

Universidad Rey Juan Carlos

#### Proyecto Tesis Doctoral

# RELACIÓN ENTRE EL ESPECTRO DE SEÑALES CARDIACAS Y LA DINÁMICA ESPACIO TEMPORAL DE LAS FUENTES CARDIACAS

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Fuenlabrada, junio de 2013

#### Resumen

inicio del resumen

#### Abstract

In this Doctoral Dissertation .....

## Índice general

Re	esumen	I
Αl	$\operatorname{bstract}$	III
1.	Introducción	1
	1.1. Motivación	1
	1.2. Objetivos	1
	1.3. Metodología	1
	1.4. Estructura	1
Ι	Nombre parte	3
2.	Modelos Cardiacos	5
	2.1. introducción	5
	2.2. concluciones	5
II	Nombre parte	7
3.	Resolución espacial del sistemas de electrodos	9
	3.1. introducción	9
	3.2. modelos de sistemas de electrodos	9
	3.3. Volumen equivalente de sistema de electrodos	9
	3.4. concluciones	9
Bi	ibliografía	26

## Índice de figuras

### Índice de tablas

#### Capítulo 1

#### Introducción

**RESUMEN:** La presente Proyecto Tesis Doctoral tiene como pilares el estudio de mecanimos de arritmias cardiacas mediante procesados digital de señales ..........

- 1.1. Motivación
- 1.2. Objetivos
- 1.3. Metodología
- 1.4. Estructura

# Parte I Nombre parte

### Capítulo 2

#### Modelos Cardiacos

- 2.1. introducción
- 2.2. concluciones

# Parte II Nombre parte

#### Capítulo 3

# Resolución espacial del sistemas de electrodos

- 3.1. introducción
- 3.2. modelos de sistemas de electrodos
- 3.3. Volumen equivalente de sistema de electrodos
- 3.4. concluciones

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