S^3 : The unit quaternion numbers

North

w

S^3

$q = \mathbf{q} + w$

θ

$\|\mathbf{q}\| = \sin(\theta)$

$\mathbf{q}$

$-q$

South