



Swerve Robotic Platform

Structural and Mechanical Analysis

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Report Outline

1. *Vehicle Introduction*
2. *Analysis Overview*
3. *Vehicle Structural Analysis*
4. *Vehicle Mechanical Analysis*
5. *References*
6. *Appendix*



1. Vehicle Introduction

Vehicle Performance, Component Detail

Vehicle Introduction

Analysis Overview

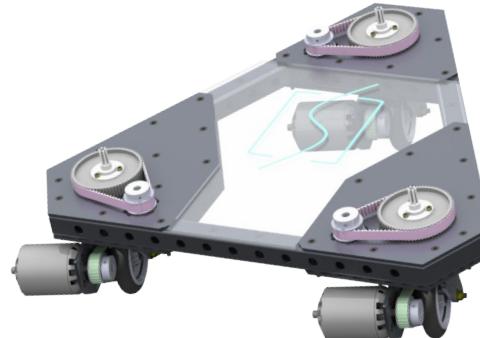
Vehicle Structural
Analysis

1. Vehicle Introduction

Performance Criteria

The vehicle is intended to accelerate and maneuver as quickly as possible. For design and analysis purposes, the acceleration rate was chosen to be 32.2 ft/s^2 (1g). Additionally, the vehicle is intended to carry a single passenger who stands on top of the vehicle in specifically marked locations. To accommodate different people, a large patron weight of 300lbs [1] was assumed for analysis purposes as a worst case. By leaning in a desired direction, the vehicle will accelerate in that direction, similar to a segway. Using pressure sensors, the vehicle accelerates at a rate that prevents the vehicle and leaning patron from tipping. Below is a rendered image of the proposed vehicle design.

The following is an structural and mechanical analysis package for the vehicle system. Using ABAQUS/CAE, a finite element model was created and analyzed per the specifications listed above. Additionally, supporting structural and mechanical calculations were completed to validate the proposed design.



1. Vehicle Introduction

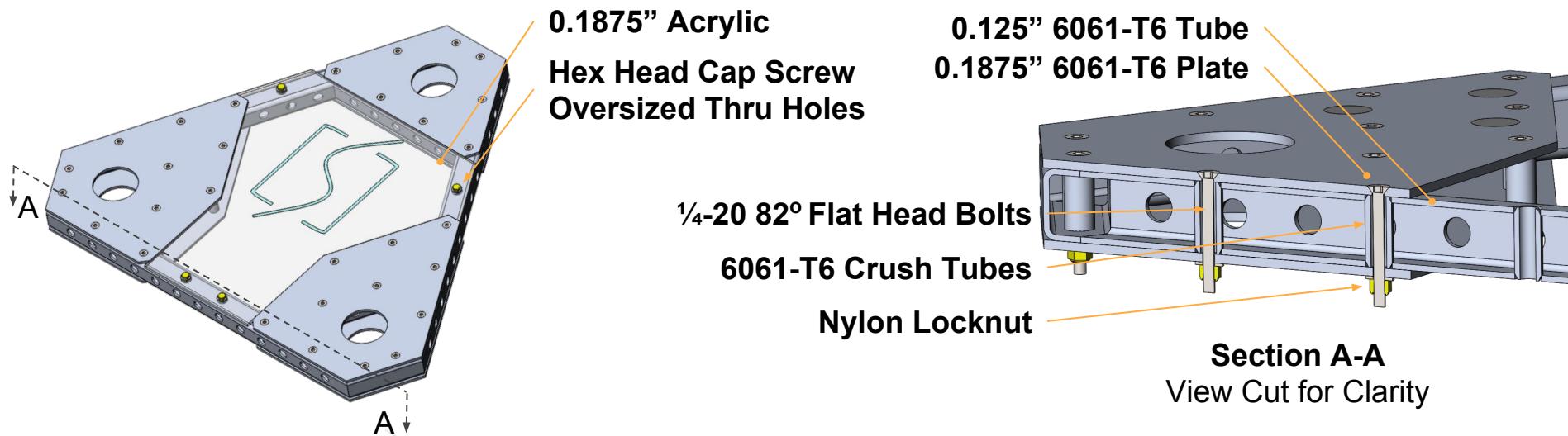
A Note About the Analysis

Per the university requirements, the timeline for this project was restricted to nine months, so the vehicle design and analysis were completed in parallel. As a result, some of the mechanical and structural components have changed since the formation of this report. However, the modifications that were made are expected to have little to no effect on the structural integrity of the system. Some changes that were made include the addition of small holes for mounting, modifications to hole size and location, etc. Over the course of the next few months, the team will return to this analysis to update accordingly, though the report will be used to validate the design for now.

1. Vehicle Introduction

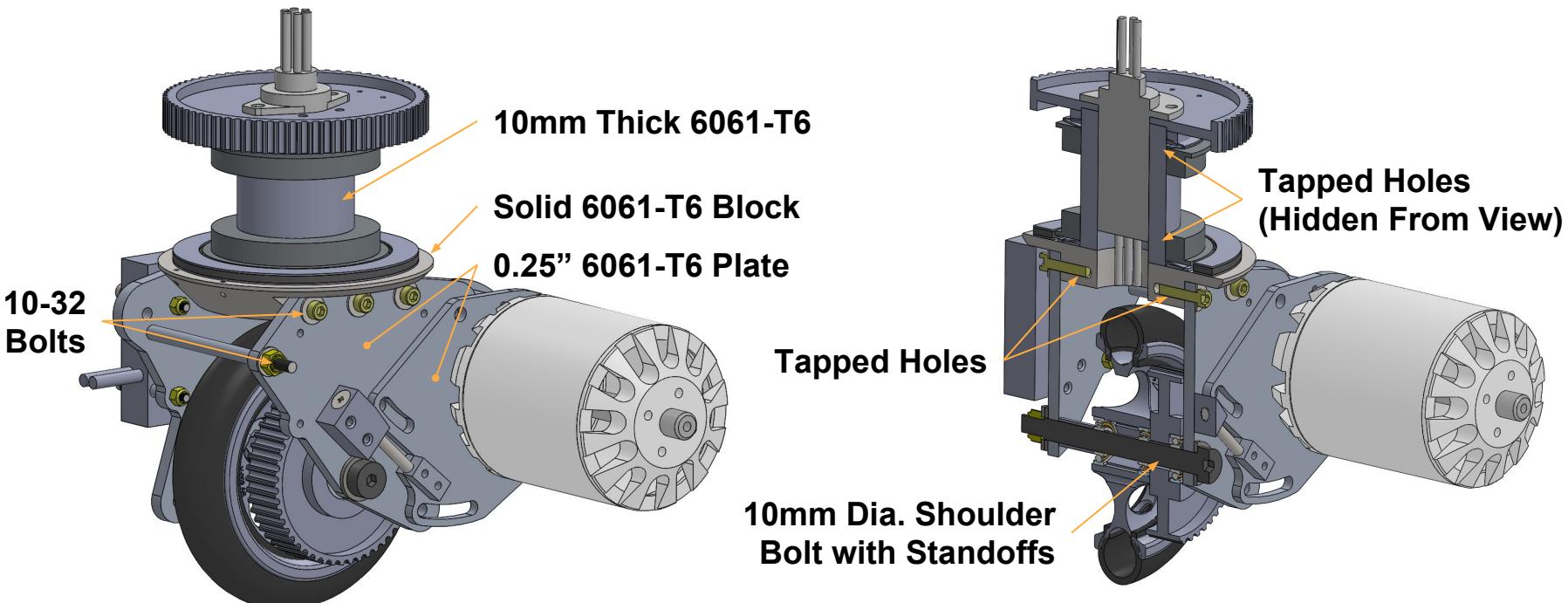
Chassis Mechanical / Structural Components

Below are the structural components of the chassis used for analysis. Due to the oversized holes in the acrylic, the acrylic is intended to be removed from the load path, and therefore it will not be used in the structural analysis.



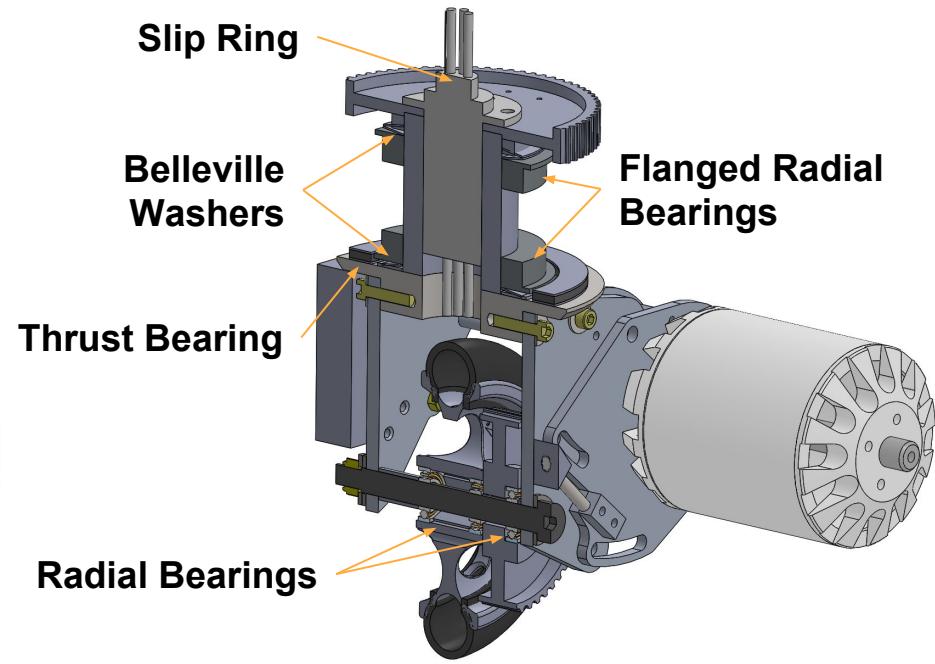
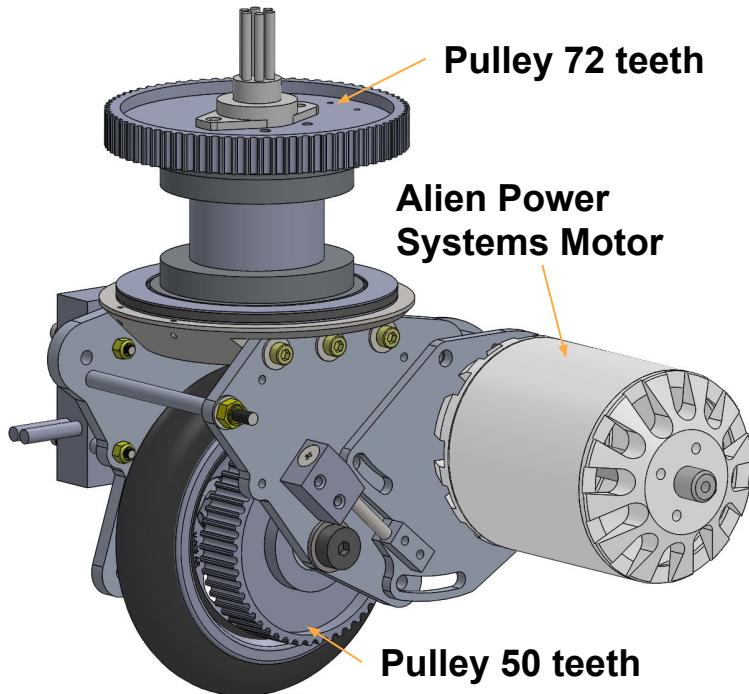
1. Vehicle Introduction

Wheel Assembly Structural Components



1. Vehicle Introduction

Wheel Assembly Mechanical Components



2. Analysis Overview

Assumptions, Success Criteria, Material Properties

Concept Design

Vehicle Introduction

Analysis Overview

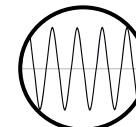
Vehicle Structural
Analysis

Vehicle Mechanical
Analysis

2. Analysis Overview

Analysis Assumptions and Considerations

Low-Cycle Life Expectancy - *Fatigue is Not Considered*



Conservative Safety Factors - *Compliant with Standards*



Consistent, Moderate Climate - *No Corrosion Considered*



This system is intended to be used for recreation, for short periods of time, and in dry as well as clean environments. Therefore, fatigue considerations and material corrosion are beyond the scope of these analyses. For analysis success, the mechanical and structural components are expected to pass conservative safety factors for strength load cases. A description of the loading criteria can be found on Page 13 of this report.

2. Analysis Overview

Material Properties and Allowables

Below are the material properties for the general materials used in the proceeding analysis. Additionally, the required safety factors for aluminum are listed as well. If a different material or safety factor is used for analysis, it will be noted specifically within that section of the report. The welded aluminum allowables are highlighted for clarification in addition to the aluminum safety factors used for the analyses. For simplicity, Building Type structures are static load dominated, while Bridge Type structures are dynamic load dominated.

| Material Name | Density [lb / in ³] | E -Modulus [psi] | Poisson | Yield σ [psi] | Ult. σ [psi] | Reference |
|----------------------|------------------------------------|---------------------|---------|------------------|-----------------|-----------|
| | - | - | - | - | - | |
| Aluminum 6061-T6 | 0.098 | 9.9E +06 | 0.33 | 35000 | 42000 | 2 |
| Structural Steel A36 | 0.284 | 2.9E +07 | 0.32 | 36000 | 55000 | 2 |
| Welded 6061-T6 | 0.098 | 9.9E +06 | 0.33 | 15000 | 24000 | 3 |

TABLE 6.1 Safety Margins in the Aluminum Specification [3]

| Type of Structure | Yield Strength | Ultimate Strength |
|-------------------|----------------|-------------------|
| Building Type | 1.65 | 1.95 |
| Bridge Type | 1.85 | 2.20 |

2. Analysis Overview

Component Material Information

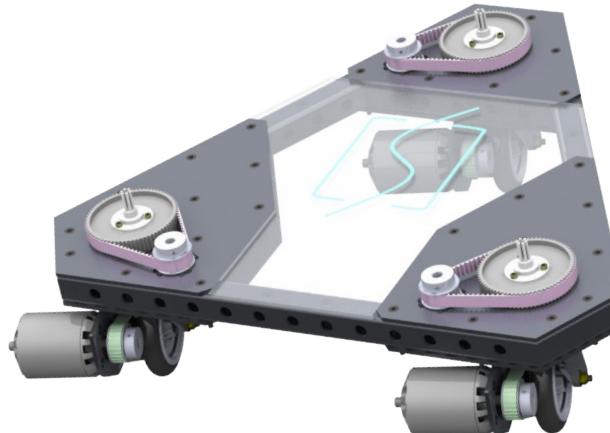
Chassis Components

| Part | Material |
|------------------|----------|
| Structural Beams | 6061-T6 |
| Gusset Plates | 6061-T6 |
| Crush Tubes | 6061-T6 |

Wheel Assembly Components

| Part | Material |
|--------------------|----------|
| Rotating Yaw Shaft | 6061-T6 |
| Connecting Block | 6061-T6 |
| Side Plates | 6061-T6 |

To reduce the weight of the system, aluminum 6061-T6 was used for many of the structural and mechanical components. Unless otherwise specified, it was assumed that bulk material was manufactured from aluminum 6061-T6 and all bolts were made from A36 steel.



2. Analysis Overview

Load Cases and Analysis Methodology

Structural Analysis Methodology

The structural components were analyzed for full-load, full performance operation. During operation, the patron will lean in a desired direction at a specific angle. This places the patron Center of Gravity (CG) away from the vehicle, and a calculated acceleration is required to avoid tipping. A lumped point mass of 300lbs was placed in the finite element model at the specified location to represent the patron CG. The contact locations of the wheels were constrained to only allow rotation (translations fixed) and global accelerations were applied to the model to represent the accelerations of the vehicle. Important factors and values are listed below:

- A Dynamic Factor was not added to loads since it is included in the required safety factor
- A 1.2 Impact Factor was applied to all accelerations per Reference 1 (ASTM F2291-17).
- The Patron CG is located 40.7in on top of the gusset plates per Reference 4.

