# Title of Report

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2021-11-02

## Preface

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## Chapter 1.

#### Introduction

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . If you read this text, you will get no information  $E = mc^2$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ . This text should contain all letters of the alphabet and it should be written in of the original language.  $\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$ . There is no need for special content, but the length of words should match the language.  $a\sqrt[n]{b} = \sqrt[n]{a^n}b$ .

This is a citation [1]. Hello, here is some text without a meaning.  $d\Omega = \sin \vartheta d\vartheta d\varphi$ . This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . This text should contain all letters of the alphabet and it should be written in of the original language  $E = mc^2$ . There is no need for special content, but the length of words should match the language.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ .

See Table 1.1 for a floating table and (1.1) for an equation.

$$y = ax + b = cz + d \tag{1.1}$$

**Table 1.1.:** This is a floating table

## Chapter 2.

#### Forward Kinematics

#### 2.1. Task 1

Denavit-Hartenberg (DH) is a convention broadly used in robotics. It was introduced in order to standardize the attachment of cordinate frames to robots. A robot can be seen as a kinematic chain of rigid bodies. These rigid bodies are called links and are connected with joints. A robot arm is represented by a kinematic chain which is a concatenation of several links and joints. If one object is manipulated by one robot the system is called open kinematic chain. If several robots manipulate one object simultanously the system is called closed kinematic chain. In this task we will focus on open chain robots. Forward kinematics is a way of of calculating the end effector pose based on the joint parameters. The relation from the end effector to the base is done by attaching one frame to the end effector and one to the base of the robot. The relation between those two frames is then determined by the homogenious transformation matrix  $T_E^B$ . To make things easier a frame can be attached to each link and then the relation between each consecutive frame can be calculated by  $T_{i+1}^i$ . Concatenating all these homogenious Transformations and building their dot product determines the homogenious Transformation from the robot base to end effector:

$$T_E^B = T_0^1 * T_1^2 * \dots * T_{i-1}^i \tag{2.1}$$

Denavit-Hartenberg (DH) is a convention which standardizes the attachment of cordinate frames to a robot. It is a convention broadly used in the community which makes the application of the recursive formula in 2.1 more intuitive. The DH convention provides rules how to attach the frames to the link. In general the result should be the same if the frames are attached differently to the links as long as every link is considered. In the DH convention four different parameters afe used in order to attach frames to the robot links. The frame of the link i+1 is determined based on the frame of the link i. The placement of a frame is visulaized in 2.2. The followinfg consecutive rules are applied:

- 1  $z_i$  alligns with the rotational axis of joint i+1
- 2  $O_i$  is placed at the intersetion of  $z_i$  and the common normal of  $z_{i-1}$  and  $z_i$
- 3  $O_{i'}$  is placed at the intersetion of  $z_{i-1}$  and the common normal of  $z_{i-1}$  and  $z_i$
- 4  $x_i$  alligns with the common normal of  $z_{i-1}$  and  $z_i$  pointing away from  $O_i$

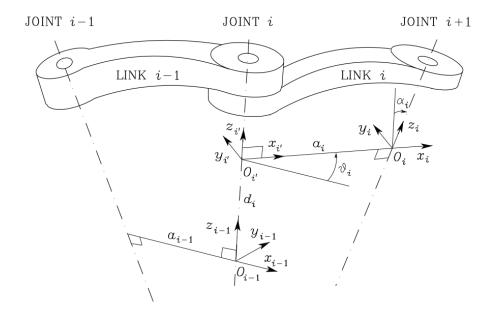


Figure 2.1.: Denavit Hartenberg convention rules [2]

5  $y_i$  is chosen according to the right hand rule for coordinate frames

The DH convention does not define enough rules to make sure that there is just one uniquie solution.

- 1 There is no frame i-1 for frame 0 we can not define  $O_0$  and  $x_0$ :  $O_0$  and  $x_0$  can be defined arbitrarily.
- 2 There is no joint i+1 when defining frame n we can not define  $z_n$ :  $z_n$  is defined parallel to  $z_{n-1}$  .

Usually there are some ways of defining those two parameters which make applying the convention easier.

There are some special cases which also do not allow a unique definition of frames:

- 1  $z_{i+1}$  and  $z_i$  are parallel:  $O_i$  and  $x_i$  can be selected arbitrarily.
- 2  $z_{i+1}$  and  $z_i$  intersect:  $O_i$  and  $x_i$  can be selected arbitrarily.
- 3 joint i is prismatic:  $x_{i-1}$  can be selected arbitrarily.

The DH convention makes finding the homogeneous transformations especially convenient. After establishing the frames at each joint the four DH parameters can be identified.

 $a_i$ : distance between  $O_i$  and  $O_{i'}$ 

 $d_i$ : distance between  $O_{i'}$  and  $O_{i-1}$  along  $z_{i-1}$ 

 $\alpha_i$ : angle between  $z_{i-1}$  and  $z_i$  about  $x_i$ 

 $\vartheta i$ : angle between  $x_{i-1}$  and  $x_i$  about  $z_{i-1}$ 

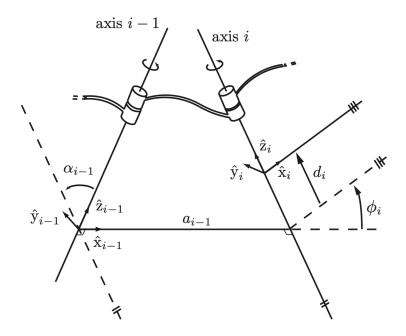


Figure 2.2.: Modified Denavit Hartenberg convention rules [3]

The parameters  $a_i$  and  $\alpha_i$  are constant and just depend on the geometry of the link i. Non constant is the parameter  $d_i$  if joint i is prismatic and the parameter  $\vartheta i$  if joint i is rotational.

