

Introduction to Quantitative Reasoning of GRE

GRE 数学小白必看

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GRE 冲分班数学
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Presentation Overview

① Score Goal

A Quick Survey About Your Intended Graduate Major
The Score Goal For Your Intended Graduate Major

② Test Format

Test Day Experience
Computer-Adaptive Test
Scoring
Question Types
How to Use the On-screen Calculator

Score Goal

A Quick Survey About Your Intended Graduate Major

What is Your Intended Graduate Major

不同专业，GRE 数学分数要求不同

- ① Computer Science, Electronic Engineering, Data Science, Finance, Physics, Chemistry, Biology, Statistics, Applied Mathematics, Management Business Analytics, Psychology(PhD.), Economics and other Engineering, Science or PhD. programs
- ② Linguistic, Psychology(Master), Education(Master), Architecture, Philosophy, Gender Studies, East Asian Studies, Marketing, and Business
- ③ Others: State your Graduate Major

The Score Goal For Your Intended Graduate Major

Admission Statistics

Mathematics of Finance (MA), Columbia University

Test scores are now optional, but still, approximately 87% of the Fall 2021 entering class submitted GRE scores.
—<https://www.math.columbia.edu/mafn/admissions/admissions-statistics/>

| GRE Quantitative Score | 2019 | 2020 | 2021 |
|-------------------------------|-------------|-------------|-------------|
| Mean | 169.1 | 169.5 | 169.17 |
| Median | 160.0 | 160.7 | 161.9 |

表: The median and average GRE QR score for the entering class of 2019, 2020 and 2021 in Mathematics of Finance MA Program of Columbia University

QR Score Goal

分数够用就行

| Your Response | Score Goal | Comments |
|---------------|------------|---|
| 1 | 169-170 | Your study is heavily dependent on Math |
| 2 | 165-170 | Your study is weakly dependent on Math |

表: Suggested Quantitative Reasoning score goal

QR Scores below the lower bound may dent your application.

Test Format

Test Day Experience

Test Day Experience

20 道题/35mins, 屏幕阅读



图: GRE Home Test

大陆考场: 9:30 封闭考场, 10 点左右开始考试, 13:40 左右结束

国外考场: 上午场和下午场可选

家考 (Recommended): 7 天/24h 可选, 安检 30 分钟, 自己设备, 印度考官

Computer-Adaptive Test

Unscored Section

第 1 个 section 往往是 routing section

可以预测加试科目，但是无法预测具体第 2 或者第 3 个 Section 是加试

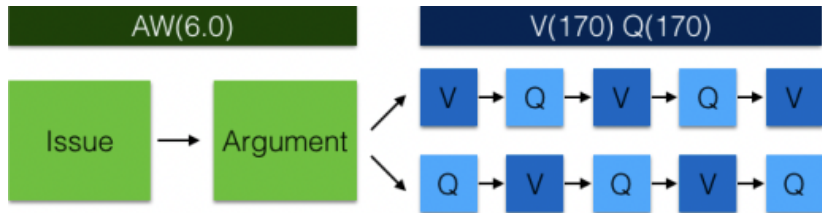
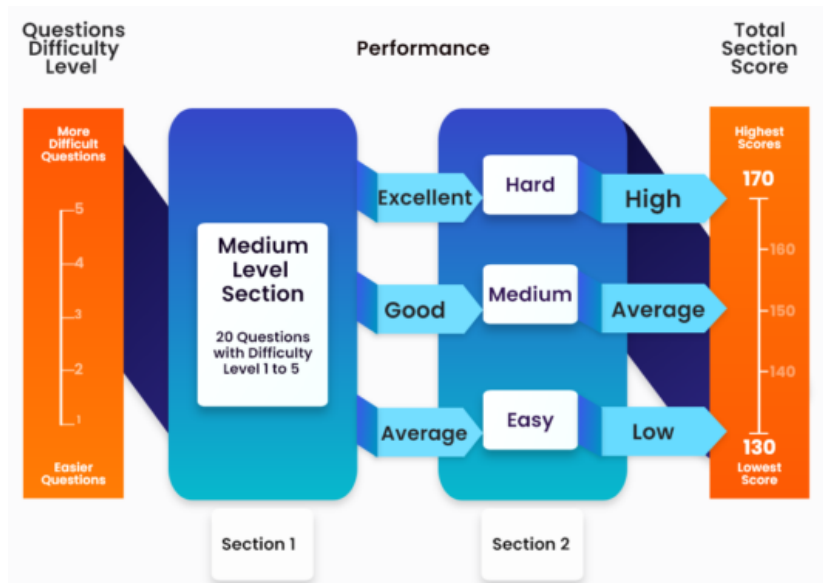


