

Probability Assignment 1

Fares Ahmed

Q1. ①

delay 1 Hour = Hour

$$P(\text{Hour} | A) = 0.3$$

$$P(A) = 0.4$$

$$P(\text{Hour} | B) = 0.4$$

$$P(B) = 0.35$$

$$P(\text{Hour} | C) = 0.2$$

$$P(C) = 0.25$$

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$$P(A) * P(\text{Hour} | A) = 0.12$$

$$P(B) * P(\text{Hour} | B) = 0.14$$

$$P(C) * P(\text{Hour} | C) = 0.05$$

$$P(\text{Hour}) = 0.12 + 0.14 + 0.05 = 0.31$$

$$\textcircled{2} \quad P(B | \text{Hour}) = \frac{P(B) P(\text{Hour} | B)}{P(\text{Hour})} = \frac{0.35}{0.31} = 0.45$$

$$\textcircled{3} \quad P(C) * P(\text{Hour} | C) = 0.05$$

$$\textcircled{4} \quad P(\text{Hour}') = 1 - P(\text{Hour}) = 0.69$$

$$\textcircled{5} \quad P(\text{ontime}) = P(\text{Hour}') = 0.69$$

$$\textcircled{6} \quad 0.1 + 0.3 + 0.4 + 0.2 = 1$$

(without any negative values)

distribution is Valid

$$\textcircled{7} \quad 0 \times 0.1 = 0, 1 \times 0.3 = 0.3, 2 \times 0.4 = 0.8, 3 \times 0.2 = 0.6$$

Sum = 0 + 0.3 + 0.8 + 0.6 = 1.7 delay per hour

ملاحظات

HOTLINE

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$$\textcircled{8} \quad E(X^2) = 0^2 \times 0.1 + 1^2 \times 0.3 + 2^2 \times 0.4 + 3^2 \times 0.2 = 3.7$$

$$\text{Var}(X) = 3.7 - (1.7)^2 = 0.81$$

$$\text{SD}(X) = \sqrt{0.81} = 0.9$$



$$\textcircled{9} \quad P(X \leq 2) + P(X \leq 3) = 0.4 + 0.2 = 0.6$$

\textcircled{10}

1. expected delays per hour are 1.7 which is moderate.
2. Std. Variability around mean is also moderate.
3. Since $P(X \geq 2) < 0.6$, ~~not~~ add extra buses and more flexible drivers.

