

Method

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Methodologies to quantify Californian forest ecosystems

Summary

- Sentinel-2 derived vegetation indices can be used to correlate with above-ground forest biomass (AGB)
- LiDAR requires higher resolution than size of the crown to identify individual trees, but is commonly used to estimate biomass in forests
- workflows to calculate biomass from FIA plots (Shana) are in practice (Hudak et al., 2020)
- Landtrends (Landsat, Google Earth) can be used to study forest regeneration patterns via normalised burn ratio (NBR) over large time intervals (30 years). Data can be used to estimate regeneration capability of forest entities
- Landsat and Sentinel-2 often fails to discriminate for vegetation phenology and does reach a saturation point in dense forest where it fails to estimate biomass (150+ t/ ha)
- Forest classes are only available on request (ideally non-profit uni, time consuming process). Idea: Use Gradient nearest neighbours (GNN) so nearest plot imputes tree list (Van Kane, April 29 meeting)

Sentinel 2

Compared to Landsat multispectral bands, the Sentinel-2 multispectral bands provide two red edge bands and one NIR band with improved spatial resolution. The Sentinel 2 bands can be used to derive various vegetation indices useful for discriminating between species and estimating forest biomass (Tab. 1)

SNAP is an open source common architecture for ESA Toolboxes ideal for the exploitation of Earth Observation data (<https://step.esa.int/main/toolboxes/snap/>). SNAP provides toolboxes to derive information (e.g. vegetation indices) from Sentinel data.

Table. 1: Overview Sentinel 2 bands (Arcgis.com)

Band	Description	Wavelength..um.	Resolution..m.
1	Coastal Aerosol	0.433 - 0.453	60
2	Blue	0.458 - 0.523	10
3	Green	0.543 - 0.578	10
4	Red	0.650 - 0.680	10
5	RE1	0.698 - 0.713	20
6	RE2	0.733 - 0.748	20
7	RE3	0.773 - 0.793	20
8	NIR	0.785 - 0.900	10
8a	Narrow NIR	0.855 - 0.875	20

Band	Description	Wavelength..um.	Resolution..m.
9	Water vapour	0.935 - 0.955	60
10	SWIR-Cirrus	1.365 - 1.385	60
11	SWIR-1	1.565 - 1.655	20
12	SWIR-2	2.100 - 2.280	20

Vegetation Indices

Vegetation indices including near-infrared wavelength have weaker relationships with biomass than those including shortwave infrared wavelength, especially for forest sites with complex stand structures. The results of image transformations such as the first principal component from the PCA showed stronger relationships with biomass than individual spectral bands, somehow independent of different biophysical conditions. However, in a study area with poor soil conditions and relatively simple forest stand structure, near-infrared band or relevant vegetation indices had a strong relationship with biomass (Lu et al., 2016)

Table. 2: Vegetation Indices derived from Sentinel 2 information (after Pandit et al., 2018 & Wang et al., 2020).

Vegetation.Indices	Equations	References
NDVI	$(NIR - Red)/(NIR + Red)$	(Tucker 1979)
RGR (Red Green Ratio)	$Red665/Green560$	(Sims & Gamon 2002)
EVI (Enhanced Vegetation Index)	$2.5((NIR - R)/(NIR + 1 + 6 \cdot Red + 7.5 \cdot Blue))$	(A. Huete et al. 2002)
SR (Simple ratio)	NIR/RED	(Jordan 1969, Wicaksono et al. 2016)
PSRI (Plant Senescence Reflectance Index)	$(665 - 560)/740$	(Hill 2013; Merzlyak et al. 1999)
NDII (Normalized Difference Infrared Index)	$(842 - 1610)/(842 + 1610)$	(Hardisky et al. 1983)
RE NDVI	$842 - 740/(842 + 740)$	(Chen et al. 2007)
SAVI (Soil-Adjusted Vegetation Index)	$(NIR - R)/(NIR + Red + L) \cdot 1.5$	(Huete 1988)
DVI	$NIR - Red$	(Zhu et al. 2015)
FDI (Forest Discrimination Index)	$NIR - (Green + Red)$	(Kamal et al. 2015)
TNDVI (Transformed Normal Difference vegetation index)	$\sqrt{[(NIR - Red)/(NIR + Red) + 0.5]}$	(Castillo et al. 2017)
Red edge based		
NDVI1	$(NIR - RE1)/(NIR + RE1)$	(Kross et al. 2015)
NDVI2	$(NIR - RE2)/(NIR + RE2)$	(Gitelson & Merzlyak 1994; Kross et al. 2015)
NDVI3	$(NIR - RE3)/(NIR + RE3)$	(Sharma et al. 2015)
NDVI4	$(NIR - RE4)/(NIR + RE4)$	(Kross et al. 2015)
Clg-RE1*	$RE1 / Green - 1$	(Gitelson et al. 2003)
Clg-RE2*	$RE2 / Green - 1$	(Gitelson et al. 2003)
Clg-RE3*	$RE3 / Green - 1$	(Gitelson et al. 2003)
IRECI (Inverted Red-Edge Chlorophyll Index)**	$(RE3 - Red)/(RE1/RE2)$	(Castillo et al. 2017)
MTCI (terrestrial chlorophyll index)	$RE2 - RE1/(RE1 - Red)$	(Dash & Curran 2004)
MCARI (modified chlorophyll absorption in reflectance index)	$[(RE1 - Red) - 0.2 \cdot (RE1 - Green)] \times (RE1/Red)$	(Daughtry et al. 2000)
MSRren (Modified Simple Ratio red-edge narrow)	$[(RE4 / RE1) - 1] / \sqrt{[(RE4 / RE1) + 1]}$	(Fernandez-Manso et al. 2016)
PSSRa (pigment specific simple ratio)	$RE3 / Red$	(Blackburn, 1998)
S2REP (Sentinel-2-red-edge position)	$[705 + 35(0.5(B7 + B4)/2) - B5]/(B6 - B5)$	(Frampton et al. 2013)
RECI (Inverted Red-Edge Chlorophyll Index)	$NIR - R/(RE1/RE2)$	(Frampton et al. 2013)
Shortwave infrared based***		