Mechanical Analysis Methodology

The mechanical components were analyzed for full-load, full-performance operation as well as system abuse and impact while patrons are getting on and off the system. The component calculations were completed assuming all of the system and patron weight are applied to only one wheel assembly. This type of loading is unlikely and will therefore be considered conservative. All of the loads are derived assuming the system will accelerate and perform at the proposed 1g rate. Important factors are listed below:

- A 2.0 Impact Factor was used in many cases for system abuse



2. Analysis Overview

Patron Center of Gravity Information

Table for Estimated Percentiles

| Percentile | Factor | Equation |
|------------|--------|---|
| 99.9 | 3.000 | $99.9 = \text{Mean} + (3 \times \text{SD})$ |
| 99.5 | 2.576 | $99.5 = \text{Mean} + (2.576 \times \text{SD})$ |
| 99 | 2.326 | $99.0 = \text{Mean} + (2.326 \times \text{SD})$ |
| 97.5 | 1.950 | $97.5 = \text{Mean} + (1.95 \times \text{SD})$ |
| 97 | 1.880 | $97.0 = \text{Mean} + (1.88 \times \text{SD})$ |
| 95 | 1.650 | $95.0 = \text{Mean} + (1.65 \times \text{SD})$ |
| 90 | 1.280 | $90.0 = \text{Mean} + (1.28 \times \text{SD})$ |
| 85 | 1.040 | $85.0 = \text{Mean} + (1.04 \times \text{SD})$ |
| 80 | 0.840 | $80.0 = \text{Mean} + (0.84 \times \text{SD})$ |
| 75 | 0.670 | $75.0 = \text{Mean} + (0.67 \times \text{SD})$ |
| 50 | 0.000 | $50.0 = \text{Mean} + (0 \times \text{SD})$ |
| 25 | -0.670 | $25.0 = \text{Mean} + (-0.67 \times \text{SD})$ |
| 20 | -0.840 | $20.0 = \text{Mean} + (-0.84 \times \text{SD})$ |
| 15 | -1.040 | $15.0 = \text{Mean} + (-1.04 \times \text{SD})$ |
| 10 | -1.280 | $10.0 = \text{Mean} + (-1.28 \times \text{SD})$ |
| 5 | -1.650 | $5.0 = \text{Mean} + (-1.65 \times \text{SD})$ |
| 3 | -1.880 | $3.0 = \text{Mean} + (-1.88 \times \text{SD})$ |
| 2.5 | -1.950 | $2.5 = \text{Mean} + (-1.95 \times \text{SD})$ |
| 1 | -2.326 | $1.0 = \text{Mean} + (-2.326 \times \text{SD})$ |
| 0.5 | -2.576 | $0.5 = \text{Mean} + (-2.576 \times \text{SD})$ |
| 0.1 | -3.000 | $0.1 = \text{Mean} + (-3 \times \text{SD})$ |

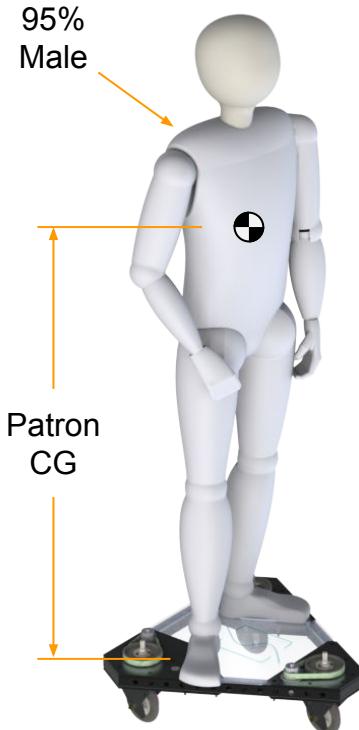
SD = Standard Deviation

Table Taken from *The Measure of Man & Woman*, John Wiley & Sons (C) 2002

Vertical CG Location (From Feet)

| Percentile | Measurement |
|---------------|-----------------|
| Mean Data: | 50 37.9 in |
| 2nd Data: | 99 41.8 in |
| Standard Dev: | SD 1.68 in |
| Interpolated: | 95 40.7 in |

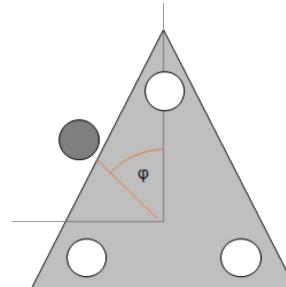
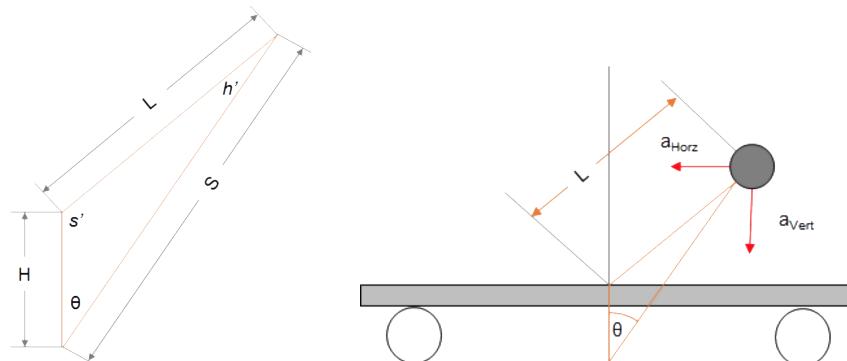
A 95 percentile male (73.7in tall) was the design patron height per Reference 1. This large patron height coupled with the large patron weight (300lbs) is conservative as the system would not accommodate riders larger than this.



2. Analysis Overview

Patron CG Positioning Calculation for Finite Element Model

All straight-line and perpendicular load cases are derived using the table to the right. These load cases are acceleration driven and the Patron CG location can be derived.



Determine CG Location due to Applied Accelerations

| Name | Var | Value | Unit | Comment / Equation |
|----------------------------|-------------------|---------|------|--------------------------------|
| User Input | | | | |
| Gravitational Acceleration | g | 1 g | | Given |
| Vertical Acceleration | a _{Vert} | 1.2 g | | Vertical Loading on System |
| Horizontal Acceleration | a _{Horz} | 1.2 g | | Horizontal Loading on System |
| CG Height of Patron | L | 40.7 in | | Height From Chassis Platen |
| Platen Height off Floor | H | 7.86 in | | Height From Floor to Platen |
| Direction Off Straight | φ' | 30 deg | | Direction From Straight Travel |

Geometry Calculations - Law of Sines

| | | | |
|-----------------------------|----|-----------|---|
| Direction Vector Angle | φ | 0.5 rad | = (π/180) * φ' |
| Acceleration Vector Angle | θ | 0.785 rad | = ATAN(a _{Horz} / a _{Vert}) |
| Angle: Patron / Line of Act | h' | 0.137 rad | = ASIN[(H/L) * SIN(θ)] |
| Angle: Internal Patron Lean | s' | 2.2 rad | = π - θ - h' |
| CG to Floor - Dist Vector | S | 45.9 in | = L * [SIN(s') / SIN(θ)] |

Resulting Acceleration Components and Patron CG Location

| | | | |
|------------------------|--------------------|----------|---|
| Accel Comp-LAT | a _{lat} | -0.600 g | = a _{Horz} * SIN(φ) |
| Accel Comp-FWD | a _{fwd} | -1.039 g | = a _{Horz} * COS(φ) |
| Accel Comp-VERT | a _{vert} | -1.200 g | = a _{Vert} |
| CG Lateral Location | CG _{lat} | 16.22 in | = S * SIN(θ) * SIN(φ) |
| CG Forward Location | CG _{fwd} | 28.09 in | = S * SIN(θ) * COS(φ) |
| CG Vertical Location | CG _{vert} | 24.58 in | = S * COS(θ) - h |
| Calc. Patron CG Height | L _{calc} | 40.7 in | = (CG _{fwd} ² + CG _{lat} ² + CG _{vert} ²) ^(1/2) |

Calculated Patron CG Height is Consistent with Input Data

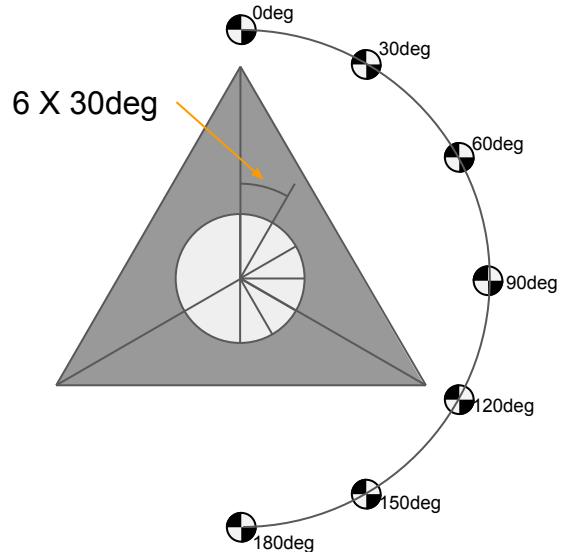
2. Analysis Overview

Load Cases for the Finite Element Model

| | Accel-X: | 0.00 g | CG-X: | 0.0 in |
|--------|----------|---------|-------|----------|
| | Accel-Y: | 0.00 g | CG-Y: | 0.0 in |
| | Accel-Z: | -1.20 g | CG-Z: | 40.7 in |
| Dead | | | | |
| 0deg | Accel-X: | -1.20 g | CG-X: | 32.4 in |
| 0deg | Accel-Y: | 0.00 g | CG-Y: | 0.0 in |
| 0deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 30deg | Accel-X: | -1.04 g | CG-X: | 28.1 in |
| 30deg | Accel-Y: | -0.60 g | CG-Y: | 16.2 in |
| 30deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 60deg | Accel-X: | -0.60 g | CG-X: | 16.2 in |
| 60deg | Accel-Y: | -1.04 g | CG-Y: | 28.1 in |
| 60deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 90deg | Accel-X: | 0.00 g | CG-X: | 0.0 in |
| 90deg | Accel-Y: | -1.20 g | CG-Y: | 32.4 in |
| 90deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 120deg | Accel-X: | 0.60 g | CG-X: | -16.2 in |
| 120deg | Accel-Y: | -1.04 g | CG-Y: | 28.1 in |
| 120deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 150deg | Accel-X: | 1.04 g | CG-X: | -28.1 in |
| 150deg | Accel-Y: | -0.60 g | CG-Y: | 16.2 in |
| 150deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| 180deg | Accel-X: | 1.20 g | CG-X: | -32.4 in |
| 180deg | Accel-Y: | 0.00 g | CG-Y: | 0.0 in |
| 180deg | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |
| Perp. | Accel-X: | 0.00 g | CG-X: | 0.0 in |
| Perp. | Accel-Y: | -1.20 g | CG-Y: | 32.4 in |
| Perp. | Accel-Z: | -1.20 g | CG-Z: | 24.6 in |

To simulate 1g acceleration in any direction, the patron CG and acceleration vectors were manipulated for load cases at 30deg increments from 0deg to 180deg. Since the structure is symmetric about the X-Z plane, only the first 180deg need to be analyzed. Nine load cases were analyzed using ABAQUS/CAE including 7 straight line acceleration load cases (0deg - 180deg) as well as one perpendicular load case where the wheels are oriented 90deg from the direction of travel. This case is to simulate high speed cornering at 1g.

The table to the left shows the cartesian vectors for the acceleration as well as the coordinates for the patron CG location per each load case. On the right is a visual representation of the patron CG location for each load case.



2. Analysis Overview

Welded Aluminum Specification and Discussion

"The damage is summarized in Aluminum Specification Table 3.3-2, Minimum Mechanical Properties for Welded Aluminum Alloys (included here as Appendix C and discussed in Section 4.5) ... The values in Table 3.3-2 for ultimate tensile strengths (F_{tuw}) must be multiplied by 0.9 before they are used for structural design. This is to account for the fact that welds may get only visual inspection and might not reliably attain the strengths in Table 3.3-2 due to undetected defects. This 0.9 factor is not applied to minimum properties other than ultimate tensile strength; here, as elsewhere in the Specification, the margin of safety against tensile fracture is the greatest concern." [3]

Although the text above recommends that a knockdown factor of 0.9 is to be used on the allowable stresses for welded aluminum, the proposed system is not intended for use at high cycles. Since inspection is not a concern, the 0.9 knockdown factor will be omitted, though the ultimate strength criteria for bridge type structures (as defined on Slide 10) will be used for the welded analysis.

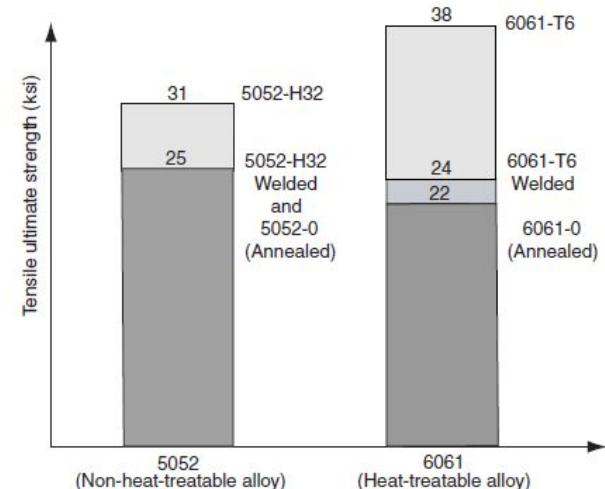


Figure 9.1 Effect of welding on tensile ultimate strength of alloys 5052 and 6061.

Ultimate Strength of Welded 6061-T6 (Defined in Graph) = **24.0ksi**
Required Ultimate Strength Factor of Safety (Bridge Type) = **2.20**
Corresponding Allowable Stress in Weld = $24.0\text{ksi} / 2.20 = 10.9\text{ksi}$

3. Vehicle Structural Analysis

Finite Element Model and Supporting Calculations

Vehicle Introduction

Analysis Overview

**Vehicle Structural
Analysis**

**Vehicle Mechanical
Analysis**

References

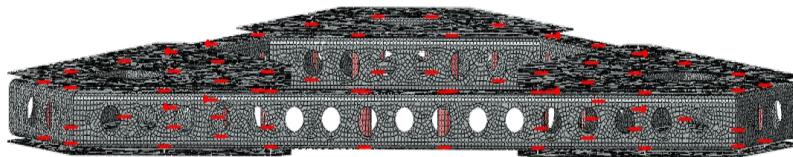


3. Vehicle Structural Analysis - Finite Element Model

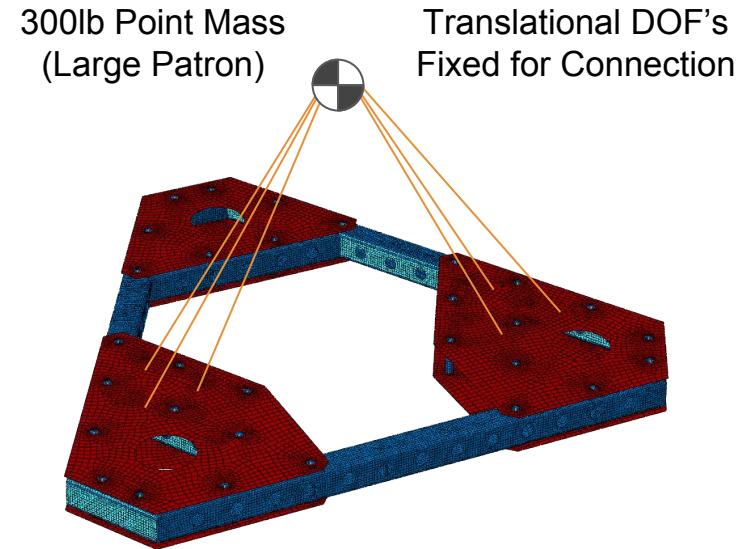
Finite Element Model of the Chassis

FEM Creation and Element Formation

- Gusset plates modeled with 2D, linear shell elements that are 0.25 in. big
- Beams and tubes modeled with 2D, linear shell elements that are 0.125 in. big
- bolts are modeled with 1D beam elements



The elements representing the crush tubes were stitched to the elements representing the beams. This is to model the welded connection by allowing direct transfer of load.



