



Universidad Rey Juan Carlos

## Proyecto Tesis Doctoral

### RELACIÓN ENTRE EL ESPECTRO DE SEÑALES CARDIACAS Y LA DINÁMICA ESPACIO TEMPORAL DE LAS FUENTES CARDIACAS

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# Resumen

inicio del resumen



# Abstract

In this Doctoral Dissertation . . . . .



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# Acrónimos y abreviaturas

A lo largo de este documento se mantendrán en su forma original aquellos acrónimos derivados de una expresión inglesa cuyo uso se encuentre extendido en la literatura científica.

De acuerdo con las recomendaciones de la Real Academia Española, en esta Tesis los acrónimos y siglas no se modifican para formar el plural.

**DF** Frecuencia Dominante.



# Capítulo 1

## Introducción

**RESUMEN:** La presente Proyecto Tesis Doctoral tiene como pilares el estudio de mecanimos de arritmias cardiacas mediante procesados digital de señales ..... en la Frecuencia Dominante (DF)

### 1.1. Motivación

### 1.2. Objetivos

### 1.3. Metodología

### 1.4. Estructura





Parte I

Nombre parte



# Capítulo 2

## Modelos Cardiacos

2.1. introducción

2.2. conclusiones



## Capítulo 3

### Resolución espacial del sistemas de electrodos

3.1. introducción

3.2. modelos de sistemas de electrodos

3.3. Volumen equivalente de sistema de electrodos

3.4. conclusiones



## Parte II

Nombre parte





# Capítulo 4

## Análisis espectral

- 4.1. introducción
- 4.2. Función de tiempos
- 4.3. Mapas de correlación
- 4.4. Relación ancho de banda
- 4.5. Mapas de frecuencia dominante
- 4.6. conclusiones

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