Having the four parameters  $a_i$ ,  $d_i$ ,  $\alpha_i$ ,  $\vartheta_i$  one can write down the homogeneous transformations T immediatelly:

$$T_i^{i-1} = \begin{bmatrix} c_{\vartheta_i} & -s_{\vartheta_i} c_{\alpha_i} & s_{\vartheta_i} s_{\alpha i} & a_i c_{\vartheta_i} \\ s_{\vartheta_i} & c_{\vartheta_i} c_{\alpha i} & -c_{\vartheta_i} s_{\alpha i} & a_i s_{\vartheta_i} \\ 0 & s_{\alpha i} & c_{\alpha i} & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 (2.2)

[2]

#### 2.2. Task 2

The modified DH convention presented in [3] differs to the original DH presented in [2]. The frames are attached to the links differntly (see table 2.1). Getting the DH parameters from the attached frames therefore also differs (see table 2.2). Like mentioned before the attachment of the frames does not change the forward dynamics. Anyway, sticking with one convention makes calculatations more intuitive and easier to understand for others.

In the following passage the differences in the frame attachement are presented.

frame	original DH	modified DH
parameters		
$\overline{z_i}$	alligns with the rotational axis	alligns with the rotational axis
	of joint i+1	of joint i
$O_i$	is placed at the intersetion of $z_i$	is placed at the intersetion of $z_i$
	and the common normal of $z_{i-1}$ and $z_i$	and the common normal of $z_i$ and $z_{i+1}$
$x_i$	alligns with the common normal of	alligns with the common normal of
	$z_{i-1}$ and $z_i$ pointing away from $O_i$	$z_{i+1}$ and $z_i$ and pointing away from $O_i$

 ${\bf Table~2.1.:~frame~attachment~original~versus~modified~DH}$ 

DH	original DH	modified DH
paramters		
$\overline{a_i}$	length of common normal of $z_{i-1}$ and $z_i$	length of common normal of $z_i$ and $z_{i+1}$
$d_i$	distance between $O_{i-1}$ and intersection of	distance between $O_i$ and intersection of
	common normal of $z_{i-1}$ and $z_i$ with $z_{i-1}$	common normal of $z_{i-1}$ and $z_i$ with $z_i$
$lpha_i$	angle between $z_{i-1}$ and $z_i$ about $x_i$	angle between $z_{i-1}$ and $z_i$ about $x_{i-1}$
$\vartheta i$	angle between $x_{i-1}$ and $x_i$ about $z_{i-1}$	angle between $x_{i-1}$ and $x_i$ about $z_i$

Table 2.2.: DH parameter original versus modified DH  $\,$ 

## Chapter 3.

## Here Comes Chapter 2

Hello, here is some text without a meaning.  $\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$ . This text should show what a printed text will look like at this place.  $a\sqrt[n]{b} = \sqrt[n]{a^n}b$ . If you read this text, you will get no information.  $d\Omega = \sin\vartheta d\vartheta d\varphi$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ .

This is the second paragraph. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . If you read this text, you will get no information  $E = mc^2$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ . This text should contain all letters of the alphabet and it should be written in of the original language.  $\sqrt[n]{a} = \sqrt[n]{a}$ . There is no need for special content, but the length of words should match the language.  $a\sqrt[n]{b} = \sqrt[n]{a^n b}$ .

And after the second paragraph follows the third paragraph. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . If you read this text, you will get no information  $E = mc^2$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ . This text should contain all letters of the alphabet and it should be written in of the original language.  $\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$ . There is no need for special content, but the length of words should match the language.  $a\sqrt[n]{b} = \sqrt[n]{a^nb}$ .

After this fourth paragraph, we start a new paragraph sequence. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . If you read this text, you will get no information  $E = mc^2$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you



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Figure 3.1.: NTNU logo

information about the selected font, how the letters are written and an impression of the look.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ . This text should contain all letters of the alphabet and it should be written in of the original language.  $\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$ . There is no need for special content, but the length of words should match the language.  $a\sqrt[n]{b} = \sqrt[n]{a^nb}$ .

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#### 3.1. Title of section 2

## Chapter 4.

## Here Comes Chapter 3

This is the second paragraph. Hello, here is some text without a meaning. This text should show what a printed text will look like at this place.  $\sin^2(\alpha) + \cos^2(\beta) = 1$ . If you read this text, you will get no information  $E = mc^2$ . Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look.  $\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$ . This text should contain all letters of the alphabet and it should be written in of the original language.  $\sqrt[n]{a} = \sqrt[n]{a}$ . There is no need for special content, but the length of words should match the language.  $a\sqrt[n]{b} = \sqrt[n]{a^nb}$ .

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Figure 4.1.: NTNU logo

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#### Chapter 5.

#### Conclusion

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- [1] J. M. McCarthy and G. S. Soh, Geometric design of linkages. SpringerVerlag, 2011, ISBN: 978-1-4614-2767-4.
- [2] B. Siciliano, *Robotics: Modelling, Planning and Control.* Springer London, 2009, ISBN: 978-1-84628-642-1.
- [3] F. C. P. Kevin M. Lynch, *Modern Robotics: Mechanics, Planning, and Control.* Cambridge University Press, 2017, ISBN: 978-1-107-15630-2.

# Appendix A.

# Name of Appendix

A.1. This is a section