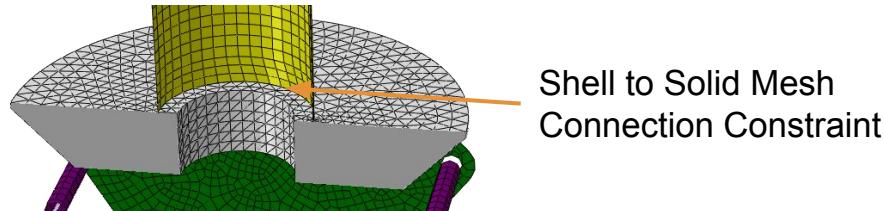
 6061-T6 : 0.188 in. Thick
 6061-T6 : 0.125 in. Thick

3. Vehicle Structural Analysis - Finite Element Model

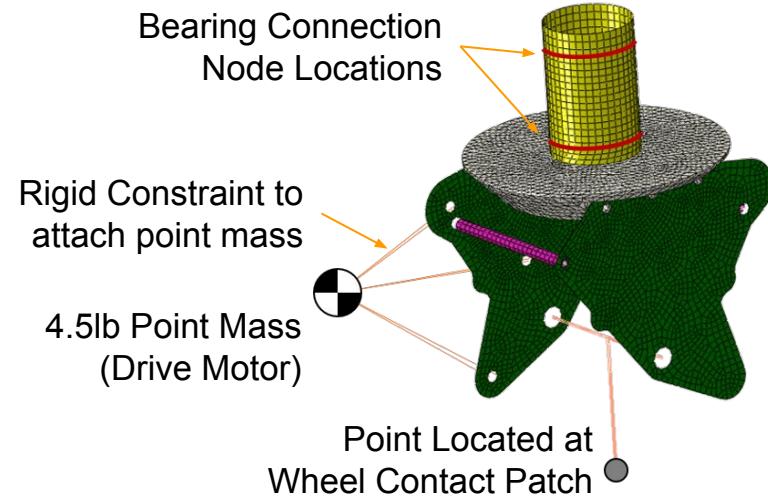
Finite Element Model of the Wheel Assembly

FEM Creation and Element Formation

- Side plates and shaft modeled with 2D, linear shell elements that are 0.125 in. big
- Connecting Plate modeled with 3D, linear tetrahedral elements that are 0.125 in. big
- bolts are modeled with 1D beam elements



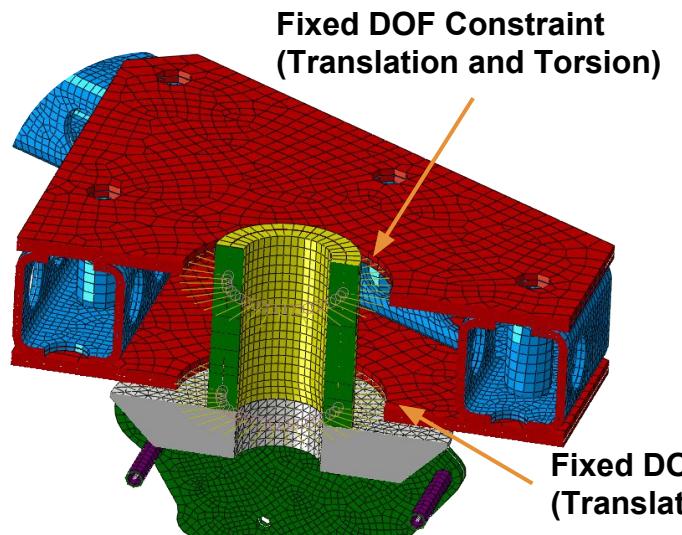
Instead of bolted connections, the nodes at the shaft and plate interface are merged to limit model size. Stresses in shaft connection are expected to be low.



3. Vehicle Structural Analysis - Finite Element Model

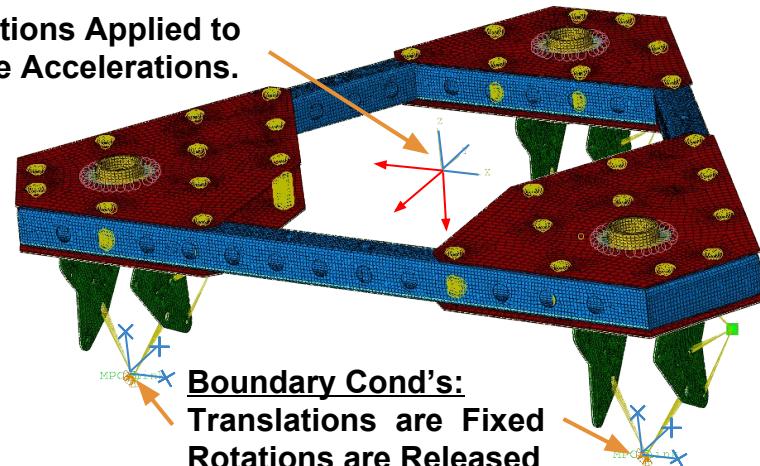
Finite Element Model of the Vehicle Assembly

The finite element assembly is shown on the right as well as the model loads and boundary conditions. Below is a detailed view of the part-to-part constraint that is consistent for all wheel assemblies.



Assembly Bearing Connections
Shell Thickness Rendered for Clarity

LOADS:
Global Accelerations Applied to Simulate Vehicle Accelerations.

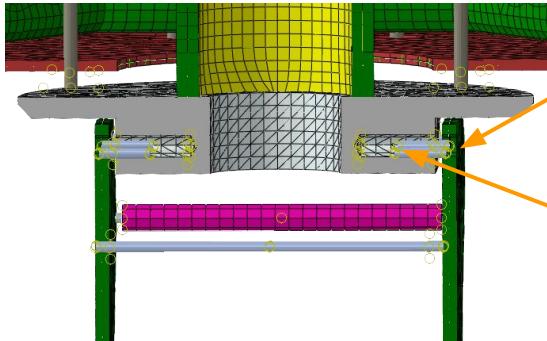


Total FEM Weight = 355.6 lbs

- Chassis Model 18.7 lbs
- Swerve Model (3) 12.3 lbs
- Large Patron 300 lbs

3. Vehicle Structural Analysis - Finite Element Model

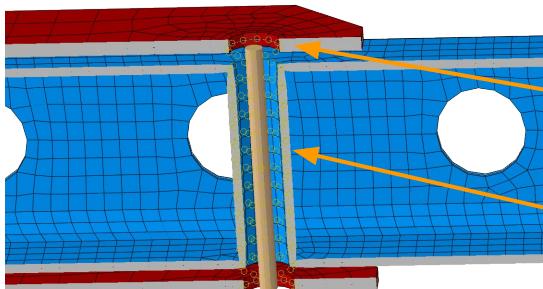
Modeling Bolted Connections



Bolted Connections in Wheel Assembly

End Nodes Connected
to Plate Shell Nodes

End Nodes Connected
to Solid Hole Nodes



Bolted Connections in Chassis

End Nodes Connected
to Plate Shell Nodes

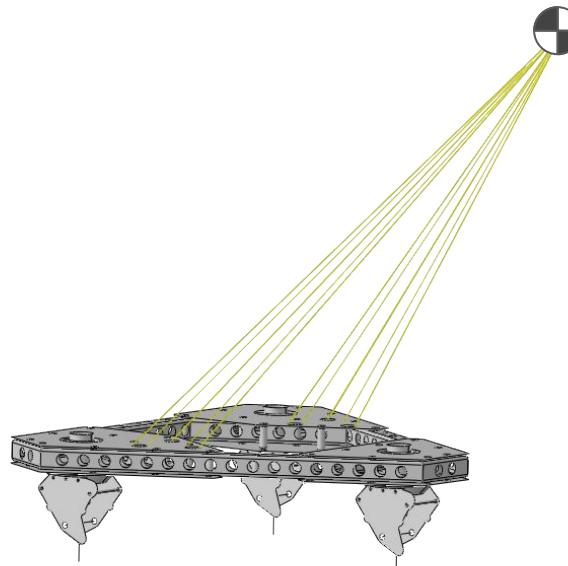
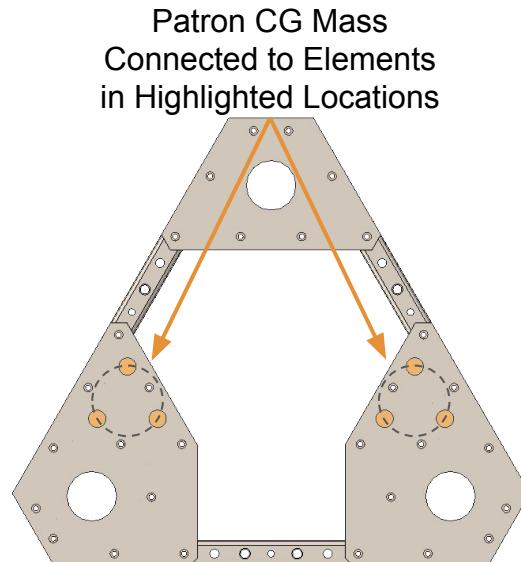
Mid Nodes Connected
to Tube Shell Nodes

For bolted connections, 1D beam elements were used with a simulation diameter twice the diameter of the proposed bolt. This is to ensure the model is adequately stiff and large deflections are avoided. The methodology used to the left is consistent for all bolted connections throughout this analysis. To account for preloaded bolts, rigid (fixed) elements were used to connect the beam nodes to the surface and solid nodes. This allows the transfer of both forces and moments.

3. Vehicle Structural Analysis - Finite Element Model

Modeling Patron Connections

To constrain the patron to the chassis, it was assumed that the feet would apply loads to the model in a distributed circle described on the below. Three smaller circles were created on the model to represent these force locations. The CG was then constrained using a Multi Point, Link constraint, the translation of the point mass was held constant while the CG was free to rotate, simulating the pitch/roll of the patron ankle.



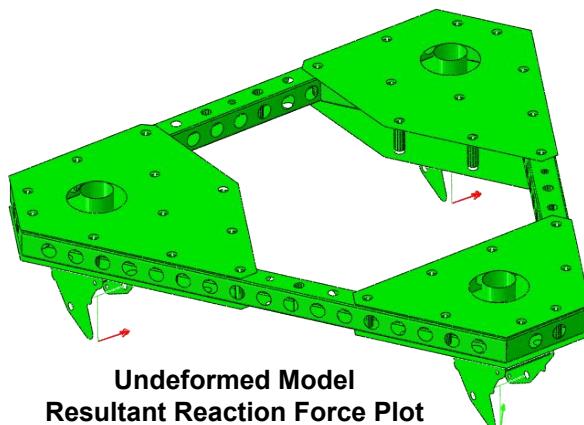
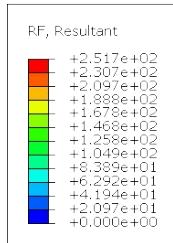
3. Vehicle Structural Analysis - Finite Element Model

Model Check: Simulation Reaction Forces

Reaction Forces

- Reactions Equal (*Model Mass * Accelerations*)
- Verify Loads, Masses, and Boundary Conditions

Load Case: 0deg



Units above are lbs

Undeformed Model
Resultant Reaction Force Plot

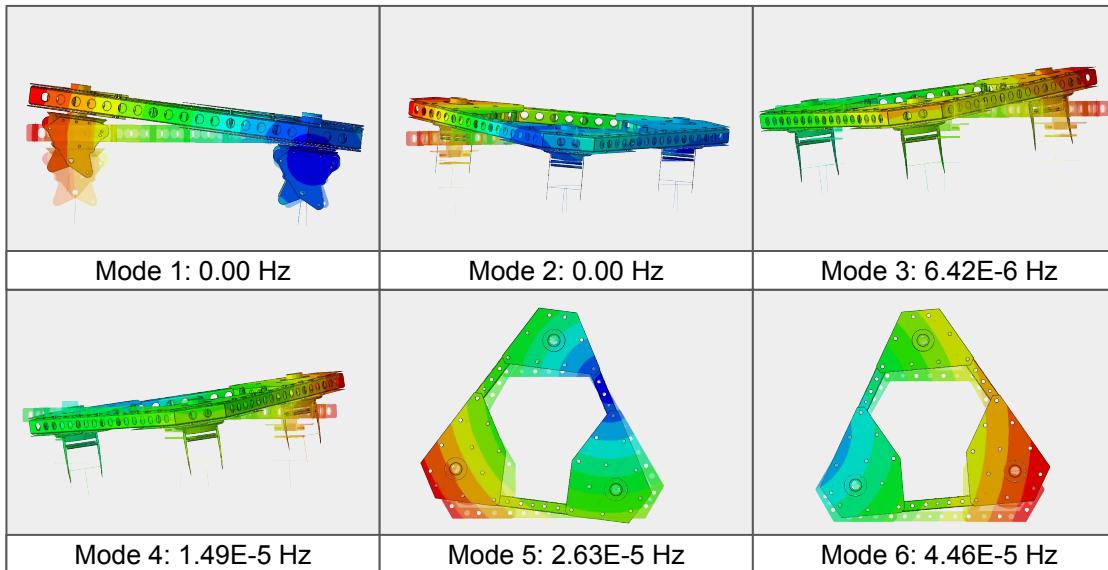
| Mass Information | | MODEL REACTION FORCES AS COMPARED TO THE EXPECTED REACTION FORCES | | | |
|-----------------------|-----------|---|---------------------|-----------------------|---------------------|
| Chassis Material | 18.73 lbs | Output from Simulation | Force-X | 0.0 lbs | Percent Error: 0.0% |
| Patron (95th%) | 300.0 lbs | Output from Simulation | Force-Y | 0.0 lbs | Percent Error: 0.0% |
| Swerve System | 38.84 lbs | Output from Simulation | Force-Z | -426.7 lbs | Percent Error: 0.0% |
| Total Mass | 355.6 lbs | Mass Summation | | | |
| Applied Accelerations | | Expected Forces | Simulation Forces | Modeling Error | |
| Dead Load | | Force-X: 0.0 lbs | Force-X: 0.0 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | 0.000 g | Force-Y: 0.0 lbs | Force-Y: 0.0 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 0.000 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| Wleg | | Force-X: -426.7 lbs | Force-X: 0.0 lbs | Percent Error: 100.0% | Percent Error: 0.0% |
| Accel-X | -1.200 g | Force-Y: 0.0 lbs | Force-Y: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 0.000 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 30deg | | Force-X: -213.3 lbs | Force-X: -213.4 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | -0.600 g | Force-Y: -389.5 lbs | Force-Y: -389.5 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | -1.039 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 60deg | | Force-X: -389.5 lbs | Force-X: -389.5 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | -1.039 g | Force-Y: -213.3 lbs | Force-Y: -213.4 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | -0.600 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 90deg | | Force-X: -426.7 lbs | Force-X: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | -1.200 g | Force-Y: 0.0 lbs | Force-Y: 0.0 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 0.000 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 120deg | | Force-X: -389.5 lbs | Force-X: -389.5 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | -1.039 g | Force-Y: 213.3 lbs | Force-Y: 213.4 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 0.600 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 150deg | | Force-X: -213.3 lbs | Force-X: -213.4 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | -0.600 g | Force-Y: 389.5 lbs | Force-Y: 389.5 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 1.039 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |
| 180deg | | Force-X: 0.0 lbs | Force-X: 0.0 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-X | 0.000 g | Force-Y: 426.7 lbs | Force-Y: 426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Y | 1.200 g | Force-Z: -426.7 lbs | Force-Z: -426.7 lbs | Percent Error: 0.0% | Percent Error: 0.0% |
| Accel-Z | -1.200 g | | | | |

3. Vehicle Structural Analysis - Finite Element Model

Model Check: Free-Free Modes Analysis

Free-Free Modes

- Rigid body modes at least five orders below first flexural body mode
- Verify model is accurately constrained and all parts are connected



Below is a list of the first ten modes output by the Free-Free Modes Simulation. Note that the first six modes are the rigid body modes, while the modes following are flexural body modes. This is consistent with the rule listed above.

| Frame | Index | Description |
|-------|-------|--|
| 0 | 0 | Increment 0: Base State |
| 1 | 1 | Mode 1: Value = -3.33695E-08 Freq = 0.0000 (cycles/time) |
| 2 | 2 | Mode 2: Value = -1.62283E-08 Freq = 0.0000 (cycles/time) |
| 3 | 3 | Mode 3: Value = 1.62733E-09 Freq = 6.42034E-06 (cycles/time) |
| 4 | 4 | Mode 4: Value = 8.76245E-09 Freq = 1.48982E-05 (cycles/time) |
| 5 | 5 | Mode 5: Value = 2.73584E-08 Freq = 2.63248E-05 (cycles/time) |
| 6 | 6 | Mode 6: Value = 7.86217E-08 Freq = 4.46264E-05 (cycles/time) |
| 7 | 7 | Mode 7: Value = 657.16 Freq = 4.0800 (cycles/time) |
| 8 | 8 | Mode 8: Value = 837.53 Freq = 4.6060 (cycles/time) |
| 9 | 9 | Mode 9: Value = 1193.8 Freq = 5.4991 (cycles/time) |
| 10 | 10 | Mode 10: Value = 1858.1 Freq = 6.8604 (cycles/time) |

3. Vehicle Structural Analysis

Safety Factor Summary by Load Case

| Load Case | Assem. Criteria | Allow σ [ksi] | Expect σ [ksi] | Expect SF | Required SF |
|---------------|------------------|---------------|----------------|-----------|-------------|
| 0deg | Chassis Assembly | 35.0 | 14.28 | 2.45 | 1.85 |
| | Chassis Welded | 24.0 | 7.14 | 3.36 | 2.20 |
| | Wheel Assemblies | 35.0 | 6.32 | 5.54 | 1.85 |
| 30deg | Chassis Assembly | 35.0 | 14.75 | 2.37 | 1.85 |
| | Chassis Welded | 24.0 | 7.81 | 3.07 | 2.20 |
| | Wheel Assemblies | 35.0 | 8.77 | 3.99 | 1.85 |
| 60deg | Chassis Assembly | 35.0 | 8.67 | 4.04 | 1.85 |
| | Chassis Welded | 24.0 | 8.63 | 2.78 | 2.20 |
| | Wheel Assemblies | 35.0 | 5.66 | 6.18 | 1.85 |
| 90deg | Chassis Assembly | 35.0 | 6.80 | 5.15 | 1.85 |
| | Chassis Welded | 24.0 | 7.78 | 3.08 | 2.20 |
| | Wheel Assemblies | 35.0 | 8.31 | 4.21 | 1.85 |
| 120deg | Chassis Assembly | 35.0 | 10.68 | 3.28 | 1.85 |
| | Chassis Welded | 24.0 | 5.43 | 4.42 | 2.20 |
| | Wheel Assemblies | 35.0 | 6.70 | 5.22 | 1.85 |
| 150deg | Chassis Assembly | 35.0 | 12.49 | 2.80 | 1.85 |
| | Chassis Welded | 24.0 | 4.26 | 5.64 | 2.20 |
| | Wheel Assemblies | 35.0 | 6.35 | 5.51 | 1.85 |
| 180deg | Chassis Assembly | 35.0 | 10.82 | 3.24 | 1.85 |
| | Chassis Welded | 24.0 | 3.61 | 6.66 | 2.20 |
| | Wheel Assemblies | 35.0 | 4.82 | 7.26 | 1.85 |
| Perpendicular | Chassis Assembly | 35.0 | 7.13 | 4.91 | 1.85 |
| | Chassis Welded | 24.0 | 8.53 | 2.81 | 2.20 |
| | Wheel Assemblies | 35.0 | 8.61 | 4.07 | 1.85 |

The expected stresses and resulting safety factors for the structural components are listed to the left. All analyzed components meet the required strength. The load cases with the smallest margin for each part is highlighted in green and corresponding stress contours are displayed on the following slides. For convenience, the minimum required safety factors for aluminum are listed below.