Vegetation.Indices	Equations	References
MNDWI (Normalised difference water index)****	$(\text{Green} - \text{SWIR1}) / (\text{Green} + \text{SWIR1})$	(Ji et al. 2009)

1* Subtraction of NIR reciprocal reflance from from reciprocal reflectance (520 to 550 nm and 695 to 705) relates closely to total chlorophyll content (Gitelson et al., 2003).

2* IRECI had highest correlation to biomass ($r = 0.8$) in Castillo et al., 2017 (Mangrove Forest Philippines) and further improved with added elevation

3* SWIR bands are used as important indicators in forest regeneration studies (Boonprong et al., 2018). Important for vegetation mapping as a standalone (Immitzer et al., 2016). Large changes for seasonal reflectance in European forest species (Grabska et al., 2019)

4* Delineating water bodies if required (Ji et al., 2009)

Papers:

Estimating ABG in sub-tropical Nepal using Sentinel 2 (Pandit et al., 2018). Field-based AGB as a dependent variable, as well as spectral band values and spectral-derived vegetation indices as independent variables in the Random Forest (Breiman, 2001). In this algorithm, decision trees are generated to the maximum extent without pruning using a randomly-selected two thirds of the samples as training data with bootstrapping (re-sampling the data many times with replacement), which strengthens the flexibility by aggregating the prediction across individual trees to make a final prediction. The paper ranks importance of spectral band data and vegetation indices from above (Tab. 2) as a typical output of a random forest to estimate AGB ($R^2 = 0.81$ and $RMSE = 25.57 \text{ t ha}^{-1}$).

Normalised Burn Ratio

The Normalized Burn Ratio (NBR) is an index designed to highlight burnt areas in large fire zones (Lima et al. 2019) and can be derived from landsat or sentinel imagery. The formula is similar to NDVI, except that the formula combines the use of both near infrared (NIR) and shortwave infrared (SWIR) wavelengths (Fig 1). It can also be used to monitor forest disturbances such as logging activities (Shimizu et al., 2017). The formula is similar to NDVI, NBR uses the ratio between NIR and SWIR bands. A high NBR value indicates healthy vegetation while a low value indicates bare ground and recently burnt areas. Non-burnt areas are normally attributed to values close to zero.

$$\text{NBR} = (\text{NIR} - \text{SWIR}) / (\text{NIR} + \text{SWIR})$$

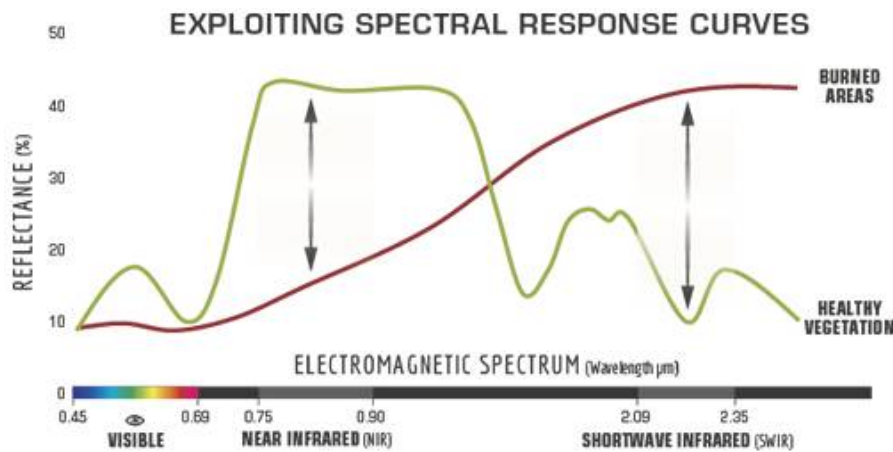


Fig: 1 Comparison of the spectral response of healthy vegetation and burned areas (USFS)

Papers:

Sentinel 2 data to create fire database in sub-Saharan Africa (Roteta et al., 2019). Sentinel-2 MSI reflectance measurements in the short and near infrared wavebands plus the active fires detected by Terra and Aqua MODIS sensor. They were able to detect smaller fires than with common MODIS approach, but Sentinel-2 based products have lower temporal resolution and consequently are more affected by cloud/cloud shadows. Available here: <https://climate.esa.int/en/projects/fire/data/>

Fire on Madeira, Spain (Navarro et al., 2017). Sentinel-2 data (5 days, 10 m resolution) for pre- and post-fire image assessments (sometimes just two). The framework can be used for the assessment of many other burnt areas globally. Enabling an extremely unprecedented perspective with a unique set of accurate, robust, timely and easily accessible information. No real measurement of accuracy provided.

Classification of burn severity for wildfire in Spain using Sentinel-2 (Fernandez-Manso et al., 2016) (with NBR). Superiority of red-edge spectral indices (particularly, Modified Simple Ratio Red-edge, Chlorophyll Index Red-edge, Normalized Difference Vegetation Index Red-edge) over conventional spectral indices. Fisher's Least Significant Difference test confirmed that Sentinel-2A MSI red-edge spectral indices are adequate to discriminate four burn severity levels.