图: Possible Routes

Computer-Adaptive Test: Section-Level Adaption



Scoring

Diagnostic Report 诊断报告

正常 15 天出分，出分后 3 天出诊断报告

First Section

Arithmetic

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|---|-----------|-------------|------------------|------------|
| 1 | Quantitative Comparison | Pure math | Right | 1 | 01:36 |
| 2 | Multiple-choice-Select One or More | Real-life | Right | 2 | 04:01 |
| 3 | Quantitative Comparison | Pure math | Right | 3 | 01:44 |
| 4 | Multiple-choice-Select One | Pure math | Right | 3 | 00:37 |

Algebra

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|---------------------------------------|-----------|-------------|------------------|------------|
| 1 | Quantitative Comparison | Pure math | Right | 2 | 00:58 |
| 2 | Multiple-choice-Select One | Real-life | Right | 3 | 01:00 |
| 3 | Quantitative Comparison | Pure math | Right | 3 | 01:22 |
| 4 | Multiple-choice-Select One | Pure math | Right | 4 | 03:09 |

Geometry

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|-------------------------|-----------|-------------|------------------|------------|
| 1 | Quantitative Comparison | Pure math | Right | 2 | 00:56 |
| 2 | Quantitative Comparison | Pure math | Right | 2 | 02:01 |
| 3 | Numeric Entry | Pure math | Right | 4 | 01:06 |
| 4 | Numeric Entry | Real-life | Right | 4 | 03:02 |

Diagnostic Report 诊断报告

Data Analysis 用时更多

Data Analysis

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|--------------------|---------------------------------------|-----------|-------------|------------------|------------|
| Discrete Questions | | | | | |
| 1 | Quantitative Comparison | Pure math | Right | 2 | 01:10 |
| 2 | Multiple-choice—Select One | Real-life | Right | 3 | 02:02 |
| 3 | Multiple-choice—Select One | Pure math | Right | 3 | 01:09 |
| 4 | Quantitative Comparison | Real-life | Right | 3 | 01:17 |
| 5 | Multiple-choice—Select One | Pure math | Right | 4 | 00:48 |
| Set Members | | | | | |
| 6 | Multiple-choice—Select One | Real-life | Right | 2 | 02:02 |
| 7 | Multiple-choice—Select One | Real-life | Right | 4 | 02:18 |
| 8 | Numeric Entry | Real-life | Right | 5 | 02:33 |

Diagnostic Report 诊断报告

Section 2 的题目更难

Second Section

Arithmetic

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|---|-----------|-------------|------------------|------------|
| 1 | Quantitative Comparison | Pure math | Right | 3 | 01:35 |
| 2 | Multiple-choice—Select One | Pure math | Right | 4 | 00:31 |
| 3 | Multiple-choice—Select One | Pure math | Right | 4 | 01:42 |
| 4 | Numeric Entry | Pure math | Right | 5 | 01:55 |
| 5 | Multiple-choice—Select One or More | Pure math | Wrong | 5 | 05:11 |

Algebra

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|---------------------------------------|-----------|-------------|------------------|------------|
| 1 | Multiple-choice—Select One | Real-life | Right | 4 | 01:28 |
| 2 | Quantitative Comparison | Pure math | Right | 4 | 02:10 |
| 3 | Quantitative Comparison | Pure math | Right | 4 | 01:05 |
| 4 | Quantitative Comparison | Pure math | Right | 4 | 00:28 |

Geometry

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|-------------|---------------------------------------|-----------|-------------|------------------|------------|
| 1 | Quantitative Comparison | Pure math | Right | 3 | 02:21 |
| 2 | Quantitative Comparison | Pure math | Right | 4 | 00:39 |
| 3 | Multiple-choice—Select One | Pure math | Right | 4 | 00:55 |
| 4 | Multiple-choice—Select One | Pure math | Right | 4 | 01:48 |

