

Space frame		Transformation			Body frame	
Vector (Cartesian space)	Lie algebra (Tangent space)	from {b} to {s}	Adjoint matrix	from {s} to {b}	Lie algebra (Tangent space)	Vector (Cartesian space)
Spatial angular velocity ω_s	$\dot{\mathbf{R}}\mathbf{R}^{-1} = [\omega_s \times]$ $\dot{\mathbf{R}} = [\omega_s \times] \mathbf{R}$ $\mathbf{R} = \exp([\omega_s \times] \cdot \Delta t)$	$[\omega_s \times] = \mathbf{R} [\omega_b \times] \mathbf{R}^{-1}$ $= [(\mathbf{R}\omega_b) \times]$ $\omega_s = \mathbf{R}\omega_b$	$[\text{Ad}_{\mathbf{R}}] = \mathbf{R}$ $\omega_s = \mathbf{R}\omega_b$ $[\text{Ad}_{\mathbf{R}^{-1}}] = \mathbf{R}^{-1}$ $\omega_b = \mathbf{R}^{-1}\omega_s$	$[\omega_b \times] = \mathbf{R}^{-1} [\omega_s \times] \mathbf{R}$ $= [(\mathbf{R}^{-1}\omega_s) \times]$ $\omega_b = \mathbf{R}^{-1}\omega_s$	$\mathbf{R}^{-1}\dot{\mathbf{R}} = [\omega_b \times]$ $\dot{\mathbf{R}} = \mathbf{R} [\omega_b \times]$ $\mathbf{R}^{-1} = \exp([\omega_b \times] \cdot \Delta t)$	Body angular velocity ω_b
Spatial velocity $\mathcal{V}_s = \begin{bmatrix} \omega_s \\ \mathbf{v}_s \end{bmatrix}$	$\dot{\mathbf{T}}\mathbf{T}^{-1} = [\mathcal{V}_s^\wedge]$ $= \left[\begin{array}{c c} [\omega_s \times] & \mathbf{v}_s \\ \hline \mathbf{0}^T & 0 \end{array} \right]$ $\dot{\mathbf{T}} = [\mathcal{V}_s^\wedge] \mathbf{T}$ $\mathbf{T} = \exp([\mathcal{V}_s^\wedge] \cdot \Delta t)$	$[\mathcal{V}_s^\wedge] = \mathbf{T} [\mathcal{V}_b^\wedge] \mathbf{T}^{-1}$ $\mathcal{V}_s = [\text{Ad}_{\mathbf{T}}] \mathcal{V}_b$	$[\text{Ad}_{\mathbf{T}}] = \begin{bmatrix} \mathbf{R} & \mathbf{0} \\ [\mathbf{r} \times] \mathbf{R} & \mathbf{R} \end{bmatrix}$ $\mathcal{V}_s = [\text{Ad}_{\mathbf{T}}] \mathcal{V}_b$ $[\text{Ad}_{\mathbf{T}^{-1}}] = \begin{bmatrix} \mathbf{R}^{-1} & \mathbf{0} \\ -\mathbf{R}^{-1} [\mathbf{r} \times] & \mathbf{R}^{-1} \end{bmatrix}$ $\mathcal{V}_b = [\text{Ad}_{\mathbf{T}^{-1}}] \mathcal{V}_s$	$[\mathcal{V}_b^\wedge] = \mathbf{T}^{-1} [\mathcal{V}_s^\wedge] \mathbf{T}$ $\mathcal{V}_b = [\text{Ad}_{\mathbf{T}^{-1}}] \mathcal{V}_s$	$\mathbf{T}^{-1}\dot{\mathbf{T}} = [\mathcal{V}_b^\wedge]$ $= \left[\begin{array}{c c} [\omega_b \times] & \mathbf{v}_b \\ \hline \mathbf{0}^T & 0 \end{array} \right]$ $\dot{\mathbf{T}} = \mathbf{T} [\mathcal{V}_b^\wedge]$ $\mathbf{T}^{-1} = \exp([\mathcal{V}_b^\wedge] \cdot \Delta t)$	Body velocity $\mathcal{V}_b = \begin{bmatrix} \omega_b \\ \mathbf{v}_b \end{bmatrix}$