Westfälische Wilhelms-Universität Münster

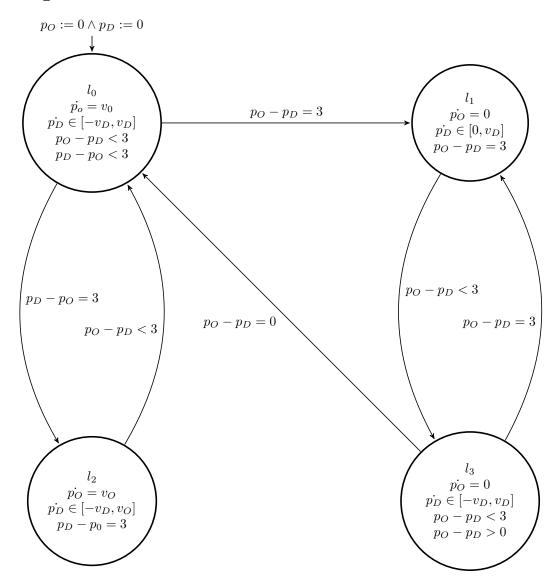
Übung Modellierung und Analyse von Dynamischen Systemen, WiSe 17/18

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Blatt 5

Aufgabe 1



Aufgabe 2

$$\begin{split} R_1 = & T_L^+(R_0) = (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \land x = x_{pre} \land x_{pre} \in R_0 \land y = y_{pre} + t \land y_{pre} \in R_0 \land x + y \leq 4) \\ = & (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \land x = x_{pre} \land y = y_{pre} + t \land x + y \leq 4 \land x_{pre} = y_{pre} = 0) \\ = & (l_0, \exists t. t \geq 0 \land x = 0 \land y = t \land x + y \leq 4) \\ = & (l_0, \exists t. t \geq 0 \land x = 0 \land y = t \land y \leq 4) \\ = & (l_0, x = 0 \land y \geq 0 \land y \leq 4) \end{split}$$

$$R_2 = D_L^+(R_1) = (l_1, \exists x_{pre}. \exists y_{pre}. x_{pre} \in R_1 \land y_{pre} \in R_1 \land x \leq 3 \land x = x_{pre} \land y = y_{pre})$$

$$R_2 = D_L^+(R_1) = (l_1, \exists x_{pre}. \exists y_{pre}. x_{pre} \in R_1 \land y_{pre} \in R_1 \land x \le 3 \land x = x_{pre} \land y = y_{pre})$$

$$= (l_1, \exists x_{pre}. \exists y_{pre}. \land x = x_{pre} \land y = y_{pre} \land x \le 3 \land y_{pre} \ge 0 \land y_{pre} \le 4 \land x_{pre} = 0)$$

$$= (l_1, x = 0 \land y \le 4 \land y \ge 0)$$

$$R_3 = T_L^+(R_2) = (l_1, \exists t. \exists x_{pre}. \exists y_{pre}. t \ge 0 \land x_{pre} \in R_2 \land y_{pre} \in R_2 \land x = x_{pre} + t \land y = y_{pre} + t \land x \le 3)$$

$$= (l_1, \exists t. \exists x_{pre}. \exists y_{pre}. t \ge 0 \land x_{pre} = 0 \land y_{pre} \le 4 \land y_{pre} \ge 0 \land x = x_{pre} + t \land y = y_{pre} + t \land x \le 3)$$

$$= (l_1, \exists t. t \ge 0 \land x = t \land y \le 4 + t \land x \le 3)$$

$$\begin{split} R_4 = & D_L^+(R_3) = (l_0, \exists x_{pre}. \exists y_{pre}. x_{pre} \in R_3 \land y_{pre} \in R_3 \land x = 0 \land y = 0 \land x + y \leq 4) \\ = & (l_0, \exists t. \exists x_{pre}. \exists y_{pre}. t \geq 0 \land x_{pre} = t \land y_{pre} \leq 4 + t \land x_{pre} \leq 3 \land x = 0 \land y = 0 \land x + y \leq 4) \\ = & (l_0, \exists t. t \geq 0 \land x = 0 \land y = 0) \\ = & (l_0, x = 0 \land y = 0) \end{split}$$

$$P_2 = \{R_4\} = \{(l_0, x = 0 \land y = 0)\}$$