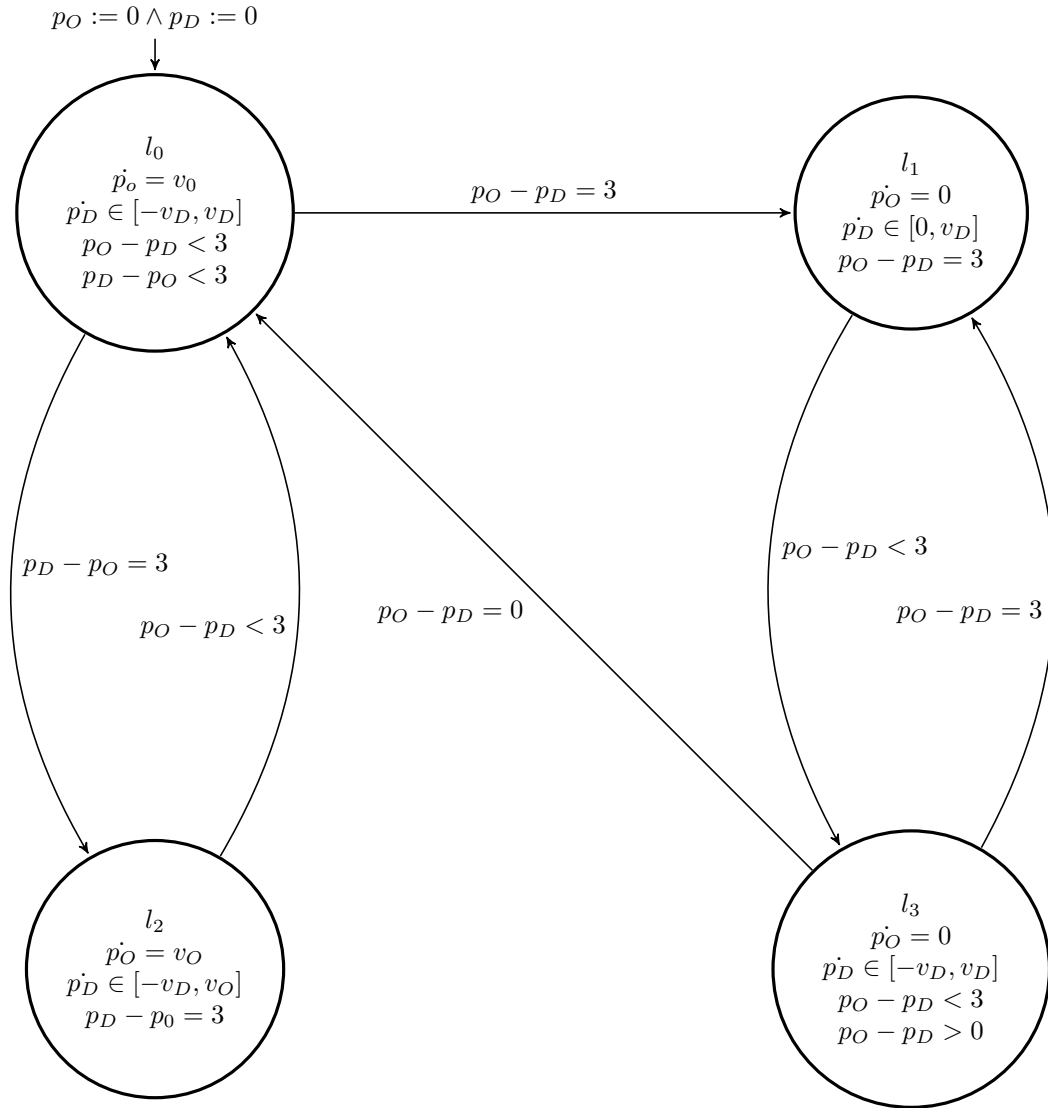


## Aufgabe 1



---

## Aufgabe 2

$$\begin{aligned} R_1 &= T_L^+(R_0) = (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \wedge x = x_{pre} \wedge x_{pre} \in R_0 \wedge y = y_{pre} + t \wedge y_{pre} \in R_0 \wedge x + y \leq 4) \\ &= (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \wedge x = x_{pre} \wedge y = y_{pre} + t \wedge x + y \leq 4 \wedge x_{pre} = y_{pre} = 0) \\ &= (l_0, \exists t. t \geq 0 \wedge x = 0 \wedge y = t \wedge x + y \leq 4) \\ &= (l_0, \exists t. t \geq 0 \wedge x = 0 \wedge y = t \wedge y \leq 4) \\ &= (l_0, x = 0 \wedge y \geq 0 \wedge y \leq 4) \end{aligned}$$

$$\begin{aligned} R_2 &= D_L^+(R_1) = (l_1, \exists x_{pre}. \exists y_{pre}. x_{pre} \in R_1 \wedge y_{pre} \in R_1 \wedge x \leq 3 \wedge x = x_{pre} \wedge y = y_{pre}) \\ &= (l_1, \exists x_{pre}. \exists y_{pre}. \wedge x = x_{pre} \wedge y = y_{pre} \wedge x \leq 3 \wedge y_{pre} \geq 0 \wedge y_{pre} \leq 4 \wedge x_{pre} = 0) \\ &= (l_1, x = 0 \wedge y \leq 4 \wedge y \geq 0) \end{aligned}$$

$$\begin{aligned} R_3 &= T_L^+(R_2) = (l_1, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \wedge x_{pre} \in R_2 \wedge y_{pre} \in R_2 \wedge x = x_{pre} + t \wedge y = y_{pre} + t \wedge x \leq 3) \\ &= (l_1, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \wedge x_{pre} = 0 \wedge y_{pre} \leq 4 \wedge y_{pre} \geq 0 \wedge x = x_{pre} + t \wedge y = y_{pre} + t \wedge x \leq 3) \\ &= (l_1, \exists t. t \geq 0 \wedge x = t \wedge y \leq 4 + t \wedge x \leq 3) \end{aligned}$$

$$\begin{aligned} R_4 &= D_L^+(R_3) = (l_0, \exists x_{pre}. \exists y_{pre}. x_{pre} \in R_3 \wedge y_{pre} \in R_3 \wedge x = 0 \wedge y = 0 \wedge x + y \leq 4) \\ &= (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \wedge x_{pre} = t \wedge y_{pre} \leq 4 + t \wedge x_{pre} \leq 3 \wedge x = 0 \wedge y = 0 \wedge x + y \leq 4) \\ &= (l_0, \exists t. t \geq 0 \wedge x = 0 \wedge y = 0) \\ &= (l_0, x = 0 \wedge y = 0) \end{aligned}$$

$$P_2 = \{R_4\} = \{(l_0, x = 0 \wedge y = 0)\}$$