Diagnostic Report 诊断报告

不定项选择题最容易错

Data Analysis

| Reference # | Question Type | Setting | Right/Wrong | Difficulty Level | Time Spent |
|--------------------|---|-----------------------|-------------|------------------|------------|
| Discrete Questions | | | | | |
| 1 | Quantitative Comparison | Real- Life | Right | 2 | 00:38 |
| 2 | Multiple-choice—Select One | Real- Life | Right | 4 | 01:42 |
| 3 | Multiple-choice—Select One | Real- Life | Right | 4 | 02:56 |
| 4 | Multiple-choice—Select One or More | Real- Life | Wrong | 5 | 01:53 |
| Set Members | | | | | |
| 5 | Multiple-choice—Select One | Real- Life | Right | 1 | 01:13 |
| 6 | Multiple-choice—Select One | Real- Life | Right | 4 | 02:32 |
| 7 | Multiple-choice—Select One | Real- Life | Right | 5 | 02:09 |

Predict Your Score

第二个 section 错题和分数的关系: 错 1-2 个 170/169

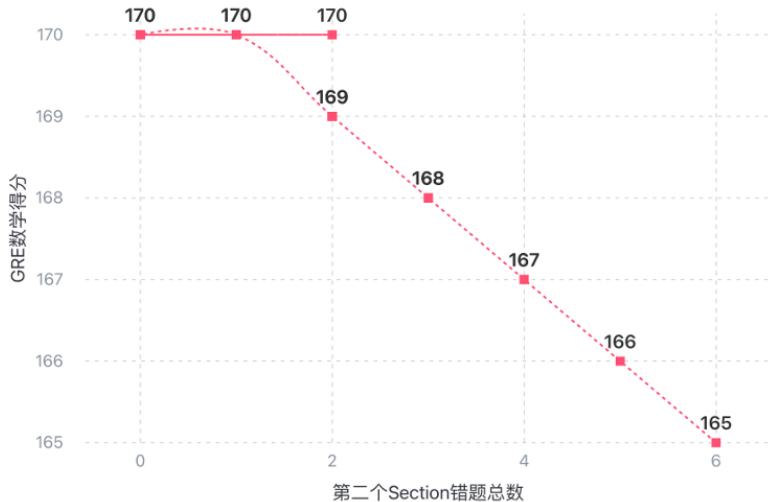


图: Regression between the number of incorrect question of the 2nd section and

Question Types

Quantitative Comparison 比大小

选项固定，带入数，估算，化简

GRE 重点Section6-medium

CalcReviewMarkHelpBackNext

Question 1 of 2000:01:44 Hide Time

Quantity A

$$13\frac{2}{13}$$

Quantity B

$$13\frac{3}{26}$$

☐ Quantity A is greater.

☐ Quantity B is greater.

☐ The two quantities are equal.

☐ The relationship cannot be determined from the information given.

Select one answer choice.

calculator

0

| | | | | |
|----|----|----|---|----|
| MR | MC | M+ | (|) |
| 7 | 8 | 9 | + | C |
| 4 | 5 | 6 | x | CE |
| 1 | 2 | 3 | - | √ |
| ± | 0 | . | + | = |

Transfer Display

Multiple-choice—Select One 单选

如果要近似，选项间隔小，一定要用计算器精确计算，最后一步再化简

GRE 重点Section6-medium

CalcReviewMarkHelpBackNext

Question 9 of 2000:05:48 Hide Time

Working alone at their respective constant rates, machine R processes one ton of ore in 4.5 hours, and machine S processes one ton of ore in 6.7 hours. Which of the following is closest to the number of hour that it would take both machines, working simultaneously at their respective constant rates, to process one ton of ore?

☐ 2.4

☐ 2.5

☐ 2.6

☐ 2.7

☐ 2.8

Select one answer choice.

Multiple-choice Questions—Select One or More Answer Choices 选一个或者多个，最后一题难度为 5

GRE 重点Section6-hard

CalcReviewMarkHelpBackNext

Question 20 of 2000:00:13 Hide Time

If $a > 1$, which of the following could be the value of $\left(1 + \frac{1}{a}\right)^{-1}$?
Indicate all such values.

☐ 0.35
☐ 0.42
☐ 0.57
☐ 0.75
☐ 0.98
☐ 1.06

Select one or more answer choice.