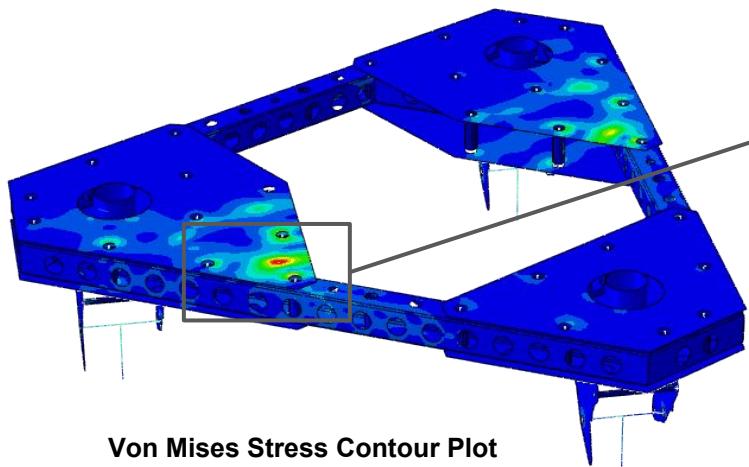
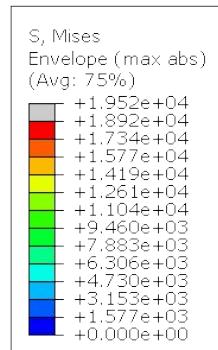
TABLE 6.1 Safety Margins in the Aluminum Specification [3]

| Type of Structure | Yield Strength | Ultimate Strength |
|-------------------|----------------|-------------------|
| Building Type | 1.65 | 1.95 |
| Bridge Type | 1.85 | 2.20 |

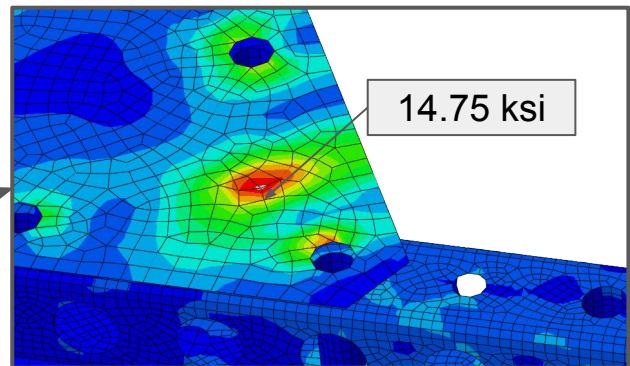
3. Vehicle Structural Analysis - Finite Element Model

Expected Von Mises Stresses are Acceptable in Chassis Gusset Plates

Load Case: 30deg



Units above are in psi
 $35 \text{ ksi} / 1.85 = 18.9 \text{ ksi}$



Components Removed for Clarity

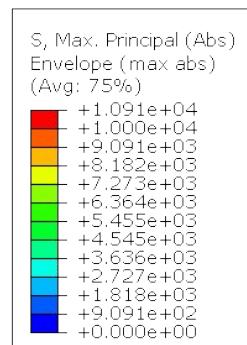
Yield Strength of 6061-T6 = 35 ksi
Expected Stress in Part = 14.75 ksi
Resulting FoS = **2.37 > 1.85**

Stresses evaluated in the chassis gusset plates are compared to the dynamic loading (bridge type) yield safety factor of 1.85. Stresses near bolted and patron connections are evaluated two elements away from the connection to ignore singularities and artifacts of the simulation. This provides a nominal stress in the parent material at the connection location.

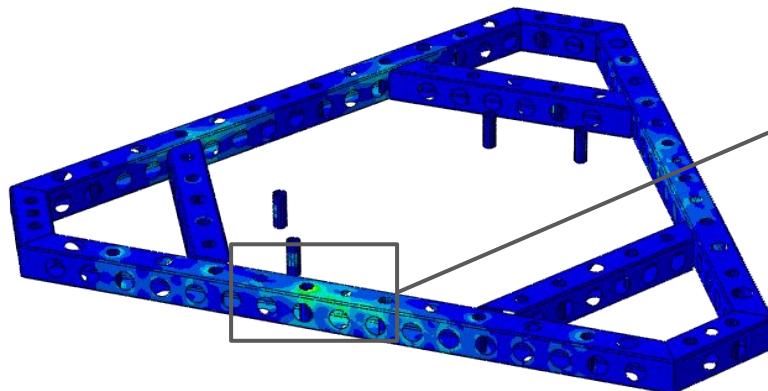
3. Vehicle Structural Analysis - Finite Element Model

Expected Principal Stresses are Acceptable in Welded 6061-T6 Material

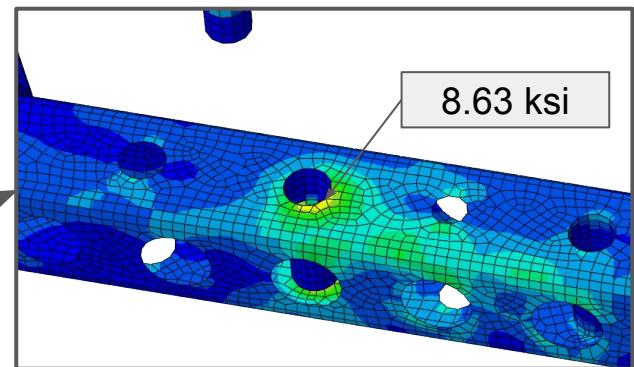
Load Case: 60deg



Units above are in psi
 $24 \text{ ksi} / 2.20 = 10.9 \text{ ksi}$



Abs. Principal Stress Contour Plot
Only Welded Components are Displayed



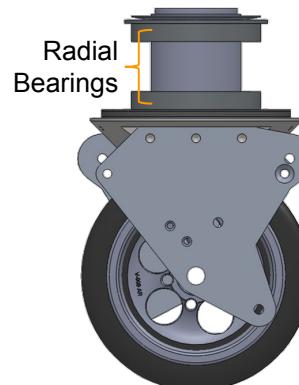
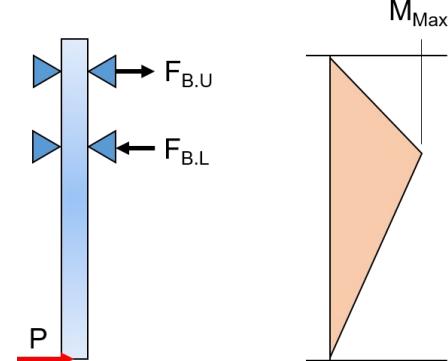
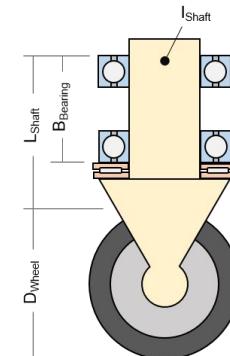
Ult. Strength Welded 6061-T6 = 24 ksi
Expected Stress in Part = 8.63 ksi
Resulting FoS = **2.78 > 2.20**

Stresses evaluated in the chassis beam members are compared to the dynamic loading (bridge type) ult safety factor of 2.20. Stresses at welded connections are evaluated at the worst nodal location, typically at the node connecting the crush tube and the chassis beam. Evaluating stresses at this location is to account for welding defects despite the conservative stress values due to the singularity of connecting shell elements at 90deg angles.

3. Vehicle Structural Analysis - Supporting Calculations

Bending Stresses in Rotating Yaw Shaft

| Bending Stresses Induced in Rotating Yaw Shaft | | | | |
|--|--------------------|----------------------|------|---|
| Name | Var | Val | Unit | Comment / Equation |
| <i>System Geometry</i> | | | | |
| Wheel Diameter | D _{Wheel} | 5 | in | Assumed |
| Shaft Length Above Wheel | L _{shaft} | 3.29 | in | Assumed |
| Distance Between Bearings | Bearing | 2.03 | in | Height of Beams |
| Shaft Outer Diameter | d _{outer} | 1.97 | in | 50mm Shaft to Inches |
| Shaft Inner Diameter | d _{inner} | 1.18 | in | Required for Slip Ring |
| <i>Load Information (Assumed on One Wheel)</i> | | | | |
| Acceleration of Vehicle | a | 1.0 g | | Specified from Stakeholder |
| Weight of Passenger | w _p | 300 lbs | | 95th Percentile Male |
| Weight of System | w _s | 62.5 lbs | | Assumed per Weight Budget |
| Total Weight of System | W | 363 lbs | | = w _p + w _s |
| Total Mass of System | m | 0.94 slug*in | | = W / 386.4 |
| Applied Load at Bottom of Wheel | P | 363 lbs | | = m * (a * 386.4) |
| <i>Modeled as an Overhang Beam</i> | | | | |
| Shaft Area Moment of Inertia | I _{shaft} | 0.64 in ⁴ | | = ($\pi/64$) * (d _{outer} ⁴ - d _{inner} ⁴) |
| Effective Beam Length | L _{eff} | 8.29 in4 | | = D _{Wheel} + L _{shaft} |
| Reaction Force on Lower Bearing | F _{B,L} | 1478 lbs | | = (P * L _{eff}) / Bearing |
| Reaction Force on Upper Bearing | F _{B,U} | -1116 lbs | | = P - F _{B,L} |
| Maximum Bending Moment | M _{Max} | -2267 in-lbs | | = F _{B,U} * Bearing |
| Bending Stress on Shaft | σ_{Bend} | 3476 psi | | = M _{Max} * (d _{outer} / 2) / I _{shaft} |
| Aluminum 6061-T6 Yield Strength | σ_{Yield} | 35000 psi | | Referenced in MMPDS |
| Resulting Factor of Safety | FoS | 10.1 > 1.85 | | = σ_{Yield} / σ_{Bend} |



The bending stresses in the vehicle rotating yaw shaft were determined by modeling the shaft as an effective beam. Although the bolt preload and the bolt holes are not considered, the significant strength margin proves the design is sufficient.

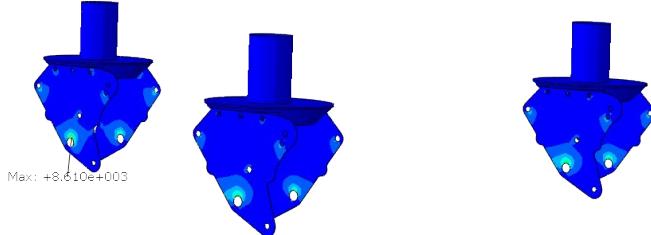
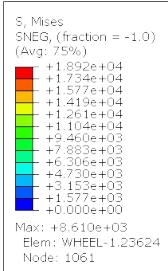
3. Vehicle Structural Analysis - Finite Element Model

Small Hole Analysis Methodology

The wheel assembly includes small holes for mounting electronics and sensors. These holes affect the mesh size and can increase the solve time. The model is idealized by removing these small holes and a nominal stress through the section is determined by the finite element solver. Using the stress concentration equations on the right, the adjusted stress can be calculated. For simplicity, the same concentration factor equations apply to holes in near proximity to others.

The maximum stresses were calculated in the wheel assembly plates over all load cases. It was determined that the *Perpendicular* load case was the most severe, and it can be seen below.

Load Case:
Perpendicular



Von Mises Stress Contour Plot

Units above are in psi
35 ksi / 1.85 = 18.9 ksi

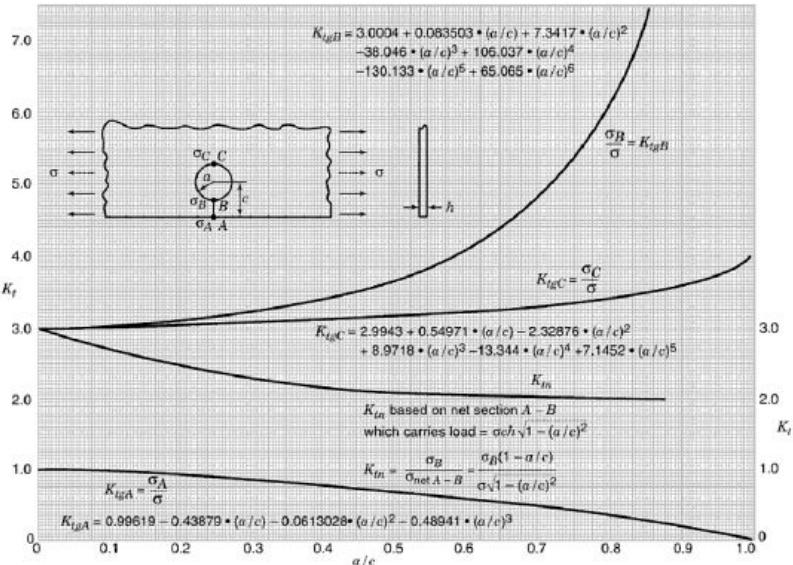


Figure above taken from Reference 5.

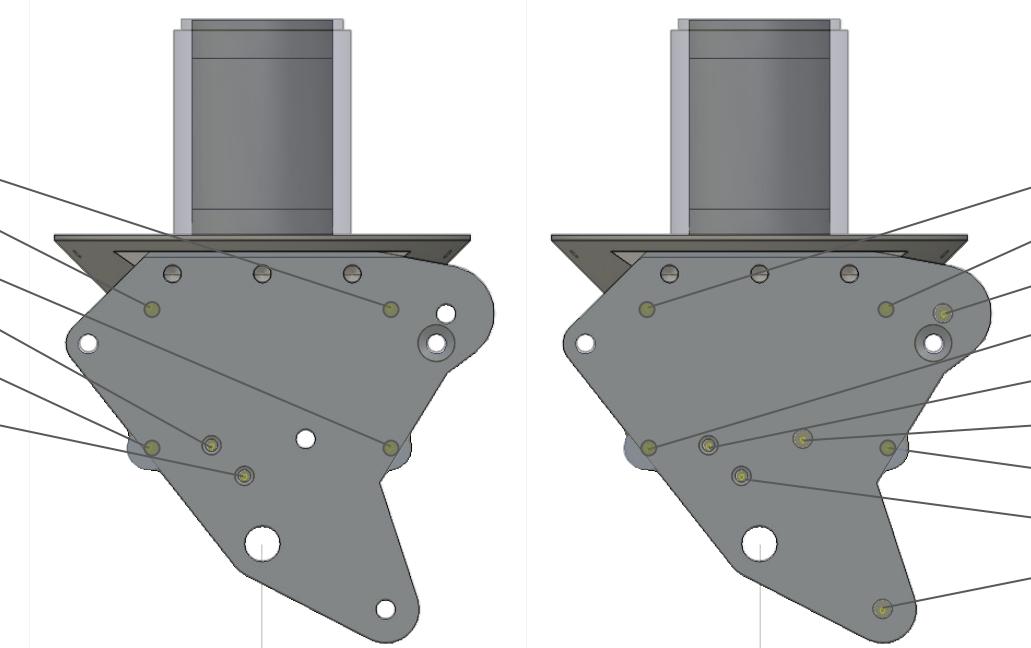
The stress contour plot for the front wheel assembly is detailed on following slides.

