\mathbf{S}^3 : The unit quaternion numbers North w1 S^3 $\mathbf{q} + w$ θ $\|\mathbf{q}\| = \sin\left(\theta\right)$ South