Problems with Sentinel 2 Data

General problem with spatial resolution (30 m). The round FIA plots overlap with multiple pixels and sometimes the forest edge. Relatively new, so does not have the high temporal value as landsat. Will probably fail to distinguish tree phenology (e.g. growth stages) and can reach a spectral saturation point if biomass is

too high.

Papers: Bamboo forest in China: Seasonality, different growth phenomena in different years. Correlation between spectral bands and biomass varies within the period of months. Biomass calculation based on DBH and age (Y. Chen et al., 2019). Also used random forest to evaluate key variables.

Sentinel-2 cleaning

The Sen2Cor atmospheric correction processor (version 2.5.5) was used to conduct atmospheric correction. The Sen2Cor processor was developed for formatting and generating Sentinel-2 Level-2A products. The processor is freely available from the European Space Agency website (<http://step.esa.int/main/third-party-plugins-2/sen2cor/>). Resampled the Level-2A images to a 10 m spatial resolution utilizing the nearest neighbor algorithm, while Bands 1, 9, and 10 were discarded because they were dedicated for atmospheric correction and had coarse resolutions of 60 m. Afterwards, the images were co-registered to the LiDAR point clouds with an accuracy of less than 0.5 pixels. (Wang et al., 2020)

Sentinel-2 estimating AGB

Tested ability of Sentinel imagery (Sentinel-1 (SAR) + Sentinel-2) for the retrieval and predictive mapping of above-ground biomass of mangroves and their replacement land uses (Mangrove Forest, Philippines) Castillo et al., 2017). Developed biomass prediction models through the conventional linear regression and novel Machine Learning algorithms (SAR raw polarisation backscatter, multispectral bands, vegetation indices, canopy biophysical variables). Model based on biophysical variable Leaf Area Index (LAI) derived from Sentinel-2 was more accurate in predicting the overall above-ground biomass (RMSE 27.8–28.5 Mg ha⁻¹). Among the Sentinel-2 multispectral bands, the red and red edge bands (bands 4, 5 and 7), combined with elevation data, were the best variable set combination for biomass prediction. The red edge-based Inverted RedEdge Chlorophyll Index had the highest prediction accuracy among the vegetation indices.

The model was prepared using the entire dataset. The dataset was first subjected to linear regression. This process steps through the variables, removing the one with the smallest standardised coefficient until no improvement was observed in the estimate of the error (AIC), eliminating collinear variables. To assess the model performance, a leave-one-out approach with 90-fold cross-validation was performed to compute the prediction error (RMSE) and correlation coefficient/agreement (r) between the observed and predicted data. In the leave-one-out approach, each sample was excluded one by one while the model is trained with the remaining samples to predict the excluded sample.

All modelling tasks were implemented using IBM SPSS Statistics version 23 (IBM, USA) and the Waikato Environment for Knowledge Analysis (WEKA, version 3.8.0, The University of Waikato, NZ). The WEKA software is a collection of machine learning algorithms (Hall et al., 2009).

To assess if the correlation with biomass and prediction error from the linear models can still be improved, the set of predictors from the linear models with the highest r and lowest RMSE for each part was further subjected to 17 machine learning algorithms available in the WEKA machine learning software. The model/algorithm with highest r and lowest RMSE was selected for use in predictive mapping of biomass which was implemented in ArcGIS (version 10.3.1, ESRI, USA). Four biomass predictive maps were produced which were derived from Sentinel-1 SAR channels, Sentinel-2 bands, Sentinel-2 vegetation index, and Sentinel-2 vegetation biophysical variable Castillo et al., 2017).

LiDAR

LiDAR data is the new standard when it comes to estimating AGB. Common procedure to calculate AGB via vegetation/canopy height and measure accuracy by comparing it to AGB derived from forest plots. Everything $> 2\text{m}$ is typically classified as canopy (Joanathan Kane, 29 April meeting). Identification of individual trees only possible if resolution matches the size of the individual canopy ($< 1\text{m}$, Van Kane, 29 April meeting). LiDAR is useful to estimate vegetation metrics (basal area and stem density with r^2 values of 0.86–0.95 across multiple studies, Zald et al., 2014)

Recent paper with Jonathan and Van Kane (Hudak et al. 2020):

Used a Carbon Monitoring System (CMS) to produce annual estimates of aboveground biomass using Random Forests (RF) for a regional and landscape approach. Field plots (mostly FIA) with self calculated AGB as a response variable to predict AGB from LiDAR derived canopy height and density information ($R^2 = 0.8$, $\text{RMSE} = 115 \text{ Mg ha}^{-1}$, $\text{Bias} = 2 \text{ Mg ha}^{-1}$). A stratified random sample of AGB pixels from landscape-level AGB maps then served as training data for predicting AGB regionally from Landsat image time series variables processed through LandTrendr. Climate metrics calculated from downscaled 30 year climate normals were used as predictors for both models (landscape and regional), as were topographic metrics calculated from elevation data; these environmental predictors allowed AGB estimation over the full range of observations with the regional model ($R^2 = 0.8$, $\text{RMSE} = 152 \text{ Mg ha}^{-1}$, $\text{Bias} = 9 \text{ Mg ha}^{-1}$), including higher AGB values ($> 400 \text{ Mg ha}^{-1}$) where spectral predictors alone saturate.

Combination of LiDAR and other remotely sensed information for biomass estimation

- A) Combination of LiDAR and QuickBird image did not improve AGB estimation in mixed coniferous forests in California; LiDAR data alone provided a better performance (Hyde et al., 2006)
- B) LiDAR and hyperspectral combination has lower accuracy than LiDAR alone in tropical forest Costa Rica (Clark et al., 2011).
- C) LiDAR and Synthetic Aperture Radar (SAR). Provide an overview table for all combinations and output accuracy (Fig. X, Kaasalainen et al., 2015). Upscaling refers to the extrapolation of LiDAR to areas where LiDAR is not available. Generally increases accuracy.