3. Vehicle Structural Analysis - Finite Element Model

Small Hole Locations in Wheel Assembly Side Plates

The holes shown below were idealized out of the finite element model. The hole diameter and distance away from the nearest edge or adjacent hole was recorded and used to determine the appropriate stress concentration factor. The results are tabulated on the following pages and the adjusted stress value is compared to the allowable.

| Hole | Dia. [in] |
|------|-----------|
| L1 | 0.130 |
| L2 | 0.130 |
| L3 | 0.130 |
| L4 | 0.136 |
| L5 | 0.130 |
| L6 | 0.136 |



| Hole | Dia. [in] |
|------|-----------|
| R1 | 0.130 |
| R2 | 0.130 |
| R3 | 0.213 |
| R4 | 0.130 |
| R5 | 0.136 |
| R6 | 0.213 |
| R7 | 0.130 |
| R8 | 0.136 |
| R9 | 0.213 |

3. Vehicle Structural Analysis - Finite Element Model

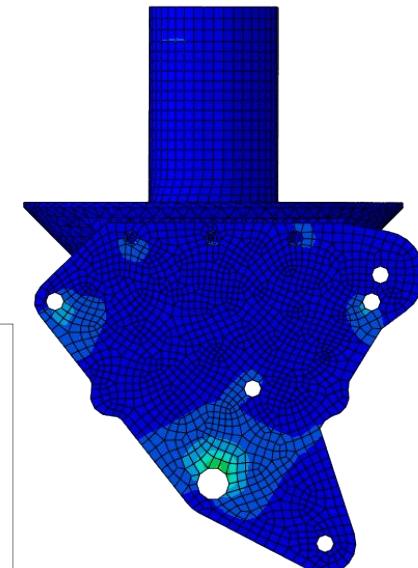
Small Hole Stresses in Left Side Plate of Wheel Assembly

| Hole | Dia. [in] | Dist [in] | Rad/Dist | K _{tgA} | K _{tgB} | K _{tgC} | Nom. σ | Adjust σ |
|-----------|--------------|--------------|-------------|------------------|------------------|------------------|-------------|-------------|
| L1 | 0.130 | 0.459 | 0.14 | 0.92 | 3.09 | 3.05 | 0.74 | 2.28 |
| L2 | 0.130 | 0.353 | 0.18 | 0.89 | 3.12 | 3.06 | 1.30 | 4.06 |
| L3 | 0.130 | 0.250 | 0.26 | 0.83 | 3.20 | 3.08 | 0.50 | 1.59 |
| L4 | 0.136 | 0.432 | 0.16 | 0.91 | 3.10 | 3.05 | 0.82 | 2.55 |
| L5 | 0.130 | 0.250 | 0.26 | 0.83 | 3.20 | 3.08 | 0.48 | 1.54 |
| L6 | 0.136 | 0.432 | 0.16 | 0.91 | 3.10 | 3.05 | 2.35 | 7.29 |

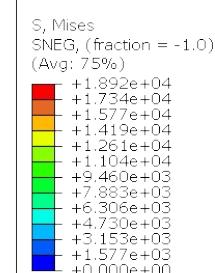
The most severe load case for the wheel assemblies is the *Perpendicular* load case. A detailed view of the nominal stress in the left side plate of the front wheel assembly is shown to the right. The table above uses values from this contour plot.

Max Expected Stress = 7.29 ksi
6061-T6 Yield Stress = 35.0 ksi
FoS 35.0 / 7.29 = 4.80 > 1.85

Front Wheel Assembly
Left Side Shown



Load Case:
Perpendicular



Units above are in psi
35 ksi / 1.85 = 18.9 ksi

Von Mises Stress Contour Plot

3. Vehicle Structural Analysis - Finite Element Model

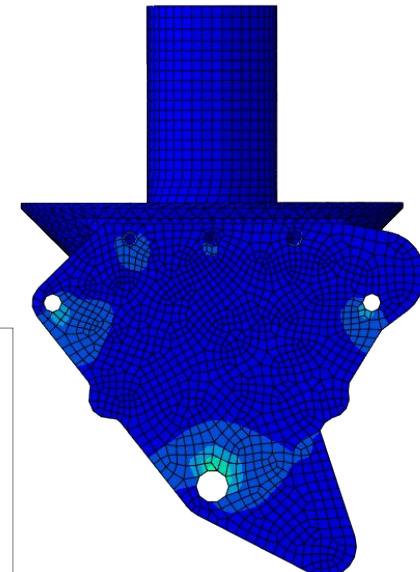
Small Hole Stresses in Right Side Plate of Wheel Assembly

| Hole | Dia. [in] | Dist [in] | Rad/Dist | K _{tgA} | K _{tgB} | K _{tgC} | Nom. σ | Adjust σ |
|------|-----------|-----------|----------|------------------|------------------|------------------|--------|----------|
| R1 | 0.130 | 0.459 | 0.14 | 0.92 | 3.09 | 3.05 | 1.72 | 5.31 |
| R2 | 0.130 | 0.353 | 0.18 | 0.89 | 3.12 | 3.06 | 0.94 | 2.92 |
| R3 | 0.213 | 0.155 | 0.69 | 0.25 | 4.73 | 3.30 | 0.07 | 0.35 |
| R4 | 0.130 | 0.250 | 0.26 | 0.83 | 3.20 | 3.08 | 0.62 | 1.99 |
| R5 | 0.136 | 0.432 | 0.16 | 0.91 | 3.10 | 3.05 | 0.72 | 2.22 |
| R6 | 0.213 | 0.730 | 0.15 | 0.92 | 3.09 | 3.05 | 0.67 | 2.08 |
| R7 | 0.130 | 0.250 | 0.26 | 0.83 | 3.20 | 3.08 | 0.45 | 1.44 |
| R8 | 0.136 | 0.432 | 0.16 | 0.91 | 3.10 | 3.05 | 1.53 | 4.75 |
| R9 | 0.213 | 0.375 | 0.28 | 0.81 | 3.23 | 3.09 | 0.15 | 0.47 |

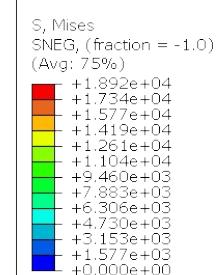
The most severe load case for the wheel assemblies is the *Perpendicular* load case. A detailed view of the nominal stress in the right side plate of the front wheel assembly is shown to the right. The table above uses values from this contour plot.

Max Expected Stress = 5.31 ksi
6061-T6 Yield Stress = 35.0 ksi
FoS 35.0 / 5.31 = 6.59 > 1.85

Front Wheel Assembly
Right Side Shown



Load Case:
Perpendicular



Units above are in psi
35 ksi / 1.85 = 18.9 ksi

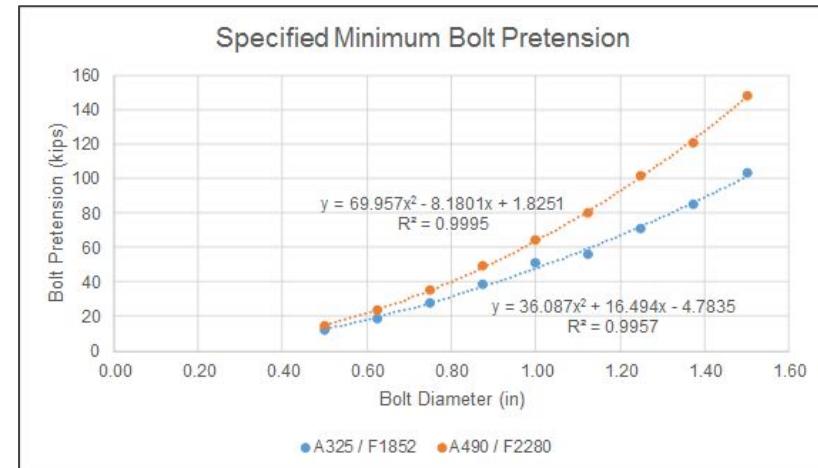
Von Mises Stress Contour Plot

3. Vehicle Structural Analysis - Finite Element Model

Required Pretension for Bolted Structural Connections

| Nominal Bolt Diameter | Specified Minimum Bolt Pretension, T_m (kips) | |
|-----------------------|---|--------------|
| | A325 / F1852 | A490 / F2280 |
| 1/2 | 12 | 15 |
| 5/8 | 19 | 24 |
| 3/4 | 28 | 35 |
| 7/8 | 39 | 49 |
| 1 | 51 | 64 |
| 1 1/8 | 56 | 80 |
| 1 1/4 | 71 | 102 |
| 1 3/8 | 85 | 121 |
| 1 1/2 | 103 | 148 |

Table 7.1 Minimum Bolt Pretension for Pre-Installation Verification [6]



Interpolating to a Different Diameter Bolt

| Diameter = 0.25 in | 1.60 kips | 4.15 kips |
|--------------------|-----------|--------------|
| A325 / F1852 | | A490 / F2280 |

To accurately analyze the bolted connections, preload values for the structural connections were required. Using Table 7.1 presented in the *Specification for Structural Joints Using High-Strength Bolts* from the Research Council on Structural Connections (RCSC), a quadratic fit was calculated using the documented values, and different bolt pretensions were determined. It is shown on the next page that the A325 / F1852 value is required for slip-critical joints, though the system is expected to operate safely in the event of bolt slipping.

3. Vehicle Structural Analysis - Finite Element Model

Bolted Joint Analysis: RCSC Calculations

| RCSC Bolt Calculations for 1/4 - 20 Bolts | | | | | |
|--|---------------|-----------------------|------|---|-------|
| Name | Var | Val | Unit | Comment / Equation | Eqn # |
| <i>Constants and Factors for Bolted Connection</i> | | | | | |
| Required Tensile Strength | T_u | 0.35 kips | | Output From FEM Simulation Defined by CAD Geometry | |
| Required Shear Strength | V_u | 0.37 kips | | | |
| Nominal Diameter of Bolt | d_b | 0.25 in | | | |
| Clamped Material Thickness | t | 0.19 in | | | |
| Hole Clearance Distance | L_c | 0.06 in | | | |
| Resistance Factor | Φ | 0.75 | | RCSC Specified, Except for Slip Critical | |
| <i>Shear and Tension Check</i> | | | | | |
| Nominal Strength per Unit Area | F_{n-Ten} | 90 ksi | | Values Referenced in Table 5.1 | |
| Nominal Strength per Unit Area | $F_{n-Shear}$ | 54 ksi | | | |
| Bolt Cross-sectional Area | A_b | 0.05 in ² | | $= (\pi / 4) * d_b^2$ | |
| Nominal Tensile Strength of Bolt | R_{n-Ten} | 5.89 kip | | $= F_{n-Ten} * A_b / \Phi$ | (5.1) |
| Nominal Shear Strength of Bolt | $R_{n-Shear}$ | 3.53 kip | | $= F_{n-Shear} * A_b / \Phi$ | (5.1) |
| Resulting Tension Safety Factor | $X_{Tension}$ | 16.7 > 1.67 | | $= R_{n-Ten} / T_u$ | |
| Resulting Shear Safety Factor | X_{Shear} | 9.6 > 1.67 | | $= R_{n-Shear} / V_u$ | |

The required tensile and resultant shear strengths were extracted from the finite element model beam elements. For conservatism, it was assumed that the maximum shear and tensile forces acted on the same bolt. The equations and analysis procedure were referenced using Reference 6, and the resulting tension and shear safety factors are referenced using Reference 7.

| RC SC Bolt Calculations for 1/4 - 20 Bolts (Continued) | | | | | |
|--|----------------|-----------------------|------|---|-------|
| Name | Var | Val | Unit | Comment / Equation | Eqn # |
| <i>Combined Shear and Tension Check</i> | | | | | |
| Design Strength in Tension | $(\Phi R_n)_t$ | 4.42 kip | | $= R_{n-Ten} / T_u$ | |
| Design Strength in Shear | $(\Phi R_n)_v$ | 2.65 kip | | $= R_{n-Shear} / V_u$ | |
| Limit-State of Bolt Configuration | L_{Comb} | 0.03 | | $= [T_u / (\Phi R_n)_t]^2 + [V_u / (\Phi R_n)_v]^2$ (5.2) | |
| Resulting Combination Margin | X_{Comb} | 38.9 > 1.67 | | $= 1 / L_{Comb}$ | |
| <i>Bearing Strength Calculations</i> | | | | | |
| Tensile Strength for 6061-T6 | F_u | 35.0 ksi | | Yield Material in Bearing | |
| Capacity of Material (Lowest Factor) | R_{Cap} | 3.28 kip | | $= 2 * d_b * t * F_u$ | (5.5) |
| Required Bolt Load (Highest Factor) | R_n | 0.62 kip | | $= 1.5 * L_c * t * F_u$ | (5.4) |
| Resulting Combination Margin | $X_{Bearing}$ | 5.3 > 1.85 | | $= R_{Cap} / R_n$ | |
| <i>Slip Critical Connection</i> | | | | | |
| Resistance Factor for Slip Critical | Φ | 0.85 | | Specified RCSC Section 5.4.1 | |
| Mean Slip Coefficient | μ | 0.33 | | Assume Lowest Slip Coefficient | |
| Pretension Multiplier | D_u | 1.0 | | Assume Bolt Pretensioned to Minimum | |
| Number of Bolts in Joint | N_b | 1 | | Assume Load on One Bolt | |
| Specified Minimum Pretension | T_m | 1.60 kip | | Interpolated From Table 7.1 | |
| Nominal Slip Resistance of Plane | R_n | 0.41 kip | | $= \mu * D_u * T_m * N_b [1 - T_u / (D_u T_m N_b)]$ (5.6) | |
| Resulting Slip Critical Margin | X_{Slip} | 1.1 > 1.0 | | $= R_n / V_u$ | |

Equations and Analysis Procedure Correspond to RCSC 2009 [6]

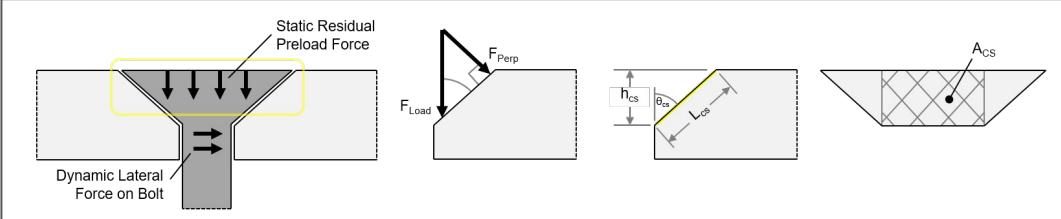
Load Case: 150deg Configuration

3. Vehicle Structural Analysis - Supporting Calculations

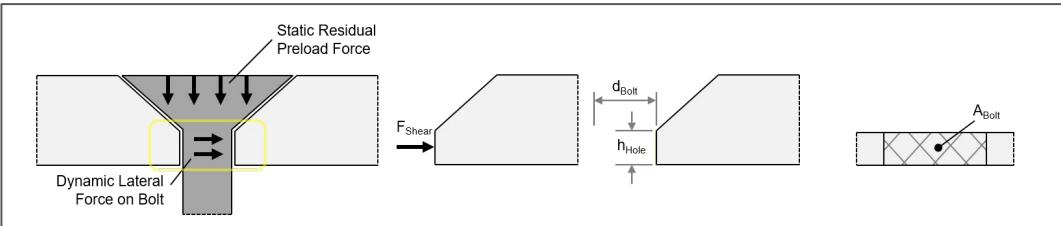
Countersunk Bolted Connections on Chassis Gusset Plates

| Countersink Preload and Dynamic Bolt Loading | | | |
|---|--------------------|-----------------------|---|
| Name | Var | Val | Unit |
| <i>Material Specifications and System Geometry</i> | | | |
| Bearing Strength 6061-T6 | $\sigma_{Bearing}$ | 50000 psi | Referenced in MMPDS |
| Angle of Countersink | θ_{CS} | 100 deg | Given |
| Gusset Plate Thickness | t_{Gusset} | 0.188 in | Specified in CAD |
| Height of Countersink | h_{CS} | 0.095 in | Specified by Countersink |
| Inner Diameter of Countersink | d_{Bolt} | 0.25 in | 1/4-20 Bolt Diameter |
| <i>Preload Derivation and Dynamic Loading</i> | | | |
| Preload Applied to Joint | F_{Load} | 1600 lbs | Assumed Preload Applied |
| Angle of Taper (1/2 Side) | $\theta_{Working}$ | 0.873 rad | $= (\pi/180) * (\theta_{CS}/2)$ |
| Perpendicular Force | F_{Perp} | 1226 lbs | $= F_{Load} * \sin(\theta_{Working})$ |
| Max Shear Force on Bolt | F_{Shear} | 369 lbs | Output From FEM |
| <i>Projected Area Derivation</i> | | | |
| Height of Through Hole | h_{Hole} | 0.092 in | $= t_{Gusset} - h_{CS}$ |
| Countersink Taper Length | L_{CS} | 0.148 in | $= h_{CS} / \cos(\theta_{Working})$ |
| Projected Countersink Area | A_{CS} | 0.116 in ² | $= \pi * L_{CS} * d_{CS}$ |
| Projected Bolt Shank Area | A_{Bolt} | 0.023 in ² | $= h_{Hole} * d_{CS}$ |
| <i>Expected Stresses - Preload and Dynamic</i> | | | |
| Preload Bearing Stress | $\sigma_{PreLoad}$ | 10533 psi | $= F_{Perp} / A_{CS}$ |
| Dynamic Bearing Stress | $\sigma_{Dynamic}$ | 16002 psi | $= F_{Shear} / A_{Bolt}$ |
| Expected Total Bearing Stress | σ_{Expect} | 26535 psi | $= \sigma_{PreLoad} + \sigma_{Dynamic}$ |
| Bearing Strength Safety Factor: 1.88 > 1.85 OK | | | |

Preload Residual Stresses



Dynamic Bearing Stresses



The total stress in the countersink connection is the superposition of residual stresses due to preload and the dynamic stresses due to loading. It is conservative to add the stresses together. The shear and preload values are referenced on previous pages.

