Complex Analysis Reference Sheet

Stuyvesant Class of 2022

Nate Strout, Joshua Yagupsky, Francis Zweifler

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Complex Calculus, Mr. Stern

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Definition 3.1 (Limit of a function, (ϵ, δ) definition)**.** A function $f : D \to \mathbb{C}$ is said to have a *limit* of L as $z \to a$ if $\forall \epsilon > 0, \exists \delta > 0, \forall z \in D : (0 < |z - a| < \delta \implies |f(z) - L| < \epsilon)$.