Table 1. Summary of studies of combined use of lidar and synthetic aperture radar (SAR) in biomass estimation. Abbreviations: above-ground biomass (AGB), digital terrain model (DTM), digital surface model (DSM), root mean square error (RMSE), airborne laser scanning (ALS).

Activity	Application	SAR Description	Results	Accuracy	References
Combined lidar/SAR data: joint use of SAR and lidar in biomass models. SAR data combined with lidar DTM/DSM	AGB in tropical forests	L-band polarimetric SAR imagery	100 m resolution AGB map	$\pm 25\%$ uncertainty	[25]
	AGB & canopy height in temperate forests	ALOS PALSAR polarimetry / interferometry (C- & L-band)	Adding SAR variables improves the lidar-based AGB estimation	RMSE is down to 7.1%–11.7%	[69]
	AGB in temperate forests	BioSAR cross-sections (80–120 MHz)	Tree height from lidar data improves the AGB estimation	$R^2 = 0.80$, RMSE = 21.3 t/ha (profiling) and $R^2 = 0.76$, RMSE = 24.2 t/ha (scanning)	[2]
	Forest height prediction with statistical fusion	C-band SRTM InSAR scattering phase center	Stand heights with tree height from LVIS	$R^2 = 0.71$, RMSE = 4.4 m (13% error)	[45]
	Stereo radargrammetry & image pairs in boreal forests	TanDEM-X DSM [70], Terra-SAR-X image pairs in 1m resolution [59]	More accurate large-area AGB using lidar DTM	RMSE = 57 m ³ /ha (plot level) and 25 m ³ /ha (stand level) [70]. RMSE = 41.3 t/ha [59]	[59,70]
Data fusion: limited or no improvement from lidar/radar data fusion.	Forest inventory in the boreal forest zone	TerraSAR-X images	No improvement compared to lidar alone	30% error level resembling manual inventories	[31]
	Stand level AGB + canopy height (US pine forests)	X- and P- band SAR cross-sections	Insignificant improvement compared to lidar alone	RMSE: 33.9 t/ha with lidar to 32.7 t/ha combined [42], 26.0 t/ha to 24.9 t/ha (with lidar canopy height) [71]	[42,71]
	Stand level AGB in Sierra Nevada mixed forest	X-band inter-ferometric phase center & 10 m resolution lidar DEM	Lidar is the best sensor, addition of SAR \rightarrow marginal or no improvement	RMSE = 75.3Mg/ha with lidar alone and with lidar + InSAR, related to field-measured biomass	[72]
	Norway spruce & pine AGB	X-band InSAR	ALS DEM improved the AGB accuracy	RMSE = 24 t/ha (spruce), 17t/ha (pine)	[1]
Upscaling: using lidar and field data as reference	Northern hard-wood forests	L-band polarimetric SAR imagery	20 m resolution extended to large areas	AGB with RMSE down to 203.9 Mg /ha	[6]
	AGB mapping in boreal hard-wood forests	L-band polarimetric SAR imagery & passive optical image combinations	Accurate large-area AGB maps, lidar combined with SAR & optical images	Reduced errors 12%–38% (11–28 Mg/ha) from those where lidar is used with SAR or optical alone	[73]
	AGB mapping in boreal hard-wood forests	C-band polarimetric SAR imagery	Accurate large-area AGB maps with LVIS & SAR	AGB within 10% of the reference (lidar) biomass map (RMSE 31.33 Mg/ha)	[74]
	AGB in tropical forests	X- and L-band SAR backscatter	Accurate large-area AGB maps	$R^2 = 0.53$, RMSE = 79 t/ha	[4]
	Plot-level bio-mass in (sub) tropical man-grove forests	C-band SRTM interferometry (90 m resolution) & ICES at GLAS	Extending lidar-based height/structure data, estimation of biomass loss	SRTM canopy height bias (–1.3 m) and estimation error (RMS = 1.9 m)	[75]

Fig: X: Overview of all combination of LiDAR and radar in research (Kaasalainen et al., 2015)

LiDAR remove noise

- Lastool in QGIS (LASnoise)
- LiDAR360 3.1 software (GreenValley, Beijing, China) to remove the noise points floating between the flight altitude and the mangroves. (Wang et al., 2020). Triangulated irregular network (TIN) densification as a filtering algorithm to deal with complex forest landscapes (Zhao et al., 2016). See IPTD details below.

Improved progressive TIN densification filtering algorithm (IPTD) performs better than other general filtering algorithms (Fig. Y). The strength of 537 the IPTD lies in its ability to retain hilltops and handle break lines and steep slopes. Four parameters are used in the IPTD, i.e., k (neighboring number), r (threshold), 0 (iterative angle), and s (iterative distance). Densifies ground points and accounts for ground surface structure with (upward/downward densification) (Zhao et al., 2016).