4. Vehicle Mechanical Analysis

Supporting Calculations

Analysis Overview

Vehicle Structural
Analysis

Vehicle Mechanical
Analysis

References

Appendix

4. Vehicle Mechanical Analysis

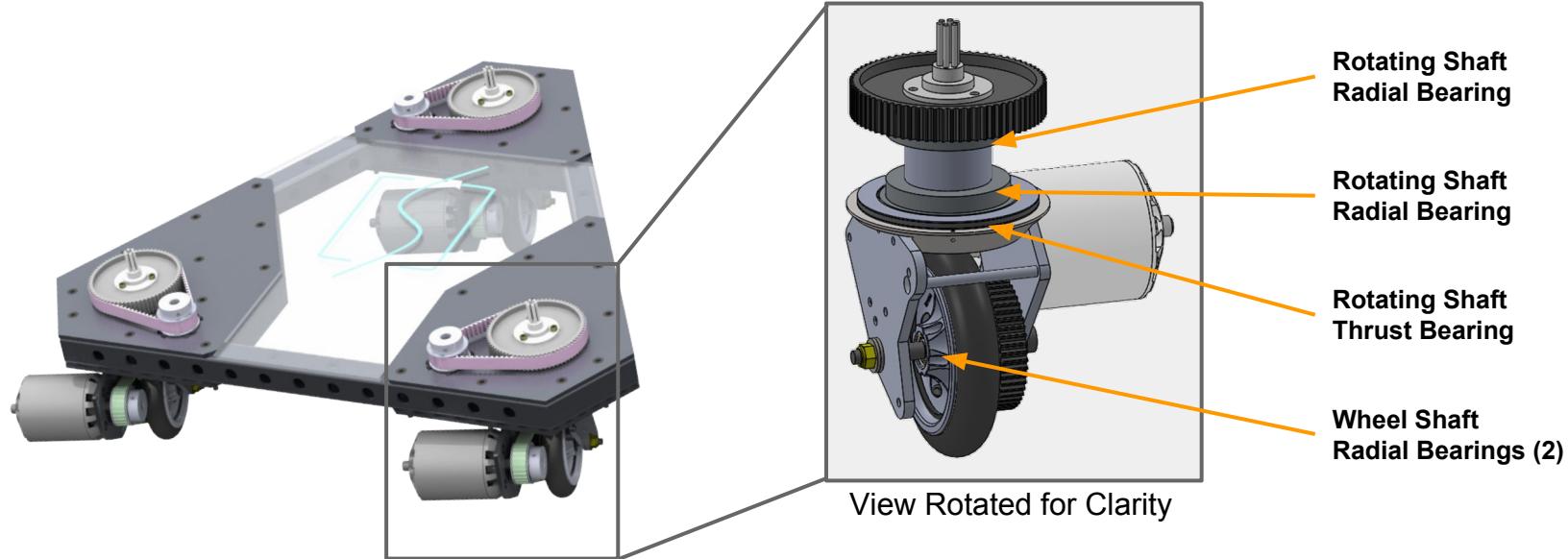
Safety Factor Summary by Component

The expected stresses and resulting safety factors for the mechanical components are listed below. For the mechanical components, either stresses or forces were analyzed and were then compared to documented allowables. The resulting safety factor is calculated below and compared to the required safety factor. If the component is a consumer off the shelf (COTS) part, the required safety factor is 1.0. The cutsheets for the COTS parts can be found in the appendix.

| <u>Component</u> | <u>Specification</u> | <u>Allowable</u> | <u>Expected</u> | <u>Expect SF</u> | <u>Required SF</u> |
|---------------------------------------|----------------------|------------------|-----------------|------------------|--------------------|
| <i>Radial Bearing Yaw Shaft</i> | Force Margin | 2.63 kip | 1.5 kip | 1.78 | > 1.00 |
| <i>Thrust Bearing Yaw Shaft</i> | Force Margin | 11.6 kip | 0.6 kip | 19.3 | > 1.00 |
| <i>Radial Bearing Wheel Shaft</i> | Force Margin | 405 lbs | 300 lbs | 1.35 | > 1.00 |
| <i>Timing Belt</i> | Force Margin | 750 lbs | 587 lbs | 1.28 | > 1.00 |
| <i>Wheel Shaft Shoulder Bolt</i> | Axial Stress | 160 ksi | 102 ksi | 1.57 | > 1.00 |
| | Shear Stress | 160 ksi | 6.0 ksi | 26.8 | > 1.00 |
| | Bearing Stress | 54 ksi | 7.4 ksi | 7.33 | > 1.85 |
| <i>Motor Bolts</i> | Shear Stress | 500 MPa | 17.9 MPa | 27.9 | > 1.00 |
| | Bearing Stress | 372 MPa | 47.9 MPa | 7.78 | > 1.85 |

4. Vehicle Mechanical Analysis

Vehicle Bearings - Design



Each wheel assembly includes two radial bearings on the rotating yaw shaft as well as a thrust bearing. Additionally, each assembly includes two radial bearings pressed into the wheel hub and another radial bearing pressed into the timing belt pulley (enveloped in the following calculations).

4. Vehicle Mechanical Analysis

Vehicle Bearings - Force Margins

Force Margin for Bearings

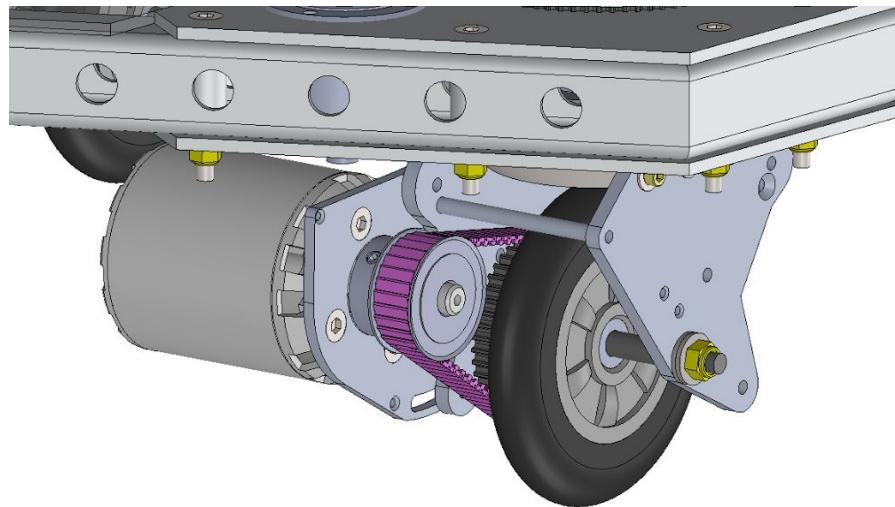
| Name | Var | Val | Unit | Comment / Equation |
|---|---------------|-------------|------|--|
| <i>Rotating Yaw Shaft - Radial Bearing</i> | | | | |
| Max Expected Load on Bearing | P_{Expect} | 1.48 kip | | Reaction Force on Lower Bearing |
| Allowable Load on Bearing (KN) | P_{Allow} | 11.7 KN | | VXB F6910ZZ Static Load |
| Allowable Load on Bearing (lbs) | P_{Allow} | 2.63 kip | | Conversion to Imperial Units |
| Resulting Force Margin | X_{Thrust} | 1.78 | | $= P_{Allow} / P_{Expect}$ |
| <i>Rotating Yaw Shaft - Thrust Bearings</i> | | | | |
| Maximum Patron Load | W_{Patron} | 300 lbs | | Max Patron Allowable |
| Abuse Loading Factor | f_{Abuse} | 2.0 | | Conservative Impact Factor |
| Max Expected Load on Bearing | P_{Expect} | 0.60 kip | | $= W_{Patron} * f_{Abuse} / 1000$ |
| Allowable Load on Bearing (KN) | P_{Allow} | 51.6 KN | | Koyo NRB NTA-5266 Dynamic Load |
| Allowable Load on Bearing (lbs) | P_{Allow} | 11.6 kip | | Conversion to Imperial Units |
| Resulting Force Margin | X_{Thrust} | 19.3 | | $= P_{Allow} / P_{Expect}$ |
| <i>Wheel Shaft - Radial Bearing</i> | | | | |
| Number of Bearings | $N_{Bearing}$ | 2 | | Bearings Pressed into Wheel Hub |
| Max Expected Load on Bearing | P_{Expect} | 600 lbs | | $= W_{Patron} * f_{Abuse}$ |
| Allowable Load on Bearing (KN) | P_{Allow} | 1800 N | | AST 71900C Static Load |
| Allowable Load on Bearing (lbs) | P_{Allow} | 404.7 lbs | | Conversion to Imperial Units |
| Resulting Force Margin | X_{Thrust} | 1.35 | | $= P_{Allow} / (P_{Expect} / N_{Bearing})$ |

Using bearing cutsheets available online, the expected forces through the bearings were compared to the rated allowables. All bearing force margins were calculated considering a 300lb patron moving at the maximum acceleration, and in the most severe direction, in order to react the forces on one wheel assembly.

For the bearing reaction force calculation, please refer to the *Bending Stresses in Rotating Yaw Shaft* calculations. In all calculations shown to the left, the expected forces, P-Expect, are compared against the allowable force, P-Allow.

4. Vehicle Mechanical Analysis

Timing Belt Pulley - Design



Single Wheel Assembly
Shown for Clarity

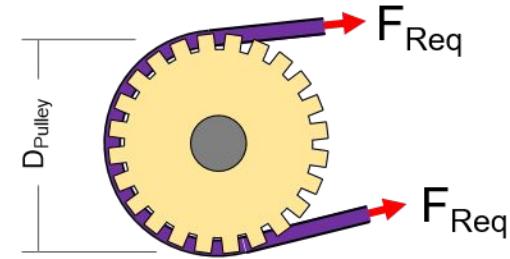
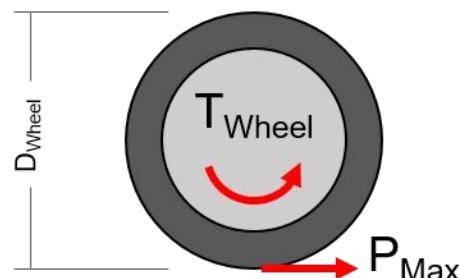
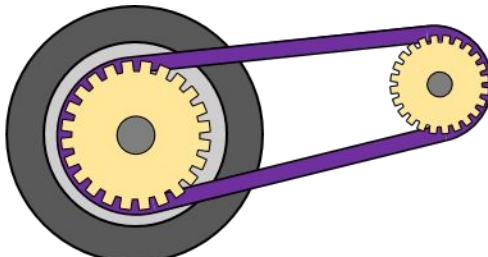
An L-Series timing belt is proposed for the propulsion system (shown in purple). The belt will be tensioned by rotating the motor mount plate away from the wheel. The wheel pulley is attached to the wheel through six bolts to transfer the torque. By using the maximum expected load on the wheel as well as the maximum acceleration, the load through the timing belt could be calculated.

4. Vehicle Mechanical Analysis

Timing Belt Pulley - Force Margin

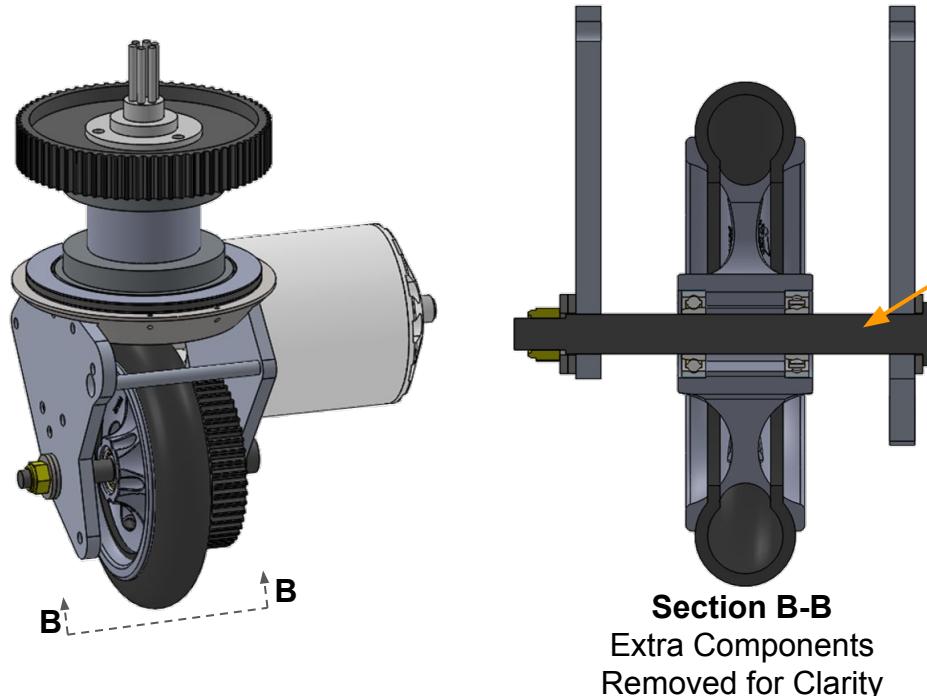
| Force Margin for Timing Belt Pulley | | | | |
|---|---------------------|----------------|--|-----------------------------|
| Name | Var | Val | Unit | Comment / Equation |
| System Geometry and Belt Specifications | | | | |
| Maximum Force on Wheel | P _{Max} | 362.5 lbs | | Weight of System and Patron |
| Diameter of Wheel | D _{Wheel} | 5.0 in | | 5in Pneumatic Wheel |
| Diameter of Pulley (mm) | D _{Pulley} | 78.4 mm | | SDP-SI Pulley Listed Below |
| Diameter of Pulley (inch) | | 3.1 in | | Convert to Inch Measurement |
| Belt Breaking Strength (per Width) | F _{Break} | 125 lbs/(1/8") | | SDP-SI L Timing Belts |
| Width of Timing Belt | W _{Belt} | 0.75 in | | SDP-SI L Timing Belts |
| Resulting Calculations for Timing Belt | | | | |
| Total Breaking Strength on Belt | F _{Belt} | 750.0 lbs | = F _{Break} * (W _{Belt} / 0.125) | |
| Effective Torque on Pulley | T _{Wheel} | 906.3 in-lbs | = P _{Max} * (D _{Wheel} / 2) | |
| Force Required by Belt | F _{Req} | 587.2 lbs | = T _{Wheel} / (D _{Pulley} / 2) | |
| Resulting Force Margin | X _{Force} | 1.28 | = F _{Belt} / F _{Req} | |

Using the total weight of the system (300lb patron and 62.5lb vehicle), a conservative force margin in the timing belt was calculated. Since it is assumed that the total weight is on one pulley assembly, the narrow force margin listed to the left is acceptable.



4. Vehicle Mechanical Analysis

Wheel Shaft - Design

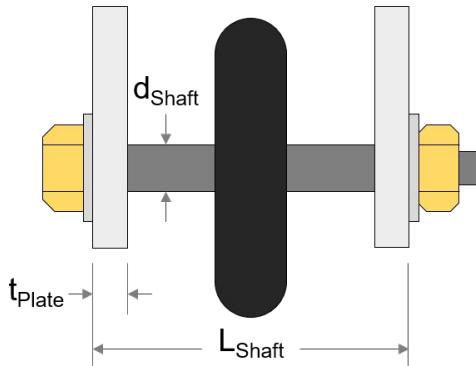


Analyzed Shaft

A 10mm diameter shoulder bolt supports the wheel and pulley assembly. The bolt is secured to the side plates of the wheel assembly and load is transferred through the bearings.

