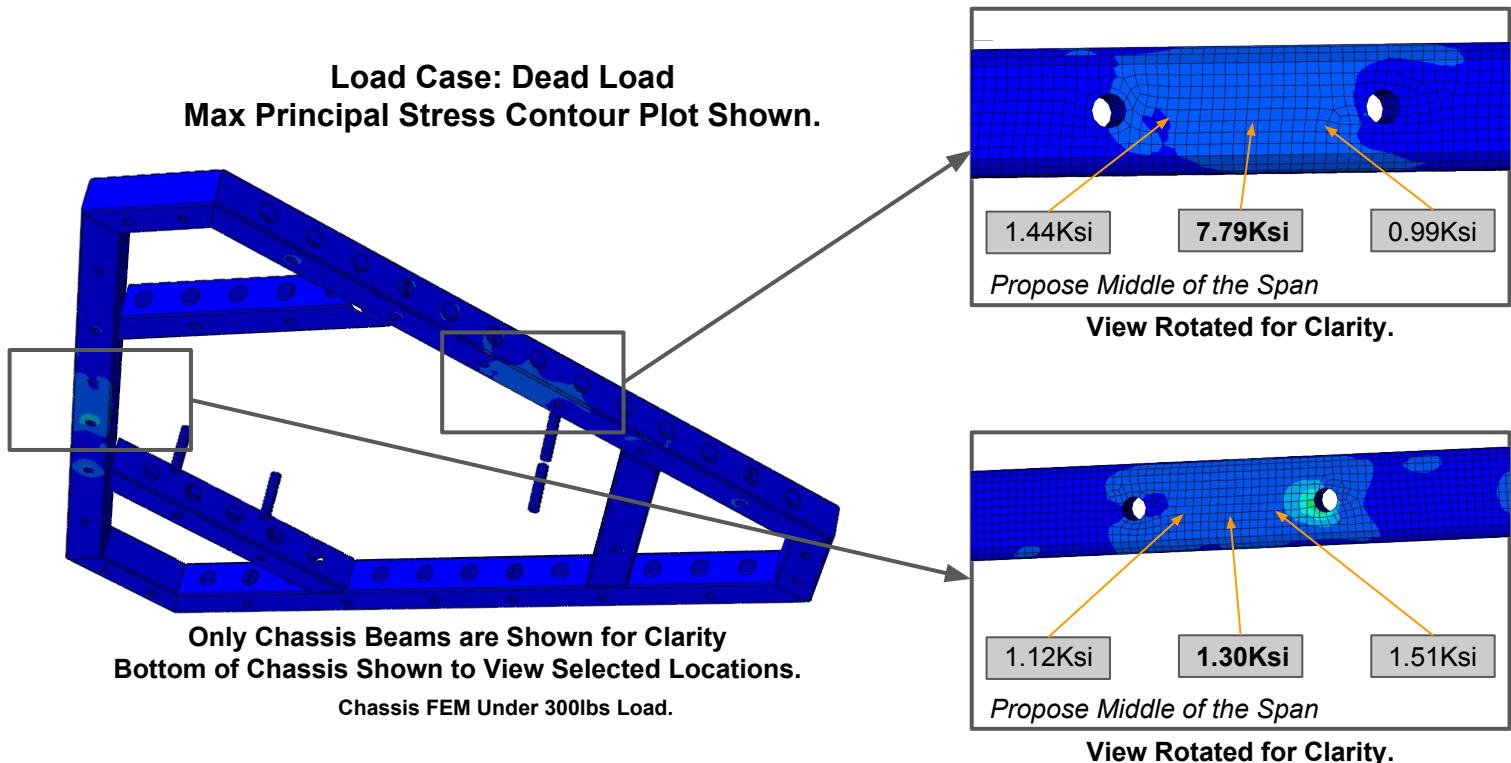


Figure 38. Strain Gauge Test.

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