Site	Filtering algorithm <i>TE</i> values (%)							
	IPTD	Terrascan	Pingel (2013)	Mongus (2012)	Evans (2007)	Chen (2007)	Vosselman (2000)	Kraus (1998)
1	3.18	2.71	3.48	3.77	4.51	4.03	4.60	4.84
2	1.86	3.78	2.87	3.02	4.57	2.93	2.81	3.70
3	4.08	2.84	18.33	15.68	13.64	9.75	13.61	20.74
4	4.04	2.93	12.35	16.84	11.88	9.55	13.35	20.35
5	1.32	2.59	2.22	2.28	4.13	2.77	2.94	7.60
6	1.76	3.63	2.28	2.34	3.98	2.98	3.14	6.09
7	1.96	4.67	2.21	2.33	2.89	2.23	2.21	2.75
8	2.41	4.14	3.09	3.36	5.81	4.98	9.38	6.00
9	3.00	1.68	4.75	4.84	7.12	9.66	13.68	6.92
10	3.64	6.20	3.58	3.97	4.93	16.3	40.03	4.08
11	2.54	4.39	6.00	6.71	7.60	9.33	22.95	9.52
12	4.47	7.82	7.47	8.27	11.35	18.36	46.56	8.88
13	5.04	9.16	7.66	7.70	9.05	28.75	56.44	8.15
14	4.32	3.14	26.02	34.73	36.46	40.10	42.97	35.37
15	3.57	7.22	1.64	1.71	3.87	4.97	14.55	2.71
ave	3.15	4.46	6.93	7.84	8.79	11.11	19.28	9.85
sd	1.1	2.1	6.73	8.49	8.06	10.48	17.62	8.66

Fig: Y: Comparison of kappa values (total error, TE) for LiDAR filtering algorithms for 15 sites tested. Lowest value in bold (Zhao et al., 2016)

Canopy height estimates from LiDAR (methods)

A) Australian wheat. 90 points/m² by using sensor on farming vehicle coupled with multispectral to identify vegetation. (Walter et al., 2019). Canopy height was extracted through percentile algorithm in R.

- 1) identifying the 98th percentile of maximum returned height in each scan line
- 2) taking the 86th percentile of these values to provide an estimate of overall canopy height

86th percentile was selected through optimization of Pearson's correlation coefficient and RMSE between lidar derived canopy height and measured canopy height for all sample times. More details in supplementary.

B) Honkong forest with thousands of individual tree measurements (dbh, height). (Chan et al., 2021)

LiDAR processed to TIN by extracting only the ground returns. The extraction and processing were performed in ArcMap 10.5 with LAStools extension (<https://rapidlasso.com/lastools/>) and the FUSION 3.7 (<http://forsys.cfr.washington.edu/fusion/fusionlatest.html>). The canopy surface was defined using all non-ground returns with height above 2.0 m. The reason of choosing 2.0 m as the threshold was to avoid canopy returns to be mixed with ground returns. (Jonathan already said we just assume > 2m canopy, Apr 29 meeting).

Canopy Surface - Ground TIN = Normalized height of canopy points -> derive LiDAR metrics

Entire 1 ha study area was divided into circular plots with three plot sizes:

- (1) twenty-five 10m radius plots (16,182 stems)
- (2) one-hundred 5m radius plot (15,538 stems)
- (3) four-hundred 2.5m radius plots (15,100 stems)

Circular plots were considered more favorable than rectangular or square plots, since the periphery-to-area ratio was the smallest and thus minimized the number of edge trees (Köhl et al., 2006).

Relevant plot metrics (LiDAR, climate) were derived by the 'cloudmetrics' function in FUSION version 3.7. The LiDAR metrics, and its log-transformed metrics were input into stepwise regression model as independent predictors of AGB. Significant predictors were selected ($F < 0.5$ were entered and $F > 1.0$ were removed) into the regression model. Tree sets of regression models were generated and the allometric models tended to be linear and normal after logarithmic transformation (old ecology ref available if necessary). Logarithmic transformation increased accuracy. Model predicted three parameters : (1) canopy cover by first returns, (2) 95th Height Percentile and (3) median of absolute deviation from mode (MADmode). Accuracy of predication increased with plot size.

Common LiDAR point metrics

There is a wealth of LiDAR plot metrics derived from the point clouds (Tab. X) and they can even be used to discriminate forest tree species (with and without leaves) (Shi et al., 2018). They are created using height profiles and point distancing (for detailed table with references see Dong et al., 2017) and can be grouped in four categories:

- 1) height (canopy height distributions within the plot) estimator for carbon and AGB (Lim & Treitz, 2004; Patenaude et al., 2004)
- 2) intensity (similar to the height metrics except that they are statistics of the intensity value rather than the height value of the point clouds, only finds application in high resolution LiDAR datasets)
- 3) density (canopy return density)
- 4) canopy volume (portray canopy morphology for canopy cover index or leaf area density)

Table. X: Overview LiDAR derived metrics (taken from Wang et al., 2020)

LiDAR Variable	Formula.Definition
Height	HMax, HMean, HMedian HSD, HVAR HSKE, HKUR HCV HIQ H01, H05, H10, H20, H25, H30, H40, H50, H60, H70, H75, H80, H90, H95, H99
Density	D01, D02, D03, D04, D05...
Canopy volume	CC1.3 CCmean CRR CTHK LADX a, b
	Maximum / Mean / Median heights Standard deviation heights, variance of heights Skewness of heights, Kurtosis of heights Coefficient of variation of height, $(Zstd / Zmean) \times 100 \%$ Interquartile distance of percentile height, H75th – H25th Height percentiles. Point clouds are sorted according to the elevation. HX is the Xth percentile of height. There are 15 height percentiles metrics from 1% to 99% height. Canopy return density. Point clouds are divided into slices with the same interval from low to high elevations. DX is the number of canopy return points in the Xth slice compared to the total points. Canopy cover above 1.3 m, $n_veg1.3 / n_total$ Canopy cover above mean height, $n_vegmean / n_total$ Canopy relief ratio $(Hmean - Hmin) / (Hmax - Hmin)$ Canopy thickness, H90th-H10th. (new in Wang et al. 2020) Leaf area density. Point clouds are divided into slices with the same interval from low to high elevations. LADX is the valid leaf area density in the Xth slice (Kamoske et al., 2019) The scale parameter a (shape of vertical distribution) and shape parameter b (increase/decrease of distribution breadth) of the Weibull density distribution fitted to the foliage profile (Liu et al., 2018)

Upscaling LiDAR with Sentinel-2

LiDAR upscaling by integrating field plots (point), UAV-LiDAR strip (line) data and Sentinel-2 imagery (polygon) based on a point-line-polygon framework for AGB estimation (Wang et al., 2020).