4. Vehicle Mechanical Analysis

Wheel Shaft - Calculations

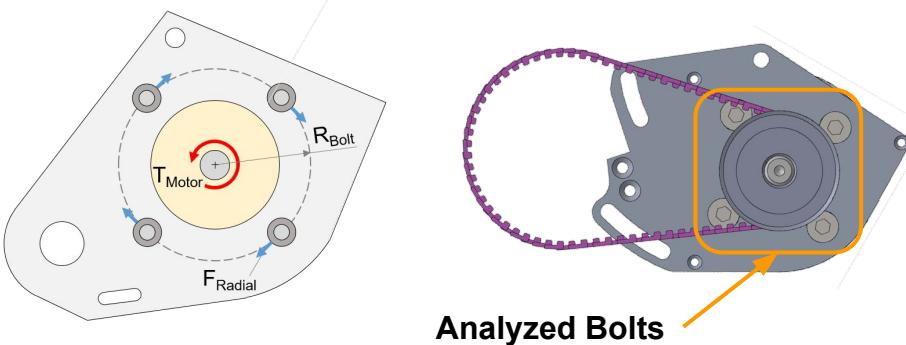


Using the total weight of the system (300lb patron and 62.5lb vehicle) and an impact / abuse factor, conservative strength safety factors for the wheel shaft were calculated. Considering the bending and shear of the shaft as well as the bearing loads in the plate, the calculated margins are acceptable and the design is sufficient for the expected loads.

| Wheel Shaft Strength Calculations | | | | |
|--------------------------------------|----------------------------|-----------------------|--|--------------------|
| Name | Var | Val | Unit | Comment / Equation |
| System Geometry and System Loading | | | | |
| Shaft Diameter (mm) | d_{Shaft} | 10 mm | 10mm Shoulder Bolt Diameter | |
| Shaft Diameter (in) | d_{Shaft} | 0.39 in | Conversion to Imperial Units | |
| Unsupported Length | L_{Shaft} | 3.4 in | Unsupported Length of Bolt | |
| Thickness of Plate Support | t_{Plate} | 0.25 in | Side Plate Thickness | |
| Total Weight of System | W | 363 lbs | Weight of System and Patron | |
| Abuse Loading Factor | f_{Abuse} | 2.0 | Conservative Impact Factor | |
| Aluminum and Bolt Allowables | | | | |
| Aluminum 6061-T6 Yield Strength | σ_{Alum-Y} | 35.0 ksi | Referenced in MMPDS | |
| Aluminum 6061-T6 Bearing Strength | σ_{Alum-B} | 54.0 ksi | Referenced in MMPDS | |
| Class 12.9 Min Yield Strength (MPa) | σ_{Bolt-Y} | 1100 MPa | Class 12.9 Allowable | |
| Class 12.9 Min Yield Strength (ksi) | σ_{Bolt-Y} | 160 ksi | Conversion to Imperial Units | |
| Bending Stress in Bolt | | | | |
| Shaft Moment of Inertia | I_{Shaft} | 0.001 in ⁴ | $= (\pi / 64) * d_{Shaft}^4$ | |
| Max Expected Load on Bearing | P_{Expect} | 725 lbs | $= W * f_{Abuse}$ | |
| Max Bending Moment in Shaft | M_{Max} | 610 in-lbs | $= P_{Expect} * L_{Shaft} / 4$ Simply Support | |
| Bending Stress in Shaft | σ_{Bend} | 102 ksi | $= M_{Max} * (d_{Shaft} / 2) / (I_{Shaft} * 1000)$ | |
| Resulting Factor of Safety | FoS | 1.57 | $= \sigma_{Yield} / \sigma_{Bend}$ | |
| Shear and Bearing Stresses | | | | |
| 10mm Bolt Shear Area | A_{Shear} | 0.122 in ² | $= (\pi / 4) * d_{Shaft}^2$ | |
| Shear Stress in Bolt | σ_{Shear} | 5.96 ksi | $= P_{Expect} / (A_{Shear} * 1000)$ | |
| Resulting Shear Safety Factor | X_{Shear} | 26.8 | $= \sigma_{Shear} / \sigma_{Bolt-Y}$ | |
| Plate Bearing Area | $A_{Bearing}$ | 0.098 in ² | $= d_{Shaft} * t_{Plate}$ | |
| Bearing Stress in Plate | $\sigma_{Bearing}$ | 7.37 ksi | $= P_{Expect} / (A_{Bearing} * 1000)$ | |
| Max Bending Moment in Shaft | X_{Bearing} | 7.33 | $= \sigma_{Bearing} / \sigma_{Alum-B}$ | |

4. Vehicle Mechanical Analysis

Motor Bolts Strength Calculations



The torque required from the motor will be reacted by the bolts mounted to the motor plate. Assuming the torque is reacted equally to all bolts in the bolt pattern, the resultant load per bolt can be calculated. The shear stress in the bolt and the bearing stress in the plate were analyzed and compared to allowables.

Motor Bolts Strength Calculations

| Name | Var | Val | Unit | Comment / Equation |
|--|--------------------|---------------------|------|--|
| System Geometry and Allowable Strengths | | | | |
| Motor Bolt Diameter | d_{Bolt} | 6 mm | | Bolts Used to Mount Motor |
| Bolt Pattern Radius | R_{Bolt} | 28 mm | | Center to Center Distance |
| Engaged Length of Bolt | L_{Bolt} | 1.8 mm | | Thickness After Countersink |
| Diameter of Motor Pulley | D_{Pulley} | 43.4 mm | | SDP-SI Timing Belt Pulley |
| DIN 965 Bolt Tensile Strength | σ_{Bolt-T} | 500 MPa | | Referenced Bolted Allowable |
| 6061-T6 Bearing Strength (ksi) | | 54 ksi | | Referenced in MMPDS |
| 6061-T6 Bearing Strength (MPa) | σ_{Alum-B} | 372 MPa | | Conversion to Metric Units |
| Effective Forces on Motor Bolts | | | | |
| Force Through Belt (lbs) | | 587 lbs | | Weight of System and Patron |
| Force Through Belt (N) | F_{Req} | 2612 N | | Conversion to Metric Units |
| Expected Torque on Motor | T_{Motor} | 56,695 N-mm | | $= F_{Req} * (D_{Pulley} / 2)$ |
| Radial Loads on Bolts | F_{Radial} | 2025 N | | $= T_{Motor} / R_{Bolt}$ |
| Resulting Safety Factors for Bolts and Aluminum | | | | |
| Shear Area on Single Bolt | A_{shear} | 28.3 mm^2 | | $= (\pi / 4) * d_{Bolt}^2$ |
| Shear Stress in Bolt | σ_{Shear} | 17.9 MPa | | $= (F_{Radial} / 4) / A_{shear}$ |
| Resulting Shear Safety Factor | X_{Shear} | 27.9 | | $= \sigma_{Bolt-T} / \sigma_{Shear}$ |
| Bearing Area on Single Bolt | $A_{Bearing}$ | 10.6 mm^2 | | $= d_{Bolt} * L_{Bolt}$ |
| Bearing Stress in Plate | $\sigma_{Bearing}$ | 47.9 MPa | | $= (F_{Radial} / 4) / A_{Bearing}$ |
| Resulting Bearing Safety Factor | $X_{Bearing}$ | 7.78 | | $= \sigma_{Alum-B} / \sigma_{Bearing}$ |

5. References

Vehicle Structural
Analysis

Vehicle Mechanical
Analysis

References

Appendix

5. References

Publications Used for Analysis

- [1] ASTM International F2291-17 “*Standard Practice for Design of Amusement Rides and Devices*” 2017.
- [2] D.O.T, “*Metallic Materials Properties Development and Standardization*”. January, 2003.
- [3] J. Randolph Kissell. “*Aluminum Structures: A Guide to Their Specifications and Design*” 2002.
- [4] John Wiley and Sons. “*The Measures of Man and Woman Revised Edition*”. Human Factors in Design. 2002.
- [5] Walter D. Pilkey, “*Peterson’s Stress Concentration Factors, Third Edition*” 2008.
- [6] Research Council on Structural Connections “*Specification for Structural Joints Using High-Strength Bolts*” 2014.
- [7] American Institute of Steel Construction 360-16 “*Specification for Structural Steel Buildings*” 2016.

6. Appendix

Specific References, COTS Cutsheets

6. Appendix: 6061-T6 Material Properties

Metallic Materials Properties Development and Standardization (2003)

| Table 3.6.2.0(b ₂). Design Mechanical and Physical Properties of 6061 Aluminum Alloy Plate | | | | | | | | | | | |
|--|---------------------------------|-----|-------------|---------------------|------------------|-----------------|---|------|---------------------------|-----------------|------------------------------|
| Specification | AMS 4026 and AMS-QQ-A-250/11 | | | AMS QQ-A- 250/11 | | | AMS 4025, AMS 4027 and AMS-QQ-A-250/11 | | | | |
| | Plate | | | | | | | | | | |
| Form | T451 | | | | T42 ^a | | | | T651 and T62 ^b | | |
| Temper | 0.250-2.000 | | 2.001-3.000 | | 0.250- 1.000 | 1.001- 3.000 | 0.250-2.000 | | 2.001-3.000 | 3.001- 4.000 | 4.001- 6.000 ^c |
| Basis | A | B | A | B | S | S | A | B | A | B | S |
| Mechanical Properties: | | | | | | | | | | | |
| F_u , ksi: | | | | | | | | | | | |
| L | | | | | | | | | | | |
| LT | 30 | 32 | 30 | 32 | 30 | 30 | 42 | 43 | ... 42 | 43 | 40 |
| F_y , ksi: | | | | | | | | | | | |
| L | | | | | | | | | | | |
| LT | 16 | 18 | 16 | 18 | 14 | 14 | 36 | 38 | ... 35 | 37 | 35 |
| F_{su} , ksi: | | | | | | | | | | | |
| L | | | | | | | | | | | |
| LT | 16 | 18 | ... | ... | ... | ... | 35 | 37 | ... | ... | ... |
| F_{sw} , ksi: | | | | | | | | | | | |
| 20 | 21 | ... | ... | ... | ... | ... | 36 | 38 | ... | ... | ... |
| F_{by} , ksi: | | | | | | | | | | | |
| $(e/D = 1.5)$ | 48 | 52 | ... | ... | ... | ... | 67 | 69 | ... | ... | ... |
| $(e/D = 2.0)$ | 63 | 67 | ... | ... | ... | ... | 88 | 90 | ... | ... | ... |
| F_{byr} , ksi: | | | | | | | | | | | |
| $(e/D = 1.5)$ | 22 | 25 | ... | ... | ... | ... | 50 | 53 | ... | ... | ... |
| $(e/D = 2.0)$ | 26 | 29 | ... | ... | ... | ... | 58 | 61 | ... | ... | ... |
| e , percent: | | | | | | | | | | | |
| L | d | ... | 16 | ... | 18 | 16 | d | ... | 6 | ... | 6 |
| E , 10^3 ksi | | | | | | | 9.9 | | | | |
| E_z , 10^3 ksi | | | | | | | | 10.1 | | | |
| G , 10^3 ksi | | | | | | | | | 3.8 | | |
| μ | | | | | | | | | | 0.33 | |
| Physical Properties: | See Figure 3.6.2.0 | | | | | | | | | | |
| ω , lb/in. ³ | 0.098 | | | | | | | | | | |
| C, K, and α | | | | | | | | | | | |
| a Design allowables were based upon data obtained from testing samples of material, supplied in the O temper, which were heat treated to demonstrate response to heat treatment by suppliers. Properties obtained by the user may be lower than those listed if the material has been formed or otherwise cold or hot worked, particularly in the annealed temper, prior to solution heat treatment. | | | | | | | | | | | |
| b Design allowables were based upon data obtained from testing T651 plate and from testing samples of plate, supplied in the O temper, which were heat treated to demonstrate response to heat treatment by suppliers. Properties obtained may be lower than those listed if the material has been formed or otherwise cold worked, particularly in the annealed temper, prior to solution heat treatment. | | | | | | | | | | | |
| c Properties for this thickness apply only to T651 temper. | | | | | | | | | | | |
| d See Table 3.6.2.0(b). | | | | | | | | | | | |

6061-T6 Plate

Tensile Ultimate Strength

Tensile Yield Strength

Shear Ultimate Strength

Bearing Yield Strength

Mechanical Properties

6. Appendix: 1025 Steel Material Properties

Metallic Materials Properties Development and Standardization (2003)

| Table 2.2.1.0(b). Design Mechanical and Physical Properties of AISI 1025 Carbon Steel | | | |
|---|----------------------------|---|----------------|
| Specification | AMS 5046 and AMS-S-7952 | AMS 5075, AMS 5077 and AMS-T-5066 ^a | ASTM A 108 |
| Form | Sheet, strip, and plate | Tubing | Bar |
| Condition | Annealed | Normalized | All |
| Thickness, in. | ... | ... | ... |
| Basis | S | S | S ^b |
| Mechanical Properties: | | | |
| F_{ut} , ksi: | | | |
| L | 55 | 55 | 55 |
| LT | 55 | 55 | 55 |
| ST | ... | ... | 55 |
| F_{ys} , ksi: | | | |
| L | 36 | 36 | 36 |
| LT | 36 | 36 | 36 |
| ST | ... | ... | 36 |
| F_{sy} , ksi: | | | |
| L | 36 | 36 | 36 |
| LT | 36 | 36 | 36 |
| ST | ... | ... | 36 |
| F_{su} , ksi | 35 | 35 | 35 |
| F_{bs} , ksi: | | | |
| (e/D = 1.5) | ... | ... | ... |
| (e/D = 2.0) | 90 | 90 | 90 |
| F_{by} , ksi: | | | |
| (e/D = 1.5) | ... | ... | ... |
| (e/D = 2.0) | ... | ... | ... |
| ϵ , percent: | | | |
| L | ... | c | c |
| LT | c | ... | ... |
| E , 10^6 ksi | 29.0 | | |
| E_c , 10^6 ksi | 29.0 | | |
| G , 10^6 ksi | 11.0 | | |
| μ | 0.32 | | |
| Physical Properties: | | | |
| ω , lb/in. ² | 0.284 | | |
| C, Btu/(lb)(°F) | 0.116 (122 to 212°F) | | |
| K, Btu/[(lb)(ft) ² (°F)/ft] | 30.0 (at 32°F) | | |
| α , 10^{-6} in./in./°F | See Figure 2.2.1.0 | | |

^a Noncurrent specification.

^b Design values are applicable only to parts for which the indicated F_{ut} has been substantiated by adequate quality control testing.

^c See applicable specification for variation in minimum elongation with ultimate strength.

Plain Carbon Steel

Tensile Ultimate Strength

Tensile Yield Strength

Shear Ultimate Strength

Mechanical Properties

6. Appendix: 6061-T6 Welded Allowables

Aluminum Structures: A Guide to Their Specifications and Design

Minimum Mechanical Properties of Aluminum Alloys (Welded) (U.S. Units)

| Alloy | Temper | Product | Thickness Range | | Tension | | Compression F_c (ksi) | Shear F_s (ksi) |
|-------------|---------------------------|-----------------|-----------------|----------|-------------|-------------|----------------------------|----------------------|
| | | | from (in.) | to (in.) | F_u (ksi) | F_y (ksi) | | |
| 1100 | H12, H14 | All | | | 11 | 3.5 | 3.5 | 8 |
| 3003 | H12, H14, H16, H18 | All | | | 14 | 5 | 5 | 10 |
| Akclad 3003 | H12, H14, H16, H18 | All | | | 13 | 4.5 | 4.5 | 10 |
| 3004 | H32, H34, H36, H38 | All | | | 22 | 8.5 | 8.5 | 14 |
| Akclad 3004 | H32, H34, H36, H38 | All | | | 21 | 8 | 8 | 13 |
| 3005 | H25 | Sheet | | | 17 | 6.5 | 6.5 | 12 |
| 5005 | H12, H14, H32, H34 | All | | | 15 | 5 | 5 | 9 |
| 5050 | H32, H34 | All | | | 18 | 6 | 6 | 12 |
| 5052 | H32, H34, O | All | | | 25 | 9.5 | 9.5 | 16 |
| 5083 | H111, O | Extrusions | | | 39 | 16 | 15 | 23 |
| 5083 | H116, H321, O | Sheet and Plate | 0.188 | 1.500 | 40 | 18 | 18 | 24 |
| 5083 | H116, H321, O | Plate | 1.501 | 3.000 | 39 | 17 | 17 | 24 |
| 5086 | H111, O | Extrusions | | | 35 | 14 | 13 | 21 |
| 5086 | H112, H32, H34, H116, O | Sheet and Plate | | | 35 | 14 | 14 | 21 |
| 5154 | H38 | Sheet | | | 30 | 11 | 11 | 19 |
| 5454 | H111, O | Extrusions | | | 31 | 12 | 11 | 19 |
| 5454 | H112 | Extrusions | | | 31 | 12 | 12 | 19 |
| 5454 | H32, H34, O | Sheet and Plate | | | 31 | 12 | 12 | 19 |
| 5456 | H116, H321, O | Sheet and Plate | 0.188 | 1.500 | 42 | 19 | 18 | 25 |
| 5456 | H116, H321, O | Plate | 1.501 | 3.000 | 41 | 18 | 17 | 25 |
| 6005 | T5 | Extrusions | | | 24 | 13 | 13 | 15 |
| 6061 | T6, T651, T6510, T6511(2) | All | | | 24 | 15 | 15 | 15 |
| 6061 | T6, T651, T6510, T6511(3) | All | 0.375 | | 24 | 11 | 11 | 15 |
| 6063 | T5, T52, T6 | All | | | 17 | 8 | 8 | 11 |
| 6351 | T5, T6(2) | Extrusions | | | 24 | 15 | 15 | 15 |
| 6351 | T5, T6(3) | Extrusions | 0.375 | | 24 | 11 | 11 | 15 |
| 6463 | T6 | Extrusions | 0.125 | 0.500 | 17 | 8 | 8 | 11 |
| 7005 | T53 | Extrusions | | 0.750 | 40 | 24 | 24 | 22 |

Notes

(1) Yield strengths are based on a 2 in. gauge length.

