S^3 : The unit quaternion numbers North w \mathcal{E} S^3 $\mathcal{Y} = \mathcal{X} \boxplus \mathcal{X}_{\tau}$ $\mathcal{Y} = \mathcal{X} \oplus \mathcal{X}_{\tau}$ South