Field data

Application of LiDAR for forest inventory requires field plot data to ground-truth the information. Field plots need to incorporate relevant parameters (volume, basal area, biomass) (Hudak et al., 2020). FIA plot data provide an unbiased, systematic sample of forest conditions in space and time and are more applicable over larger areas and for successive effects such as climate change and forest regeneration rates (Tinkham et al., 2018).

Shana sampling plots

Sampling plot data from the Forest Inventory and Analysis National Program (FIA).

- Allometric: DBH, size classes (e.g. saplings) > height groups, largest tree measured, height to live crown, crown ratio, crown width, age data sparse and based on 1-2 cores
- Biomass derived from LiDAR datasets
- plot center GPS using Javad
- plot date and size
- Ancillary data: Slope, ground cover, vegetation cover by type (e.g. shrub, forb, etc), modal vegetation height by different types of vegetation, fuel models, fuels data, seedlings, site history (e.g. plantation, if there was a fire, etc)

Sampling techniques used: <https://www.fia.fs.fed.us/program-features/index.php>

Forest plots are triangle with 4 circular subplots (Fig. 2), just assume they are representative of 1 ha of forest (Van Kane, 29 April meeting). Spatial mismatch between the 7.3 m radius, round configuration of an FIA subplot and 30 m \times 30 m square Landsat pixels (Tinkham et al 2018). Inevitably, the four subplots will intersect a different number of pixels and in varying proportions.

Criteria to match LiDAR with FIA plots (Hudak et al., 2020):

- fixed-area plots
- georeferenced with a GNSS capable of differential correction
- established within ± 3 years of an overlapping LiDAR collection
- not disturbed in the time between field and LiDAR data collections

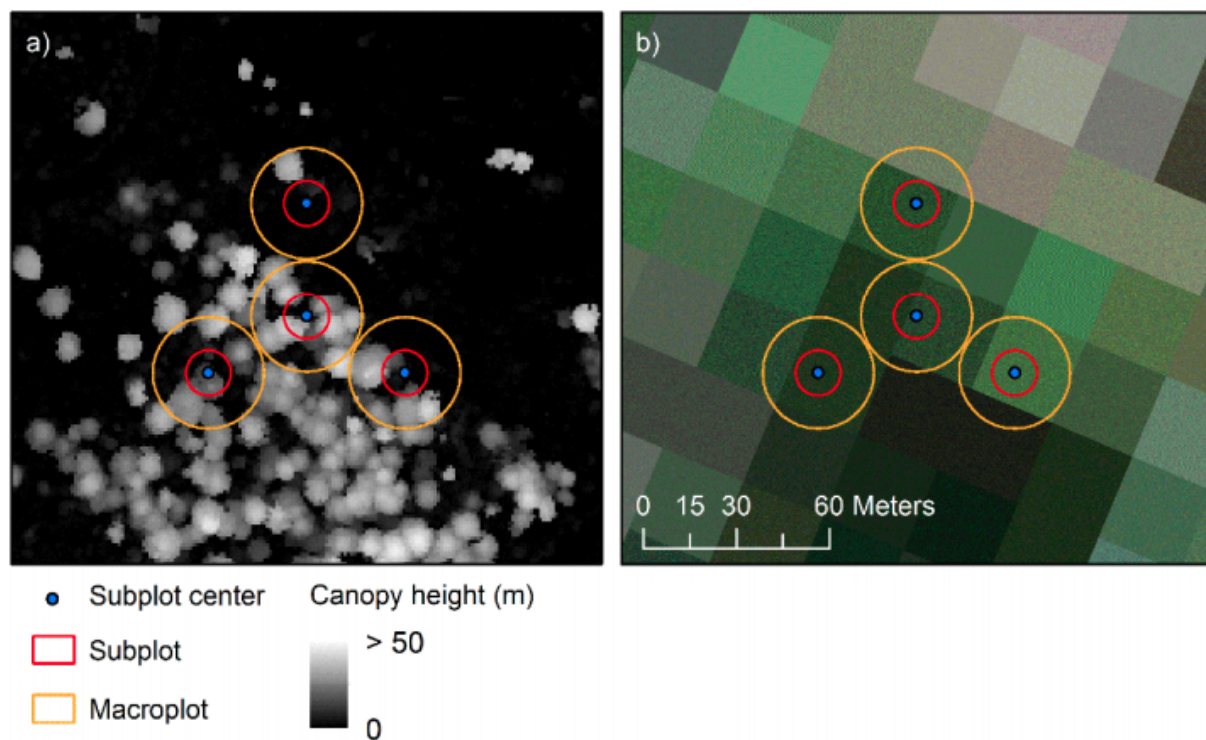


Figure 2: FIA sampling plot layout. a) generated canopy height model from LiDAR and b) landsat 30m imagery overlay (taken from Hudak et al., 2020)

Biomass estimation in the field

Collection of a large number of biomass reference data at the plot level is time-consuming and labor-intensive. It is only suitable for a small area and cannot provide the spatial distribution. However, this kind of data is a

prerequisite for developing biomass estimation models (Lu et al., 2016). Allometric models most common, but require data about soil, land use history and climate influence (paper here for tropical) (Clark & Kellner, 2012).