Numeric Entry Questions 数字填空题

注意单位；近似精度；Transfer Display；只能填一个整数或者分数

Section 4 of 6 | Question 17 of 20

00:34:27 ⌵ Hide Time

If $x = \sqrt{10}$, what is the value of $(5\sqrt{10} + x)^2$?

Enter your answer as an integer or a decimal in the answer box. Backspace to erase



Numeric Entry Questions 数字填空题

不用化简；分子分母分开填；

Section 6 of 6 | Question 13 of 20

00:34:35 ⌵ Hide Time

A bag contains a total of 12 bagels consisting of 5 plain bagels, 3 garlic bagels, and 4 cinnamon raisin bagels. If 2 bagels are to be selected at random from the bag without replacement, what is the probability that both bagels will be garlic bagels?

Give your answer as a fraction.

| |
|--|
| |
| |

Enter your answer as a fraction, with the numerator and denominator in their respective answer boxes. Backspace to erase.

Data Interpretation Sets 数据解读题套题

多道题目对应一组数据; 可单选, 不定项, 或者填空

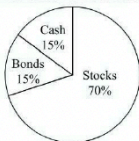
Section 6 of 6 | Question 14 of 20

00:34:33 ⌵ Hide Time

Questions 14 to 16 are based on the following data.

Assets in Mutual Fund X, January 1, 2012

Distribution of Total Assets



Total Assets: \$15 billion
(1 billion = 10^9)

Distribution of Stock Assets in Fund X

| | |
|------------------|-----|
| Foreign Stocks | 25% |
| Domestic Stocks: | |
| Technology | 15% |
| Finance | 10% |
| Utilities | 18% |
| Retail | 10% |
| Health Care | 17% |
| Other | 5% |

Approximately what was the amount of assets in domestic utilities stocks in Fund X?

- ☐ \$0.12 billion
- ☐ \$0.19 billion
- ☐ \$1.2 billion
- ☐ \$1.9 billion
- ☐ \$11.5 billion

Select one answer

How to Use the On-screen Calculator

When to Use the Calculator

For tedious calculation only

$$\begin{array}{r} 49.25 \\ 12 \overline{) 591.00} \\ \underline{48} \\ 111 \\ \underline{108} \\ 30 \\ \underline{24} \\ .60 \\ \underline{.60} \\ 0 \end{array}$$

- Long division
- Square roots
- Addition, subtraction or multiplication of numbers that have several digits

图: Long Division

When to **Not** Use the Calculator

Simple Calculations

① $10 - 490$

② 4×70

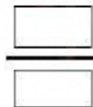
③ $\frac{4300}{10}$


④ $\sqrt{25}$

⑤ 30^2

Fraction

Avoid using it to introduce decimals if you are asked to give an answer as a fraction.



: Numeric Entry Question For a Fraction

Demo: 请打开以下网址

群内有链接，建议用电脑打开，用小键盘或者鼠标操作

https://tonypottera24.github.io/gre_calculator/web/

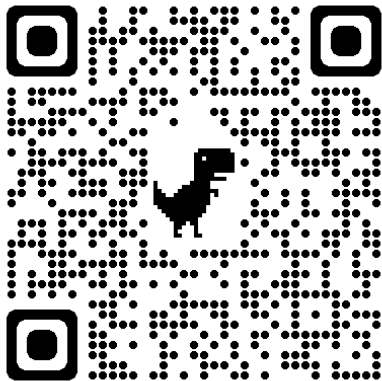


图: GRE Calculator Website

Demo: Order of Operations 运算优先级

From the Most Prioritized to Least Prioritized

- ① Parentheses
- ② Exponentiation (including square roots)
- ③ Multiplications and divisions (from left to right)
- ④ Additions and subtractions (from left to right)

Have a try!