(2) Values when welded with 5183, 5356, or 5556 filler, regardless of thickness, and to thicknesses ≤ 0.375 in., when welded with 4043, 5554, or 5654 filler.

(3) Values when welded with 4043, 5554, or 5654 filler.

6. Appendix: Cutsheets

Bearings for Yaw Shaft and Wheels / Pulley Mechanisms

All Categories > Extra Thin Metric Series Bearings > Flanged Shielded Extra Thin Metric Ball Bearings > Item # F6910ZZ

Item # F6910ZZ, 1.9685 Inch (in) Bore Diameter (d) Flanged Shielded Extra Thin Metric Ball Bearing

[Request Information](#)

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All bearings are available in 52100 Chrome Steel or 440 Stainless Steel.
Bearings also available with single shield or seal : suffix Z, RS, RU.

[Specifications](#) | [Ball Complement](#)

Specifications

| Bearing Type | Extra Thin Metric Bearing |
|-----------------------------------|---------------------------|
| Bore Diameter (d) | 50 mm 1.9685 in |
| Outer Diameter (D) | 72 mm 2.8346 in |
| Flange Diameter (D _f) | 75.0 mm 2.9528 in |
| Min. Radius (r _s) | 0.60 mm 0.0235 in |
| Width (B) | 12.0 mm 0.4724 in |
| Flange Width (B _f) | 2.5 mm 0.0984 in |
| Load Rating (Cr) | 14540 N |
| Load Rating (Cor) | 11710 N |

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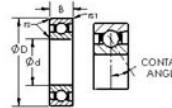
Home > Bearings Catalog > Ball Bearings > Angular Contact Ball Bearings > 71900C

71900C Angular Contact Ball Bearing
Model: **71900C**

[Request Quote](#) Quantity 1 [Send RFQ to AST](#)

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[View 3D Model](#) [View Spec Sheet](#)



1. 15 degree contact angle, relieved outer ring
2. Also available with metal shields (ZZ) or rubber seals (2RS)
3. The desired preload must be specified.

Product Details

| Specifications | | | Documentation | | |
|--------------------------------|----------------------|-----|----------------------|---------------------------------------|-------------------------------|
| Bearing Type | 15 deg contact angle | | General | Nomenclature | Material |
| Bore Dia (d) | 10.000 | mm | Cages and Retainers | Tolerances and Precision | Lubrication |
| Outer Dia (D) | 22.000 | mm | Fitting and Mounting | Load and Life Calculation Information | eDrawings file (.ePRT, .eASM) |
| Width (B) | 6.000 | mm | | | |
| Radius (min) (r _s) | 0.30 | mm | | | |
| Dynamic Load Rating (Cr) | 2,900 | N | | | |
| Static Load Rating (Cor) | 1,800 | N | | | |
| Max Speed (Grease) | 70,000 | rpm | | | |
| Max Speed (Oil) | 110,000 | rpm | | | |

6. Appendix: Cutsheets

Bearings for Yaw Shaft Axial Loading

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Home > Bearings > Roller Bearings > Roller-Thrust Bearings > Needle Roller Thrust Bearings > NTA-5266

Koyo.

Koyo NRB NTA-5266 **\$36.99 each**

Needle Roller Thrust Bearing - 3-1/4 in Bore, 4-1/8 in OD, 1/8 in Width **IN STOCK**

Mi Item #: 00094529

Quantity



 0 Reviews - Be the first to review this item. 

 Print |  Share

Please Note: Photo may not represent actual item, please refer to title and product specifications for all details.

Product Content Feedback

Specifications

| | | | |
|-----------------------|------------------------|------------------------|----------|
| Bore diameter: | 3-1/4 in | Dynamic load capacity: | 51.6 kN |
| Outside diameter: | 4-1/8 in | Cage material: | Steel |
| Bearing width: | 1/8 in | Maximum rpm: | 4000 RPM |
| Thrust bearing type: | Roller & Cage Assembly | Compatible washer: | TRA-5266 |
| Bearing material: | Steel | Series: | NTA |
| Static load capacity: | 294.9 kN | | |

6. Appendix: Cutsheets

Timing Belt Pulley

L TIMING BELTS • 3/8" OR 9.525 mm PITCH

SDPSI

BELT WIDTHS
INCH - 1/2, 3/4 & 1 in.
METRIC - 12.5, 19 & 25.4 mm

► MATERIAL:
Nylon Covered, Fiberglass Reinforced, Neoprene

► SPECIFICATIONS:
Breaking Strength:
125 lbf per 1/8 in. (175 N per 1 mm) Belt Width; not representative of the load-carrying capacity of the belt.
Temperature Range:
-30°F to +185°F (-34°C to +85°C)

► MODIFICATIONS:
Special Widths - cut to size from sleeves available from stock.

Pulleys are available with inch or metric standards.

INCH COMPONENT CATALOG NUMBER

| | | | | |
|----------------|------|-------|------|-----|
| A | 6R | 4 | □□□□ | □□□ |
| No. of Grooves | Code | Width | | |
| 1/2 | 699 | 699 | | |
| 3/4 | 675 | 675 | | |
| 1 | 100 | 100 | | |

METRIC COMPONENT CATALOG NUMBER

| | | | | |
|----------------|------|-------|------|-----|
| A | 6R | 4M | □□□□ | □□□ |
| No. of Grooves | Code | Width | | |
| 11.5 | 111 | 111 | | |
| 19 | 199 | 199 | | |
| 25.4 | 254 | 254 | | |

0 .020 R (0.5 R) TYP. 128 (3.25) .375 (9.525) .075 (1.9) 40°

NOTE: Dimensions in () are mm.

Continued on the next page

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L TIMING BELTS • 3/8" OR 9.525 mm PITCH

SDPSI

BELT WIDTHS
INCH - 1/2, 3/4 & 1 in.
METRIC - 12.5, 19 & 25.4 mm

► MATERIAL:
Nylon Covered, Fiberglass Reinforced, Neoprene

► SPECIFICATIONS:
Breaking Strength:
125 lbf per 1/8 in. (175 N per 1 mm) Belt Width; not representative of the load-carrying capacity of the belt.
Temperature Range:
-30°F to +185°F (-34°C to +85°C)

► MODIFICATIONS:
Special Widths - cut to size from sleeves available from stock.

Pulleys are available with inch or metric standards.

INCH Component Catalog Number

| | | |
|-------------|--------------|--------|
| Groove Code | Pitch Length | |
| Inch | mm | |
| 026 | 9.750 | 247.65 |
| 027 | 12.000 | 304.80 |
| 033 | 12.875 | 324.33 |
| 035 | 13.125 | 333.38 |
| 036 | 13.500 | 342.9 |
| 038 | 14.000 | 355.6 |
| 040 | 15.000 | 381 |
| 041 | 15.375 | 390.53 |
| 042 | 15.750 | 400.05 |
| 044 | 16.000 | 406.4 |
| 045 | 16.875 | 428.63 |
| 046 | 17.250 | 438.15 |
| 047 | 17.625 | 448.67 |
| 048 | 18.000 | 476.25 |
| 052 | 19.500 | 495.3 |
| 053 | 19.875 | 504.83 |
| 054 | 20.250 | 513.5 |
| 055 | 20.625 | 523.68 |
| 056 | 21.000 | 533.4 |
| 058 | 21.750 | 552.45 |
| 060 | 22.500 | 571 |
| 062 | 23.250 | 590.55 |
| 063 | 23.625 | 600.08 |
| 064 | 24.000 | 609.6 |
| 065 | 24.375 | 619.13 |
| 066 | 24.750 | 628.65 |
| 067 | 25.125 | 638.05 |
| 068 | 25.500 | 647.7 |

Metric Component Catalog Number

| | | |
|-------------|--------------|---------|
| Groove Code | Pitch Length | |
| mm | mm | |
| 060 | 25.875 | 657.23 |
| 072 | 27.000 | 685.6 |
| 074 | 27.750 | 704.85 |
| 076 | 28.500 | 723.9 |
| 080 | 29.000 | 736.6 |
| 081 | 30.375 | 771.53 |
| 082 | 30.750 | 781.05 |
| 084 | 31.500 | 800.1 |
| 085 | 31.875 | 810.63 |
| 086 | 32.250 | 819.15 |
| 089 | 33.375 | 847.73 |
| 090 | 33.750 | 857.25 |
| 092 | 34.000 | 866.5 |
| 094 | 35.250 | 895.35 |
| 095 | 36.000 | 914.4 |
| 096 | 36.750 | 933.5 |
| 100 | 37.500 | 952.5 |
| 104 | 39.000 | 990.6 |
| 105 | 39.275 | 1000.13 |
| 106 | 40.000 | 1019.2 |
| 112 | 42.000 | 1066.8 |
| 114 | 42.750 | 1085.85 |
| 116 | 43.500 | 1104.5 |
| 118 | 44.250 | 1123.43 |
| 119 | 44.625 | 1133.48 |
| 120 | 45.000 | 1143.48 |
| 123 | 46.125 | 1171.58 |

0 .020 R (0.5 R) TYP. 128 (3.25) .375 (9.525) .075 (1.9) 40°

NOTE: Dimensions in () are mm.

6. Appendix: Cutsheets

Pulley - Attached to Motor

GT® 2 / GT® 3 TIMING BELT PULLEYS • 5 mm PITCH

SDPSI

FOR 15 mm BELTS
FOR USE WITH GT®2 and GT®3 BELTS
DOUBLE FLANGE
TRUE METRIC PROFILE

PHONE: 516.329.3300 • FAX: 516.326.8827 • WWW.SDPSI.COM

Metric
0 10

> MATERIAL: Aluminum Alloy
> FINISH: Clear Anodized
> SPECIFICATIONS:
D Tolerance: 12 to 16 grooves is +0.050
17 to 32 grooves is +0.100
34 grooves is +0.150
Pulleys with 12 and 13 grooves have 1 set screw; others have 2 set screws at 90°

METRIC COMPONENT

| Catalog Number | No. of Grooves | P.D. | D Dia. ± 0.4 | D ₁ Dia. ± 0.4 | d Bore ± 0.025 | L Length ± 0.4 | D ₂ Hub Dia. ± 0.4 | I Hub Proj. ± 0.4 | A Set Screw |
|------------------|----------------|-------|---------------------|----------------------------------|-----------------------|-----------------------|--------------------------------------|--------------------------|-------------|
| A 6ASMM012DF1506 | 12 | 19.1 | 17.96 | 22.2 | 6 | 26.2 | 11.1 | 6.4 | 3.2 M3 |
| A 6ASMM013DF1506 | 13 | 20.7 | 19.56 | 23.8 | 6 | 26.2 | 12.7 | 6.4 | 3.2 M3 |
| A 6ASMM014DF1506 | 14 | 22.68 | 21.13 | 24.4 | 6 | 26.2 | 14.2 | 6.4 | 3.2 M3 |
| A 6ASMM015DF1506 | 15 | 24.68 | 22.13 | 25.9 | 6 | 26.2 | 15.8 | 6.4 | 3.2 M3 |
| A 6ASMM016DF1506 | 16 | 25.48 | 24.33 | 27.8 | 6 | 26.2 | 14.2 | 6.4 | 3.2 M3 |
| A 6ASMM017DF1506 | 17 | 27.05 | 25.91 | 30.2 | 6 | 26.2 | 15.9 | 6.4 | 3.2 M3 |
| A 6ASMM018DF1506 | 18 | 28.65 | 27.51 | 31.8 | 6 | 26.2 | 17.5 | 6.4 | 3.2 M3 |
| A 6ASMM019DF1506 | 19 | 30.25 | 29.45 | 33.4 | 6 | 26.2 | 19.1 | 6.4 | 3.2 M3 |
| A 6ASMM020DF1506 | 20 | 31.83 | 30.68 | 34.9 | 6 | 26.2 | 20.6 | 6.4 | 3.2 M3 |
| A 6ASMM021DF1506 | 22 | 35.03 | 33.88 | 38.1 | 6 | 26.2 | 23.8 | 6.4 | 4.8 M5 |
| A 6ASMM022DF1506 | 24 | 38.7 | 37.45 | 43 | 10 | 26.2 | 26.2 | 6.4 | 4.8 M5 |
| A 6ASMM023DF1506 | 25 | 41.78 | 40.63 | 45.9 | 10 | 26.2 | 28.8 | 6.4 | 4.8 M5 |
| A 6ASMM024DF1510 | 26 | 41.38 | 40.23 | 44.5 | 10 | 37.5 | 27 | 9.5 | 6.4 M6 |
| A 6ASMM025DF1512 | 28 | 44.95 | 43.41 | 47.6 | 12 | 37.5 | 30.2 | 12.7 | 6.4 M6 |
| A 6ASMM026DF1512 | 30 | 48.52 | 46.97 | 50 | 12 | 37.5 | 32.5 | 12.7 | 6.4 M6 |
| A 6ASMM027DF1512 | 32 | 50.93 | 49.79 | 54 | 12 | 37.5 | 31.8 | 12.7 | 6.4 M6 |
| A 6ASMM028DF1512 | 34 | 54.1 | 52.96 | 57.2 | 12 | 37.5 | 35 | 12.7 | 6.4 M6 |

REV: 02.20.15 JC

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METRIC COMPONENT

| Catalog Number | No. of Grooves | P.D. | D Dia. ± 0.4 | D ₁ Dia. ± 0.4 | d Bore $+0.025$ 0 | L Length ± 0.4 | D ₂ Hub Dia. ± 0.4 | I Hub Proj. ± 0.4 | A | Set Screw |
|-------------------------|----------------|-------|---------------------|----------------------------------|-------------------------|-----------------------|--------------------------------------|--------------------------|------|-----------|
| A 6A55M012DF1506 | 12 | 19.1 | 17.96 | 22.2 | 6 | 26.2 | 26.2 | 11.1 | 6.4 | 3.2 M3 |
| A 6A55M013DF1506 | 13 | 20.7 | 19.56 | 23.8 | 6 | 26.2 | 26.2 | 12.7 | 6.4 | 3.2 M3 |
| A 6A55M014DF1506 | 14 | 22.68 | 21.13 | 24.4 | 6 | 26.2 | 26.2 | 14.2 | 6.4 | 3.2 M3 |
| A 6A55M015DF1506 | 15 | 24.68 | 22.13 | 25.9 | 6 | 26.2 | 26.2 | 15.9 | 6.4 | 3.2 M3 |
| A 6A55M016DF1506 | 16 | 25.48 | 24.33 | 27.8 | 6 | 26.2 | 26.2 | 17.5 | 6.4 | 3.2 M3 |
| A 6A55M017DF1506 | 17 | 27.05 | 25.91 | 30.2 | 6 | 26.2 | 26.2 | 19.1 | 6.4 | 3.2 M3 |
| A 6A55M018DF1506 | 18 | 28.65 | 27.51 | 31.8 | 6 | 26.2 | 26.2 | 20.6 | 6.4 | 3.2 M3 |
| A 6A55M019DF1506 | 19 | 30.25 | 29.45 | 33.4 | 6 | 26.2 | 26.2 | 22.2 | 6.4 | 3.2 M3 |
| A 6A55M020DF1506 | 20 | 31.83 | 30.68 | 34.9 | 6 | 26.2 | 26.2 | 23.8 | 6.4 | 3.2 M3 |
| A 6A55M022DF1506 | 22 | 35.03 | 33.88 | 38.1 | 6 | 26.2 | 26.2 | 25.4 | 6.4 | 4.8 M5 |
| A 6A55M024DF1510 | 24 | 38.7 | 37.45 | 43 | 10 | 26.2 | 29.4 | 25.4 | 9.5 | 4.8 M5 |
| A 6A55M025DF1510 | 25 | 41.78 | 40.63 | 45.9 | 10 | 26.2 | 29.4 | 25.4 | 9.5 | 4.8 M5 |
| A 6A55M026DF1510 | 26 | 41.38 | 40.23 | 44.5 | 10 | 37.5 | 27 | 25.4 | 9.5 | 6.4 M6 |
| A 6A55M028DF1512 | 28 | 44.95 | 43.41 | 47.6 | 12 | 37.5 | 32.5 | 30.2 | 12.7 | 6.4 M6 |
| A 6A55M030DF1512 | 30 | 47.5 | 46.61 | 50.8 | 12 | 37.5 | 32.5 | 30.2 | 12.7 | 6.4 M6 |
| A 6A55M032DF1512 | 32 | 50.93 | 49.79 | 54 | 12 | 37.5 | 32.5 | 31.8 | 12.7 | 6.4 M6 |
| A 6A55M034DF1512 | 34 | 54.1 | 52.96 | 57.2 | 12 | 37.5 | 35 | 32.5 | 12.7 | 6.4 M6 |

Contact Us



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SwerveRoboticSystems.github.io