Two methods:

- 1) Use data of national forest inventories. Calculate with volume expansion factor (VEF), average wood density (WD), biomass expansion factor (BEF) (Brown et al., 1989; Lehtonen et al., 2004; Wang et al., 2011):

$$\text{ABG (kg/ha)} = \text{volume (m}^3 \text{ / ha)} * \text{VEF} * \text{WD} * \text{BEF} + e$$

- 2) Calculate AGB from field plots using equations from Fire and Fuels Extension (FFE) of the Forest Vegetation Simulator (FVS) (Rebain 2015, Dixon 2018). These equations are based on a series of regional volume and biomass equations. The aboveground portion of the live and standing dead trees were summed to a single, plot-level AGB value; the belowground portion of the trees and non-tree species were excluded from the AGB estimates. These plot-level AGB estimates were the response variable for a landscape model (Hudak et al., 2020).

Problems with field data

Taken from Lu et al., 2016:

- (1) tree variables, including sampling, measurement, recording and grouping errors when tree variables such as DBH and height are measured;
- (2) conversion coefficients and models including variation of conversion factors from volume to biomass and then to carbon, inappropriate selection and usage of allometric models for relationship of tree volume and DBH and height, and incorrect regression models relating forest biomass/carbon to spectral variables;
- (3) uncertainties of spectral values due to unbalanced platforms, scanner motions, poor atmospheric conditions, and slope; inappropriate spatial interpolation methods for geometrical and radiometric corrections, and incorrect methods for image enhancement and analysis;
- (4) sample plot locations, including global positioning system (GPS) coordinates used to locate the sample plots, geometric correction and the uncertainties due to mismatch of sample plots with spatial resolutions of remotely sensed data;
- (5) differences in sizes of sample plots and image pixels, disagreement between remotely sensed data and plot observations when portions of trees on boundaries are outside plots although both sample plots and pixels have the same spatial resolutions; and
- (6) temporal differences between field plot measurements and remotely sensed data.

Depending on the protocol and the quality of the Global Navigation Satellite System (GNSS) receiver used in the field; the three peripheral subplots, while systematically laid out from the center subplot by consistent distances (36.6 m) and bearings (120°, 240°, 360°) are usually not georeferenced, making them more subject to locational inaccuracy due to additive errors in accounting for horizontal distance on slopes and for magnetic declination on compass azimuths (Zald et al., 2014).

Forest classification

Van Kane (meeting Apr 29): forest service cannot reveal plot locations, only if project output is open access (ideally uni projects) Idea: Use Gradient nearest neighbours (GNN) so nearest plot imputes tree list

Other relevant datasets

Landsat

Table. 3: Landsat 8-9 Operational Land Imager (OLI) and Thermal Infrared Sensor (TIRS) (USGS, 2018)

Bands	Wavelength..um.	Resolution..m.
Band 1- Coastal aerosol	0.43-0.45	30
Band 2- Blue	0.45-0.51	30
Band 3- Green	0.53-0.59	30
Band 4- Red	0.64-0.67	30
Band 5- Near Infrared (NIR)	0.85-0.88	30
Band 6- SWIR 1	1.57-1.65	30
Band 7- SWIR 2	2.11-2.29	30
Band 8- Panchromatic	0.50-0.68	15
Band 9- Cirrus	1.36-1.38	30
Band 10- Thermal Infrared (TIRS) 1	10.6-11.19	100
Band 11- Thermal Infrared (TIRS) 2	11.50-12.51	100

LandTrendr is set of spectral-temporal segmentation algorithms that are useful for change detection in a time series of moderate resolution satellite imagery (primarily Landsat) and for generating trajectory-based spectral time series data largely absent of inter-annual signal noise. Can be used to assess forest regeneration over larger timescales (Fig. 3). They provide a github repository evaluating how to extract the data from e.g. Google Earth (<https://emapr.github.io/LT-GEE/landtrendr.html>).

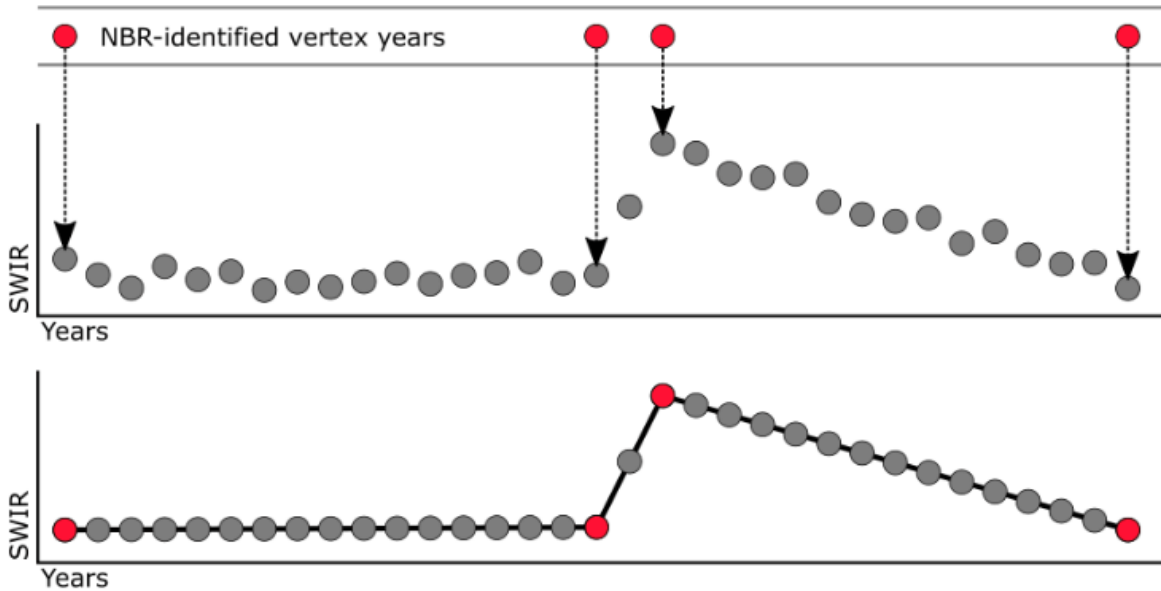


Fig 2.4. Impose the segmentation structure of one spectral representation on another. Here we have identified four breakpoints or vertices for a pixel time series using NBR, and then used the year of those vertices to segment and interpolate the values of a SWIR band time series for the same pixel.