- $1 + 2 \times 4 = 9$
- $(1 + 2) \times 4 = 12$
- $7 + (3 \times 15 - 5) \div 8 - 13 = ?$

CE: Clear Entry 清零屏幕上所有输入

C: Clear 清零之前所有输入

Demo: Memory Buttons

Buttons

- ① **MR**:
Memory
Recall
- ② **MC**:
Memory
Clear
- ③ **M+**:
Memory
Plus

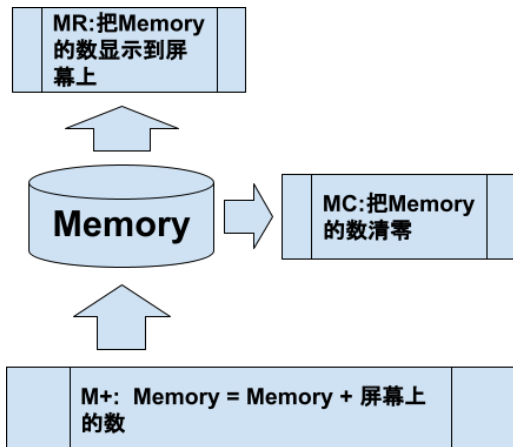


图: How **MR**, **MC**, **M+** works

Demo: Memory Buttons

Have a try!

- 1 If a car run 33 miles with 20 gallons gas, how many gallons will the car use for 1 mile? With 45 gallons of gas, how many miles can the car run?
- 2 Convert this fraction to decimal.
$$\frac{43 \times 6 + 21 \times 80 + 16 \times 100}{43 + 21 + 16}$$
- 3 Calculate the Standard Deviation of ages for Alice(56 years-old) and Bob(73 years-old).



图: The "M" symbol will appear on the left of the display.

Demo: the Mysterious "±"

不是加减，而是负号

"±" **dose not** suggest that the calculator will perform the plus and minus operation at the same time.
"±" suggest a negative sign is added to the number on the display.

Have a try!

- ① Compute $-\frac{8.4+9.3}{70}$:

$$\boxed{(} \boxed{8.4} \boxed{+} \boxed{9.3} \boxed{)} \boxed{\div} \boxed{70} \boxed{=} \boxed{\pm}$$

- ② Compute $(-15)^3$:

$$\boxed{15} \boxed{\times} \boxed{15} \boxed{\times} \boxed{15} \boxed{=} \boxed{\pm}$$

Demo: The Square root

先得出数字，然后按 $\sqrt{}$

Find the length, to the nearest 0.01, of the hypotenuse of a right triangle with legs of length 21 and 54;

Compute $\sqrt{21^2 + 54^2}$:

$$21 \boxed{\times} 21 \boxed{+} 54 \boxed{\times} 54 \boxed{=} \boxed{\sqrt{}}$$

Demo: Deal with Error

按 **C**；减小运算位数



图: The error on the display

Why do you got an error?

- Undefined Behaviors For Real Numbers
 - Divided by zero:
 $6 \div 0 = \text{Error}$
 - The Square root of a negative:
 $7 \pm \sqrt{} = \text{Error}$
- The 8-Digits Limit
 - 99,999,999 is the maximum allowable number:
 $10000000 \times 10 = \text{Error}$
 - 0.0,000,001 is the minimum positive number:
 $0.0000001 \div 10 = 0.$

Incomplete brackets will not cause an error. $1 + (10 = 11$

Use the Calculator

To purchase a new sweater, Kledia paid \$51.41, which was the sum of the selling price plus 6 percent sales tax on the selling price. How much was the sales tax?

- ☐ \$1.41
- ☐ \$1.95
- ☐ \$2.41
- ☐ \$2.91
- ☐ \$3.08

Use the Calculator

To purchase a new sweater, Kledia paid \$51.41, which was the sum of the selling price plus 6 percent sales tax on the selling price. How much was the sales tax?

- ☐ \$1.41
- ☐ \$1.95
- ☐ \$2.41
- ☐ \$2.91
- ☐ \$3.08

$$51.41 \div (1 + 0.06) \times 0.06 = 2.91 \text{ D}$$

Don't Use the Calculator!

How much more is 20 percent of x than $\frac{1}{5}$ of 1 percent of x ?

☐ $\frac{x}{19.8}$

☐ $0.18x$

☐ $0.192x$

☐ $0.198x$

☐ $19.8x$

Don't Use the Calculator!

How much more is 20 percent of x than $\frac{1}{5}$ of 1 percent of x ?

☐ $\frac{x}{19.8}$

☐ $0.18x$

☐ $0.192x$

☐ $0.198x$

☐ $19.8x$

$$0.2 - 0.2 \times 0.01 = 0.198 \quad \text{D}$$

- ① Arithmetic 算术
- ② Algebra 代数
- ③ Geometry 几何
- ④ Data Analysis 数据分析

1 Min Break

Questions? Comments?