Figure 3: Pixel change over updated intervals for the Normalised Burn Ratio (NBR)

Papers:

Jonathan Kane paper (Kolden et al., 2012). Characterized unburned area within fire perimeters by fire size and severity, characterized distance to an unburned area across the burned portion of the fire, and investigated patch dynamics of unburned patches within the fire perimeter. From 1984 through 2009, the total area within the fire perimeters that was classified as unburned from dNBR was 37% for Yosemite, 17% for Glacier, and 14% for Yukon-Charley.

The complex biophysical environments and vegetation characteristics, e.g. phenology, species composition, growth phase, and health – will affect vegetation spectral signatures; thus, biomass estimation models based on optical spectral features cannot be directly transferred to different study areas for biomass mapping (Foody et al., 2003; Lu, 2005)

Combination of Landsat and land cover to estimate AGB in Uganda (Avitabile et al., 2012). A regression tree-based model (Random Forest) produces good results (cross-validated R^2 0.81, RMSE 13 T/ha) when trained with a sufficient number of field plots representative of the vegetation variability at national scale. Specific limitations are mainly related to saturation of the optical signal at high biomass density and cloud cover, which hinders the compilation of a radiometrically consistent multi-temporal dataset. Land cover data increases the model performance because it provides information on vegetation phenology .

Synthetic aperture radar (SAR)

Most radar-based biomass estimation studies use L-band SAR data, especially the ALOS PALSAR L-band data (Mitchard et al. 2011; Carreiras et al. 2012; Rahman and Sumantyo 2013). The SAR C-band data have not been extensively used because of the C-band's inability to capture forest biomass features (Le Toan et al. 1992; Lu 2006).

In summary, it is difficult to use radar data for distinguishing vegetation types (Li et al. 2012b) because radar data reflect the roughness of land cover surfaces instead of the difference between the vegetation types, thus resulting in difficulty of biomass estimation. The speckle in radar data is another problem affecting its applications. Properly employing filtering methods to reduce noise and outliers in InSAR data is needed to improve the vegetation height estimation performance (Kellndorfer et al. 2004).

NASA-GEDI LiDAR

GEDI has the highest resolution and densest sampling of any LiDAR ever put in orbit (25 m to 1 km resolution)

Website: <https://gedi.umd.edu/>

RapidEye

ESA is offering access to the full RapidEye archive for scientific research and application development. Access is only available to submitted proposals that are accepted. 5 m pixel size (RGB, RE and NIR). **Overall, RapidEye data are not suitable for AGB estimation**, but when AGB falls within 50–150 Mg/ha, support vector regression based on stratification of vegetation types provided good AGB estimation; Problem for biomass estimates can be fixed incorporating tree height if LiDAR data or stereo image is available (Brazilian Rainforest) (Feng et al., 2017)

ICESat-2

Ice, Cloud and Land Evaluation Satellite, 91-day repeat

While ATLAS onboard ICESat-2 was primarily designed to determine changes in ice sheet elevation and mass, it will provide information about vegetation that may be used to estimate AGB. ATLAS is a photon counting system, operating in the visible wavelengths, at 532 nm [7]. It generates three pairs of tracks, with each pair approximately 3.3 km apart and each track within a pair separated by 90 m [11]. LiDAR footprints are produced every 70 cm in the along-track direction and measure approximately 14 m in diameter [14]. Given the unprecedented coverage and spatial detail from ICESat-2, translating ICESat-2 measurements to AGB estimates would allow for large-scale AGB and forest carbon assessments.

Paper: ICESat-2 for mapping forest biomass with deep learning (Narine et al., 2019). A first set of models were developed using vegetation indices calculated from single-date Landsat imagery, canopy cover, and land cover, and a second set of models were generated using metrics from one year of Landsat imagery with canopy cover and land cover maps. With the extended dataset containing metrics calculated from Landsat images acquired on different dates, substantial improvements in model performance for all data scenarios were noted. The R² values increased to 0.64, 0.66, and 0.67. Comparisons with Random forest (RF) prediction models highlighted similar results, with the same R² and root mean square error (RMSE) range (15–16 Mg/ha) for daytime and nighttime scenarios. ICESat-2 profiles, especially with the nighttime scenario (R² = 0.66), highlight the potential for generating a wall-to-wall AGB product with ICESat-2 by adopting a synergistic approach with Landsat optical imagery, canopy cover, and land cover

Climate data

Paper: For climate, data were used from the North American Regional Reanalysis (NARR) (Mesinger et al 2006), the National Center for Environmental Prediction's high-resolution combined model and assimilated dataset available eight-times daily 1979-2000 at 32 km resolution. Ecosystem demography model trained with hourly land surface weather data to calculate carbon assimilation rate and transpiration (2 m air temperature, dew point, downward solar radiation, precipitation, soil temperature)(Hurt et al., 2019).

(Hongkong Forest) (Chan et al., 2021): Three parameters to account for climatic variations: Temperature seasonality (TS), Long-term Maximum Climatological Water Deficit (CWD) and Precipitation Seasonality (PS) (Hongkong Forest)

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